

HIGGS THEORY

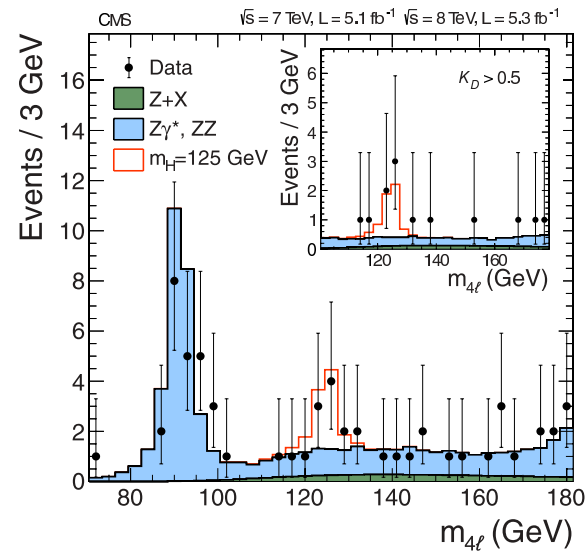
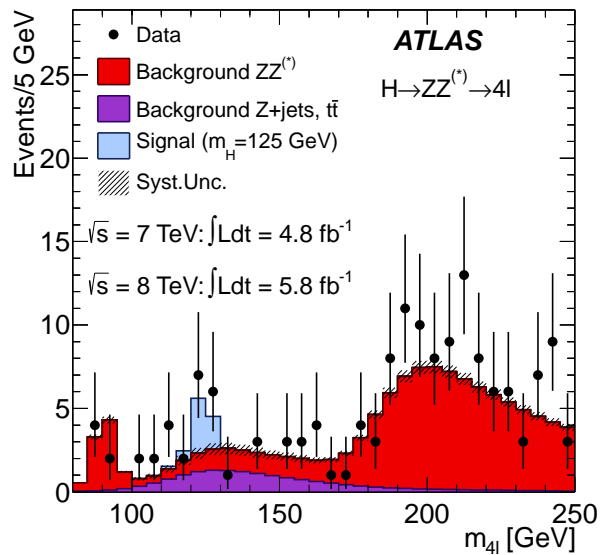
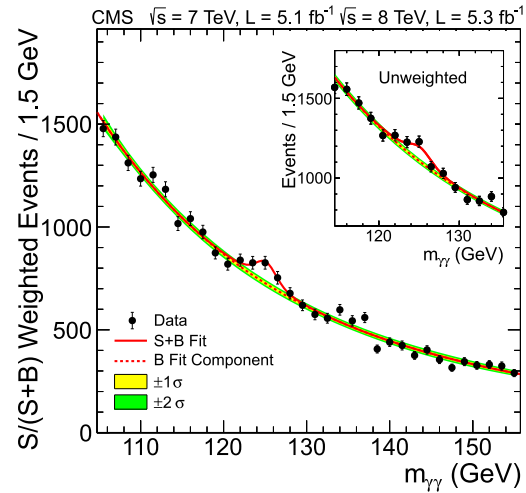
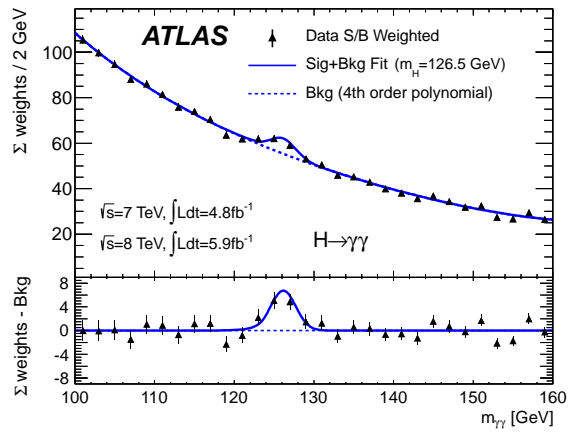
Michael Spira (PSI)

- I Introduction
- II Higgs Boson Production
- III Conclusions

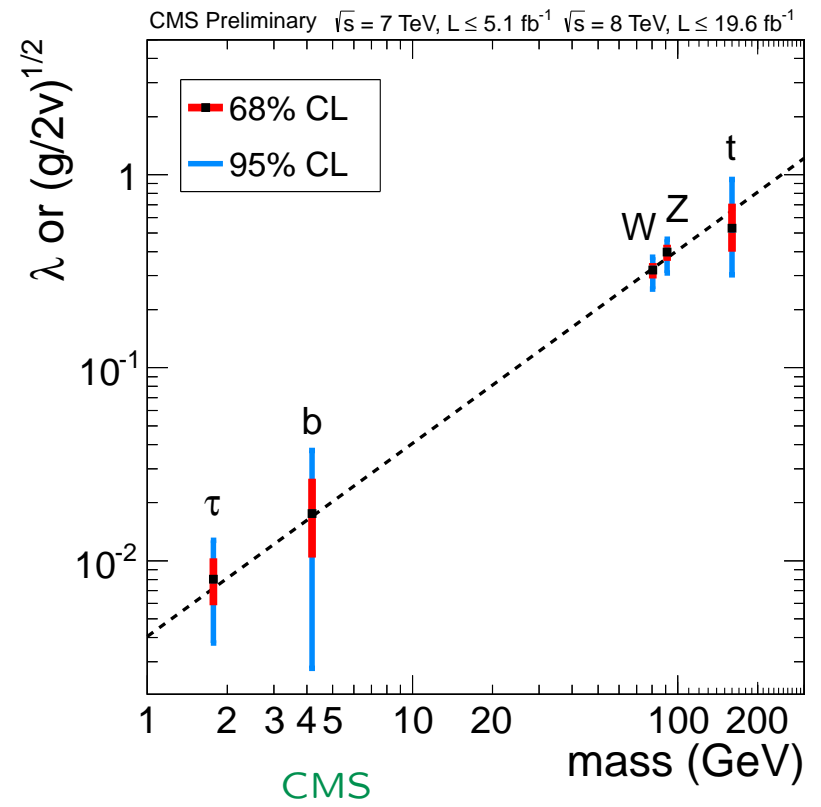
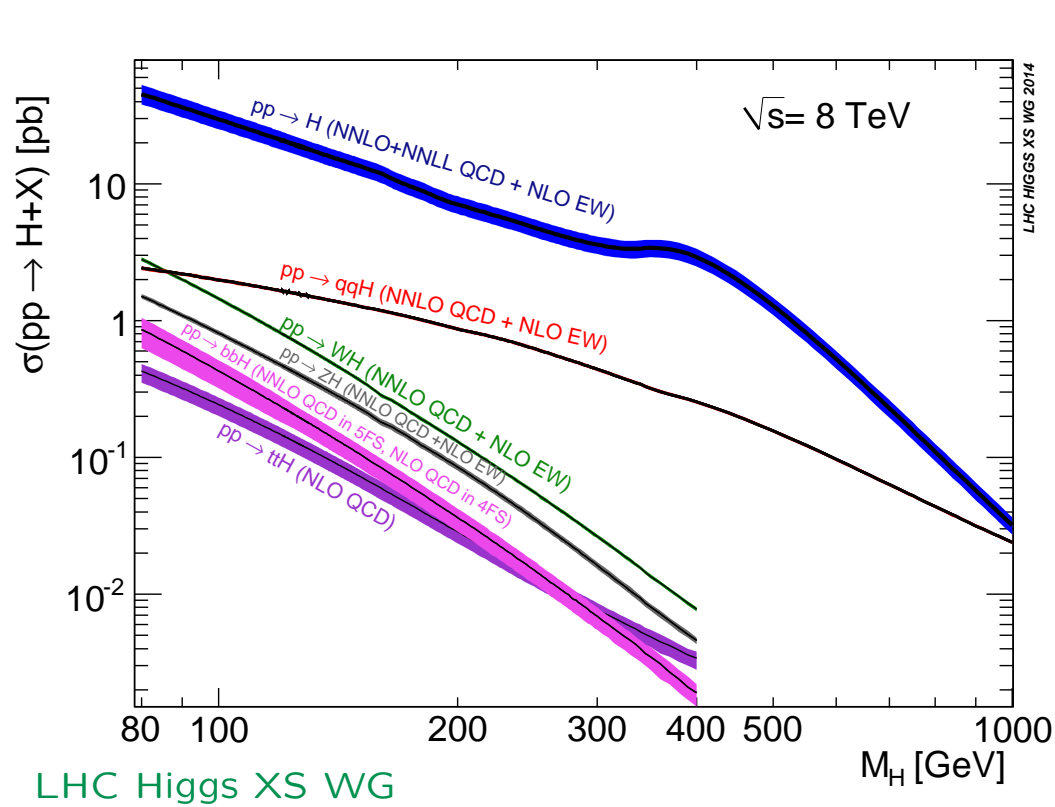
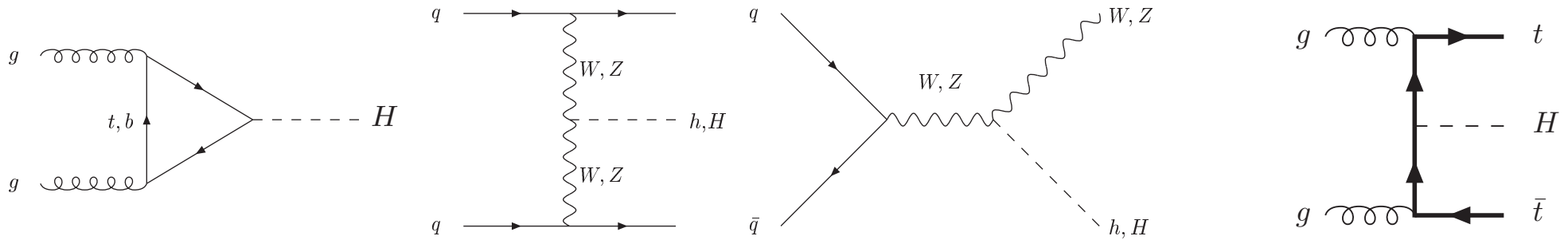
I INTRODUCTION

