

# PROBING HEAVY QUARKONIUM PRODUCTION MECHANISM: $\chi_c$ POLARIZATION

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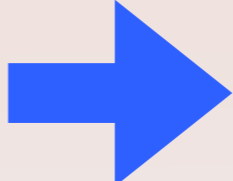
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# OPENING WORDS

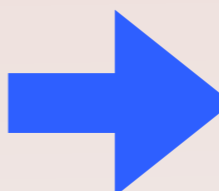

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- Do we understand QCD ?
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  - Non-perturbative: no !
  - Heavy Quarkonium plays the role at the interplay between perturbative regime and non-perturbative regime.

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  - Heavy Quarkonium plays the role at the interplay between perturbative regime and non-perturbative regime.

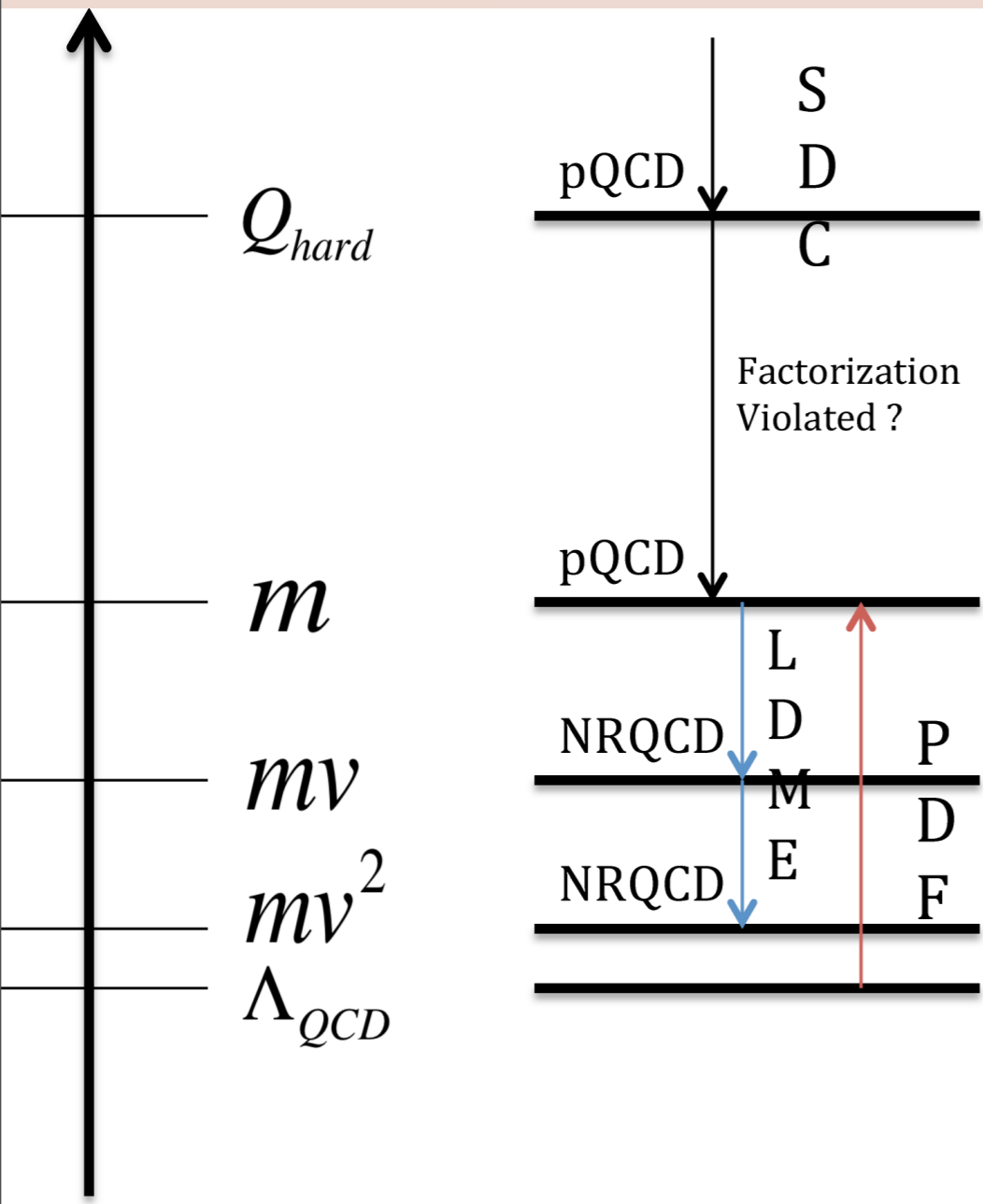
# OPENING WORDS

- Do we understand **QCD** ?
  - Perturbative: yes !
  - Non-perturbative: no !  
  - **Heavy** Quarkonium plays the role at the interplay between perturbative regime and non-perturbative regime.

# BACKGROUND

- Heavy quarkonium
  - bound state with a heavy-flavor quark pair
  - color-singlet meson
  - the relative velocity of the quark pair is small
    - $v^2 \approx 0.3$  for charmonium
    - $v^2 \approx 0.1$  for bottomonium

# BACKGROUND



- Heavy quarkonium production is a multi-scale process:
  - $Q_{hard}$  : scale at which a heavy-flavor quark pair is generated.
  - $m$  : mass of heavy quarks.
  - $mv$  : relative momentum of a heavy quark in the rest frame of heavy quarkonium.
  - $mv^2$  : binding energy of heavy quarkonium.
  - $\Lambda_{QCD}$  : intrinsic QCD scale

# MODELS

- Color-Singlet Model (CSM) [Einhorn, Ellis (1975) ...]

- $Q\bar{Q}$  are produced in the CS state at scale  $Q_{hard}$ .

- Color-Evaporation Model (CEM) [Fritzsch (1977) ...]

- Under quark-hadron duality,  $Q\bar{Q}$  are produced with their invariant mass less than the threshold of open-flavor heavy meson pair.

- Fragmentation Function

Approach (FF) [Braaten et al. (1996) ...]

- Cross section can be factorized in terms of convolutions of parton production cross section with FFs in limit of  $p_T \gg m$ .

