

XIth Quark Confinement and the  
Hadron Spectrum  
08.09-12.09 2014  
Saint-Petersburg

# The QCD Parton-Hadron Phase Boundary

Reinhard Stock



# The Veneziano-Webber Model

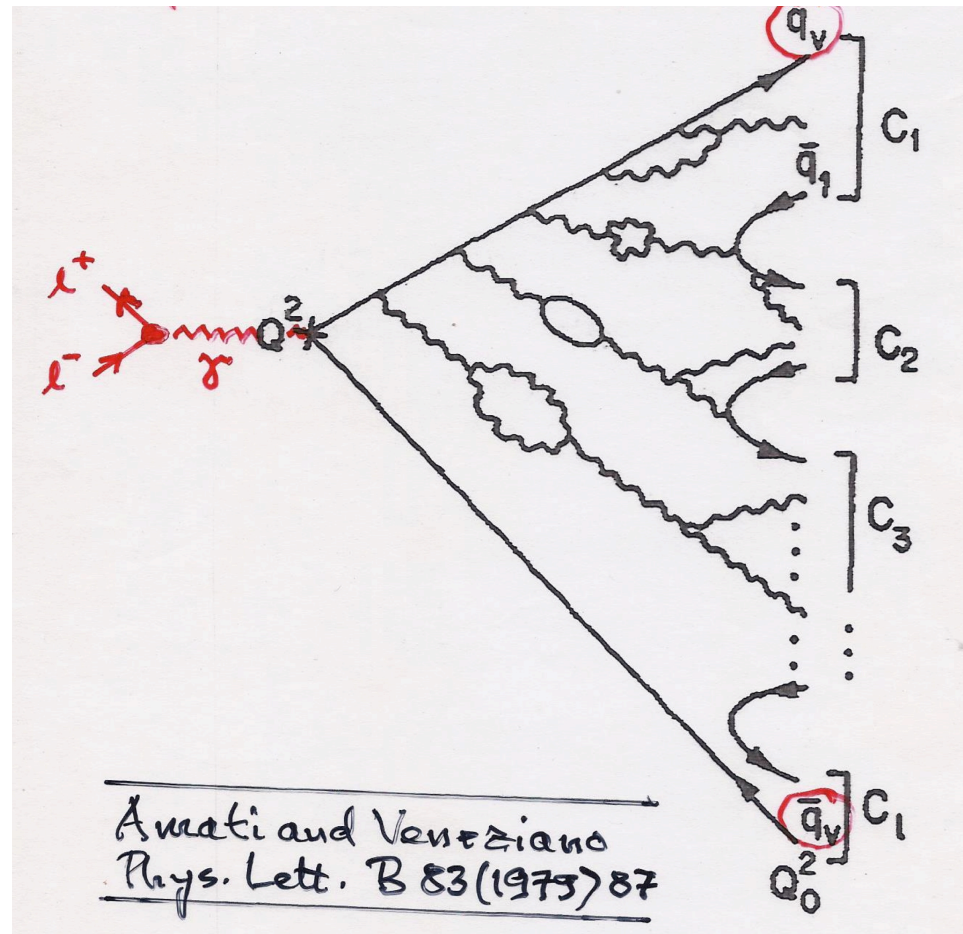
## $e^+e^-$ Annihilation to Hadrons: QCD DGLAP

Note: the photon is “virtual”:  
It has  $E_{CM}$  but no  $P_{CM}$ !  
For “real” particles:  $E^2 = p^2 + m^2$

**Virtuality  $\approx$  virtual mass!**

End of pQCD phase: spatial order  
of color in “cluster” regions:

**“Color pre-confinement!”**



# QCD Evolution in di-jet Hadronization: The Singlet Cluster Mass Spectrum

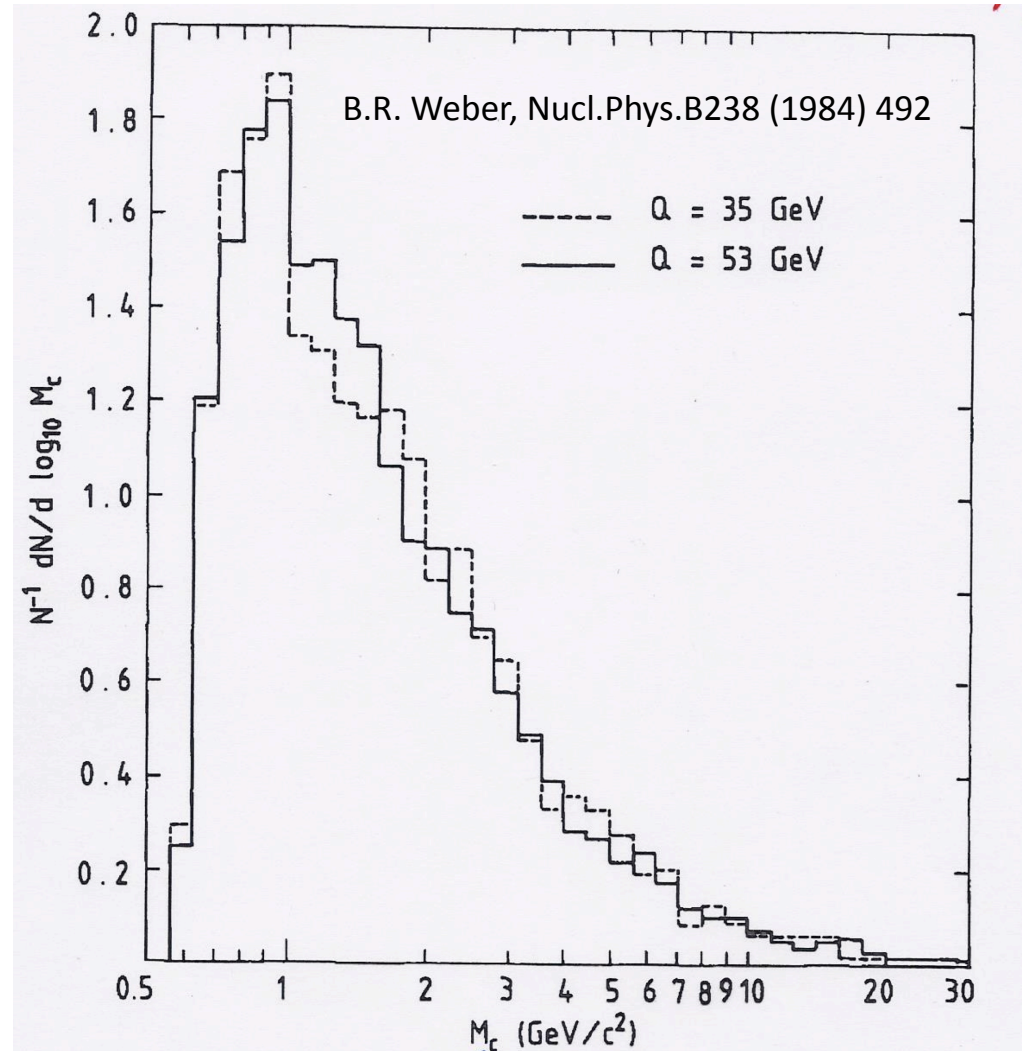
The Code "HERWIG"  
pQCD invariant mass of clusters  
gets reinterpreted in non-  
perturbative language:

**"Condensates, hadronic  
mass"**

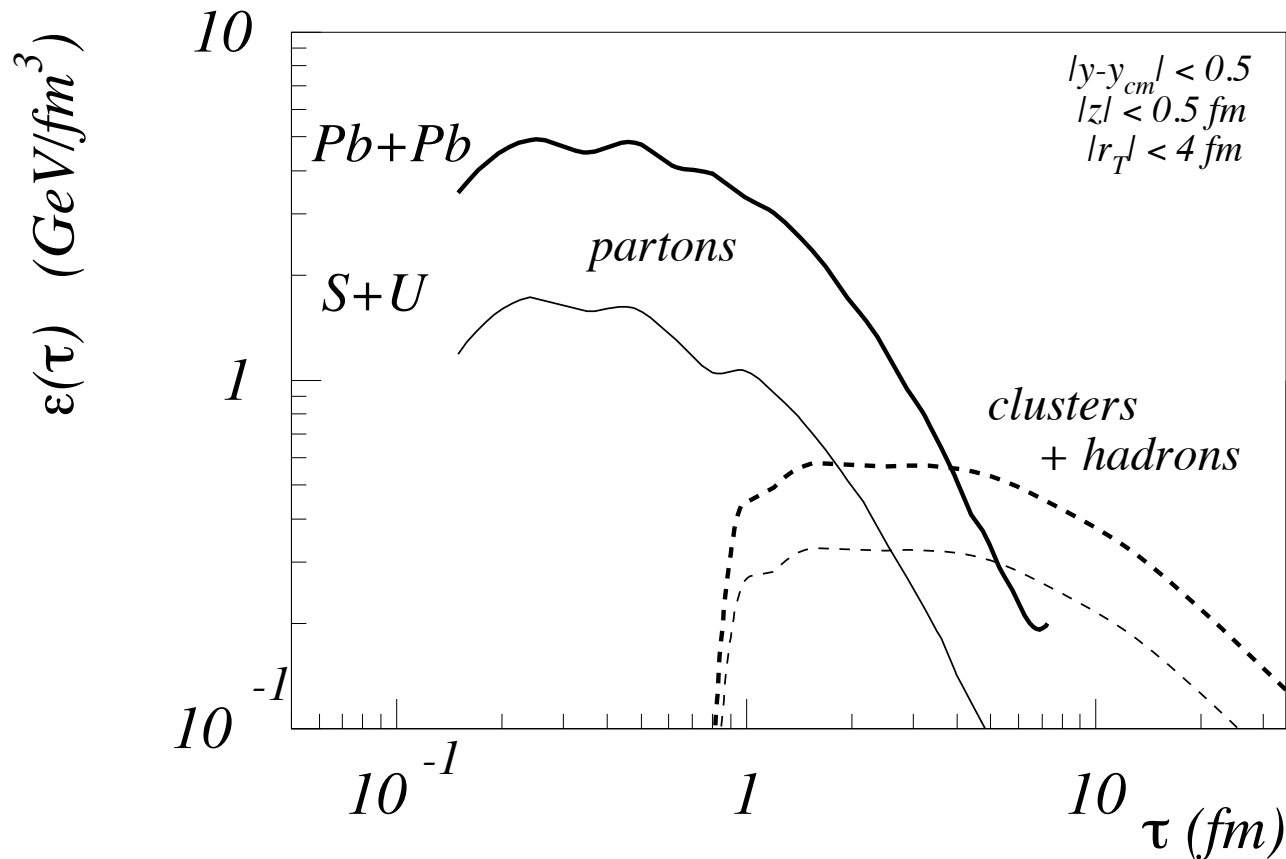


Statistical decay into on-shell  
hadron spectrum

**Phase space dominance**



# Parton Cascade Description of Heavy-Ion Collisions at CERN ? (Klaus Geiger, 1998)



**Evolution of mid-rapidity energy density** (J.Ellis and K.Geiger Phys.Rev. D54 (1996) 1967)

Note: Hadron formation occurs at about  $0.7 \text{ GeV}/\text{fm}^3$

Like in the statistical Hadronization Model

# The Hagedorn Legacy: Statistical Hadronization Model

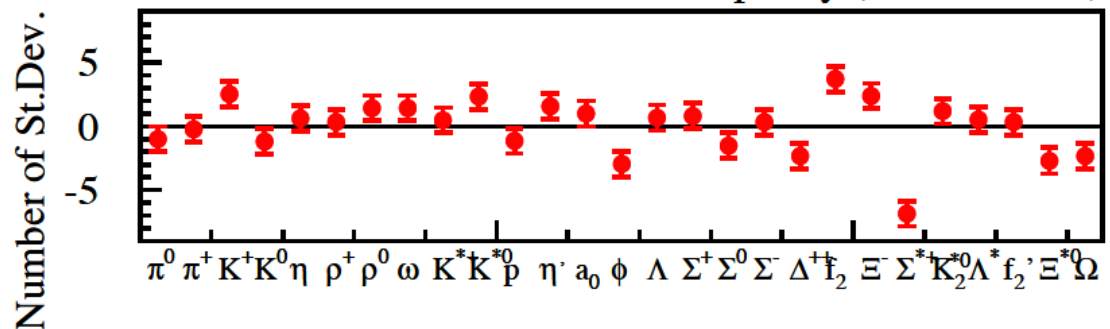
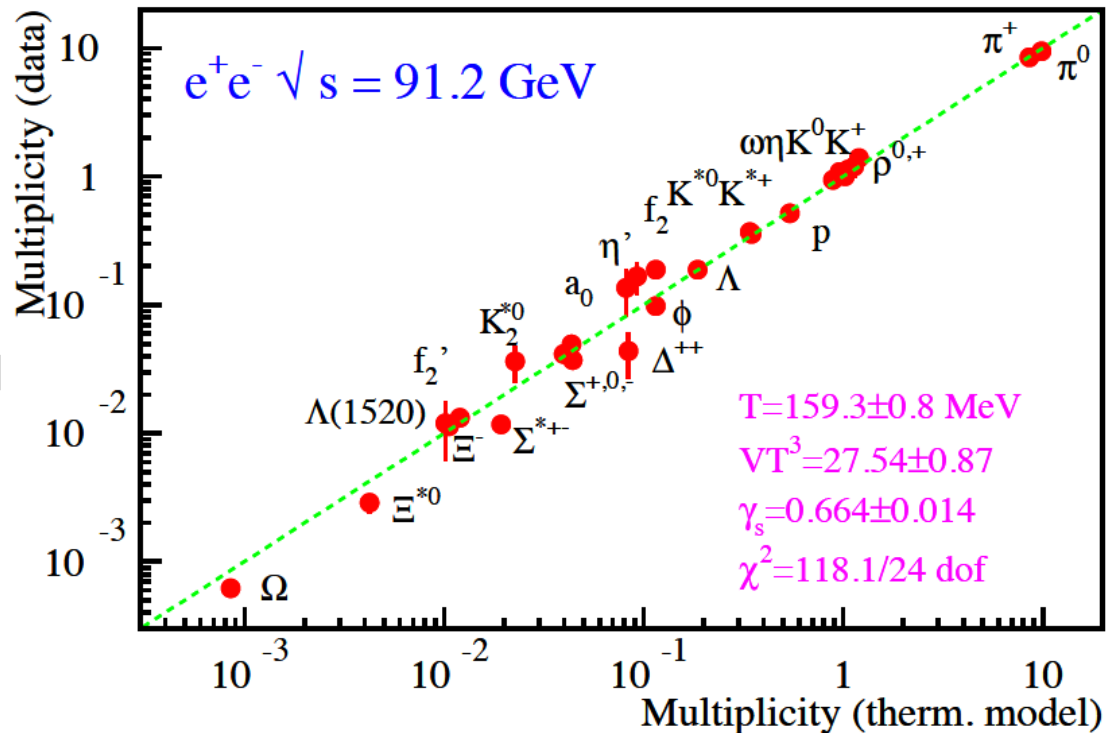
Francesco Becattini  
Nucl.Phys. A702 (2002) 336

