

# *Recent Results on Flavour Physics*

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## - *Outline* ---

- ✓ What is Flavour Physics?:
  - ⇒ CKM, Higgs → Flavour Physics
- ✓ What do we understand about New Physics so far?
  - ⇒ *Results from Babar, Belle, Tevatron & LHC*
- ✓ Future perspectives for New Physics via the Flavour Window
  - ⇒  $\Delta F=2$  processes:  $\epsilon_K, \Delta M_s \rightarrow 3\sigma$  **tension  $\sin\beta$  vs  $\epsilon_K$**
  - ⇒  $\Delta F=1$  processes:  $b \rightarrow s$  modes from LHCb →  **$4\sigma$  tension  $B \rightarrow K^{(*)}\mu\mu, ee$**

# Introduction: What is Flavour Physics?

- Flavour Transitions:

- W interactions violate Flavour and CP: *complex 3x3 matrix (CKM)*

$$\mathcal{L}_{int} = \bar{t}_L \gamma_\mu V^{CKM} b_L W^\mu$$

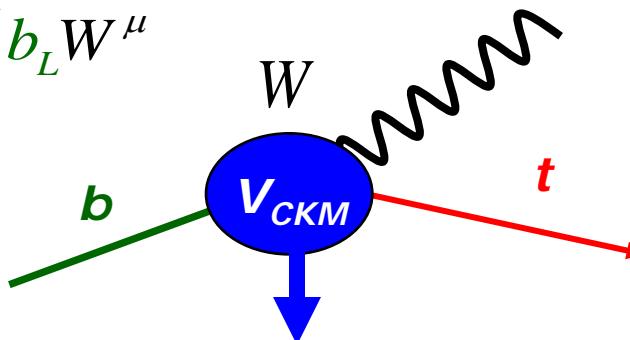
...

1937

$\beta$  decay:  $n \rightarrow p e^- \nu$

1964

$K \leftrightarrow \bar{K}$  mixing



$$V^{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ D \rightarrow \pi l\nu & D \rightarrow K l\nu & B \rightarrow D^{(*)} l\nu \\ D \rightarrow l\nu & D_s \rightarrow l\nu & \\ V_{td} & V_{ts} & V_{tb} \\ \langle B_d | \bar{B}_d \rangle & \langle B_s | \bar{B}_s \rangle & \end{pmatrix}$$

(unitarity)

→ 3 angles and 1 Phase

- Z interactions conserve Flavour and CP.

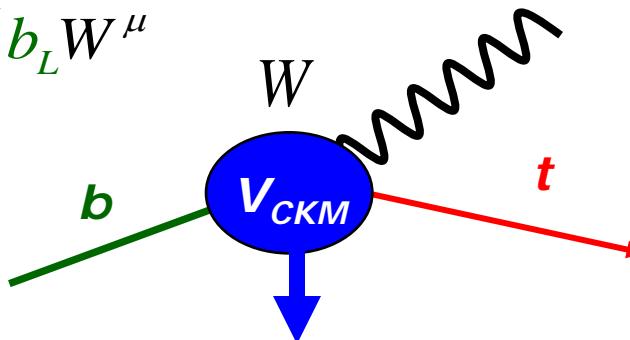
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...



But this is only macroscopic picture  
(phenomenological couplings at low scales)

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...

**Microscopic picture  $\leftrightarrow$  Higgs mediator**

1973

$$\mathcal{L}_{int} = \mathcal{L}_{gauge}(A_i, Q_i) + \bar{Q}_L Y_U U_R H + \bar{Q}_L Y_D D_R \tilde{H}$$

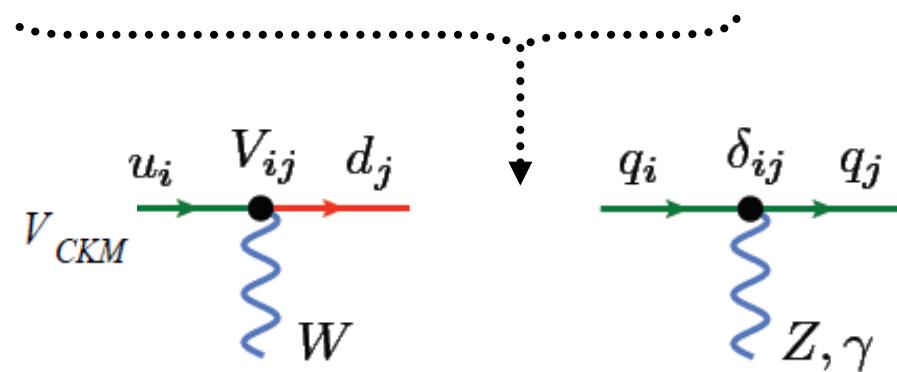
**Higgs gives rise to CKM and Masses by Yukawa interactions**

$$Y_U = V_{CKM}^\dagger \hat{M}_u \quad V_{CKM}^\dagger V_{CKM} = 1 \quad Y_D = \hat{M}_d$$

# Flavour Physics Today

Thanks to modern experiments (*Babar, Belle, KLOE, NA48, Tevatron & LHC*) ,  
the Yukawa interaction has been confirmed with high accuracy  
as the dominant source of Flavour and CP violation at low energy.

$$\mathcal{L}_{SM} = \mathcal{L}_{gauge}(A_i, Q_i) + \overline{Q}_L \mathbf{Y}_U \mathbf{U}_R H + \overline{Q}_L \mathbf{Y}_D \mathbf{D}_R \tilde{H}$$



✓ Two of 9 unitarity relations of CKM,  
tested at percent level

$$1) |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

$$2) V_{cd} V_{cb}^* + V_{ud} V_{ub}^* + V_{td} V_{tb}^* = 0$$

✓ Only 4 parameters  $V_{us}$ ,  $V_{cb}$ ,  $\rho$  and  $\eta$ ,  
control a large set of Flavour  
observables to a high accuracy!

✓ Only 1 parameter  $\eta$  controls CP violation!

$V$ : CKM matrix

$\delta$ : unit matrix

$$V_{CKM} = \begin{pmatrix} d & s & b \\ u & c & t \end{pmatrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix}$$

$$V_{us} = \lambda, \quad V_{cb} = A\lambda^2$$

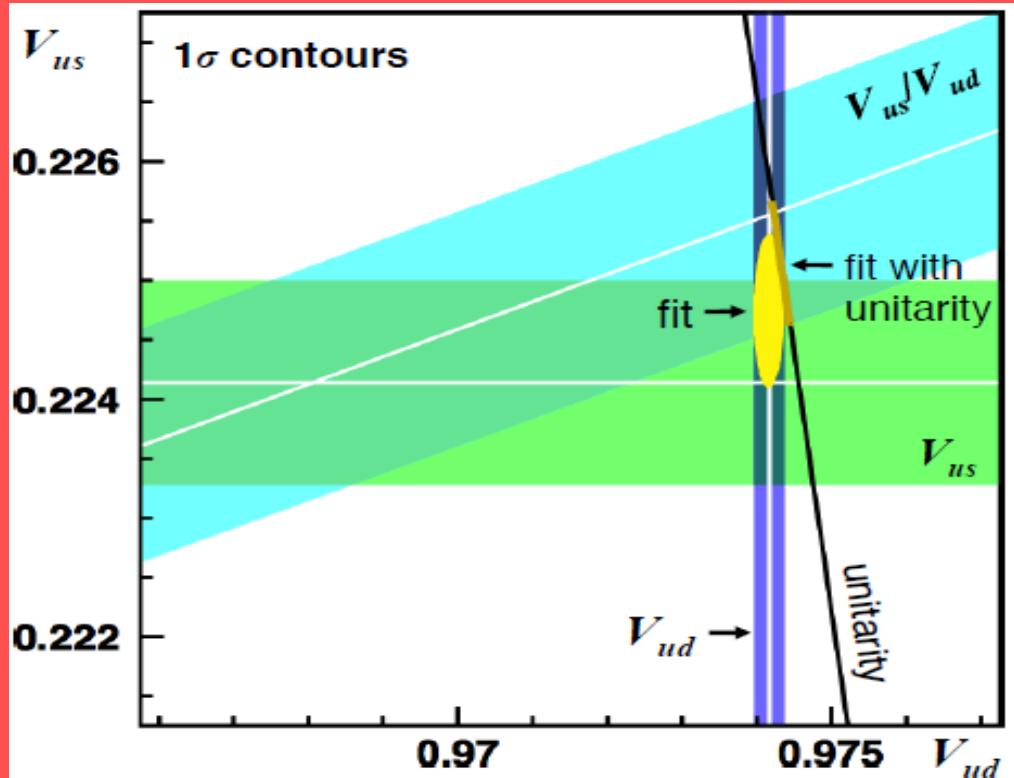
## $V_{us}$ and $V_{ud}$ - unitarity test

$$\left( V_{CKM}^\dagger V_{CKM} \right)_{uu} \equiv |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = -0.0005(5)$$

- ❖ 1 angle to fit 3 measurements
- ❖ lattice inputs,  $f_K/f_\pi$  &  $f_+(0)$ , @0.4%

$|V_{ud}|$  from  $\beta$  nuclear decays  
 $|V_{us}|$  from  $K \rightarrow \pi/\nu$  decays  
 $|V_{us}|/|V_{ud}|$  from  $K \rightarrow \mu\nu$  decays



Fit results, no constraint:

$$\begin{aligned}
 |V_{ud}| &= 0.97416(21) \\
 |V_{us}| &= 0.2248(7) \\
 \Delta_{CKM} &= -0.0005(5)
 \end{aligned}$$

Fit results, unitarity constraint:

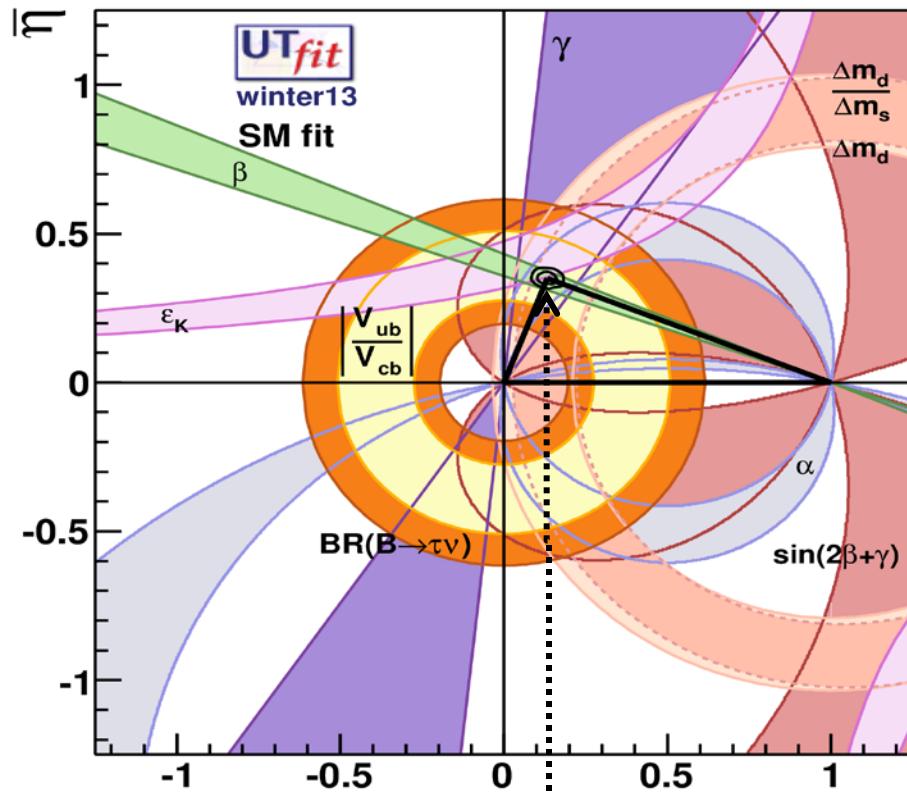
$$\begin{aligned}
 |V_{ud}| &= \cos\theta_c = 0.97432(12) \\
 |V_{us}| &= \sin\theta_c = 0.2251(5)
 \end{aligned}$$

See FLAG13, 1310.8555,  
for last results

# Unitarity triangle Analysis:

$$\left( V_{CKM} V_{CKM}^\dagger \right)_{db} \equiv V_{cd} V_{cb}^* + V_{ud} V_{ub}^* + V_{td} V_{tb}^* = 0$$

see also results by CKMfitter and Laiho, E. Lunghi & R. Van de Water



$$V_{cd} V_{cb}^* + V_{ud} V_{ub}^* + V_{td} V_{tb}^* = 0$$

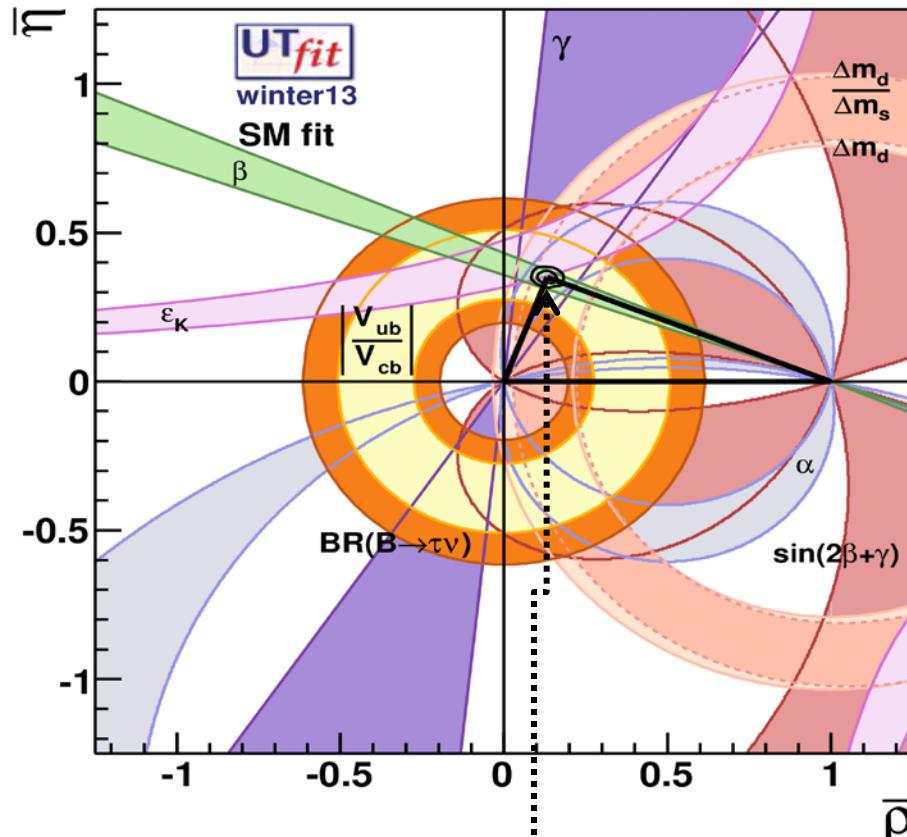
$$1 + \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} + \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} = 0$$