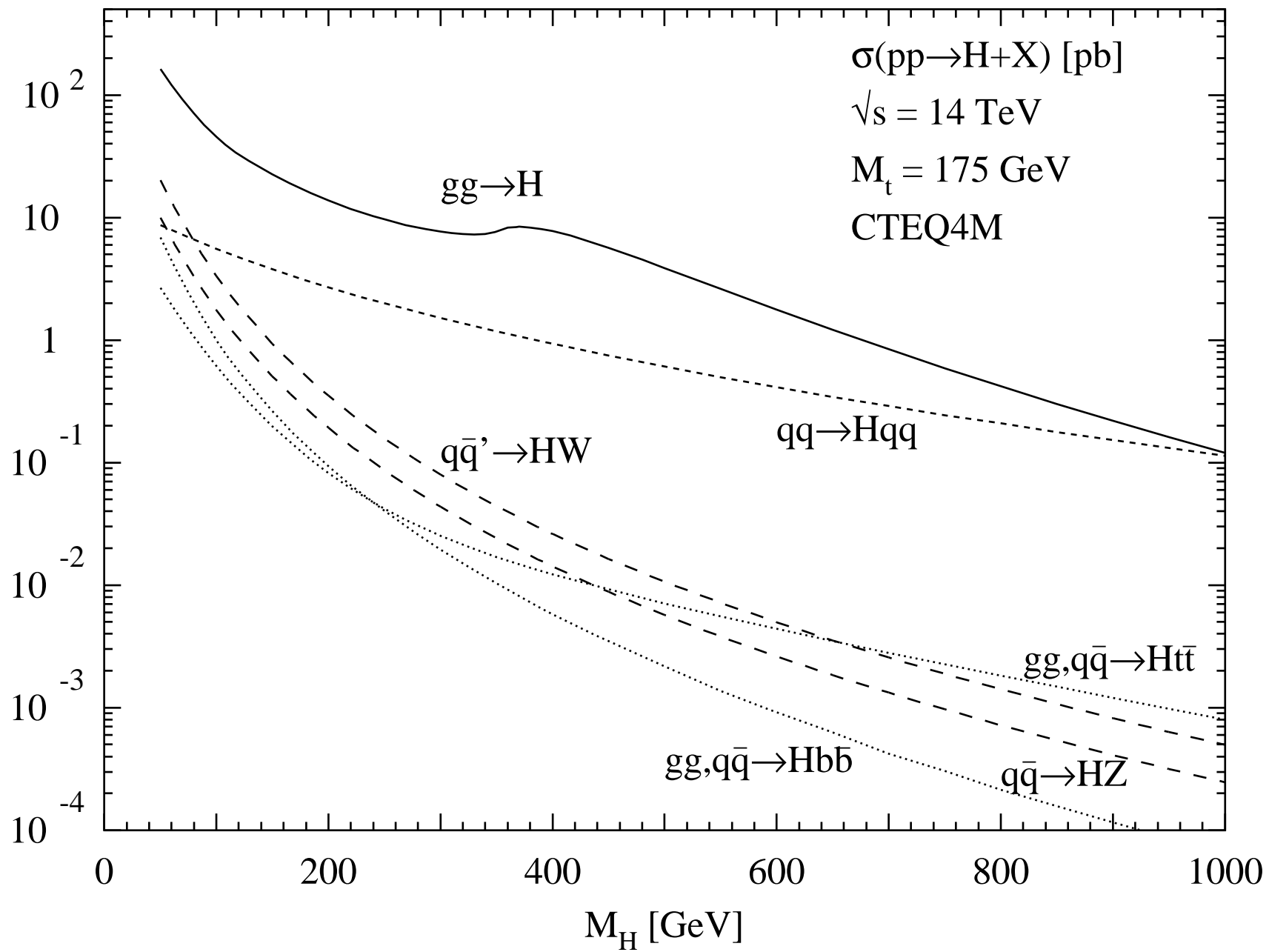
(i) Standard Model

- we have found the Higgs: $M_H \sim 125$ GeV
- $gg \rightarrow H$ dominant



• Higgs Boson Production





(ii) MSSM

• 2 Higgs doublets $\xrightarrow{\text{ESB}}$ 5 Higgs bosons: h, H, A, H^\pm

• LO: 2 input parameters: $M_A, \text{tg}\beta = \frac{v_2}{v_1}$

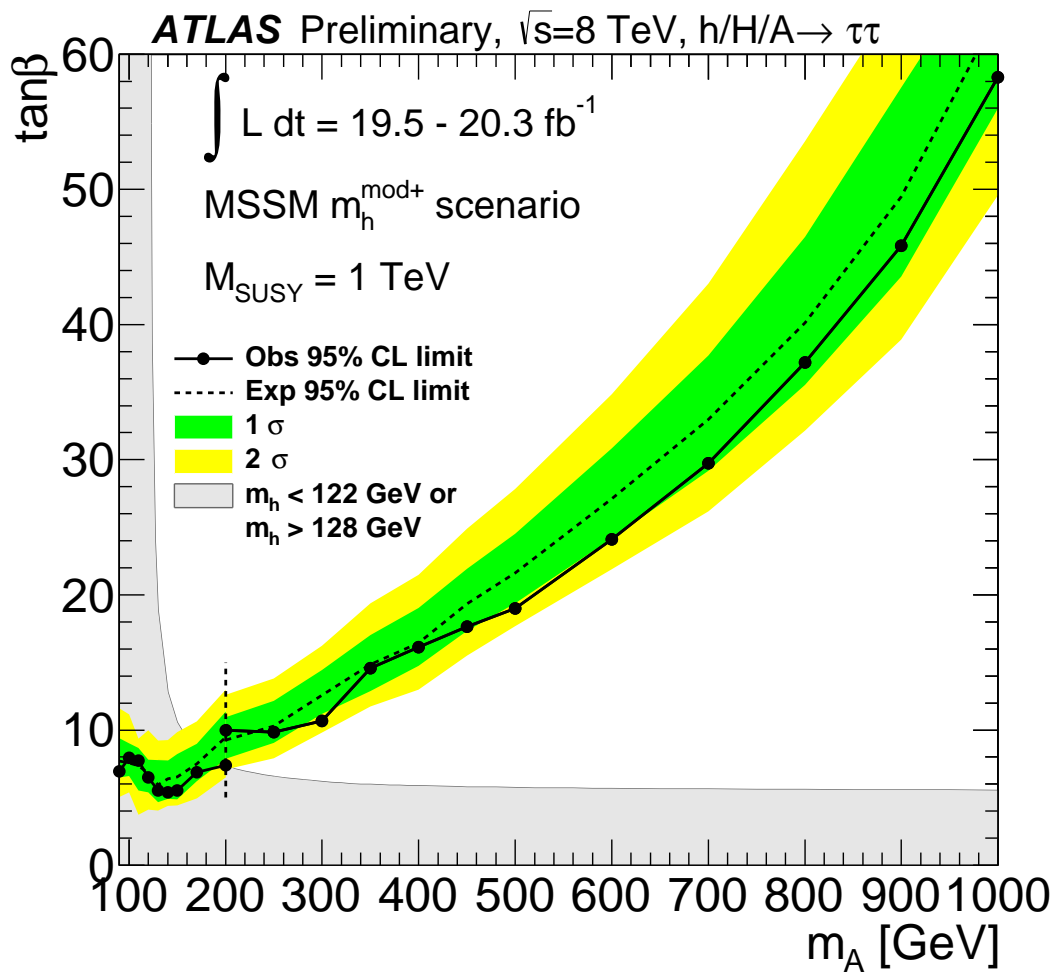
• radiative corrections $\propto m_t^4 \log \frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \rightarrow \boxed{M_h \lesssim 135 \text{ GeV}}$

Haber
Carena,...
Heinemeyer,...
Zhang
Slavich,...
...

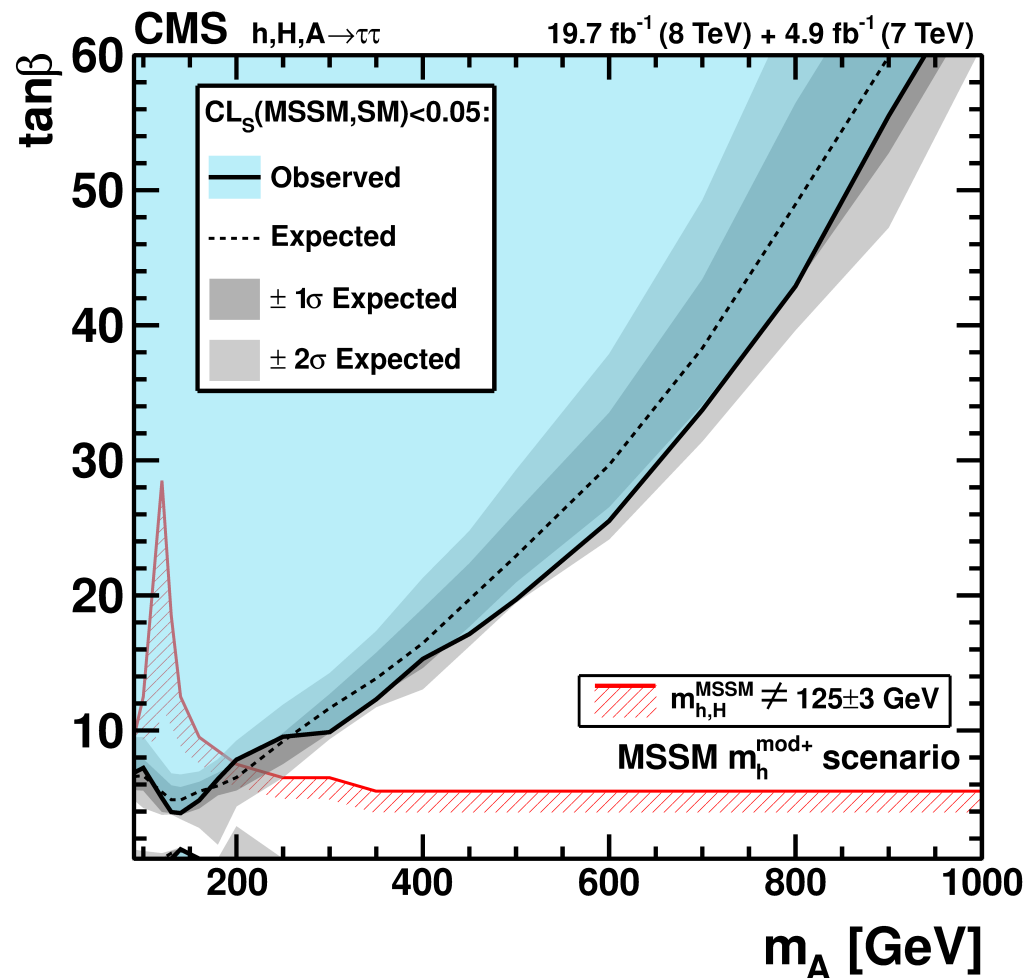
• Yukawa couplings: $\text{tg}\beta \uparrow \Rightarrow g_u^\phi \downarrow \quad g_d^\phi \uparrow \quad g_V^\phi \downarrow$

• LHC: $gg \rightarrow \phi$ dominant for $\text{tg}\beta \lesssim 10$
 $gg \rightarrow \phi b\bar{b}$ dominant for $\text{tg}\beta \gtrsim 10$

