

Exotic few-body systems with a heavy meson

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in collaboration with

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XIth Quark Confinement and the Hadron Spectrum

Outline

1 Introduction

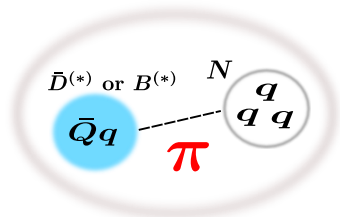
- Hadronic molecule
- Heavy Quark Spin Symmetry and one pion exchange potential

2 Results of $\bar{D}N$ and BN

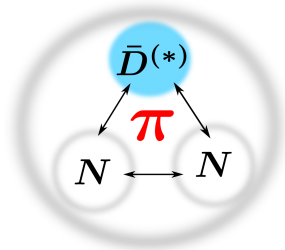
3 Results of $\bar{D}NN$ and BNN

4 Results in the heavy quark limit ($m_Q \rightarrow \infty$)

5 Summary



2-body system



3-body system

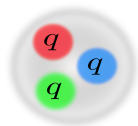
Exotic hadrons in the heavy quark region

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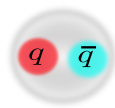
- Constituent quark model has been successfully applied to hadron spectra. : qqq and $q\bar{q}$ (Ordinary hadrons)

S. Godfrey and N. Isgur, PRD32(1985)189, S. Capstick and N. Isgur, PRD 34(1986)2809

Baryon



Meson



- New Exotic hadron** X, Y, Z : KEK, SLAC, ...
(in the heavy quark (c, b) sector)

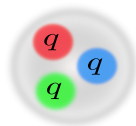
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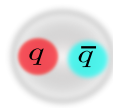
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Baryon



Meson



- **New Exotic hadron** X, Y, Z : KEK, SLAC, ...
(in the heavy quark (c, b) sector)
- How can we understand structures of the exotic hadrons?

Exotic hadrons in the heavy quark region

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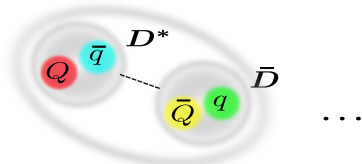
Baryon

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Multiquark states? (Meson)



Tetraquark
(Compact)



Hadronic molecule

Q : Heavy quark (c, b), q : Light quark (u, d)

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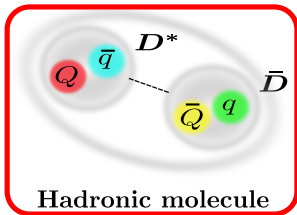
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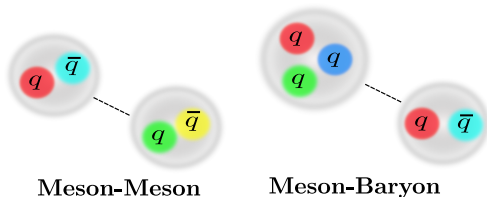
→ Candidates? $X(3872)(D\bar{D}^*?)$, $Z_b(B\bar{B}^*?)$...

S.K.Choi *et al.*, PRL91 (2003) 262001, A.Bondar, *et al.*, PRL108(2012)122001

Hadronic molecule

Introduction

Hadronic molecules



- Loosely bound states (resonances) of hadrons
→ Analogous to **Deuteron (proton-neutron)**

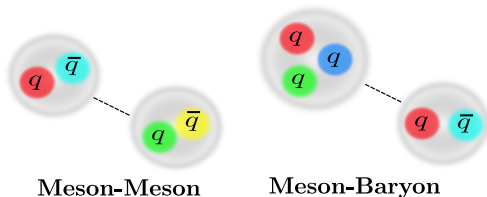
N. A. Tornqvist, Z. Phys. C **61** (1994) 525

- ▷ near the threshold, $E_B \sim 2.2$ MeV
- ▷ spatially expanded, $\langle r^2 \rangle^{1/2} \sim 3.9$ fm
- In Hadron composite systems,

Hadronic molecule

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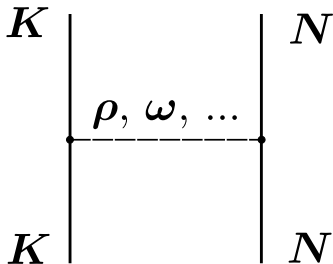
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Interactions between hadrons are important!