All exp. band overlap in a common area

$$\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \approx \sqrt{\bar{\rho}^2 + \bar{\eta}^2}$$

$$\frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \approx \sqrt{(1 - \bar{\rho})^2 + \bar{\eta}^2}$$

## **Unitarity triangle Analysis:** $\left( V_{CKM} V_{CKM}^\dagger \right)_{db} \equiv V_{cd} V_{cb}^* + V_{ud} V_{ub}^* + V_{td} V_{tb}^* = 0$



$$\bar{\rho} = 0.139 \pm 0.021 \rightarrow 15\%$$

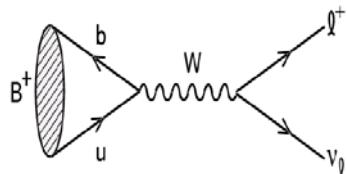
$$\bar{\eta} = 0.352 \pm 0.016 \rightarrow 4.5\%$$

**4 CKM parameters to fit more than 11 measurements**

$ V_{ud} ,  V_{us} ,  V_{cb} ,  V_{ub} _{SL}$	$B \rightarrow \tau \nu$
$\Delta m_d, \Delta m_s, \epsilon_K$	
$\alpha, \sin 2\beta, \gamma$	

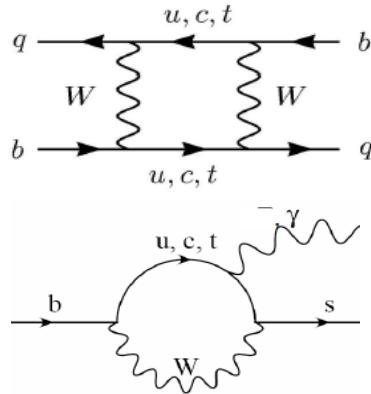
# Unitarity triangle Analysis: closer look

## I. Remarkable consistency between tree-level processes

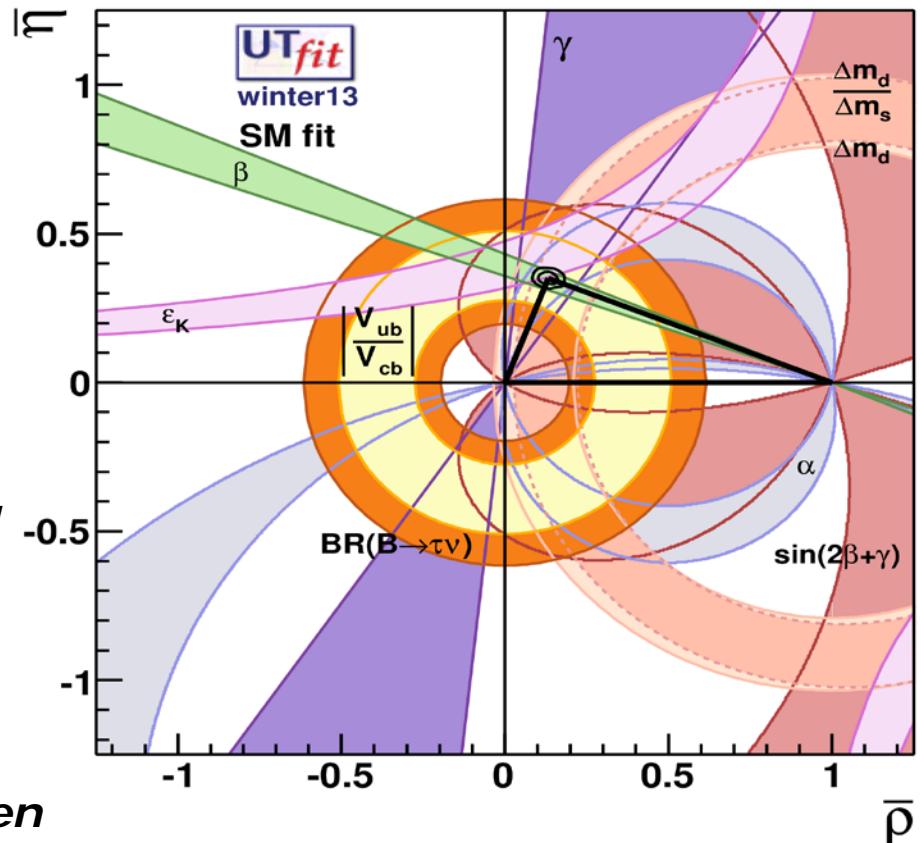


$\gamma, \alpha, V_{ub}, V_{cb}$

## and loop induced observables (FCNC)



$\sin(2\beta), \Delta m_{ds}, \varepsilon_K, b \rightarrow s \gamma \dots$

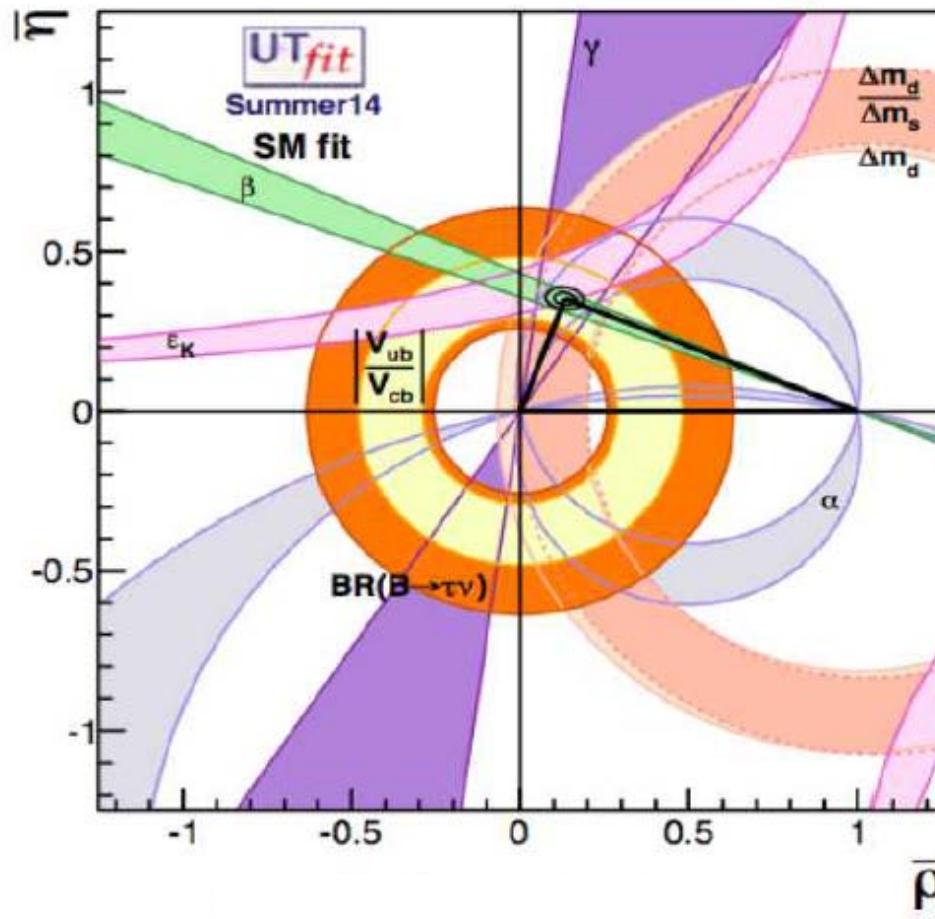


## II. Remarkable consistency between CPC and CPV observables

$\Delta m_{ds}, \varepsilon_K$

$$V_{cd} V_{cb}^* + V_{ud} V_{ub}^* + V_{td} V_{tb}^* = 0$$

## What's Next?



❖ Despite all its successes, the SM is likely to be an effective theory, the low-energy limit of a more fundamental theory, with new degrees of freedom above the electroweak scale

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Already many hints for physics beyond SM:

- :( gravity, :(neutrino oscillations,
- :(dark matter, :(matter/anti-matter asymmetries

no clear clues to NP model **but n.o.f at high scale looks necessary!**

Moreover, open questions within Flavour dynamics itself

➤ What is the origin of Yukawa couplings in the SM?

→ new degrees of freedom at unification scale  $10^{15}$  TeV,  $M_{\text{planck}}$ ?

**Yukawa int.:** large loop corrections to the higgs mass → NP at O(1 TeV)?

$$m_H^2 \propto \frac{\Lambda_{\text{cutoff}}^2}{16\pi^2} \log \frac{\Lambda_{\text{cutoff}}^2}{m_{\text{top}}^2}$$

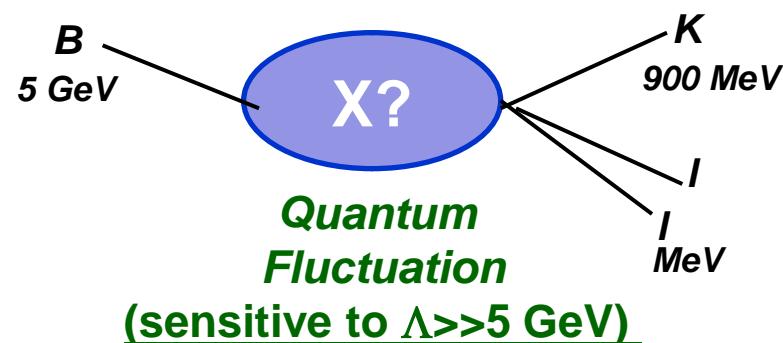
Diagram illustrating the loop correction to the Higgs mass. A circular loop with arrows indicates a top quark loop. External lines are labeled with Higgs bosons (H) and top quarks (t). The loop is enclosed in a dashed circle.

# What's Next?

- ❖ Despite all its successes, the SM is likely to be an effective theory, the low-energy limit of a more fundamental theory, with new degrees of freedom above the electroweak scale



Potential new degrees of freedom can modify Flavour decays through quantum fluctuations



twofold role of Flavour physics in the LHC era

Identify BSM mechanism of Flavour-breaking

Probe physics at energy scale not accessible at LHC

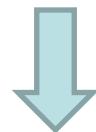
Are the Yukawa couplings the only source of Flavour?

# Twofold role of Flavour for BSM - Example $\epsilon_K$ and SUSY

- NATURAL SUSY Constraints from  $\epsilon_K$ :

[Mescia, Virto, 1208.0533]

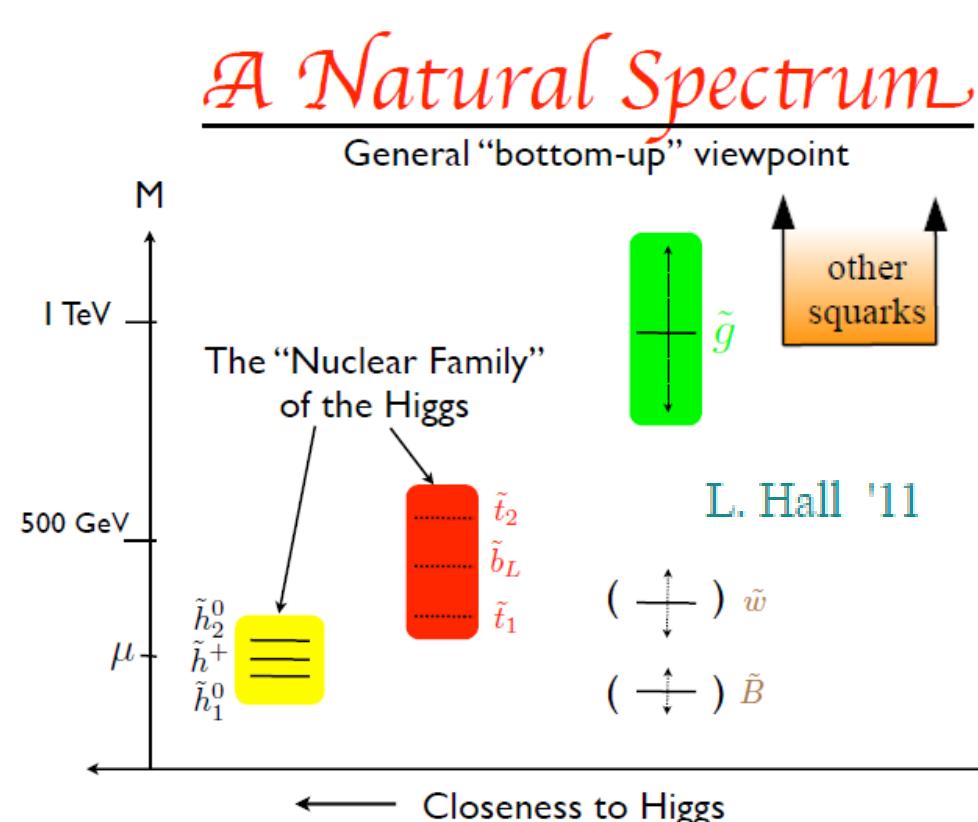
- i. 1<sup>st</sup> & 2<sup>nd</sup> gen. squarks has to be heavy to escape current LHC bounds
- ii. But stop, sbottom and Higgsinos need to be light to avoid tuning in  $m_h$



NATURAL SUSY:



- non-trivial flavour spectrum:  
3<sup>rd</sup> gen. of squarks lighter than others

