

# Dynamical Chiral Polarization in QCD Dirac Spectrum

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# *Large View*

- Develop model-independent approaches to the structure of strongly coupled vacuum/thermal states
- Based on Lattice QCD equilibrium configurations  
bottom-up approach ([hep-lat/0605008](#))
- Gauge invariant
- Apply it to the associated phase structure (finite temperature and quantum transitions)
- Use non-standard (non-Pearson) correlations for this purpose  
= dynamics

# *Small View (this talk)*

- Local chiral properties: correlation coefficient of polarization

[arXiv:1405.2968]

- Focus on Dirac (overlap) modes

[arXiv:1210.7849]

[arXiv:1009.4451]

## Plan:

- (1) Dynamical polarization and local chirality
- (2) Overview and **Chiral Symmetry Breaking–Chiral Polarization conjecture**
- (3) Anomalous mode behavior in thermal pure glue SU(3)  
(SChSB without confinement)

- (4) **Anomalous mode behavior in  $N_f=12$  !**

Anomalous = non-monotonic  
mode density +

# SAMPLE POLARIZATION AS CORRELATION

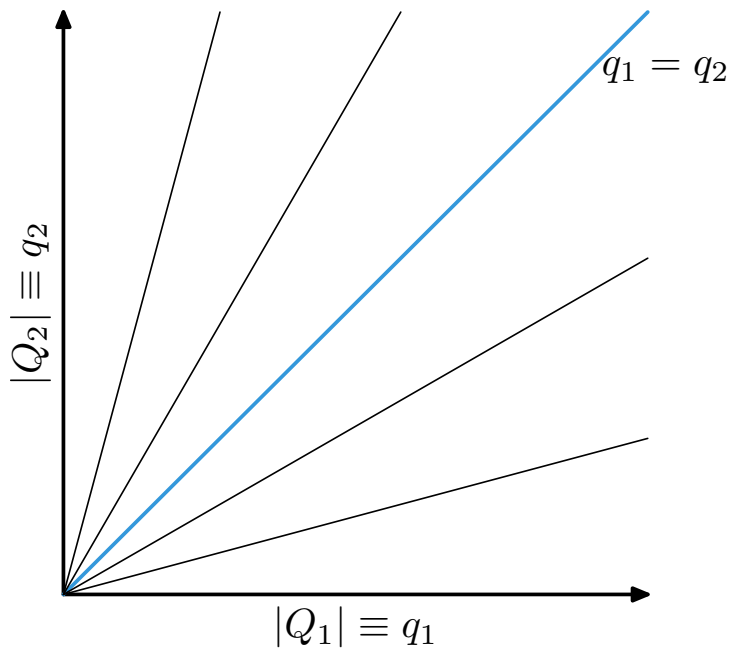
Simplest:

$$\mathcal{P}(Q_1, Q_2)$$

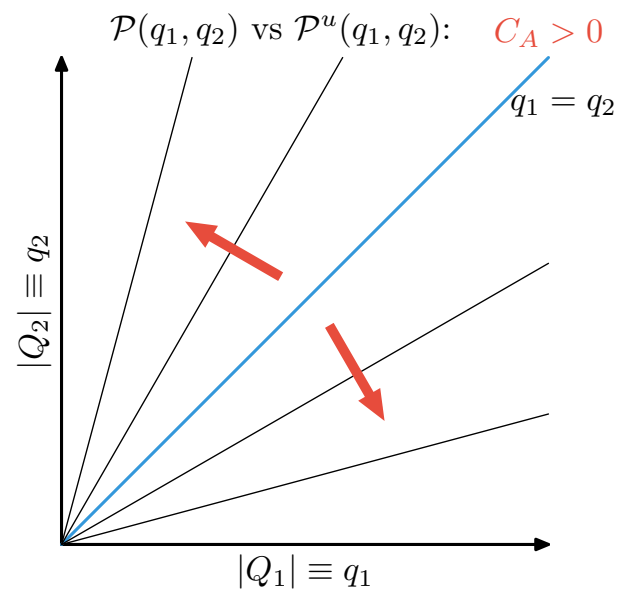
$$Q = Q_1 + Q_2$$

$$Q_1 \cdot Q_2 = 0$$

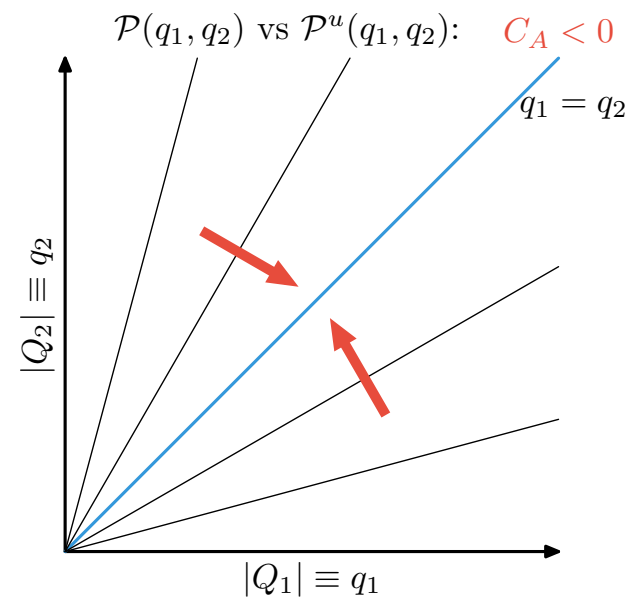
chiral components, dual components etc



Non-Pearson definition necessary  
to describe sample polarization  
as correlation!



correlation



anti-correlation

$C_A$  is uniquely defined!