LEP data

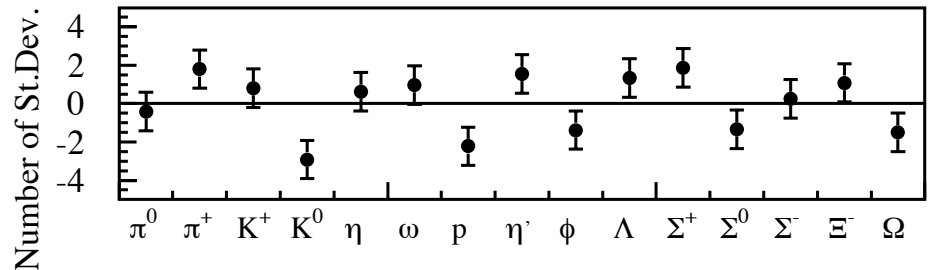
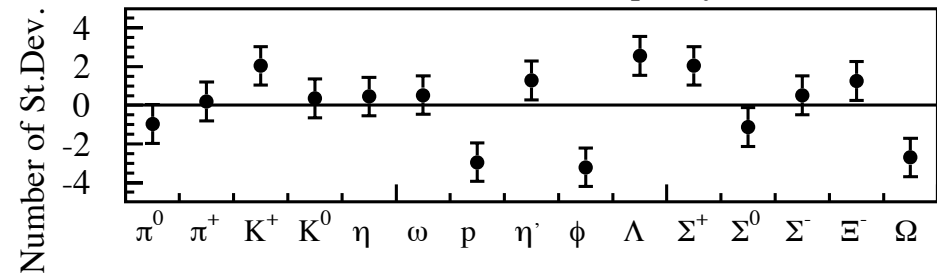
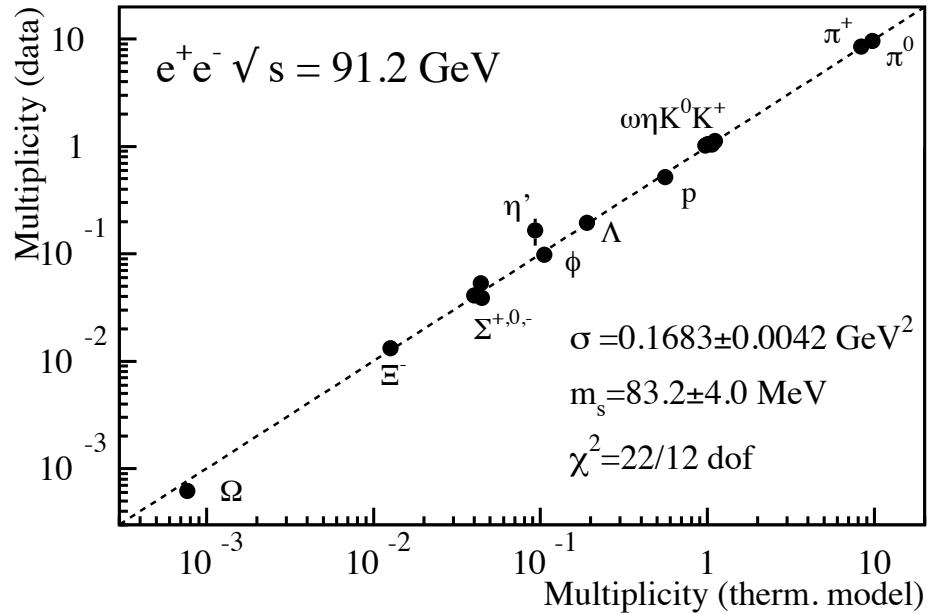
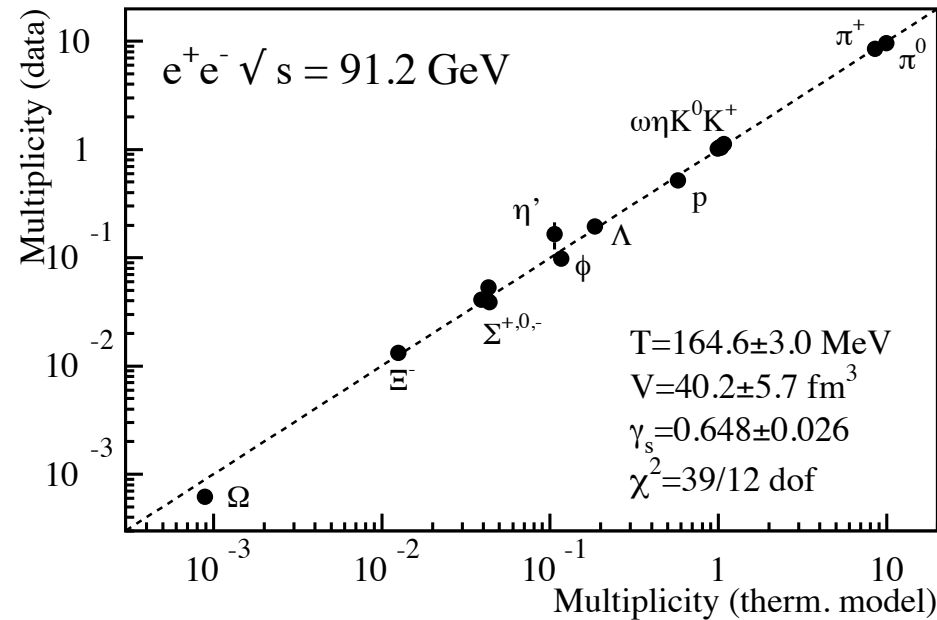
Canonical statistical model  
analysis

**$T \approx 160$  MeV**  
**the hadronization**  
**temperature**

Phase space weights plus  
quantum number  
conservation



# A more Recent Version of $e^+e^-$ Annihilation Analysis (2008)



F.Becattini, P.Castorina, J.Manninen and H.Satz Eur.Phys.J. C56 (2008) 493

**T=164 MeV**

# The Statistical Hadronization Model

R. Hagedorn 1967-71

for recent reference: F. Becattini et al., PRC 69(04)2149

Fireball decay  $\rightarrow$  Grand Canonical Gibbs ensemble of hadron/resonances  $\{i\}$

The species  $i$  are populated according to their "statistical weights", expressed by the "partition functions"  $Z_i$ , where

$$\ln Z_i = \frac{g_i V}{6\pi^2 T} \int_0^\infty \frac{d^4 k}{E_i(k) \exp\{(E_i(k) - \mu_i)/T\} \pm 1}$$

$E_i^2(k) = k^2 + m_i^2$  : in vacuum energy of species  $i$   
 $\mu_i$  the "hadro-chemical potential" " "

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Parameters:  $V$  = system volume,  $T$ ,  $\mu$

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# Grand Canonical Model II

Note: the term  $\exp\{(E_i - \mu_i)/T\}$  in the denominator  $\equiv$  the "Maxwell punishment factor"

regulating the abundance of species  $i$  in the ensemble  $\{i\}$

Multiplicity  $M_i = V \cdot n_i$  where  $n_i = \frac{T}{V} \frac{\partial}{\partial \mu_i} \ln Z_i$

$$\rightarrow M_i = \frac{g_i V}{(2\pi)^2} \int \frac{k^2 dk}{\exp\{(E_i(k) - \mu_i)/T\} \pm 1}$$

