

# Semileptonic B decays

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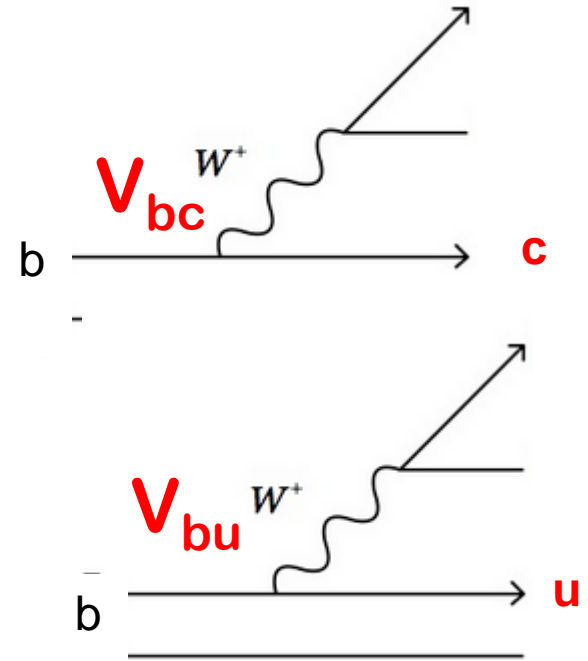
**Quark Confinement and the Hadron Spectrum XI**

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St. Petersburg

# Overview

- $b \rightarrow c \ell \nu$
- Exclusive  $B \rightarrow D^{(*)} \ell \nu$ ,
  - Inclusive  $B \rightarrow X_c \ell \nu$

- $b \rightarrow u \ell \nu$
- Exclusive  $B \rightarrow \pi (\dots) \ell \nu$ ,
  - Inclusive  $B \rightarrow X_u \ell \nu$



Most precise determination of  $|V_{ub}|$   $|V_{cb}|$

- Tension between inclusive and exclusive determinations
- Low mass open charm spectrum
- BSM when  $\ell \rightarrow \tau$

# Exclusive decays $B \rightarrow D^{(*)} \ell \nu$

$$\frac{d\Gamma}{d\omega} (B \rightarrow D^* (D)) \propto |V_{cb}|^2 (\omega^2 - 1)^{1/2 (3/2)} \mathcal{F}(\omega)^2 (G(\omega)^2)$$

$$\omega = \frac{p_{D^{(*)}} \cdot p_B}{m_B m_{D^{(*)}}}$$

Standard Step by Step

Comparison with data at a kinematically not suppressed point  $\mathcal{F}(\omega)^2 |V_{cb}|^2$

Extrapolation at zero-recoil point  $\omega=1$



dependence on  
parameterization

Perturbative and non-perturbative  $1/m_{c,b}^n$   
corrections to unity form factors (in HF limit)

↑ perturbative order:  
complete  $\alpha_s^2$  at zero  
recoil

$|V_{cb}|$  extraction

Czarnecki, Melnikov 1996-99

# $B \rightarrow D^* \ell \nu$

Generally Preferred

- ✓ less suppressed at zero recoil:  $(w^2-1)^{1/2}$  (rather than  $(w^2-1)^{3/2}$ )
- ✓ vanishing corrections order  $1/m$  (Luke's theorem)

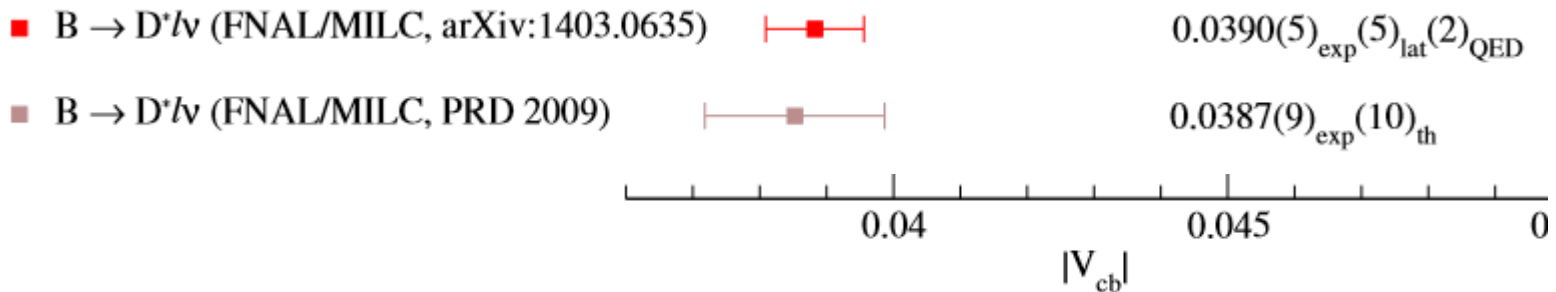
✓ Latest from Lattice

-first unquenched calculation

includes loops of sea quarks, up, down, strange  $N_f=2+1$

$$\mathcal{F}(1) = 0.906 \pm 0.004 \pm 0.012$$

Bailey et al. Fermilab/MILC 1403.0635



Bailey,  
lattice 14

Central value unchanged, total uncertainty on  $|V_{cb}|$  reduced to 1.9%;  
lattice and exp errors commensurate