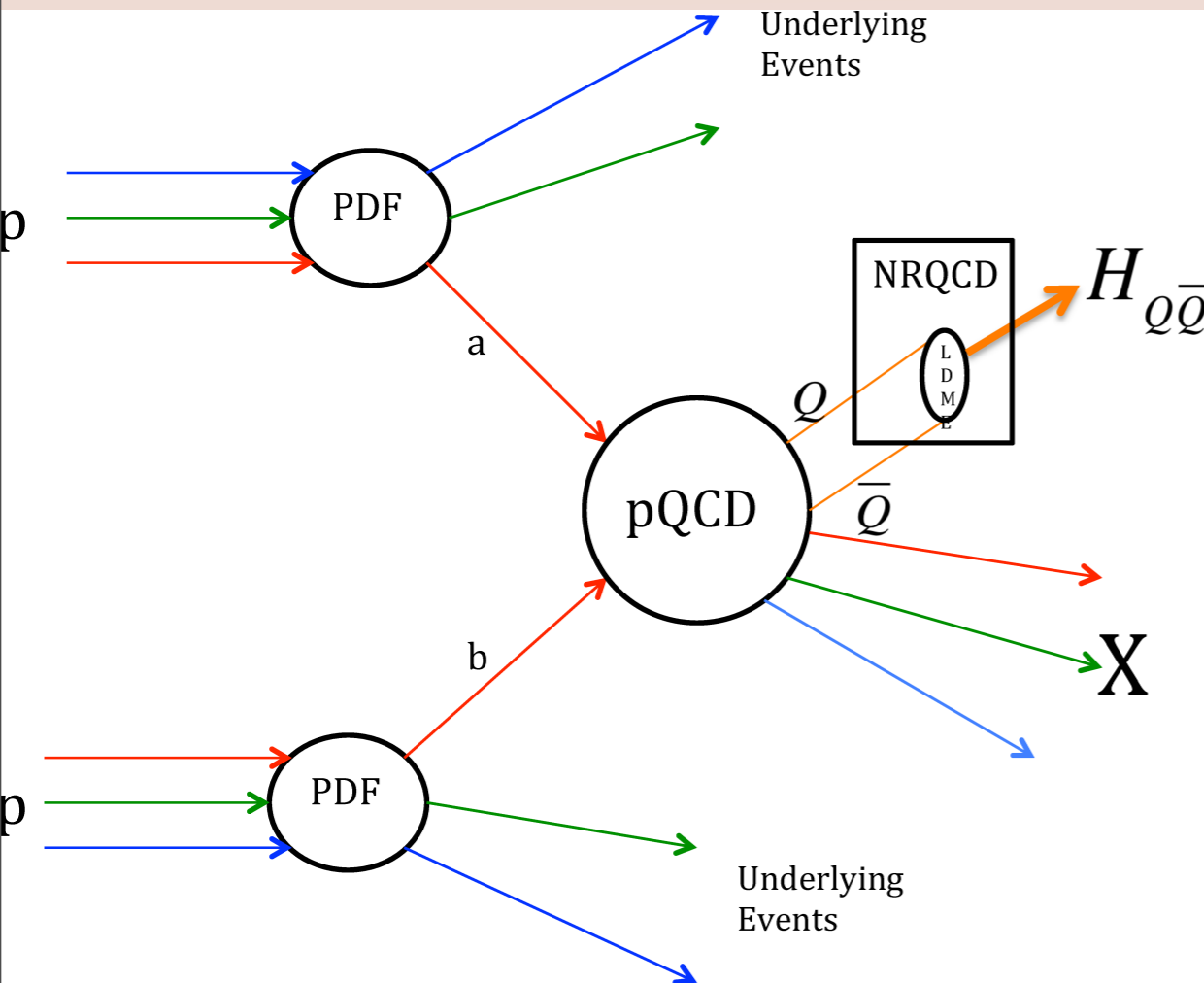
- Non-relativistic QCD

(NRQCD) [Bodwin et al. (1995)]

- An effective field theory based on factorization conjecture.  $Q\bar{Q}$  can be produced in both of CS and CO states at scale  $Q_{hard}$ .



# NRQCD FACTORIZATION



- NRQCD factorization

$$d\sigma(pp \rightarrow H_{Q\bar{Q}} + X)$$

$$= \sum_n d\sigma(pp \rightarrow Q\bar{Q}[n] + X) \times \langle \mathcal{O}^{H_{Q\bar{Q}}}(n) \rangle$$

- pQCD factorization

$$d\sigma(pp \rightarrow Q\bar{Q}[n] + X)$$

$$= \sum_{a,b} f_{a/p}(x_1) f_{b/p}(x_2) |\mathcal{A}(ab \rightarrow Q\bar{Q}[n] + X)|^2$$

- LDME  $\langle \mathcal{O}^{H_{Q\bar{Q}}}(n) \rangle$  and PDF  $f_{i/p}(x)$  are **non-perturbative**.

# POWER COUNTING

- Number of Fock states  $n = \binom{2S+1}{J} L_J^{[c]}$  is infinity but scaling in  $v$ . A practical perturbative calculation always truncates it at a specific order.
- Some examples in the following table

Power counting	$\eta_c, \eta_b$	$J/\psi, \psi(2S), \Upsilon$	$h_c, h_b$	$\chi_{cJ}, \chi_{bJ}$
$v^3$	$^1S_0^{[1]}$	$^3S_1^{[1]}$	—	—
$v^5$	—	—	$^1P_1^{[1]}, ^1S_0^{[8]}$	$^3P_J^{[1]}, ^3S_1^{[8]}$
$v^7$	$^1S_0^{[8]}, ^3S_1^{[8]}, ^1P_1^{[8]}$	$^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_J^{[8]}$	—	—