# CHIRAL POLARIZATION OF DIRAC MODES (few points)

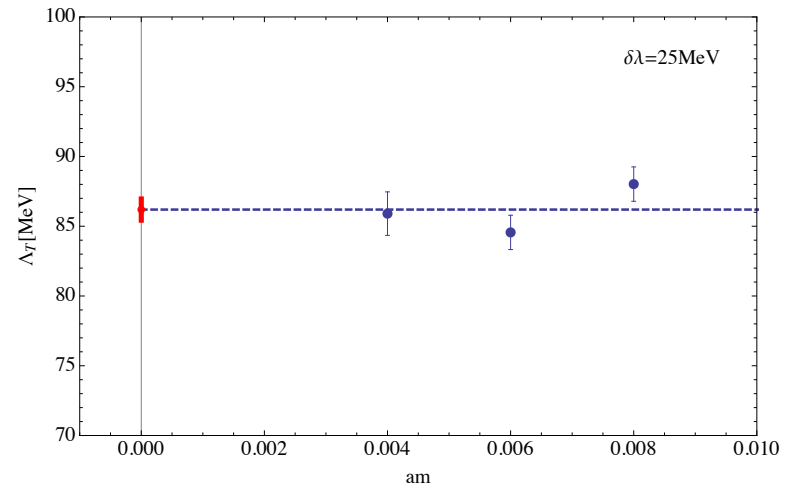
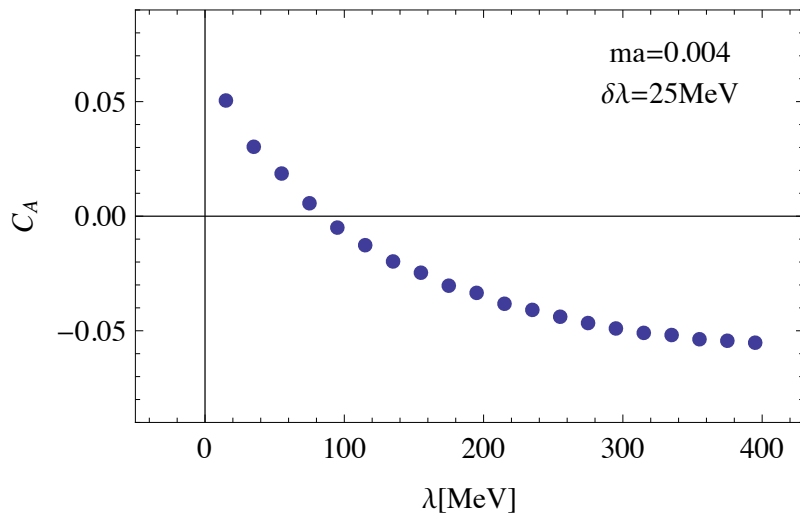
$$Q = Q_1 + Q_2 \quad \longrightarrow \quad \psi = \psi_L + \psi_R$$

Apply to a given Dirac mode:

$$Q \cdot Q \quad \longrightarrow \quad \psi^+ \psi$$

- $N_f=2+1$  QCD, Domain Wall Fermions (RBC)
- $a = 0.085$  fm ,  $V = 32^3 \times 64$ , lightest  $m_\pi \approx 295$  MeV

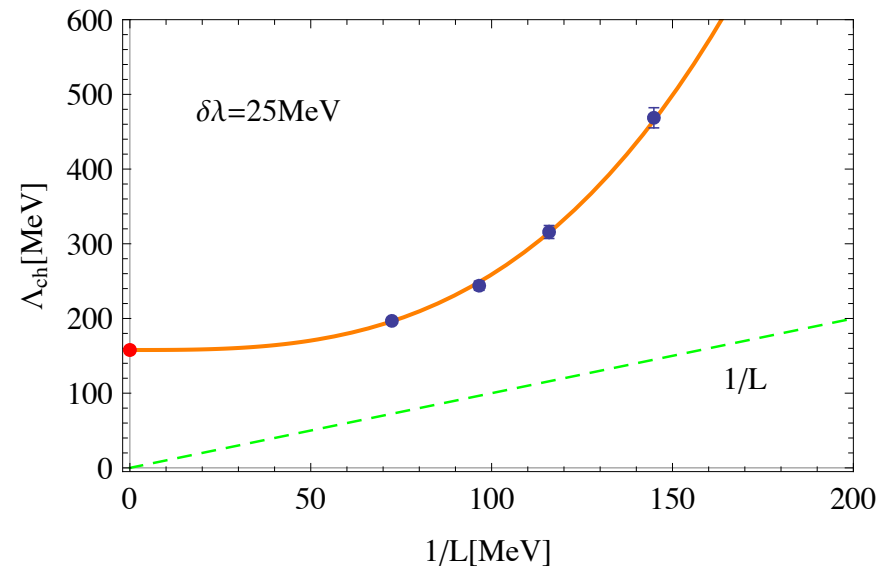
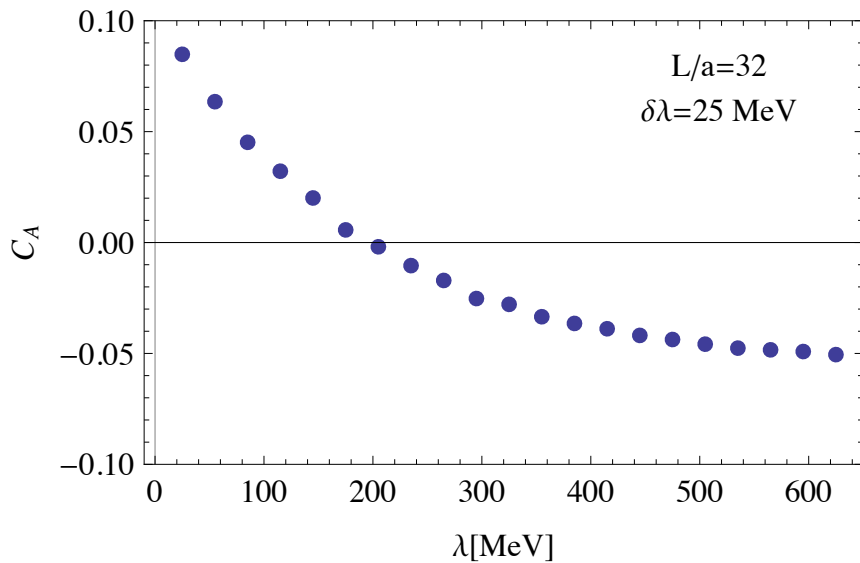
[arXiv:1210.7849]



Low Dirac spectrum of “real world” QCD is chirally polarized!