# $B \rightarrow D^* \ell \nu$

✓ Important to have additional LQCD calculations

-Preliminary results ETM Nf=2 ensembles ("ratio method" to reduce errors)  
in agreement Atoui 1305.0462

-only quenched results at the non-recoil point de Divitiis et al 0707.0582  
(«step scaling» method, alternative to HQET)

✓ Comparison with most recent zero recoil sum rules

$$\mathcal{F}(1) = 0.86 \pm 0.02$$

Gambino, Mannel, Uraltsev, 1206.2296+HFAG 12  
Gambino Schwanda 1307.4551

-Slightly lower average than LQCD ( $\rightarrow$  higher  $|V_{cb}|$ )

-Much larger th error (More than twice on  $|V_{cb}|$ )

# $B \rightarrow D \ell \nu$

## ✓ Latest from Lattice

unquenched calculations at non-zero recoil full kinematic range

Qiu et al Fermilab/MILC 1312.0155

-same valence-quark actions and ensembles than  $B \rightarrow D^*$   
consistent  $|V_{cb}|$  (less precise :total uncertainty of about 5%)

-Heavy-quark discretization errors largest source of uncertainty  
work in progress to reduce it

Jang et al SWME, MILC, and Fermilab 1311.5029

## ✓ Non-lattice

heavy quark expansion (+ BPS limit)

Uraltsev 04  
+PDG 0312001

$$\mathcal{G}(1) = 1.04 \pm 0.02$$

-Consistently lower than unquenched  
-Exp+th on  $|V_{cb}|$  uncertainty comparable with LQCD

# Prospects

## ✓ Experimental progress

- high statistics at LHCb for  $B \rightarrow D^{(*)} \ell \nu$ ; however, at B factories fully reconstruction of B (or conjugate) helps measurements in presence of missing neutral particle ( $\nu$ )

- Belle II estimated error on  $|V_{cb}|$  at  $75 \text{ ab}^{-1}$  is about 1%

## ✓ Lattice attacking $B_s \rightarrow D_s \ell \nu$

- More affordable on lattice: light spectator fixed to its known mass ( $m_s$ ) and no extrapolation in the light quark mass needed

- Modification of step scaling method

Blossier et al( ETM Collab). 0909.3187

- Agreement with SR data

$$\mathcal{G}(1) = 1.052(46)$$

Atoui et al 1310.5238

✓ Extraction from baryonic decays at hadronic machines, (exp hard)