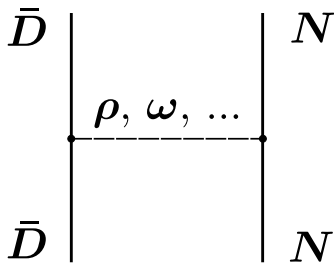
KN int. and $\bar{D}N$ int.

Introduction

Strange (Light)



Charm (Heavy)

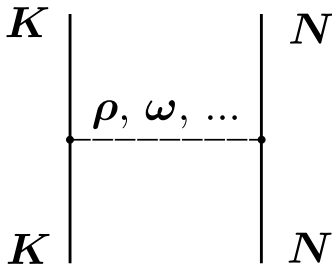


- Short range force (ρ, ω exchanges...) in KN .

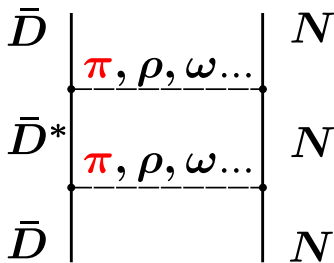
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Introduction

Strange (Light)



Charm (Heavy)



- Short range force (ρ, ω exchanges...) in KN .
- In the heavy sector, **one π exchange potential (OPEP)** is enhanced by the $\bar{D} - \bar{D}^*$ mixing. ($\Delta m_{\bar{D}\bar{D}^*}$ is small)
- The small mass splitting is induced by **the Heavy Quark Spin Symmetry!**
⇒ Interaction is different!

Heavy Quark Spin Symmetry and OPEP

Introduction

Heavy Quark Spin Symmetry (HQSS) N.Isgur, M.B.Wise,PRL66,1130

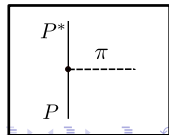
- HQSS appears in the heavy quark mass limit ($m_Q \rightarrow \infty$).
- Spin-spin interaction $\rightarrow 0$
e.g. Heavy meson ($\bar{Q}q$)

P^* P $\left\{ \begin{array}{l} \text{Heavy pseudoscalar meson } P(0^-) \text{ and} \\ \text{Heavy vector meson } P^*(1^-) \text{ are degenerate.} \end{array} \right.$

Indeed, mass splitting between P and P^* is small.

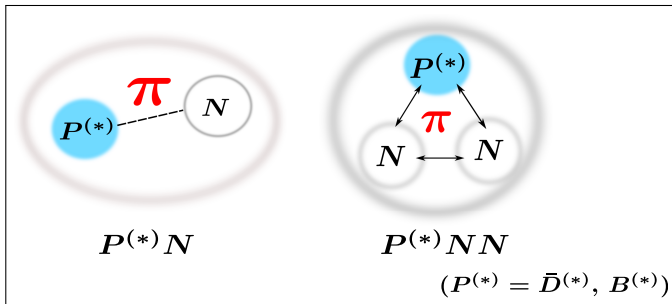
$$\left\{ \begin{array}{l} m_{B^*} - m_B \sim 45 \text{ MeV} \\ m_{D^*} - m_D \sim 140 \text{ MeV} \end{array} \right. \Leftrightarrow \begin{array}{l} \text{For strangeness sector} \\ m_{K^*} - m_K \sim 400 \text{ MeV} \end{array}$$

- ▷ OPEP appears through $PP^*\pi$ and $P^*P^*\pi$ vertices. ($PP\pi$ is forbidden.)
- ▷ Thanks to the degeneracy, **OPEP is enhanced**.



Main Subject

- Hadronic molecules formed by **Heavy meson-Nucleon with the π exchange potential.**



- $P = \bar{D}(\bar{c}q), B(\bar{b}q) \rightarrow$ No $q\bar{q}$ annihilation! **Genuinely exotic states!**
 \Leftrightarrow **KN molecules have not been found.**
(KN interaction is repulsion.)