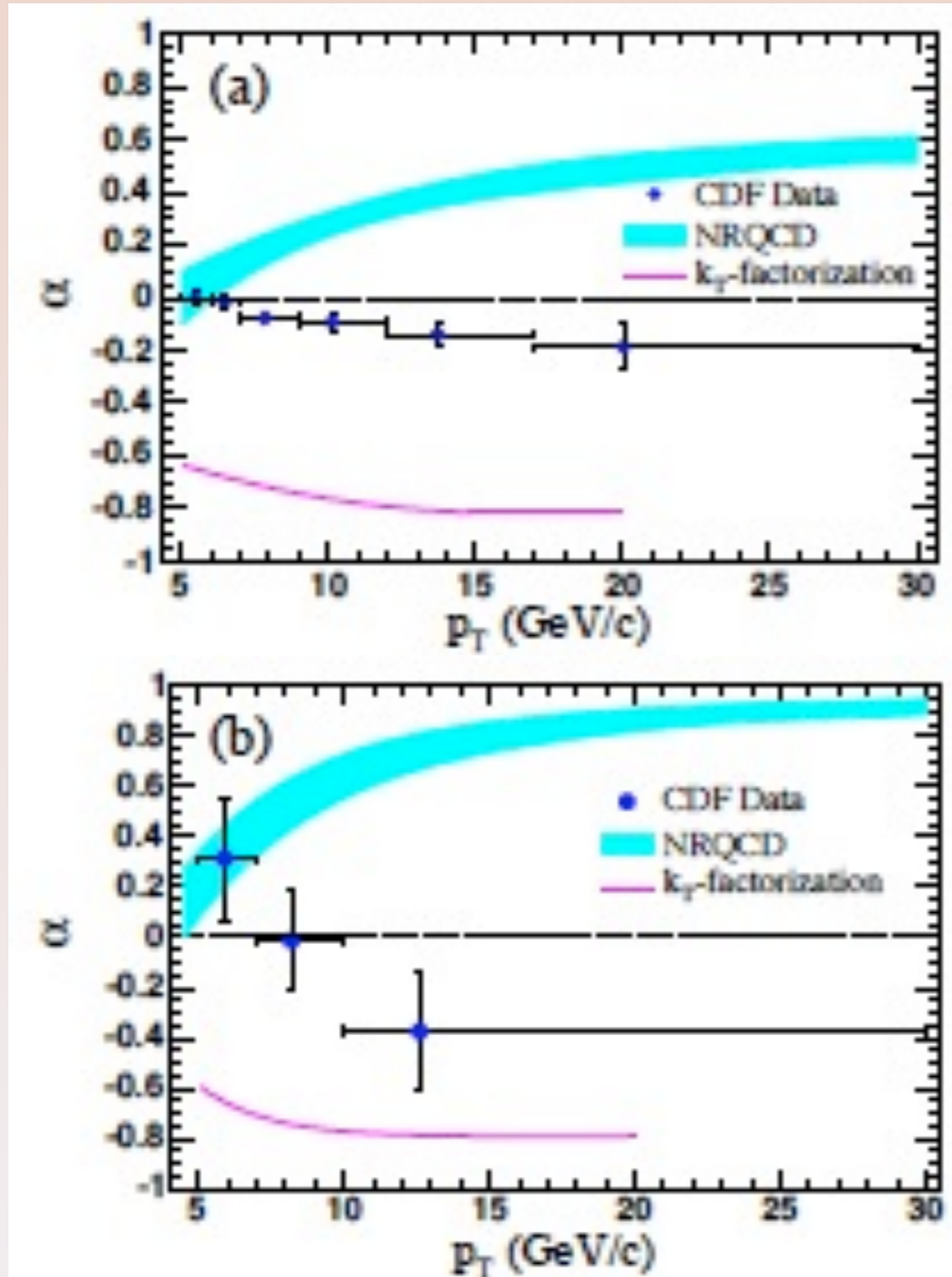
# CHALLENGES IN NRQCD

- Lacking proof of NRQCD factorization conjecture.
  - Very large higher-order corrections.
  - NRQCD confronts experiments.

# NEW TOPOLOGIES AT HO ONLY

	CSM	COM
LO	$p_T \gg m \sim \alpha_S^3 \frac{(2m)^4}{p_T^6}$	$p_T \gg m \sim \alpha_S^3 \frac{1}{p_T^4}$ $p_T \gg m \sim \alpha_S^3 \frac{(2m)^2}{p_T^6}$
NLO	$p_T \gg m \sim \alpha_S^4 \frac{(2m)^2}{p_T^6}$	$p_T \gg m \sim \alpha_S^4 \frac{1}{p_T^4}$
NNLO	$p_T \gg m \sim \alpha_S^5 \frac{1}{p_T^4}$	

CDF Collaboration (2007)



- NRQCD confronts various heavy quarkonium experimental data, include  $pp, p\bar{p}, e^+e^-, \gamma p, \gamma\gamma, e^-p, pA, AA$  collisions.
- At low scale  $Q_{hard} \sim m$  production (like integrated- $p_T$  cross section in hadroproduction, B factories data [HSS (2014)]), CSM seems to be already fine to describe the data.
- At high scale  $Q_{hard} \gg m$  quarkonium production (like high- $p_T$  data at Tevatron and LHC), COM seems to be necessary especially for polarisation.

# $J/\psi$ CASE

- CSM cannot explain the yields and polarization (up to NNLO\*).  
[Campbell, Maltoni, Tramontano (2007); Artoisenet, Lansberg, Maltoni (2007)]
- In NRQCD, there are three leading CO LDMEs should be tuned to data. However, the current hadroproduction experimental data are not sufficient to determine the three CO LDMEs (which means that most of these data are correlated). Other experimental data are most likely in the small momentum transfer region, where the factorization may be unreliable. [Chao, Ma, HSS, Wang, Zhang (2012); Bodwin, Chung, Kim, Lee (2014); Faccioli, Knunz, Lourenco, Seixas, Wohri (2014)]
- It receives substantial smearing from feed-down contribution ( $\chi_c, \psi(2S)$ ).

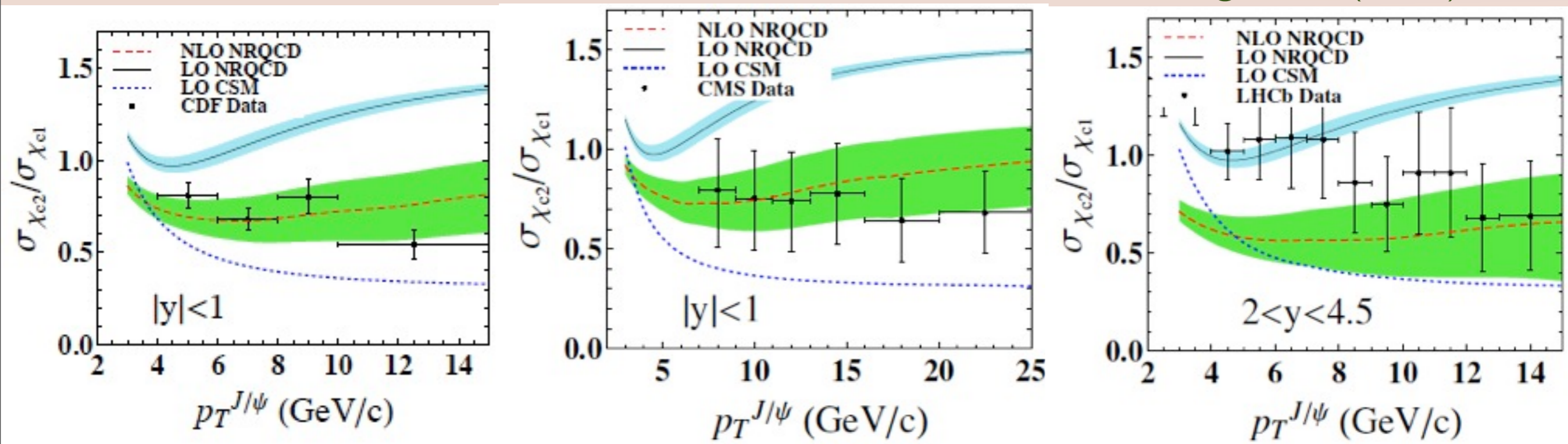
## WHY $\chi_c$ ?

- CSM has the problem of canceling IR divergence. The only way to treat it perturbatively is by introducing a CO contribution to cancel the IR div, which is naturally guaranteed in NRQCD.
- In contrast to  $J/\psi$ , there is only ONE leading CO LDME should be determined from data in  $\chi_c$ .
- No significant feed-down contribution in prompt  $\chi_c$  production.
- Lesson from  $J/\psi$  case : the polarization may be sensitive to the value of the CO LDME, i.e. its CO production mechanism.