$$\Lambda_b^0 \rightarrow \Lambda_c^+ \ell^- \bar{\nu}$$

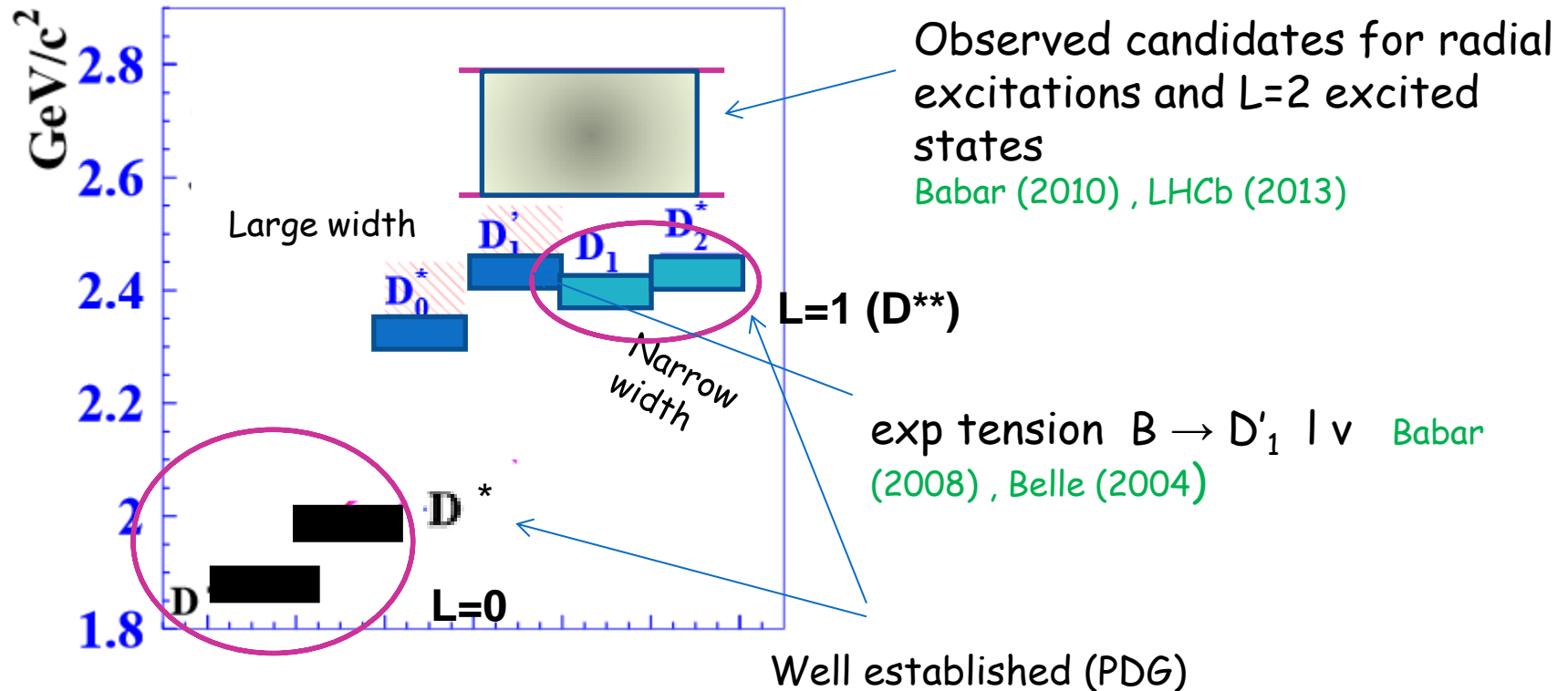
Stone and Zhang 1402.4205

# Exclusive summary

<i>Exclusive decay</i>	$ V_{cb}  \times 10^3$
<i><math>B \rightarrow D^* l \bar{\nu}</math></i>	
FNAL/MILC (Lattice unquenched 2014)	$39.04 \pm 0.49_{\text{exp}} \pm 0.53_{\text{QCD}} \pm 0.19_{\text{QED}}$
HFAG (Lattice unquenched 2012)	$39.54 \pm 0.50_{\text{exp}} \pm 0.74_{\text{th}}$
Rome (Lattice quenched $\omega \neq 1$ 2008)	$37.4 \pm 0.5_{\text{exp}} \pm 0.8_{\text{th}}$
HFAG (Sum Rules 2012)	$41.6 \pm 0.6_{\text{exp}} \pm 1.9_{\text{th}}$
<i><math>\bar{B} \rightarrow D l \bar{\nu}</math></i>	
FNAL/MILC (Lattice unquenched $\omega \neq 1$ 2013)	$38.50 \pm 1.9_{\text{exp+lat}} \pm 0.2_{\text{QED}}$
PDG (HQE + BPS 2012)	$40.6 \pm 1.5_{\text{exp}} \pm 0.8_{\text{th}}$
Rome (Lattice quenched $\omega \neq 1$ 2009)	$41.6 \pm 1.8 \pm 1.4 \pm 0.7_{FF}$



# Low mass open charm spectrum



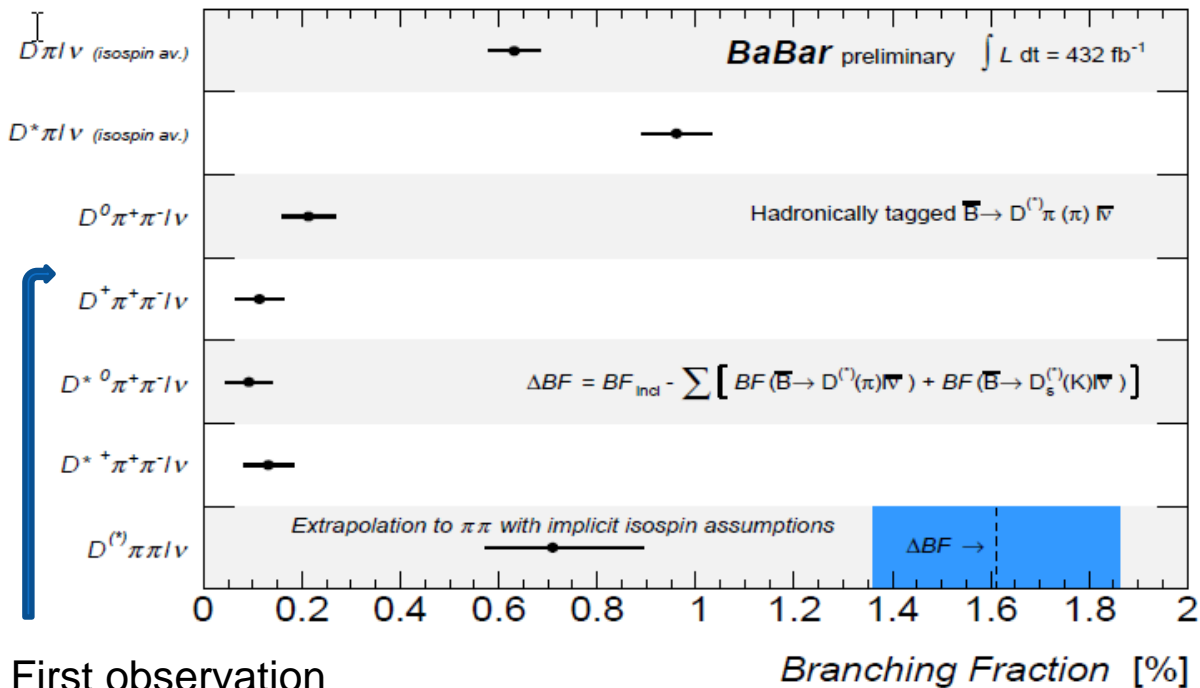
higher mass charm states background events to  $B \rightarrow D^{(*)} \ell \nu$   
 (e.g. via  $B \rightarrow D^{**} \ell \nu$ )