$P^{(*)}N$ Interaction ($P^{(*)} = \bar{D}^{(*)}, B^{(*)}$): OPEP

$$V_{PN-P^*N}^{\pi} = -\frac{g_{\pi}g_{\pi NN}}{\sqrt{2}m_N f_{\pi}} \frac{1}{3} \left[\vec{\epsilon}^{\dagger} \cdot \vec{\sigma} C(r) + S_{\epsilon} T(r) \right] \vec{\tau}_P \cdot \vec{\tau}_N$$

$$V_{P^*N-P^*N}^{\pi} = \frac{g_{\pi}g_{\pi NN}}{\sqrt{2}m_N f_{\pi}} \frac{1}{3} \left[\vec{T} \cdot \vec{\sigma} C(r) + S_T T(r) \right] \vec{\tau}_P \cdot \vec{\tau}_N$$

S.Yasui and K.Sudoh PRD**80**(2009)034008

$C(r)$: Central force, $T(r)$: Tensor force

▶ $T(r)$ generates a strong attraction! \Leftrightarrow Deuteron

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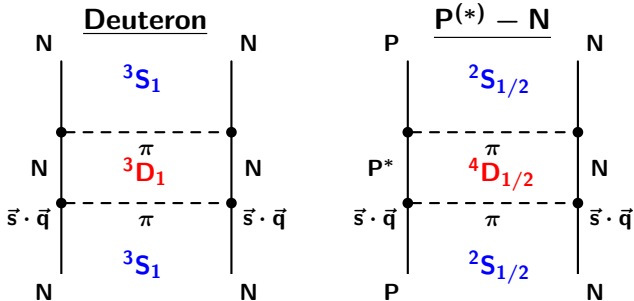
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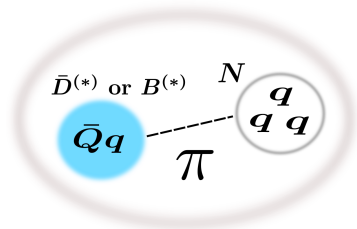
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Tensor force \Rightarrow ${}^3S_1 - {}^3D_1$

$PN({}^2S_{1/2}) - P^*N({}^4D_{1/2})$

Results of $P^{(*)}N$ states (2-body)



$\bar{D}N, BN$
Exotic states ($\bar{Q}q + qq$)

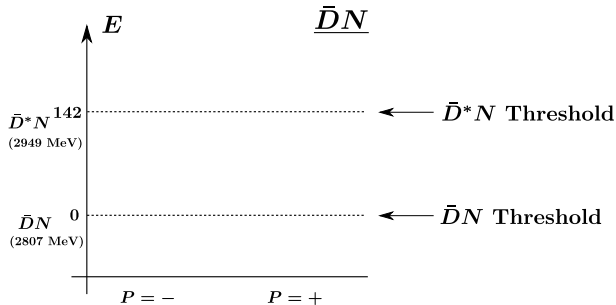
Bound state and Resonance

- We solve the coupled-channel Schrödinger equations for PN and P^*N channels.
- Interaction: π, ρ, ω exchange potentials

Numerical results: $\bar{D}N$ and $\bar{B}N$ for $I = 0$ (2-body)

$\bar{D}N$ and $\bar{B}N$ states

- $J^P = 1/2^\pm, 3/2^\pm, 5/2^\pm$ with $I = 0$
- Bound and Resonant states.



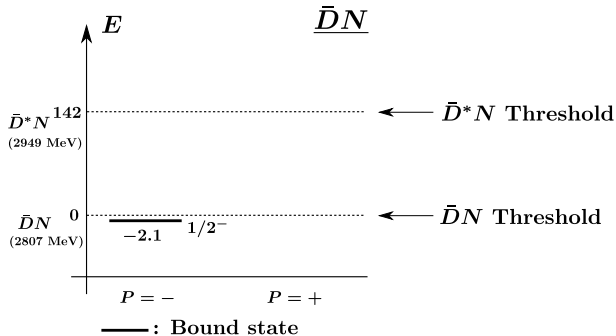
Unit: MeV

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD**84** 014032 (2011) and PRD**85** 054003 (2012)