$$gg \rightarrow b\bar{b}\phi^0, \quad gg \rightarrow \phi^0$$



$$\phi^0 \rightarrow \tau^+ \tau^-$$



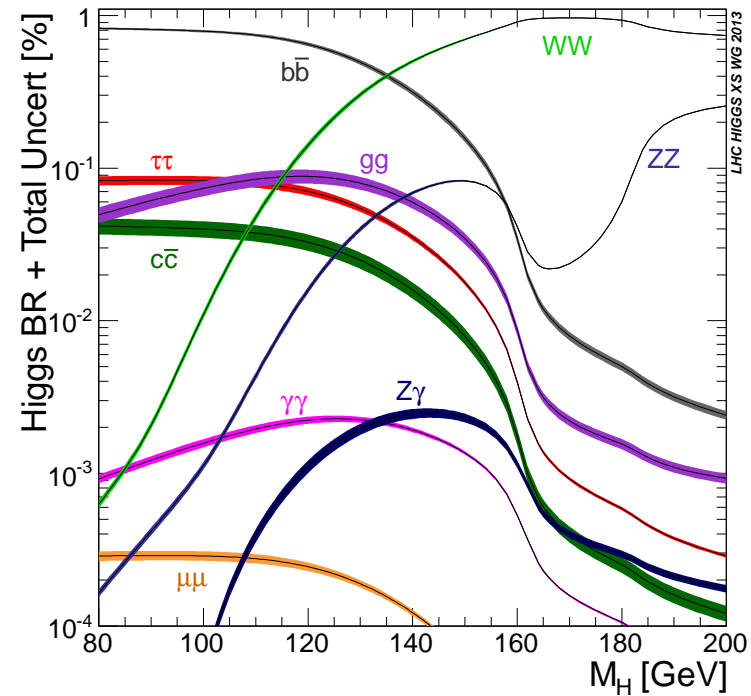
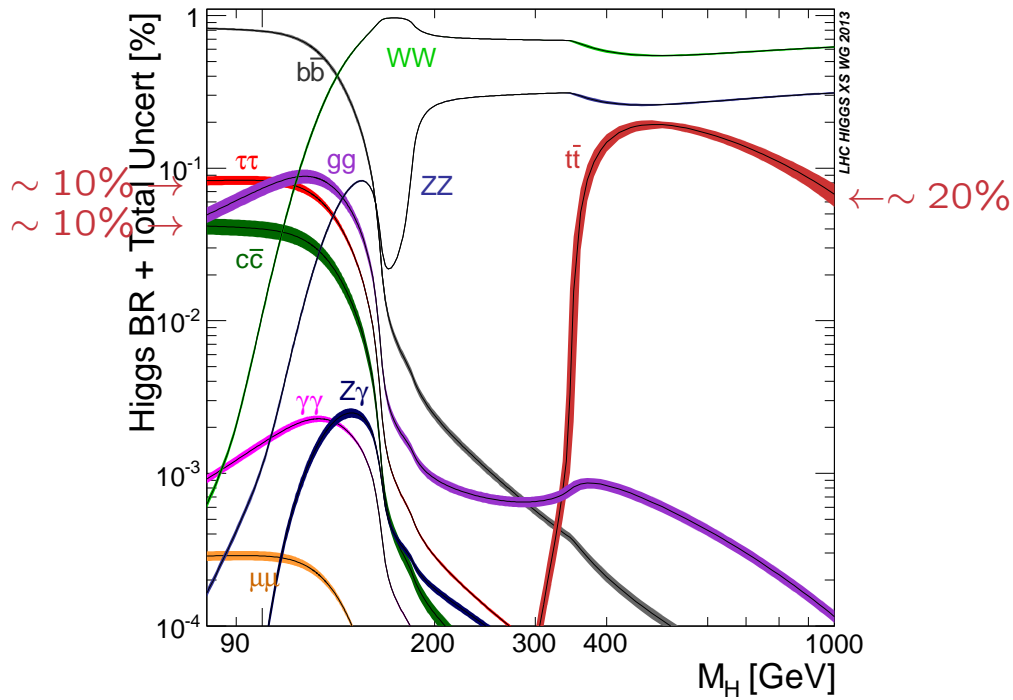
Partial Width	QCD	Electroweak	Total	
$H \rightarrow b\bar{b}/c\bar{c}$	$\sim 0.1\%$	$\sim 1\text{--}2\%$ for $M_H \lesssim 135\text{GeV}$	$\sim 2\%$	NNNNLO / NLO
$H \rightarrow \tau^+\tau^-/\mu^+\mu^-$		$\sim 1\text{--}2\%$ for $M_H \lesssim 135\text{GeV}$	$\sim 2\%$	NLO
$H \rightarrow t\bar{t}$	$\lesssim 5\%$	$\lesssim 2\text{--}5\%$ for $M_H < 500\text{GeV}$ $\sim 0.1(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 5\%$ $\sim 5\text{--}10\%$	(NNN)NLO / LO
$H \rightarrow gg$	$\sim 3\%$	$\sim 1\%$	$\sim 3\%$	NNNLO approx. / NLO
$H \rightarrow \gamma\gamma$	$< 1\%$	$< 1\%$	$\sim 1\%$	NLO / NLO
$H \rightarrow Z\gamma$	$< 1\%$	$\sim 5\%$	$\sim 5\%$	(N)LO / LO
$H \rightarrow WW/ZZ \rightarrow 4f$	$< 0.5\%$	$\sim 0.5\%$ for $M_H < 500\text{GeV}$ $\sim 0.17(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 0.5\%$ $\sim 0.5\text{--}15\%$	(N)NLO

- QCD: variation of Higgs widths for scale by factor 2 and 1/2
elw: missing HO estimated from known structure at NLO
 $M_H \gtrsim 500$ GeV: Higgs self-interactions dominate error
different uncertainties added linearly for each channel
- parametric uncertainties:

$$m_t = 172.5 \pm 2.5 \text{ GeV} \quad \alpha_s(M_Z) = 0.119 \pm 0.002$$

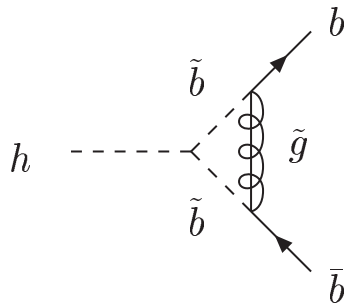
$$m_b(m_b) = 4.16 \pm 0.06 \text{ GeV} \quad m_c(m_c) = 1.28 \pm 0.03 \text{ GeV}$$
 different uncertainties added quadratically for each channel
- total uncertainties: parametric & theor. uncertainties added linearly

HDECAY & Prophecy4f



Denner, Heinemeyer, Puljak, Rebuszi, S.

- MSSM: large SUSY-QCD corrections to $\phi^0 \rightarrow b\bar{b}$



$$\propto \frac{\alpha_s}{\pi} \frac{m_{\tilde{g}} \mu t g \beta}{M_{SUSY}^2} \sim \Delta_b$$

Hall, ...
 Carena, ...
 Nierste, ...
 Häfliger, ...
 Noth, S.
 Mihaila, Reisser
 etc.

SUSY-QCD Corrections to $b\bar{b}\phi^0$

$[\Delta \lesssim 1\%]$

$$\mathcal{L}_{eff} = -\lambda_b \bar{b}_R \left[\phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b$$

$$\begin{aligned} = & -m_b \bar{b} \left[1 + i\gamma_5 \frac{G^0}{v} \right] b - \frac{m_b/v}{1 + \Delta_b} \bar{b} \left[g_b^h \left(1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) h \right. \\ & \left. + g_b^H \left(1 + \Delta_b \frac{\text{tg}\alpha}{\text{tg}\beta} \right) H - g_b^A \left(1 - \frac{\Delta_b}{\text{tg}^2\beta} \right) i\gamma_5 A \right] b \end{aligned}$$

$$\Delta_b = \Delta_b^{QCD(1)} + \Delta_b^{elw(1)}$$

$$\Delta_b^{QCD(1)} = \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2)$$

$$\Delta_b^{elw(1)} = \frac{\lambda_t^2(\mu_R)}{(4\pi)^2} \mu A_t \text{tg}\beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2)$$

$$I(a, b, c) = -\frac{ab \log \frac{a}{b} + bc \log \frac{b}{c} + ca \log \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

\Rightarrow resummed Yukawa couplings \tilde{g}_b^Φ

Carena, Garcia, Nierste, Wagner
Guasch, Häfliger, S.

small α_{eff} scenario [modified]