# Theoretical puzzles

1) BR for inclusive  $B \rightarrow X_c l \nu$  not saturated by sum of exclusive BR (gap puzzle)

- Decays into  $D^{(*)}$  make up  $\sim 70\%$  of total inclusive  $B \rightarrow X_c l \nu$  rate
- Decays into  $D^{**}$  make up  $\sim 15\%$  of total inclusive  $B \rightarrow X_c l \nu$  rate

Leaves a gap of about 15%



Closing the gap experimentally?

assigning about 0.7% to  $B \rightarrow D^{(*)} \pi \pi l \nu$  production, significance reduced from  $7\sigma$  to  $3\sigma$ .

In the HQ limit  $j_l = L \otimes s_l$

P-wave mesons can be grouped into two doublets:

$j_l=1/2$

strongly decays only through S-waves  $\rightarrow$  broad states

$j_l=3/2$

strongly decays only through D-waves  $\rightarrow$  narrow states

2) narrow width dominates over large width states (sum rules + HQ, quark models)

*Le Yaouanc et al 96, Uraltsev 2001, Morenas et al. 1997, Ebert et al. 1998, Leibovich et al. 2007, Bigi et al. 2007....)*

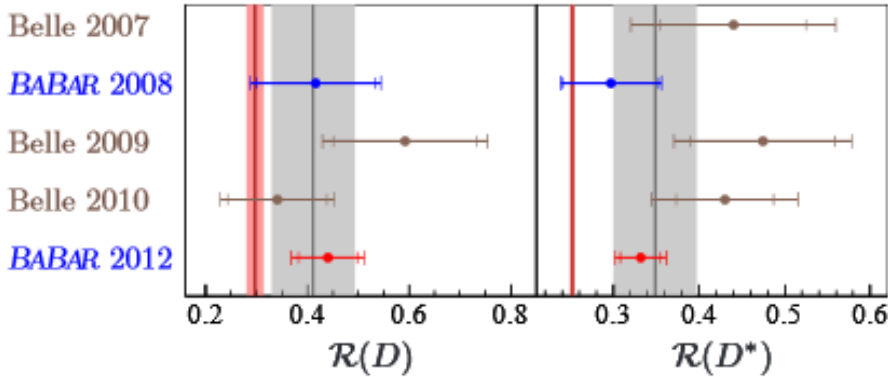
not confirmed by data (1/2 vs 3/2 puzzle)

*Belle, Babar 06*

- ✓ Relevance of the infinite mass limit approach in  $b \rightarrow c$  decay
- ✓ Background for  $|V_{ub}|$

# B → D<sup>(\*)</sup> τ ν<sub>τ</sub>

B factories



$$\mathcal{R}_{\tau/l}^* \equiv \frac{\mathcal{B}(B \rightarrow D^* \tau \nu)}{\mathcal{B}(B \rightarrow D^* l \nu)} = 0.332 \pm 0.024 \pm 0.018$$

$$\mathcal{R}_{\tau/l} \equiv \frac{\mathcal{B}(B \rightarrow D \tau \nu)}{\mathcal{B}(B \rightarrow D l \nu)} = 0.440 \pm 0.058 \pm 0.018$$

Babar 2012 1205.5442

$$\mathcal{R}_{\tau/l}(SM) = 0.297 \pm 0.017 \quad \mathbf{2.7\sigma}$$

Combined **3.4σ**

$$\mathcal{R}_{\tau/l}^*(SM) = 0.252 \pm 0.003 \quad \mathbf{2.0\sigma}$$

✓ Agreement with Belle sample 657 × 10<sup>6</sup> B pair events

Belle 0910.4301.

✓ NP breaking of lepton-flavour universality?