# PROCEED TO NLO LEVEL

Yields of prompt  $\chi_c$  in hadroproduction

HSS, Ma, Wang, Chao (2014)

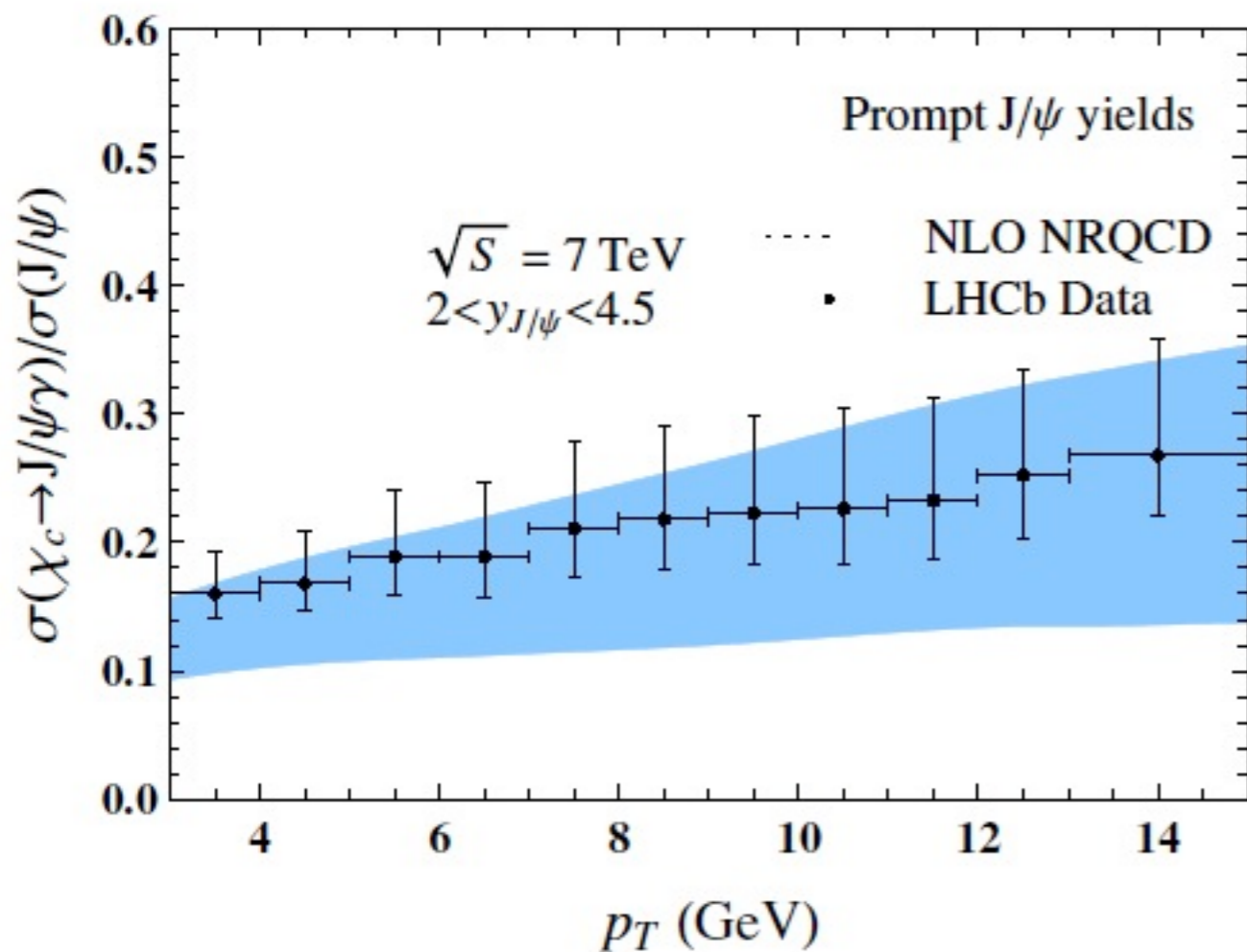


- Fit the Tevatron data of  $\sigma_{\chi_{c2}}/\sigma_{\chi_{c1}}$  to extract CO LDME.
- Good agreement achieved with LHC data.



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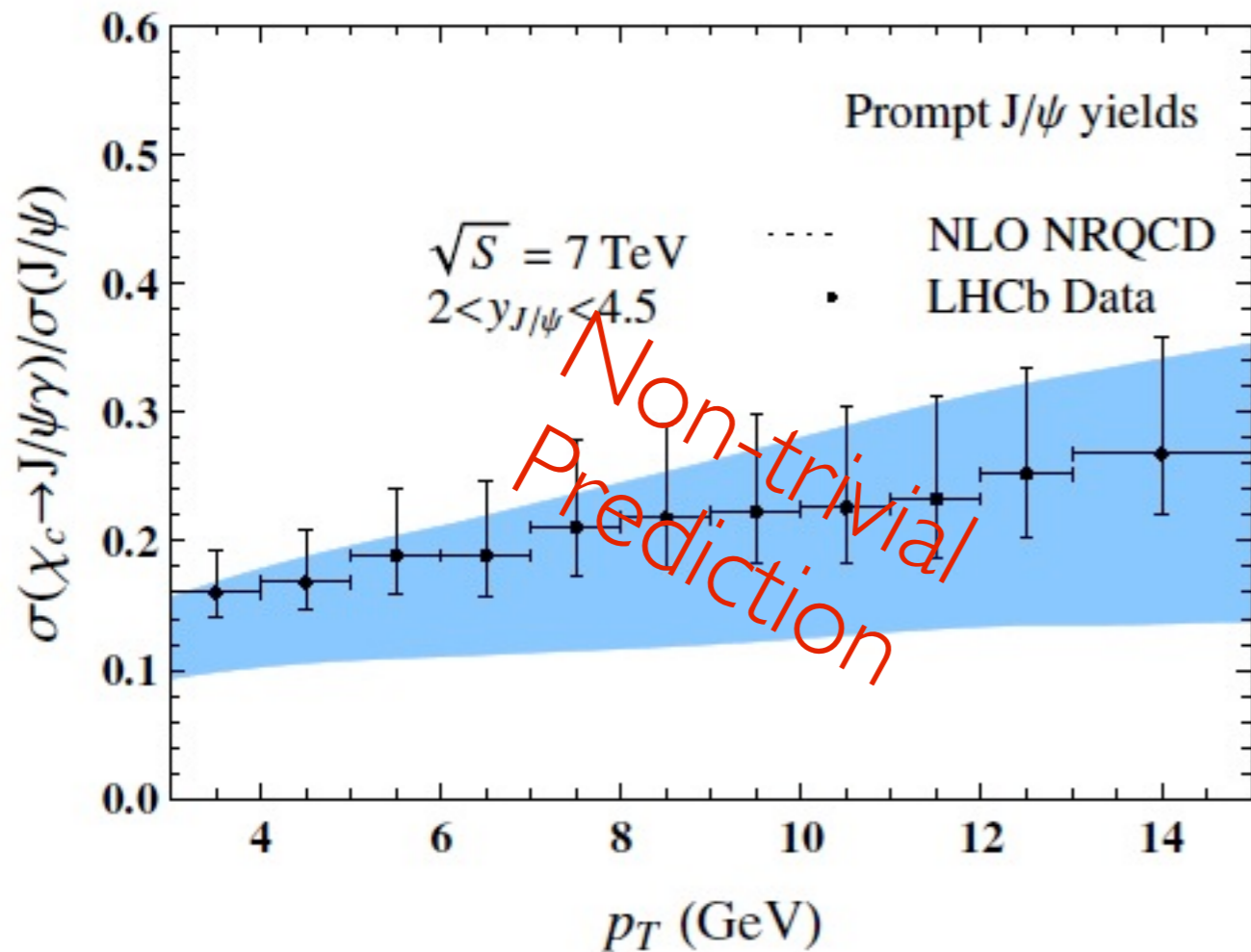


- Also predicts a very good feed-down ratio for prompt  $J/\psi$  production compared with LHCb data.

