

# 125-126 GeV Higgs mass & scalar dark matter

FLASY2014, 17-21 June 2014

**Naoyuki Haba** (Shimane U, Japan)

H. Ishida, K. Kaneta, R. Takahashi, NH,  
arXiv:1406.0158 [hep-ph].



# contents

- §1 introduction
- §2 standard model + scalar DM +  $v_R$
- §3 numerical analyses
- §4 Higgs inflation
- §5 summary



# §1 introduction

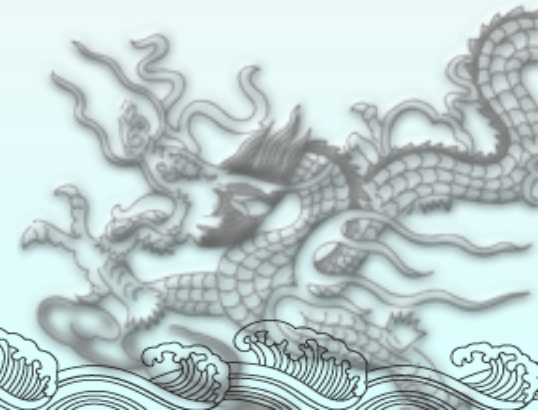
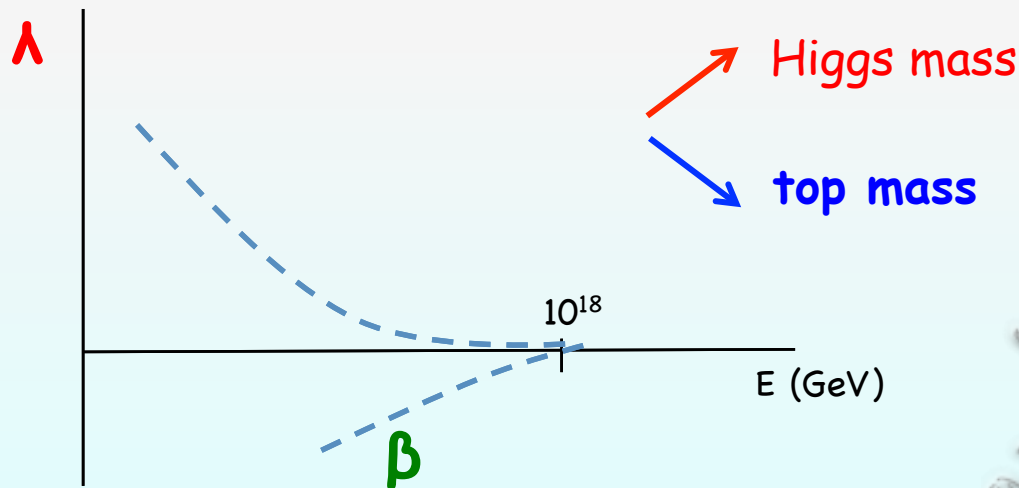


# Higgs (but still no BSM) discovery at LHC

$m_H = 125.9_{\pm 0.4} \text{ GeV}$ ,  $m_{\text{top}} = 172.58 \sim 174.10 \text{ GeV}$  in the SM  
combine LHC/Tevatron  $\sim 2\sigma$  (arXiv:1403.4427 [hep-ex])

## RGE of Higgs self coupling

$$(4\pi)^2 \frac{d\lambda}{dt} = \underline{12\lambda^2} + 12\lambda y_t^2 - \underline{12y_t^4} - 3\lambda(g'^2 + 3g^2) + \frac{3}{8}[2g^4 + (g'^2 + g^2)^2]$$

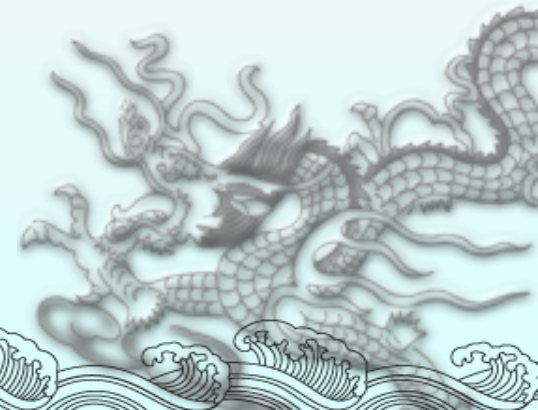
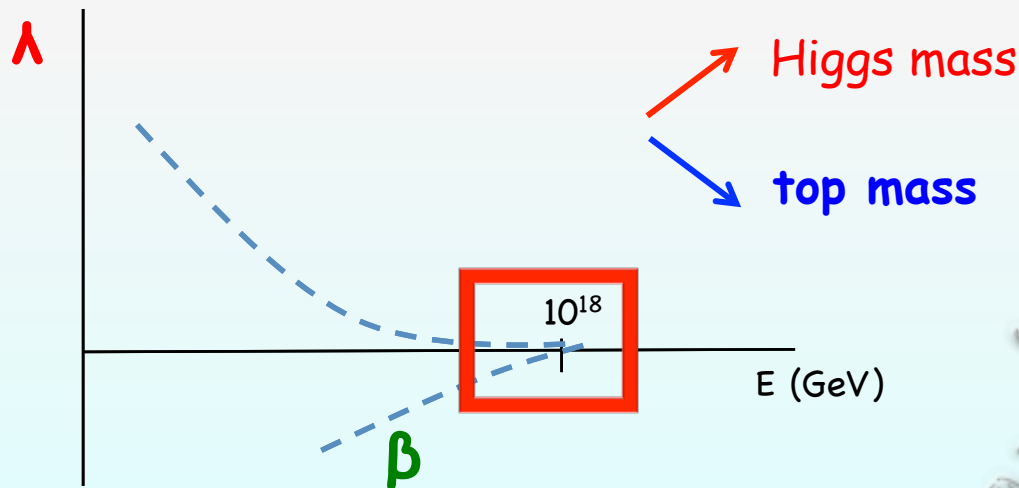


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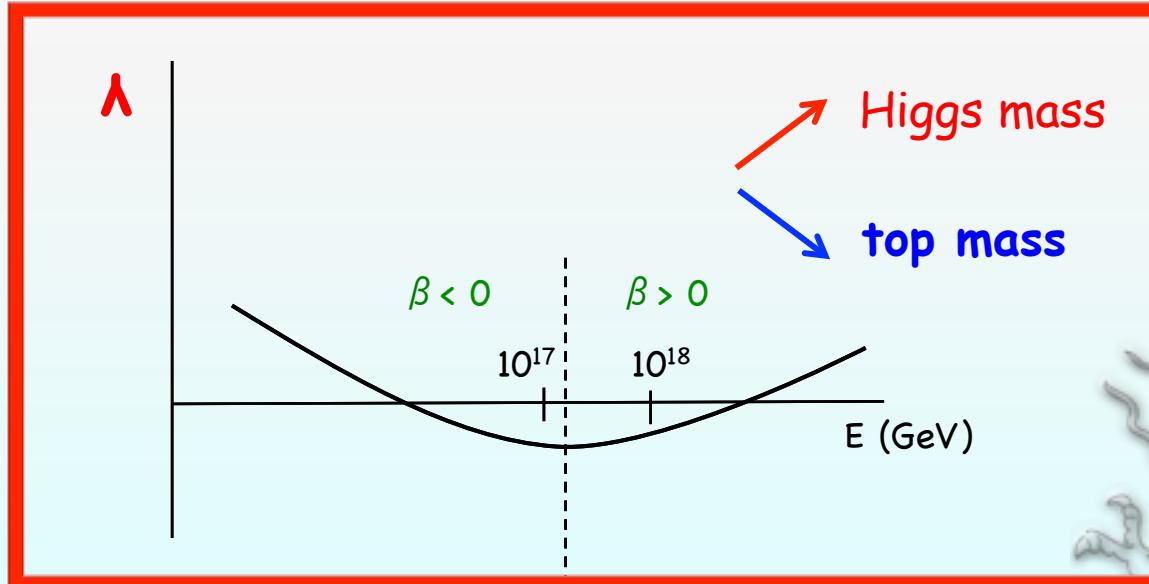


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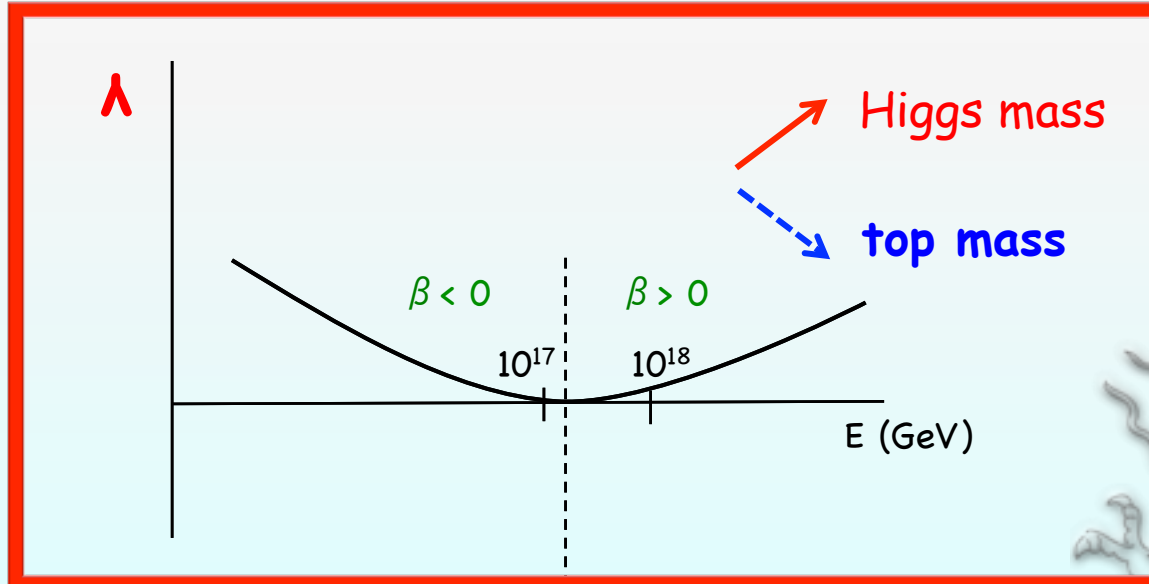


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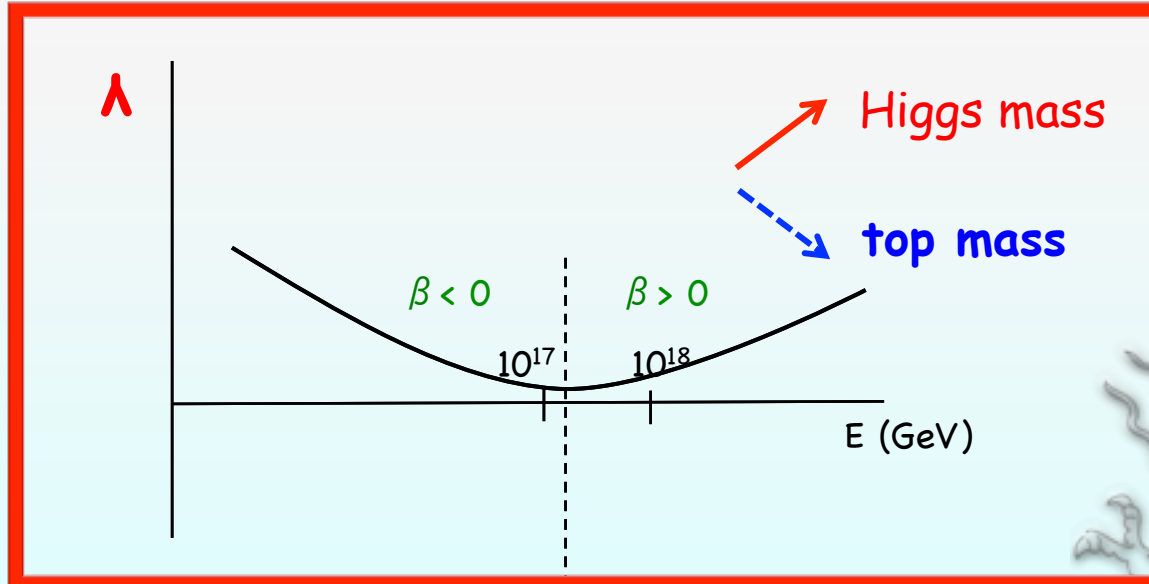