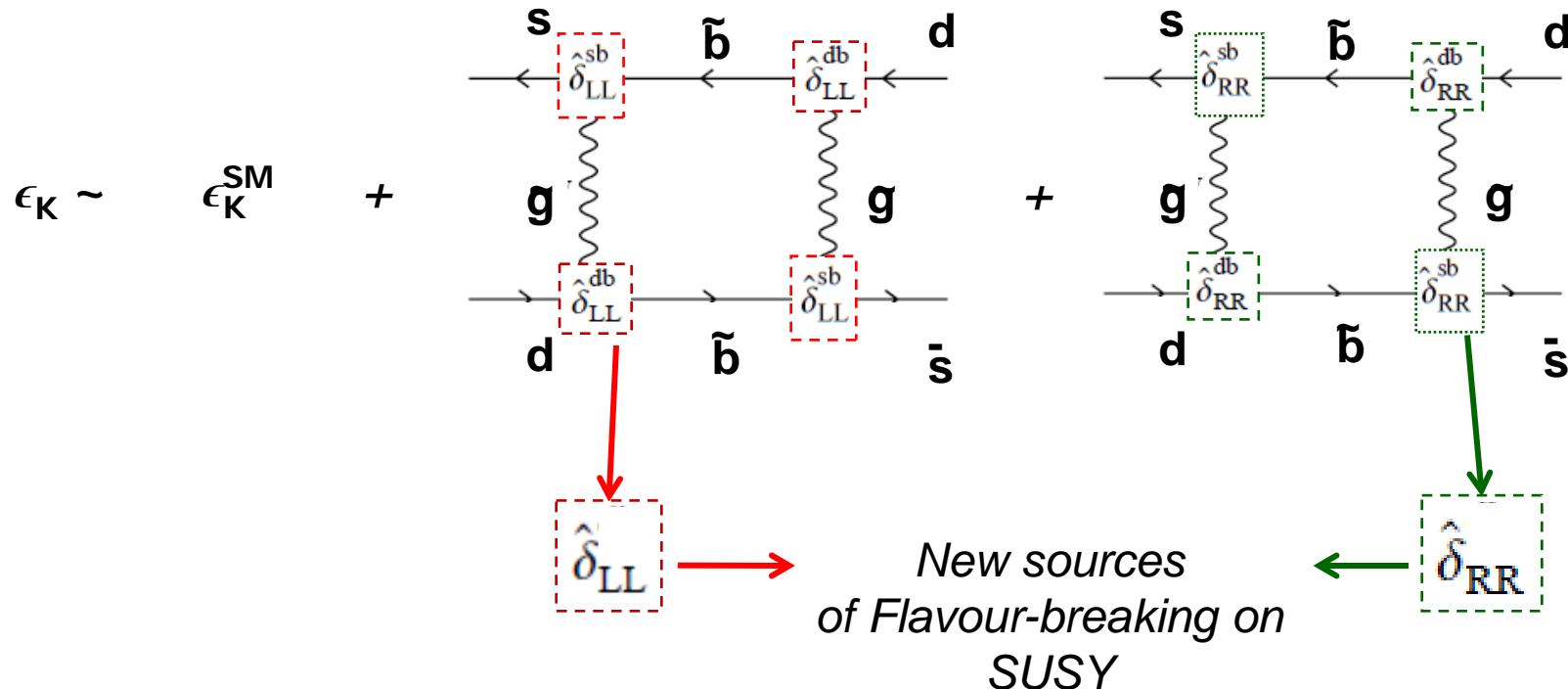


$\epsilon_K$  mediated by 3<sup>rd</sup> generations of squarks!!

# Twofold role of Flavour for BSM - Example $\epsilon_K$ and SUSY

- NATURAL SUSY Constraints from  $\epsilon_K$ :

[Mescia, Virto, 1208.0533]



Two scenarios and the  
twofold role of Flavour:

$$\hat{\delta}_{LL} = \hat{\delta}_{RR} \sim \text{CKM}$$

1

$$\hat{\delta}_{LL} \sim \text{CKM}, \hat{\delta}_{RR} = 0$$

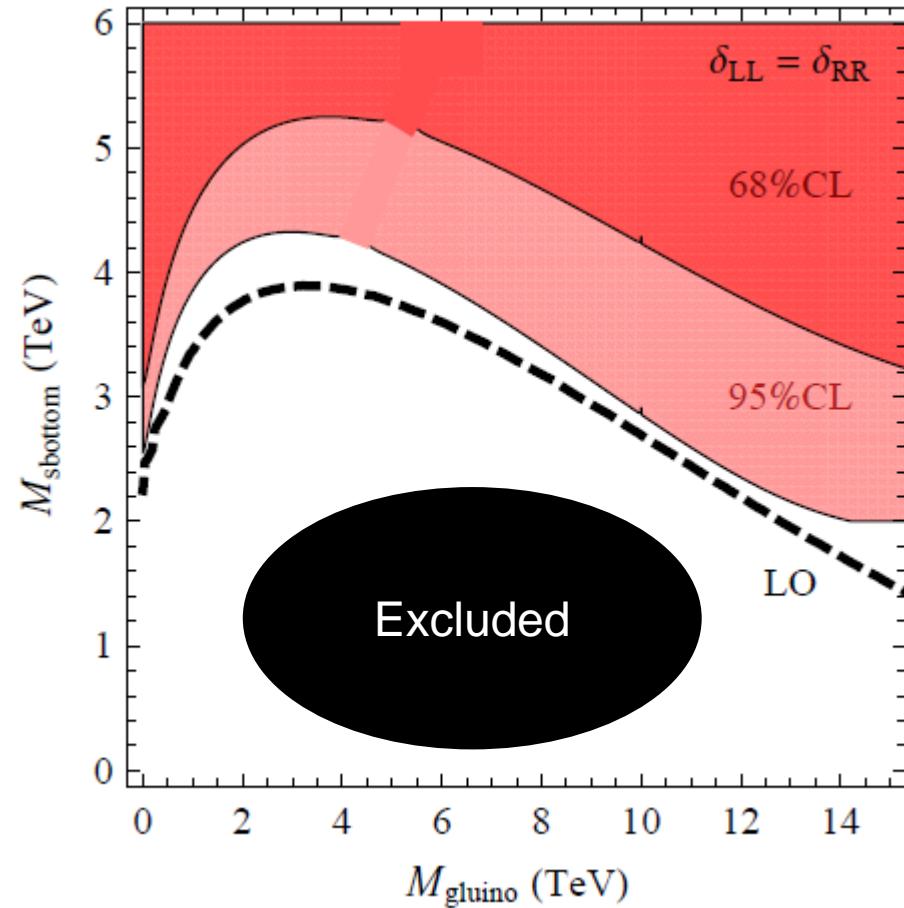
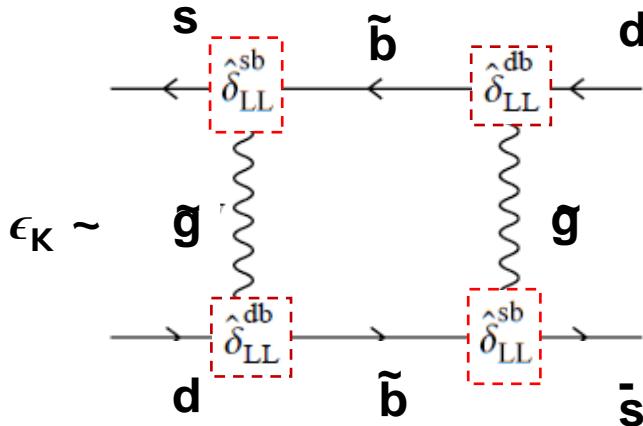
2

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$$\hat{\delta}_{LL} = \hat{\delta}_{RR} \sim \text{CKM}$$



The twofold role of Flavour

1

Natural SUSY hypothesis ( $m_{sbottom} < 1$  TeV) ?  
built in to pass LHC searches excluded by Flavour breaking 1

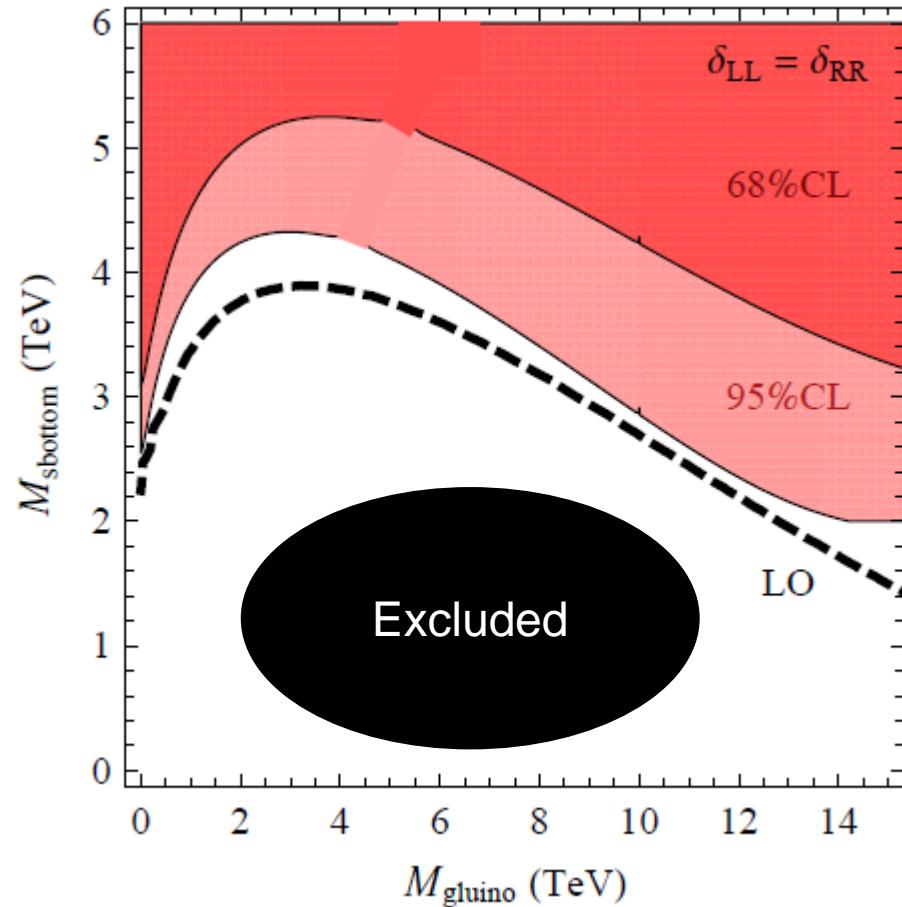
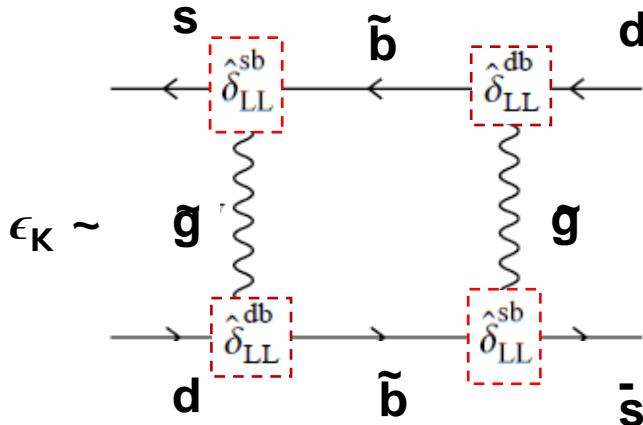


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Powerful role of Flavour

1

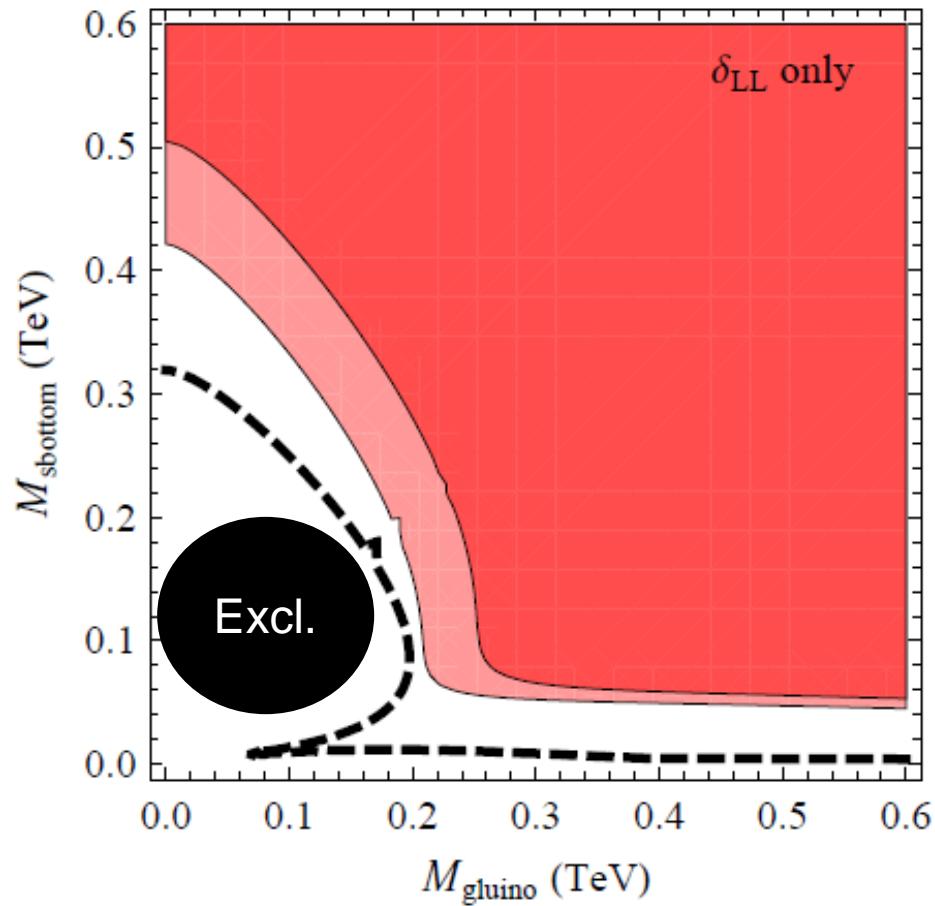
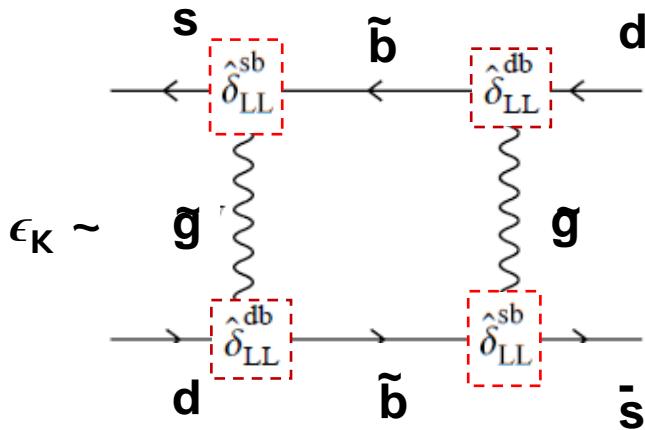
NP too heavy and not directly accessible at LHC:  $m_{\text{sbottom}} > 3$  TeV  
– but still accessible by Flavour observables through loops –