$g_i$  is the degeneracy "Landé" factor of

$\mu_i$

is the parameter of the Grand Canonical Ensemble that assures e.g. baryon-number conservation by modifying the vacuum penalty factor



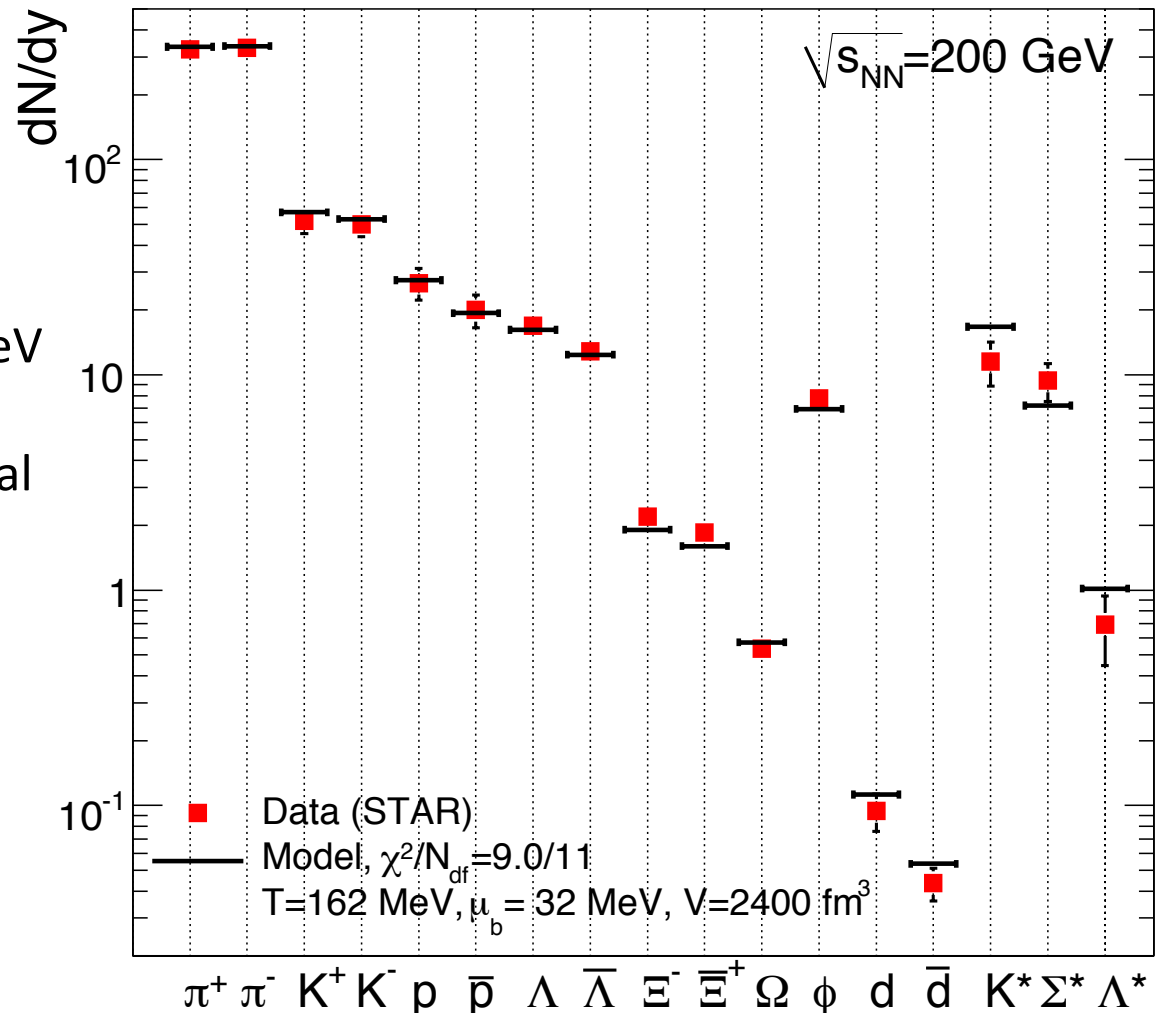
# Statistical Hadronization Model in A+A Collisions