LHCb Collaboration (2012)

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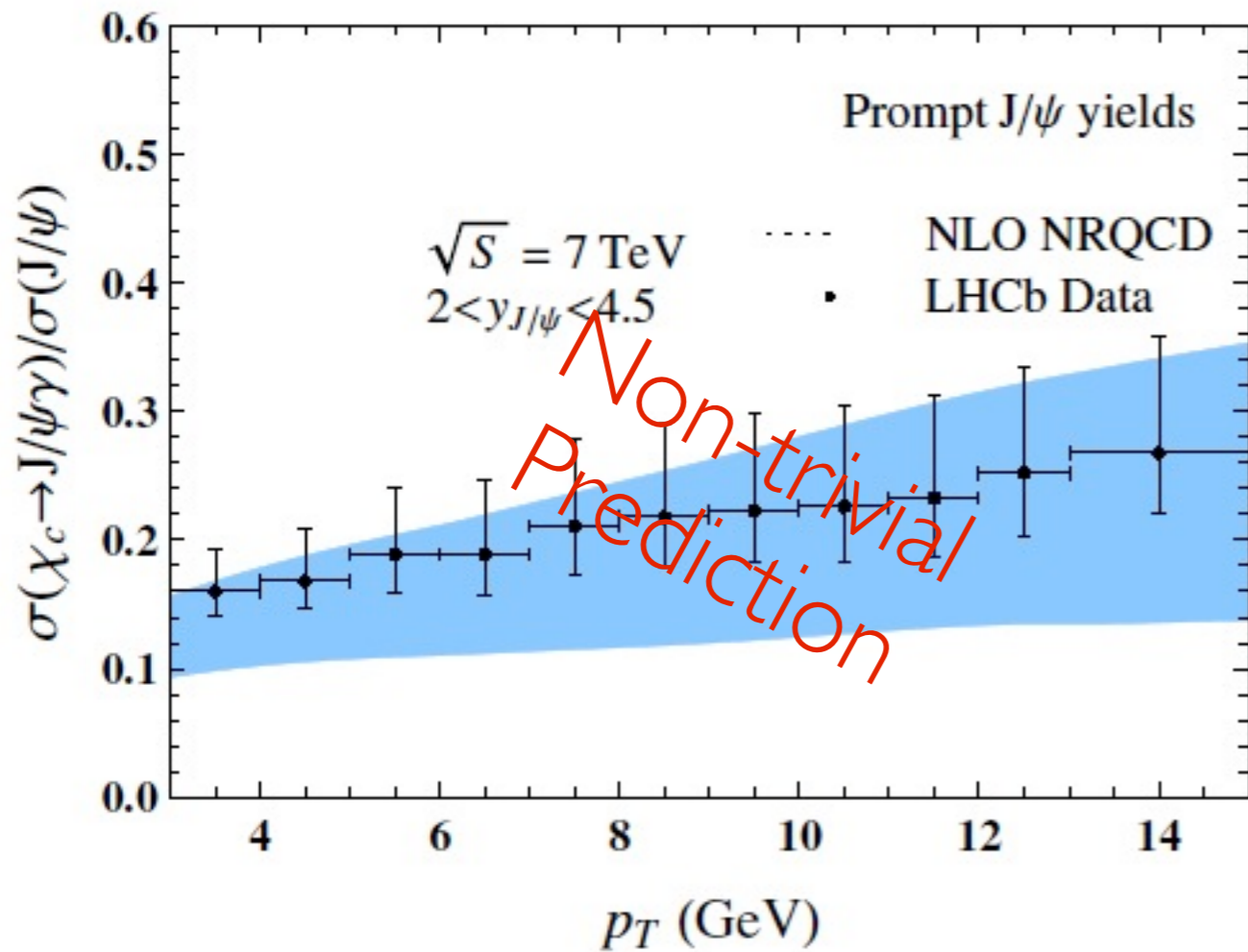


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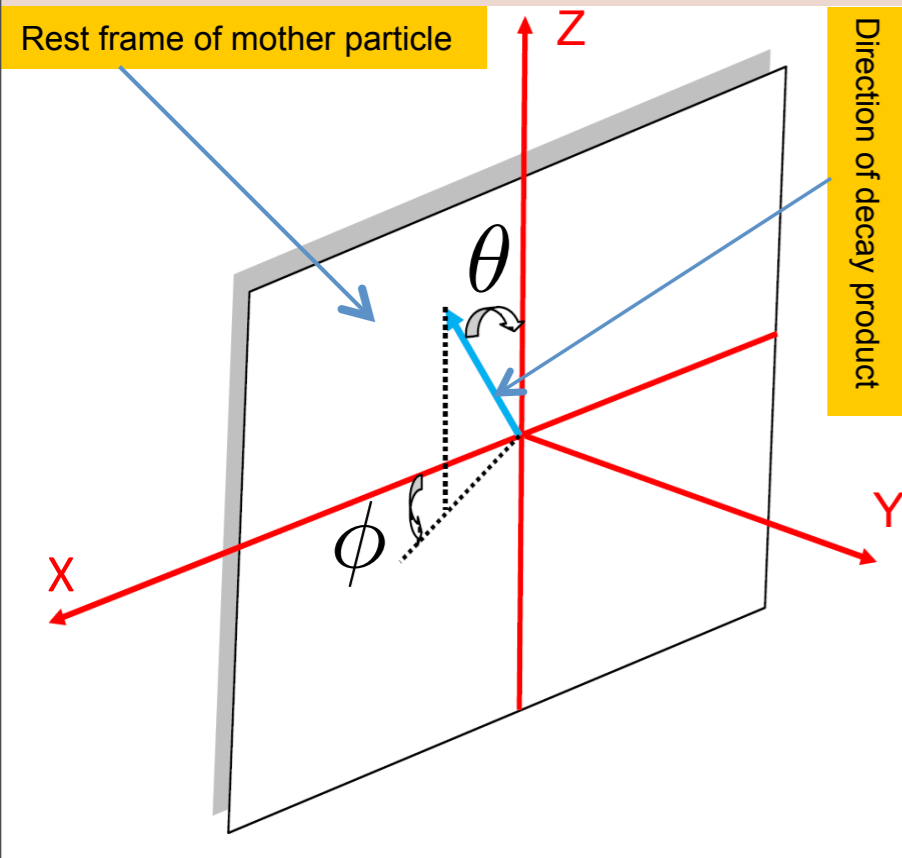
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**How about polarization ?**

