



Advances in Nb₃Sn Performance

Medium magnetic fields, very high current densities

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Acknowledgments



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- **NHMFL:** Markiewicz
- **PSFC-MIT:** Salvetti
- **Geneva:** Abächerli (EAS), Flükiger, Seeber, Uglietti (NIMS)



Supergenics I LLC

● **OST:** Hong, Parrell
SMI Lindenhovius

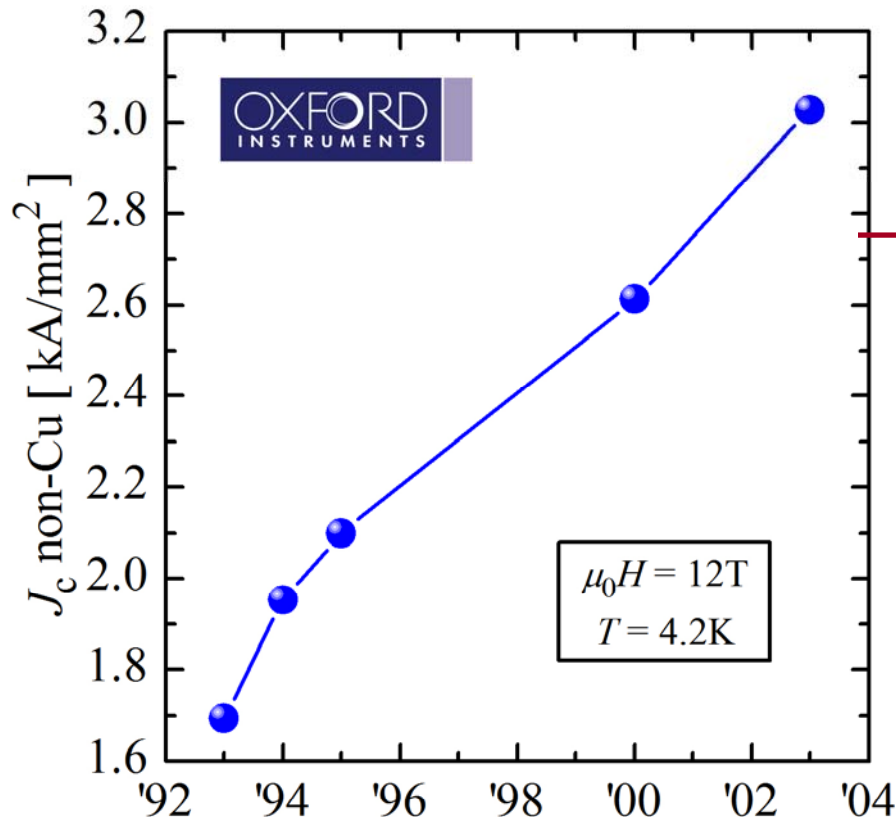
SupraMagnetics: Motowidlo
EAS: Schlenga, Thoener

Supergenics: Gregory
Supercon: Wong, Renaud



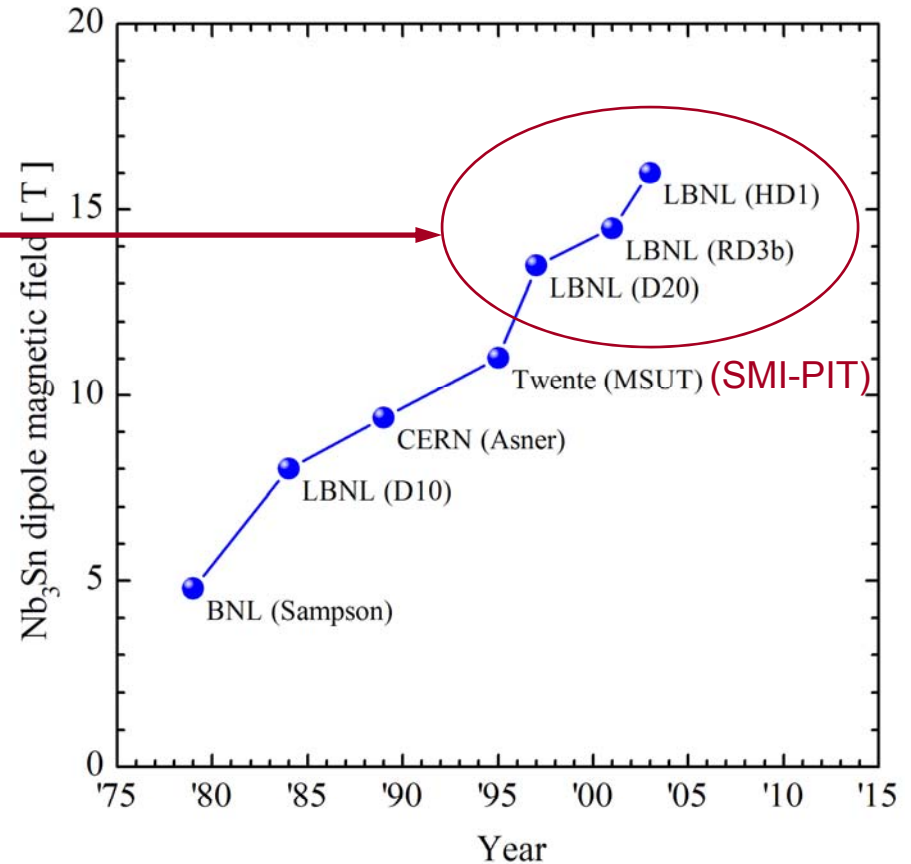
Increasing non-Cu J_c pays off

Progress in Nb_3Sn wire J_c ...



Parrell, ACE 2004 Year

...and in Nb_3Sn dipole magnetic fields



Dieterich, Cryogenics 2008

But where does J_c come from...



Outline

- Main properties of Nb_3Sn
 - ➔ Composition
 - ➔ Pinning
 - ➔ Strain
- Critical current density and critical current
 - ➔ What determines these?
- Modern high J_c Nb_3Sn wires
 - ➔ Overview of (some) manufacturers
- Prospects for future improvements
 - ➔ Possible ways to increase J_c
- Scaling of the critical current density

Superconductivity in Nb₃Sn

Matthias, PRB 95 (1954)

- Molten Sn over Nb powder in a quartz tube at 1200 C
- T_c onset at 18.05 ± 0.1 K

PHYSICAL REVIEW

VOLUME 95, NUMBER 6

SEPTEMBER 15, 1954

Superconductivity of Nb₃Sn

B. T. MATTHIAS, T. H. GEHALL, S. KELLER, AND E. CORENZWIT
Bell Telephone Laboratories, Murray Hill, New Jersey

(Received June 10, 1954)

Intermetallic compounds of niobium and tantalum with tin have been found. The superconducting transition temperature of Nb₃Sn at 18°K is the highest one known.

SOME intermetallic compounds crystallizing with the β -wolfram structure become superconducting, as was first pointed out by Hardy and Hulm.¹ In particular one of these, V₃Si, showed a remarkably high transition temperature between 16.9°K and 17.1°K. These authors made various attempts to raise this temperature by introducing a third component but were not successful.

The β -wolfram structure is a very peculiar structure with rather varying interatomic distances,² a fact which may render the addition of a third component rather difficult. It seemed therefore more favorable to look for another β -W compound with a large volume and a favorable electron/atom ratio³ in order to raise the superconducting transition temperature. There is very little known about the systematic occurrence of intermetallic compounds in this β -W structure. The fact that thus far no niobium compounds have been reported seemed therefore not significant.

It was expected that in the Nb-Sn and Ta-Sn this crystal form would be found, an assumption which was verified. We have determined that Nb₃Sn and Ta₃Sn both crystallize in a β -W structure with a lattice constant of about 5.3Å. The Ta₃Sn was measured in the apparatus previously described,⁴ and became superconducting near 6°K. The transition temperature of the Nb₃Sn was determined by immersing the sample surrounded by a copper coil in liquid hydrogen. The self-inductance of the coil was measured on a General Radio Model 650A Bridge at 1 kc/sec as the sample was slowly cooled. Figure 1 shows the results for two different samples made under somewhat different conditions which were cooled from 18.5°K to 17.5°K during a period of about 30 minutes. The sharpness of the transition together with the reproducibility between samples indicates that these samples are indeed well-defined compounds. The onset of superconductivity at

18.05°K \pm 0.1° is determined by extrapolating the line of steepest slope to the high temperature line. Temperatures were measured by a copper constantan thermocouple secured to the measuring coil and independently checked with the vapor pressure of hydrogen.

APPENDIX

While the synthesis of an intermetallic compound is generally a rather straightforward process, it may be necessary to describe briefly the formation of these

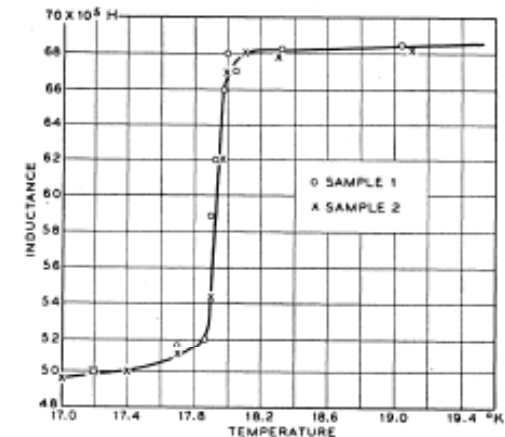


Fig. 1. Variation of susceptibility with temperature of Nb₃Sn.

compounds. No reference to Nb-Sn or Ta-Sn was found in the literature. The melting point of niobium is nearly 400° above the boiling point of tin, and an arc furnace is therefore out of place. A complete reaction can, however, easily be obtained by having molten tin run over Nb or Ta powder in a closed-off quartz tube at 1200°C. Nb₃Sn and Ta₃Sn seem to be formed by a peritectic reaction between 1200°C and 1550°C.

¹ G. Hardy and J. K. Hulm, Phys. Rev. **89**, 884 (1953).

² H. I. Wallbaum, Z. Metallkunde **31**, 362 (1939).

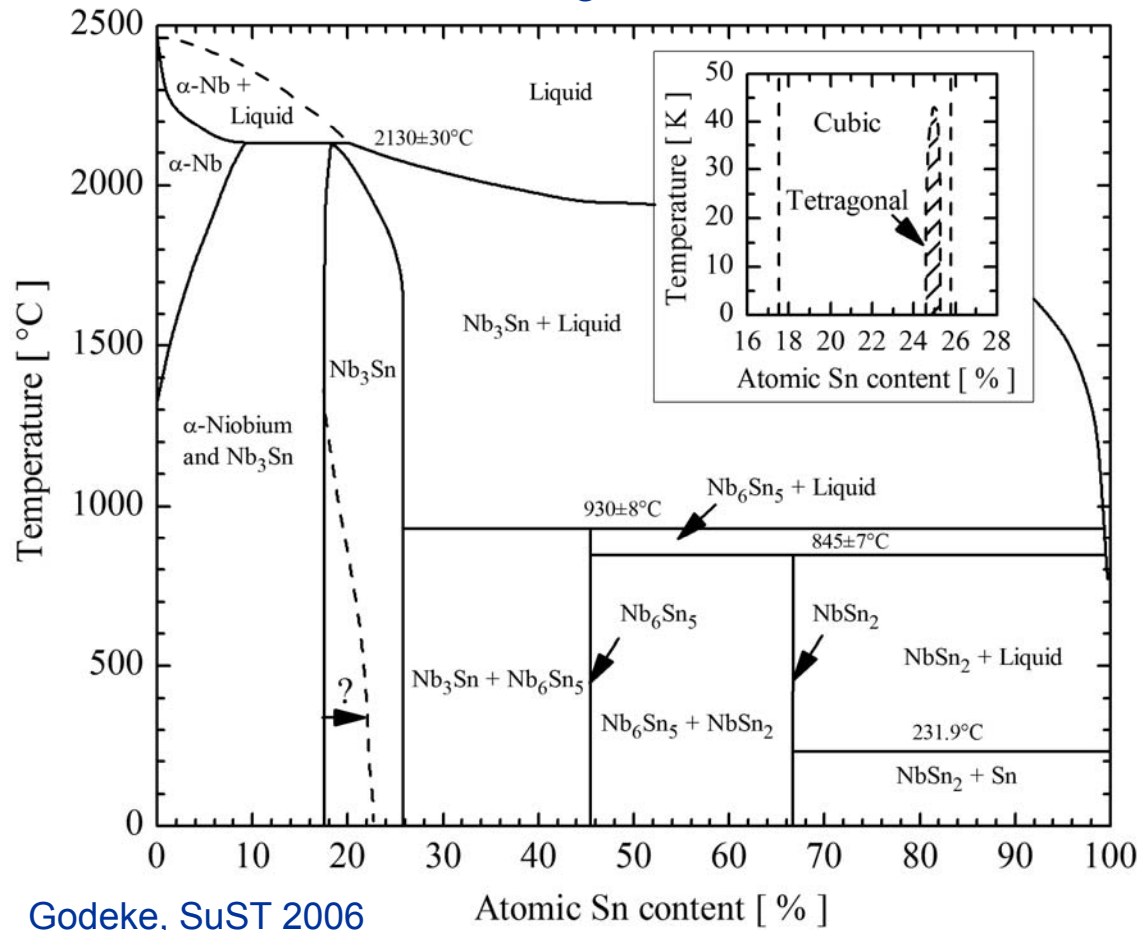
³ B. T. Matthias, Phys. Rev. **92**, 874 (1953).

⁴ B. T. Matthias and J. K. Hulm, Phys. Rev. **87**, 799 (1952).

Nb₃Sn is not a line compound: Nb_{1-β}Sn_β

Binary phase diagram

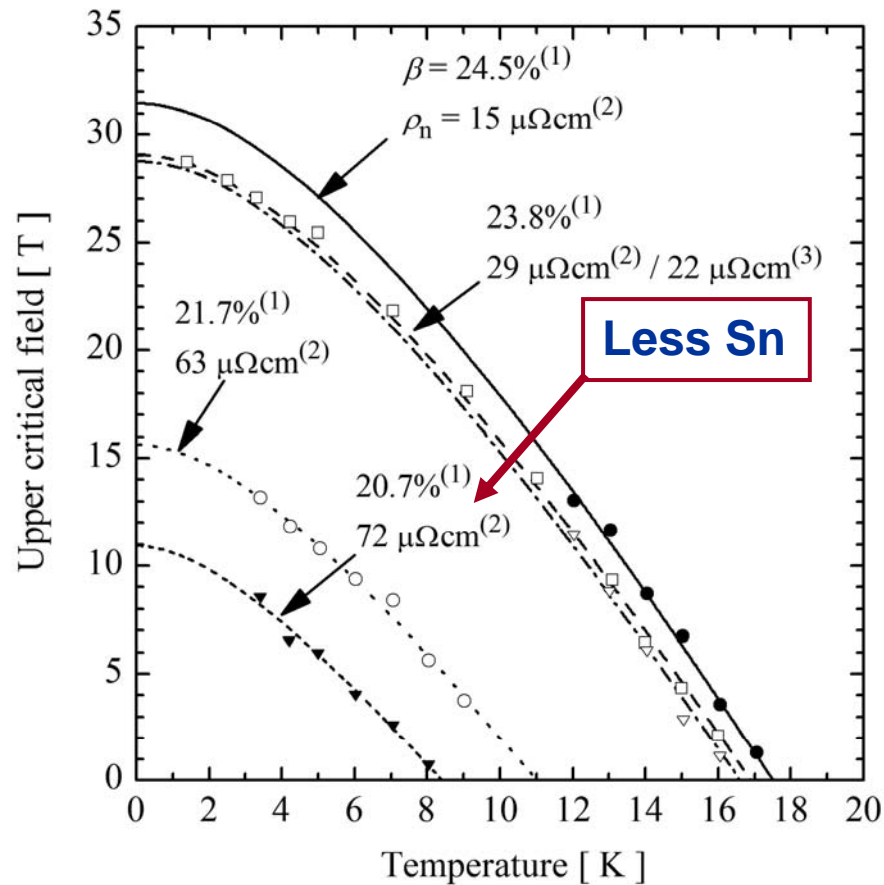
- Charlesworth, JMS 1970; Flükiger, ACE 1982



Nb-Sn stable from 18 to 25 at.% Sn → 'A15'