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# Higgs potential

$$V_{\text{eff}}(H) \sim \lambda(H)H^4$$

$$\rightarrow \frac{dV_{\text{eff}}(H)}{dH} \sim \lambda(H)H^3 + \frac{d\lambda(H)}{dH}H^4$$

$$\simeq (\lambda + \beta)H^3$$



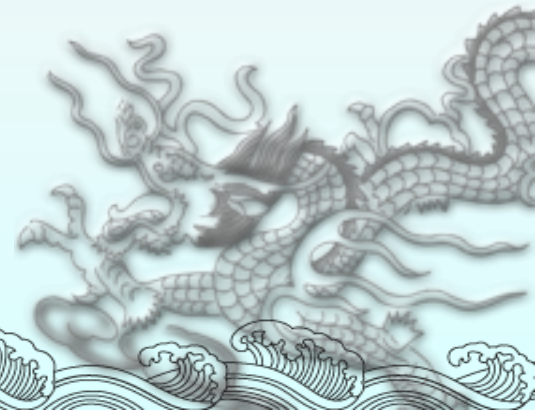
$$\frac{dV_{\text{eff}}(H)}{dH} \sim (\lambda + \beta)H^3 \sim 0$$

$$(1): \lambda > 0, \beta < 0$$

$$(2): \lambda = 0, \beta = 0$$

$$(3): \lambda < 0, \beta > 0$$

$$|\lambda| \gg |\beta|$$



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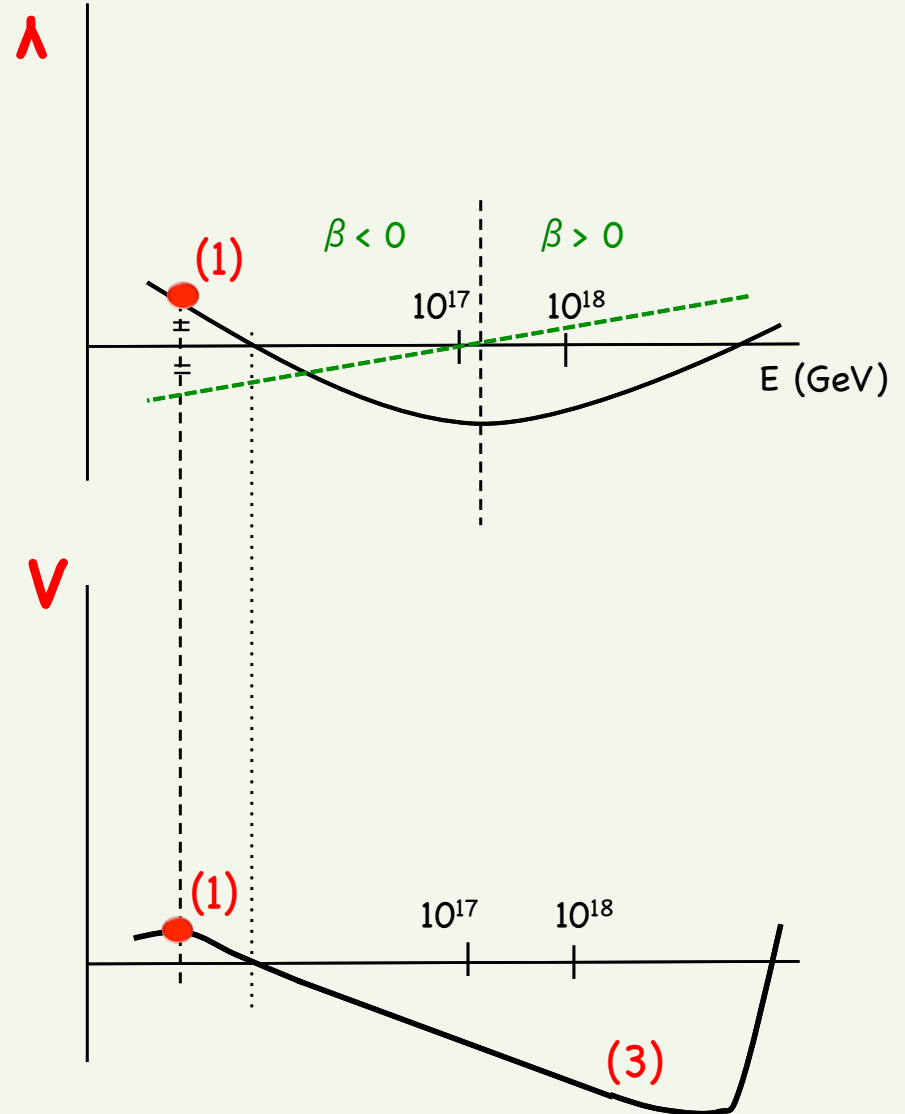
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$$m_{\text{top}} > 179 \text{ GeV}$$

in-stable tunneling amplitude is shorter than age of universe



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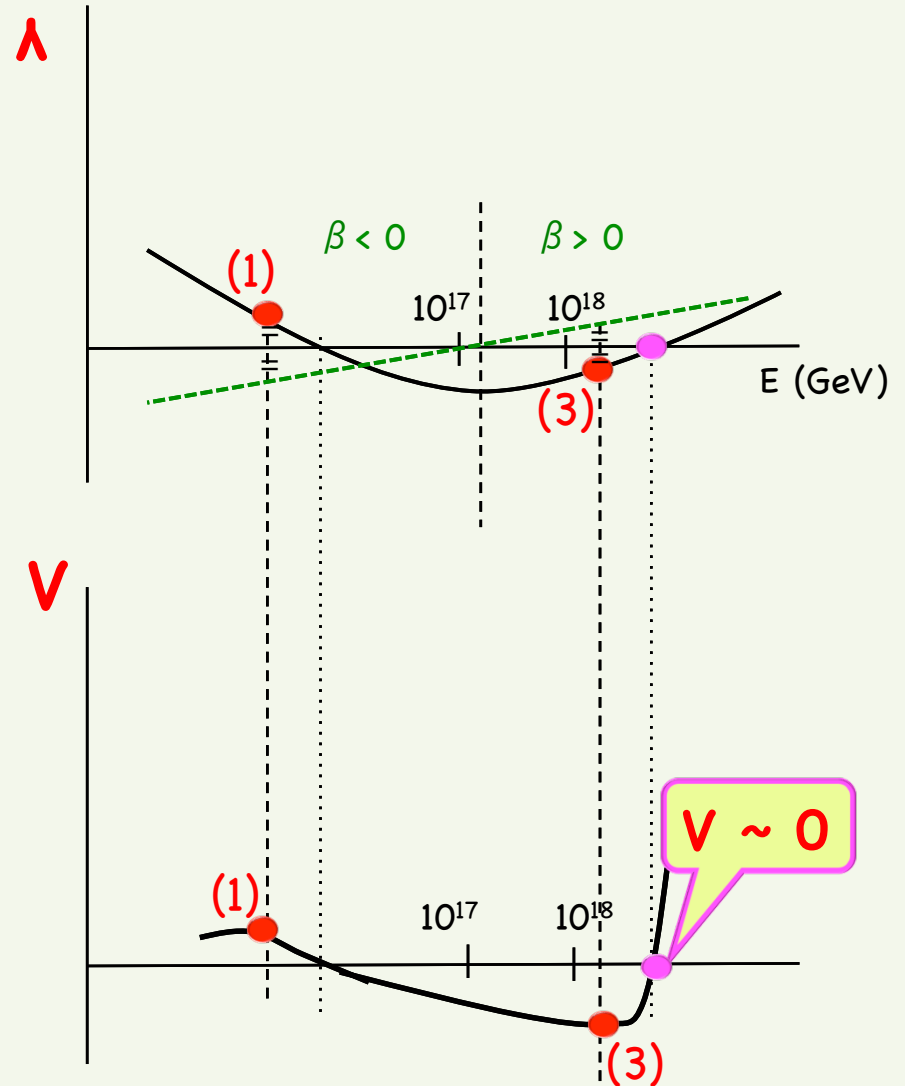
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$m_{\text{top}} = 172.58 \sim 174.10 \text{ GeV}$   
meta-stable



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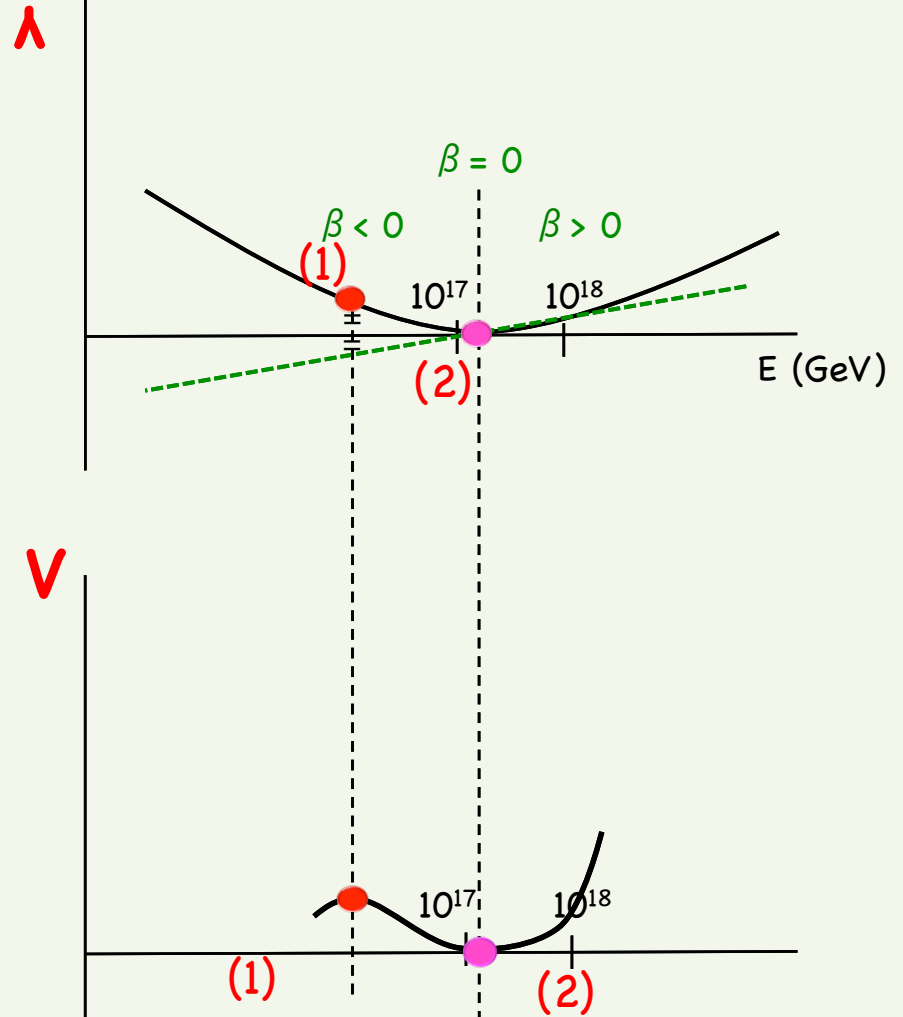
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$m_{\text{top}} = 171.081 \text{ GeV}$   
multiple-point critical principle (MPCP)



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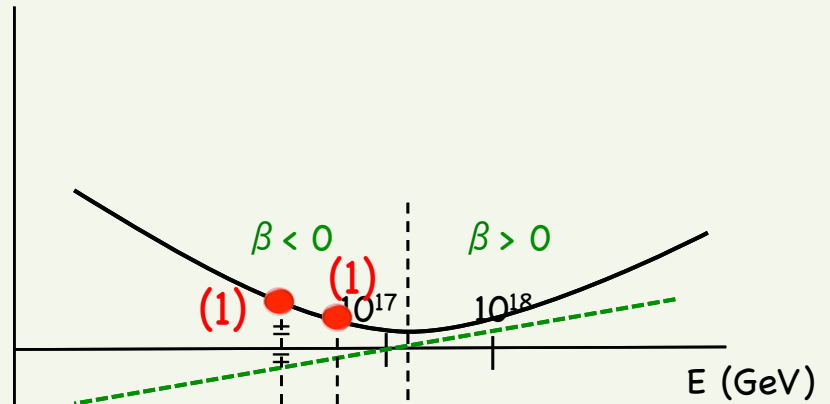
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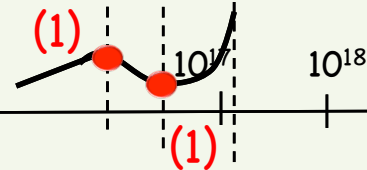
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$$m_{\text{top}} = 171.080 \text{ GeV}$$

$\lambda$



$V$



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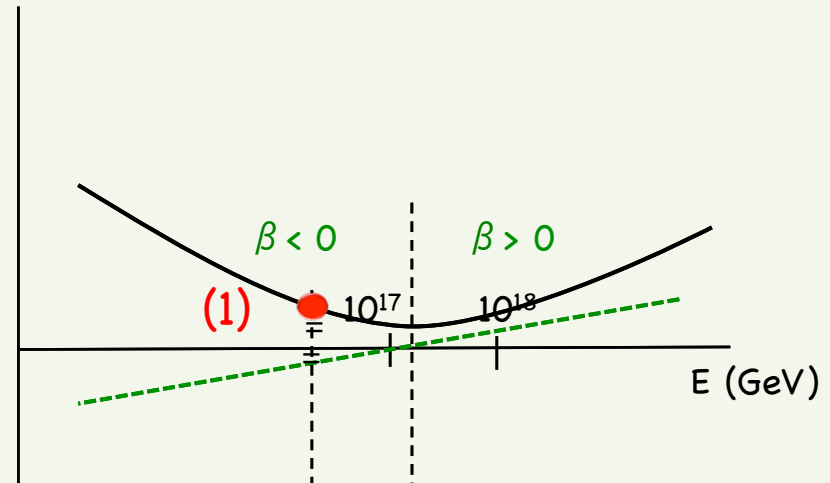
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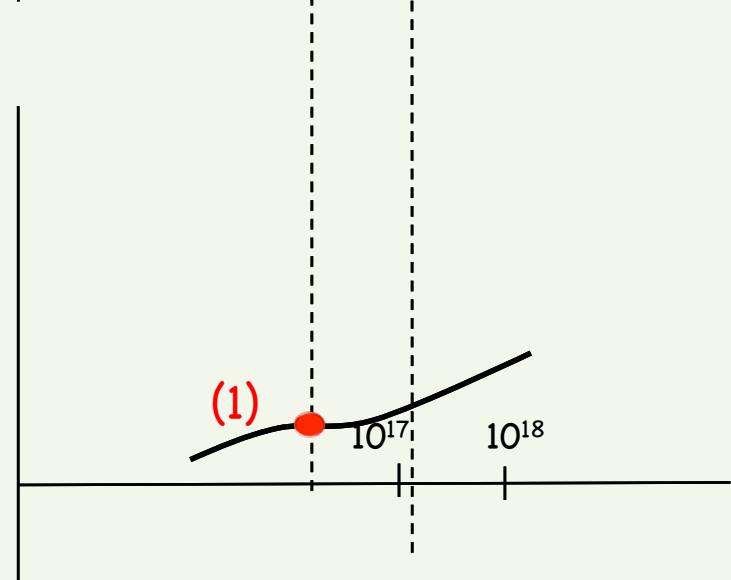
$$|\lambda| \gg |\beta|$$

$m_{\text{top}} = 171.079 \text{ GeV}$   
Higgs inflation?