# ANGULAR DISTRIBUTION I

Kniesl, Kramer, Palisoc(2003); Faccioli, Lourenco, Seixas, Wohri (2011); HSS, Chao (2012)



$$\chi_{cJ} \rightarrow J/\psi + \gamma$$

$$\frac{d\mathcal{N}^{\chi_{cJ}}}{d\cos\theta} \propto 1 + \sum_{k=1}^J \lambda_{k\theta} \cos^{2k}\theta$$

$$\chi_{c1} \rightarrow J/\psi + \gamma$$

$$\lambda_{\theta} = (1 - 3\delta) \frac{N_{\chi_{c1}} - 3\rho_{0,0}^{\chi_{c1}}}{(1 + \delta)N_{\chi_{c1}} + (1 - 3\delta)\rho_{0,0}^{\chi_{c1}}}$$

$$N_{\chi_{c1}} \equiv \rho_{1,1}^{\chi_{c1}} + \rho_{0,0}^{\chi_{c1}} + \rho_{-1,-1}^{\chi_{c1}}$$

$$\delta = (1 + 2a_1^{J=1}a_2^{J=1})/2$$

$$\chi_{c2} \rightarrow J/\psi + \gamma$$

$$\lambda_{\theta} = 6[(1 - 3\delta_0 - \delta_1)N_{\chi_{c2}} - (1 - 7\delta_0 + \delta_1)(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) - (3 - \delta_0 - 7\delta_1)\rho_{0,0}^{\chi_{c2}}]/R,$$

$$\lambda_{2\theta} = (1 + 5\delta_0 - 5\delta_1)[N_{\chi_{c2}} - 5(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) + 5\rho_{0,0}^{\chi_{c2}}]/R$$

$$N_{\chi_{c2}} \equiv \rho_{2,2}^{\chi_{c2}} + \rho_{1,1}^{\chi_{c2}} + \rho_{0,0}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}} + \rho_{-2,-2}^{\chi_{c2}},$$

$$R \equiv (1 + 5\delta_0 + 3\delta_1)N_{\chi_{c2}} + 3(1 - 3\delta_0 - \delta_1)(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) + (5 - 7\delta_0 - 9\delta_1)\rho_{0,0}^{\chi_{c2}}$$

$$\delta_0 = [1 + 2a_1^{J=2}(\sqrt{5}a_2^{J=2} + 2a_3^{J=2})$$

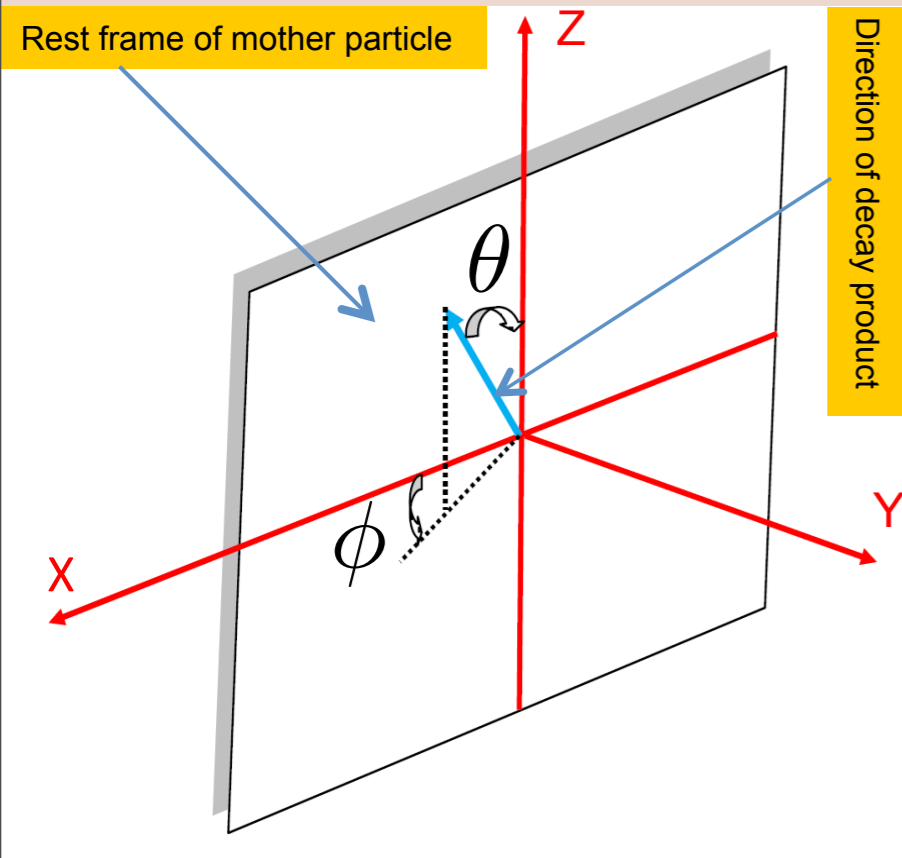
$$+ 4a_2^{J=2}(a_2^{J=2} + \sqrt{5}a_3^{J=2}) + 3(a_3^{J=2})^2]/10,$$

$$\delta_1 = [9 + 6a_1^{J=2}(\sqrt{5}a_2^{J=2} - 4a_3^{J=2})$$

$$- 4a_2^{J=2}(a_2^{J=2} + 2\sqrt{5}a_3^{J=2}) + 7(a_3^{J=2})^2]/30$$

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**E1, M2, E3**

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$$\lambda_{2\theta} = (1 + 5\delta_0 - 5\delta_1)[N_{\chi_{c2}} - 5(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) + 5\rho_{0,0}^{\chi_{c2}}]/R$$