# Twofold role of Flavour for BSM - Example $\epsilon_K$ and SUSY

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$$\hat{\delta}_{LL} \sim \text{CKM}, \hat{\delta}_{RR} = 0$$



Powerful role of Flavour

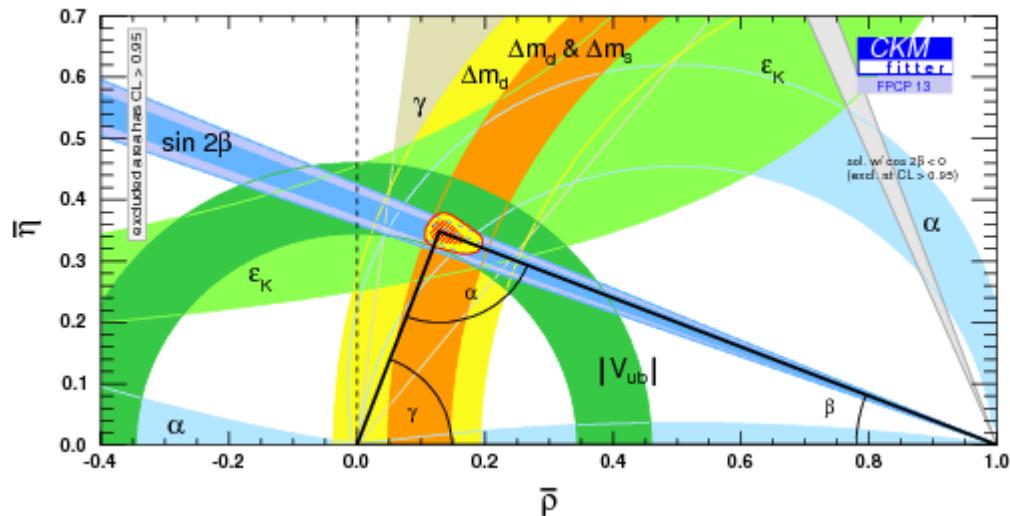
2

OK Natural SUSY spectrum ( $m_{\text{sbottom}} < 1$  TeV)!  
- Flavour helpful to fix BSM symmetries.  $\hat{\delta}_{RR}^{db} = 0$



# Future perspective for New Physics via Flavour Window

- What is the origin of Yukawa couplings in the SM?
- Are the Yukawa couplings the only source of Flavour?



- In many observables theoretical errors still larger than exp. ones
  - 1. Refined CKM fits to 1% by Belle II and LHCb:  
→ new physics in  $B_d$ ,  $B_s$  and  $K$  mixing! **2020**
  - 2.  $b \rightarrow s$  transitions: possible "rich" ground for surprises!  
→ already some anomalies in  $B_d \rightarrow K^* \mu \mu$ ! **NOW LHCb**
  - 3. Rare Kaon decays:  $s \rightarrow d$  penguins  
→ 2020, NA62, JPARC..

# 1. CKM fits to 1% by tree-level modes (2020)

Experimental errors on  $B$  and  $K$  mixings are already below 1%

$\epsilon_K$ :  $K^0$ - $\bar{K}^0$  mixing  
exp. err 0.5%  
th.err 10%

$\Delta M_d$ :  $B^0_d$ - $B^0_d$  mixing  
exp. err 0.7%  
th.err 6%

$\Delta M_s$ :  $B^0_s$ - $B^0_s$  mixing  
exp. err 0.1%  
th.err 6%

By reducing the theory errors we become more sensitive to NP:  
2 sources of th. error: hadronic + parametrical (CKM, masses) ones

2 sources of theory error:  
hadronic + parametrical  
uncertainties  
(CKM, masses)

$$A_{\Delta F=2} \left( P_{ij} \rightarrow \bar{P}_{ij} \right) \sim \underbrace{\left( V_{ti} V_{tj}^* \right)^2}_{4\%} \times \underbrace{m_t^2}_{2\%} \times m_P^2 \underbrace{f_P^2}_{6\%} \underbrace{B_P}_{3\%}$$

parametrical uncertainties

hadronic uncertainties

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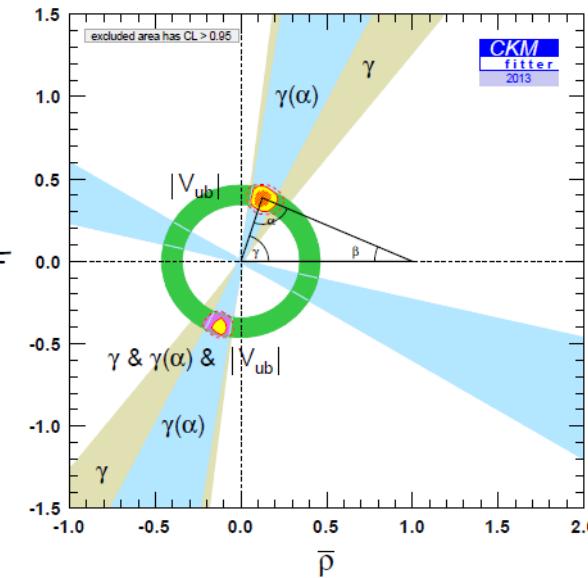
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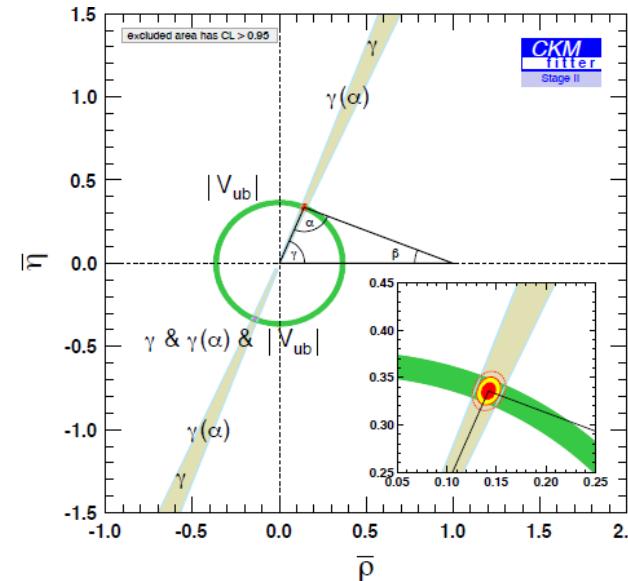
2014

$$\begin{aligned}\bar{\rho} &\sim 15\% \\ \bar{\eta} &\sim 10\%\end{aligned}$$

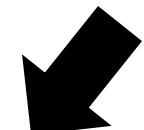


2020

$$\begin{aligned}\bar{\rho} &\sim 1\% \\ \bar{\eta} &\sim 1\%\end{aligned}$$



*Drastic reduction of CKM parametrical uncertainties  
by improving  $V_{ub}$  and  $\gamma$*



Belle II @  $50\text{ab}^{-1}$   
LHCb @  $50\text{fb}^{-1}$

# Tension in CKM fits: $\epsilon_K \sin(2\beta)$ , $V_{ub}$

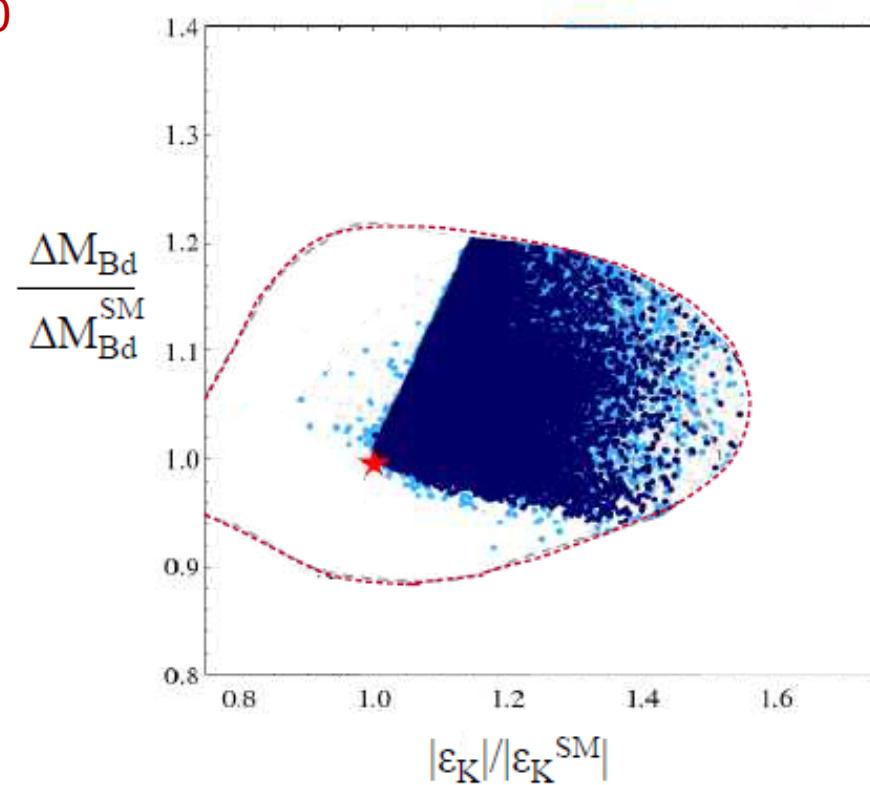
Parameter	Input value	SM Prediction	UTfit Collaboration
$\sin(2\beta)$	$S_{\psi K_s} = 0.680 \pm 0.023$	$0.755 \pm 0.044$	-
$ \epsilon_K $	$0.002228 \pm 0.000013$	$0.00188 \pm 0.0002$	+ fit vs. exp $\approx 2.4\sigma$

Weak evidence of  $|\epsilon_K^{\text{Exp}}| - |\epsilon_K^{\text{SM}}| > 0$

A positive contribution to  $\epsilon_K$  is common to MFV-like (SUSY) models

Barbieri, Buttazzo, Sala, Straub '13

In order to clarify the picture we need a more clean determination of  $|V_{ub}|$  &  $\gamma$



Points allowed by [present CMS/ATLAS data](#) + [present flavor data](#)

## 2. $b \rightarrow s$ transitions: possible “rich” ground for surprises!

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- ✓ Large amount of observables: a rich anatomy of  $b \rightarrow s$  couplings

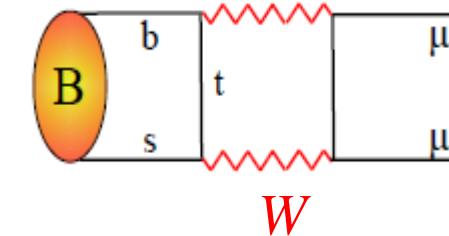
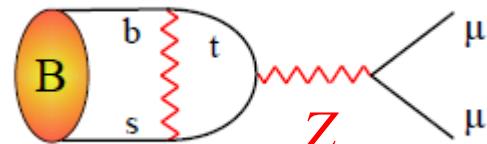
*LHCb TASK*

# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu$

SM operators

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}, O_9 = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \ell$$

$$O_{10} = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \gamma_5 \ell$$



$$\Gamma(B_s^0 \rightarrow \mu^+ \mu^-) \sim \frac{G_F^2 \alpha^2}{64\pi^3} m_{Bs}^2 f_{Bs}^2 |V_{tb} V_{ts}|^2 |2m_\mu C_{10}|^2$$

Special Mode

- ❖ double suppressed!
  - No SM tree-level contributions (FCNC)
  - Helicity suppression
- ❖ hadronic uncertainties under control

Only one hadronic parameter:  $f_{Bs}$

$$\langle 0 | \bar{b} \gamma^\mu \gamma_5 s | B_s^0 \rangle = i q^\mu f_{Bs}$$

$$f_{Bs} = (228 \pm 5) \text{ MeV}$$

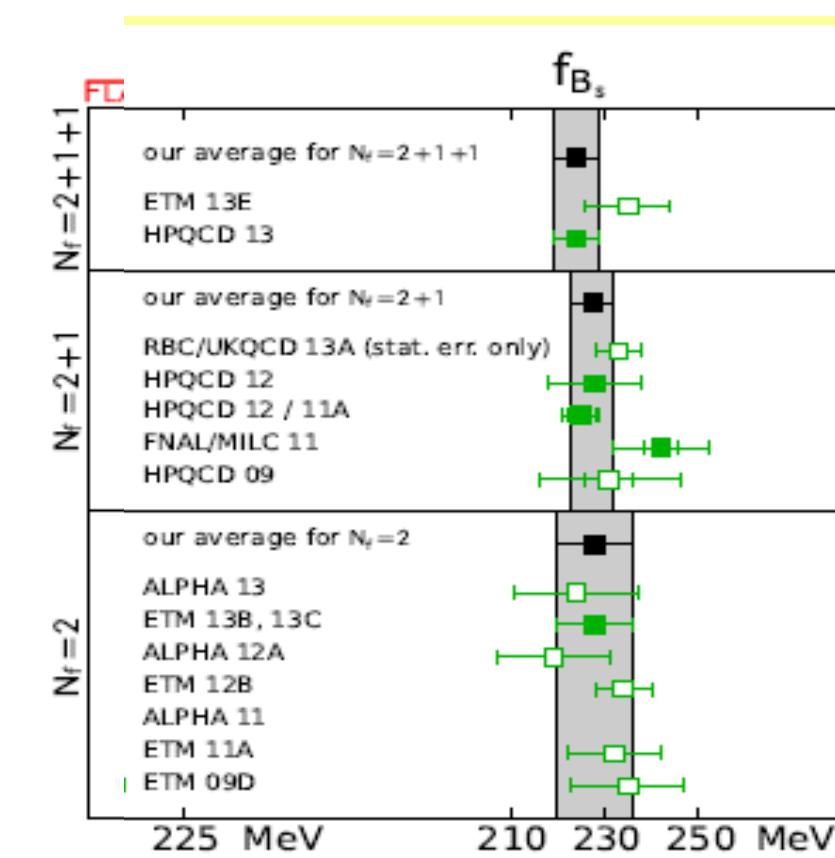
3% hadronic uncertainty

Lattice from many groups

# Theory: Hadronic Uncertainties

$B_s \rightarrow \mu\mu$

$f_{B_s}$



Only one hadronic parameter:  $f_{B_s}$

$B_s \rightarrow \mu\mu$

$$\langle 0 | \bar{b} \gamma^\mu \gamma_5 s | B_s^0 \rangle = i p^\mu f_{B_s}$$

$$\text{Br}(B_s \rightarrow \mu\mu)^{\text{SM}} = (3.3 \pm 0.3) \times 10^{-9} \text{ (8%)}$$