$\lambda$



$V$



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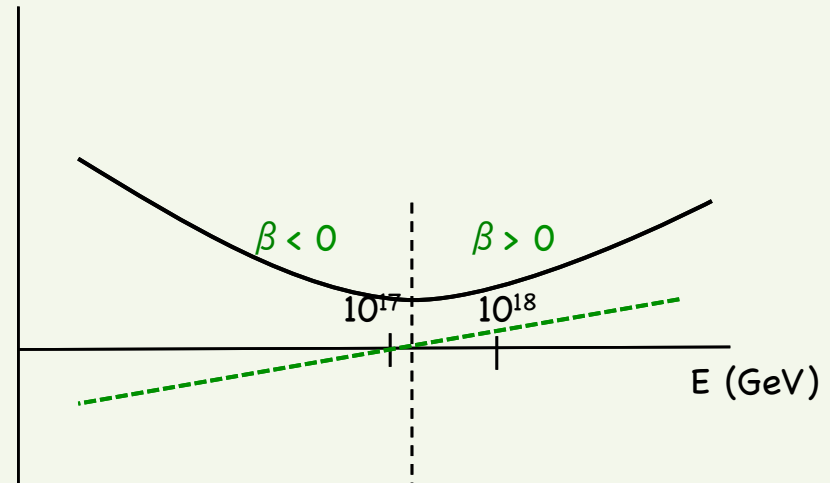
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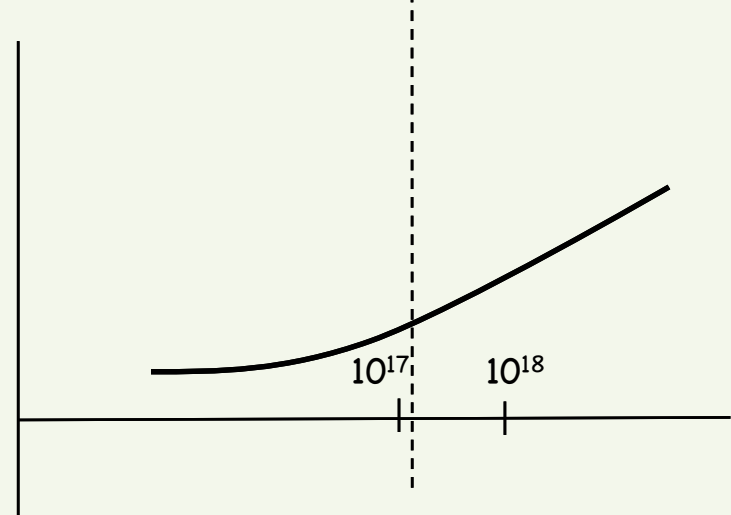
$$|\lambda| \gg |\beta|$$

$$M_{\text{top}} < 171.079 \text{ GeV}$$

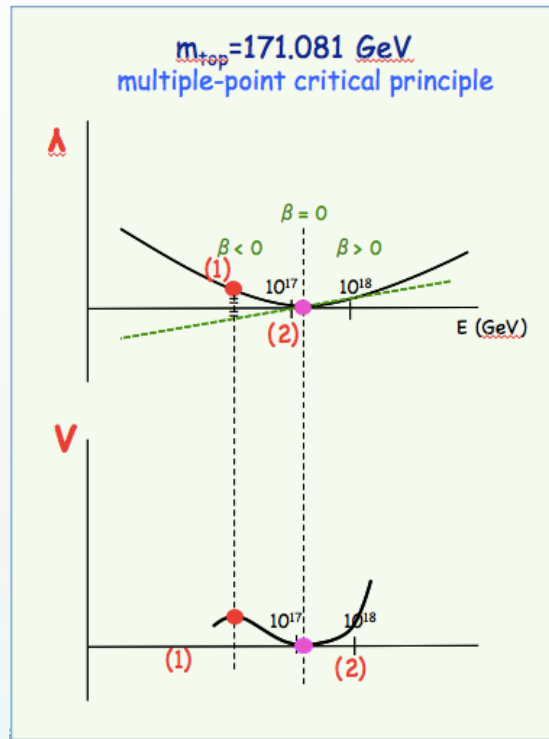
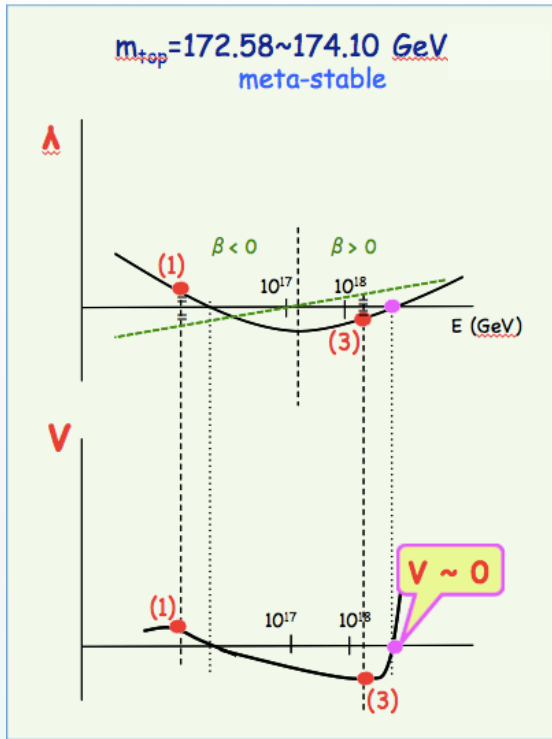
$\lambda$



$V$

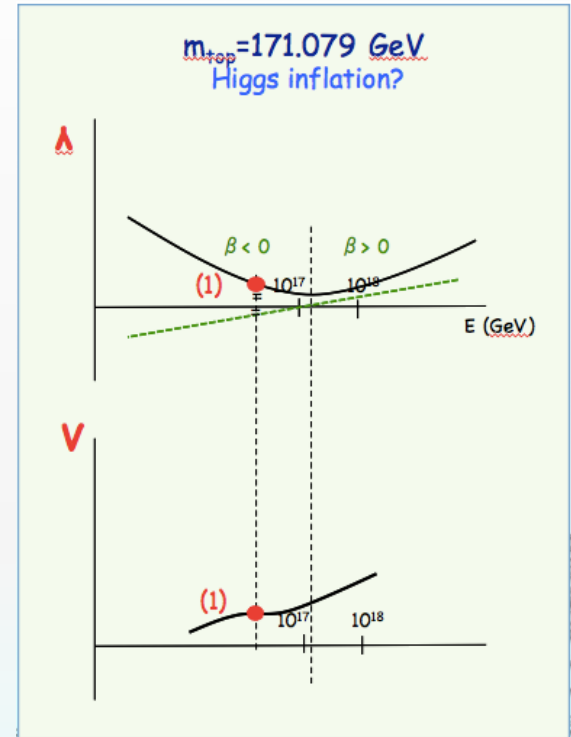


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$\lambda(M_{\text{Pl}}) = \beta(M_{\text{Pl}}) = 0$   
 $(V(M_{\text{Pl}}) = 0)$

seem special



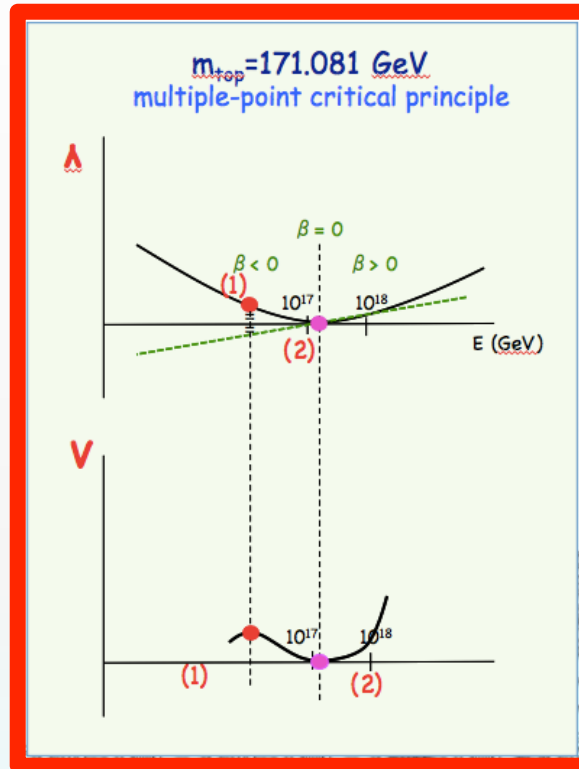
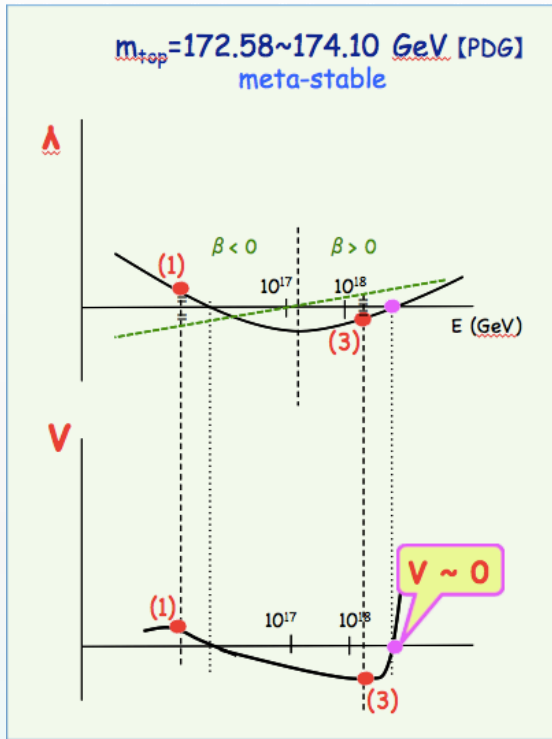
Higgs inflation

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↘ fermion eff.

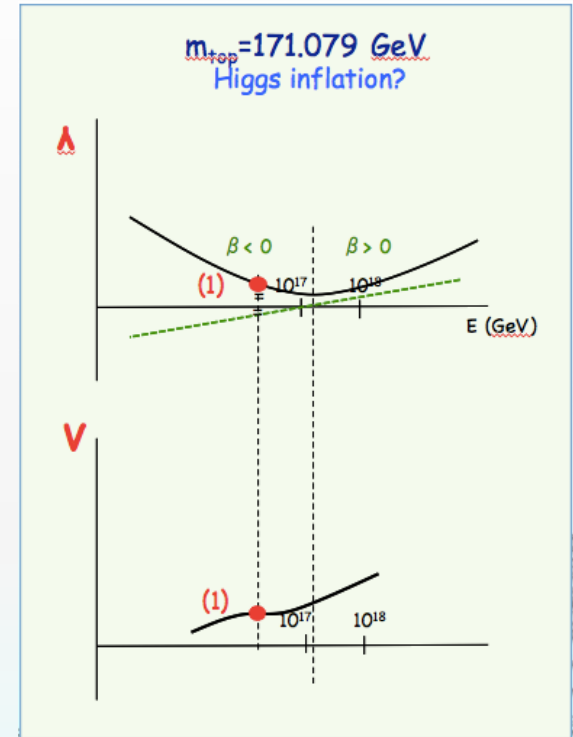


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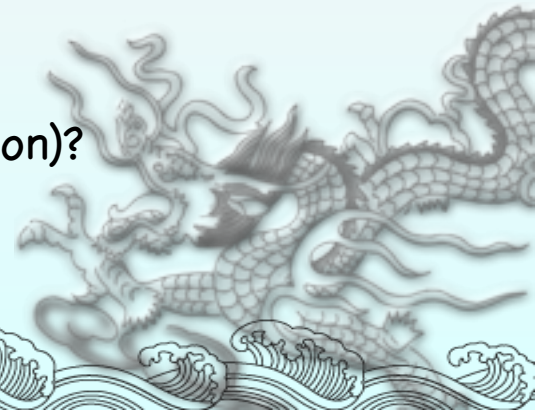
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seems roughly satisfies  $\lambda \sim \beta \sim 0 @ M_p$ , but not exact

could be directly connected to  $M_p$  if  $\lambda = \beta = 0 @ M_p$  ( $\leftarrow M_p$  physics)

in addition, the SM has problems as

- no DM candidate
- $\nu$  mass, BAU?
- inflation?
- cosmological constant?
- charge quantization (gauge coupling unification)?
- strong CP ?
- 



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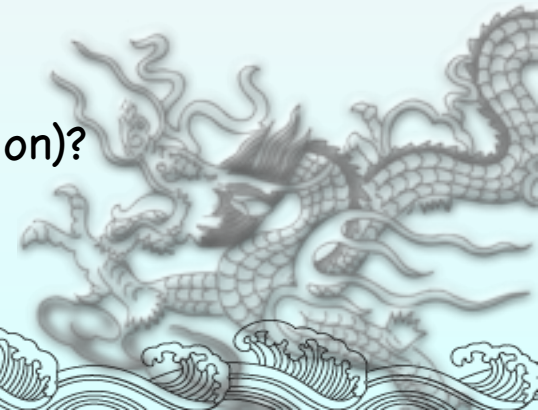
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- $\nu$  mass, BAU?  $\leftarrow$  seesaw & leptogenesis
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minimal extension of SM  
SM + scalar DM +  $\nu_R$

:



## §2 SM + scalar DM + $\nu_R$

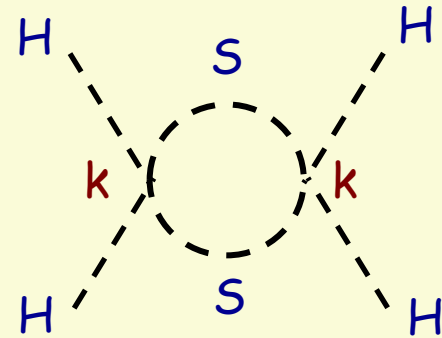
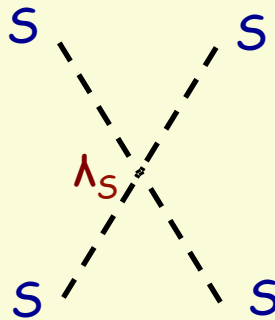
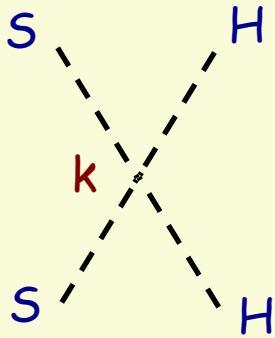
arXiv:1312.2089 [hep-ph] (to appear JHEP)  
NH, K. Kaneta, R. Takahashi,