$$\text{tg}\beta = 30$$

$$M_{\tilde{Q}} = 800 \text{ GeV}$$

$$M_{\tilde{g}} = 1000 \text{ GeV} \quad \leftarrow$$

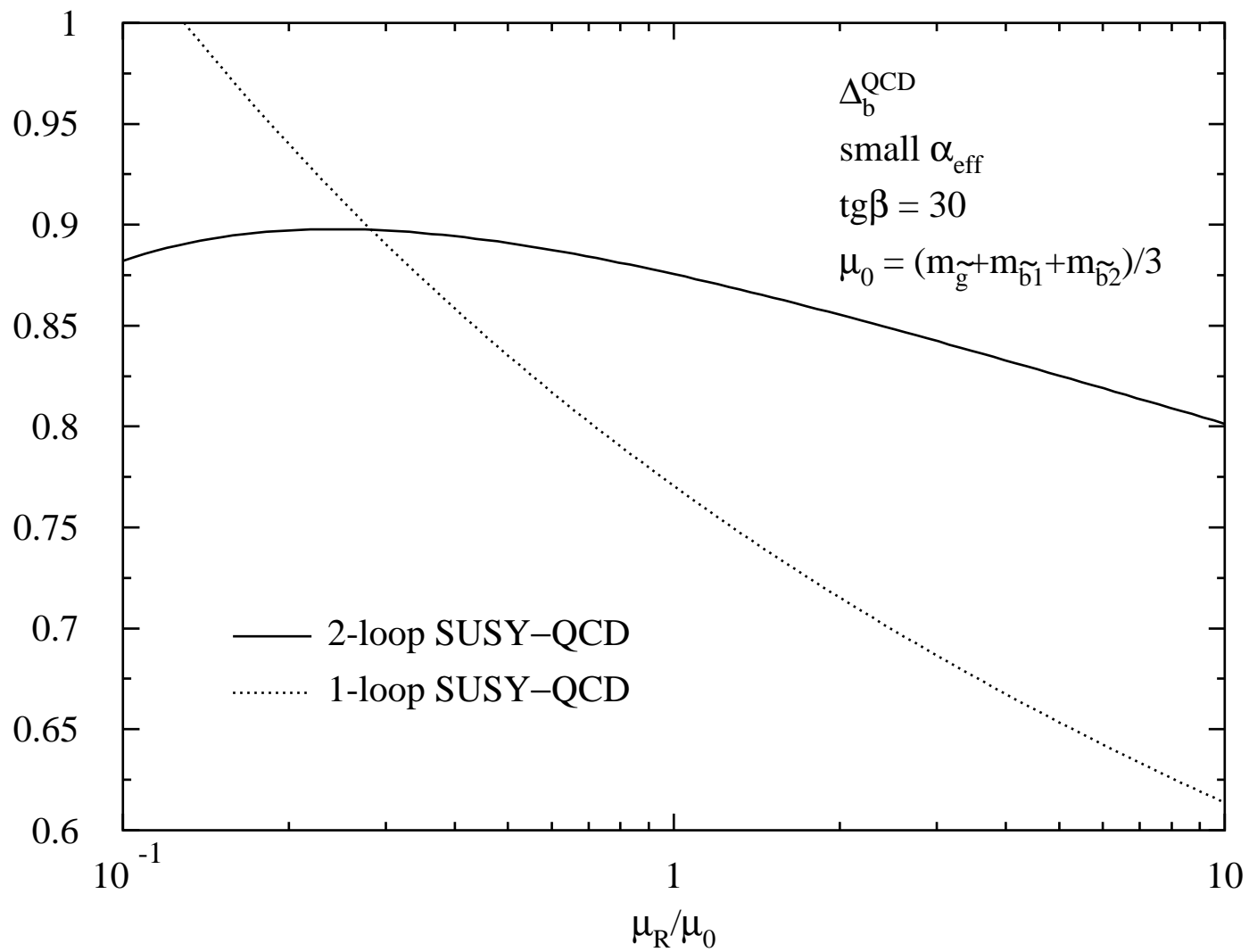
$$M_2 = 500 \text{ GeV}$$

$$A_b = A_t = -1.133 \text{ TeV}$$

$$\mu = 2 \text{ TeV}$$

$$m_{\tilde{t}_1} = 679 \text{ GeV} \quad m_{\tilde{t}_2} = 935 \text{ GeV}$$

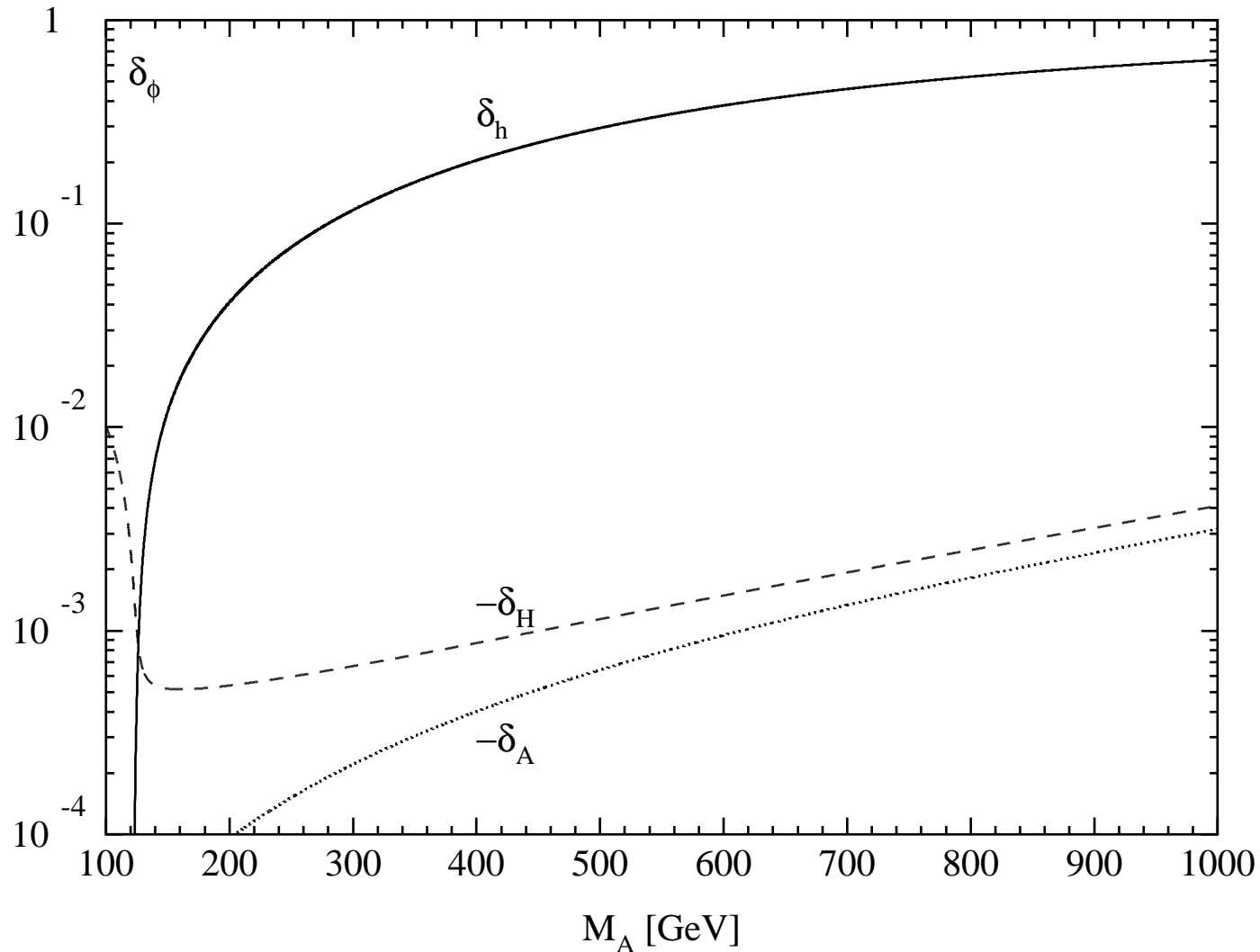
$$m_{\tilde{b}_1} = 601 \text{ GeV} \quad m_{\tilde{b}_2} = 961 \text{ GeV}$$



Noth, S.
 (Mihaila, Reisser)

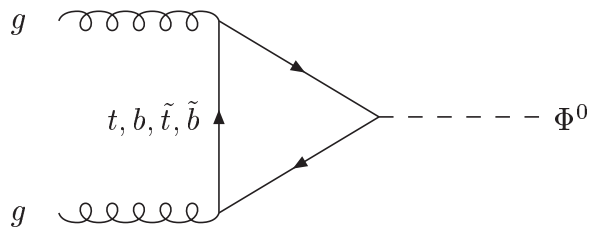
$$\Gamma[\Phi \rightarrow b\bar{b}] = \frac{3G_F M_\Phi}{4\sqrt{2}\pi} \bar{m}_b^2(M_\Phi) \Delta_{\text{QCD}} \tilde{g}_b^{\Phi^2} [1 + \delta_\Phi]$$

$$M_A^2 \gg M_Z^2 : \text{tg}\alpha \rightarrow -\frac{1}{\text{tg}\beta} \Rightarrow \tilde{g}_b^h \rightarrow \frac{1}{1 + \Delta m_b} \left(1 - \frac{\Delta m_b}{\text{tg}\alpha \text{tg}\beta} \right) \rightarrow 1$$



II HIGGS BOSON PRODUCTION

(i) $gg \rightarrow h/H$



Georgi,...

Gamberini,...

S., Djouadi, Graudenz, Zerwas
Dawson, Kauffman

- NLO QCD corrections: $\sim 10 \dots 100\%$

- NNLO calculated for $m_t \gg M_\phi \Rightarrow$ further increase by 20–30%
[mass effects small]

Harlander, Kilgore

Anastasiou, Melnikov

Ravindran, Smith, van Neerven

Marzani, Ball, Del Duca, Forte, Vicini
Harlander, Ozeren
Pak, Rogal, Steinhauser

- NNNLO estimated for $m_t \gg M_\phi \Rightarrow$ scale stabilization
scale dependence: $\Delta \lesssim 10 - 15\%$

Moch, Vogt

Ravindran

de Florian, Mazzitelli, Moch, Vogt

Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger

Ball, Bonvini, Forte, Marzani, Ridolfi

- NNLL soft gluon resummation: 5 – 10%

Catani, de Florian, Grazzini, Nason
Ravindran
Ahrens, Becher, Neubert, Yang
Ball, Bonvini, Forte, Marzani, Ridolfi

- elw. corrections: -4% – 6%

Aglietti, . . .
Degrassi, Maltoni
Actis, Passarino, Sturm, Uccirati

- QCD corrections to squark loops: 10–100%

Mühlleitner, S.
Bonciani, Degrassi, Vicini

- genuine SUSY–QCD corrections: 10–100%
[$\leftarrow \Delta_b$ @ large $\tan\beta$]

Harlander, Steinhauser, Hofmann
Degrassi, Slavich
Anastasiou, Beerli, Daleo
Mühlleitner, Rzehak, S.

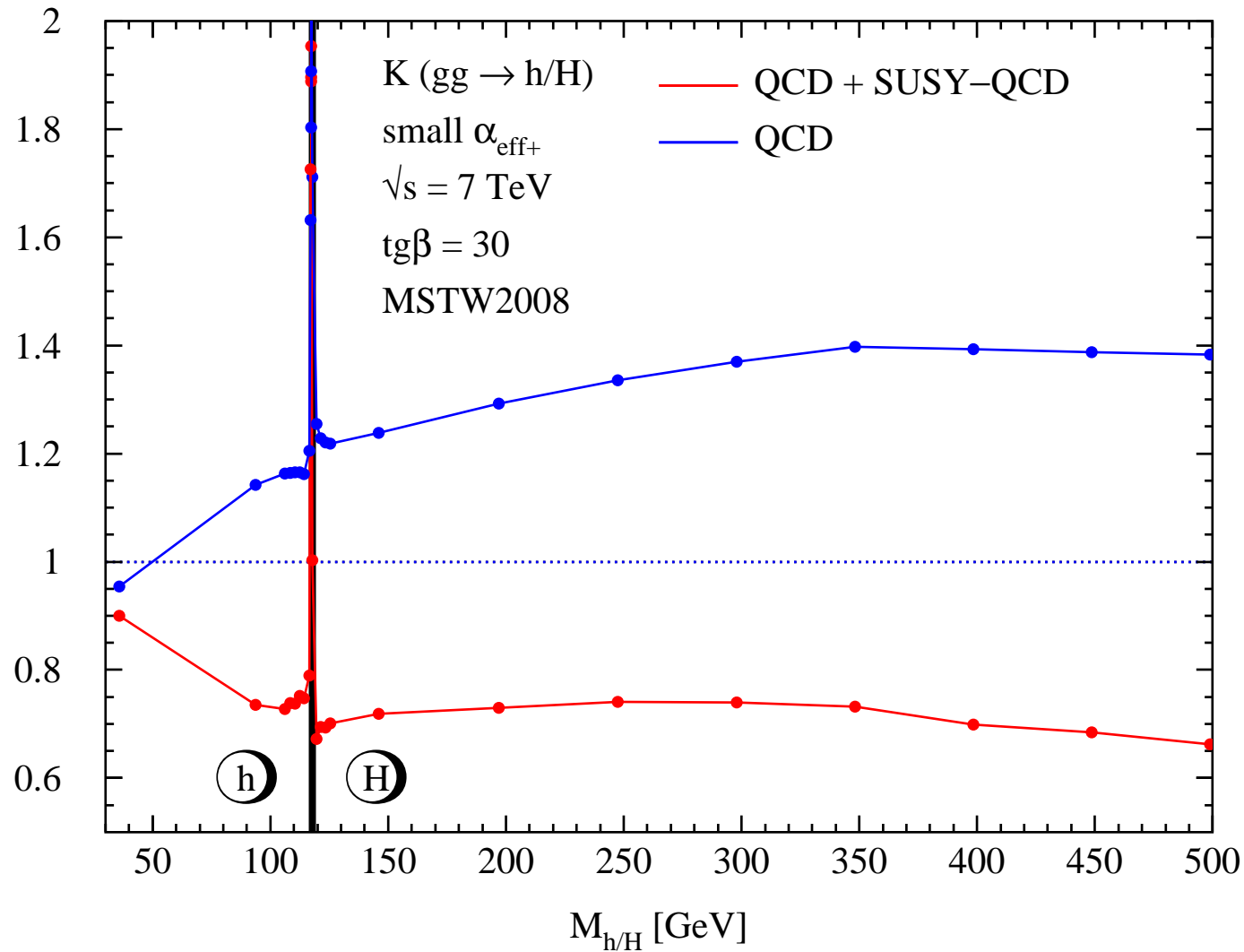
- SUSY-elw. corrections unknown

- impl. of $gg \rightarrow \phi$ in POWHEG including mass effects @ NLO

Bagnaschi, Degrassi, Slavich, Vicini

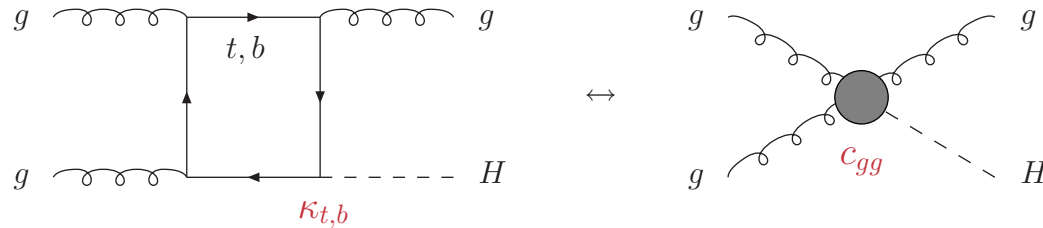
$$\sigma(gg \rightarrow \Phi) = \sigma_{LO}(g_t^\Phi, \tilde{g}_b^\Phi) [1 + \delta_{QCD} + \delta_{SQCD}]$$