See FLAG13, 1310.8555,  
for last results

$$f_{B_s} = (228 \pm 5) \text{ MeV}$$

3% hadronic uncertainty

Lattice from many groups

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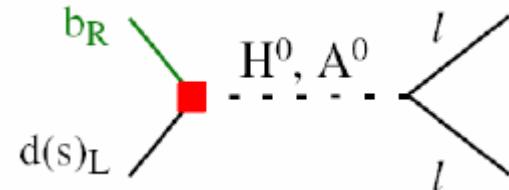
$$O_{10} = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

BSM operators

$$O_{S(P)} = (\bar{b}_R s_L) \bar{\ell} \ell_{S(P)}, O_T = (\bar{b}_R \sigma^{\mu\nu} s_L) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

SUSY at large  $\tan\beta$



$$A(B \rightarrow ll)_H \sim \frac{m_b m_l}{M_A^2} \frac{\mu A_U}{\tilde{M}_q^2} \tan^3 \beta$$

GOLDEN MODE at LHCb  
enhanced  $C_{S(P)} \sim \tan^3 \beta$

Only one hadronic parameter:  $f_{B_s}$

$$\begin{aligned} \Gamma(B_s^0 \rightarrow \mu^+ \mu^-) &\sim \frac{G_F^2 \alpha^2}{64\pi^3} m_{B_s}^2 f_{B_s}^2 |V_{tb} V_{ts}|^2 \\ &\times \left[ \left| 2m_\mu (C_{10} - C'_{10}) + m_{B_s} (C_P - C'_P) \right|^2 \right. \\ &\quad \left. + m_{B_s} \left| (C_S - C'_S) \right|^2 \right] \end{aligned}$$

$$\langle 0 | \bar{b} \gamma^\mu \gamma_5 s | B_s^0 \rangle = i q^\mu f_{B_s}$$

$$\begin{aligned} \langle 0 | \bar{b} \gamma_5 s | B_s^0 \rangle &= -i f_{B_s} M_{B_s}^2 / m_b \\ &\text{(PCAC Ward Identity)} \end{aligned}$$

# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu$

SM operators

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}, O_9 = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \ell$$

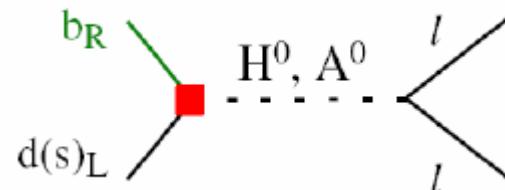
$$O_{10} = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

BSM operators

$$O_{S(P)} = (\bar{b}_R s_L) \bar{\ell} \ell_{S(P)}, O_T = (\bar{b}_R \sigma^{\mu\nu} s_L) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

SUSY at large  $\tan\beta$



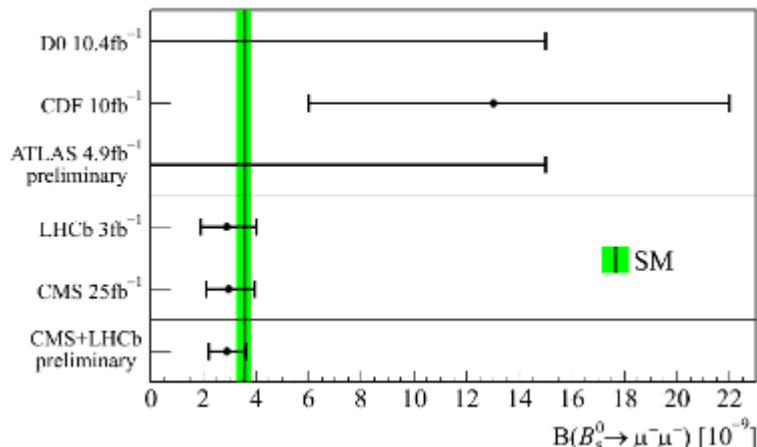
$$A(B \rightarrow ll)_H \sim \frac{m_b m_l}{M_A^2} \frac{\mu A_U}{\tilde{M}_q^2} \tan^3 \beta$$

GOLDEN MODE at LHCb  
enhanced  $C_{S(P)} \sim \tan^3 \beta$

**BIG News:**

- ✓ Nov. 2012, first evidence of  $B_s \rightarrow \mu^+ \mu^-$  from LHCb
- ✓ July 2013, LHCb-CMS world average

⇒ **PANIC:**  $\text{Br}^{\text{exp}}(B_s \rightarrow \mu\mu) = (2.9 \pm 0.7) 10^{-9}$  (25%)  
 $\text{Br}^{\text{SM}}(B_s \rightarrow \mu\mu) = (3.3 \pm 0.3) 10^{-9}$  (8%)



# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu$

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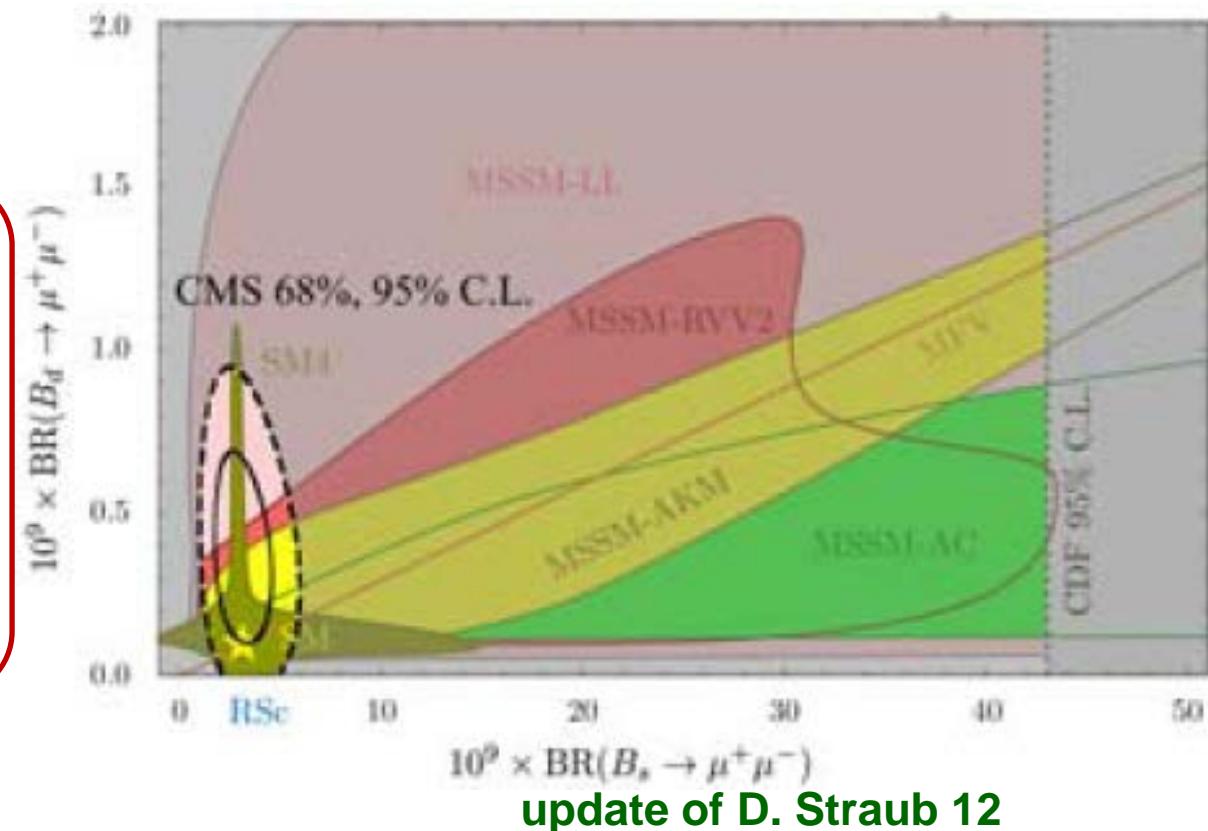
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$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

☞ PANIC:

$$\text{Br}^{\text{exp}}(B_s \rightarrow \mu\mu) = (2.9 \pm 0.7) 10^{-9}$$

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BSM operators

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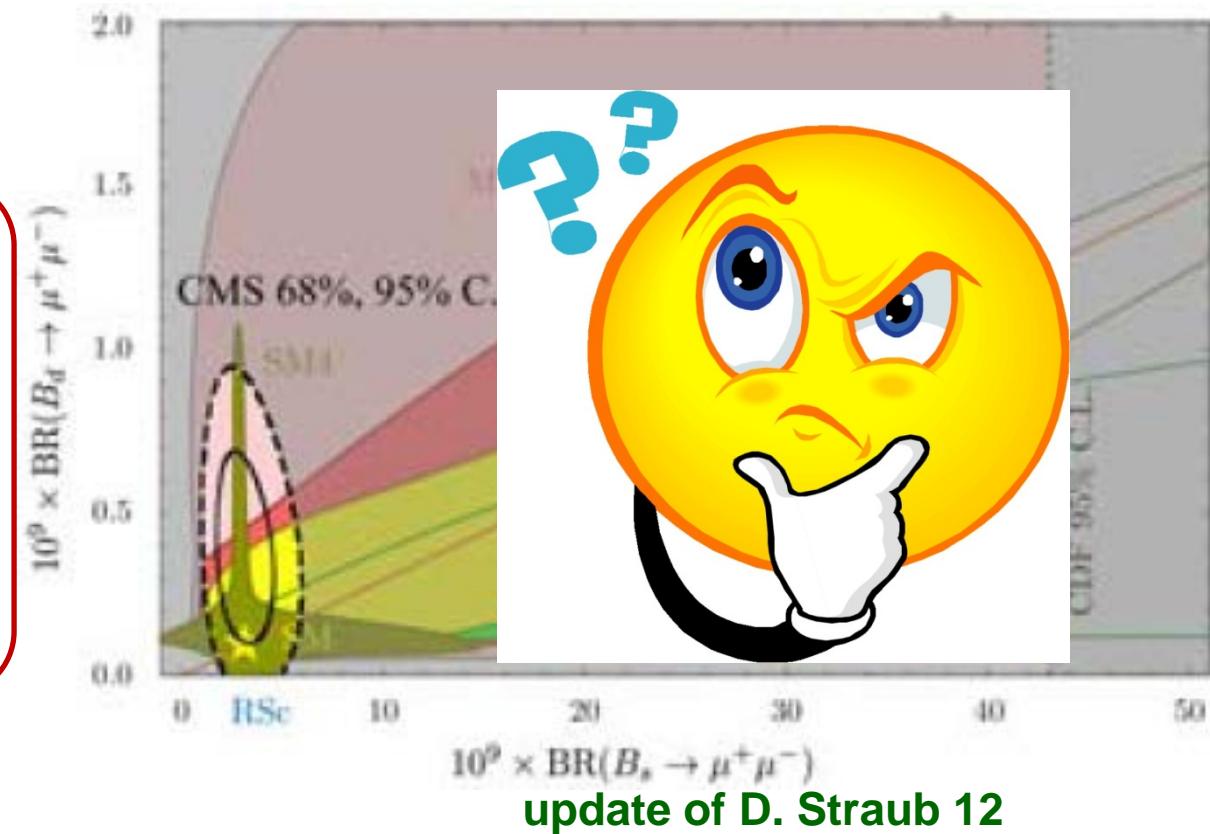
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$$\text{Br}^{\text{SM}}(B_s \rightarrow \mu\mu) = (3.3 \pm 0.3) 10^{-9}$$

☞ NO NEW PHYSICS?



# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu + B \rightarrow K^{(*)}\mu\mu + B_s \rightarrow \tau\tau$

## SM operators

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}, O_9 = \left( \bar{b} \gamma^\mu s \right) \bar{\ell} \gamma^\mu \ell$$

$$O_{10} = \left( \bar{b} \gamma^\mu s \right) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

## BSM operators

$$O_{S(P)} = \left( \bar{b}_R s_L \right) \bar{\ell} \ell_{S(P)}, O_T = \left( \bar{b}_R \sigma^{\mu\nu} s_L \right) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

⇒ PANIC:

$$\text{Br}^{\text{exp}}(B_s \rightarrow \mu\mu) = (2.9 \pm 0.7) 10^{-9}$$

$$\text{Br}^{\text{SM}}(B_s \rightarrow \mu\mu) = (3.3 \pm 0.3) 10^{-9}$$

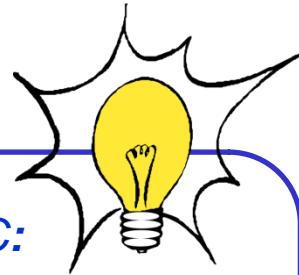
⇒ NO NEW PHYSICS?