# ☆ SM + scalar DM ☆

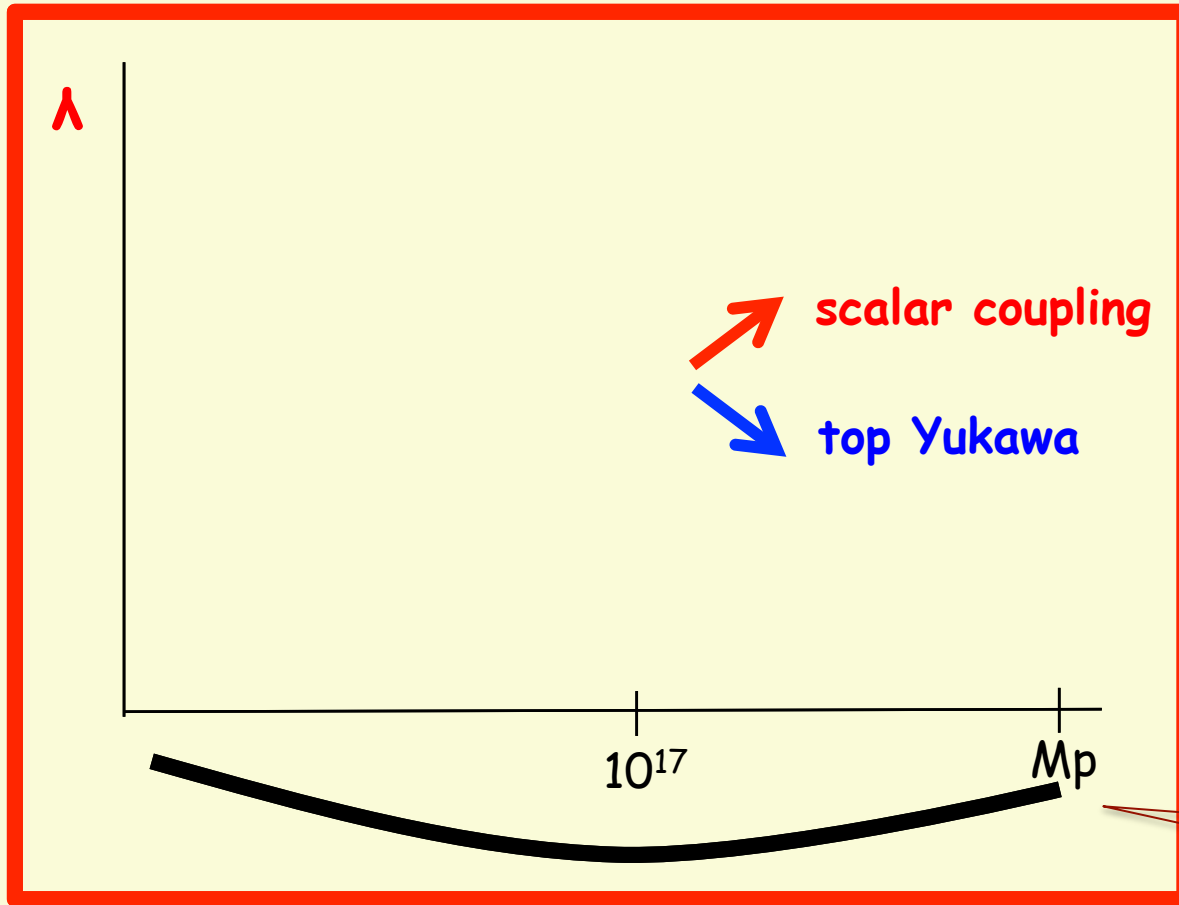
$$(L_{SM} +) L_{DM} = -\frac{m_{S0}^2}{2} \underline{S^2} - \frac{k}{2} |H|^2 \underline{S^2} - \frac{\lambda_S}{4} \underline{S^4}$$

↙ **real scalar S is DM** [ $Z_2$ -odd (stable)]



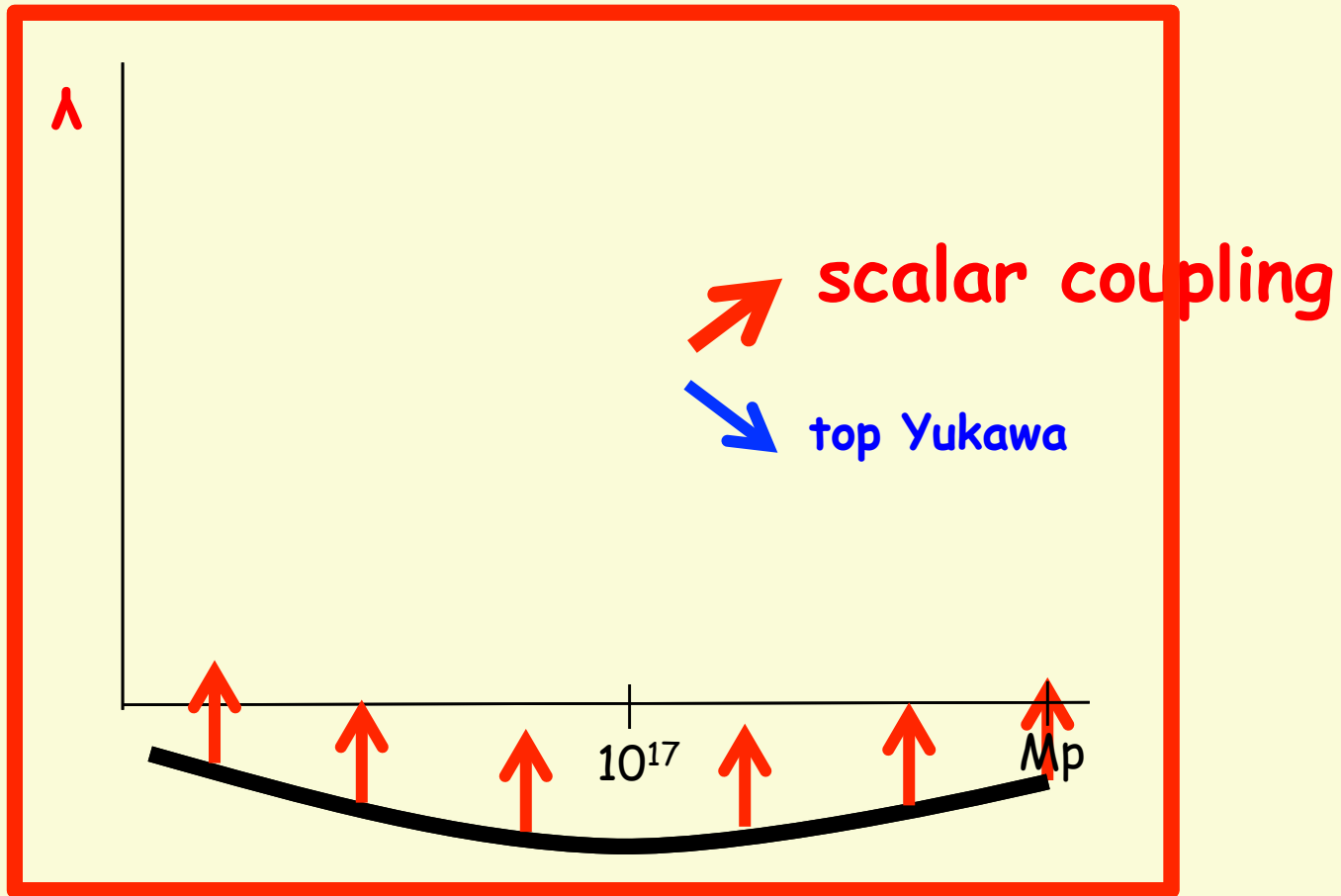
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☆ SM ☆



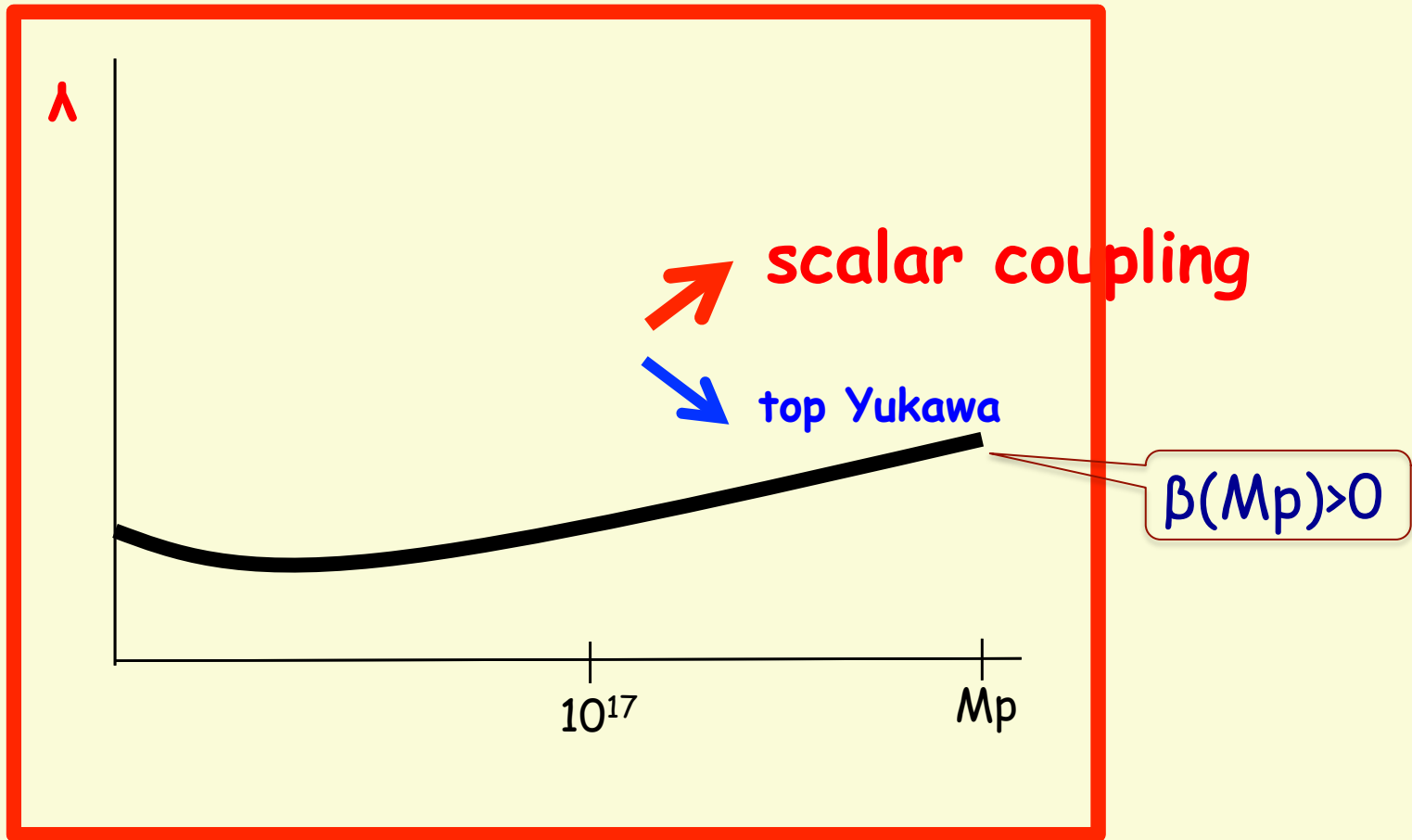
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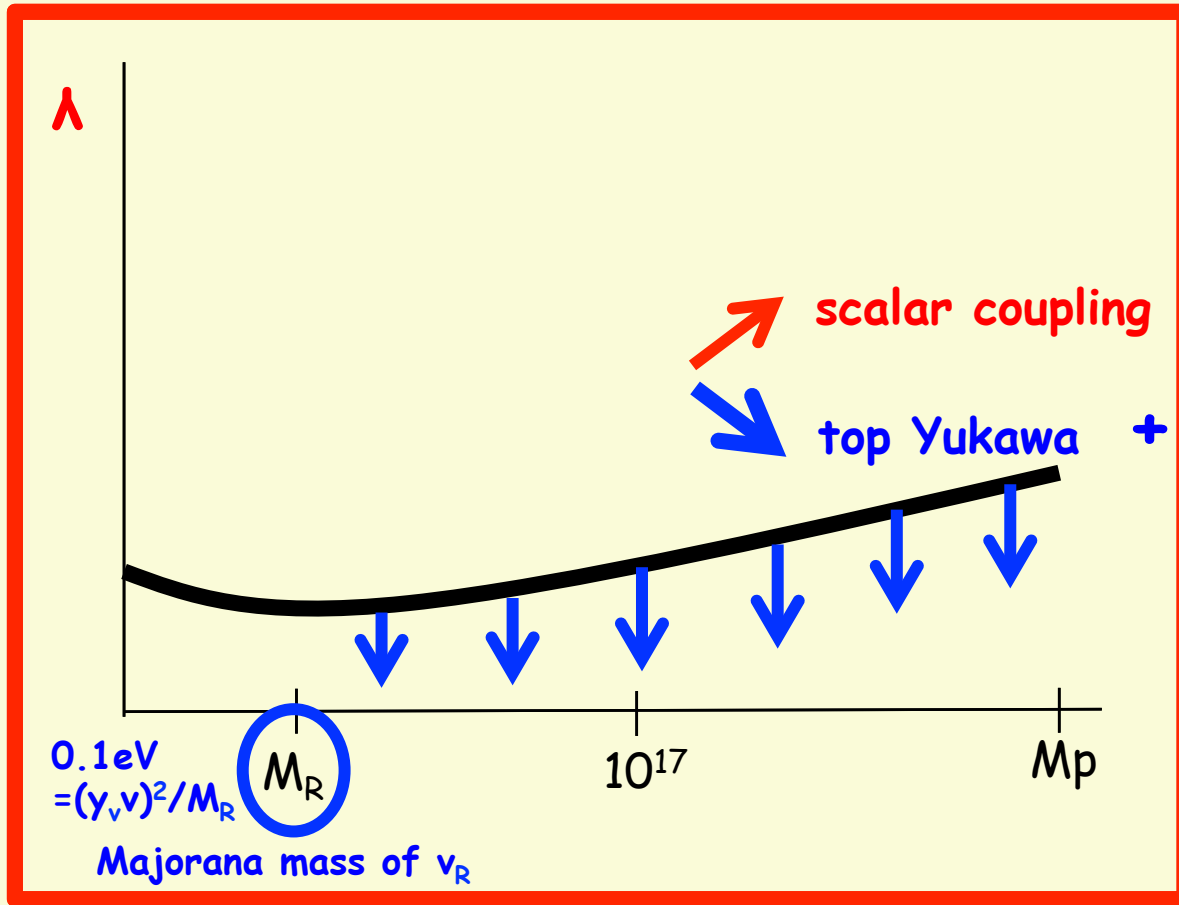
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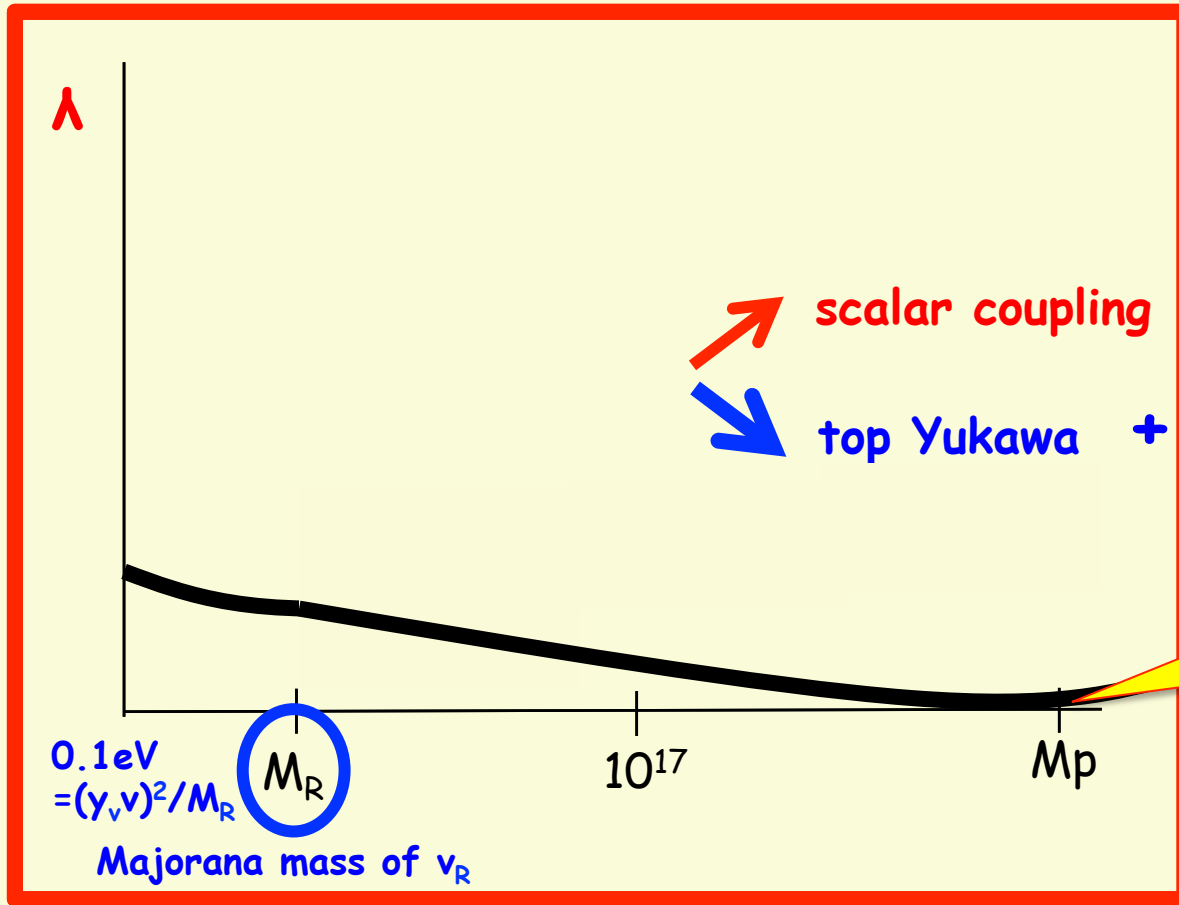