# Chiral Polarization...

- $N_f=0$  QCD, Wilson action,  $a=0.085$  fm ( $r_0$ ) [\[arXiv:1210.7849\]](#)



$\Lambda_{\text{ch}}$  is a dynamical scale distinct from infrared cutoff!

# *vSChSB-Chiral Polarization Correspondence*

[arXiv:1210.7849]

$\langle \bar{\eta}\eta \rangle > 0$	$\langle \bar{\eta}\eta \rangle = 0$
$C_A[\eta] > 0$	$C_A[\eta] \leq 0$
$\Omega > 0$	$\Omega = 0$
$\rho_{ch}(0) > 0$	$\rho_{ch}(0) = 0$

$\mathcal{T}$

$\mathcal{T}$  = SU(3) theories, arbitrary fundamental  $N_f$ , masses, temperature

$\eta$  = massless valence field

$\Omega$  = cumulative correlation

$\rho_{ch}$  = spectral chirality density

symmetry breaking  $\iff$  local NP correlation

Fixed quark masses and  $N_f$ : defines temperature  $T_{ch}$

Massless quarks and  $T=0$  : defines critical flavors  $N_{f,cr}$

*Here: Existence of anomalous phase in  $N_f=12$  at low mass!* [arXiv:1405.2968]



# vSChSB-ChP: the Instruments

◆ For valence Spontaneous Chiral Symmetry Breaking (vSChSB) :

use  $\rho(\lambda \rightarrow 0)$

$$\lim_{m_v \rightarrow 0} \lim_{V \rightarrow \infty} \langle \bar{\eta} \eta \rangle_V \neq 0 \iff \lim_{\lambda \rightarrow 0} \lim_{V \rightarrow \infty} \rho(\lambda, V) > 0$$

Banks, Casher, 1980

vSChSB  $\iff$  mode condensation

◆ For dynamical Chiral Polarization (ChP) :

use  $\Omega$

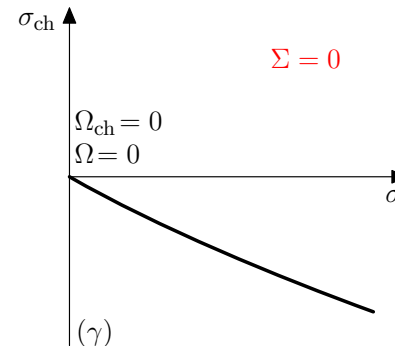
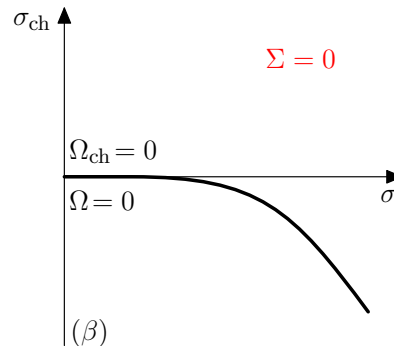
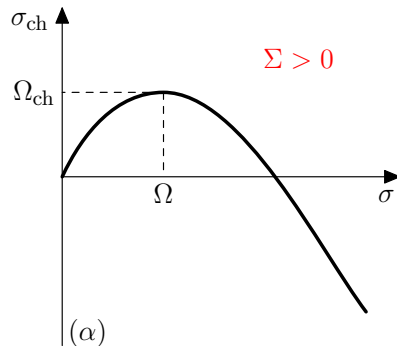
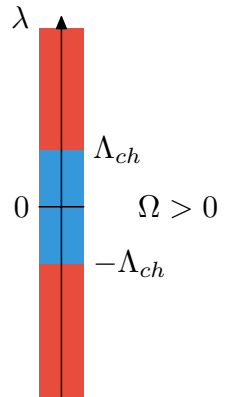
$$\sigma_{ch}(\lambda, V) \equiv \frac{1}{V} \left\langle \sum_{0 \leq \lambda_k < \lambda} C_{A,k} \right\rangle_V$$

$$\sigma(\lambda, V) \equiv \frac{1}{V} \left\langle \sum_{0 \leq \lambda_k < \lambda} 1 \right\rangle_V$$