⇒ NO PANIC:

$$B \rightarrow K^* \mu\mu, B \rightarrow K \mu\mu \& B \rightarrow \tau\tau$$

sensitive to different “ $b \rightarrow s$  couplings”

3 ways out to overcome the  $B_s \rightarrow \mu\mu$  constraints



# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu + B \rightarrow K^{(*)}\mu\mu$

SM operators

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}, O_9 = \left( \bar{b} \gamma^\mu s \right) \bar{\ell} \gamma^\mu \ell$$

$$O_{10} = \left( \bar{b} \gamma^\mu s \right) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

BSM operators

$$O_{S(P)} = \left( \bar{b}_R s_L \right) \bar{\ell} \ell_{S(P)}, O_T = \left( \bar{b}_R \sigma^{\mu\nu} s_L \right) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

$$\begin{aligned} \Gamma(B_s^0 \rightarrow \mu^+ \mu^-) &\sim \frac{G_F^2 \alpha^2}{64\pi^3} m_{Bs}^2 f_{Bs}^2 |V_{tb} V_{ts}|^2 \\ &\times \left[ \left| 2m_\mu (C_{10} - C'_{10}) + m_{Bs} (C_P - C'_P) \right|^2 \right. \\ &\quad \left. + m_{Bs} \left| (C_S - C'_S) \right|^2 \right] \end{aligned}$$

☺ **No contribution from  $O_9$**   
 ☺  **$C_9$  couplings unconstrained by  $B_s \rightarrow \mu\mu$**



J. Matias, S Descotes-Genon, J. Virto '13

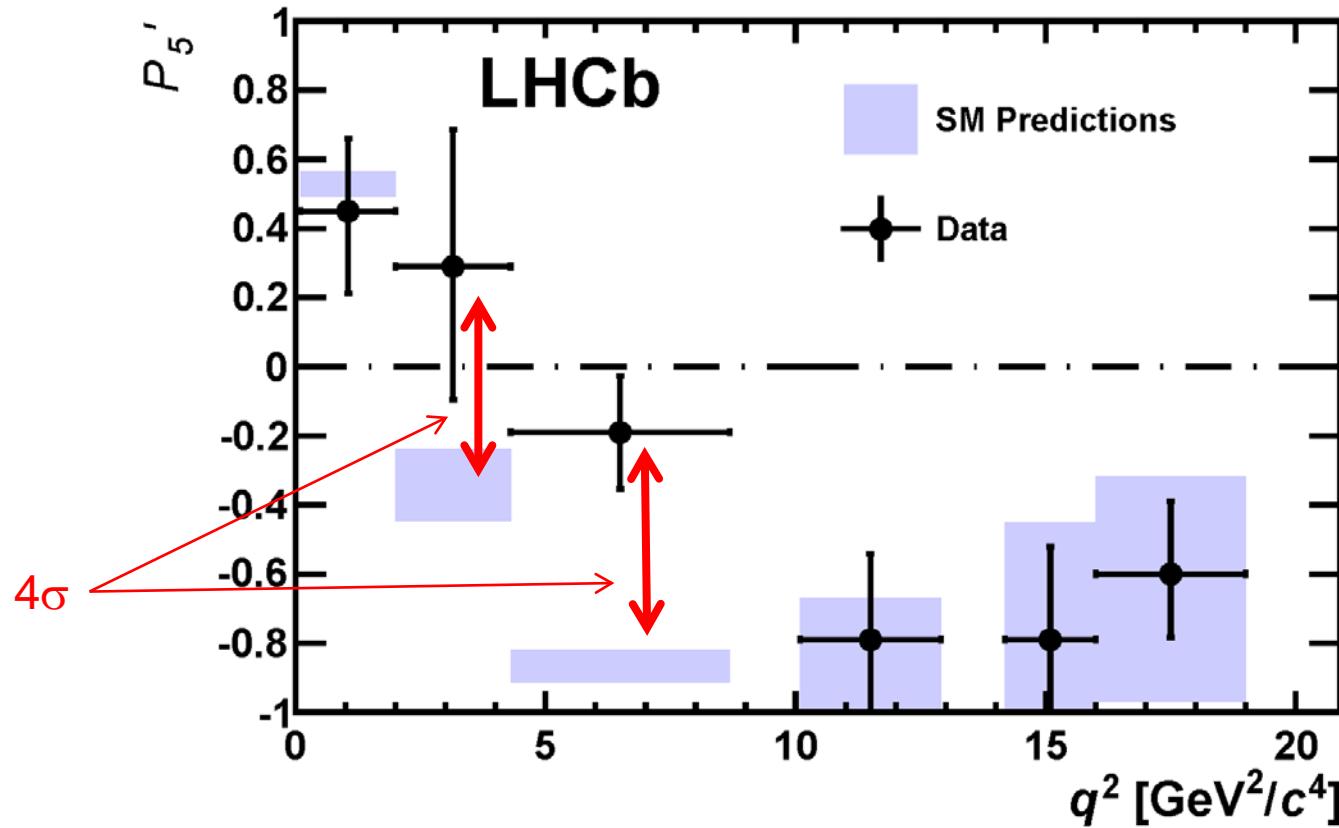
However,  $O_9$  gives contribution to  $B \rightarrow K^*\mu\mu$ ,  $B \rightarrow K\mu\mu$ , and non-SM effects can be possible

1

$$\langle B(p) | \bar{b} \gamma^\mu s | K(k) \rangle = (p^\mu + k^\mu - \frac{m_B^2 - m_K^2}{q^2} q^\mu) f_+(q^2) + \frac{m_B^2 - m_K^2}{q^2} q^\mu f_0(q^2)$$

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu\mu$

July 2013, LHCb found a deviation of about  $4\sigma$  w.r.t the SM in the  $P_5'$  observable, one of the coefficients of the  $B \rightarrow K^* \mu\mu$  angular distribution

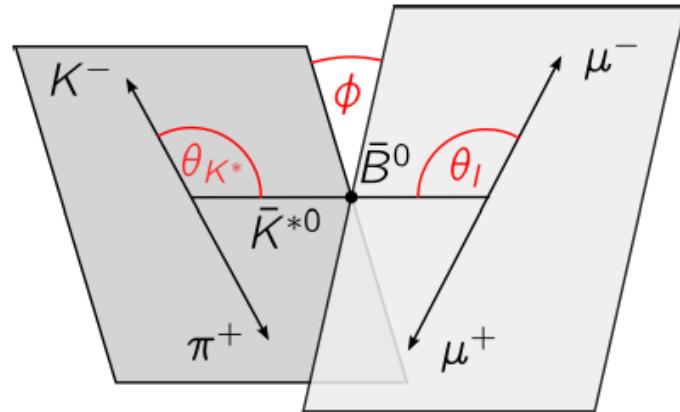


July  
2013

Warning: LHCb analysis low statistics -- about 800 events  $B \rightarrow K^* \mu\mu$

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu \mu$

$$\bar{B}^0 \rightarrow \bar{K}^{*0} (\rightarrow K^- \pi^+) \mu^+ \mu^-$$



$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + \cancel{F_L} \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell + \cancel{S_3} \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + \cancel{S_4} \sin 2\theta_K \sin 2\theta_\ell \cos \phi + \cancel{S_5} \sin 2\theta_K \sin \theta_\ell \cos \phi + \cancel{S_6} \sin^2 \theta_K \cos \theta_\ell + \cancel{S_7} \sin 2\theta_K \sin \theta_\ell \sin \phi + \cancel{S_8} \sin 2\theta_K \sin 2\theta_\ell \sin \phi + \cancel{S_9} \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right],$$

11 angular coefficients to measure from

$$\bar{B}^0 \rightarrow \bar{K}^{*0} (\rightarrow K^- \pi^+) \mu^+ \mu^-$$

$$P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}$$

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu\mu$

## SM operators

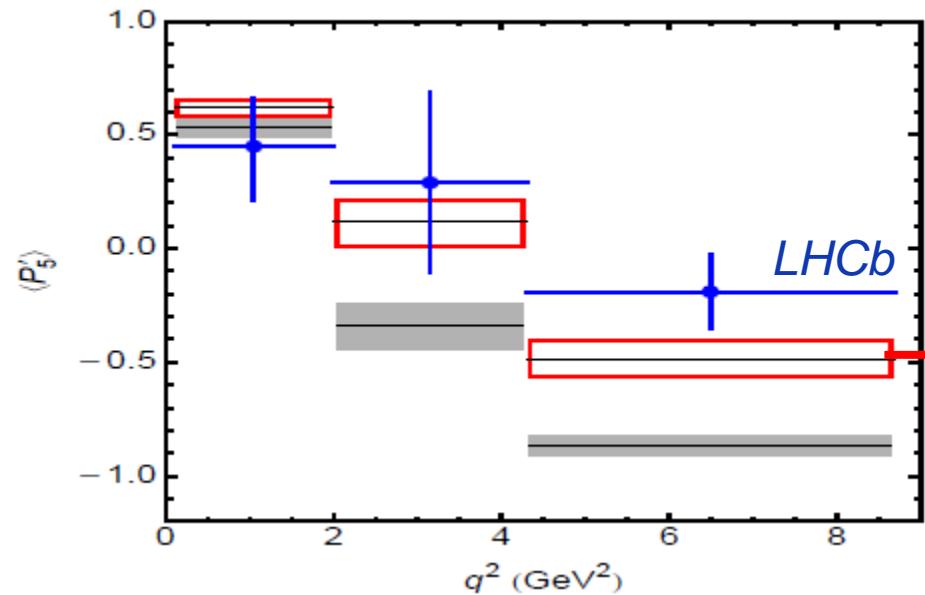
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$$O_{10} = (\bar{b} \gamma^\mu s) \ell \gamma^\mu \gamma_5 \ell$$

## BSM operators

$$O_{S(P)} = (\bar{b}_R s_L) \bar{\ell} \ell_{S(P)}, O_T = (\bar{b}_R \sigma^{\mu\nu} s_L) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$



Warning: LHCb analysis low statistics -- about 800 events  
 $B \rightarrow K^* \mu\mu$

A negative contribution to  $C_9 = C_9^{SM} - 1.5$  improves the agreement between LHCb and SM ( $4\sigma \rightarrow 1.8\sigma$ )

J. Matias, S Descotes-Genon, J. Virto '13

**Warning: still some controversial!**

Are hadronic effects?

J. Lyon, R. Zwicky '14,

S. Jäger, J. M. Camalich '12

NP ruled out by other modes?

Straub et al '14

Experimental fluctuations?

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)}\mu\mu$

## SM operators

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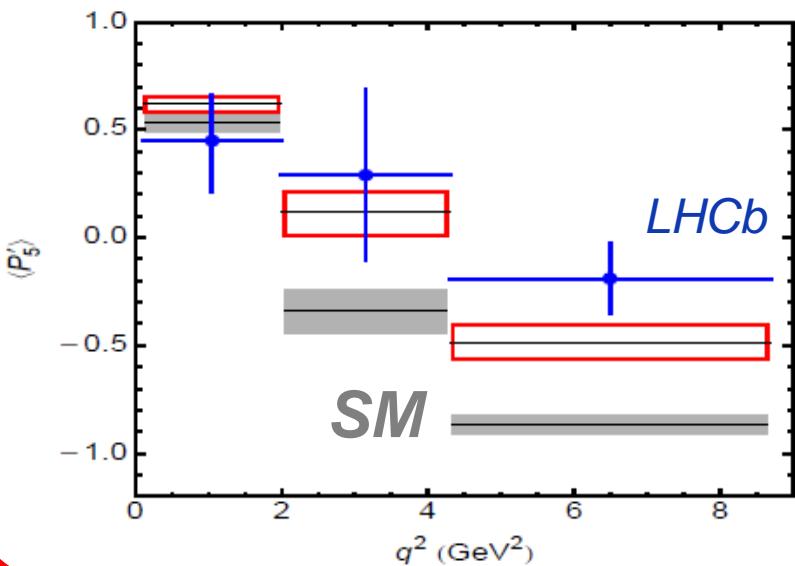
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$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

## 2013 - Anomaly on $B \rightarrow K^*\mu\mu$



## 2014 - Tension on $B \rightarrow K\mu\mu/B \rightarrow Kee$

$$\left( \frac{Br(B \rightarrow K\mu\mu)}{Br(B \rightarrow Kee)} \right)^{SM} = 1.0003 \pm 0.0001$$

$$\left( \frac{Br(B \rightarrow K\mu\mu)}{Br(B \rightarrow Kee)} \right)^{LHCb} = 0.745 \pm 0.096$$

at large recoil region:  
 $1 \text{ GeV}^2 < q^2 < 6 \text{ GeV}^2$

$\sim 2.6\sigma$

A negative contribution to the  $b \rightarrow s\mu\mu$   $C_9$  couplings improves the agreement between LHCb and SM in both cases

R. Alonso '14, G. Hiller '14,  
D. Ghosch '14

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu\mu$

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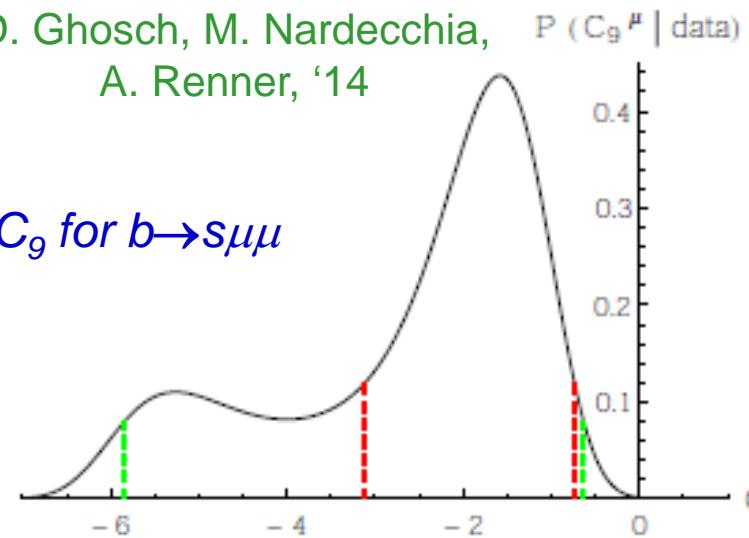
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$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

D. Ghosch, M. Nardecchia,  
A. Renner, '14



2014 - Tension on  $B \rightarrow K \mu\mu / B \rightarrow Kee$

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R. Alonso '14, G. Hiller '14,  
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## Theory: Hadronic Uncertainties

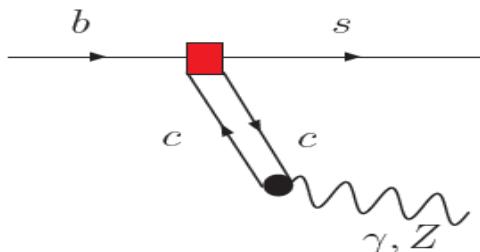
Detour on hadronic  
uncertainties  
*of  $B\rightarrow K^{(*)}\mu\mu$*

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)}\mu\mu$

## Theory: Hadronic Uncertainties

GOAL: calculate  
Matrix elements of 2-  
quark operators  
between hadrons  
(decay constants & Form  
factors)