☆ SM + scalar DM +  $\nu_R$  ☆



$$(4\pi)^2 \frac{d\lambda}{dt} = \underline{24\lambda^2} + 12\lambda y_t^2 - \underline{6y_t^4} - 3\lambda(g'^2 + 3g^2) + \frac{3}{8}[2g^4 + (g'^2 + g^2)^2] + \frac{1}{2}k^2 - \underline{\underline{2y_\nu^4 + 4\lambda y_\nu^2}}$$

☆ SM + scalar DM +  $\nu_R$  ☆



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# §3 numerical analyses



# ☆ SM + scalar DM ☆

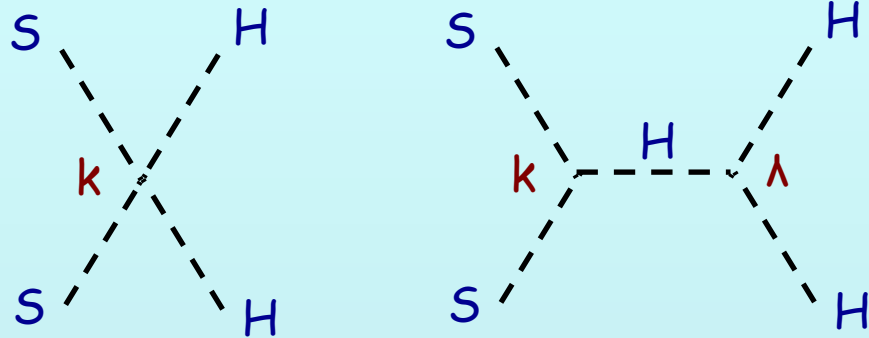
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## Input:

$\lambda(M_Z) = 0.131$  ( $m_h = 126 \text{ GeV}$ ), top pole mass = 172.58 ~ 174.10 GeV

DM relic density,  $\Omega_S h^2 = 0.119$  (depends on  $\lambda$  &  $k$  (not  $\lambda_S$ ))

→ pair annihilation process

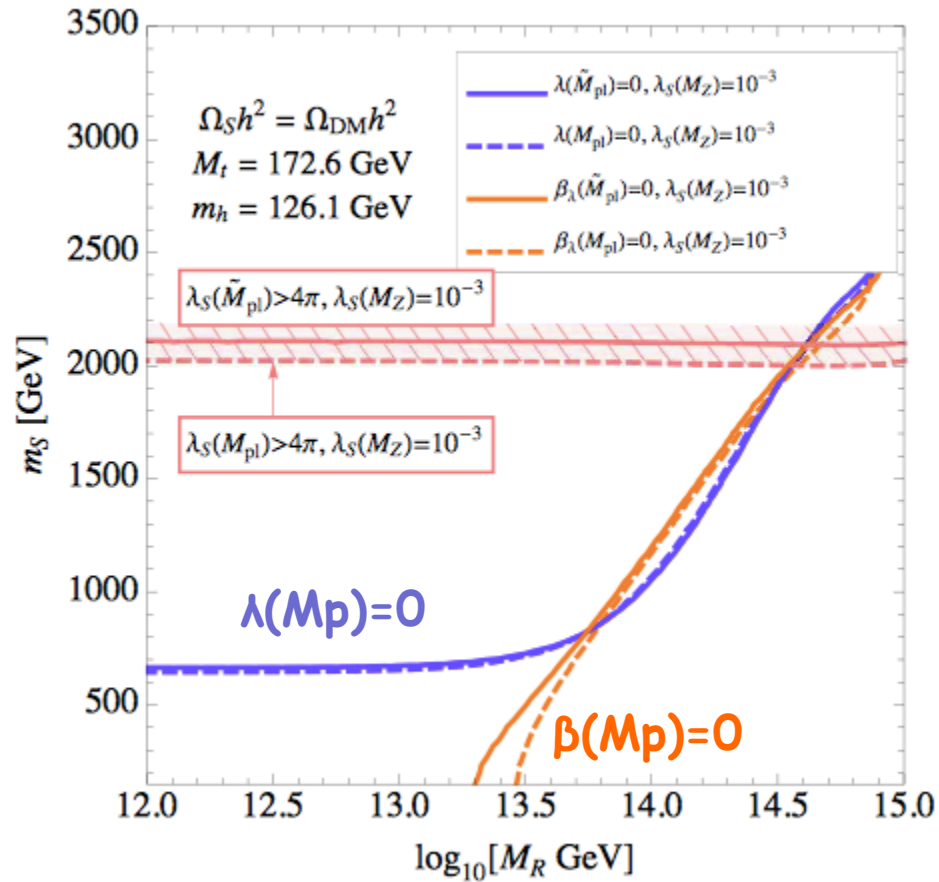


• cross section  $\propto k$  &  $1/m_S^2$

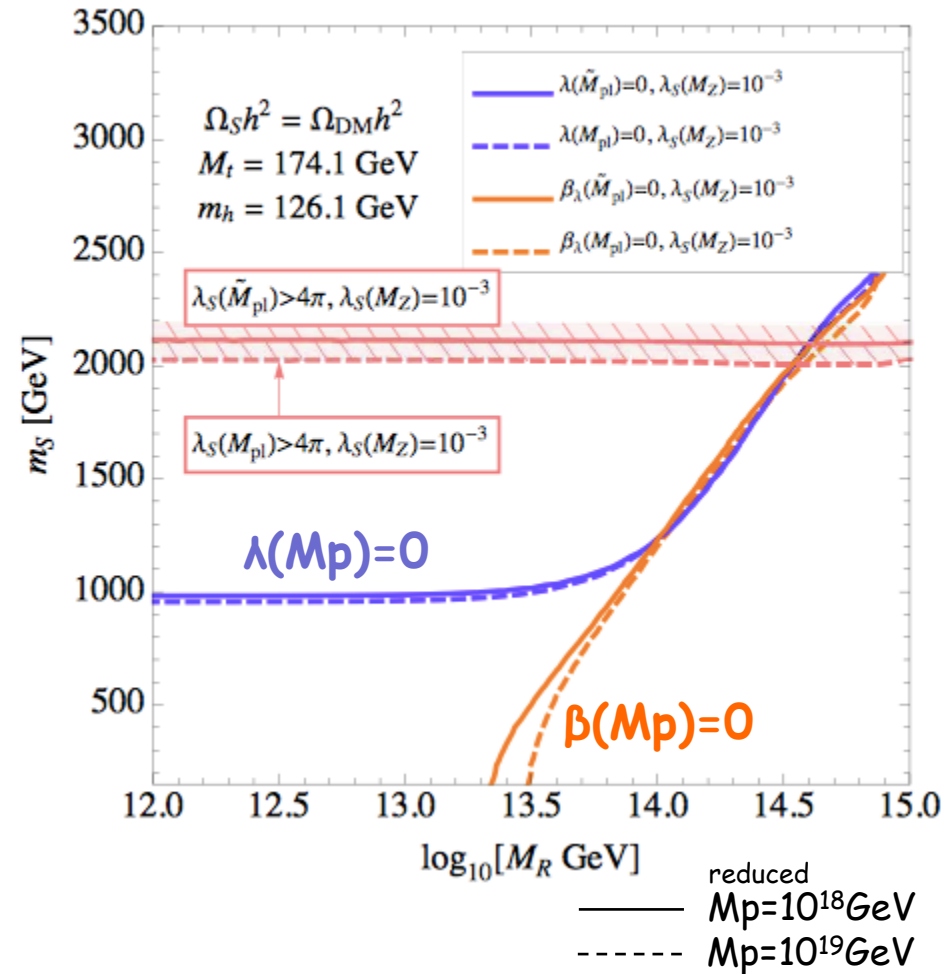
•  $k \rightarrow$  large and/or  $m_S \rightarrow$  small,  $\Omega_S h^2 \rightarrow$  small **【strong pair annihilation】**  
 (small) (large) (large) (weak)

→ to keep  $\Omega_S h^2 = 0.119$ ,  $k \propto m_S$  [ $k \rightarrow$  large (small) with  $m_S \rightarrow$  large (small)]