P. Braun-Munzinger,  
J. Stachel  
arXiv:0901.2500 (2009)

RHIC data, Au+Au, 200 GeV

Grand Canonical statistical  
model analysis

**$T \approx 162$  MeV**  
**the hadronization**  
**temperature ?**

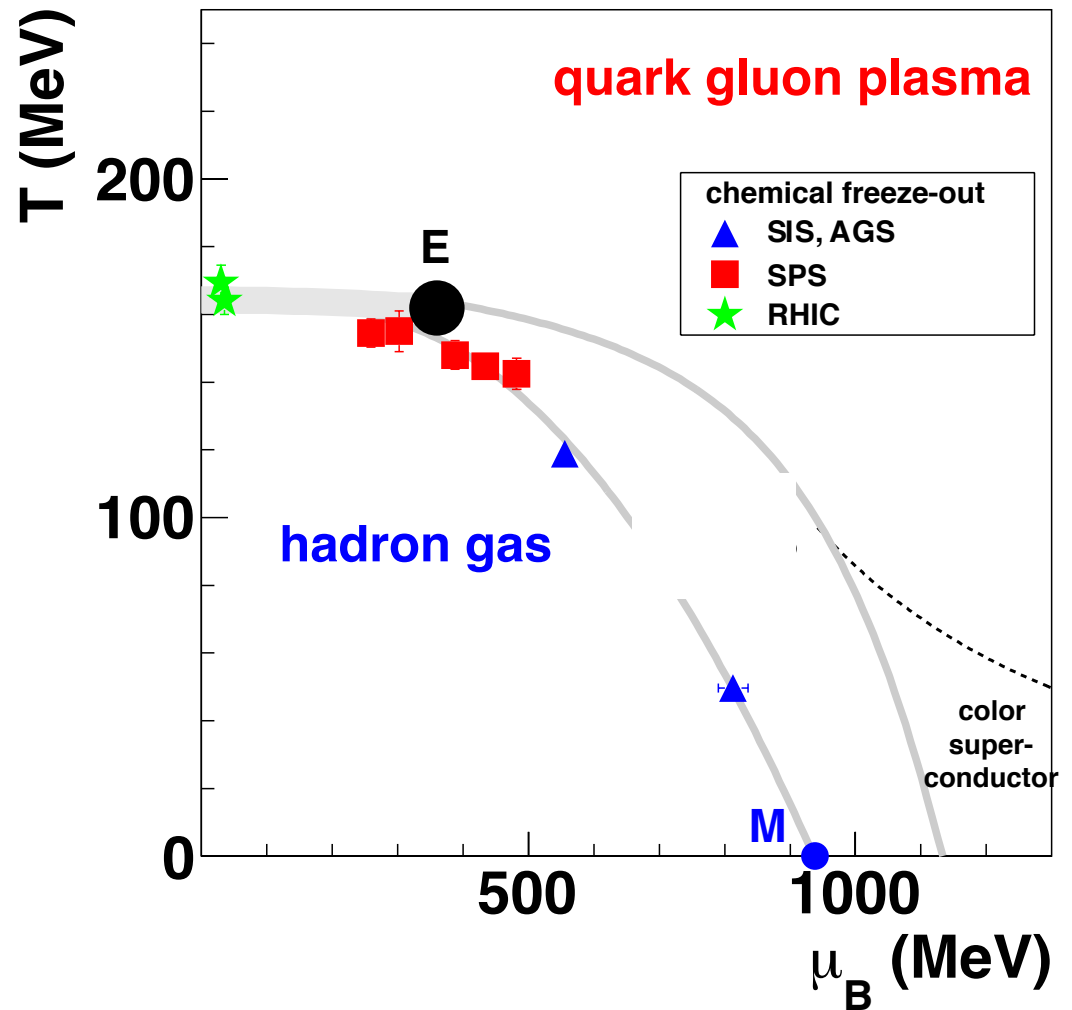


# Sketch of the QCD Phase Diagram

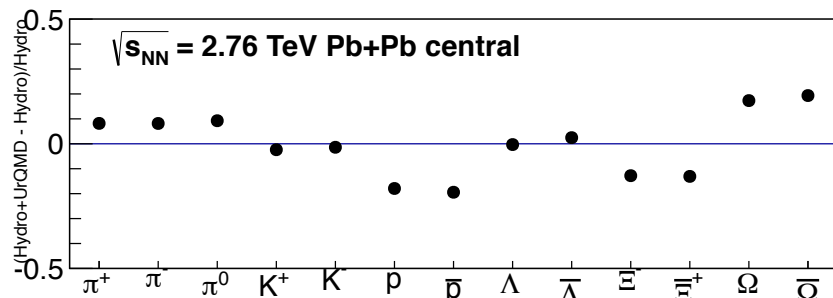
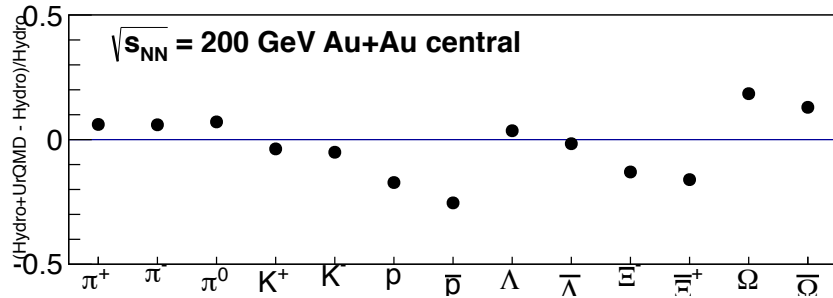
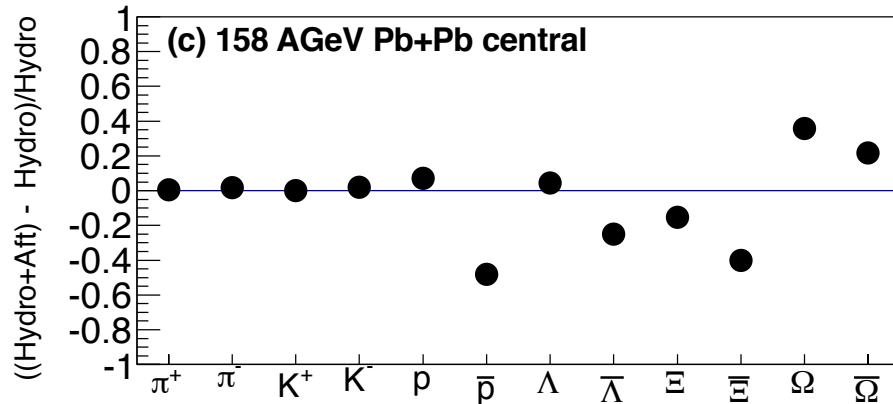
Assumption in the stat. model analysis:

Hadron abundances freeze out directly at QCD hadronization and thus survive the hadronic expansion stage

**TRUE?**



# UrQMD Study of Hadronic Expansion Effects on Hadron Yields



- Employ the recent hybrid version of UrQMD:
  - Hydrodynamic (3+1) phase until energy density  $< 1$  GeV/fm<sup>3</sup>, plus hadronic emission à la Cooper-Frye.
  - Attach UrQMD hadronic expansion as an "afterburner" stage.