$H_{c2}(T)$ versus Sn content

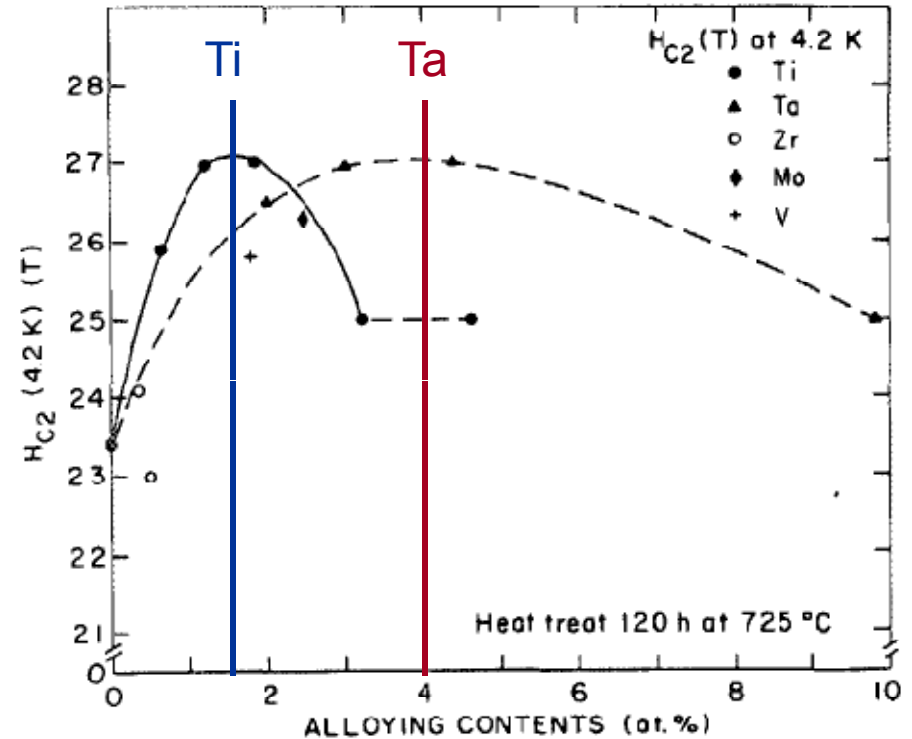
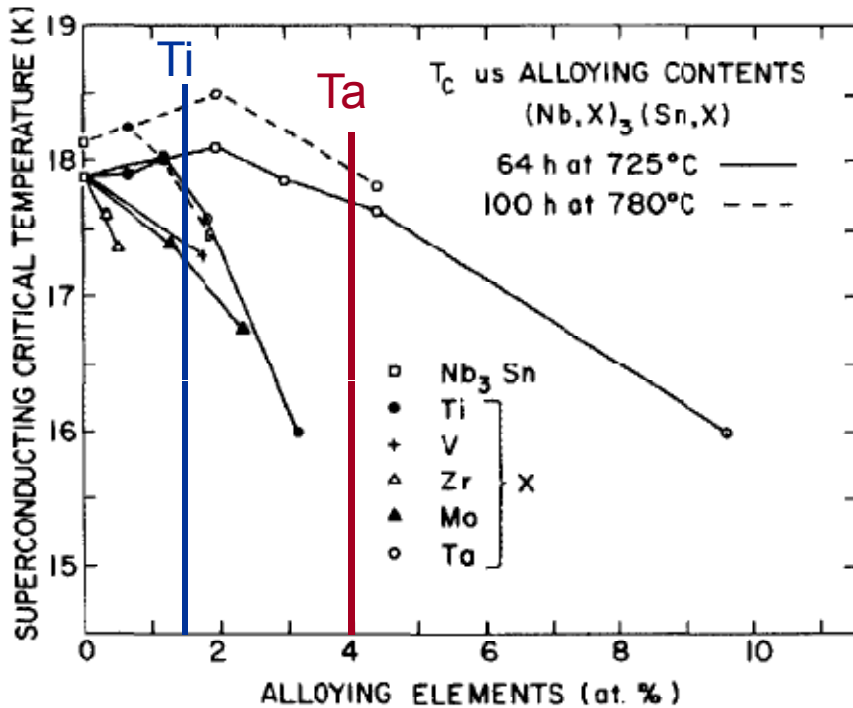
Jewell, ACE 2004, bulk samples



Sn richer A15 has higher $H_{c2}(T)$ (until ~ 24.5 at.% Sn)

Alloying of Nb-Sn

Suenaga, JAP 1986



- Ti: Optimal H_{c2} at 1.5 at.%, Ta: Optimal H_{c2} at 4 at.%, Both: slight variation T_c
- Flükiger, SuST 2008: Different optima: $(Nb_{1-x}Ta_x)_3Sn$ and $Nb_3(Sn_{1-x}Ti_x)$

Alloying increases H_{c2}



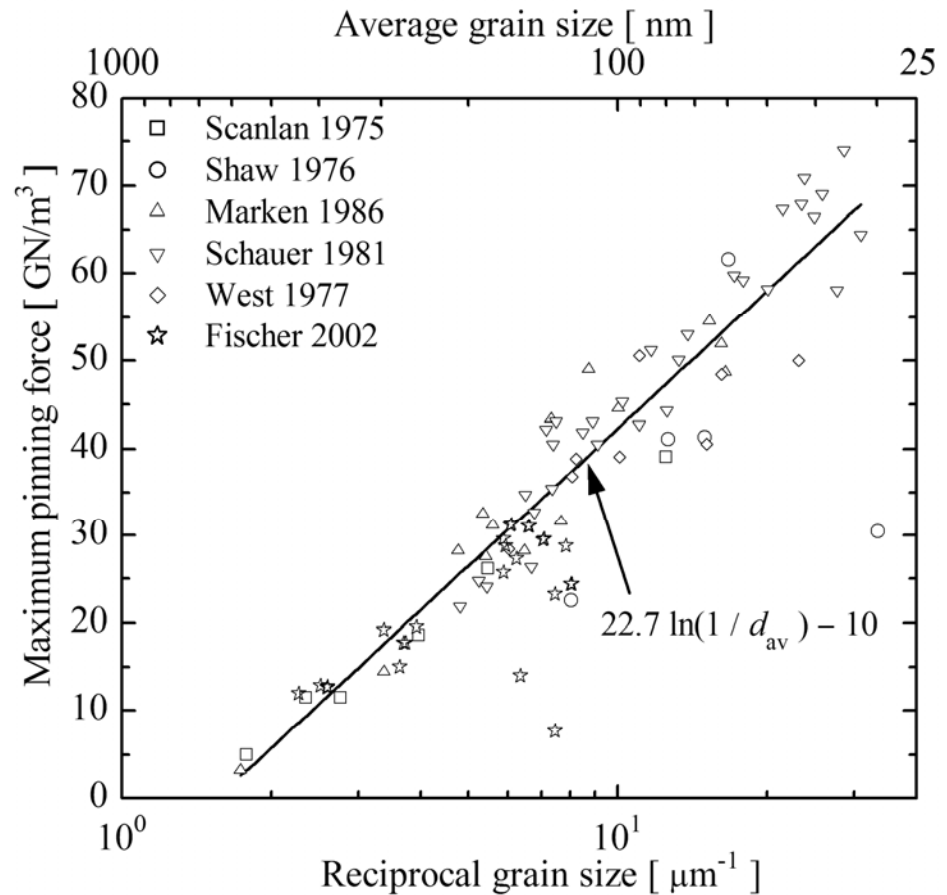
What determines pinning capacity?

Pinning centers

- Positions with minima in SC wave function
 - Normal regions
 - Grain boundaries
 - Lattice imperfections
 - ...

Nb₃Sn

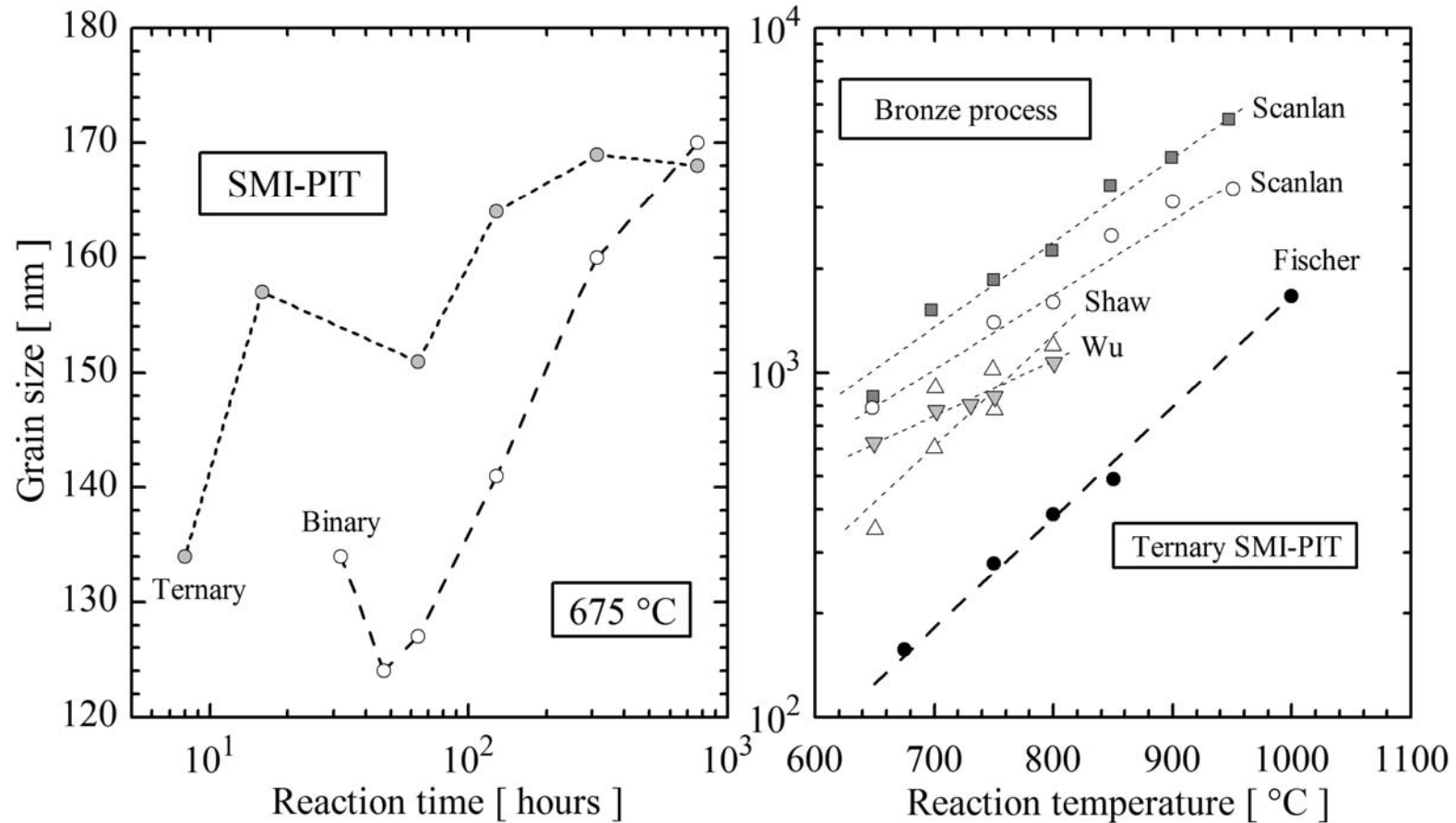
- Grain boundaries
 - Main pinning centers



Godeke, SuST 2006

Grain size determines F_{Pmax}

What determines grain size?



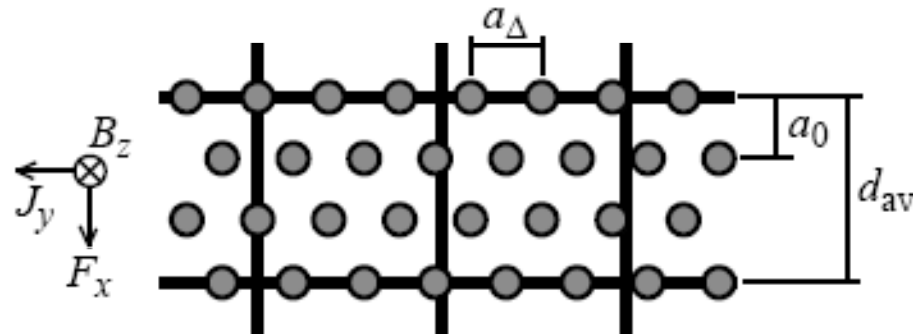
Godeke, Cryogenics 2008

Reaction time (somewhat) and temperature (a lot)

What is an optimal grain size?

Ideal: One pinning center per flux-line

- Flux-line spacing $a_0 \approx$ average grain size d_{av}



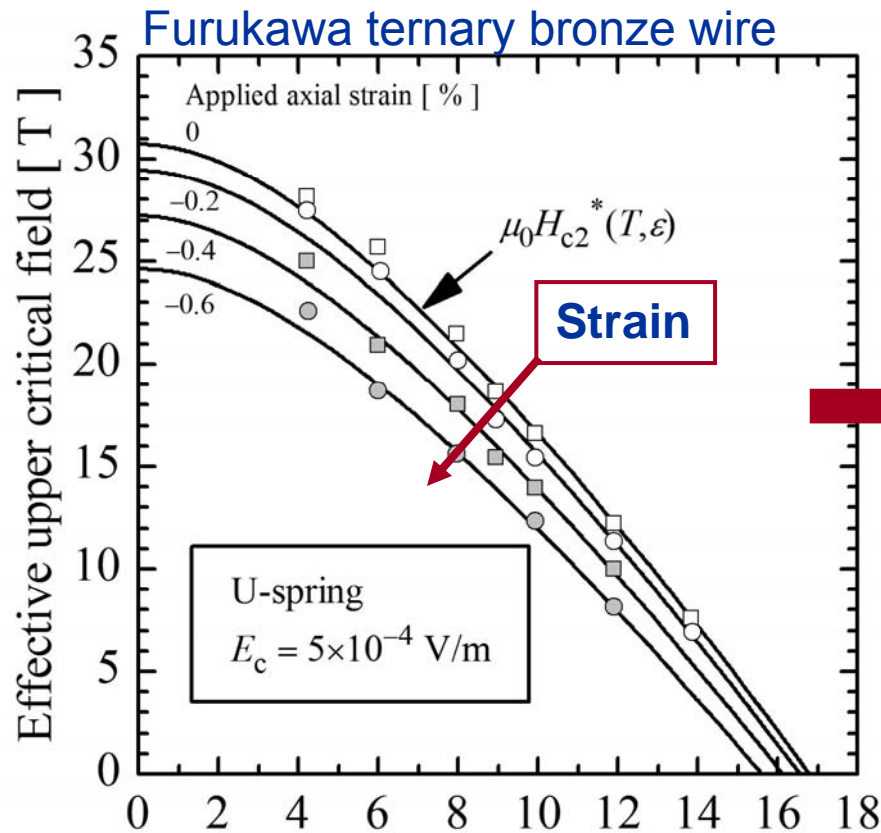
Schematic: Cubic grains and flux-line lattice
Godeke, to be published 2008

- Flux-line spacing \rightarrow field dependent
 - E.g. at 12 T $a_0 = (3/4)^{1/4} (\phi_0 / \mu_0 H)^{1/2} = 12$ nm
 - Grain size in Nb₃Sn wires \rightarrow 100 – 200 nm

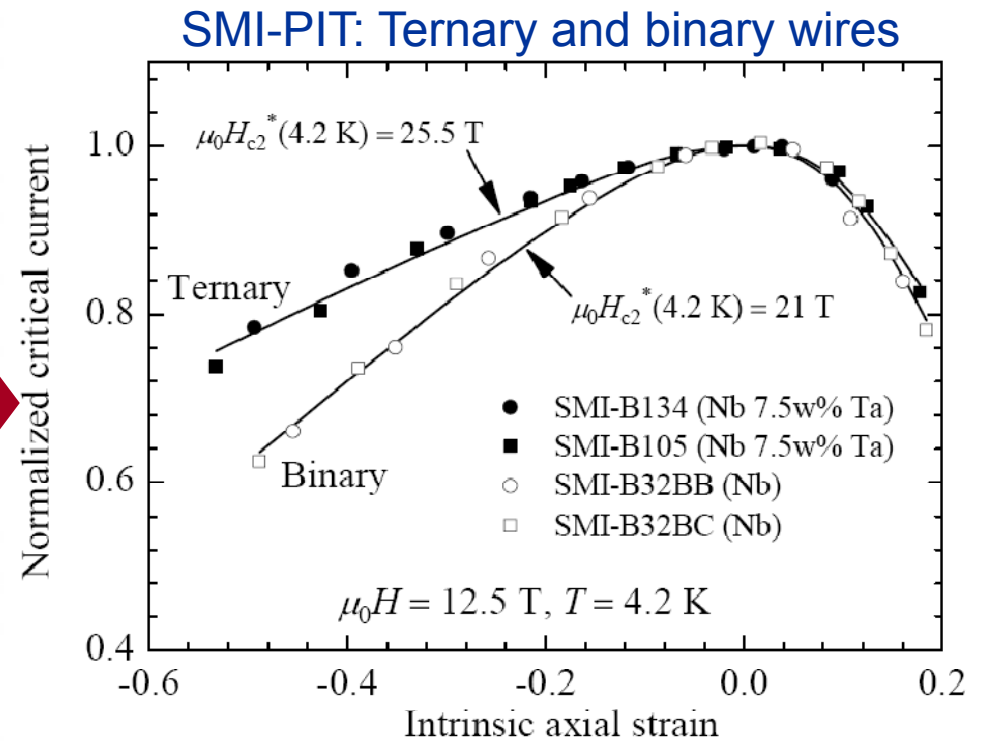
Grain sizes in wires are one order of magnitude from optimal

Strain sensitivity

Longitudinal strain effects on effective $H_{c2}(T)^*$



Godeke, TAS 2002 Temperature [K]