*Charm Loops*



*SM operators*

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}$$

$$O_9 = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \ell$$

$$O_{10} = (\bar{b} \gamma^\mu s) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

$O_2 = (\bar{b} \gamma^\mu c) (\bar{c} \gamma^\mu s)$

*BSM operators*

$$O_{S(P)} = (\bar{b}_R s_L) \bar{\ell} \ell_{S(P)}, O_T = (\bar{b}_R \sigma^{\mu\nu} s_L) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$+ L \leftrightarrow R$$

Under control (to some extent)  
at low and large  $q^2$ , out of resonance region

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)}\mu\mu$

$$\langle V(p', \varepsilon) | \bar{q} \gamma^\mu b | B(p) \rangle = \frac{2iV(q^2)}{m_B + m_V} \epsilon^{\mu\nu\rho\sigma} \varepsilon_\nu^* p'_\rho p_\sigma$$

$$\langle V(p', \varepsilon) | \bar{q} \gamma^\mu \gamma^5 b | B(p) \rangle = 2m_V A_0(q^2) \frac{\varepsilon^* \cdot q}{q^2} q^\mu$$

**Form Factor Definition for  
 $B \rightarrow K^*\gamma, B \rightarrow K^*ll$**

$$+ (m_B + m_V) A_1(q^2) \left( \varepsilon^{*\mu} - \frac{\varepsilon^* \cdot q}{q^2} q^\mu \right)$$

$$- A_2(q^2) \frac{\varepsilon^* \cdot q}{m_B + m_V} \left( (p + p')^\mu - \frac{m_B^2 - m_V^2}{q^2} q^\mu \right)$$

$$q^\nu \langle V(p', \varepsilon) | \bar{q} \hat{\sigma}_{\mu\nu} b | B(p) \rangle = 2(T_1(q^2)) \varepsilon_{\mu\rho\tau\sigma} \varepsilon^{*\rho} p^\tau p'^\sigma \xrightarrow{\text{one ff. at } q^2=0} \text{Br}(B \rightarrow K^*\gamma)$$

$$q^\nu \langle V(p', \varepsilon) | \bar{q} \hat{\sigma}_{\mu\nu} \gamma^5 b | B(p) \rangle = i T_2(q^2) [\varepsilon_\mu^* (m_B^2 - m_V^2) - (\varepsilon^* \cdot q)(p + p')_\mu]$$

$$+ i T_3(q^2) (\varepsilon^* \cdot q) \left[ q_\mu - \frac{q^2}{m_B^2 - m_V^2} (p + p')_\mu \right]$$

$\text{Br}(B \rightarrow K^*ll)$ : 7 form factors in QCD

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)}\mu\mu$

## Form Factor Definition for $B \rightarrow Kll$

$$\langle B(p) | \bar{b} \gamma^\mu s | K(k) \rangle = (p^\mu + k^\mu - \frac{m_B^2 - m_K^2}{q^2} q^\mu) f_+(q^2) + \frac{m_B^2 - m_K^2}{q^2} q^\mu f_0(q^2)$$

$$\langle B(p) | \bar{b} \sigma^{\mu\nu} s | K(k) \rangle = \frac{i f_T}{m_B + m_K} [(p^\mu + k^\mu) q^\nu - (p^\nu + k^\nu) q^\mu]$$

$Br(B \rightarrow Kll)$ : 3 form factors in QCD

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu\mu$

## Studies of form-factor calculations on the Lattice:

$B \rightarrow K II$

- ❖ HPQCD 2013 -> mature calculation

$N_F=2+1$  stag. fermions: NRQCD,  $m_\pi > 250$  MeV,  $a^{-1} \sim 2$  GeV  $\rightarrow 0$   
**relative form-factor error @5%**

$$f_{+,0,T}(q^2)$$

$N_F=0$ : Wilson fermions: **relativistic fermions**

- ❖ D. Becirevic, N. Kosnik, F. M., E. Schneider, 2012

$B \rightarrow K^* II$

- ❖ R. Horgan et al. 2013

$N_F=2+1$  stag. fermions: NRQCD ,  $m_\pi > 300$  MeV,  $a^{-1} \sim 2$  GeV

**still an exploratory stage:  
K\* stable?**

$$T_{12}(q^2), V(q^2), A_{012}(q^2)$$

see Horgan's talk on PIII-HQ,  
11/09 at 16:00

$N_F=0$ : Wilson fermions: **relativistic fermions**

- ❖ D. Becirevic, V. Lubicz & F. M. 2007

$$T_{12}(q^2)$$

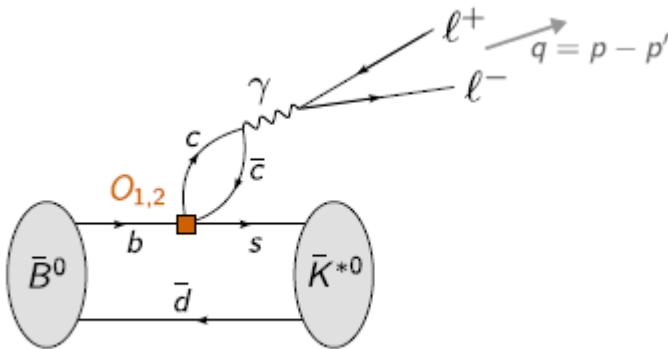
# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu\mu$

## Studies of form-factor calculations on the Lattice:

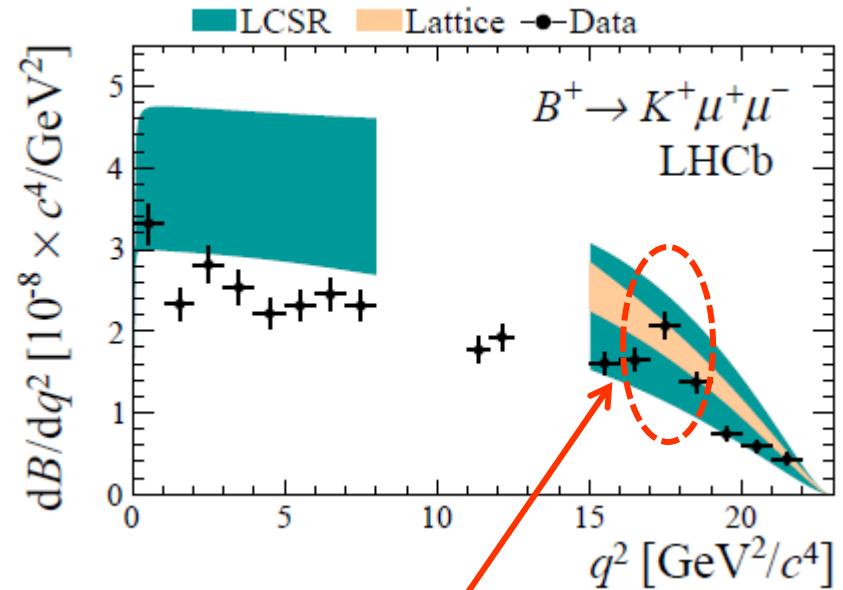
RISK  
AHEAD

❖ NRQCD method

-> automatically gives form factors at zero recoil:  $q^2 > 16 \text{ GeV}^2$



New LHCb results with  $3 \text{ fb}^{-1}$  [arXiv:1403.8044]:



Large contribution from  $\psi(4160)$  at high  $q^2$

See yesterday talk @PII-LQ by AGADJANOV

RISK  
AHEAD

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)}\mu\mu$

$$\bar{B}^0 \rightarrow \bar{K}^{*0} (\rightarrow K^- \pi^+) \mu^+ \mu^-$$

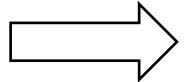
$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + \cancel{F_L} \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ - F_L \cos^2 \theta_K \cos 2\theta_\ell + \cancel{S_3} \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \\ + \cancel{S_4} \sin 2\theta_K \sin 2\theta_\ell \cos \phi + \cancel{S_5} \sin 2\theta_K \sin \theta_\ell \cos \phi \\ + \cancel{S_6} \sin^2 \theta_K \cos \theta_\ell + \cancel{S_7} \sin 2\theta_K \sin \theta_\ell \sin \phi \\ \left. + \cancel{S_8} \sin 2\theta_K \sin 2\theta_\ell \sin \phi + \cancel{S_9} \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right],$$

$F_i$  and  $S_i$  coefficients are plagued by large hadronic uncertainties.



**KEY STRATEGY:** *by using appropriate normalization, we can define observables,  $P_i$ , theoretically clean*

$$P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}$$



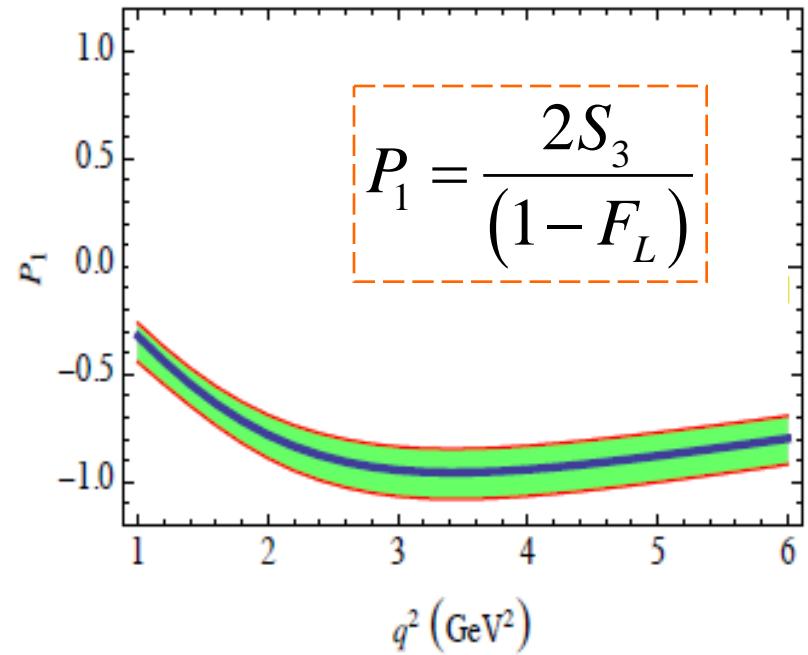
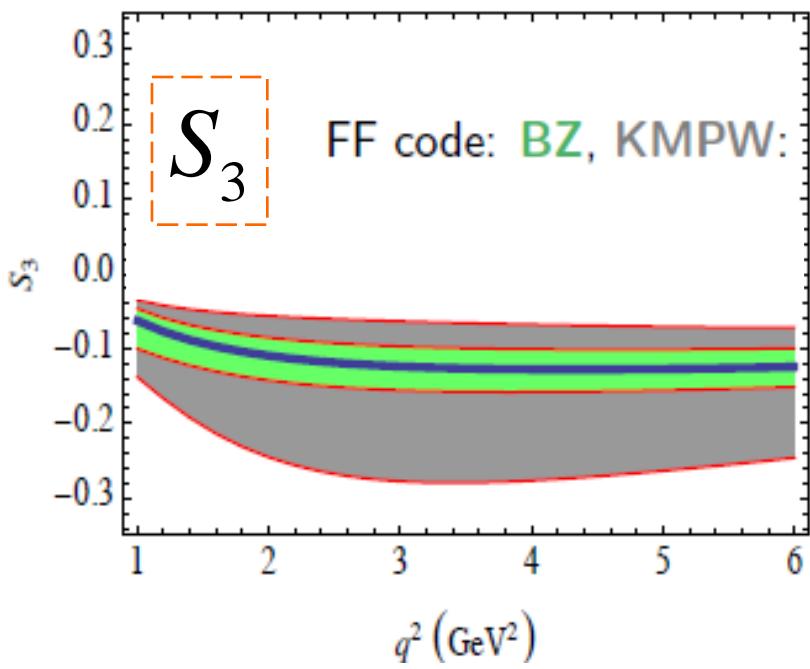
J. Matias, F.M., J. Virto & M. Ramon in '12.

F.Kruger, J.Matias '05; D.Becirevic, E. Schneider '12; C.Bobeth, G. Hiller & D. Van Dvck '12

# $b \rightarrow s$ transitions: Anomaly on $B \rightarrow K^{(*)} \mu\mu$

$F_L$  and  $S_i$  coefficients are plagued by large hadronic uncertainties.