PRELIMINARY

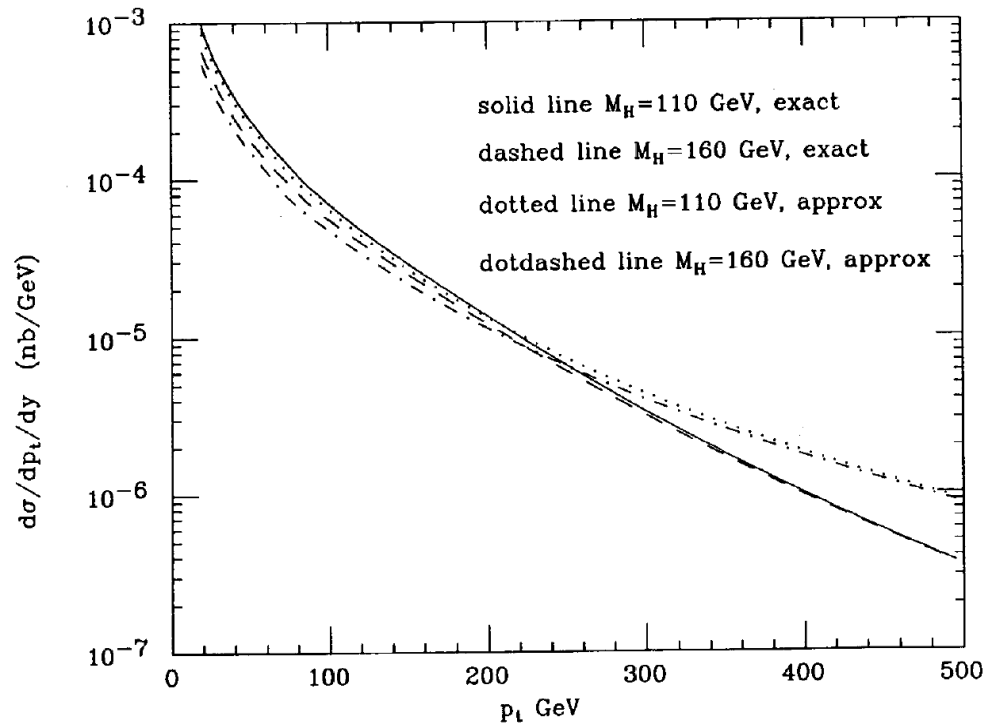


Mühlleitner, Rzehak, S.

Higgs p_T (or how to prove that ggF is loop-mediated)



- distinction dim4 \leftrightarrow dim5



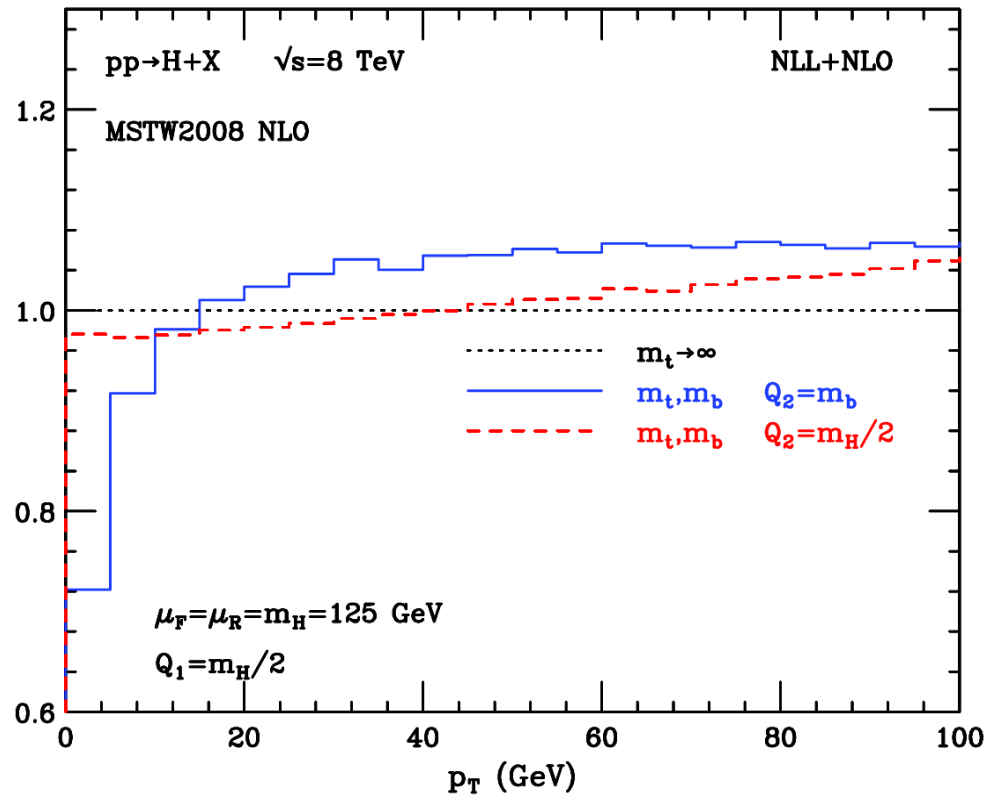
$m_t = 160$ GeV

Ellis, Hinchliffe, Soldate, van der Bij

- QCD corrections large [$m_t^2 \gg M_H^2, p_{TH}^2$]
 [$\leftarrow b$ @ large $\tan\beta$: LO, soft spectrum]

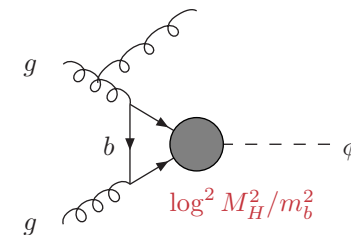
Schmidt
 de Florian, Grazzini, Kunszt
 Ravindran, Smith, van Neerven
 Kauffman
 Balazs, Yuan
 Bozzi, Catani, de Florian, Grazzini

- factorization: $p_T \ll 2m_b \rightarrow Q \sim m_b$ [\leftarrow POWHEG, MC@NLO]

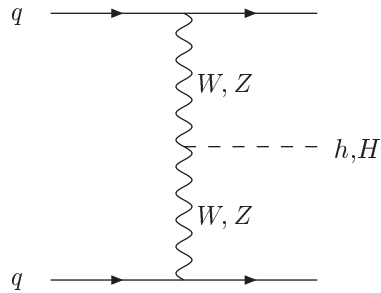


Grazzini, Sargsyan

- Sudakov form factor \rightarrow unresummed logs



(ii) W/Z fusion: $pp \rightarrow W^*W^*/Z^*Z^* \rightarrow h/H$



Cahn, Dawson
Hikasa
Atarelli, Mele, Pitolli

- QCD corrections \leftarrow DIS: $\sim 10\%$

Han, Valencia,
Willenbrock
Figy, Oleari, Zeppenfeld
Berger, Campbell

2-loop: $\lesssim 1\%$ [approx]

Bolzano, Maltoni, Moch, Zaro

- elw. corrections: $\sim 10\%$

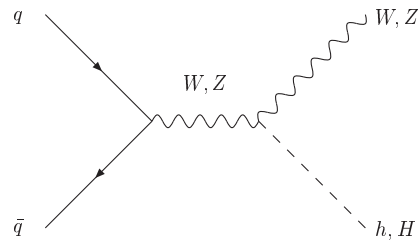
Ciccolini, Denner, Dittmaier

- full NLO SUSY-elw. corrections

Hollik, Rzehak, Plehn, Rauch
Figy, Palmer, Weiglein

- implemented in VBFNLO

(iii) Higgs–strahlung: $pp \rightarrow W^*/Z^* \rightarrow W/Z + h/H$



Glashow,...
Kunszt,...

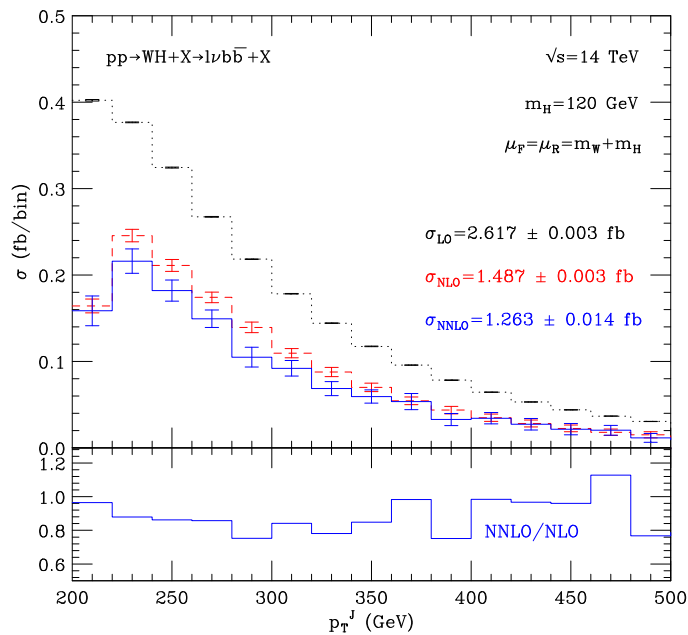
- QCD corrections \leftarrow DY: $\sim 30\%$
2-loop: $\lesssim 5\%$
- SUSY-QCD corrections small
- electroweak corrections: $\sim -10\%$
- WH : fully exclusive @ NNLO QCD

Han, Willenbrock
Brein, Djouadi, Harlander

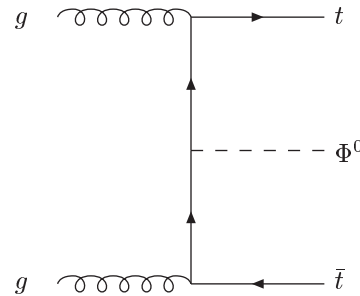
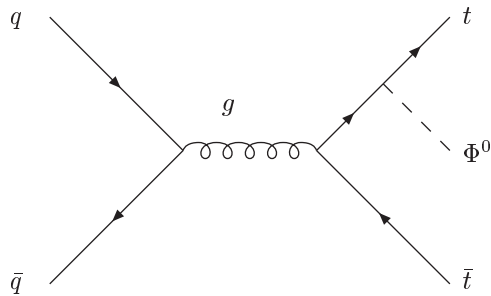
Djouadi, S.

Ciccolini, Dittmaier, Krämer

Ferrera, Grazzini, Tramantano



(iv) Bremsstrahlung: $pp \rightarrow t\bar{t} + h/H/A$



dominant

Kunszt
Gunion
Marciano, Paige

- $t\bar{t}h \rightarrow t\bar{t}b\bar{b}$ important @ LHC \rightarrow top Yukawa cplg.