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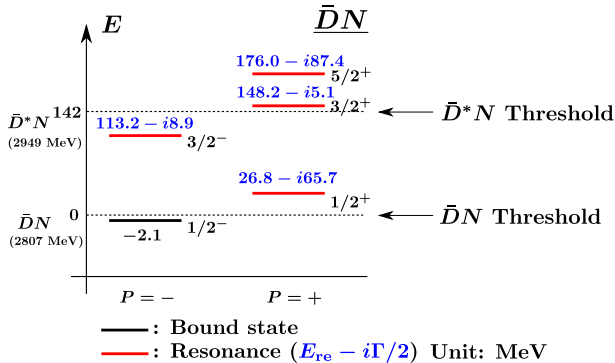
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- One bound state

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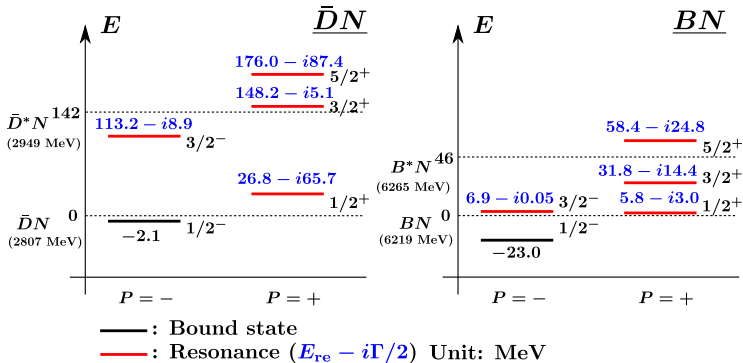
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- One bound state, and resonances!
- $E(BN) > E(\bar{D}N)$ due to large μ and small Δm_{BB^*} .

Numerical results: Bound state in $I(J^P) = 0(1/2^-)$

$\bar{D}N$ and BN states

- Expectation values of OPEP

Table: Expectation values of V_π ([MeV])

$\bar{D}N$	$\langle V_{\bar{D}N-\bar{D}^*N} \rangle$	$\langle V_{\bar{D}^*N-\bar{D}^*N} \rangle$
Central	-1.8	-4.0×10^{-3}
Tensor	-32.8	0.1

- The tensor force of π exchange potential generates **a strong attraction**. Especially, $\bar{D}N - \bar{D}^*N$ mixing is important.

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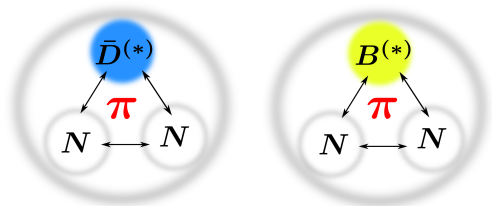
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Comment:

- ρ , ω exchanges play **a minor role** due to the cancellation of them.

Results of $P^{(*)}NN$ states (3-body)

Exotic dibaryon states: $\bar{D}^{(*)}NN$, $B^{(*)}NN$



with $J^P = 0^-, 1^-$ and $I = 1/2$

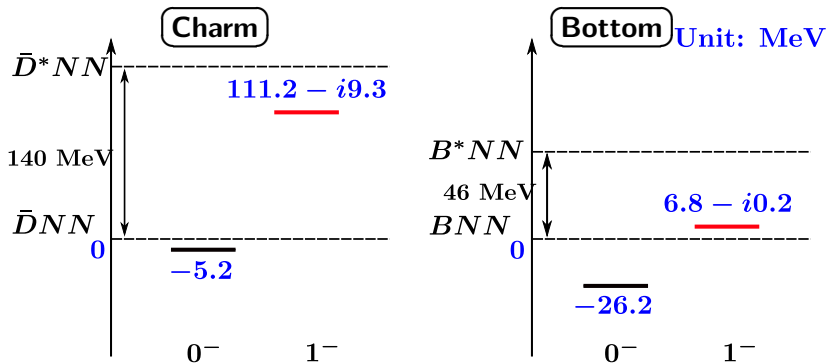
Bound state and Resonance

- $P^{(*)}N$ interaction: OPEP
- NN interaction: AV8' potential (B. S. Pudliner, *et al.*, PRC56(1997)1720)

Numerical Results: $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ for $I = 1/2$ (3-body)