- Compare hadronic yields directly after Cooper-Frye with those after the "afterburner" stage.

SERIOUS ANNIHILATION EFFECTS in baryon and antibaryon sector!

Regeneration also active.

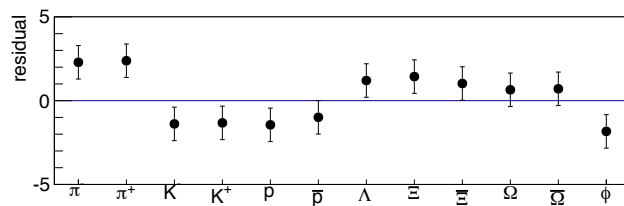
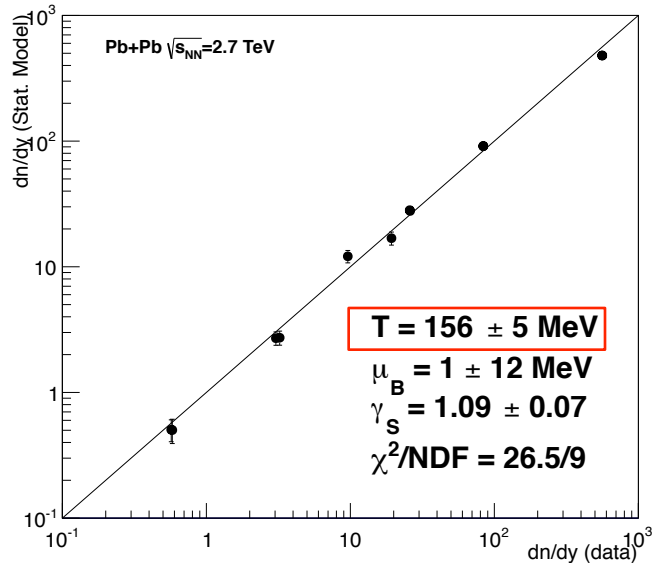
- Effect depends on energy

**Survival factors from UrQMD**

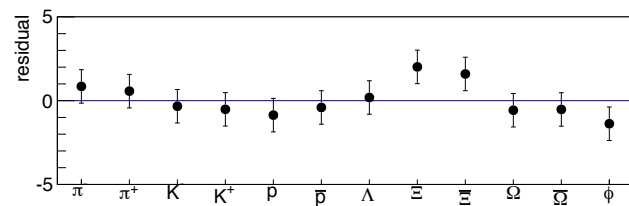
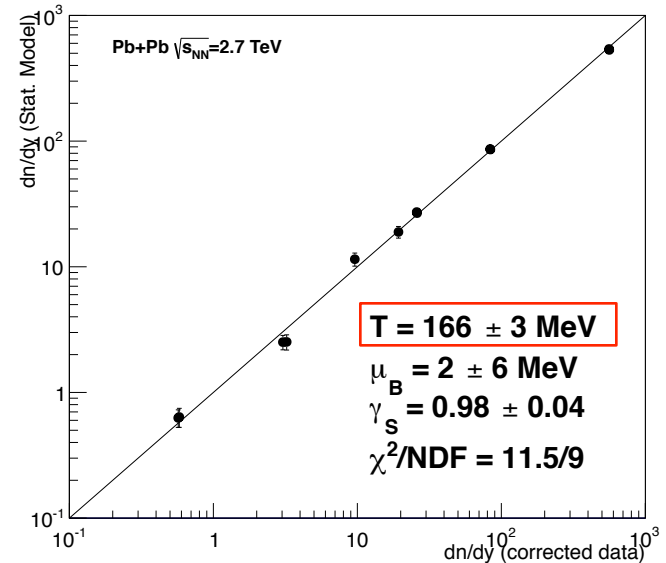
# LHC at 2.76 TeV, Central Pb+Pb

F.Becattini et al., arXiv:1212.2431 (accepted by PRL)