Eliminate  $\lambda$  in favor of  $\sigma$

$\implies$

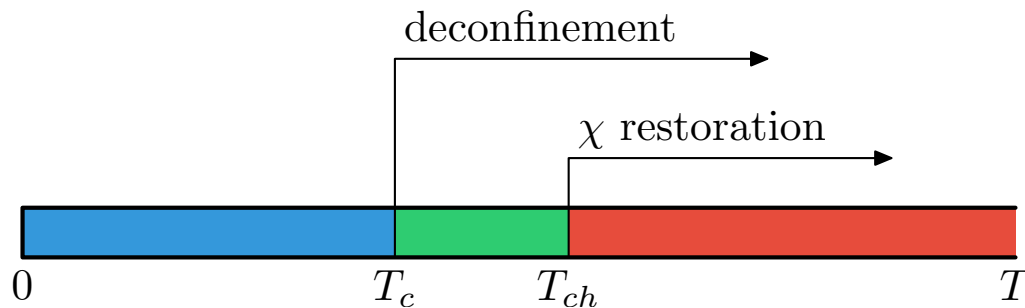
$$\sigma_{ch} = \sigma_{ch}(\sigma)$$



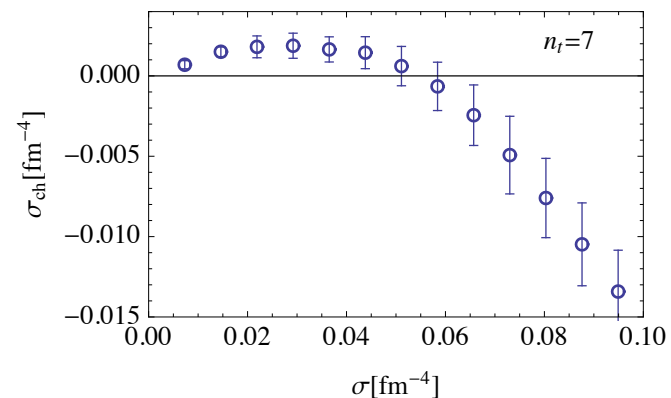
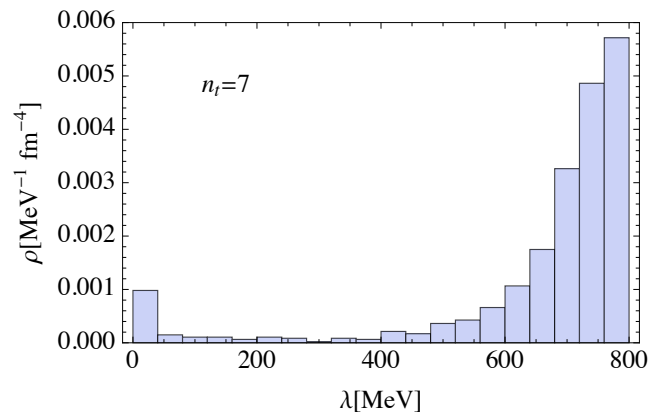
# Anomalous Phase $T_c < T < T_{ch}$ in $N_f=0$

Edwards, Heller, Kiskis, Narayanan, 1999

“real Polyakov line” vacuum



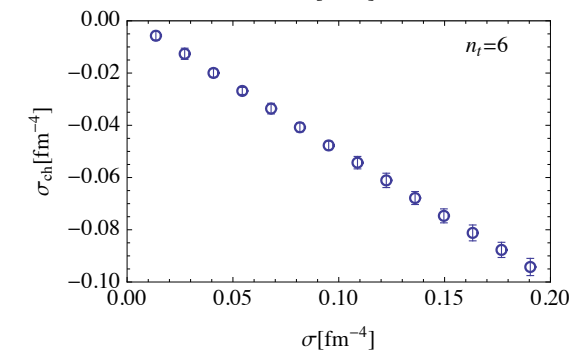
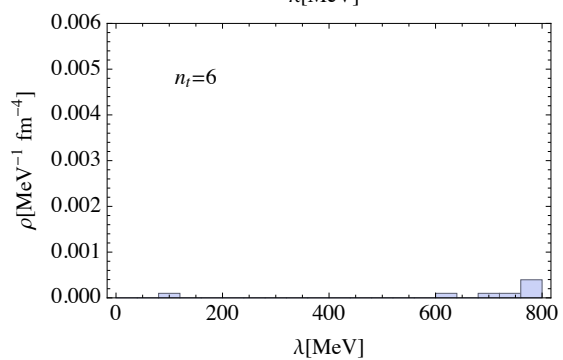
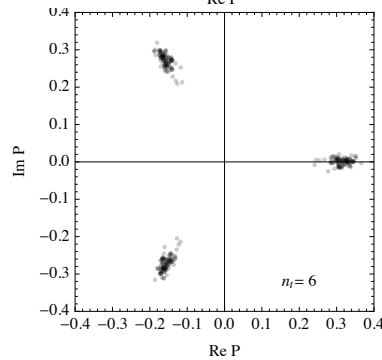
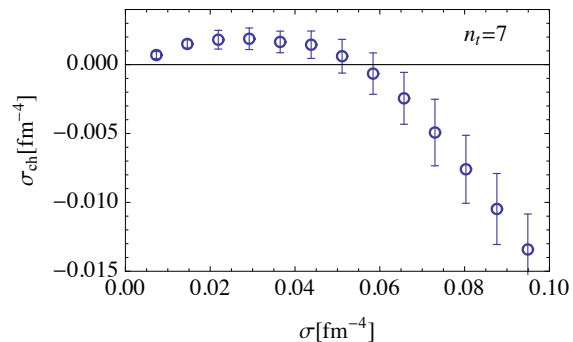
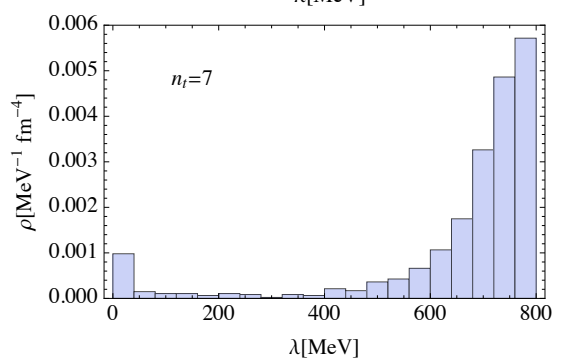
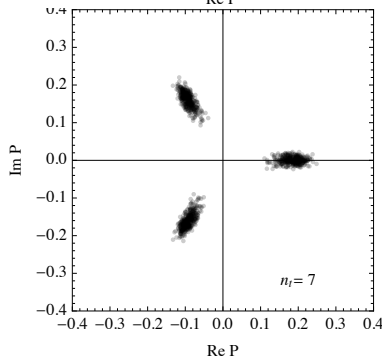
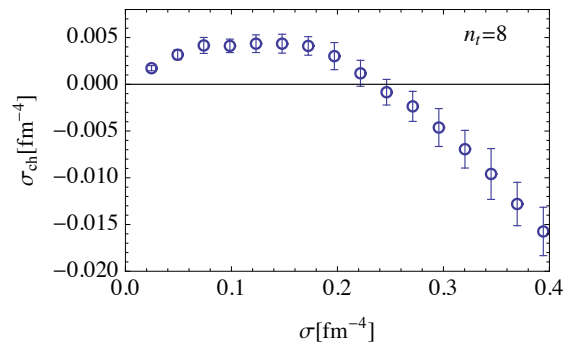
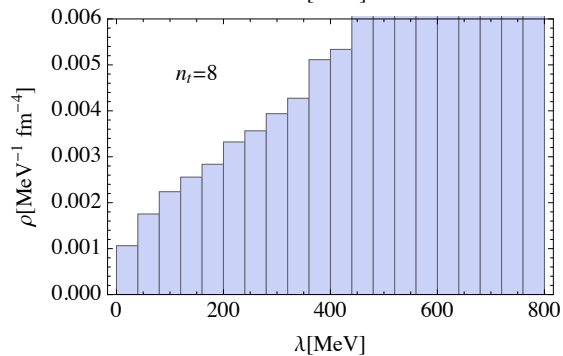
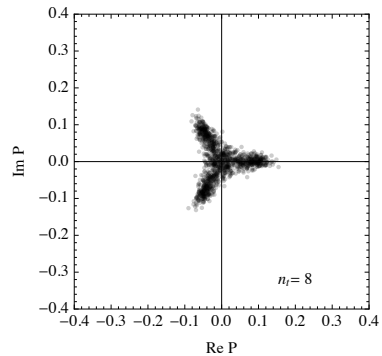
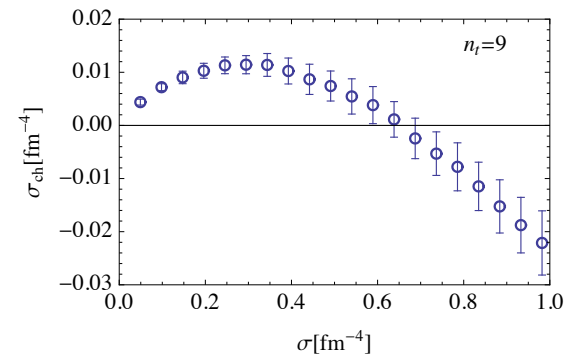
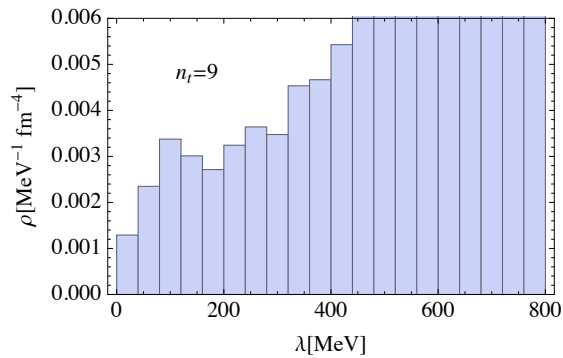
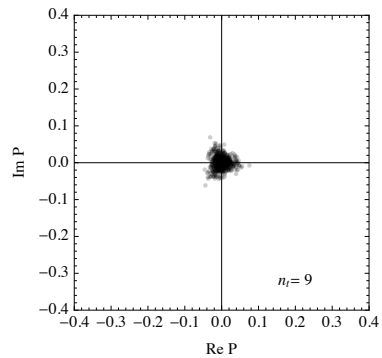
Qualitatively:



“anomalous” vSchSB

chirally polarized

[arXiv:1210.7849]



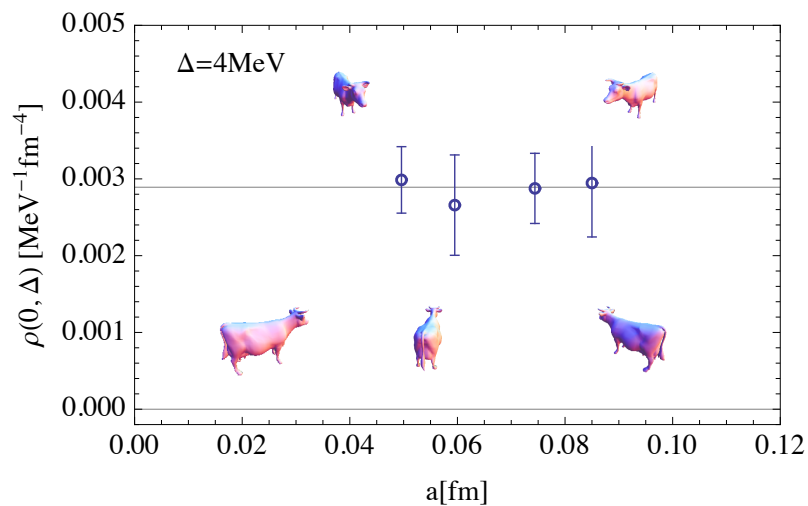
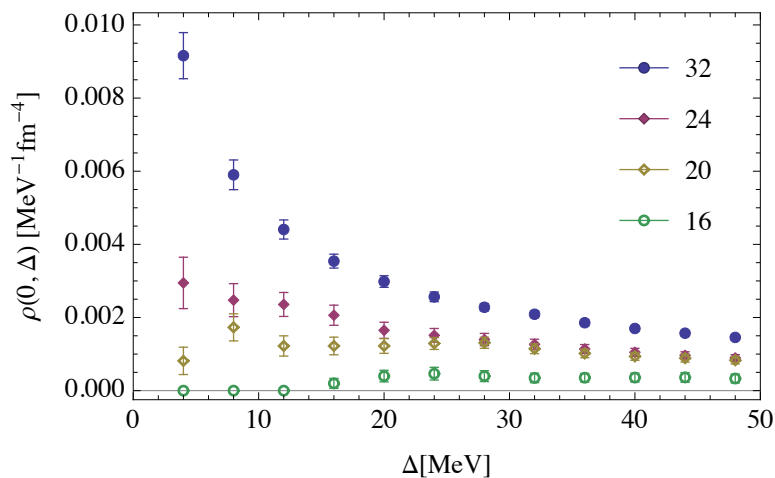
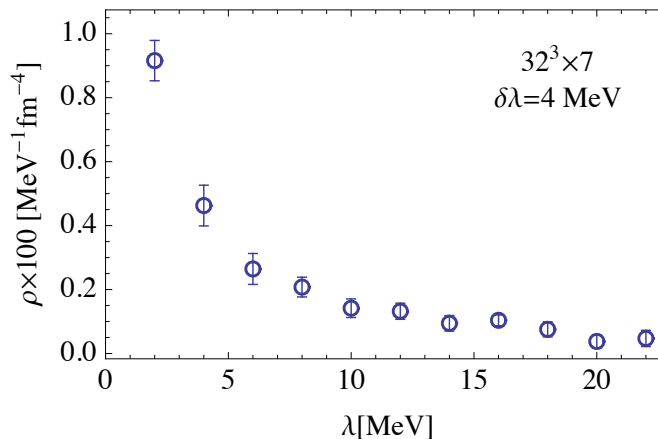
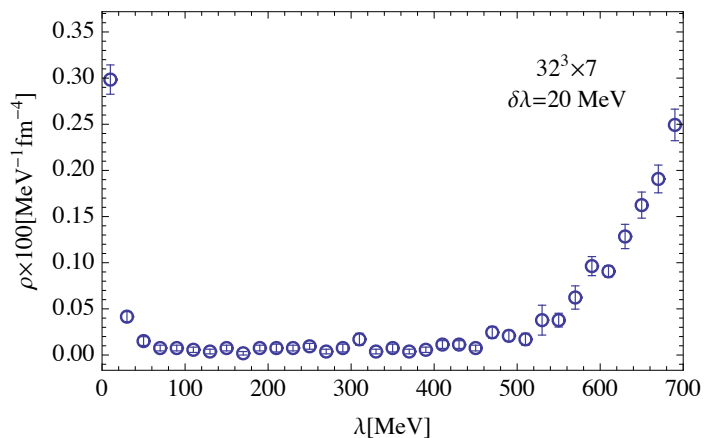
# Anomalous phase in $N_f=0$ is real!