- QCD corrections [SM]: $\sim 20\%$

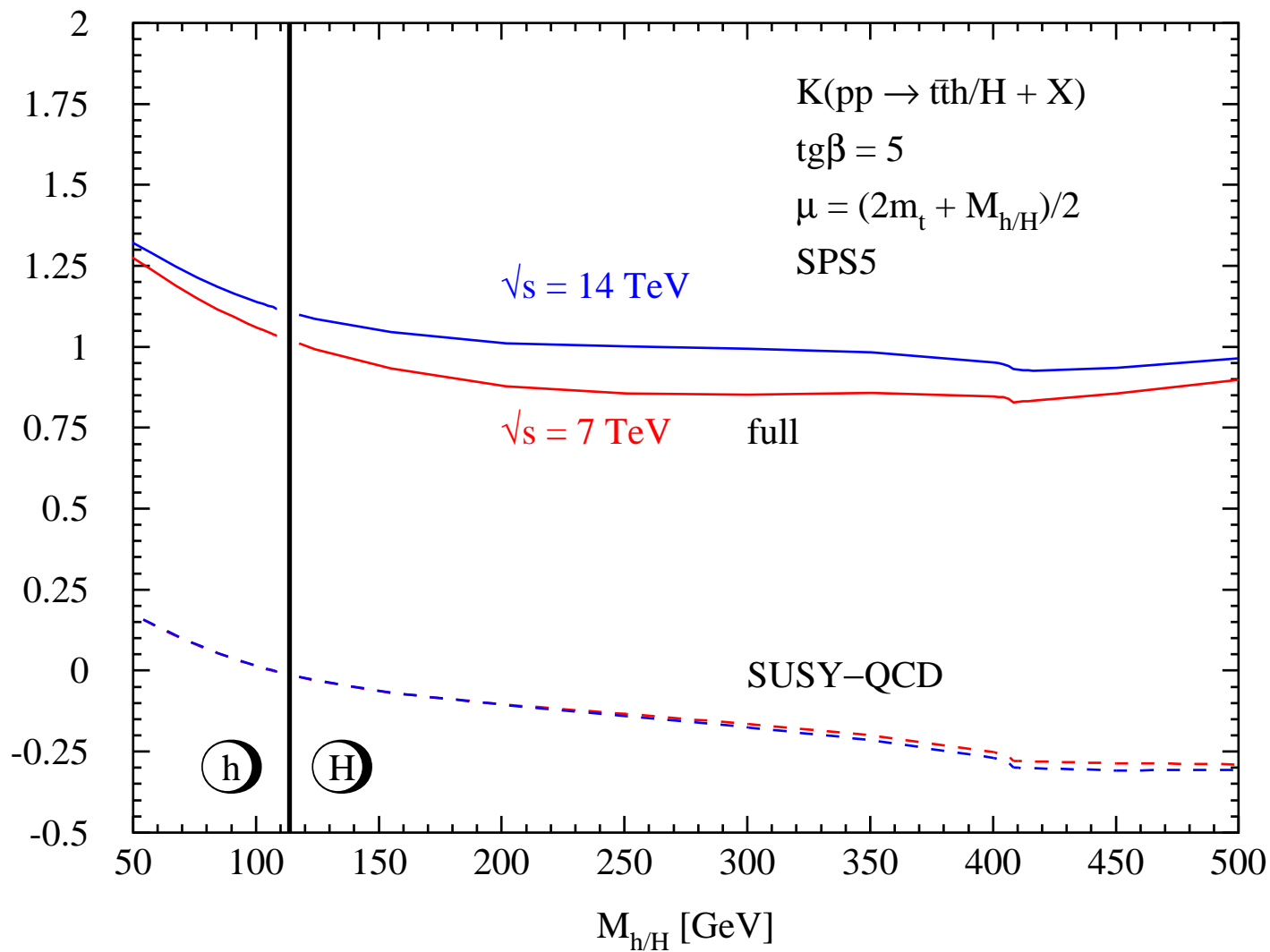
Beenakker, ...
Dawson, ...

- SUSY-QCD corrections: moderate

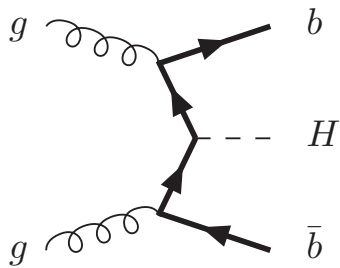
Dittmaier, Häfliger, Krämer, S., Walser

- link to parton showers: aMC@NLO, PowHel

Frederix et al.
Garzelli, Kardos, Papadopoulos, Trócsányi

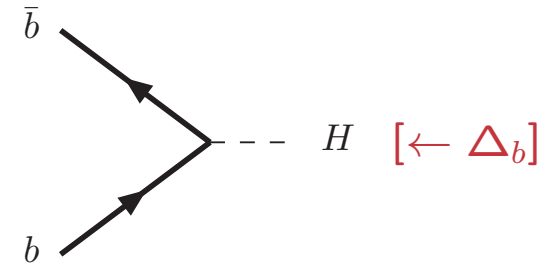


(v) $b\bar{b}$ +Higgs production



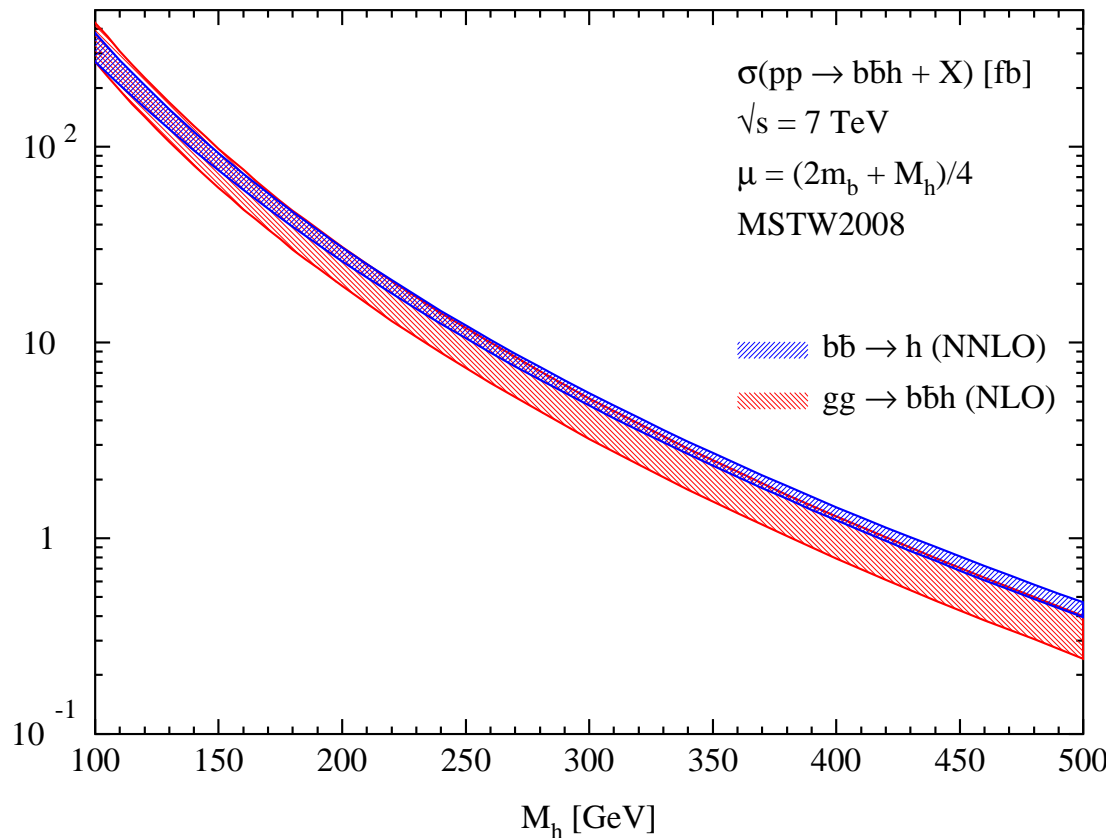
NLO

exact $g \rightarrow b\bar{b}$ splitting & mass/off-shell effects
no resummation of $\log M_H^2/m_b^2$ terms



NNLO

massless/on-shell b 's, no p_{Tb}
resummation of $\log M_H^2/m_b^2$ terms



Santander matching:

$$\sigma = \frac{\sigma^{4FS} + w\sigma^{5FS}}{1 + w}$$

$$w = \log \frac{M_H}{m_b} - 2$$

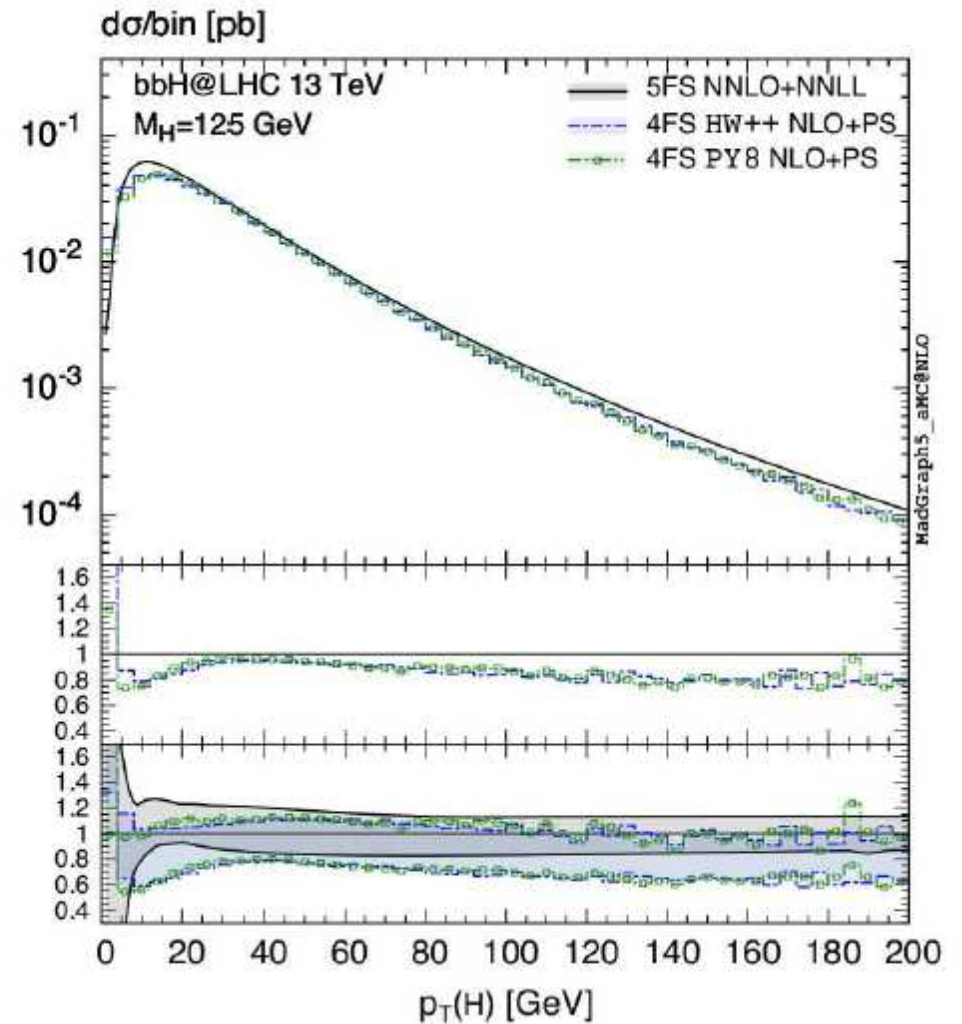
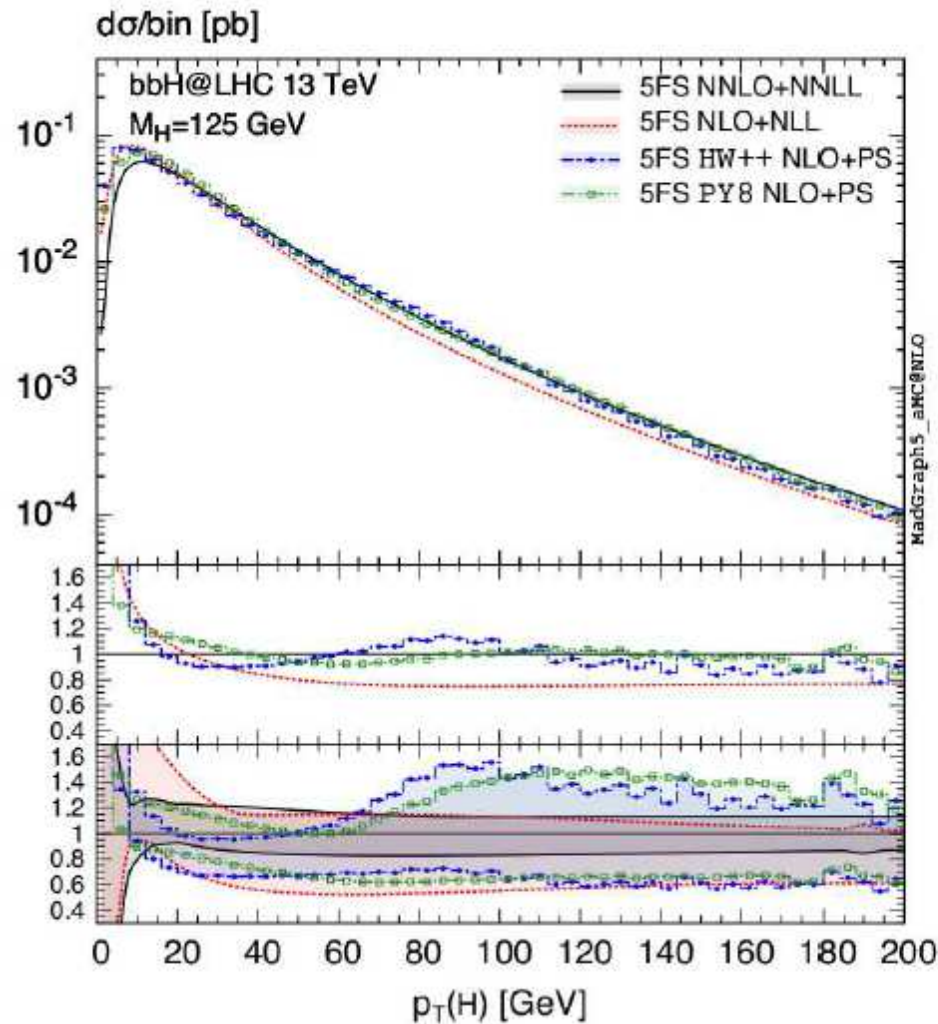
Harlander, Krämer, Schumacher