$\bar{D}NN$ and BNN

- Bound states** for $J^P = 0^-$ and **Resonances** for $J^P = 1^-$ are found!
YY, S. Yasui, and A. Hosaka, NPA **927** (2014) 110



Energy expectation values of the bound states

$\bar{D}NN$ and BNN

- Energy expectation values

The bound state of $\bar{D}NN(0^-)$

$\bar{D}^{(*)}NN$	$\langle V_{\bar{D}N-\bar{D}^*N} \rangle$	$\langle V_{\bar{D}^*N-\bar{D}^*N} \rangle$	$\langle V_{NN} \rangle$
Central	-2.3	-0.1	-9.5
Tensor	-47.1	0.7	-0.2
LS	—	—	-0.03

YY, S. Yasui, and A. Hosaka, NPA **927** (2014) 110

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- Tensor force of $V_{\bar{D}N-\bar{D}^*N}$ generates **the strongest attraction**.
⇒ It dominates in the bound state.

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$\bar{D}NN$ and BNN

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In the bound states, $NN(0^+)$ subsystem dominates, while $NN(1^+)$ (=Deuteron) is minor.

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$\bar{D}NN$ and BNN

- Energy expectation values

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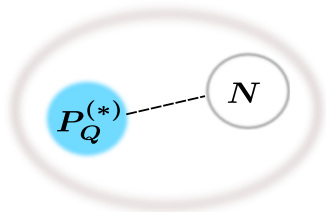
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$$\underline{J^P = 0^-, \bar{D}(0^-) \Rightarrow NN(0^+) \text{ is major.}}$$

Results of $P_Q N$ states ($m_Q \rightarrow \infty$)

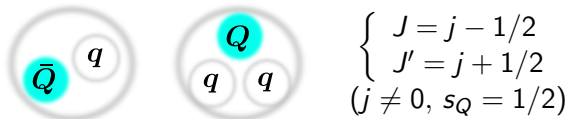


$$P_Q^{(*)} N \quad (m_{P_Q^{(*)}} - m_{P_Q} = 0)$$

Heavy quark mass limit

Heavy Quark Spin Symmetry (Again)

- In the ordinary heavy hadrons, the mass degeneracy is found.

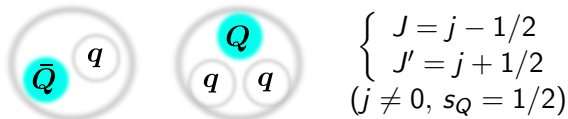


(j : Total angular momentum of Everything other than the heavy quark (Brown muck) $\Leftrightarrow \vec{J} = \vec{j} + \vec{s}_Q = \vec{L} + \vec{S}$)

e.g. $D(0^-) \sim D^*(1^-)$, $\Sigma_c(1/2^+) \sim \Sigma_c(3/2^+)$

Heavy Quark Spin Symmetry (Again)

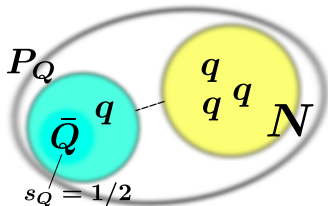
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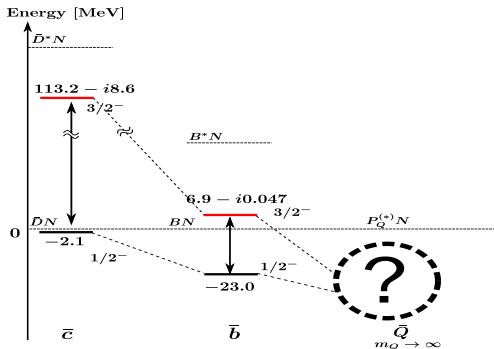
- Hadronic molecule (Multi-hadron system)



- Is a mass degeneracy realized?