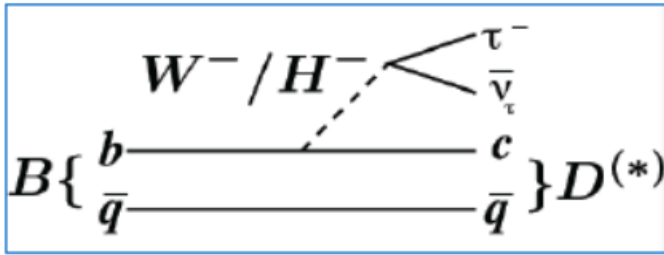
compare with B → τ ν<sub>τ</sub>

Previous disagreement with SM; now (with full Belle data set) consistency

Belle 1208.4678

Awaiting for Belle update with full data set (772 × 10<sup>6</sup> B pairs)

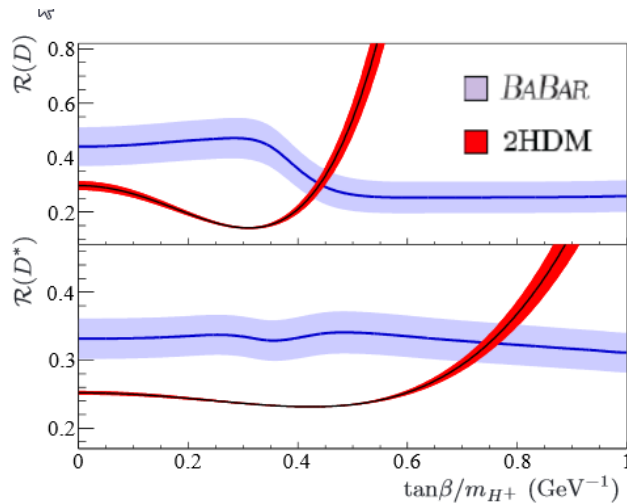
# New charged Higgs?



2HDM:

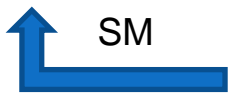
Type I: only one Higgs doublet couples to fermions

Type II: one Higgs couples to up-type fermions and the other to down-type quarks (MSSM)



- ✓ Excludes type II 2HDM charged Higgs boson with 99.8% CL ( $m_{H^+} > 10$  GeV) (Region with  $m_{H^+} < 10$  GeV already excluded by  $B \rightarrow Xs \gamma$  measurements)

Misiak 0609232



Babar 2012 1205.5442

# Inclusive decays $B \rightarrow X_c l \nu$

$$\Gamma(B \rightarrow X_q l \nu) = \frac{G_F^2 m_b^5}{192\pi^3} |V_{qb}|^2 \left[ c_3 \langle O_3 \rangle + c_5 \frac{\langle O_5 \rangle}{m_b^2} + c_6 \frac{\langle O_6 \rangle}{m_b^3} + O\left(\frac{1}{m_b^4}\right) \right]$$

OPE factorization of short and long distance dynamics

- ✓ Scheme dependence (quark mass definition: 1S, kinetic, etc.)
- ✓ Kinetic scheme
  - Complete  $O(\alpha_s^2)$  corrections to leading term (parton model)+BLM terms  $\alpha_s^{n+1} \beta_0^n$   
[Melnikov, Czarnecki, Pak, Biswas, Gambino, ...]
  - Complete  $\alpha_s \frac{\Lambda^2}{mb^2}$  [Becher, Boos, Lunghi, Alberti, Ewerth, Gambino, Nandi, ...]
  - $O(1/m_b^{2,3})$  known,  $O(\Lambda/m_b^{4,5})$  estimated  
[Gremm, Kapustin, Dassinger, Turczyk, Mannel, Gambino, Bigi, Uraltsev, Zwicky ...]
  - $\log mc, 1/mc^2$  ... intrinsic charm estimates  
[Breidenbach, Feldmann, Mannel, Turczyk, Bigi, Mannel, Uraltsev, ...]
- Threshold resumming (double Sudakov-like logs) not relevant (cut off by the mc mass)  
Di Giustino, GR, Trentadue 11, ..

# Global fit results

width + hadron, lepton momenta: about 70 measurements available (80% from B factories)

Additional constraint to increase precision estimate in  $m_b$   
 photon energy moments in  $B \rightarrow X_s \gamma$ , or a precise constraint on  $m_c$

Constraint	$ V_{cb}  (10^{-3})$
$B \rightarrow X_s \gamma$	$41.94 \pm 0.43_{\text{fit}} \pm 0.59_{\text{th}}$
$m_c^{\overline{\text{MS}}}(3 \text{ GeV})$	$41.88 \pm 0.44_{\text{fit}} \pm 0.59_{\text{th}}$

kinetic scheme **HFAG 12**  $\frac{\delta V_{cb}}{V_{cb}} < 2\%$

to compare with excl  $\sim 2\%$

Latest global fits in kinetic scheme (mc constraint)

$$|V_{cb}| = (42.42 \pm 0.86) \times 10^{-3}$$

Gambino Schwanda 2014

Including  $\alpha_s/m_b^2$ : error decreases

$$|V_{cb}|_{\text{inc}} = (42.42 \pm 0.81) \times 10^{-3}$$

Healey ICHEP 2014

Incorporating  $\alpha_s/m_b^3$  in progress

# $|V_{cb}|$ summary

<i>Exclusive decay</i>	$ V_{cb}  \times 10^3$
<i><math>B \rightarrow D^* l \bar{\nu}</math></i>	
FNAL/MILC (Lattice unquenched 2014)	$39.04 \pm 0.49_{\text{exp}} \pm 0.53_{\text{QCD}} \pm 0.19_{\text{QED}}$
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<i>Inclusive decays</i>	
HFAG ( $B_s \rightarrow X_s \gamma$ constraint)	$41.94 \pm 0.43_{\text{fit}} \pm 0.59_{\text{th}}$
HFAG ( $m_c$ constraint)	$41.88 \pm 0.44_{\text{fit}} \pm 0.59_{\text{th}}$
Gambino, Schwanda 2014	$42.42 \pm 0.86$