$M_t=172.6\text{GeV}$

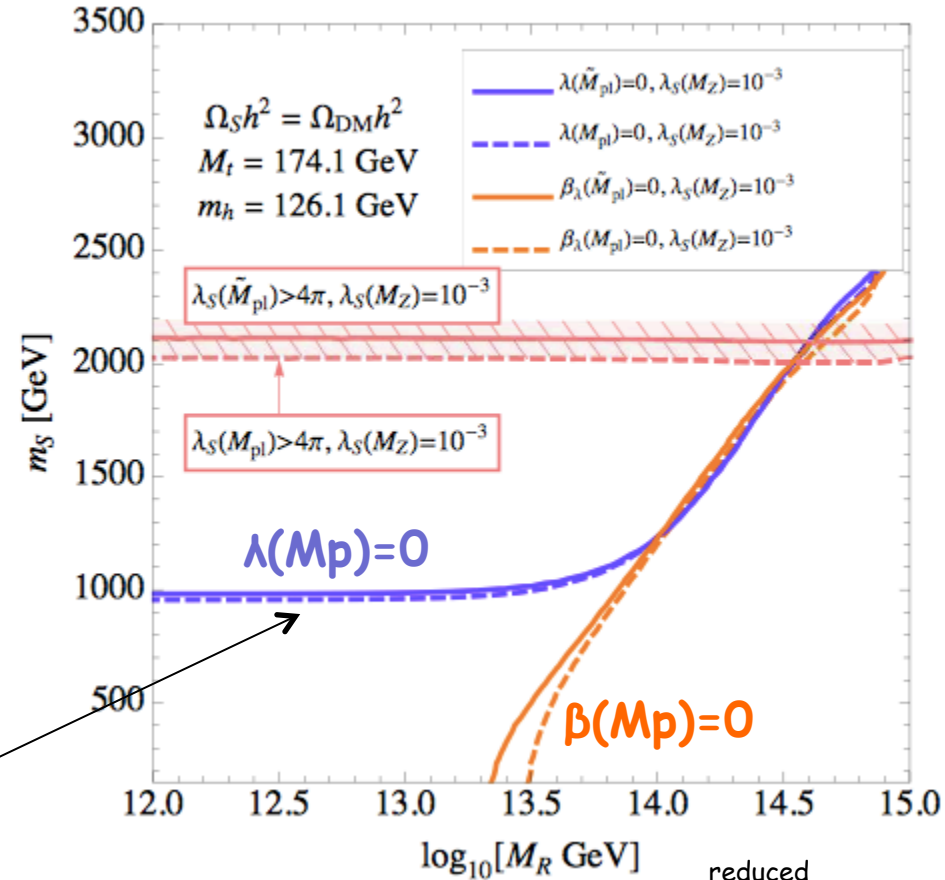
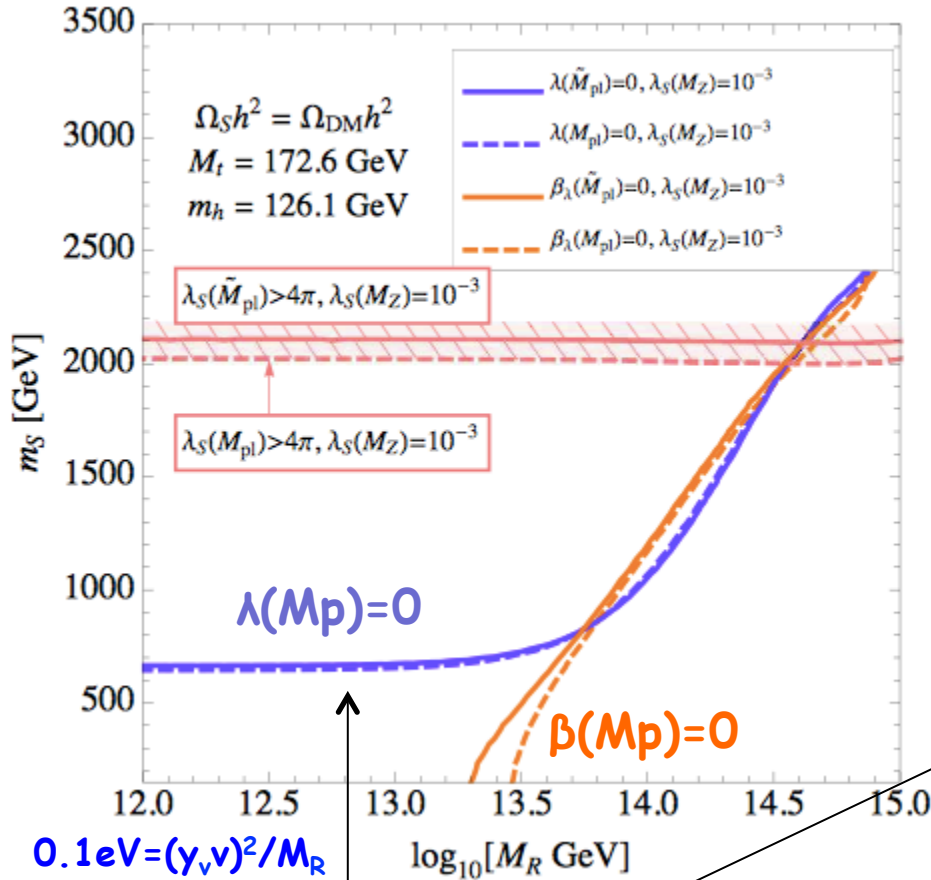


$M_t=174.1\text{GeV}$



$M_t=172.6\text{GeV}$

$M_t=174.1\text{GeV}$



small  $M_R \leftrightarrow$  small  $y_\nu$   
 same as SM+S model,  
 $[\lambda=0$  is realized by  
 $y_t$  &  $k$  cancellation  
 with definite values.  
 $(k \propto m_S)$

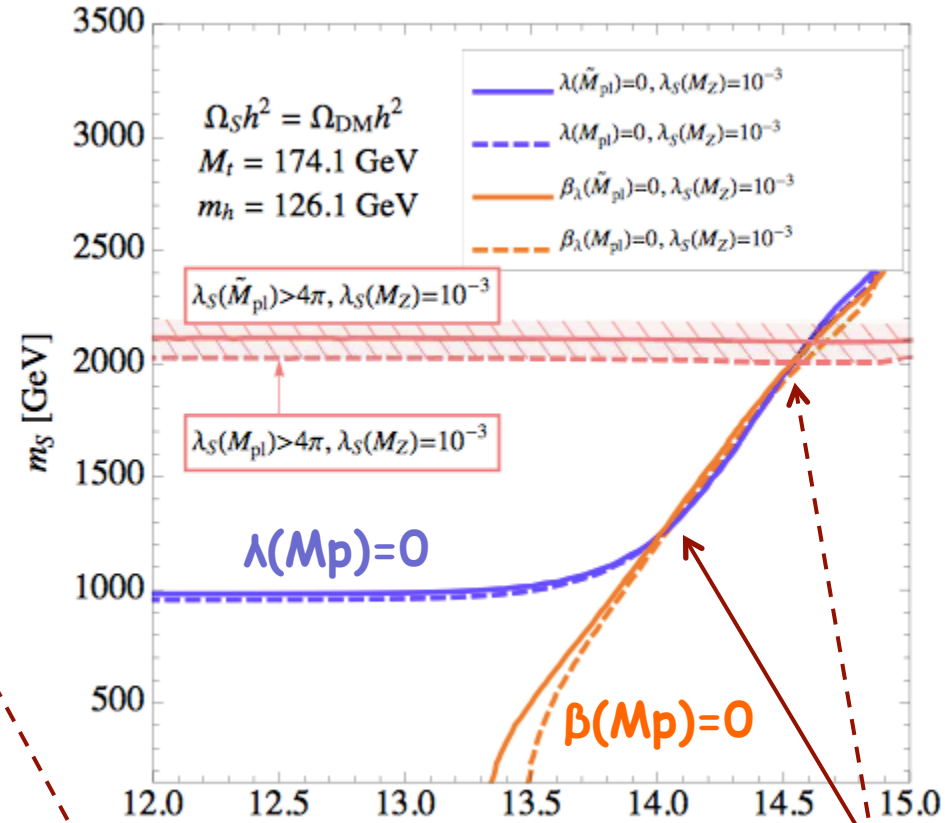
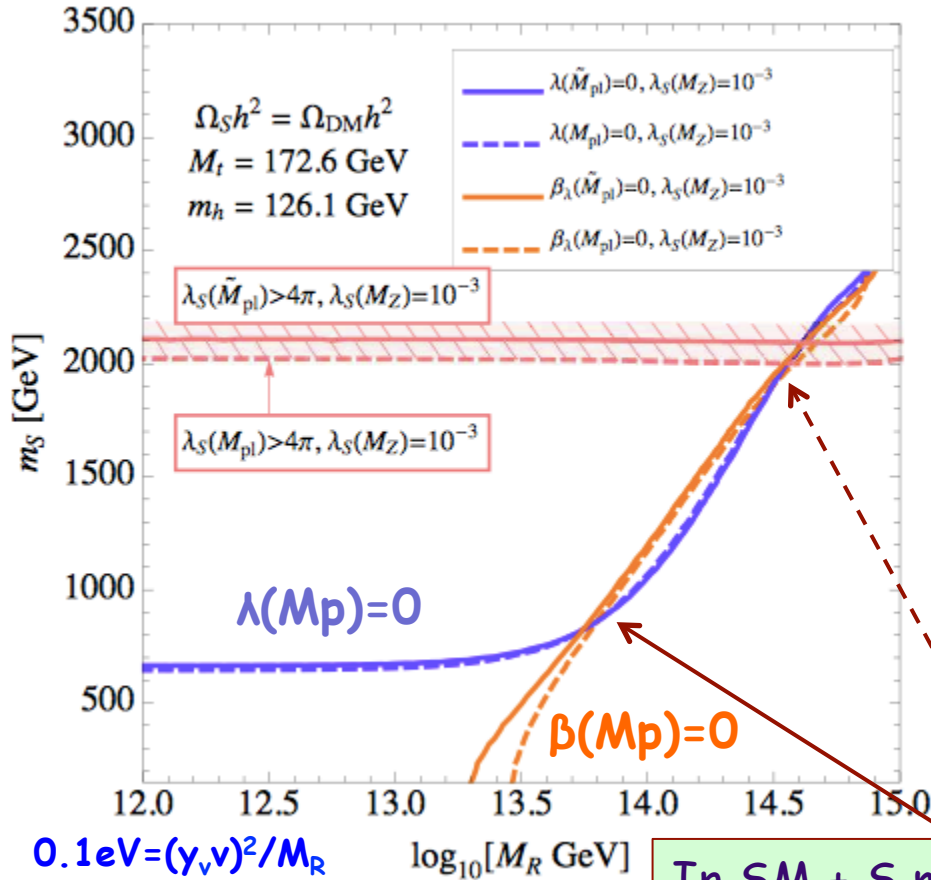
$$(4\pi)^2 \frac{d\lambda}{dt} = 24\lambda^2 + 12\lambda y_t^2 - \underline{6y_t^4} - 3\lambda(g'^2 + 3g^2) + \frac{3}{8}[2g^4 + (g'^2 + g^2)^2] + \underline{\frac{1}{2}k^2}$$

large  $y_t \rightarrow$  large  $k$  (in order to get  $\lambda=0$ )  
 $\rightarrow$  large  $m_S$  ( $m_S^2 = m_{S0}^2 + kv^2/2$ ,  $\Omega_S h^2(k) = 0.119$ )

reduced  
 —  $M_p=10^{18}\text{GeV}$   
 - -  $M_p=10^{19}\text{GeV}$

$M_t=172.6\text{GeV}$

$M_t=174.1\text{GeV}$

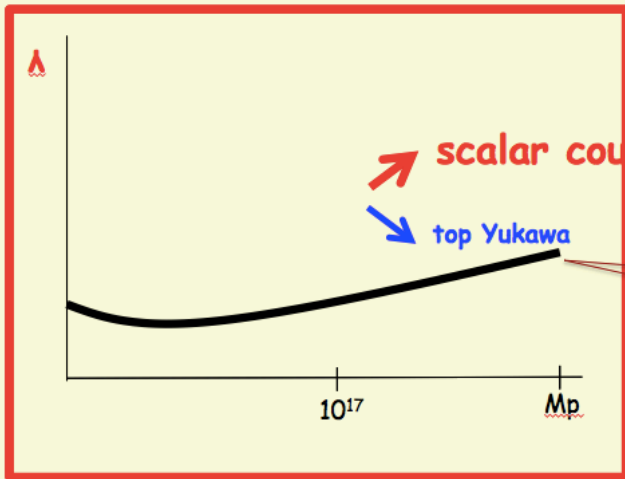


In SM + S model,  $\beta(M_p) > 0$ .  
 In SM + S +  $\nu_R$  model, large  $y_\nu$  can make  $\beta(M_p)=0$ , but  $k$  must be also large to keep  $\beta(M_p)=0$ . ( $k \propto m_S$ )

$$(4\pi)^2 \frac{d\lambda}{dt} = 24\lambda^2 + 12\lambda y_t^2 - 6y_t^4 - 3\lambda(g'^2 + 3g^2) + \frac{3}{8}[2g^4 + (g'^2 + g^2)^2] + \frac{1}{2}k^2 - 2y_\nu^4 + 4\lambda y_\nu^2$$

$M_t=174.1\text{GeV}$

☆SM + scalar DM☆



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$\Omega_S h^2 = \Omega_{DM} h^2$   
 $M_t = 174.1 \text{ GeV}$   
 $m_h = 126.1 \text{ GeV}$

- $\lambda(\tilde{M}_{pl})=0, \lambda_S(M_Z)=10^{-3}$
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$\lambda_S(\tilde{M}_{pl}) > 4\pi, \lambda_S(M_Z) = 10^{-3}$

$\lambda_S(M_{pl}) > 4\pi, \lambda_S(M_Z) = 10^{-3}$

$\lambda(M_p) = 0$

$\beta(M_p) = 0$

$0.1\text{eV} = (y_\nu v)^2 / M_R$

$\log_{10}[M_R \text{ GeV}]$

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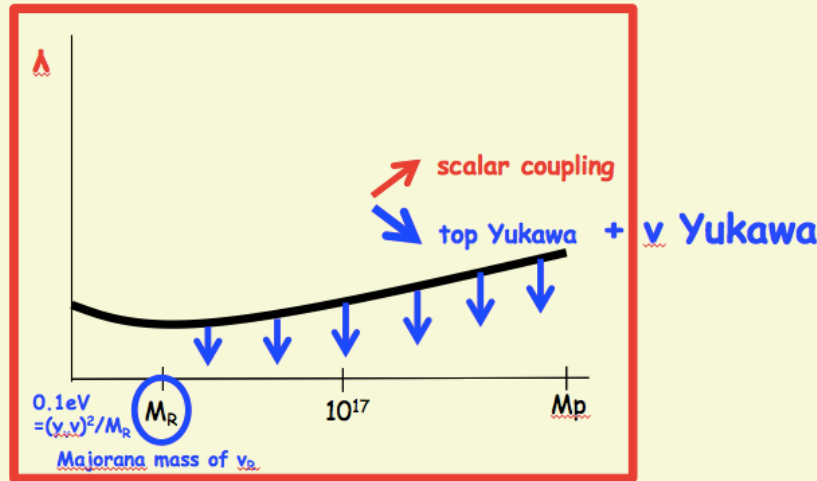
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$$\underline{-2y_\nu^4} + 4\lambda y_\nu^2$$