[arXiv:1405.2968]

IH and A. Alexandru, talk, Lattice '14

A. Alexandru, IH, in preparation

$N^3 \times 7$  system at  $\beta=6.054$ ,  $a=0.085$  fm



$$V_3 = (2 \text{ fm})^3, T/T_c = 1.12$$

## *Anomalous Phase $m_{ch} < m < m_c$ in $N_f=12$ ?*

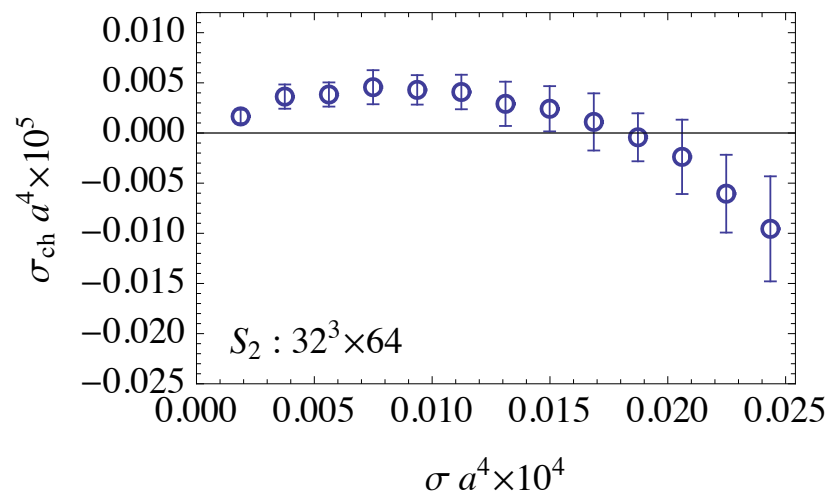
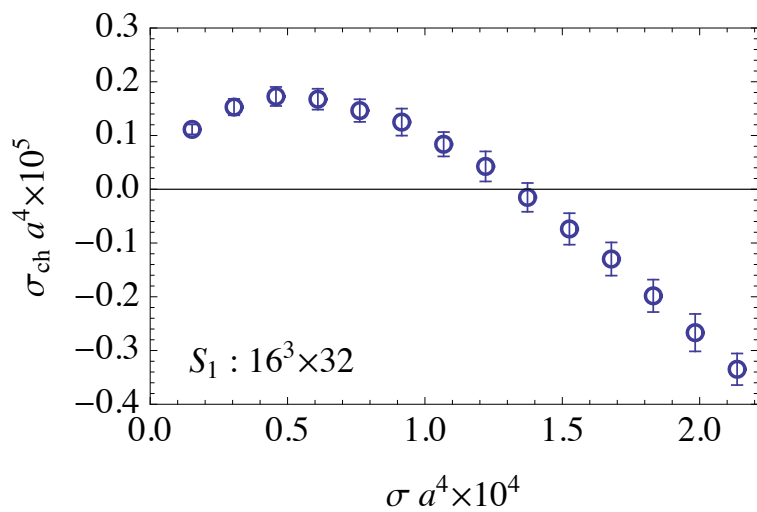
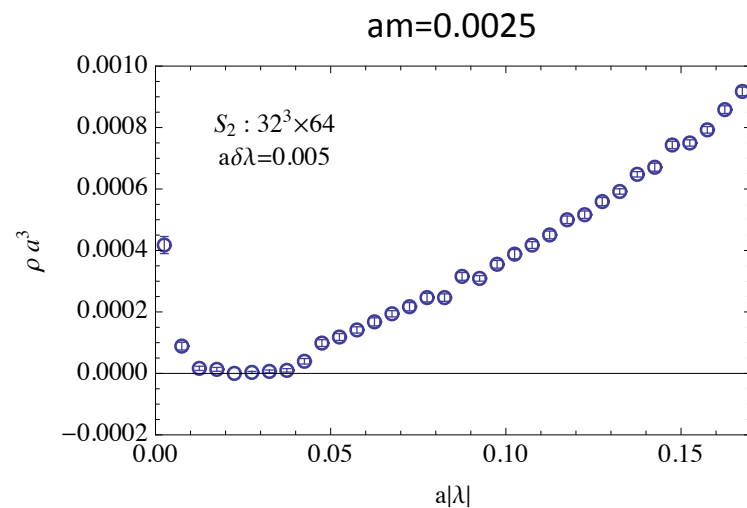
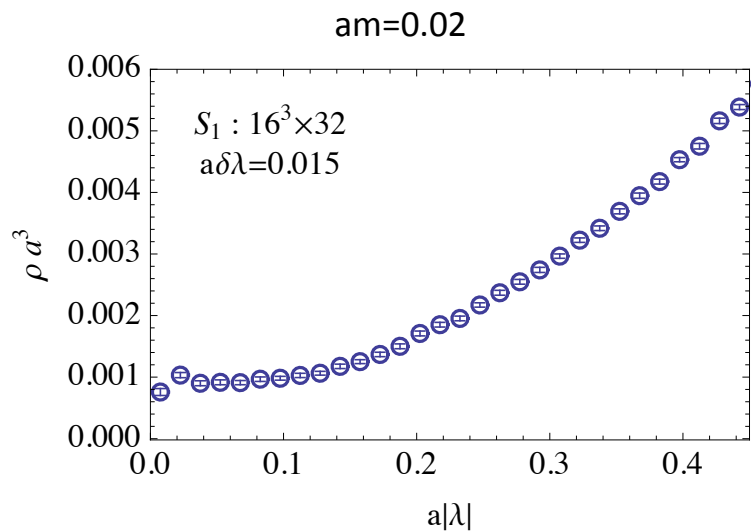
- Ways to restore valence chiral symmetry: increasing  $T$ ,  $N_f$  and lowering  $m$
- Can lowering  $m$  lead to anomalous phase at suitable  $N_f$  ?
- $N_f=12$  a suitable candidate
- Controversy over whether  $N_{f,cr} < 12$