Dittmaier, Krämer, S. Dawson, Jackson, Reina, Wackerath
Harlander, Kilgore

	M_A	M_H [GeV]	δ_{QCD}^A	δ_{SUSY}^A	$\delta_{SUSYrem}^A$	δ_{QCD}^H	δ_{SUSY}^H	$\delta_{SUSYrem}^H$
7 TeV	100	113.9	0.23	-0.30	0.4×10^{-4}	0.27	-0.38	0.3×10^{-4}
	200	200	0.38	-0.30	2.9×10^{-4}	0.39	-0.30	5.8×10^{-4}
	300	300	0.46	-0.30	6.7×10^{-4}	0.47	-0.30	9.3×10^{-4}
	400	400	0.53	-0.30	1.3×10^{-3}	0.53	-0.30	1.5×10^{-3}
	500	500	0.57	-0.30	2.0×10^{-3}	0.59	-0.30	2.2×10^{-3}
14 TeV	100	113.9	0.14	-0.30	0.4×10^{-4}	0.17	-0.38	0.5×10^{-4}
	200	200	0.28	-0.30	2.7×10^{-4}	0.29	-0.30	5.7×10^{-4}
	300	300	0.37	-0.30	6.5×10^{-4}	0.39	-0.30	9.3×10^{-4}
	400	400	0.45	-0.30	1.2×10^{-3}	0.45	-0.30	1.5×10^{-3}
	500	500	0.50	-0.30	2.1×10^{-3}	0.49	-0.30	2.3×10^{-3}

	$\text{tg}\beta$	M_A	M_H [GeV]	δ_{SUSY}^A	$\delta_{SUSYrem}^A$	δ_{SUSY}^H	$\delta_{SUSYrem}^H$
7 TeV	3	200	209.7	-0.04	2.1×10^{-4}	-0.04	5.7×10^{-4}
	5	200	204.0	-0.06	2.4×10^{-4}	-0.06	5.3×10^{-4}
	7	200	202.1	-0.08	2.5×10^{-4}	-0.09	3.9×10^{-4}
	10	200	200.9	-0.12	2.5×10^{-4}	-0.12	3.8×10^{-4}
	20	200	200.1	-0.21	2.6×10^{-4}	-0.21	4.4×10^{-4}
	30	200	200.0	-0.30	2.9×10^{-4}	-0.30	5.8×10^{-4}
14 TeV	3	200	209.7	-0.04	2.0×10^{-4}	-0.04	7.2×10^{-4}
	5	200	204.0	-0.06	2.2×10^{-4}	-0.06	5.0×10^{-4}
	7	200	202.1	-0.08	2.4×10^{-4}	-0.09	4.4×10^{-4}
	10	200	200.9	-0.12	2.5×10^{-4}	-0.12	4.1×10^{-4}
	20	200	200.1	-0.21	2.7×10^{-4}	-0.21	4.4×10^{-4}
	30	200	200.0	-0.30	2.7×10^{-4}	-0.30	5.7×10^{-4}

distributions



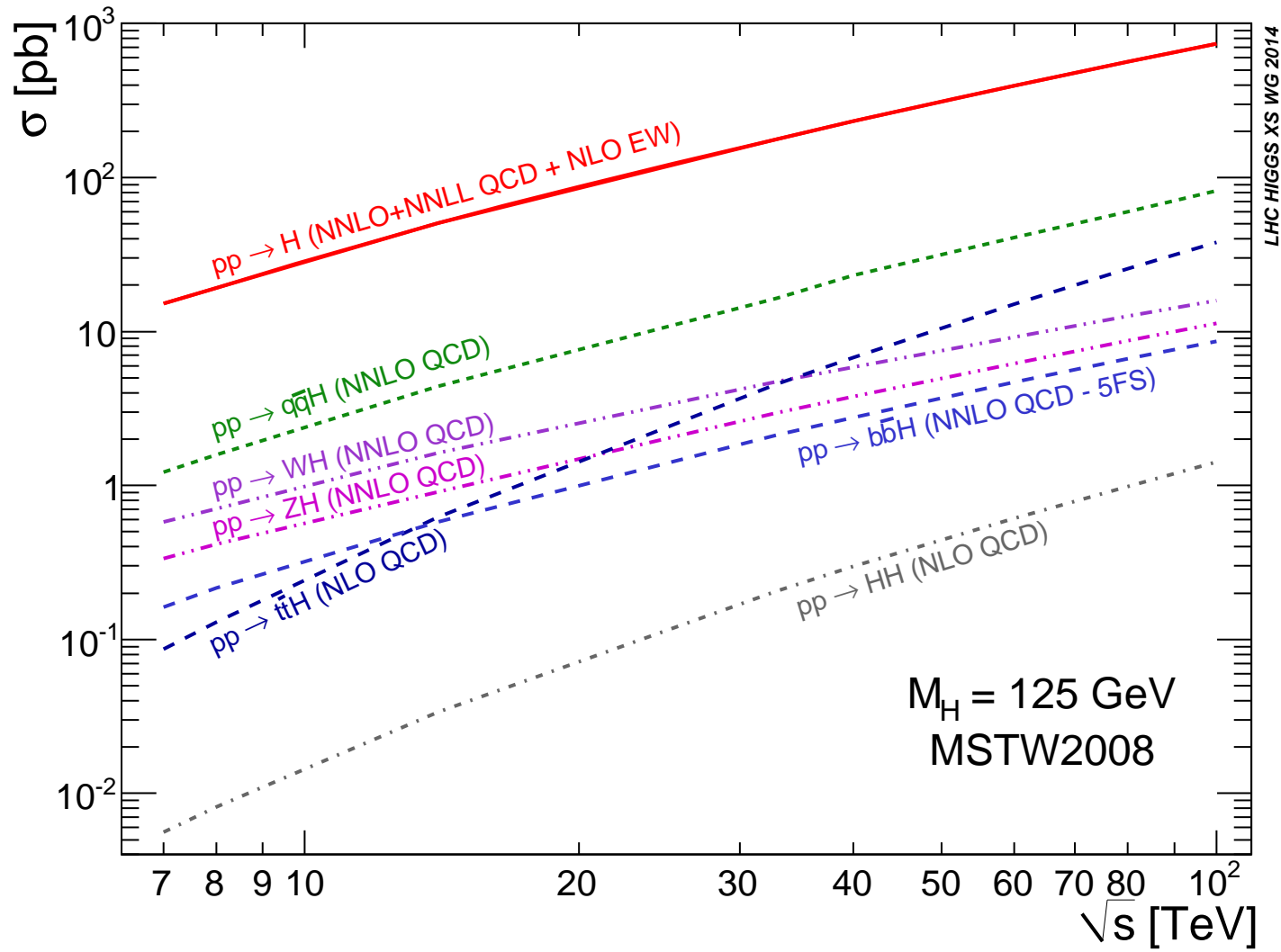
Wiesemann, Frederix, Frixione, Hirschi, Maltoni, Torrielli

III CONCLUSIONS

- Higgs boson searches/studies at LHC belong to major endeavours
- most QCD and elw. corrections known $\rightarrow \Delta \lesssim 10 - 15\% \text{ @ LHC}$
- important to develop NLO event generators [\leftarrow backgrounds]