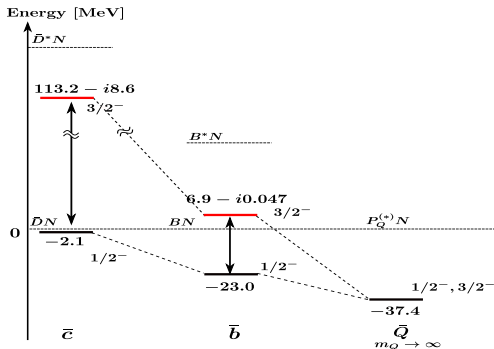
PN molecule in $m_Q \rightarrow \infty$

- In the finite heavy quark mass, **Bound states** ($J^P = 1/2^-$) and **resonances** ($3/2^-$) in $\bar{D}N$ and BN were found.



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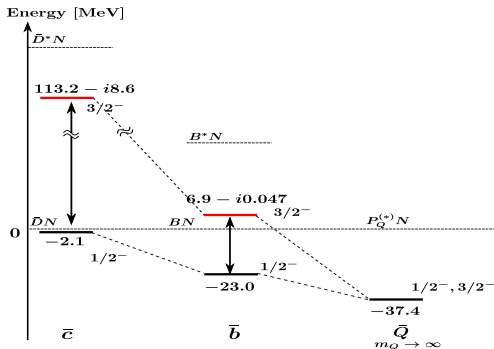


- Degenerate states** are found! ($1/2^-$ and $3/2^-$)

YY, S. Ohkoda, A. Hosaka, T. Hyodo, S. Yasui, arXiv:1402.5222 [hep-ph]

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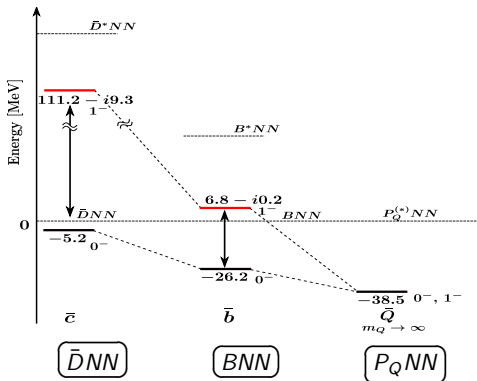


- Degenerate states** are found! ($1/2^-$ and $3/2^-$)
 \Rightarrow They belong to the **HQS doublet**.

YY, S. Ohkoda, A. Hosaka, T. Hyodo, S. Yasui, arXiv:1402.5222 [hep-ph]

Degenerate states in $P^{(*)}NN$ states ($m_Q \rightarrow \infty$)

- Energy-levels for $\bar{D}NN$, BNN and $P_Q NN$ ($m_Q \rightarrow \infty$)



- PNN states with $J^P = 0^-$ and 1^- are **degenerate!**

Summary

- We have investigated exotic baryons formed by $P^{(*)}N$ and $P^{(*)}NN$ with respecting the Heavy Quark Symmetry.
- For $\bar{D}^{(*)}N$ and $B^{(*)}N$, many bound states and resonances are found in $I = 0$.
- For the $\bar{D}NN$ and BNN states, we have found the bound states with $J^P = 0^-$ and resonances with $J^P = 1^-$ for $I = 1/2$.
- **Tensor force of π exchange** plays a crucial role to produce a strong attraction.
- The **PN – P*N mixing** component is important to yield these states.
- In $m_Q \rightarrow \infty$, we have obtained the degenerate states in hadronic molecular states.

Thank you for your kind attention.

Back up

Lagrangian($P^{(*)} - N$) ; π , ρ and ω exchanges

Heavy-light chiral lagrangian

R.Casalbuoni *et al.* PhysRept.281(1997)145

- $\mathcal{L}_{\pi HH} = -\frac{g_\pi}{\sqrt{2}f_\pi} \text{Tr} [H_b \gamma_\mu \gamma_5 \vec{\tau} \cdot \partial^\mu \vec{\pi}_{ba} \bar{H}_a]$
- $\mathcal{L}_{\nu HH} = -i\beta \text{Tr} [H_b \nu^\mu (\rho_\mu)_{ba} \bar{H}_a] + i\lambda \text{Tr} [H_b \sigma^{\mu\nu} F_{\mu\nu}(\rho)_{ba} \bar{H}_a]$