3 $\sigma$  disagreement

Future:

- ❑ CLEO  $\rightarrow$   $\approx$ 50-70 more stat B factories  $\rightarrow$   $\approx$ 50 more stat Belle II
- ❑ LHCb: about 5 million  $B \rightarrow D^* \mu \nu$  decay no prospects for  $|V_{cb}|$  measurement



# $|V_{ub}|$ exclusive determination

- Traditionally extracted by the decay  $B \rightarrow \pi \ell \nu$   
(only a single form factor in massless limit)

$$\frac{d\Gamma(\bar{B}^0 \rightarrow \pi^+ \ell \bar{\nu})}{dq^2} = \frac{G_F^2 |\vec{p}_\pi|^3}{24\pi^3} |V_{ub}|^2 |f_+(q^2)|^2 \quad \langle \pi^+(p) | \bar{u} \gamma_\mu b | \bar{B}^0(p+q) \rangle = f_+(q^2) (2p_\mu + q_\mu)$$

Non-pert th predictions for  $f_+$  usually confined to regions of  $q^2$

## Complementarity

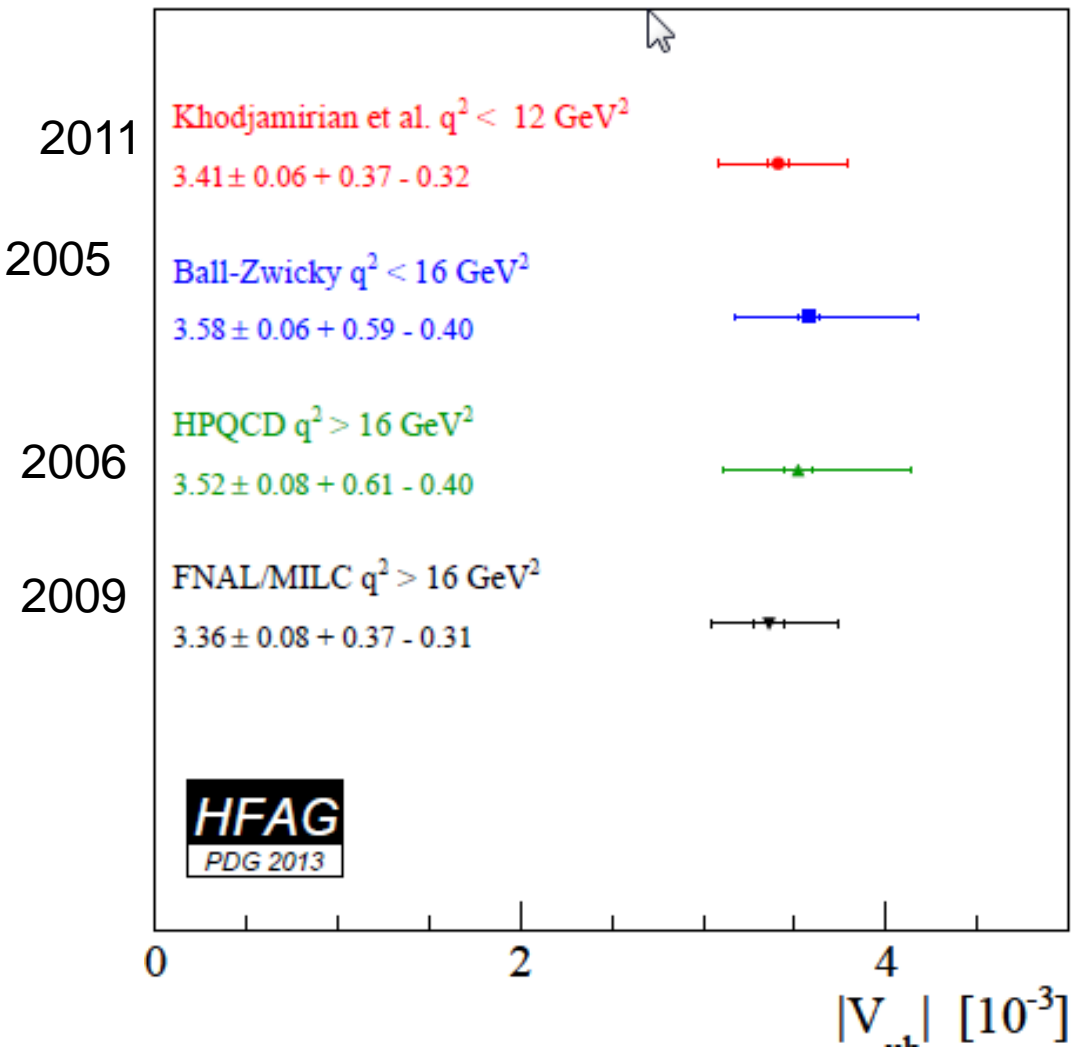
- ✓ Light Cone Sum Rules LCSR **low  $q^2$  regions  $\sim < 16 \text{ GeV}$**   
(OPE near the light-cone)

LCSR Khodjamirian et al 11, BGL: Boyd, Grinstein, Lebed, ...