Godeke, Cryogenics 2008

Note: Increased H_{c2}^* can provide lower strain dependence at medium fields

Strain and Sn content have similar effects

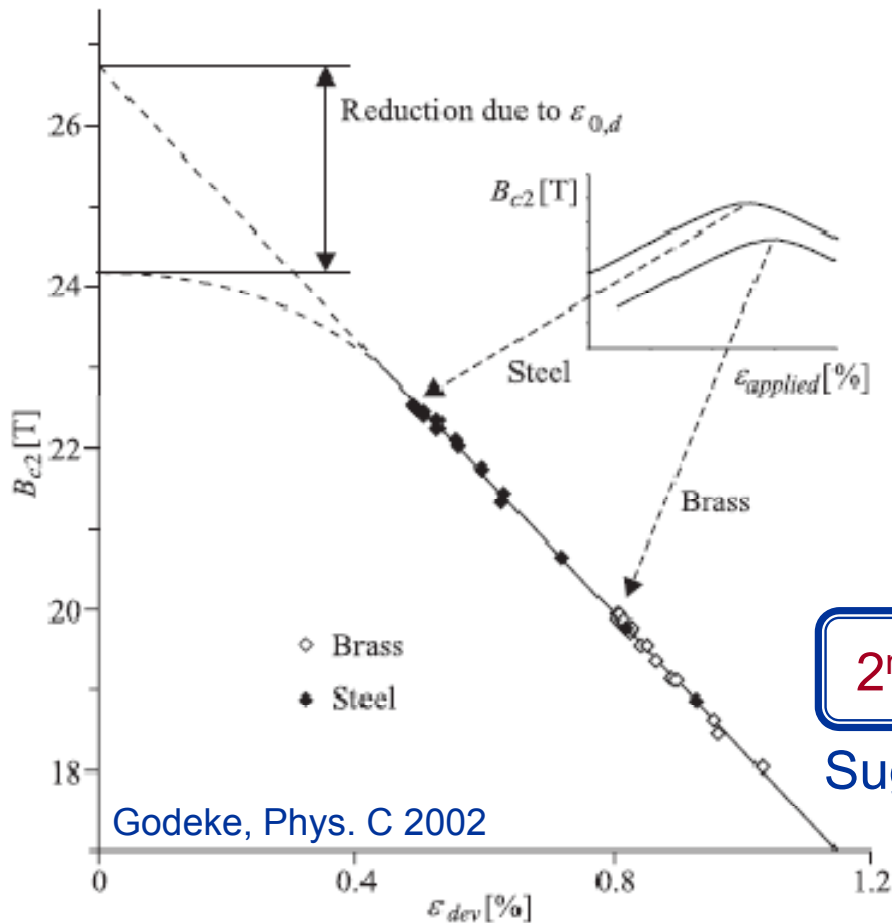
Strain models existing

- 1D empirical (Ekin, Cryogenics 1980, Taylor, SuST 2005):

$$s(\epsilon) = 1 - a \left| \epsilon_{\text{axial}} \right|^u$$

$$s(\epsilon) = 1 + c_2 \epsilon^2 + c_3 \epsilon^3 + c_4 \epsilon^4$$

- 3D empirical (Ten Haken, Thesis 1994): Data from quasi 2D tapes



$$s(\epsilon_{\text{dev}}) \cong 1 - C_d \sqrt{(\epsilon_{\text{dev}})^2 + (\epsilon_{0,d})^2}$$

$$H_{c2}^*(\epsilon) \equiv H_{c2m}^* s(\epsilon)$$

$$T_c^*(\epsilon) \equiv T_{cm}^* s(\epsilon)^{\frac{1}{\bar{\sigma}}}$$

2nd invariant (deviatoric strain) dominates

Suggested originally by Welch and Testardi

Strain models progress (I)

More fundamental approach (Markiewicz, Cryogenics 2004)



Strain modifies

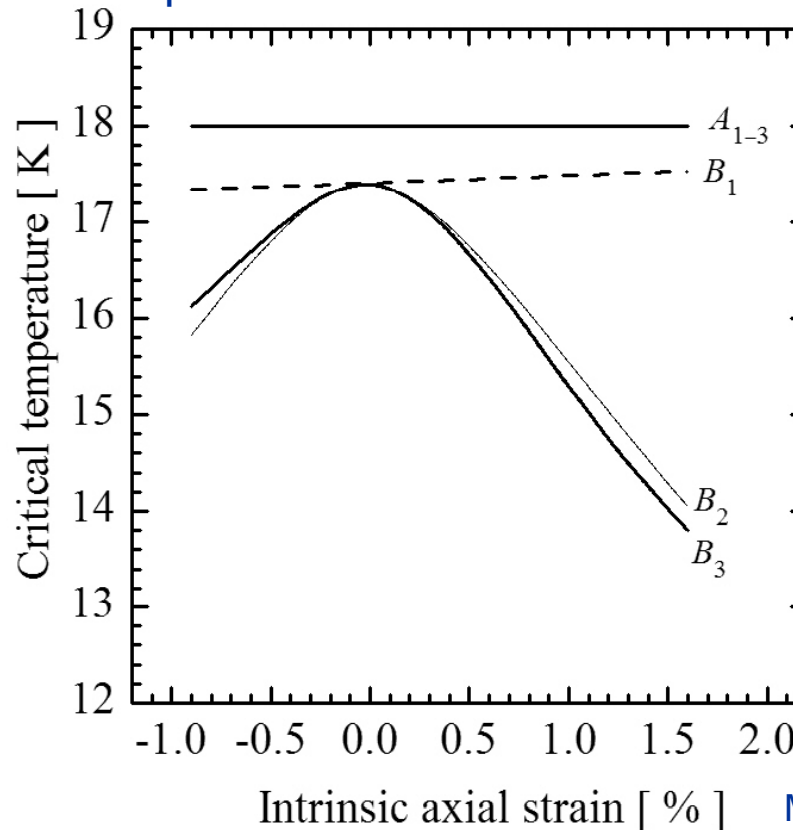
- Lattice vibration modes (phonons)
- Electron-phonon interaction spectrum

$$\lambda_{ep} = 2 \int \frac{\alpha^2(\omega) F(\omega)}{\omega} d\omega$$

$$\lambda_{eff} = \frac{(\lambda_{ep} - \mu^*)}{(1 + 2\mu^* + 1.5\lambda_{ep}\mu^* e^{-0.28\lambda_{ep}})}$$

$$T_c = \frac{0.25 \langle \omega^2 \rangle^{\frac{1}{2}}}{(e^{2/\lambda_{eff}} - 1)^{\frac{1}{2}}} \quad \mu_0 H_{c2} = \dots ?$$

$$s(\varepsilon) = \frac{1}{1 + c_2 \varepsilon^2 + c_3 \varepsilon^3 + c_4 \varepsilon^4}$$



Strain free value
Hydrostatic (1st inv)

Symmetric (2nd inv)
non-hydrostatic

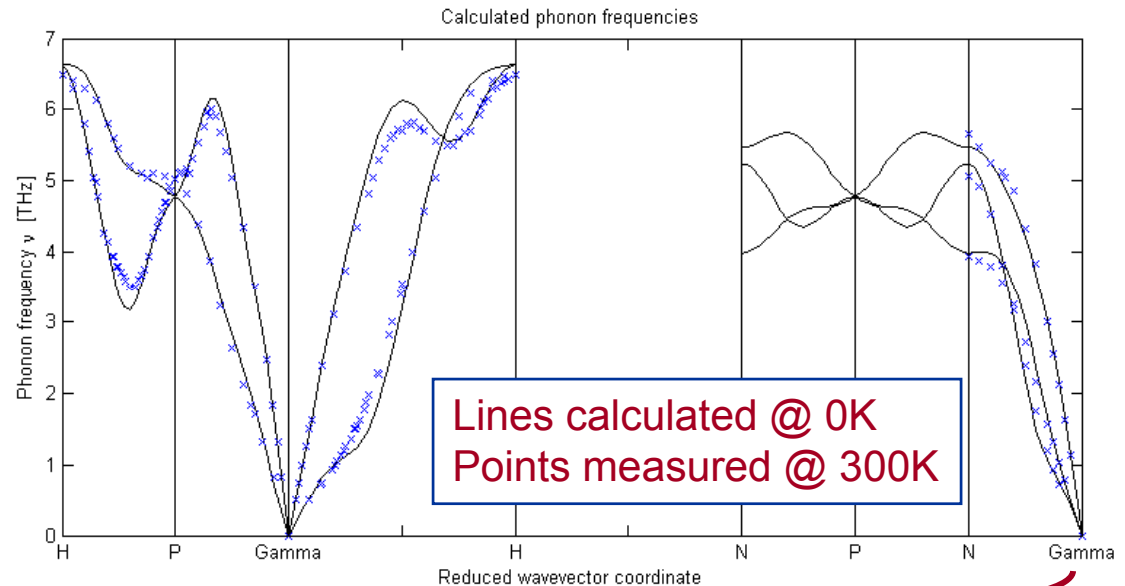
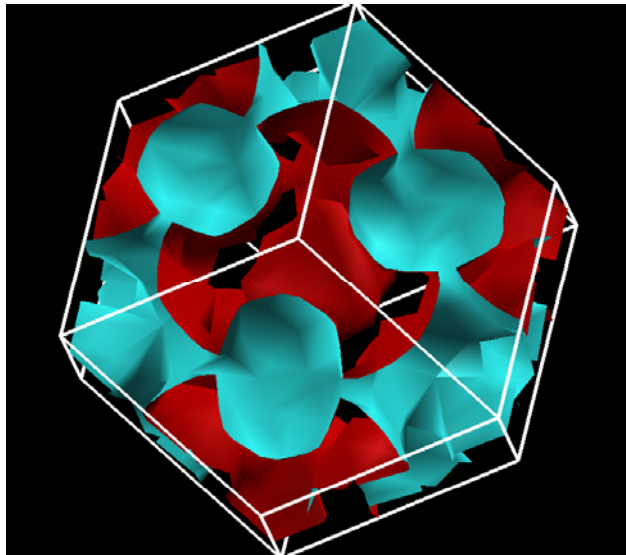
Asymmetric (3rd inv)
non-hydrostatic

2nd invariant dominates, $H_{c2}(\varepsilon)$ missing

Strain models progress (II)

Truly fundamental approach (**Salvetti**, in progress):

- Goal: Ab-initio calculation of critical properties Nb, Nb₃Sn and Nb₃Al
 - ➔ Only external input is lattice deformation (strain)
- Density Functional Theory → Phonon dispersion curves and e-p interactions
- Example: Calculated Fermi surface and phonon dispersion curves Nb



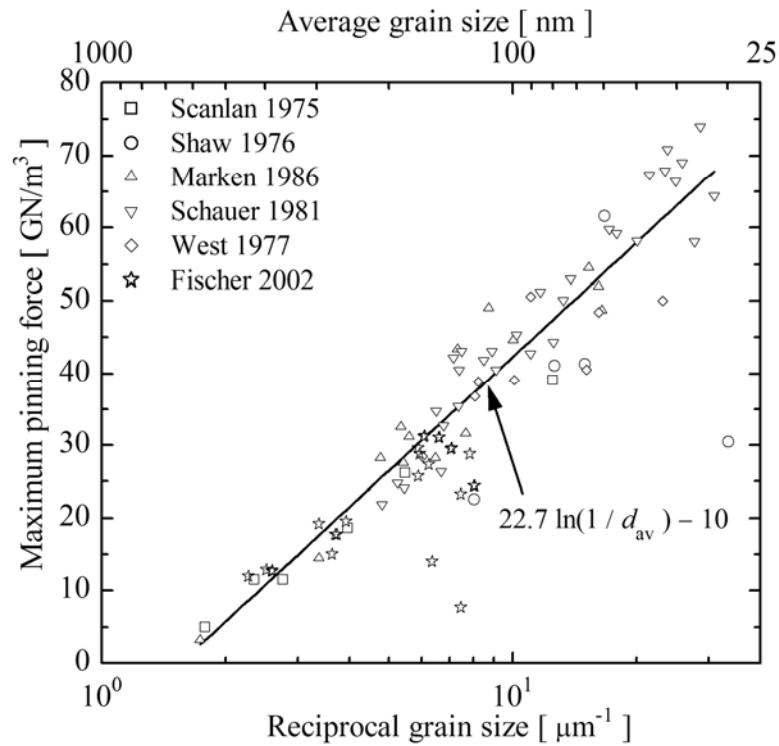
PSFC

$$+\varepsilon \text{ and } \lambda_{ep} = 2 \int \frac{\alpha^2(\omega) F(\omega)}{\omega} d\omega \rightarrow T_c(\varepsilon)$$

- Principally also allows calculation of Sn deficiency

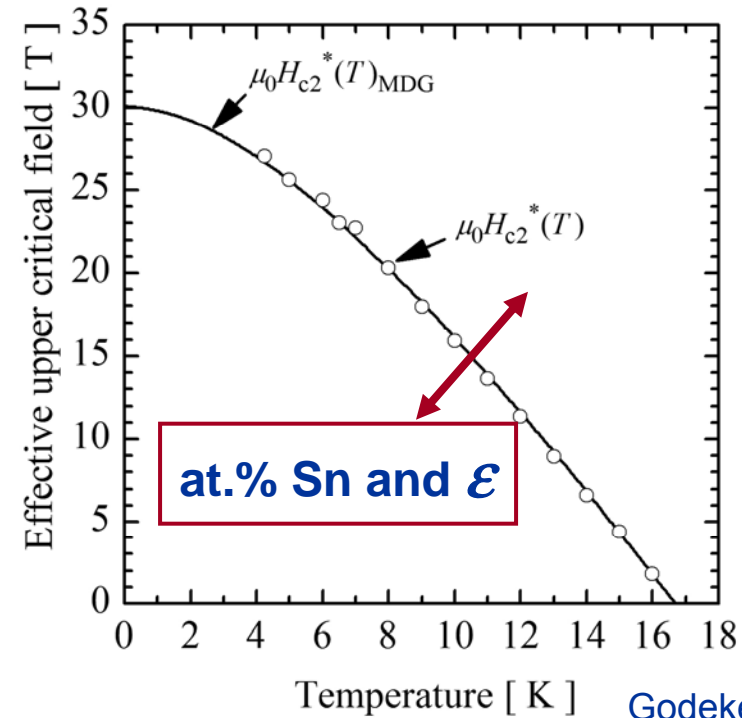
In summary: What determines J_c ?

Pinning capacity



+

Effective $H - T$ phase boundary



= J_c

● Average grain size

● Composition

● Strain state

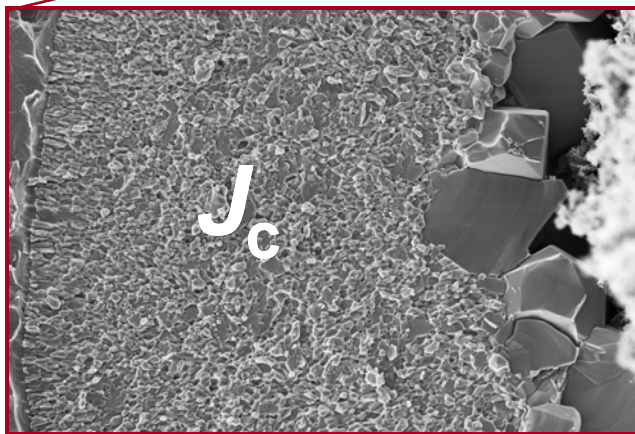
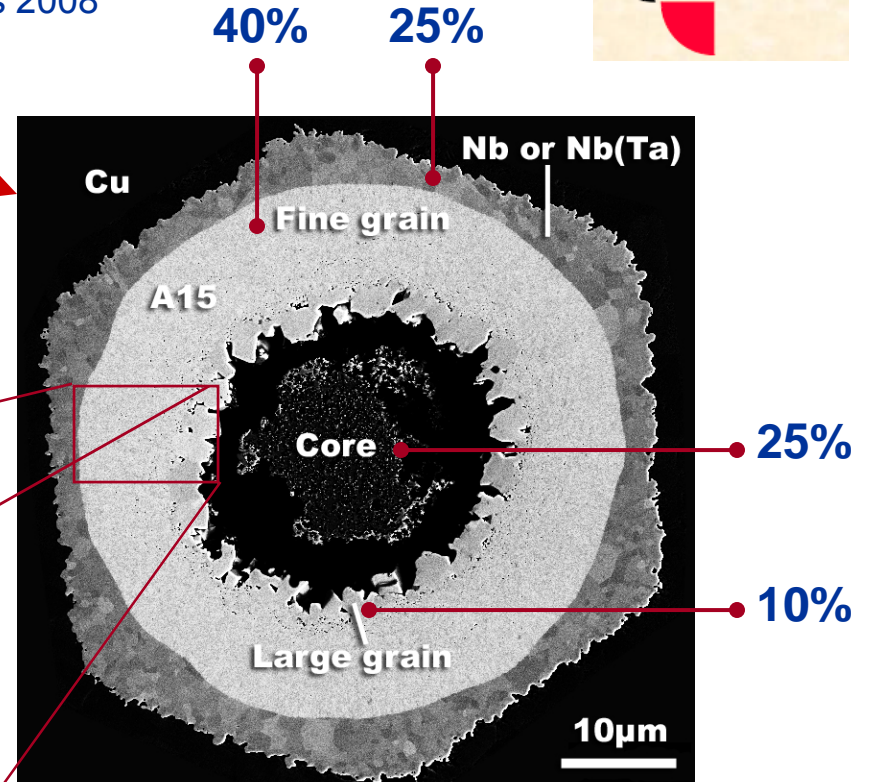
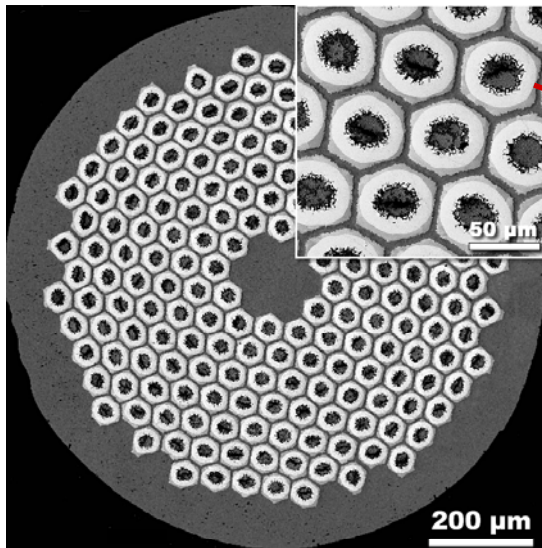
What determines I_c ?