Heavy meson field

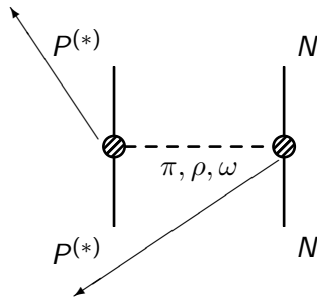
$$H_a = \frac{1+\not{\gamma}}{2} [\mathbf{P}_{a\mu}^* \gamma^\mu - \mathbf{P}_a \gamma^5], \quad \bar{H}_a = \gamma^0 H_a^\dagger \gamma^0$$

vector pseudoscalar

Bonn model

R. Machleidt, PRC63(2001)024001

- $\mathcal{L}_{\pi NN} = i g_{\pi NN} \bar{N}_b \gamma^5 N_a \vec{\tau} \cdot \vec{\pi}_{ba}$
- $\mathcal{L}_{\nu NN} = g_{\nu NN} \bar{N}_b \left(\gamma^\mu (\hat{\rho}_\mu)_{ba} + \frac{\kappa}{2m_N} \sigma_{\mu\nu} \partial^\nu (\hat{\rho}^\mu)_{ba} \right) N_a$



Lagrangian($P^{(*)} - N$) ; π , ρ and ω exchanges

Heavy-light chiral lagrangian

R.Casalbuoni *et al.* PhysRept.281(1997)145

- $\mathcal{L}_{\pi HH} = -\frac{g_{\pi}}{\sqrt{2}f_{\pi}} \text{Tr} [H_b \gamma_{\mu} \gamma_5 \vec{\tau} \cdot \partial^{\mu} \vec{\pi}_{ba} \bar{H}_a]$

From $D^{*} \rightarrow D\pi$ decay

- $\mathcal{L}_{\nu HH} = -i\beta \text{Tr} [H_b \nu^{\mu} (\rho_{\mu})_{ba} \bar{H}_a] + i\lambda \text{Tr} [H_b \sigma^{\mu\nu} F_{\mu\nu}(\rho)_{ba} \bar{H}_a]$

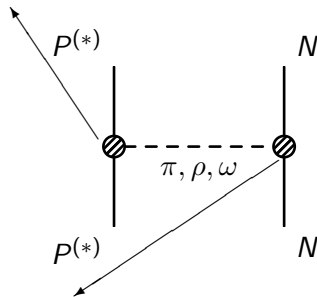
From radiative and semileptonic decays of heavy meson

Isola *et al.* PRD68,114001(2003)

Heavy meson field

$$H_a = \frac{1+\not{v}}{2} [\mathbf{P}_{a\mu}^* \gamma^{\mu} - \mathbf{P}_a \gamma^5], \quad \bar{H}_a = \gamma^0 H_a^{\dagger} \gamma^0$$

vector pseudoscalar



Bonn model

R. Machleidt, PRC63(2001)024001

From NN data

- $\mathcal{L}_{\pi NN} = i g_{\pi NN} \bar{N}_b \gamma^5 N_a \vec{\tau} \cdot \vec{\pi}_{ba}$

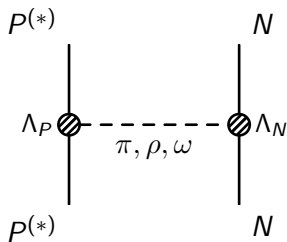
- $\mathcal{L}_{\nu NN} = g_{\nu NN} \bar{N}_b \left(\gamma^{\mu} (\hat{\rho}_{\mu})_{ba} + \frac{\kappa}{2m_N} \sigma_{\mu\nu} \partial^{\nu} (\hat{\rho}^{\mu})_{ba} \right) N_a$

These coupling constants are fixed!

Form factor and Cut-off parameter Λ

- Form factor F with cutoff $\Lambda = \Lambda_N, \Lambda_P$

$$F(\Lambda, \vec{q}) = \frac{\Lambda_N^2 - m_\pi^2}{\Lambda_N^2 + |\vec{q}|^2} \frac{\Lambda_P^2 - m_\pi^2}{\Lambda_P^2 + |\vec{q}|^2}$$



Form factor and Cut-off parameter Λ

- Form factor F with cutoff $\Lambda = \Lambda_N, \Lambda_P$

$$F(\Lambda, \vec{q}) = \frac{\Lambda_N^2 - m_\pi^2}{\Lambda_N^2 + |\vec{q}|^2} \frac{\Lambda_P^2 - m_\pi^2}{\Lambda_P^2 + |\vec{q}|^2}$$