- ✓ Lattice **large  $q^2 \sim > 16 \text{ GeV}$**  (to avoid large discretization errors)  
Better fit with data

[Unquenched HPQCD 07, FNAL/MILC 09, ma preliminary from ALPHA, HPQCD, FNAL/MILC, RBC/UKQCD 2012]

# $|V_{ub}|$ HFAG exclusive determination



also

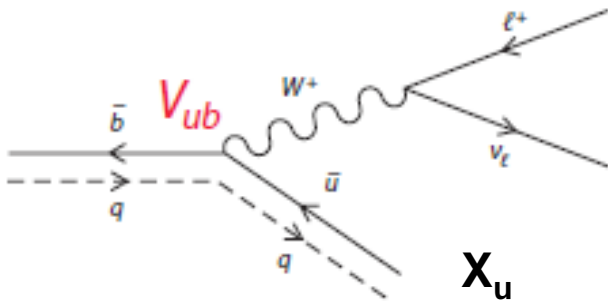
simultaneous fit of the BCL parameterization to data and LQCD calculations (all  $q^2$  range)

$$|V_{ub}| = (3.28 \pm 0.29) \times 10^{-3}$$

# new players

$X_w$	Theory	$q^2$ GeV/ $c^2$	$ V_{ub} $ $10^{-3}$
$\pi_0$	LCSR [33]	$< 12$	$3.35 \pm 0.23 \pm 0.09^{+0.36}_{-0.31}$
	LCSR [34]	$< 16$	$3.63 \pm 0.20 \pm 0.10^{+0.60}_{-0.40}$
	HPQCD [35]	$> 16$	$3.44 \pm 0.31 \pm 0.09^{+0.59}_{-0.39}$
	FNAL [36]	$> 16$	$3.29 \pm 0.30 \pm 0.09^{+0.37}_{-0.30}$
$\pi^+$	LCSR [33]	$< 12$	$3.40 \pm 0.13 \pm 0.09^{+0.37}_{-0.32}$
	LCSR [34]	$< 16$	$3.58 \pm 0.12 \pm 0.09^{+0.59}_{-0.39}$
	HPQCD [35]	$> 16$	$3.81 \pm 0.22 \pm 0.10^{+0.66}_{-0.43}$
	FNAL [36]	$> 16$	$3.64 \pm 0.21 \pm 0.09^{+0.40}_{-0.33}$
$\rho_0$	LCSR [24]	$< 16$	$3.56 \pm 0.11 \pm 0.09^{+0.54}_{-0.37}$
	BM [37]		$3.76 \pm 0.11 \pm 0.10^{+0.31}_{-0.25}$
	UKQCD [38]	full range	$3.68 \pm 0.10 \pm 0.10^{+0.29}_{-0.34}$
	ISGW2 [25]		$3.98 \pm 0.11 \pm 0.10$
$\rho^+$	LCSR [24]	$< 16$	$3.51 \pm 0.16 \pm 0.13^{+0.53}_{-0.36}$
	BM [37]		$3.66 \pm 0.15 \pm 0.14^{+0.30}_{-0.24}$
	UKQCD [38]	full range	$3.59 \pm 0.15 \pm 0.13^{+0.28}_{-0.33}$
	ISGW2 [25]		$3.87 \pm 0.16 \pm 0.15$
$\omega$	LCSR [24]	$< 12$	$3.08 \pm 0.29 \pm 0.11^{+0.44}_{-0.31}$
	ISGW2 [25]	full range	$3.03 \pm 0.23 \pm 0.11$

# Inclusive $|V_{ub}|$



large  $b \rightarrow c$  background ( $|V_{cb}/V_{ub}|^2 \approx 100$ )

Need experimental phase space cuts to reduce background;  
in general

$$m_X \ll E_X$$

Phase space regions where OPE fails become dominant; new  
unwelcome effects (with respect to semileptonic  $b \rightarrow c$ ):