- Powder-in-tube wire (SMI)

- 50% Non – Cu fraction



Courtesy, Lee and Fisher 2005
Godeke, Cryogenics 2008



Only ~20% of a wire carries J_c



Recipe for a very high current wire

Real estate

- ▶ As much A15 in the non-Cu cross-section as possible
 - Much (typically ~ 25%) is still lost as Sn source

Filaments / sub-elements
below ~50 micrometer

Sn content

- ▶ Optimal around 24.5 at.% Sn
- ▶ Abundant Sn supply

Short diffusion distances

- ▶ Long diffusion distances inevitably result in Sn gradients

Alloying: 1.5 at.% Ti and 4 at.% Ta additions

- ▶ Commercial alloys: Nb 47 wt.% Ti and Nb 7.5 wt.% Ta

Grain sizes around 10 – 15 nm for optimal pinning in 10 – 15 T regime

- ▶ Requires short, low temperature reactions (which result in Sn deficiency)
- ▶ Wire grain sizes typically 100 – 200 nm

Strain dependence

- ▶ Engineer applications around it
- ▶ Present status of knowledge does not suggest tweaks (**much to be done here!**)



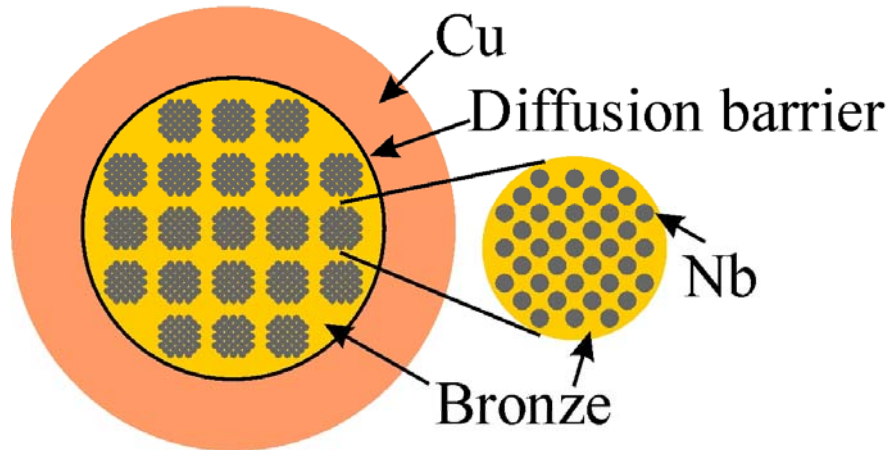
Wires

What is being made using the aforementioned knowledge?

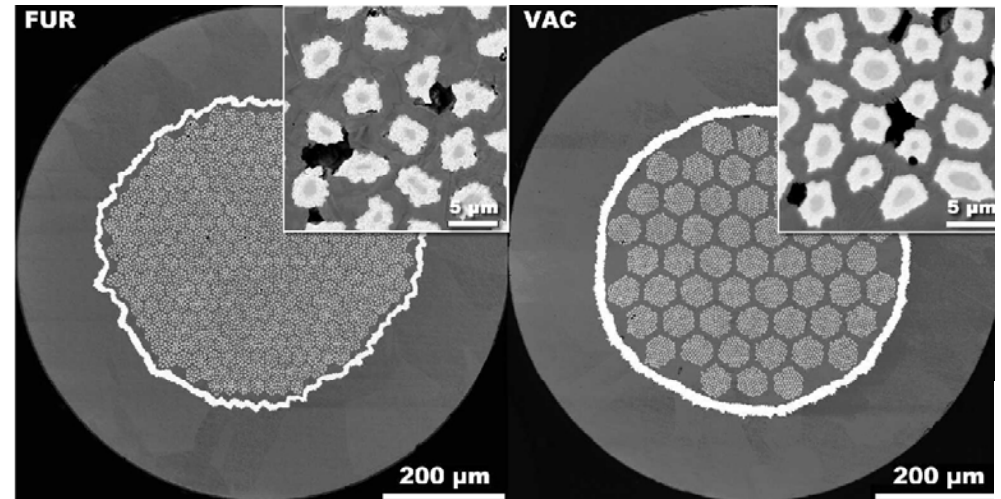
A very **incomplete** list!

Apologies to those not included

The 'classic' Bronze process



Godeke, JAP 2005 (Courtesy, Lee 2005)

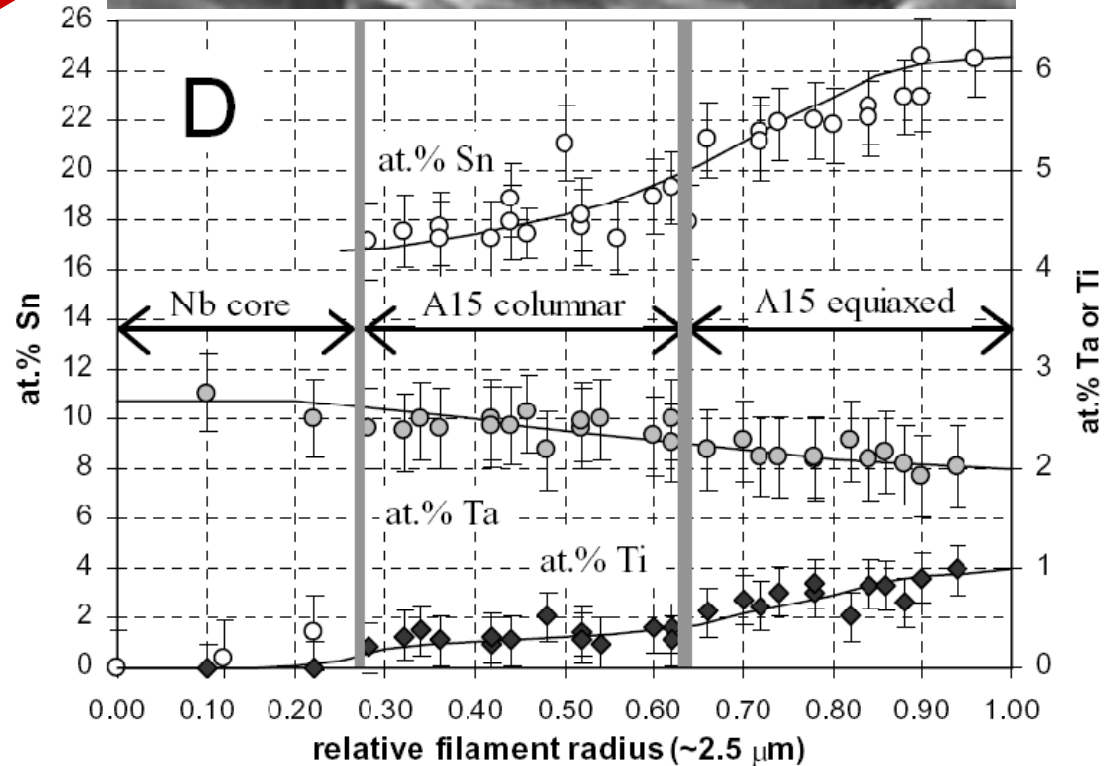
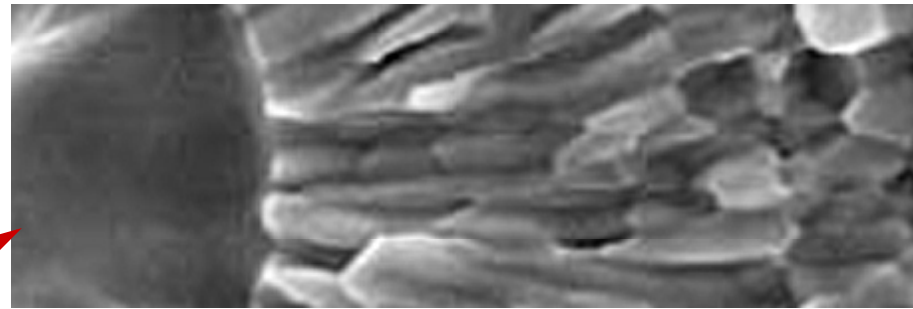
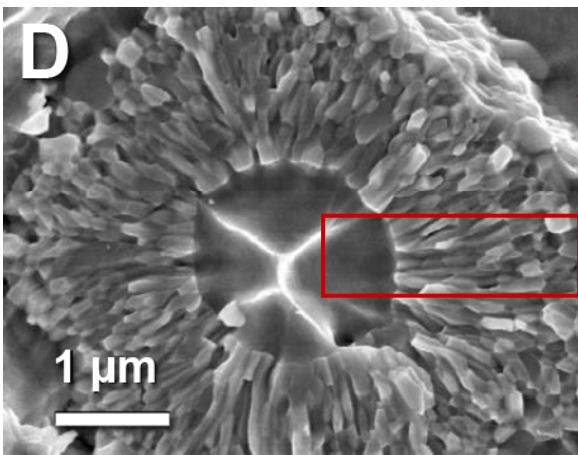


Made by many manufacturers

- Proven technology, large billets, very fine filaments, low loss, but...
- Limited J_c due to limited Sn source
 - Solubility of Sn in Cu < 16%
 - Sn depletion of source gives Sn gradients

Composition variation in Bronze wires

Bronze process wire



- 4 at.% Sn/μm
- $J_c(12T, 4.2) = 720 \text{ A/mm}^2$

Small A15 fraction is high Sn

Abächerli, TAS 2005

Powder-in-Tube wires from SMI-EAS

Process

- Powder: NbSn₂ plus Cu
- Tubes: pure Nb or Nb-7.5Ta
- Production unit ~45 kg net

Low loss (ITER) version

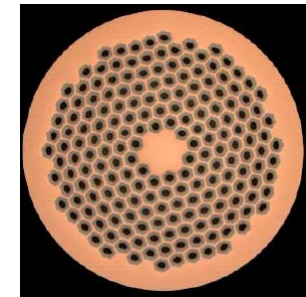
- 504 filaments @ 25 micrometer
- 0.81 mm
- 50% Cu
- 1350 A/mm² (Binary)
- 1950 A/mm² (Ternary)



M. Thoener: Wednesday 15.45

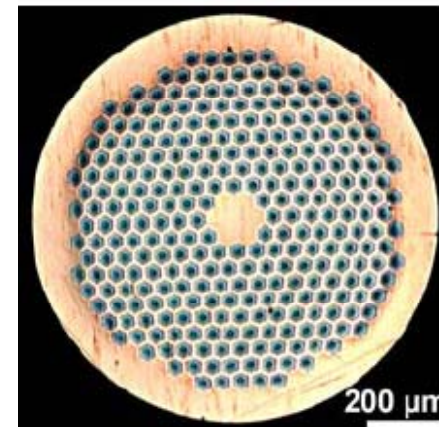
Maximum performance

- Non-Cu $J_c(12T, 4.2K)$ 2582 A/mm²
- 192 filaments, 1 mm
- 52% Cu



High current (NED) version

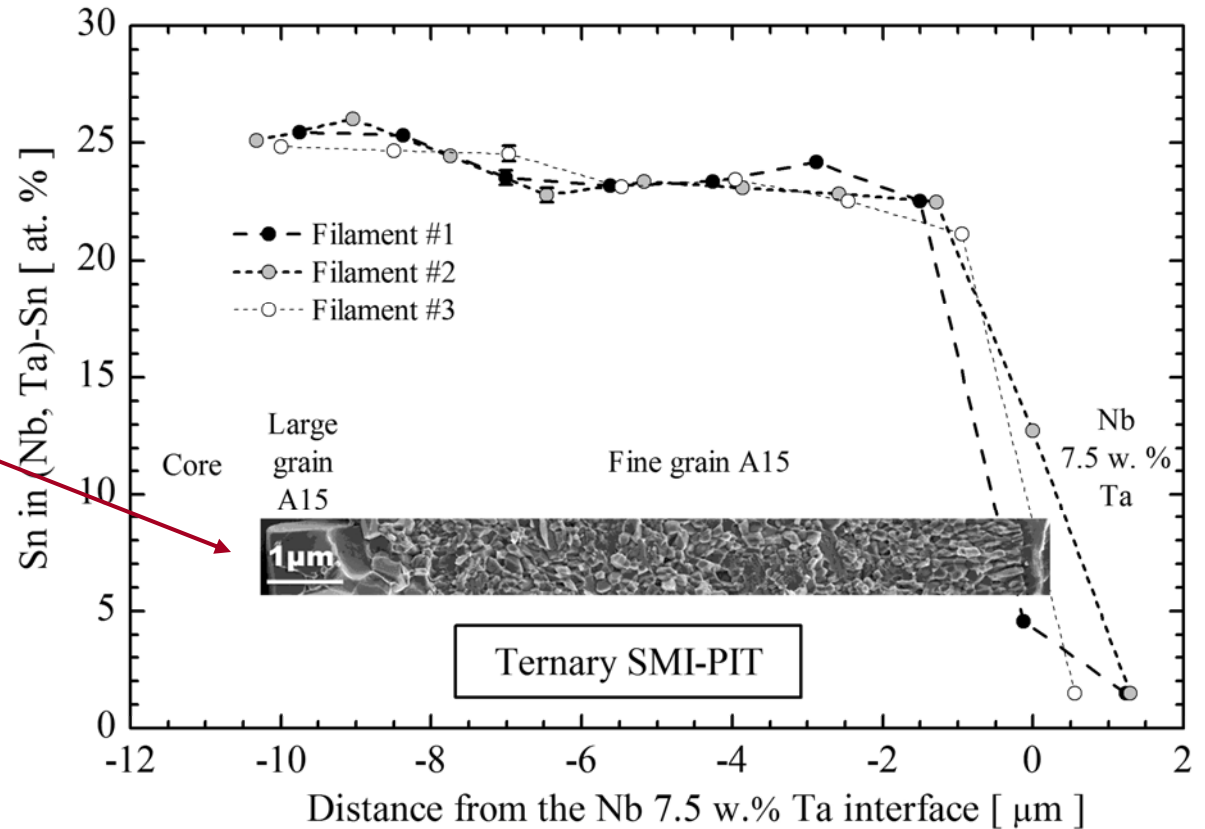
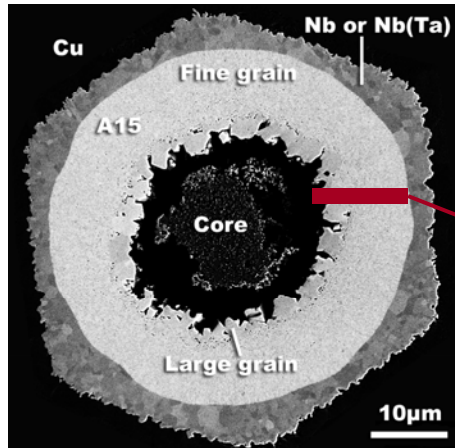
- 288 filaments @ 35 micrometer
- 1.25 mm
- 55% Cu
- 2500 A/mm² (Ternary)



Composition variation in PIT wires

Composition analysis on SMI Powder-in-Tube wire (from ~2001)

- 0.3 at.% Sn/ μm , $J_c(12\text{T}, 4.2) = 2250 \text{ A/mm}^2$ (Now ~2600)