BACKUP SLIDES

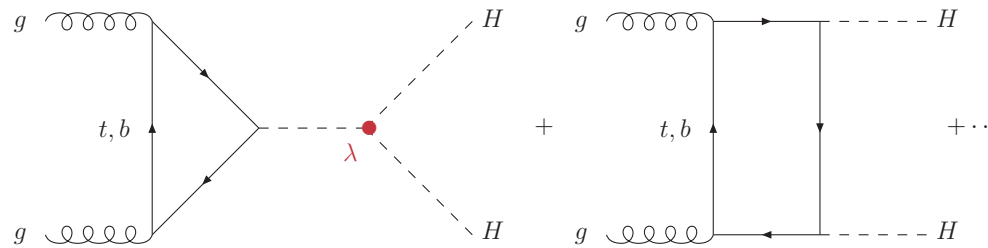
Energy Dependence → VLHC



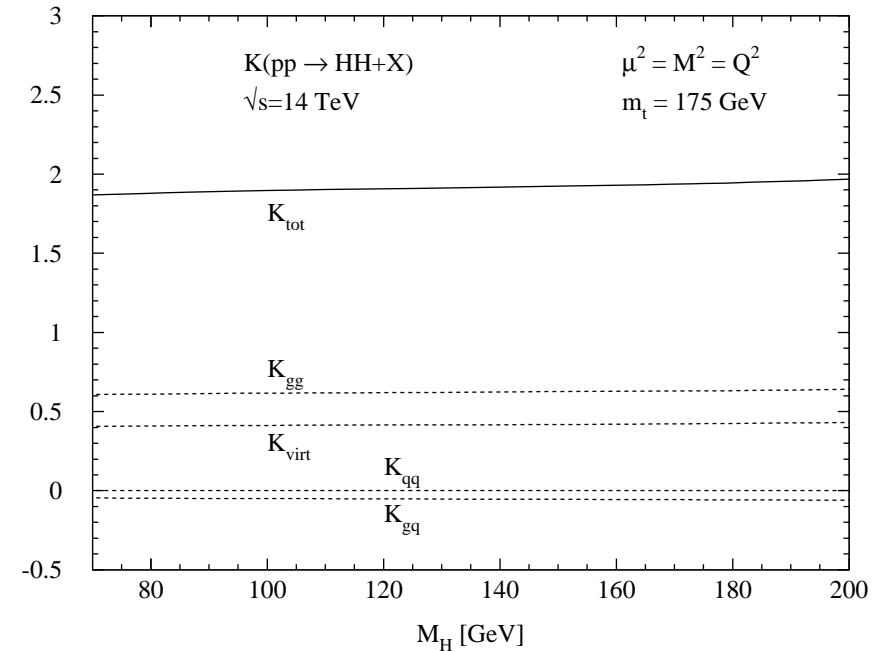
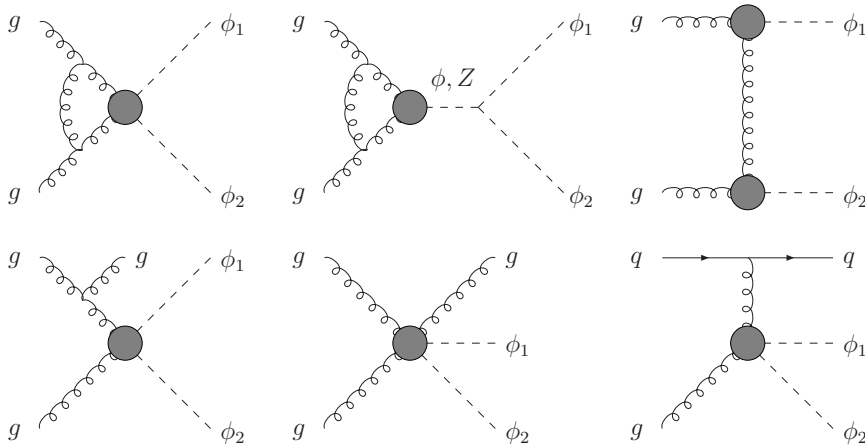
LHC Higgs XS WG

(i) $gg \rightarrow HH$

SM



- third generation dominant $\rightarrow t, b$
- 2-loop QCD corrections: $\sim 90 - 100\%$
 $[M_H^2 \ll 4m_t^2, \quad \mu = M_{HH}]$



Dawson, Djouadi, S.

- 2-loop QCD corrections:

$$\sigma = \sigma_0 + \frac{\sigma_1}{m_t^2} + \dots + \frac{\sigma_4}{m_t^8}$$

Grigo, Hoff, Melnikov, Steinhauser

- NLO mass effects @ NLO in real corrections

Frederix,...

- NNLO QCD corrections: $\sim 20\%$

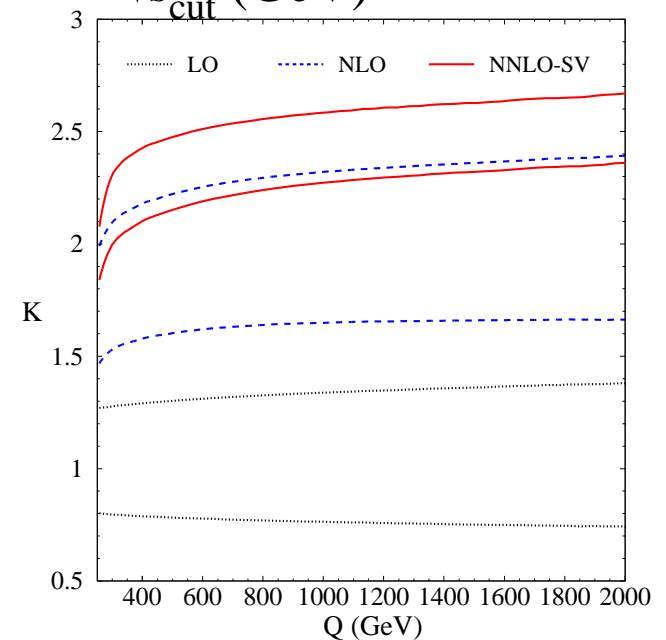
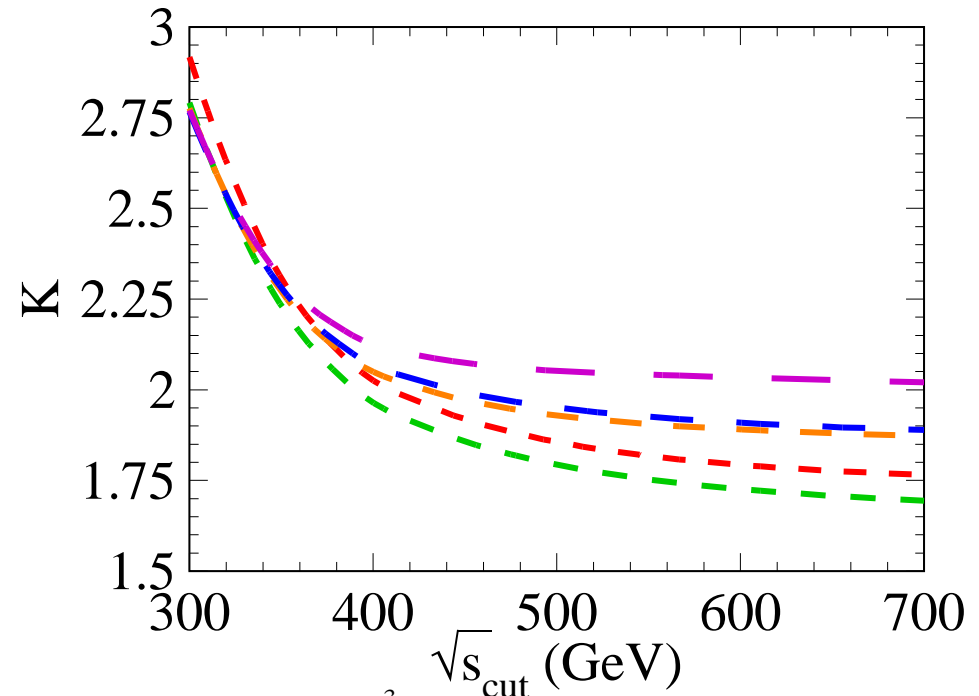
$$[M_H^2 \ll 4m_t^2]$$

de Florian, Mazzitelli

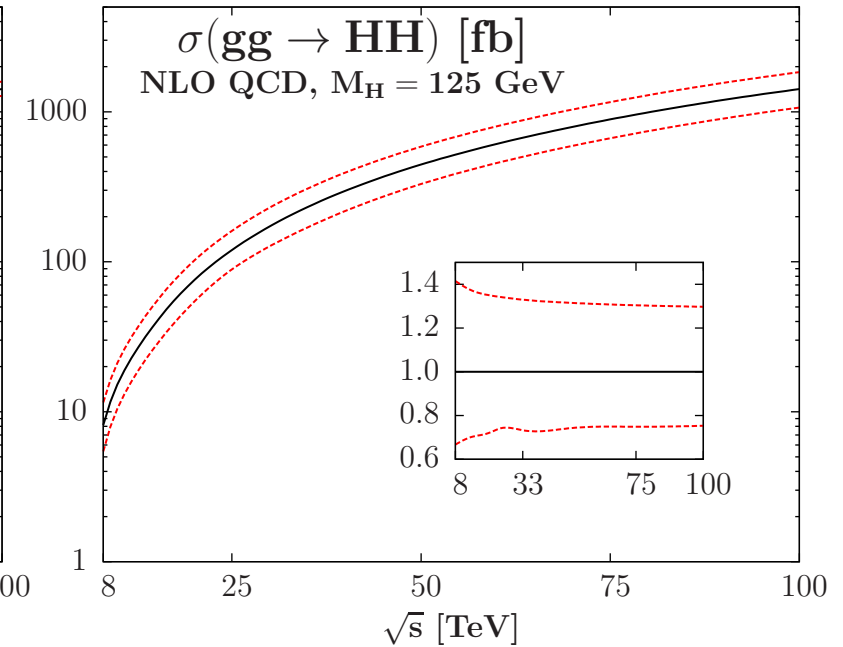
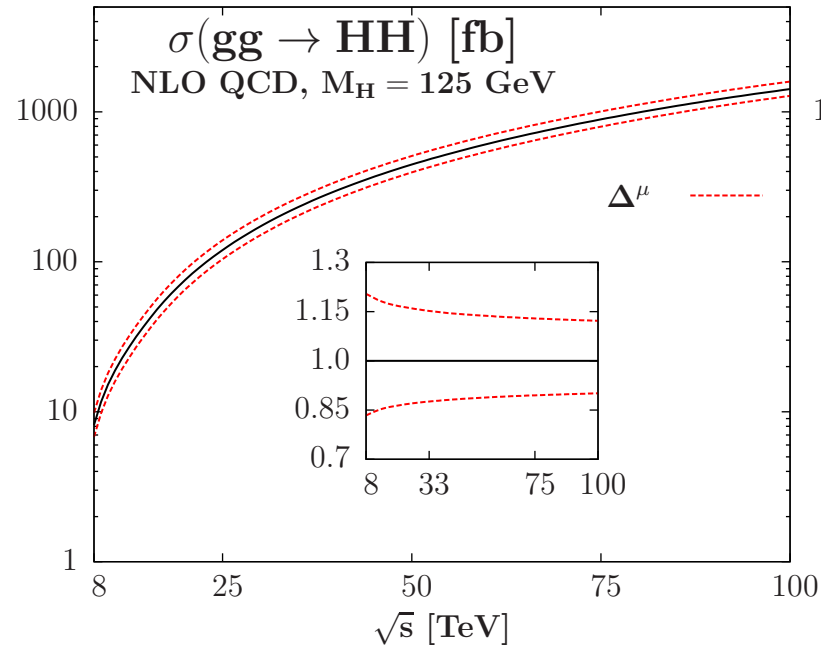
- soft gluon resummation [SCET]: $\sim 30\%$

$$[M_H^2 \ll 4m_t^2]$$

Shao, Li, Li, Wang



Uncertainties:



Baglio, Djouadi, Gröber, Mühlleitner, Quevillon, S.

- scale: $\sim 15 - 20\%$
- PDF + α_s : $\sim 6 - 7\%$ [MSTW2008]
- EFT: $\sim 10\%$
- total: $\sim 30 - 40\%$

Channels: need 3 ab^{-1}

$HH \rightarrow b\bar{b}\gamma\gamma$: low signal rate, most promising?

$HH \rightarrow b\bar{b}\tau^+\tau^-$: mass reconstruction difficult

$HH \rightarrow b\bar{b}W^*W^{(*)}$: hopeless?

• $b\bar{b}\gamma\gamma$: $\begin{matrix} +160\% \\ -190\% \end{matrix}$ @ 600 fb^{-1}

$\begin{matrix} +74\% \\ -62\% \end{matrix}$ @ 6 ab^{-1}

Baur, Plehn, Rainwater

• boosted kinematics: less sensitivity to λ

Dolan, Englert, Spannowsky

• $HH + jet \rightarrow b\bar{b}b\bar{b}j, b\bar{b}\tau^+\tau^-j$ promising?

Dolan, Englert, Spannowsky

• reduction of THUs by ratio $\frac{\sigma(gg \rightarrow HH)}{\sigma(gg \rightarrow H)} \rightarrow \frac{\delta\lambda}{\lambda} \sim 30\% ?$

Goertz, Papaefstathiou, Yang, Zurita