Standard SM fit



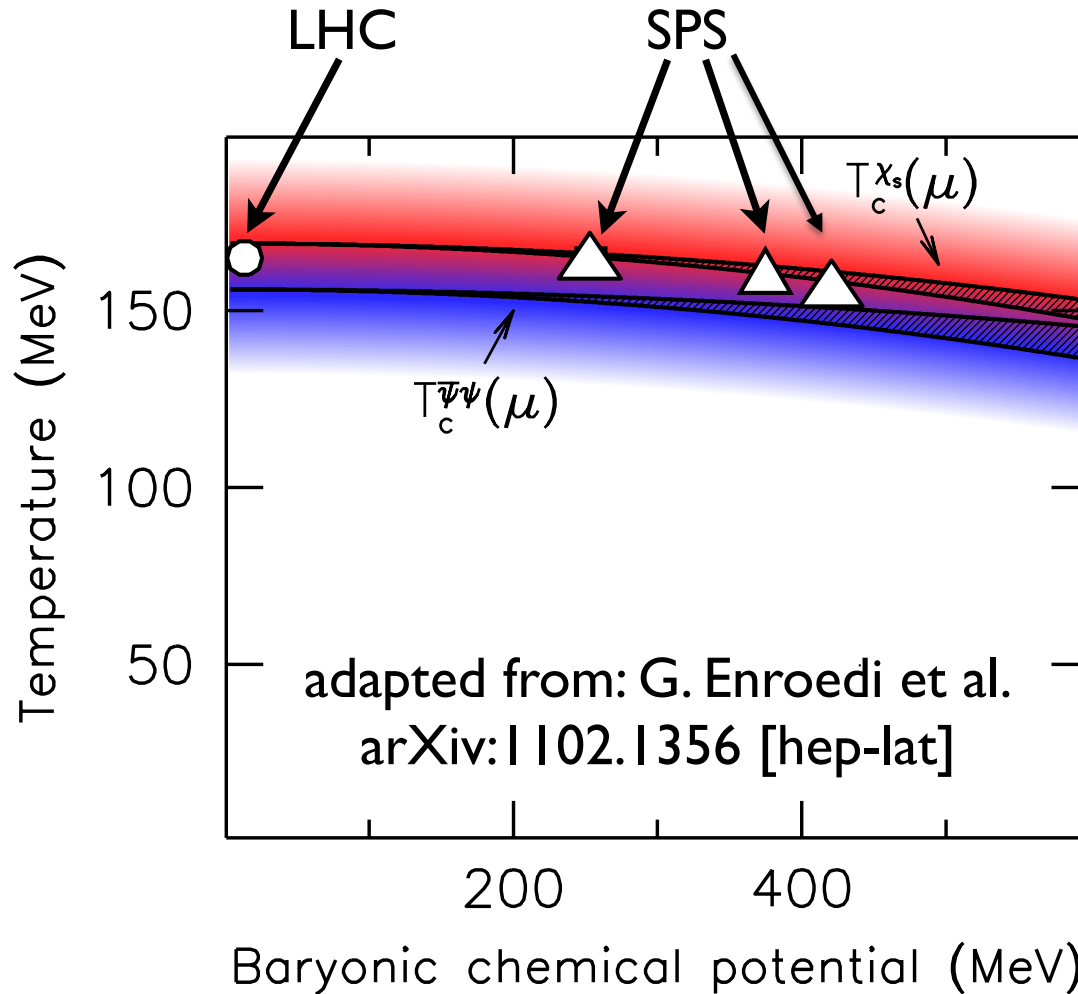
Apply correction factors



**T as in  $e^+e^-$  Annihilation**

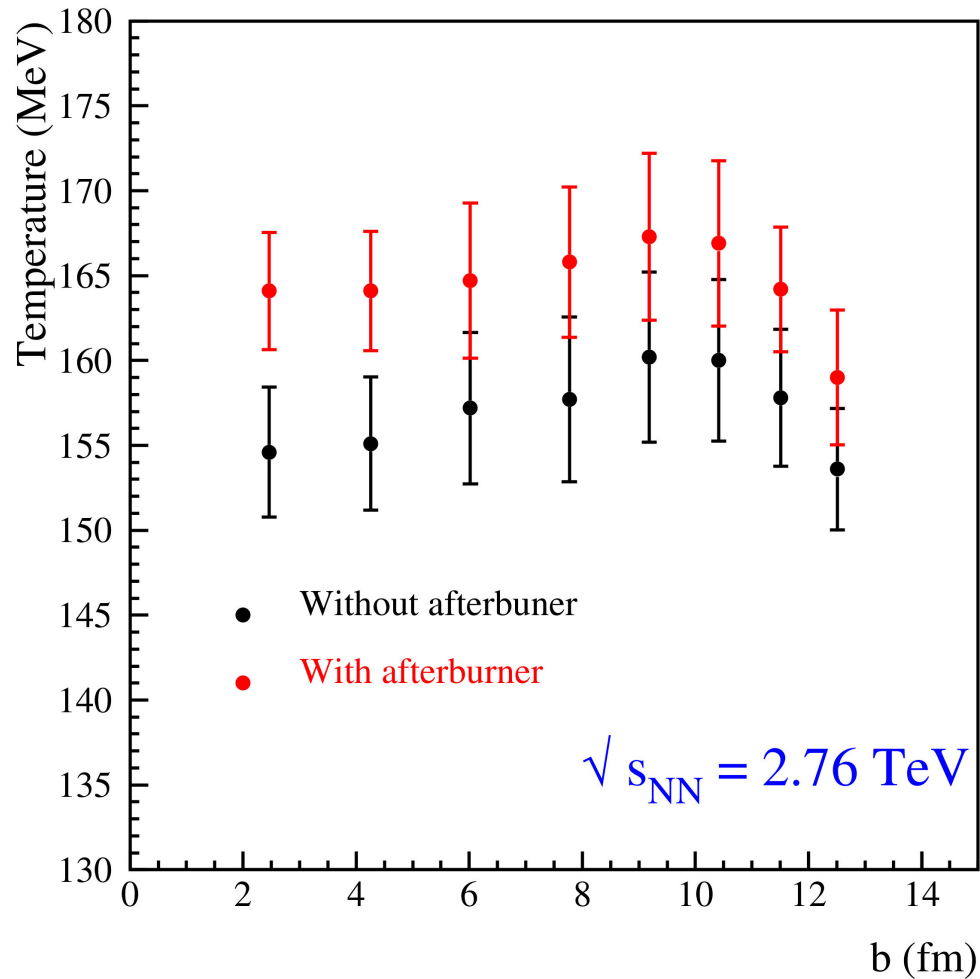
Data:ALICE collaboration, preliminary Quark Matter 2012

# Freeze-out revisited: The Phase Diagram



# Data: ALICE minimum bias Pb+Pb, 2.76 TeV

Stat. Mod.: Becattini et al., arXiv:1405.0710



# Afterburner increases T

Effect diminishes toward large b

Becattini et al., arXiv:1405.0710