Godeke, Cryogenics 2008

Large A15 fraction is high Sn

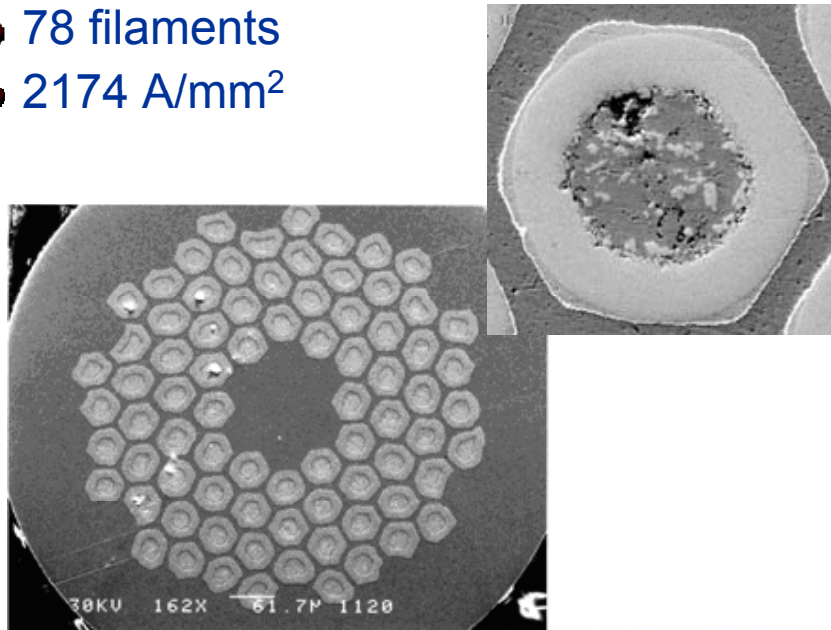
High current wires from Supercon

PIT with novel modifications

- Cost effective NbSn₂ powder
- Custom Nb-Ti and Nb-Ta alloy tubes
 - ➔ From fine grain Nb, Nb-7.5Ta and Nb-47Ti sheets
- Thin Ta barrier around each filament

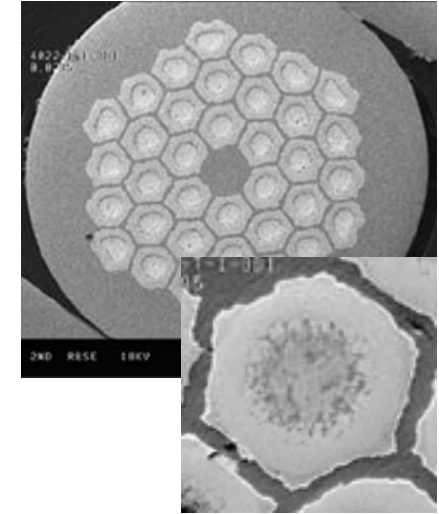
Best results

- Nb7.5wt.%Ta ternary
- 78 filaments
- 2174 A/mm²



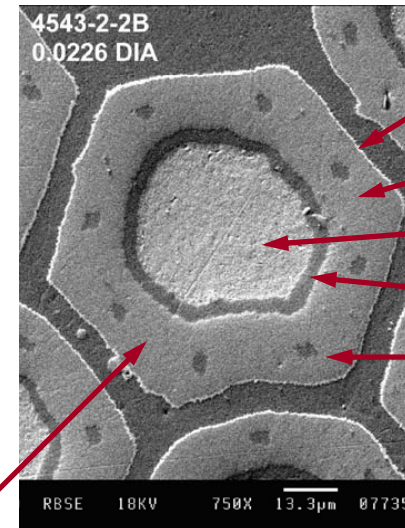
Internal-Tin-Tube process

- Nb-7.5Ta Tubes
- Sn-3Cu powder
- 36 filaments
- 1371 A/mm²



SUPERCON^{INC}

- Present work:



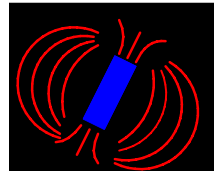
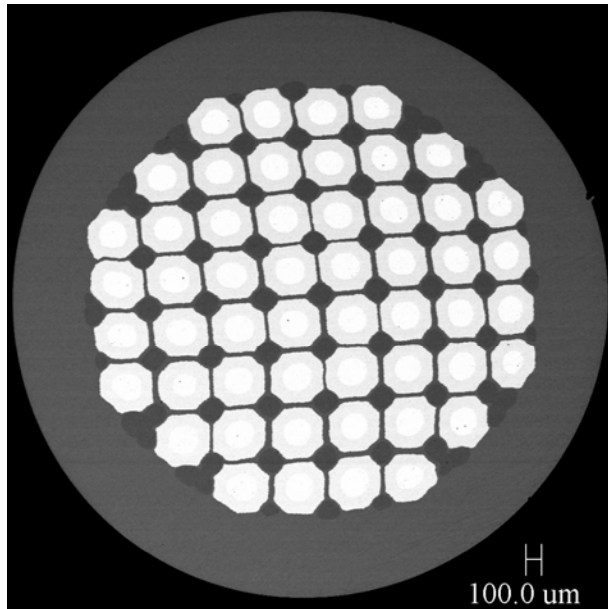
Ta
Nb
Sn
Cu
Nb-47Ti

- Becomes Nb 1.5 at.%Ti, 1800 A/mm²

Powder-in-Tube wires at SupraMagnetics

PIT with novel modifications

- Jet milled Cu_5Sn_4 powder
 - ➔ Cost effective, more Sn available
- Octagonal filament design allows for internal strengthening

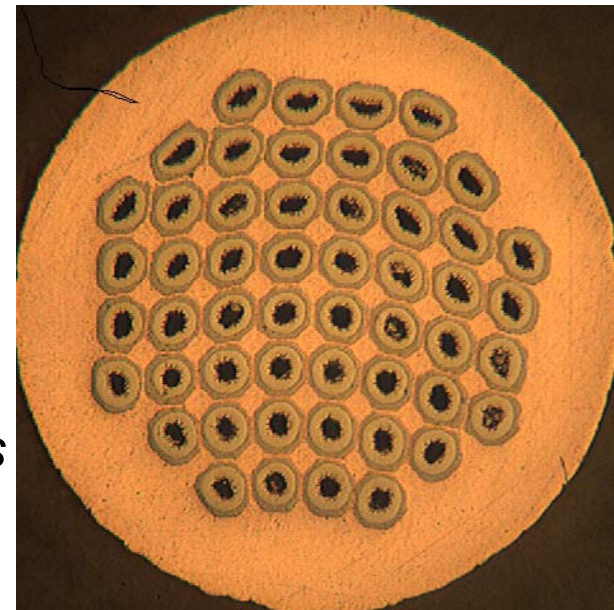


SupraMagnetics

- 52 filaments
- Drawn down to 0.25 mm (20 μm fil.)
- 17.2% Monel between filaments

New high strength conductor

- 52 filaments at 0.5 mm OD



- Octagonal filaments
 - Glid Cop Al-15
 - A15 layer 675Cx96h
- 
- $J_c \sim 2000 \text{ A/mm}^2$
 - ➔ In earlier hexagonal Cu_5Sn_4 wires

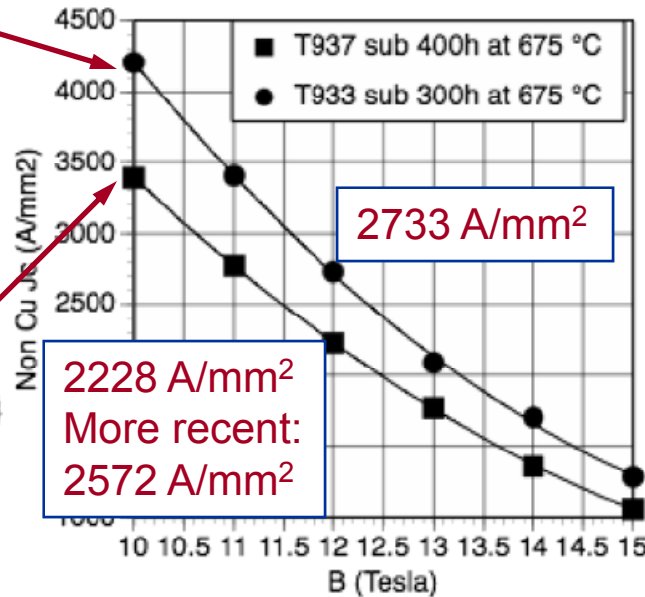
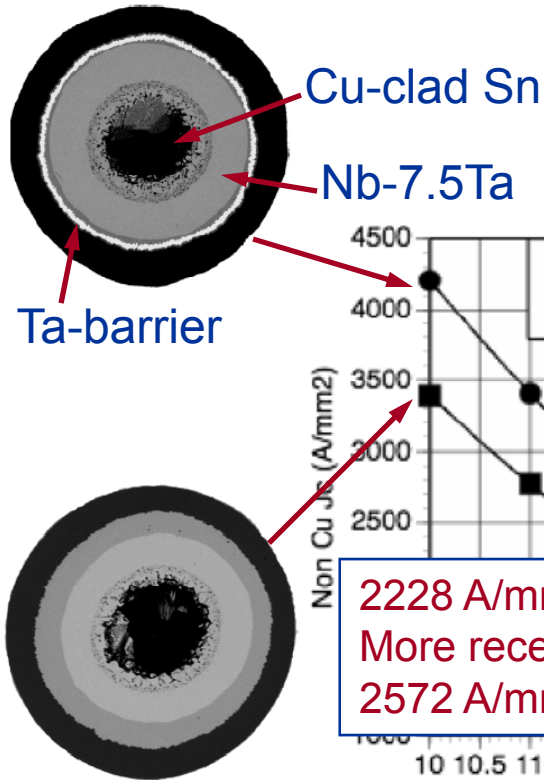
Tubular process at Supergenics I LLC

Process:

- Cu-clad Sn in Nb-7.5Ta tube
 - ➔ Sn can be pure or alloyed

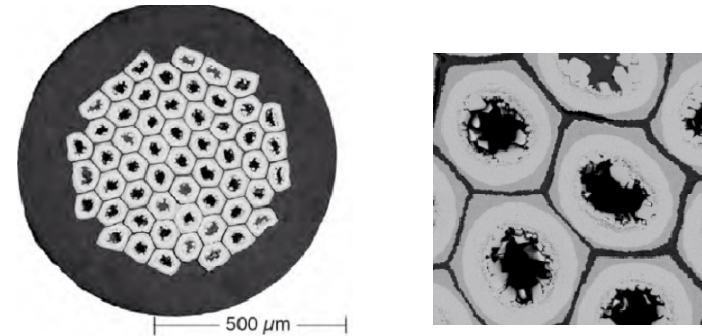
Pure Cu-clad Sn

- Sub-elements at 0.25 mm

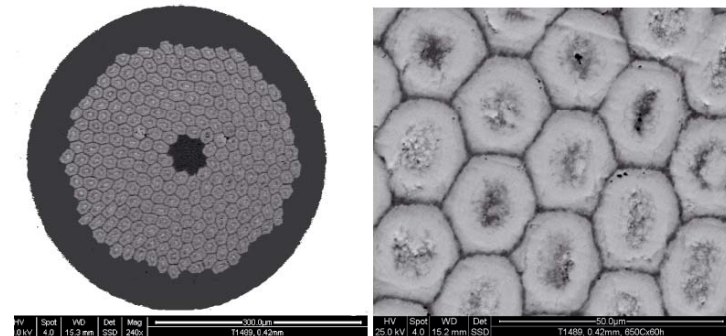


Wires

- ~0.8 mm, filaments 70 μ m, 55+6



- 0.42 mm, filaments 18 μ m, 246+25



Performance

- 2050 A/mm² at 18 μ m, 2250 @ 35 μ m
- Billet 37mm x 1m: 2km @ 0.7mm done
- Now: 37mm x 5m billet

Internal-Tin wires at OST

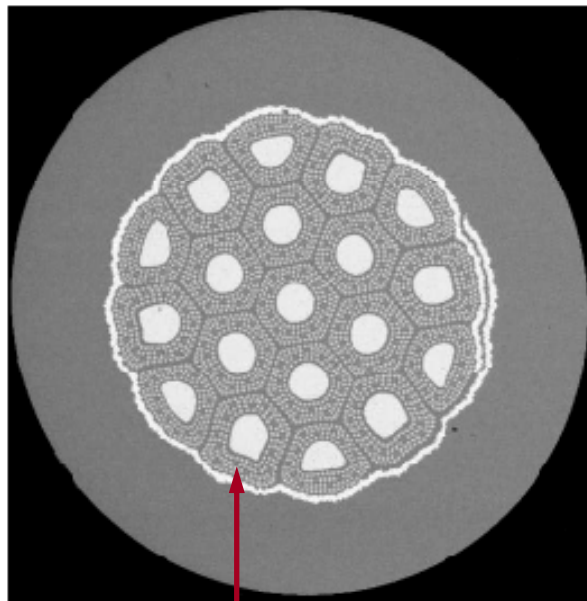
Modified Jelly Roll, Hot Extruded Rod → Rod Restack Process (RRP®) wires

Low loss, medium current

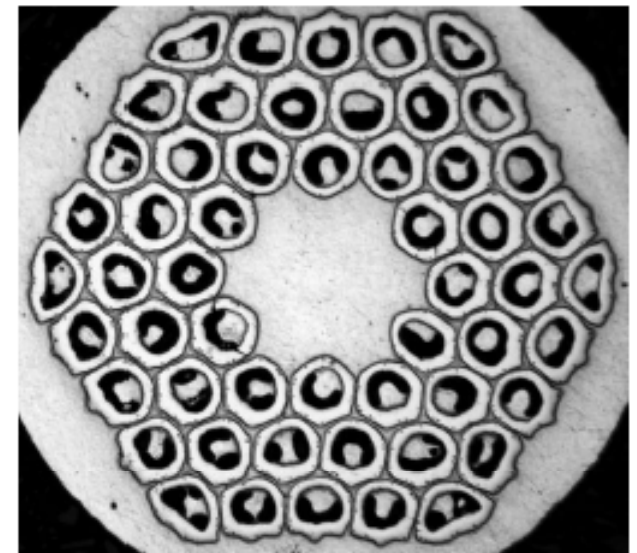
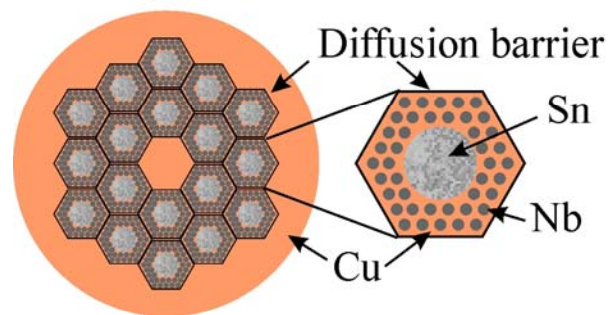
- Sub-element contains separate filaments after reaction
- $J_c(12T, 4.2K)$ 800 – 1200 A/mm²
- Single Ta diffusion barrier

High current 54/61

- Filaments in sub-elements grow together during reaction
- Record $J_c(12T, 4.2K) > 3$ kA/mm²
- Each sub-element has its own Nb-Ta diffusion barrier (partially reacts)

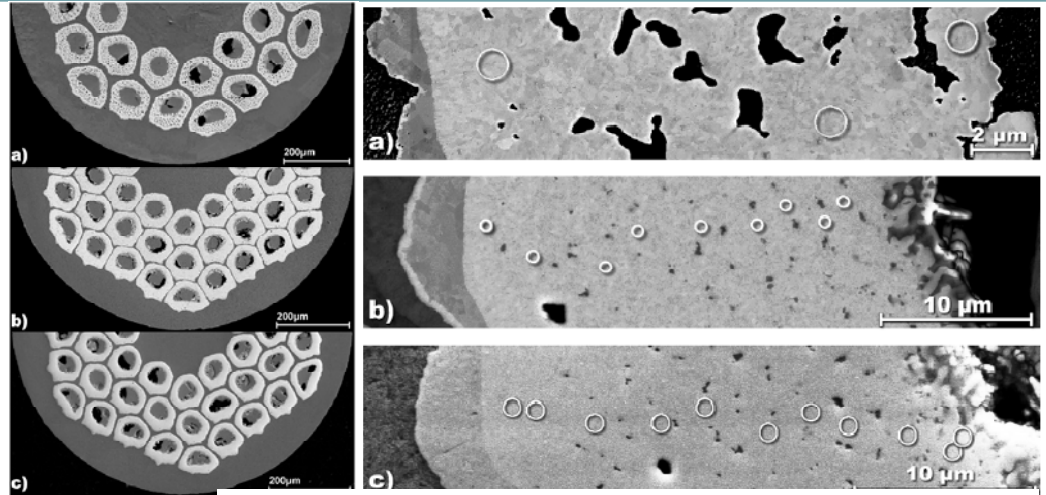


Nb-47w.%Ti rods



Composition variation in IT wires

- MJR1 $J_c(12T, 4.2) = 2200 \text{ A/mm}^2$
- RRP1 $J_c(12T, 4.2) = 2900 \text{ A/mm}^2$
- RRP2 $J_c(12T, 4.2) = 3000 \text{ A/mm}^2$