$N_f=12 \dots$

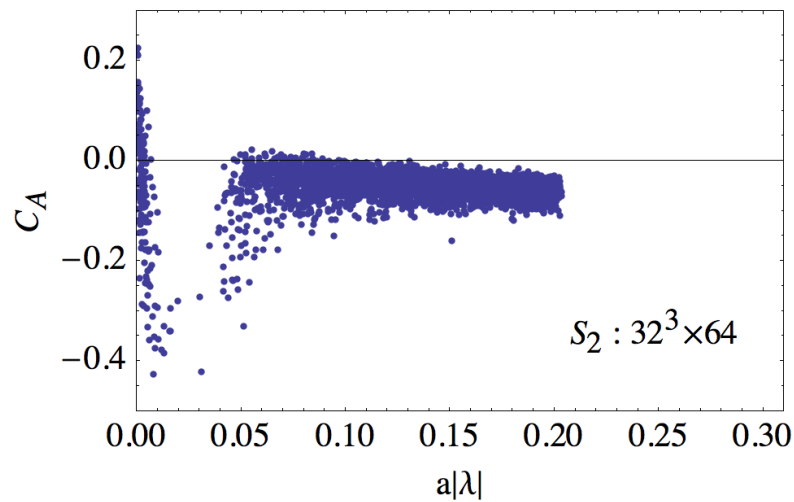
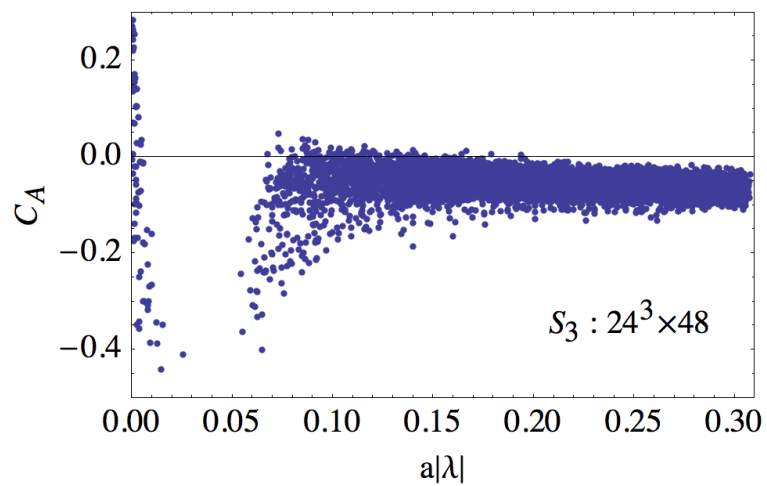
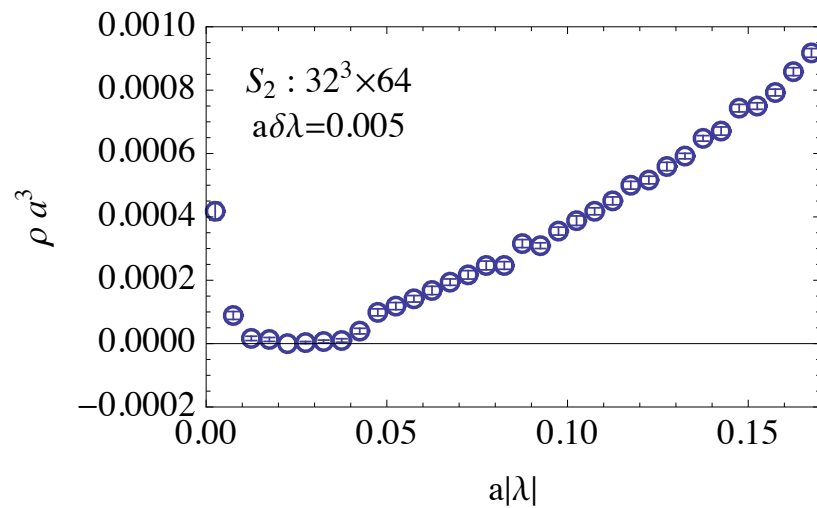
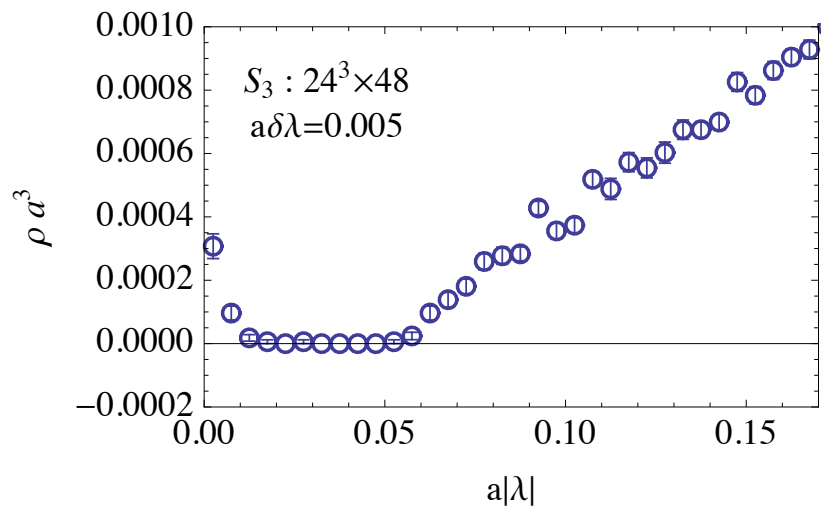
Ensembles from A. Hasenfratz et al, arXiv:1207.7162