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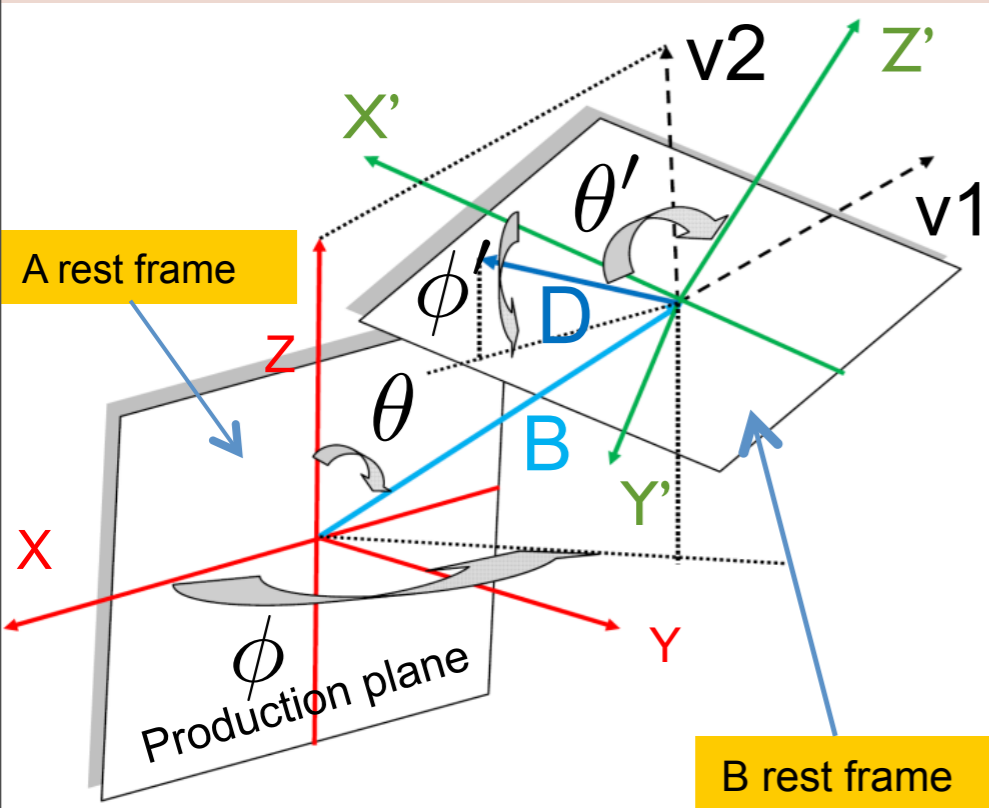
$$R \equiv (1 + 5\delta_0 + 3\delta_1)N_{\chi_{c2}} + 3(1 - 3\delta_0 - \delta_1)(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) + (5 - 7\delta_0 - 9\delta_1)\rho_{0,0}^{\chi_{c2}}$$

$$\delta_0 = [1 + 2a_1^{J=2}(\sqrt{5}a_2^{J=2} + 2a_3^{J=2}) + 4a_2^{J=2}(a_2^{J=2} + \sqrt{5}a_3^{J=2}) + 3(a_3^{J=2})^2]/10,$$

$$\delta_1 = [9 + 6a_1^{J=2}(\sqrt{5}a_2^{J=2} - 4a_3^{J=2}) - 4a_2^{J=2}(a_2^{J=2} + 2\sqrt{5}a_3^{J=2}) + 7(a_3^{J=2})^2]/30$$

# ANGULAR DISTRIBUTION II

Kniefel, Kramer, Palisoc(2003); Faccioli, Lourenco, Seixas, Wohri (2011); HSS, Chao (2012)



$$A \rightarrow B(\rightarrow D + E) + C$$

$$\chi_{cJ} \rightarrow J/\psi(\rightarrow \ell^+ \ell^-) + \gamma$$

$$\frac{d\mathcal{N}^{\chi_{cJ}}}{d\cos\theta'} \propto 1 + \lambda_{\theta'} \cos^2\theta'$$

$$Z' = v2$$

$$\chi_{c1} \rightarrow J/\psi(\rightarrow \ell^+ \ell^-) + \gamma$$

$$\lambda_{\theta'} = \frac{-N_{\chi_{c1}} + 3\rho_{0,0}^{\chi_{c1}}}{R_1},$$

$$N_{\chi_{c1}} \equiv \rho_{1,1}^{\chi_{c1}} + \rho_{0,0}^{\chi_{c1}} + \rho_{-1,-1}^{\chi_{c1}}$$

$$R_1 \equiv [(15 - 2(a_2^{J=1})^2)N_{\chi_{c1}} - (5 - 6(a_2^{J=1})^2)\rho_{0,0}^{\chi_{c1}}] / (5 - 6(a_2^{J=1})^2)$$

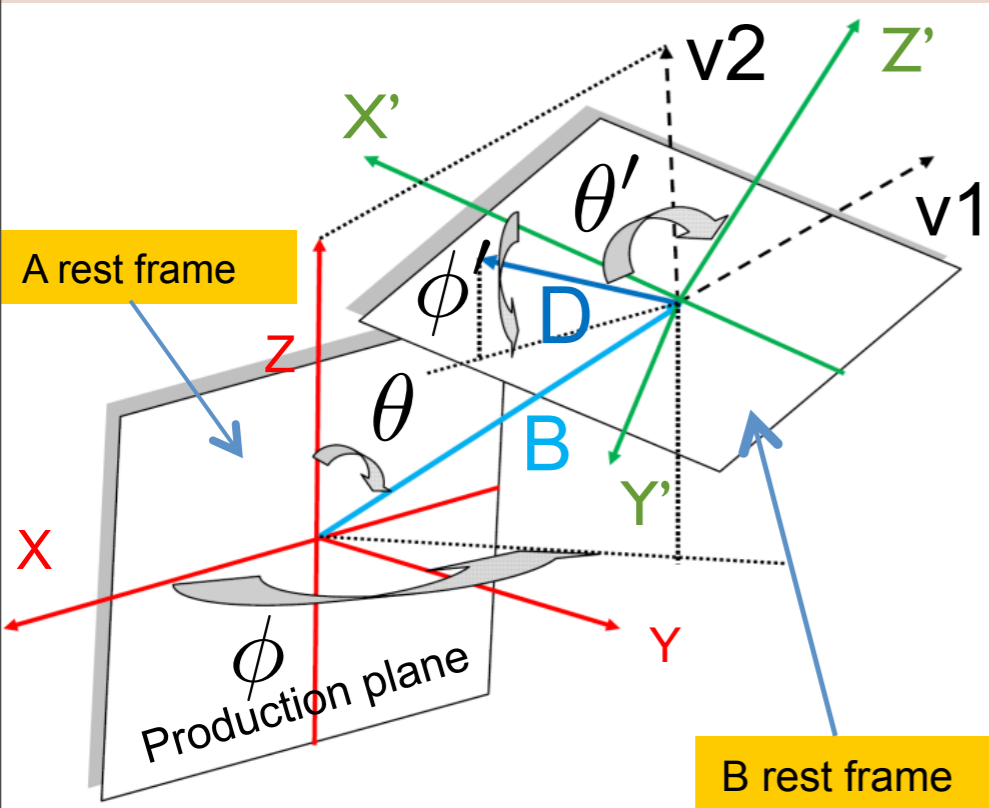
$$\chi_{c2} \rightarrow J/\psi(\rightarrow \ell^+ \ell^-) + \gamma$$

$$\lambda_{\theta'}^{\chi_{c2}} = \frac{6N_{\chi_{c2}} - 9(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) - 12\rho_{0,0}^{\chi_{c2}}}{R_2}$$

$$R_2 \equiv [2(21 + 14(a_2^{J=2})^2 + 5(a_3^{J=2})^2)N_{\chi_{c2}} + 3(7 - 14(a_2^{J=2})^2 - 5(a_3^{J=2})^2)(\rho_{1,1}^{\chi_{c2}} + \rho_{-1,-1}^{\chi_{c2}}) + 4(7 - 14(a_2^{J=2})^2 - 5(a_3^{J=2})^2)\rho_{0,0}^{\chi_{c2}}] \div [7 - 14(a_2^{J=2})^2 - 5(a_3^{J=2})^2]$$

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M2, E3 square

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# ANGULAR DISTRIBUTIONS

- $J/\psi$  or  $\gamma$  angular distribution is sensitive to the value of the higher order multipole amplitudes, which are still inconsistent from CLEO, Crystal Ball and E760 measurements. It might be helpful to measure these values from LHC data.
- $\lambda_{20}$  is suppressed by the value of higher order multipole amplitudes. Re-weighting may help to extract it [HSS, Chao (2012)].