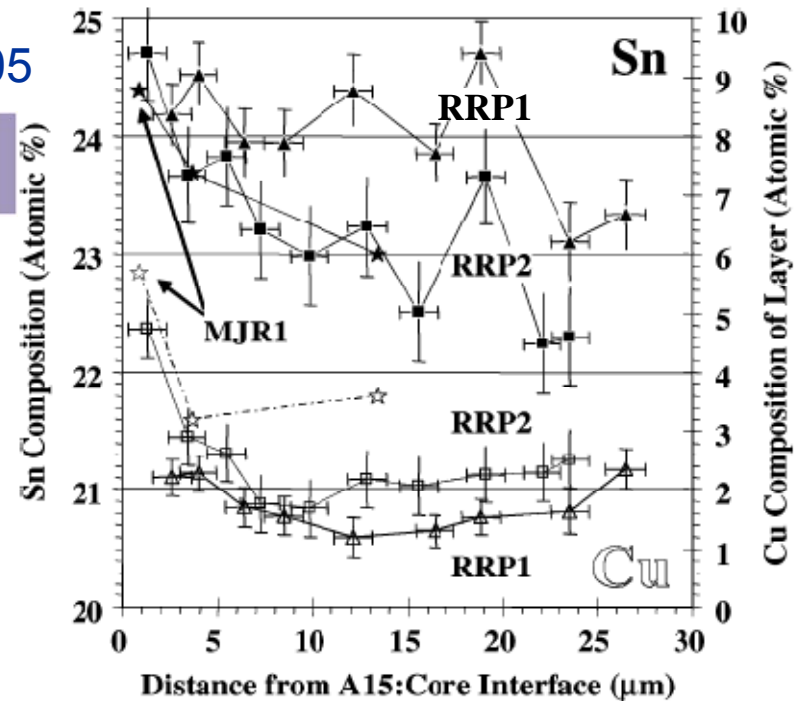


Lee, TAS 2005



- OST Internal-Tin
 - Inter-filament Cu
 - Relatively flat Sn gradient
 - Optimized A15 fraction in non-Cu

Large A15 fraction is close to optimal Sn

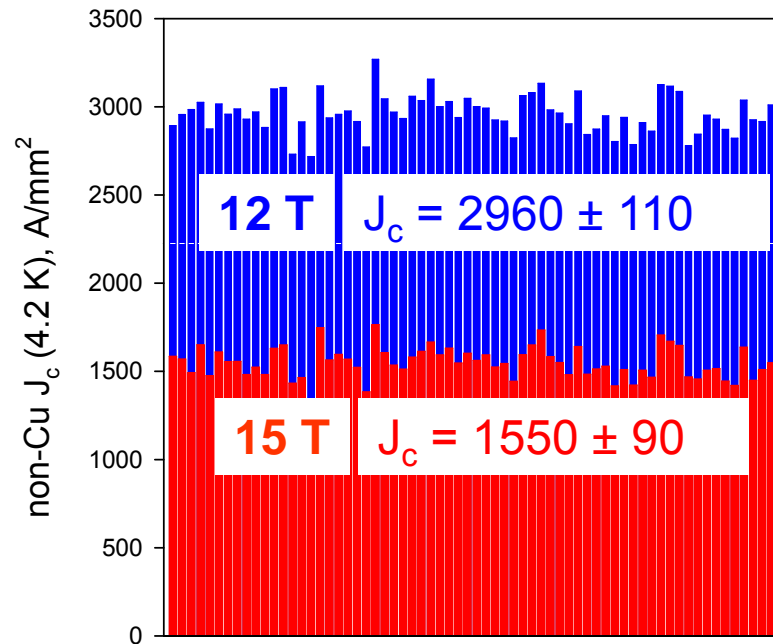


3 kA/mm² RRP[®] commercial production

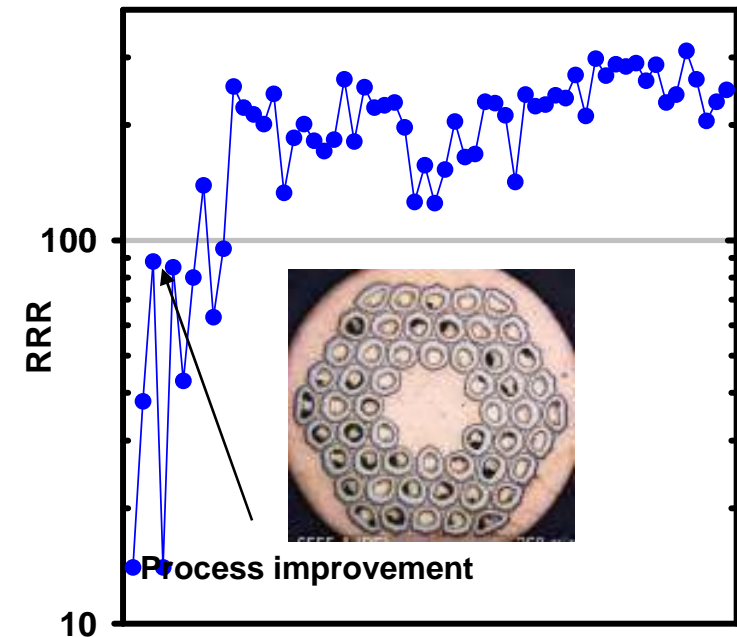
- Production measured in tons per year
- Consistent J_c and RRR
- Unit lengths >10 km



0.7mm and 0.8 mm strands $\sim 80\mu\text{m } d_{\text{eff}}$



Sampling of billets produced 2002-2007



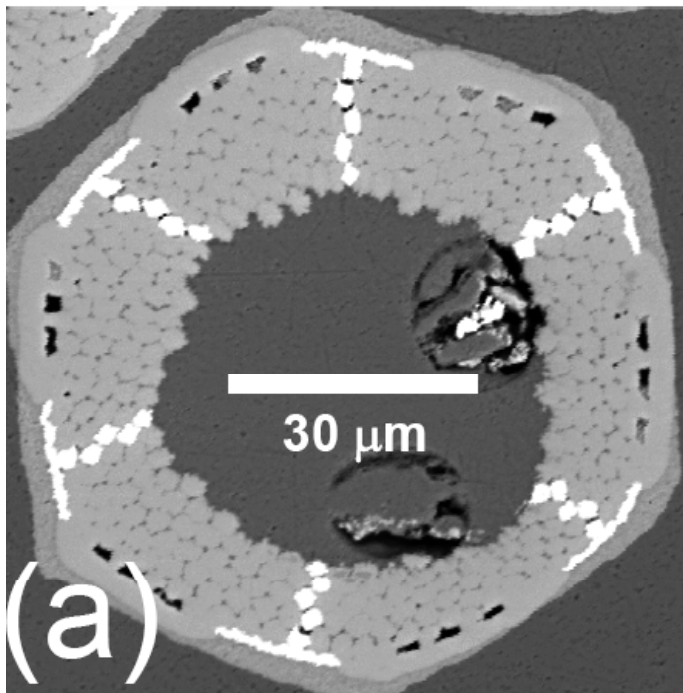
Sampling of billets produced 2002-2007

But...Large d_{eff} , very high J_c , cabling distorting barriers (RRR loss):
Low and medium field instabilities (Sumption and Bordini, this workshop)

Attempts at OST to reduce d_{eff}

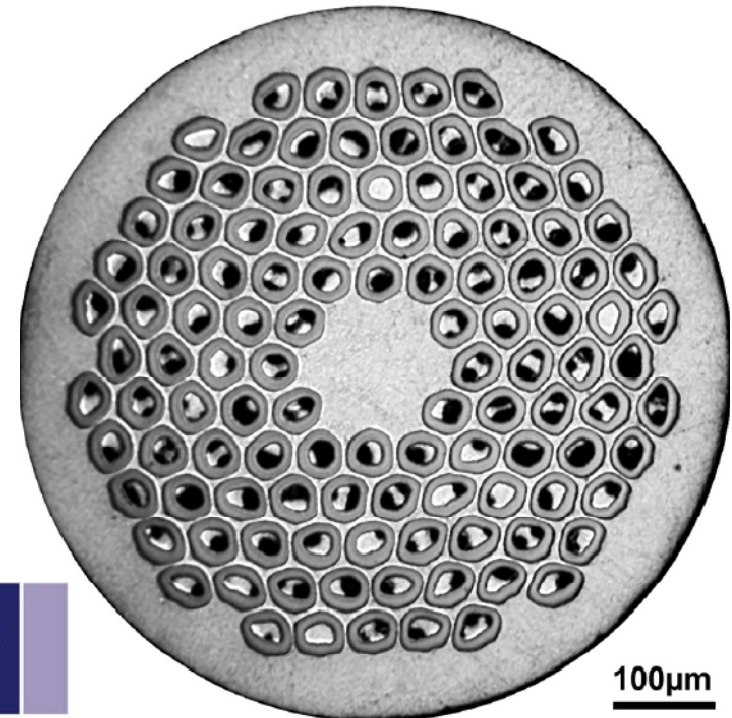
Sub-divided sub-elements

- Using Ta rods
- Now abandoned



Restacking

- 114 – 127 version ($\sim 40 \mu\text{m}$)
- Further restacks under development



Restacking appears route towards smaller d_{eff}



An outlook to the future

(An academic exercise on performance potential)



General trend: Increasing J_c with increasing Sn

Geneva Bronze Process	25 at.% Sn @ source 4 at.% Sn/μm gradient	$J_c(12\text{T},4.2) =$ 720 A/mm²
SMI Powder-In-Tube	25 at.% Sn @ source 0.3 at.% Sn/μm gradient	$J_c(12\text{T},4.2) =$ 2250 A/mm² (2600 A/mm²)
OST Internal Tin	24 \pm 1 (or more?) at.% Sn Virtually no gradient	$J_c(12\text{T},4.2) =$ 3000 A/mm²

**Sn richer
Higher J_c**

→ Homogenization potential exhausted?

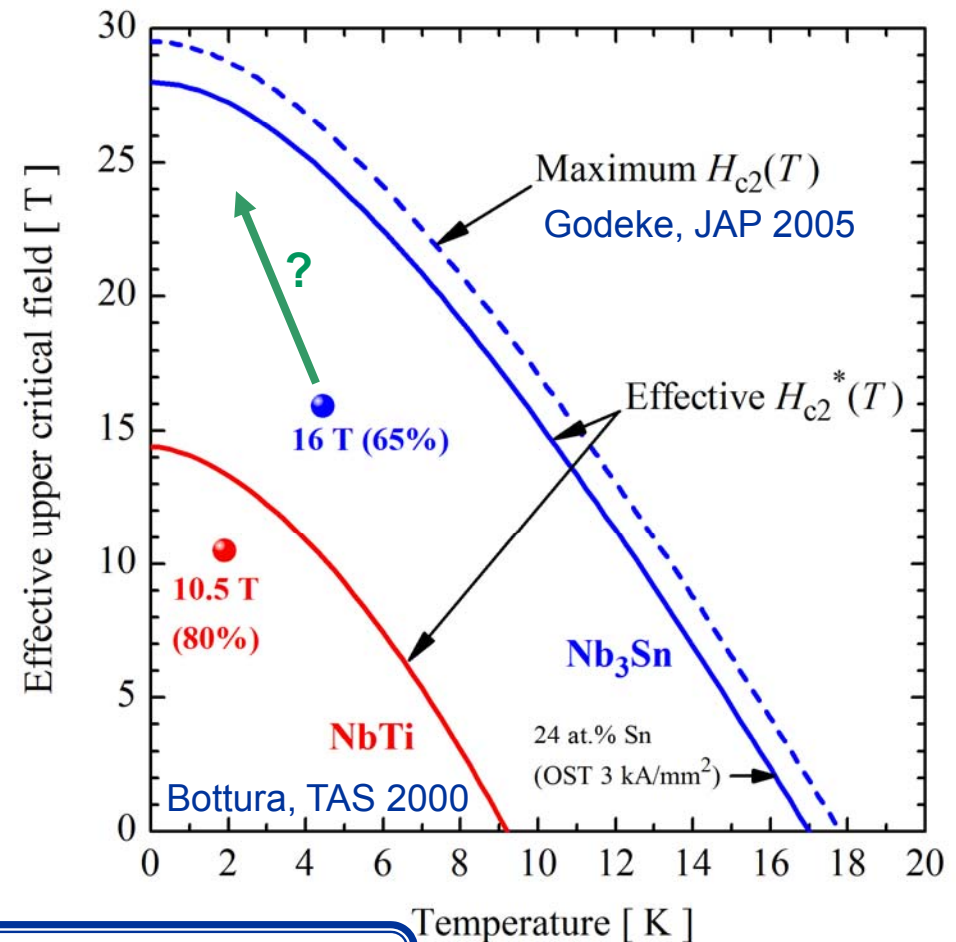
Nb₃Sn wire performance in dipole magnets

Field – temperature limitations and achieved dipole fields

- NbTi
 - ➔ 10.5 T (Leroy, Proc. MT15 1998)
 - ➔ 80% of H_{c2}^* (1.8 K)

- Nb₃Sn
 - ➔ 16 T (LBNL HD1, 2004)
 - ➔ 65% of H_{c2}^* (4.5 K)

 - ➔ 80% of H_{c2}^* (4.2 K)?
 - ➔ 20 T
 - ➔ 80% of H_{c2}^* (1.8 K)?
 - ➔ 22 T



What limits Nb₃Sn to 65% of H_{c2}^* ?



What limits high field performance of Nb₃Sn?

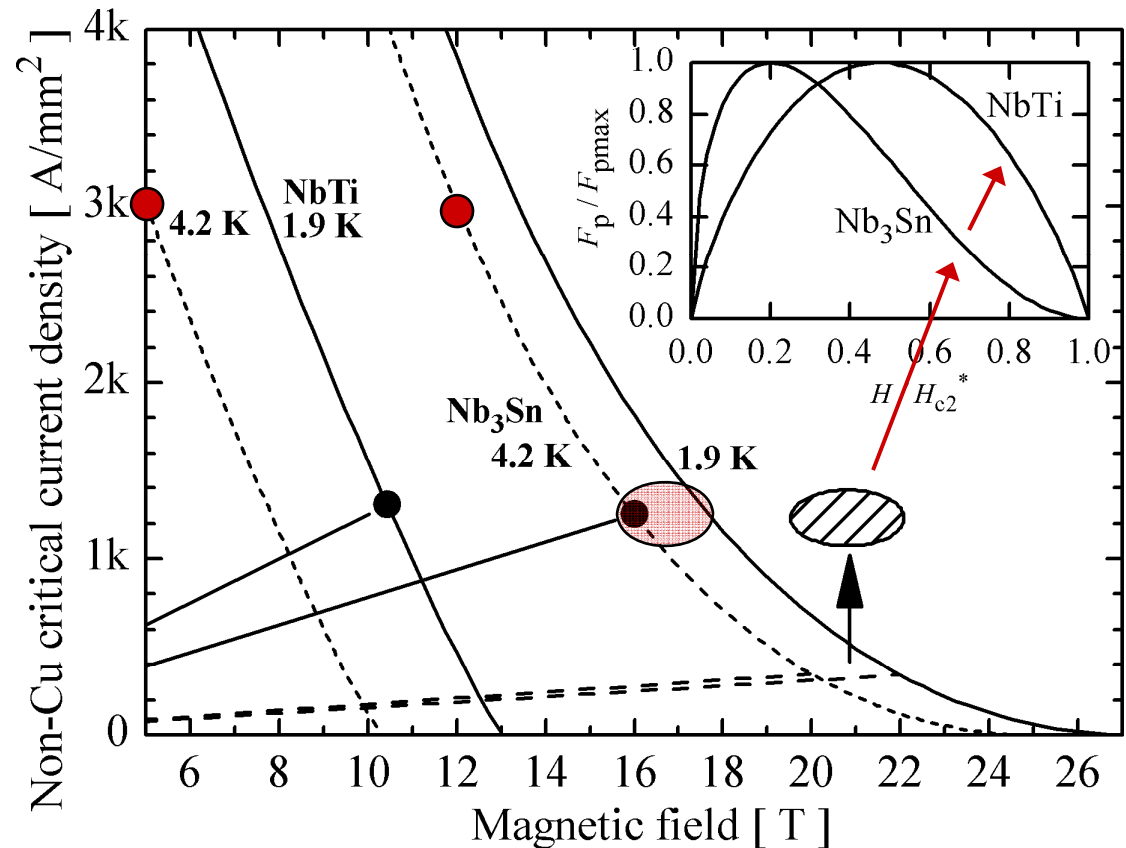
NbTi

- Pinning optimized
 - ➔ ~1 pinning cite/vortex
 - ➔ $F_p \propto h(1 - h)$

NbTi: Bottura, TAS 2000
 Nb₃Sn: Godeke, SuST 2006

Nb₃Sn

- Insufficient pinning centers
 - ➔ Collective pinning
 - ➔ $F_p \propto h^{0.5}(1 - h)^2$
 - ➔ Reduced high field efficiency
- Practical dipole limitation 17 – 18 T

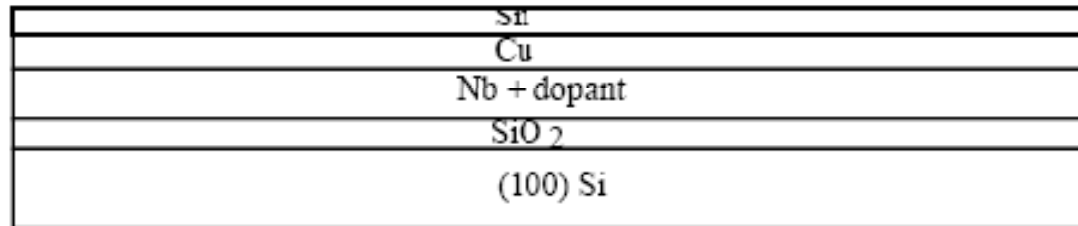


Pinning inefficiency at higher fields limits performance

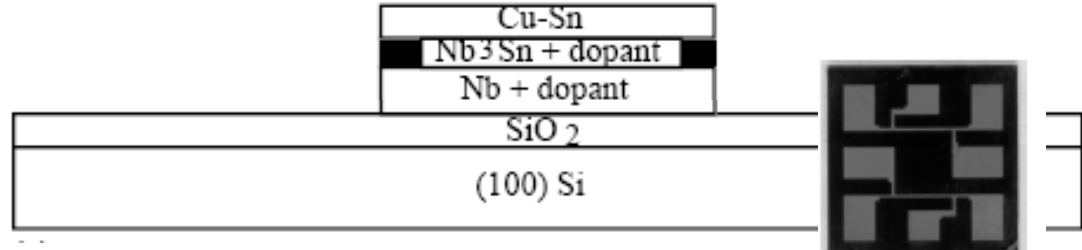
Can high field pinning be improved?