staggered with nHYP,  $\beta_F=2.8$ ,  $\beta_A/\beta_F=-0.25$

overlap valence probe



# $N_f=12 \dots$ volume



correlation coefficients for individual overlap modes

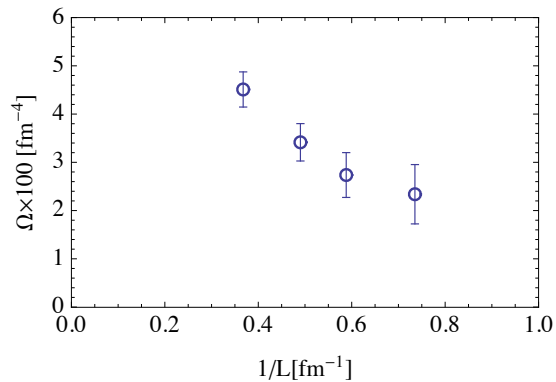
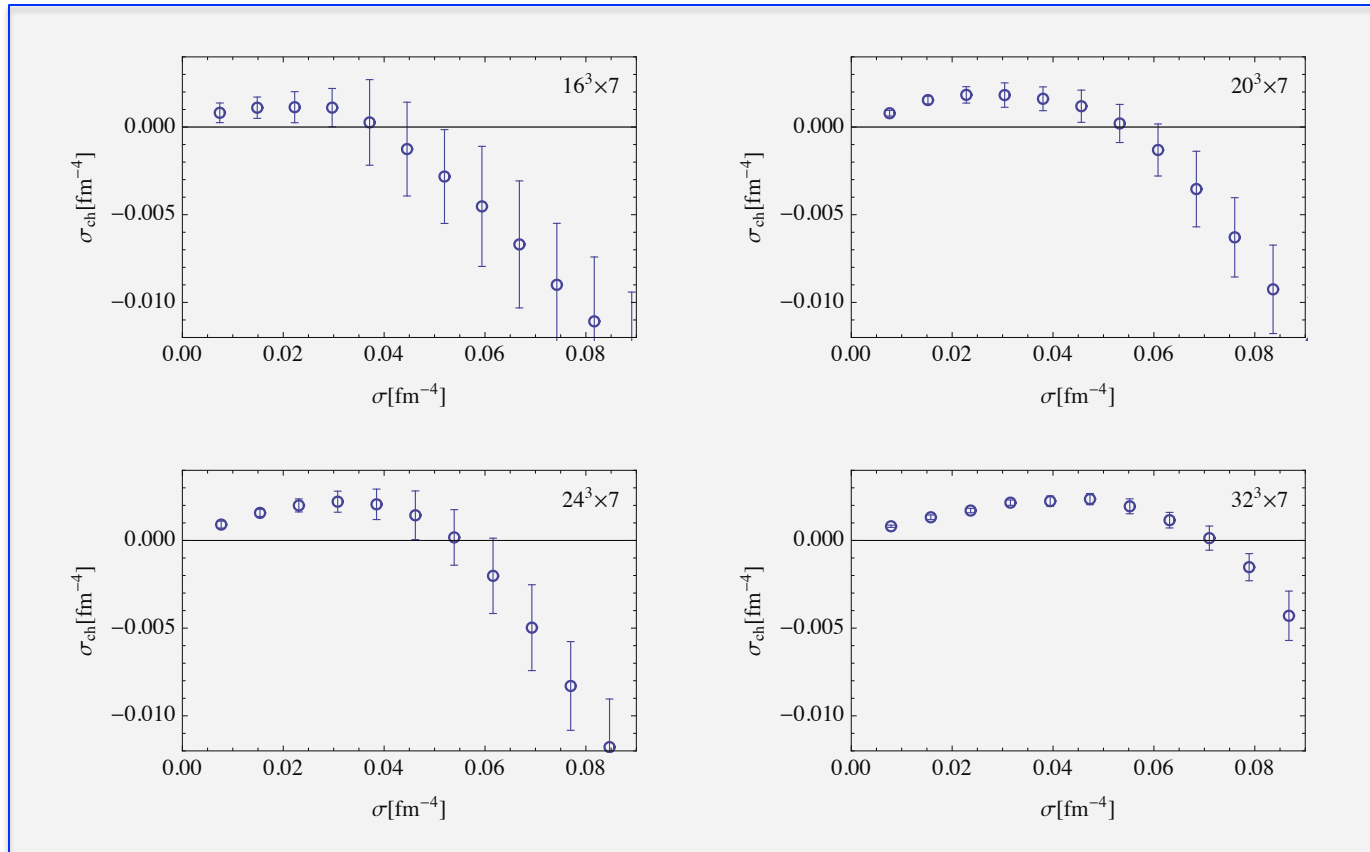
Apparently stable!

# Summary

- ◆ Underlying idea: symmetry breaking  $\iff$  local NP correlation
- ◆ Here: vSChSB  $\iff$  Chiral Polarization
- ◆ vSChSB-ChP correspondence holds in all known studied cases!  
[New characterization of QCD vacuum/thermal states. Phase diagrams etc.]
- ◆ Anomalous temperature phase in  $N_f=0$  screams it is real!
- ◆ *There is an anomalous phase(in mass) at  $N_f=12!!!$* 
  - Does it survive continuum limit?
  - Does it exist with fewer flavors?
  - Is  $m_{cr} > 0$ ? (conformal window issue)
  - What are physical consequences?
  - To what extent are thermal fluctuations and quantum fluctuations due to many flavors similar?



# Volume at fixed cutoff:



**vSchSB – ChP correspondence holds!**