Experiment	$a_2^{J=1} (10^{-2})$
CLEO[26]	$-6.26 \pm 0.63 \pm 0.24$
Crystal Ball [27]	$-0.2^{+0.8}_{-2.0}$
E835 [29]	$0.2 \pm 3.2 \pm 0.4$

Experiment	$a_2^{J=2} (10^{-2})$	$a_3^{J=2} (10^{-2})$
CLEO(Fit 1)[26]	$-9.3 \pm 1.6 \pm 0.3$	0(fixed)
CLEO(Fit 2)[26]	$-7.9 \pm 1.9 \pm 0.3$	$1.7 \pm 1.4 \pm 0.3$
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# ROTATION INVARIANT OBSERVABLES

HSS, Chao (2012)

- Angular distributions (as well as their coefficients) are frame dependent.
- A general relation between Wigner functions guarantees some rational functions of the angular coefficients are rotational invariant in its production plane.
- For an arbitrary integer-spin  $n$  particle,  $a_k$  ( $k=-n, \dots, n$ ) are its polarized amplitudes. One is able to derive the following rotational invariant amplitudes

$$b_{2k} \equiv \sum_{m=-k}^k \langle k, m; k, m | 2k, 2m \rangle a_{2m}, \text{ when } n = 2k,$$

$$b_{2k+1} \equiv \sum_{m=0}^k \langle 2k+1-m, 0; m, 0 | 2k+1, 0 \rangle$$

$$(a_{2k+1-m} + a_{m-1-2k}), \text{ when } n = 2k+1$$

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Any functions of  $|b_n|^2$  and

$N_n \equiv \sum_{k=-n}^n |a_n|^2$  are rotational invariant

$$b_{2k} \equiv \sum_{m=-k}^k \langle k, m; k, m | 2k, 2m \rangle a_{2m}, \text{ when } n = 2k,$$

$$b_{2k+1} \equiv \sum_{m=0}^k \langle 2k+1-m, 0; m, 0 | 2k+1, 0 \rangle (a_{2k+1-m} + a_{m-1-2k}), \text{ when } n = 2k+1$$

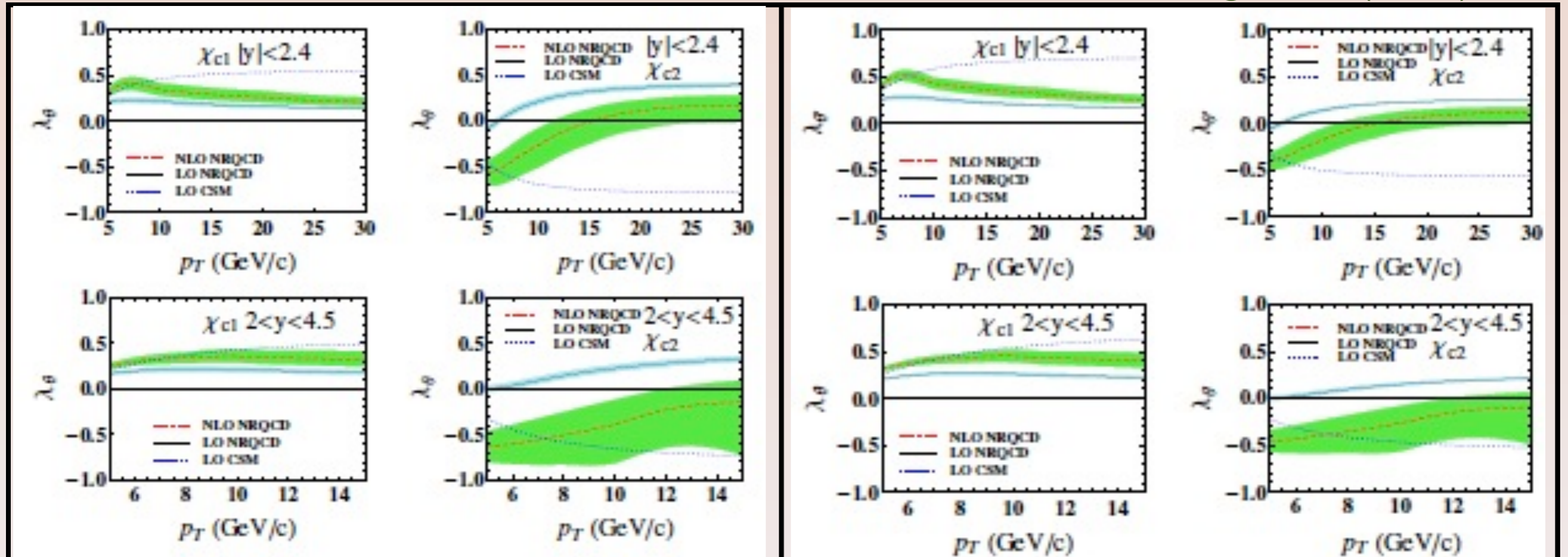


# PROCEED TO NLO LEVEL

Polarization of prompt  $\chi_c$  in hadroproduction

$$\chi_c \rightarrow J/\psi (\rightarrow \ell^+ \ell^-) + \gamma$$

HSS, Ma, Wang, Chao (2014)



photon angular distribution coefficient

di-lepton angular distribution coefficient

# CONCLUSION

- We can understand some features of the non-perturbative QCD through heavy quarkonium production.
- The simultaneously describing the yields and polarization of  $J/\psi$  and  $\psi(2S)$  require tuning to the experimental data in NRQCD. On the contrast,  $\chi_{cJ}$  has only ONE CO LDME to be determined from experimental data, i.e. has more predictive power.
- On the theoretical side, many features of the  $\chi_{cJ}$  polarization have been explored. It may encode rich information about its production mechanism. The NRQCD predictions for the yields and polarization of prompt  $\chi_{cJ}$  hadroproduction are already available up to NLO in QCD.
- We are looking forward to the future experimental measurements at the LHC on  $\chi_{cJ}$  polarization to reveal the heavy quarkonium production mechanism.

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- We can understand some features of the non-perturbative QCD through heavy quarkonium production.
- The simultaneously describing the yields and polarization of  $J/\psi$  and  $\psi(2S)$  require tuning to the experimental data in NRQCD. On the contrast,  $\chi_{cJ}$  has only ONE CO LDME to be determined from experimental data, i.e. has more predictive power.
- On the theoretical side, many features of the  $\chi_{cJ}$  polarization have been explored. It may encode rich information about its production mechanism. The NRQCD predictions for the yields and polarization of prompt  $\chi_{cJ}$  hadroproduction are already available up to NLO in QCD.
- We are looking forward to the future experimental measurements at the LHC on  $\chi_{cJ}$  polarization to reveal the heavy quarkonium production mechanism.

**Thank you for your attention !**