Doping in thin films (Dietderich, ACE 1998)

- As deposited



- After HT and etch

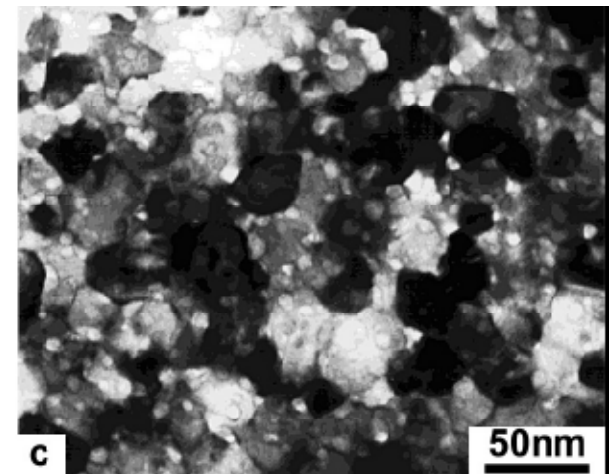
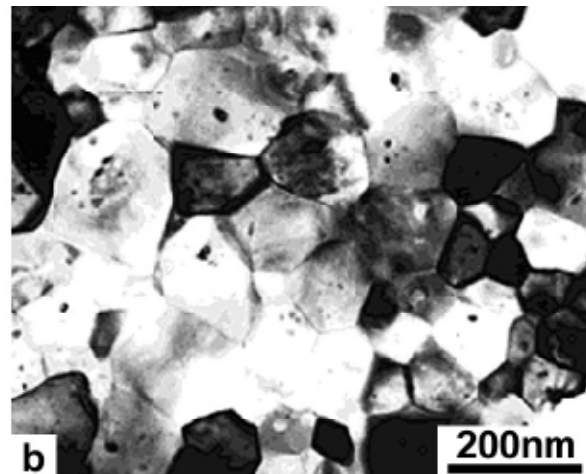
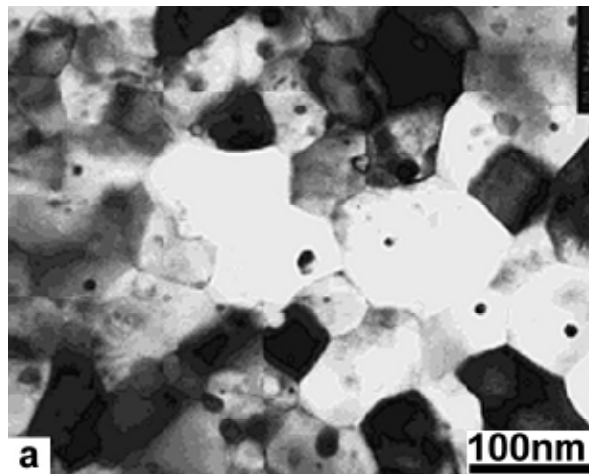


Average grain sizes:

Undoped: 75 nm

Ti-doped: 130 nm

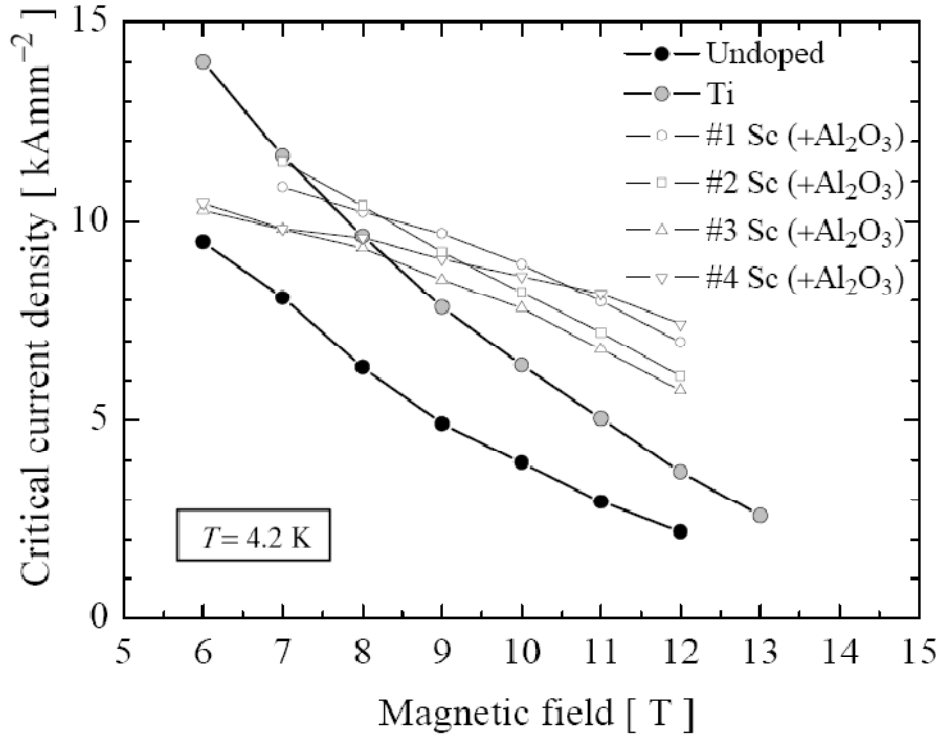
Sc+Al₂O₃ doped: 25 & 7 nm



Improved high field pinning

Field dependence of J_c

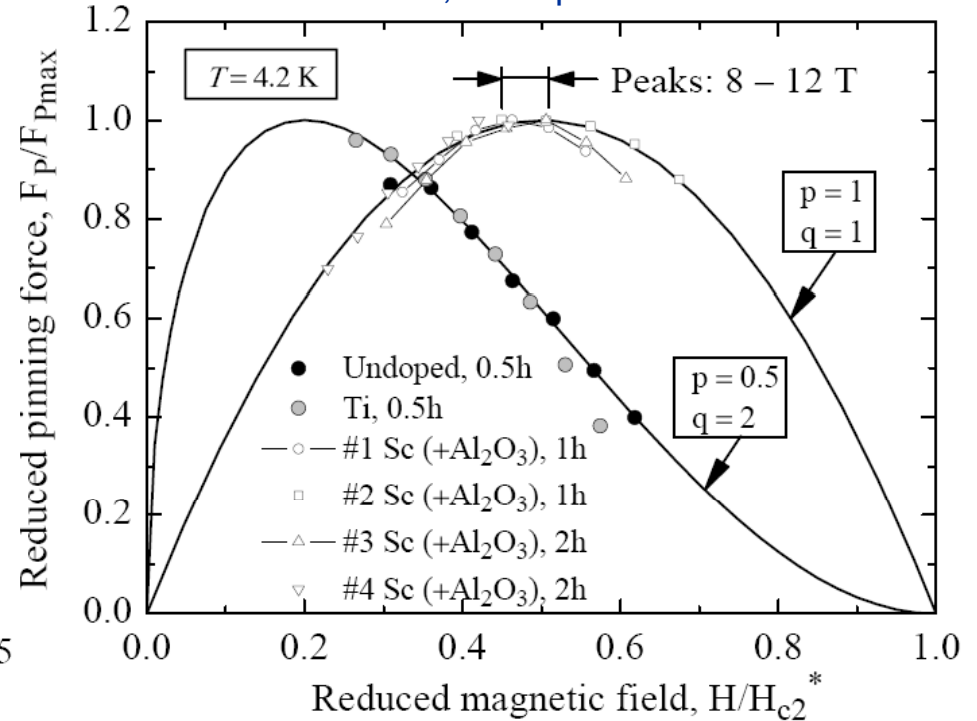
- $J_c(12T, 4.2K)$:
 - ➔ Undoped 2200 A/mm² x3.4 (!)
 - ➔ Ti-doped 3700 A/mm²
 - ➔ Sc+Al₂O₃ doped 7400 A/mm²



Normalized pinning curves

- Peaks at 50% of H_{c2}^*

Dietderich, Cryogenics 2008
Godeke, to be published 2008



Grain refinement could be the next big step (but how to do this in wires...?)



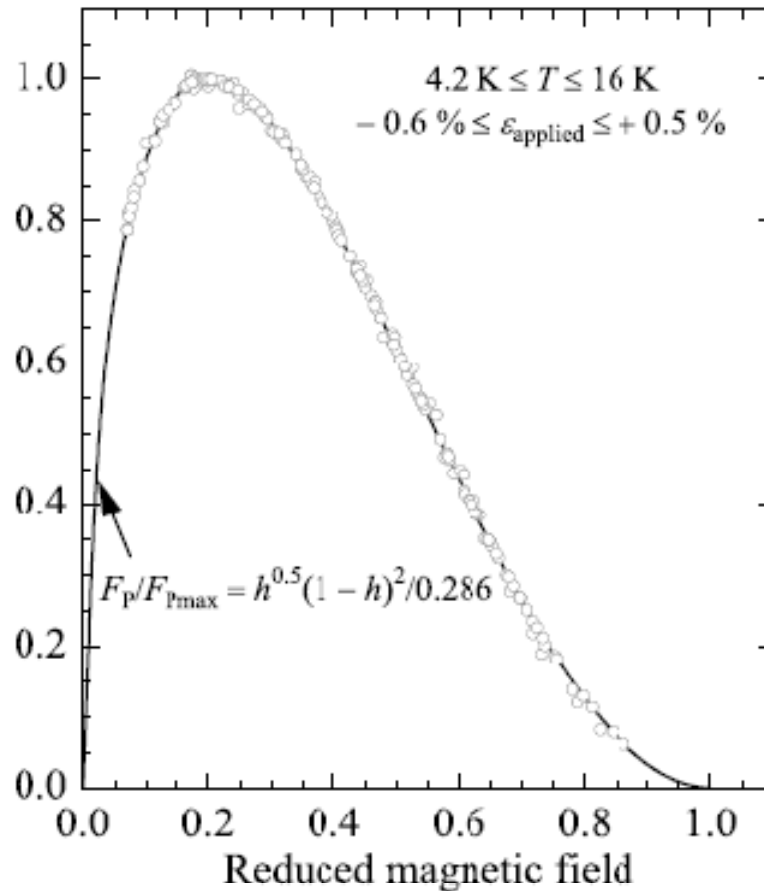
Some words on scaling...

A tool to describe the critical surface

$$J_c = F_p(H) + H_{c2}^*(T)$$

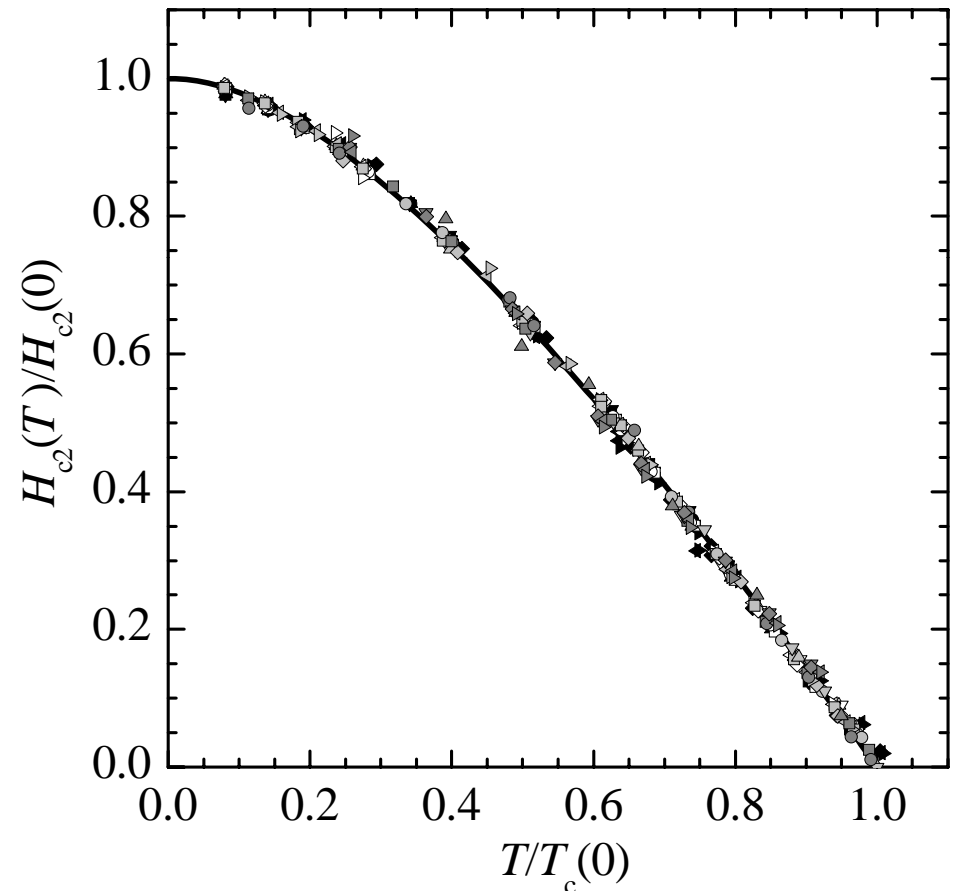
Pinning force as a function of field

- Example: Furukawa bronze wire
- All temperatures and strain states



Field-temperature phase boundary

- All literature results (27 samples)
- Thin film, bulk, single X-tals, wires



Scaling of J_c can be done accurately

Twente scaling relation for $J_c(H, T, \epsilon)$



University of Twente

- $J_c(H, T, \epsilon)$ data & general form



Applied Superconductivity Center

- Materials basis

$$J_c(H, T, \epsilon) \cong \frac{C_1}{\mu_0 H} s(\epsilon) \underbrace{(1 - t^{1.52})}_{(p)} (1 - t^2) h^{0.5} (1 - h)^2, \quad (q)$$

Godeke, SuST 2006

with

$$C_1 = C [\mu_0 H_{c2m}^*(0)]^2 / \kappa_{1m}(0),$$

$$t \equiv T/T_c^*(\epsilon), \quad h \equiv H/H_{c2}^*(T, \epsilon),$$

$$H_{c2}^*(T, \epsilon) \cong H_{c2m}^*(0) s(\epsilon) (1 - t^{1.52}),$$

$$T_c^*(\epsilon) = T_{cm}^* s(\epsilon)^{\frac{1}{3}},$$

More accurately:

$$MDG(t) \cong (1 - t^{1.52})$$

Longitudinal strain description:

$$s(\epsilon_a) = \frac{1}{1 - C_{a1} \epsilon_{0,a}} \left(C_{a1} \left[\sqrt{(\epsilon_{sh})^2 + (\epsilon_{0,a})^2} - \sqrt{(\epsilon_a - \epsilon_{sh})^2 + (\epsilon_{0,a})^2} \right] - C_{a2} \epsilon_a \right) + 1,$$

$$\epsilon_{sh} = \frac{C_{a2} \epsilon_{0,a}}{\sqrt{(C_{a1})^2 - (C_{a2})^2}},$$

$$\epsilon_a = \epsilon_{applied} + \epsilon_m.$$

6 fit parameters:

Deformation			Superconducting		
C_{a1}	C_{a2}	$\epsilon_{0,a}$	$\mu_0 H_{c2m}^*(0)$	$T_{cm}^*(0)$	C_1
47.6	6.4	0.273	30.7	16.8	46.3