By using appropriate normalization, we defined observables,  
 $P_i$ , theoretically clean



The green/gray bands are the hadronic uncertainties for 2 different determinations of QCD form factors

**Large hadronic uncertainties reduced: clean gain on New Physics search**

# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu + B \rightarrow K^{(*)}\mu\mu$

## SM operators

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}, O_9 = \left( \bar{b} \gamma^\mu s \right) \bar{\ell} \gamma^\mu \ell$$

$$O_{10} = \left( \bar{b} \gamma^\mu s \right) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

## BSM operators

$$O_{S(P)} = \left( \bar{b}_R s_L \right) \bar{\ell} \ell_{S(P)}, O_T = \left( \bar{b}_R \sigma^{\mu\nu} s_L \right) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

$$\Gamma(B_s^0 \rightarrow \mu^+ \mu^-) \sim \frac{G_F^2 \alpha^2}{64\pi^3} m_{Bs}^2 f_{Bs}^2 |V_{tb} V_{ts}|^2$$

$$\times \left[ \left| 2m_\mu (C_{10} - C'_{10}) + m_{Bs} (C_P - C'_P) \right|^2 + m_{Bs} \left| (C_S - C'_S) \right|^2 \right]$$

$B_s \rightarrow \mu\mu$  (**P=-1**)

2) Only contributions from axial combinations

D. Becirevic, N. Kosnik, F. M, E. Scheider '12

However, orthogonal combinations of couplings enters  $B \rightarrow K^* \mu\mu, B \rightarrow K \mu\mu$

2

$B \rightarrow K ll$  (**P=1**)

$$\langle K | \bar{b} \gamma^\mu \gamma_5 s | B_s^0 \rangle = \langle K | \bar{b} \gamma_5 s | B_s^0 \rangle = 0$$

$$\text{Br} \propto (C_9 + C'_9), (C_{10} + C'_{10}), (C_P + C'_P), (C_S + C'_S)$$

# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu + B_s \rightarrow \tau\tau$

SM operators

$$O_7 = \bar{b}_R \sigma^{\mu\nu} s_L F_{\mu\nu}, O_9 = \left( \bar{b} \gamma^\mu_L s \right) \bar{\ell} \gamma^\mu \ell$$

$$O_{10} = \left( \bar{b} \gamma^\mu_L s \right) \bar{\ell} \gamma^\mu \gamma_5 \ell$$

BSM operators

$$O_{S(P)} = \left( \bar{b}_R s_L \right) \bar{\ell} \ell_{S(P)}, O_T = \left( \bar{b}_R \sigma^{\mu\nu} s_L \right) \bar{\ell} \sigma^{\mu\nu} \ell$$

$$O'_{7,9,10,S,P} = O_{7,9,10,S,P} (L \leftrightarrow R)$$

$$\Gamma(B_s^0 \rightarrow \mu^+ \mu^-) \sim \frac{G_F^2 \alpha^2}{64\pi^3} m_{Bs}^2 f_{Bs}^2 |V_{tb} V_{ts}|^2$$

$$\times \left[ \left| 2m_\mu (C_{10} - C'_{10}) + m_{Bs} (C_P - C'_P) \right|^2 \right.$$

$$\left. + m_{Bs} \left| (C_S - C'_S) \right|^2 \right]$$

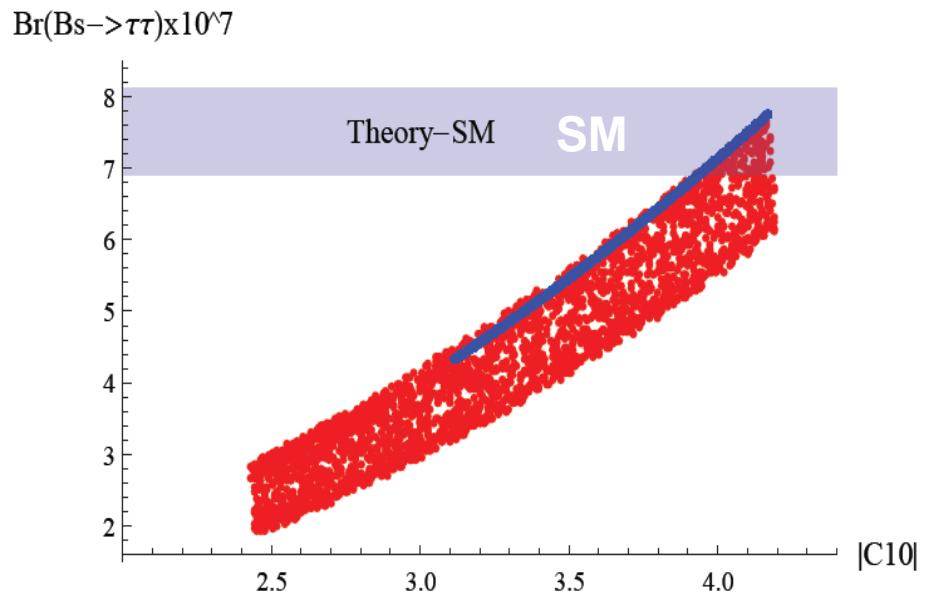
1) Helicity suppression is not fully working for  $B \rightarrow \tau\tau$



3

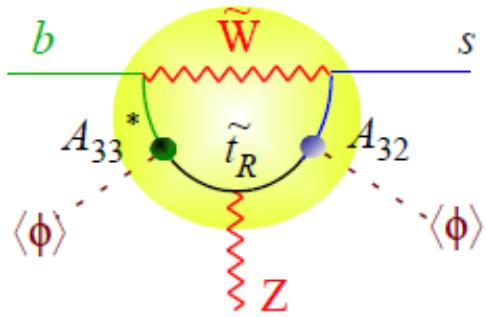
Smallish contributions to  $B \rightarrow \mu\mu$  can still give sizeable deviations of the rate for  $B \rightarrow \tau\tau$

# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu + B_s \rightarrow \tau\tau$



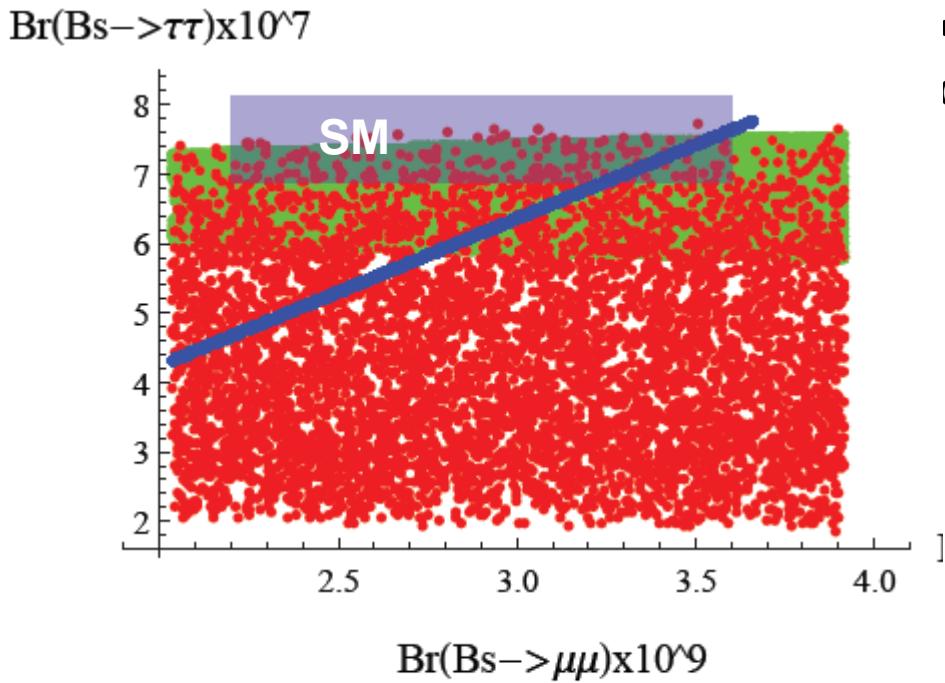
- All the points compatible with present constraints
- Blue Line with only  $C_{10}$  not-vanishing
- Red points  $C_{10}, C_S, C_P$  free

3  
Non-SM contributions to  $C_{10}$  easily expected in SUSY



LR mixing term still largely unknown  
( $m_h \sim 125$  GeV  $\rightarrow$  large  $A_{33}$ )

# $b \rightarrow s$ transitions: $B_s \rightarrow \mu\mu + B_s \rightarrow \tau\tau$



- All the points compatible with present constraints
  - Blue Line with only  $C_{10}$  not-vanishing
  - Red points  $C_{10}, C_S, C_P$  free
  - Green points  $C_S, C_P$  free and  $C_{10} = C_{10}^{SM}$

3  
 However, smallish contributions to  $B \rightarrow \mu\mu$  can still give sizeable deviations of the rate for  $B \rightarrow \tau\tau$

❖  $Br(B_s \rightarrow \mu\mu)$  is genuinely sensitive to (pseudo)scalar operators

$$O'_S = \left( \bar{b} P_{R,L} s \right) \bar{\ell} \ell, \text{ and } O_P = \left( \bar{b} P_{R,L} s \right) \bar{\ell} \gamma_5 \ell$$

⇒ Only one hadronic parameter enters,  $f_{B_s} \rightarrow \text{small th. error}$

❖  $Br(B \rightarrow K ll)$  &  $Br(B \rightarrow K^* ll)$  are sensitive to scalar + vector operators (+ tensors)

- ⇒ hadronic uncertainties -> **still large th. error**
- ⇒ With respect to  $B_s \rightarrow \mu\mu$  &  $B_s \rightarrow X_s \gamma$ , they probe the effective Hamiltonian in an “orthogonal” direction!
- ⇒ Improvement of form factors calculation would make the observables a high resolution probe of scalar operators

# Conclusions

## What about BSM effects?



- We learned a lot about Flavour physics during last years:
- Disentangling New Physics, it is mainly a question of precision and new modes
- Potential n.d.f at the TeV scale must have a rather sophisticated Flavour structure ... which we have not clearly understood yet
- Some tension emerging in several modes:  $B \rightarrow K^*$ ,  $\sin(2\beta)$  vs  $\epsilon_K$

➤ **Multiple probes! Almost all channels are sensitive at NP at well motivated levels!**

d-quarks	Probe
$s-d$	$K-K$
$b-d$	$B-B$
$b-s$	$B_s-B_s$

Higgs couplings
Rare $K$ decays
Rare $B$ decays

Leptons	Probe
$\mu-e$	muons
$\tau-e$	eEDM
$\tau-\mu$	LHC

***THANKS VERY MUCH***

$$\frac{m_{Higgs}^2}{2} = -|\mu|^2 + \dots + \delta m_H^2$$

Higgsinos

**1loop**

$$\delta m_H^2|_{stop} = -\frac{3}{8\pi^2} y_t^2 \left( \underline{m_{U_3}^2 + m_{Q_3}^2} + |A_t|^2 \right) \log \left( \frac{\Lambda}{\text{TeV}} \right)$$

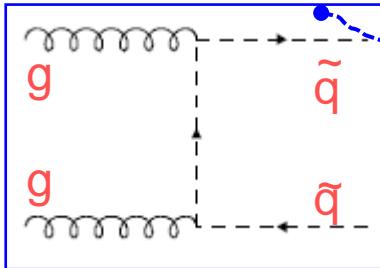
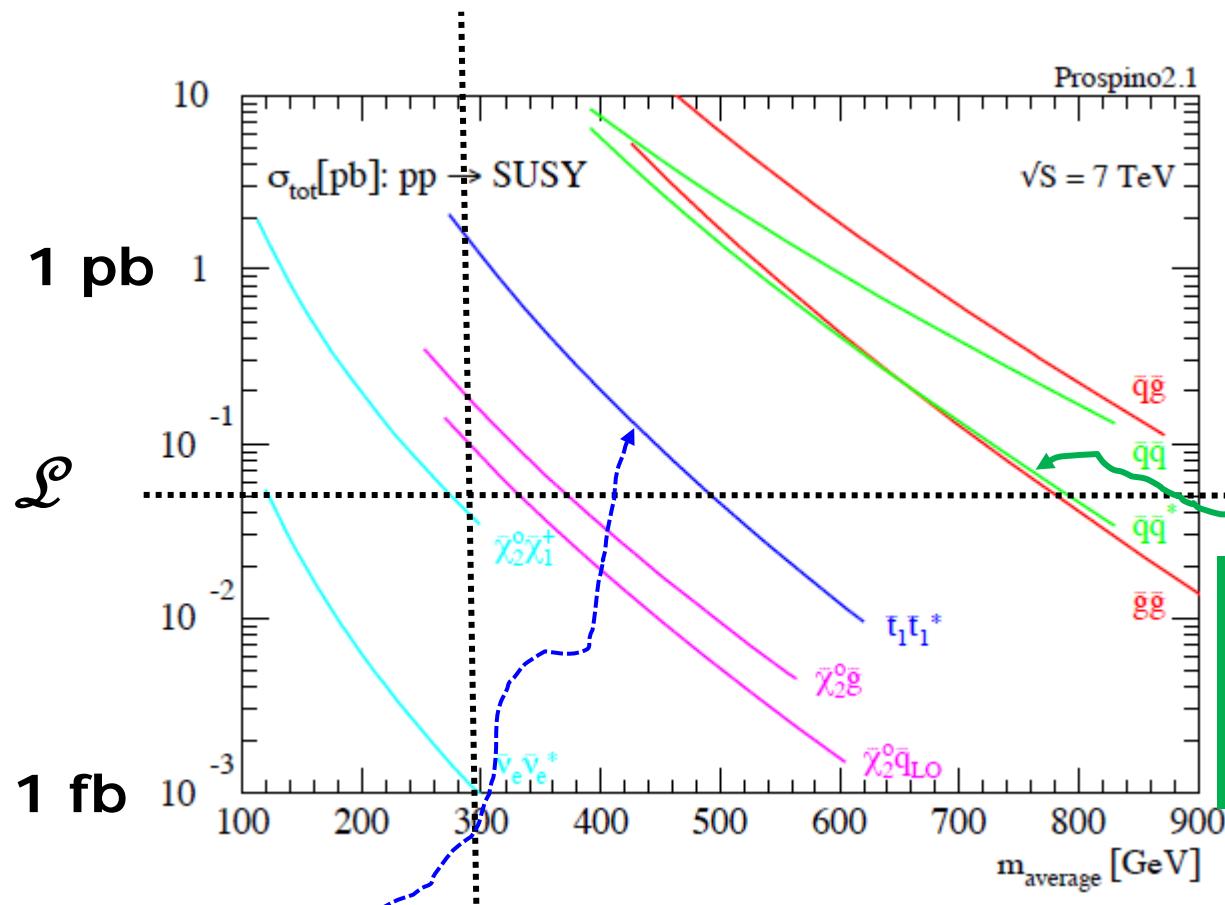
**stops, sbottom<sub>L</sub>**

**2loop**

$$\delta m_H^2|_{gluino} = -\frac{2}{\pi^2} y_t^2 \left( \underline{\frac{\alpha_s}{\pi}} \right) |M_3|^2 \log^2 \left( \frac{\Lambda}{\text{TeV}} \right)$$

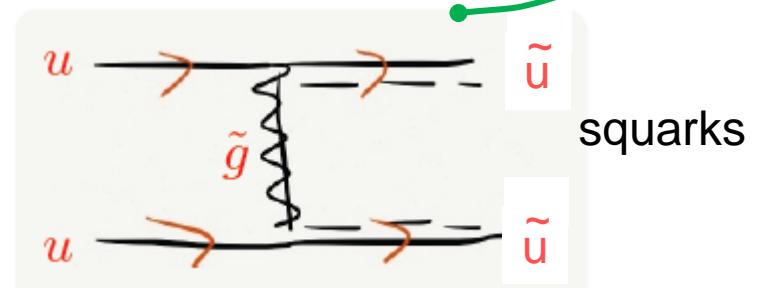
**gluino**

**Natural SUSY:**  
*no fine tuning on the Higgs mass:  
 stops, sbottom<sub>L</sub> and gluinos lights*



$\sigma \sim \text{pb} (300 \text{ GeV}/m)^6$

Flavour Independent



$$\sigma \sim (\text{TeV}/m_g)^2$$

Flavour Dependent: U/D PDF large