- Λ_N is fixed to reproduce the properties of Deuteron.
(NN system with Bonn potential)

$$\Rightarrow \Lambda_N = 830 (\pi), 846 (\pi\rho\omega) \text{ MeV}$$

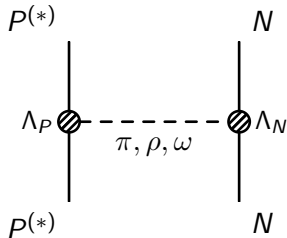
- Λ_P is determined by the ratios of radii of P and N . We assume $\Lambda_P/\Lambda_N = r_N/r_P$.

$$\begin{cases} \Lambda_D = 1.35\Lambda_N \\ \Lambda_B = 1.29\Lambda_N \end{cases}$$

S.Yasui and K.Sudoh PRD**80**,034008

$$\Rightarrow \Lambda_D = 1121 \text{ MeV}(\pi), 1142 \text{ MeV}(\pi\rho\omega)$$

$$\Lambda_B = 1070 \text{ MeV}(\pi), 1091 \text{ MeV}(\pi\rho\omega)$$



Cut-off parameters are also fixed!

Central force and Tensor force

- Central force $C(r)$ and Tensor force $T(r)$

$$C(r) = \int \frac{d^3q}{(2\pi)^3} \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} e^{i\vec{q}\cdot\vec{r}} F(\Lambda_P, \vec{q}) F(\Lambda_N, \vec{q})$$

$$S_T(\hat{r}) T(r) = \int \frac{d^3q}{(2\pi)^3} \frac{-\vec{q}^2}{\vec{q}^2 + m_\pi^2} S_T(\hat{q}) e^{i\vec{q}\cdot\vec{r}} F(\Lambda_P, \vec{q}) F(\Lambda_N, \vec{q})$$

$$F(\Lambda, \vec{q}) = \frac{\Lambda^2 - m_\pi^2}{\Lambda^2 + \vec{q}^2}$$

- Spin operators

$$\vec{\varepsilon}^\pm = (\mp 1/\sqrt{2}, \pm i\sqrt{2}, 0), \quad \vec{\varepsilon}^{(0)} = (0, 0, 1)$$

$$T^i = i\varepsilon^{ijk} \varepsilon_j^\dagger \varepsilon_k$$

- Coupling constants

$$g_\pi = 0.59 \text{ for } \bar{D} \text{ and } B, \quad g_{\pi NN}^2/4\pi = 13.6$$

$$(g_{D^*D\pi} = 2\sqrt{m_D m_{D^*}} g_\pi / f_\pi = 17.9)$$

The bound state in $I(J^P) = 0(1/2^-)$

$\bar{D}N$ and BN states

- Expectation values of meson exchange potentials
- $\bar{D}^{(*)}N(1/2^-)$: $\bar{D}N(^2S_{1/2})$, $\bar{D}^*N(^2S_{1/2}, ^4D_{1/2})$

The bound state of $\bar{D}N(1/2^-)$

Components	V_π	V_ρ	V_ω
$\langle \bar{D}N(S) V \bar{D}N(S) \rangle$	0.0	-2.7	3.6
$\langle \bar{D}N(S) V \bar{D}^*N(S) \rangle$	-2.4	-5.2	1.0
$\langle \bar{D}N(S) V \bar{D}^*N(D) \rangle$	-35.2	3.4	-0.6
$\langle \bar{D}^*N(S) V \bar{D}^*N(S) \rangle$	0.4	0.7	0.1
$\langle \bar{D}^*N(S) V \bar{D}^*N(D) \rangle$	-5.0	0.6	-0.1
$\langle \bar{D}^*N(D) V \bar{D}^*N(D) \rangle$	3.7	-0.9	0.4
Total	-38.6	-4.4	4.4

- The tensor force of π exchange potential generates a **strong attraction**. Especially, $\bar{D}N - \bar{D}^*N$ mixing is important.
- ρ, ω exchanges play a **minor role** due to the cancellation of them.