Accepted by ITER in 2008
with p and q variable

Mathematical simplification

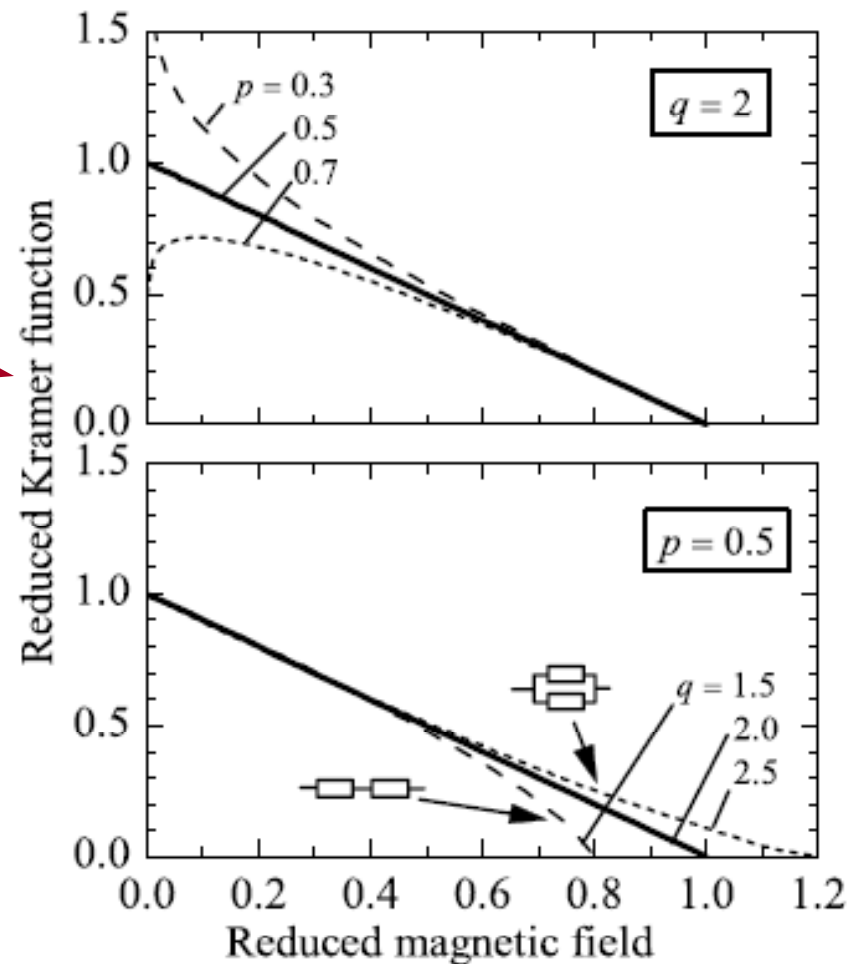
Matthijs Mentink (Univ. of Twente) @ LBNL, 2008:

$$J_c(H, T, \varepsilon) = \sqrt{2} C \mu_0 H_c(t) h^{p-1} (1-h)^q$$

Relevant:

- p and q
 - ➔ I.e.: Linearity of Kramer plots
 - ➔ $F_K = J_c^{0.5} B^{0.25}$ vs B
 - linear if $p=0.5, q=2$
- Thermodynamic critical field

$$H_c(t) \cong H_c(0)(1-t^2)$$

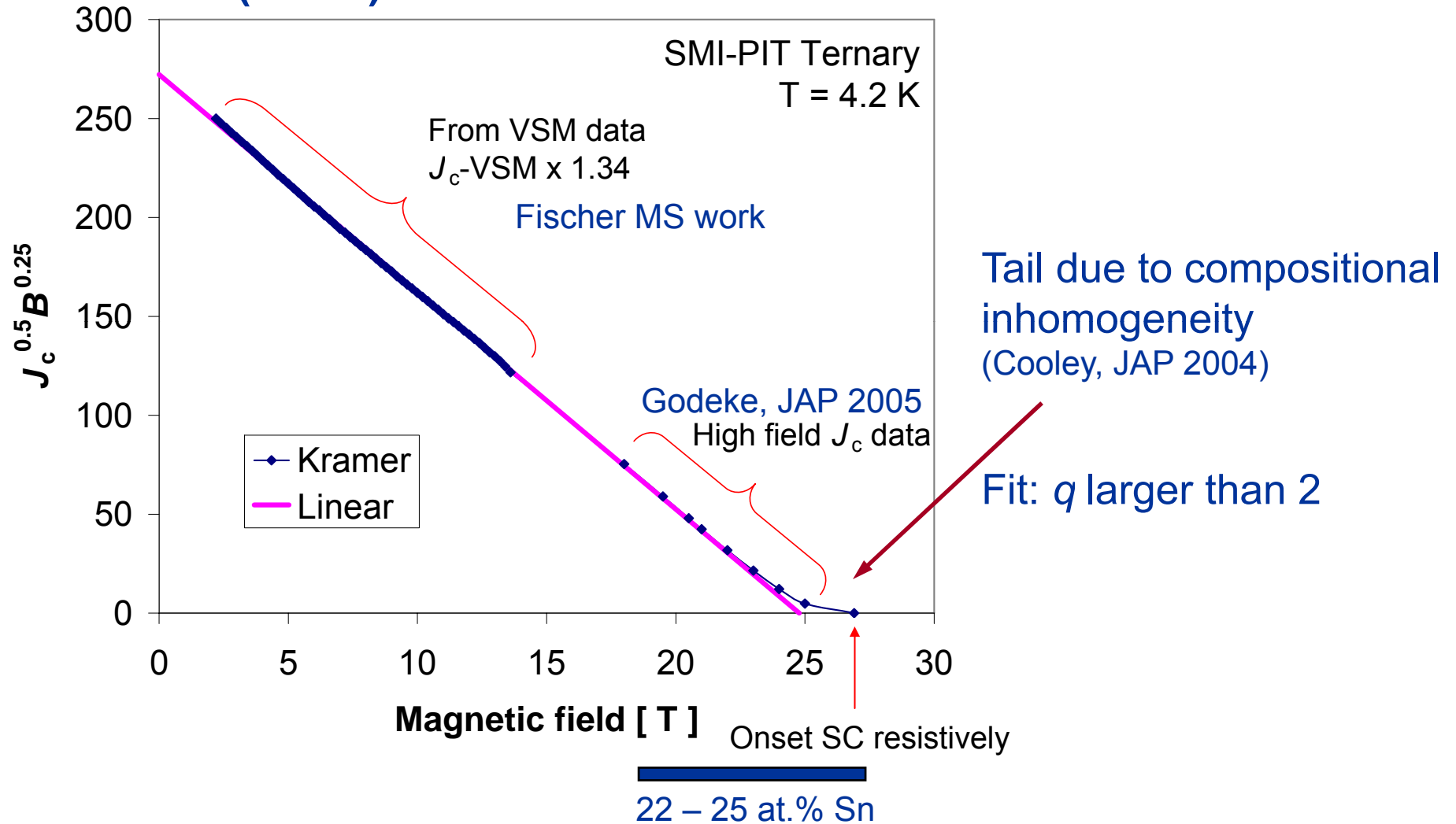


Godeke, Thesis 2005



How linear are Kramer plots? (I)

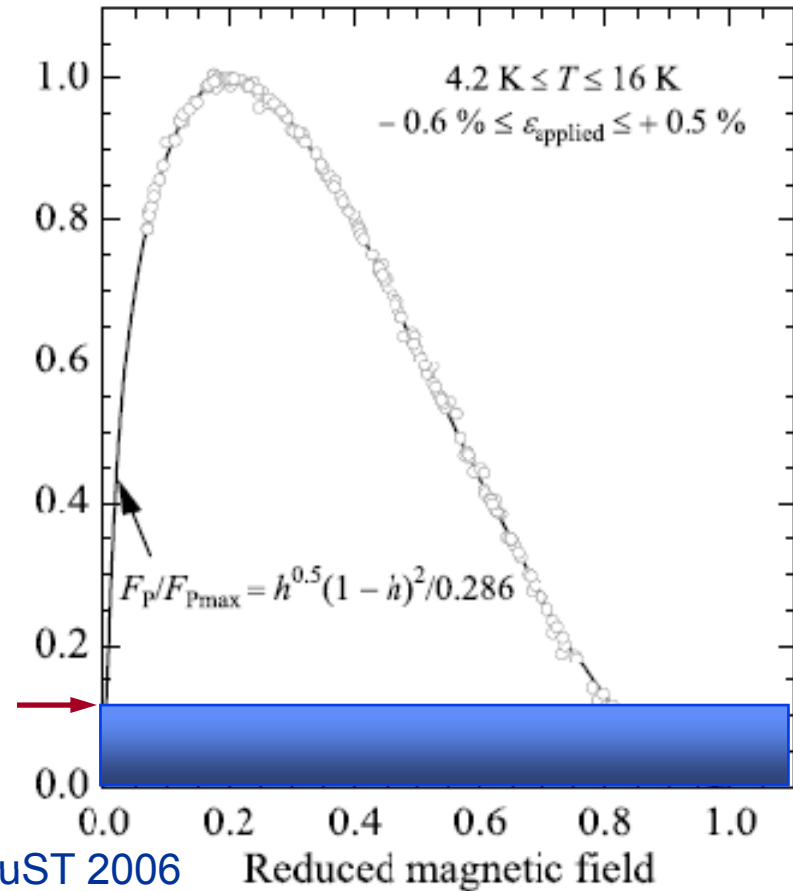
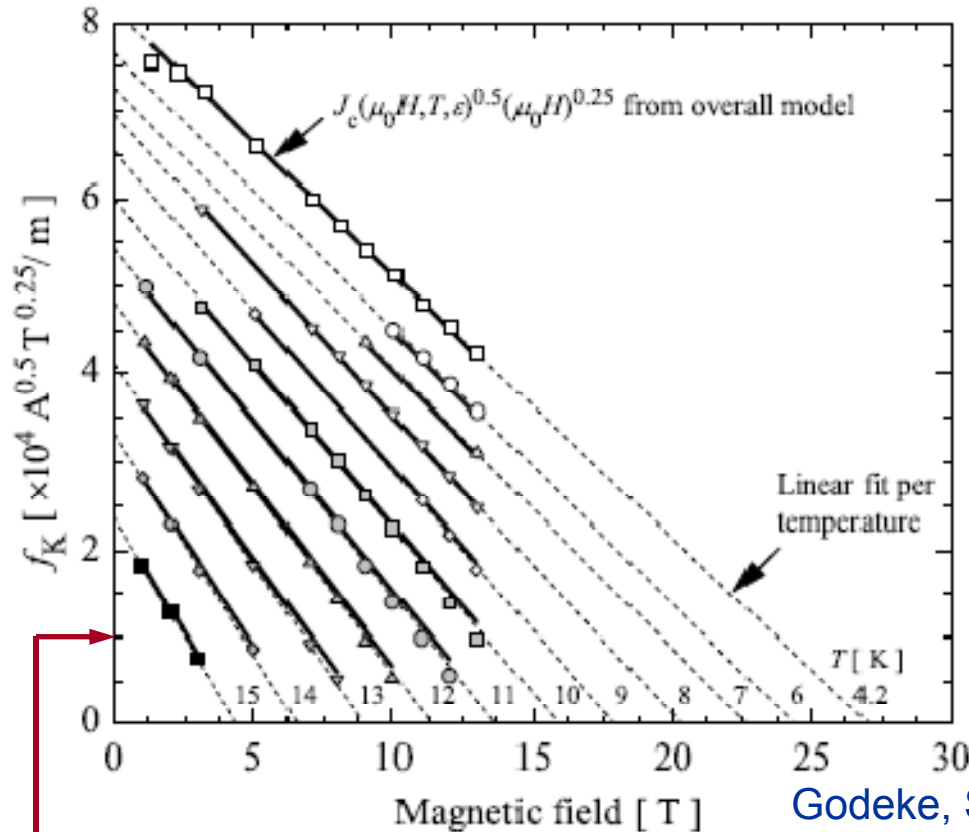
SMI-PIT data (~2003)



Kramer plots can be very linear

How linear are Kramer plots? (II)

Furukawa ternary bronze (~1998)



Below this less relevant for applications $\rightarrow q = 2$ to remain generic?

Generality *apparently* retainable by keeping $q = 2$, **BUT...**

Simulation of three homogeneous conductors

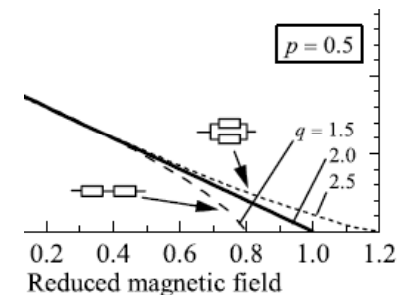
Mentink, 2008

- 3 homogeneous conductors in parallel

$$H_c(t) \cong H_c(0)(1-t^u)$$

at.% Sn	T_c^*	H_{c2}^*	p	q	u
22%	12	20	0.5	2	2
23%	15	25	0.5	2	2
24%	17	30	0.5	2	2

$$J_c(H, T, \varepsilon) = \sqrt{2} C \mu_0 H_c(t) h^{p-1} (1-h)^q$$



- Overall fit with $p = 0.5$ and $q = 2$ enforced yields $u = 1.6$
 - An *apparent* different temperature dependence of H_c occurs
 - But we defined $u = 2$ for each independent conductor!
 - $u = 2$ can be retained if q is larger than 2 (which it should)

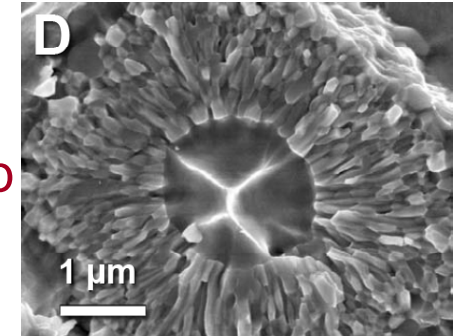
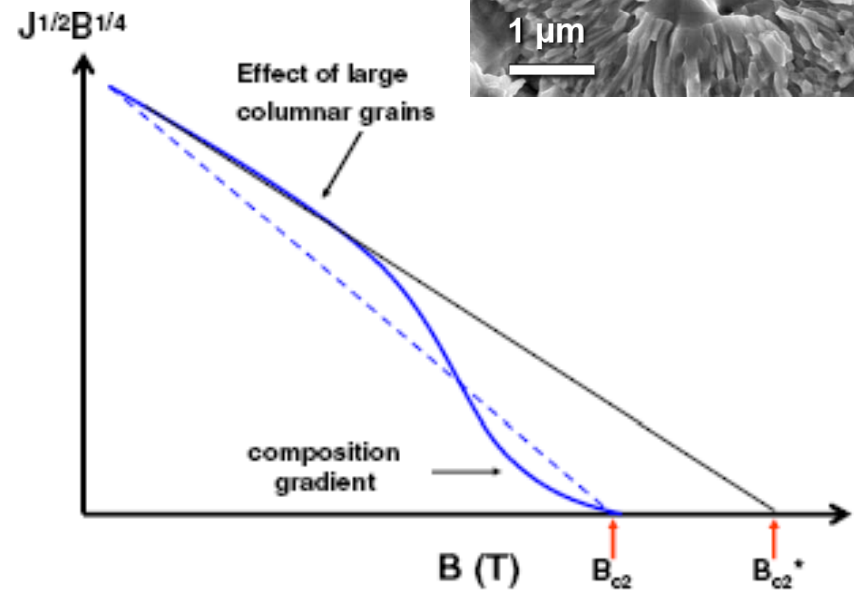
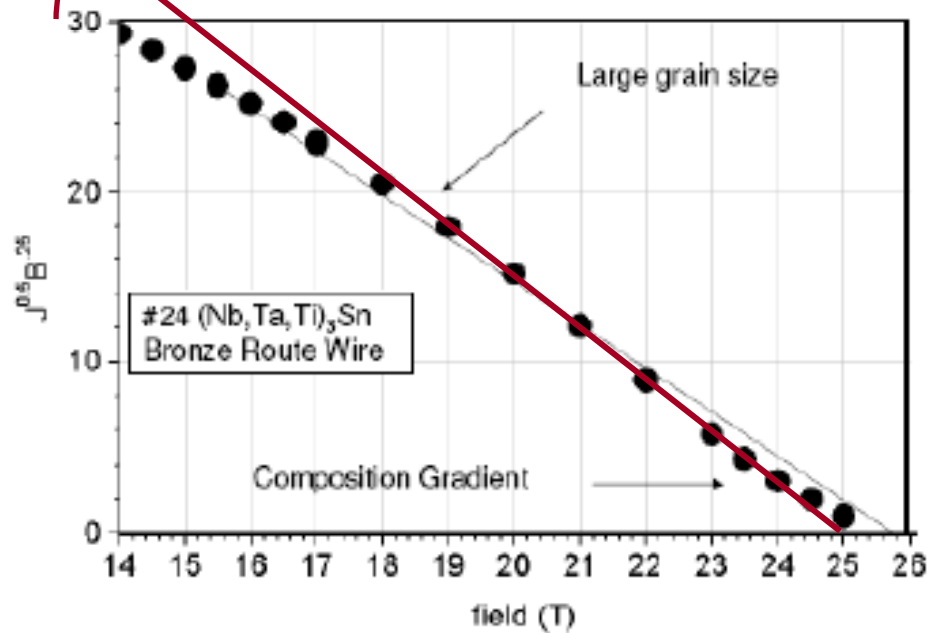
Inhomogeneities have to be accounted for by allowing q variable

What about p ?

Flükiger, SuST 2008

- Kramer plots bronze wires

Applying (more?) self-field correction can swing this up



- Low field behavior: large, columnar, Sn poor grains + fine, Sn rich grains
- High field behavior: fine, equiaxed, Sn rich grains + compo. averaging

Having q (and p) variable does not seem such a bad choice



Summary

Optimizations of...

- Sn content
- homogeneity
- A15 fraction

...led to commercially available > 3000 A/mm² and very high field magnets

- Combining high J_c with smaller filaments is present development

Future optimizations could include

- Grain refinement/APC → Very large potential (x2 – x3)
- Further optimization of A15 fraction in non-Cu (retain Sn source for A15)

Scaling relations

- Have become accurate and refined (but appear a never ending story...)
- ...**but** fundamental understanding of strain dependence is sorely lacking
 - This needs to be known for multi-billion \$ applications
 - Fundamental knowledge might provide ways to ‘tweak’ strain dependence
 - How much would it really cost to properly tackle this?