- Final gluon radiation strongly inhibited: soft and collinear singularities
- perturbative expansion of spectra affected by large logarithms

$$\alpha_s^n \log^{2n}(2 E_X/m_X)$$

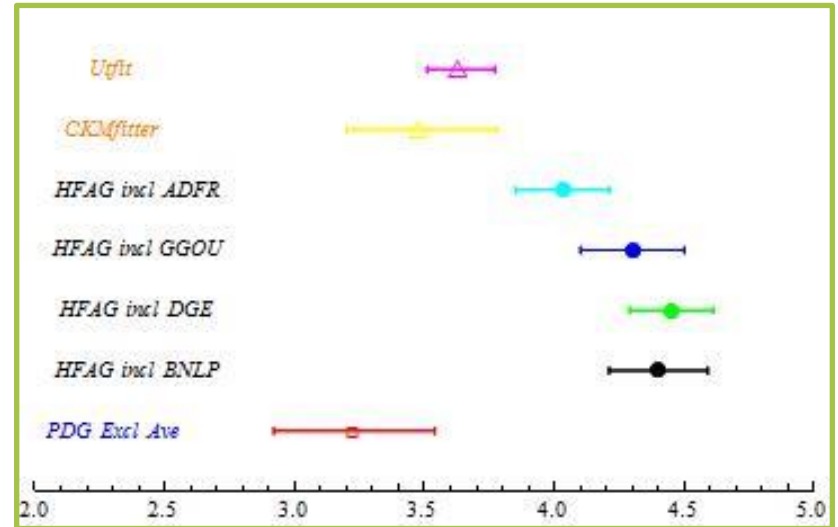
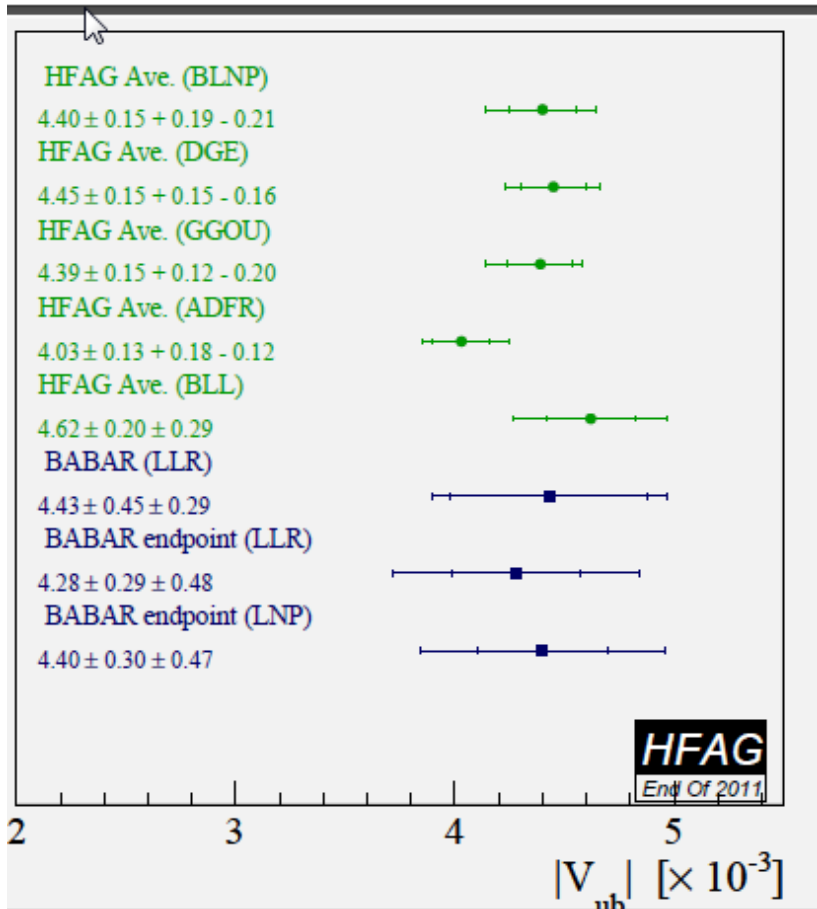
to be resummed at all orders in PT

- non-perturbative effects related to a small vibration of the  $b$  quark in the  $B$  meson (Fermi motion) enhanced

- Experimental progress
  - Belle & Babar results access 90% data
  
- Theoretical approaches (HAFG averages)
  - predictions based on parameterizations of shape function, and OPE constraints
    - Bosch, Lange, Neubert , Paz, Gambino, Giordano, Ossola, Uraltsev , ...
  - predictions based on resummed pQCD
    - Andersen, Gardi, Aglietti, Di Lodovico, Ferrera , GR
  - global fit of shape function,  $|V_{ub}|$  and  $m_b$ 
    - Tackmann, Lacker, Ligeti, Stewart...

# Results averages: Long lasting puzzle

Inclusive



Space for NP reducing (?)  
Pokorski Crivellin 1407.1320

At SuperFlavour factories ( $75 \text{ ab}^{-1}$ ) errors expected to reduce to 3% (excl) 2% (incl)

# Conclusions

Semileptonic B decays on a well deserved podium to extract CKM matrix elements and to validate theoretical tools

Long standing  $|V_{ub}|$   $|V_{cb}|$  discrepancy between exclusive, inclusive

Encouraging and impressive recent experimental progresses (LHCb now and Belle II from 2016 joining the arena)

---- We need th updates (Lattice , inclusive  $b \rightarrow u$ )