$M_t=174.1\text{GeV}$

☆ SM + scalar DM +  $\nu_R$  ☆



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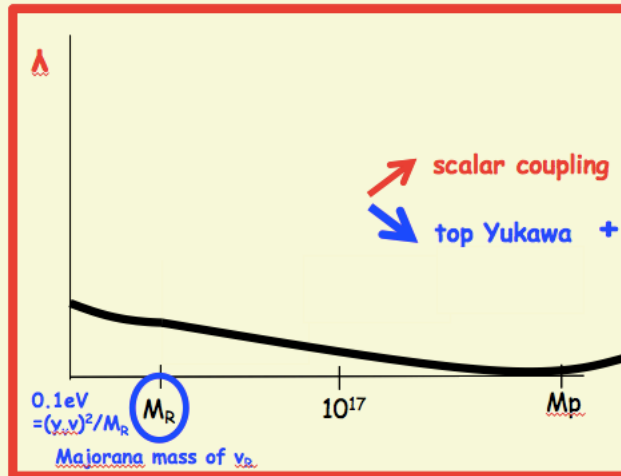
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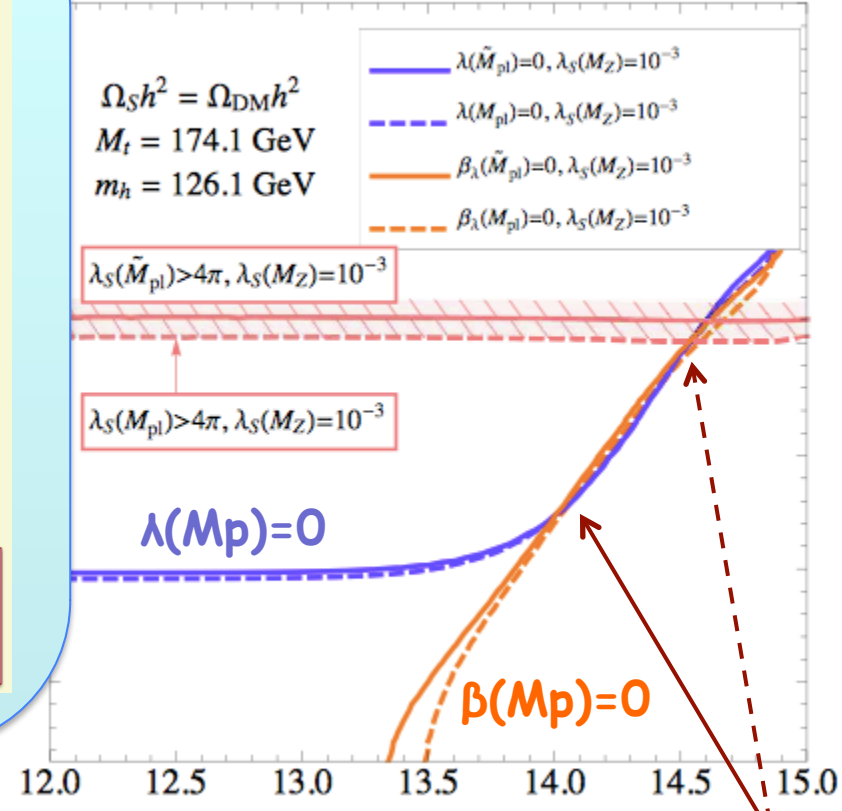
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$M_t=174.1\text{GeV}$

☆ SM + scalar DM +  $\nu_R$  ☆



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$0.1\text{eV}=(y_\nu v)^2/M_R$

$\log_{10}[M_R \text{ GeV}]$

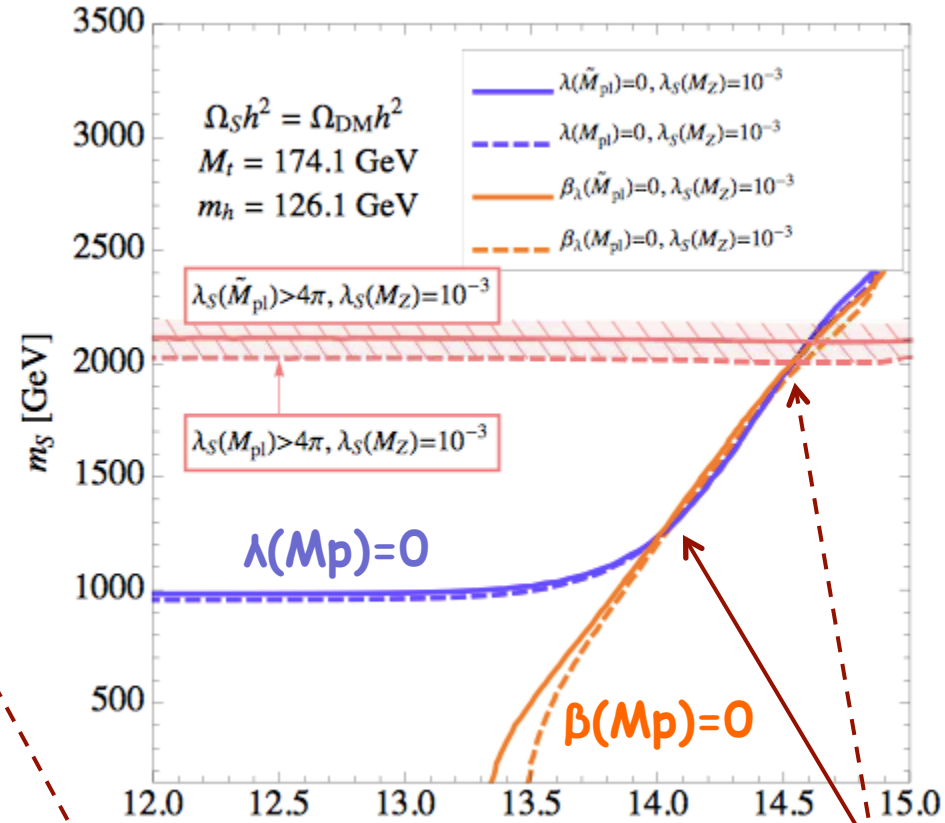
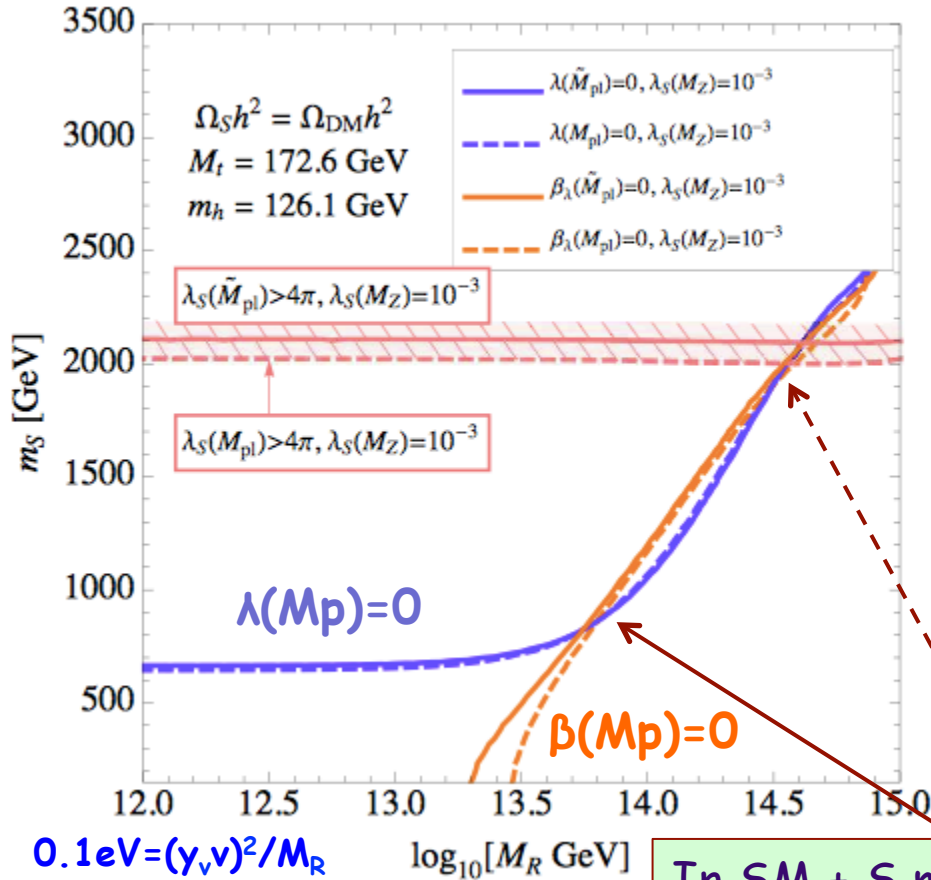
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$M_t=172.6\text{GeV}$

$M_t=174.1\text{GeV}$

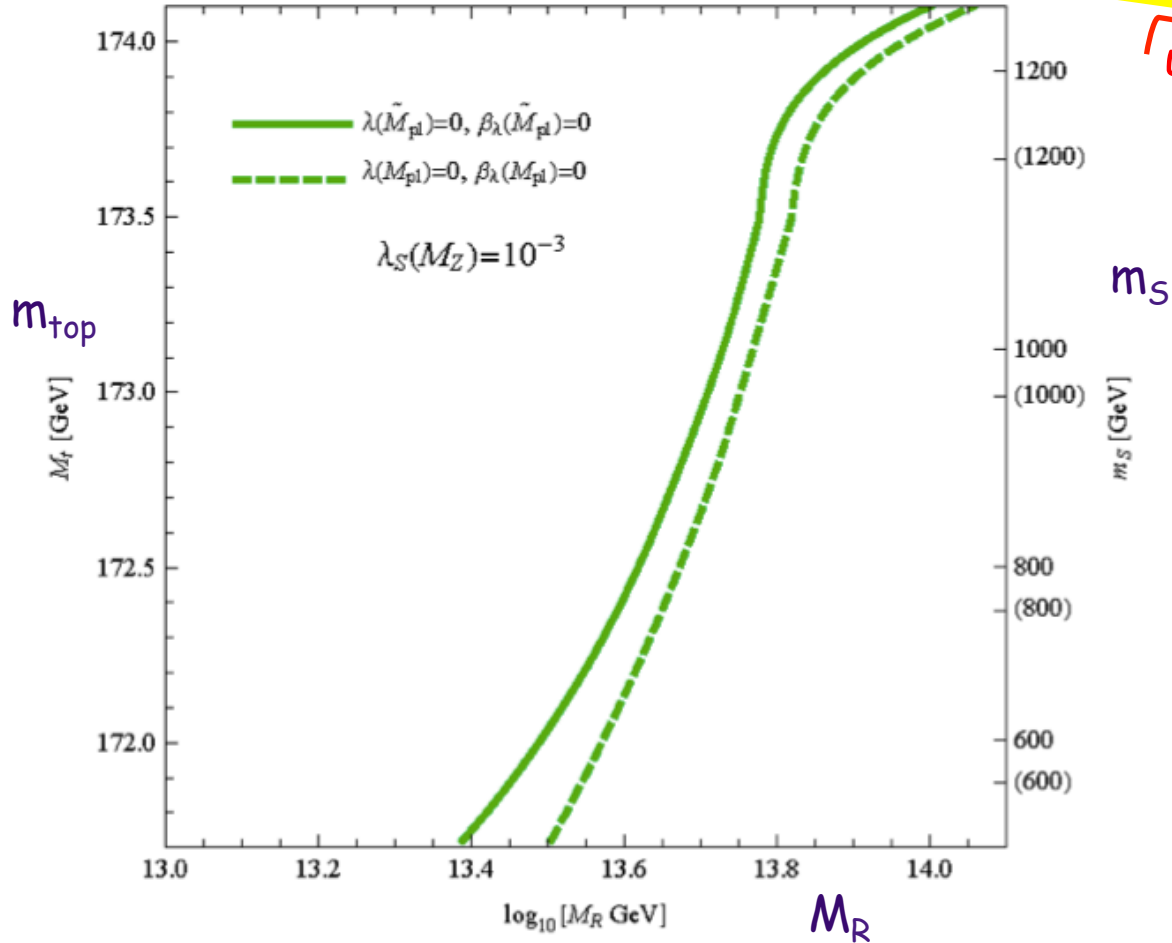


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$m_S (M_+)$  &  $M_R$  which satisfy  $\lambda=\beta=0$

$m_S$  &  $M_R$  are determined!  
uniquely



parameters:

$\lambda,$



fixed by Higgs mass

$k,$



eliminate by  $\Omega_S h^2(k) = 0.119$

$\lambda_S,$

fix

$\gamma_+,$

fix

$\gamma_ν,$



eliminate by  $0.1 \text{eV} = (\gamma_ν v)^2 / M_R$

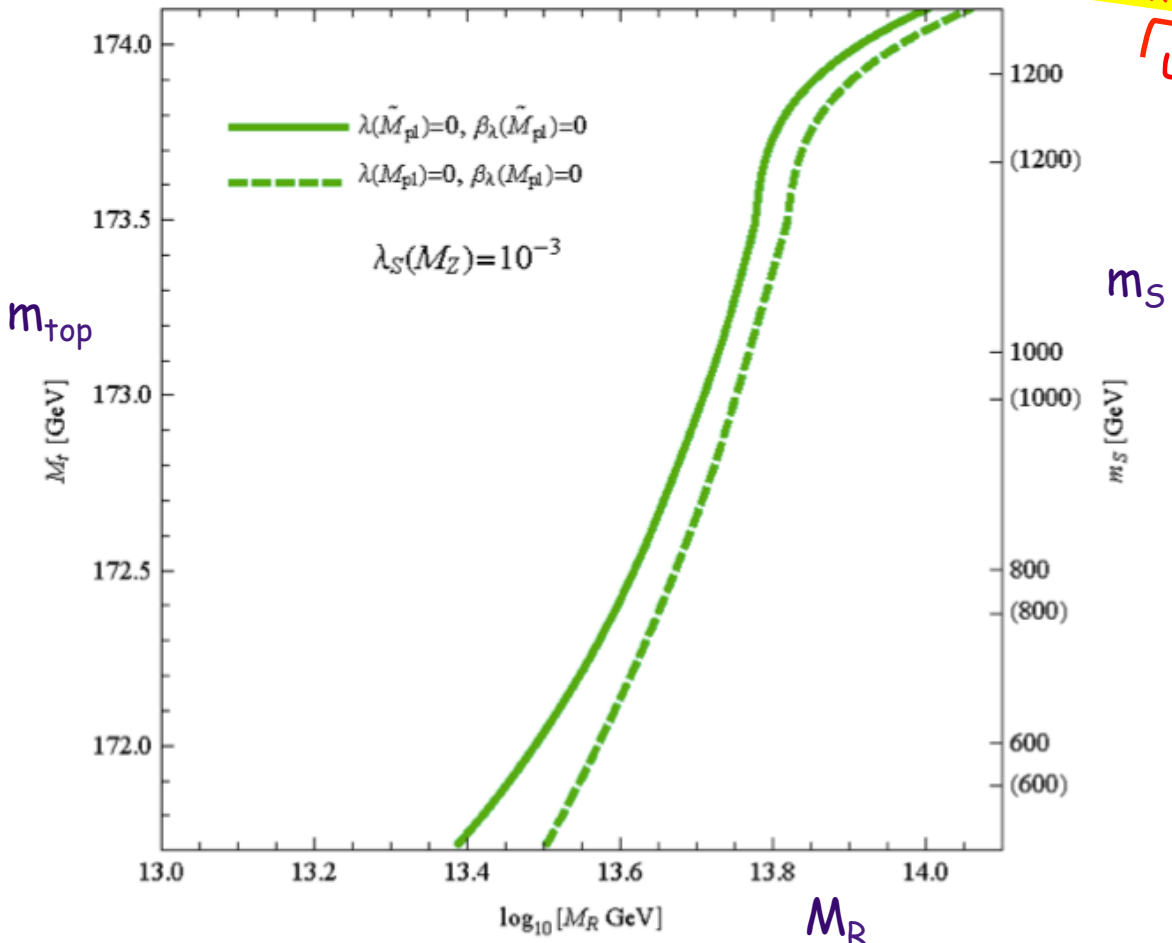
$m_S,$

$M_R$

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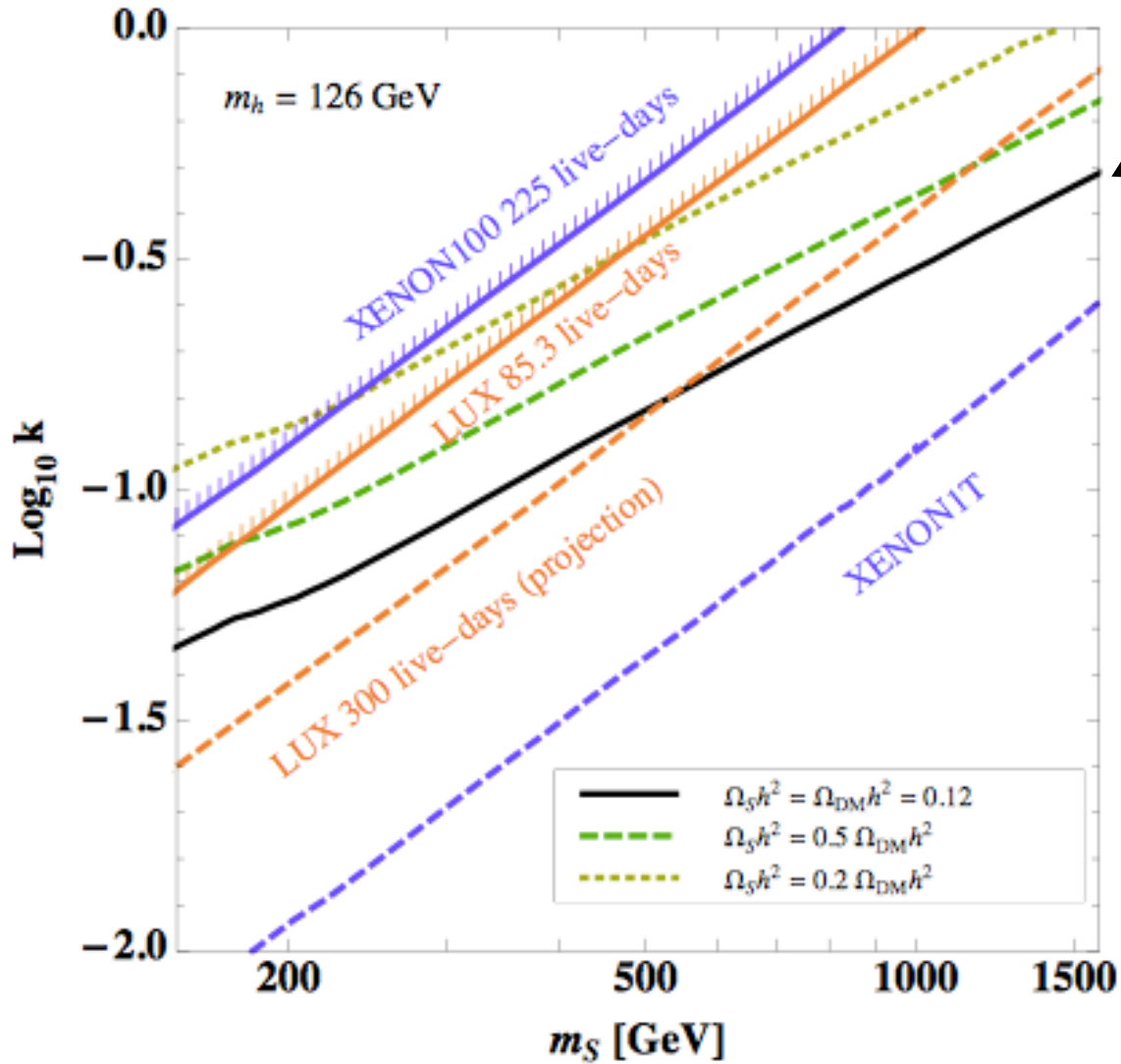


As  $M_+ = 172.58 \sim 174.10$  GeV,  $\lambda(M_p)=\beta(M_p)=0$  satisfying point runs

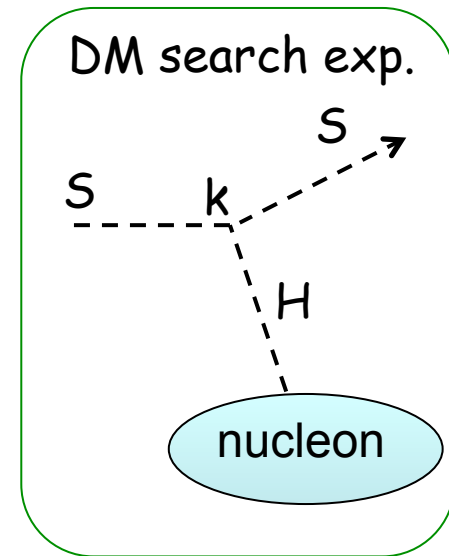
$M_p=10^{18}$  GeV:  $m_S = 800$  GeV  $\sim 1.2$  TeV,  $M_R = 6.3 \times 10^{13} \sim 1.6 \times 10^{14}$  GeV

$M_p=10^{19}$  GeV:  $m_S = 850$  GeV  $\sim 1.4$  TeV,  $M_R = 5.5 \times 10^{13} \sim 1.2 \times 10^{14}$  GeV

# current experimental bounds on $k$ & $m_S$

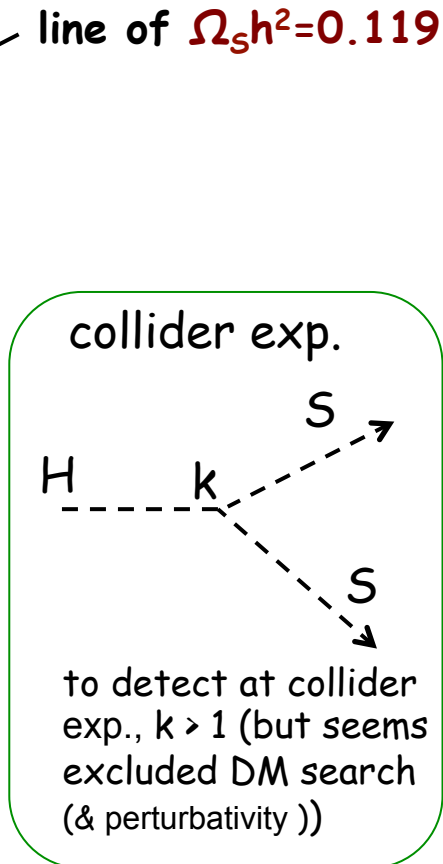
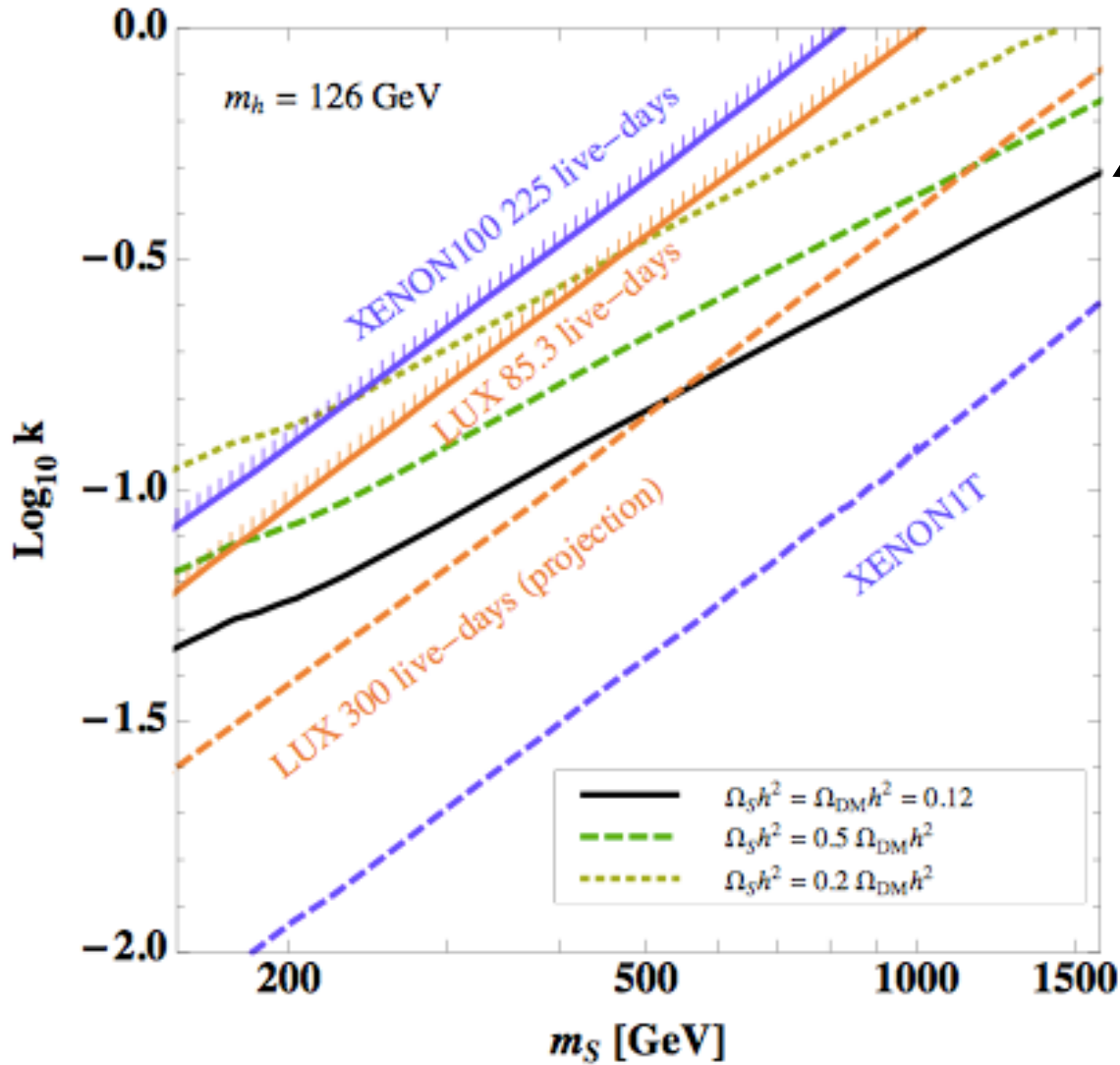


line of  $\Omega_S h^2 = 0.119$



to keep constant  $\Omega_S h^2 = 0.119$ ,  $k \propto m_S$  [ $k \rightarrow$  large (small) with  $m_S \rightarrow$  large (small)]

# current experimental bounds on $k$ & $m_S$



to keep constant  $\Omega_S h^2 = 0.119$ ,  $k \propto m_S$  [ $k \rightarrow$  large (small) with  $m_S \rightarrow$  large (small)]

# §4 Higgs inflation

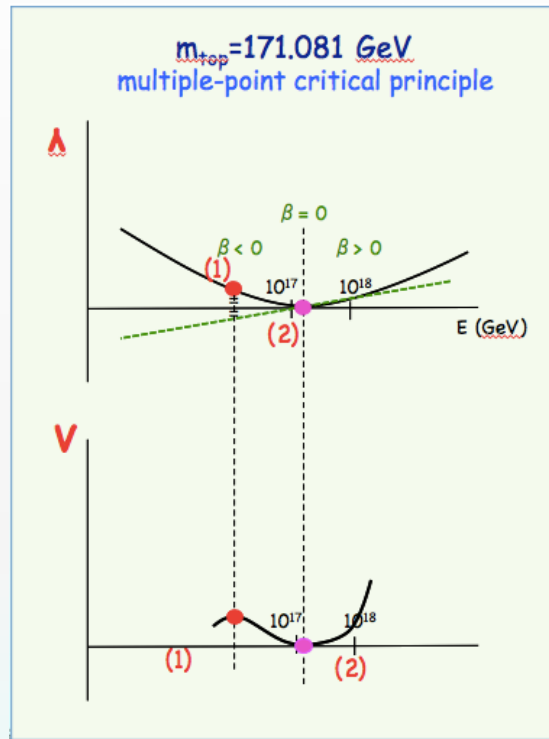
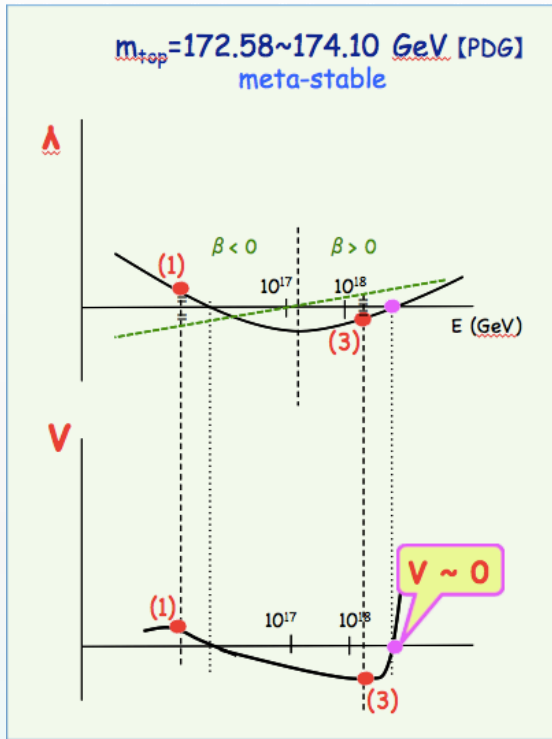
arXiv:1404.4737 [hep-ph], NH, R. Takahashi

arXiv:1405.5738 [hep-ph], NH, H. Ishida and R. Takahashi,

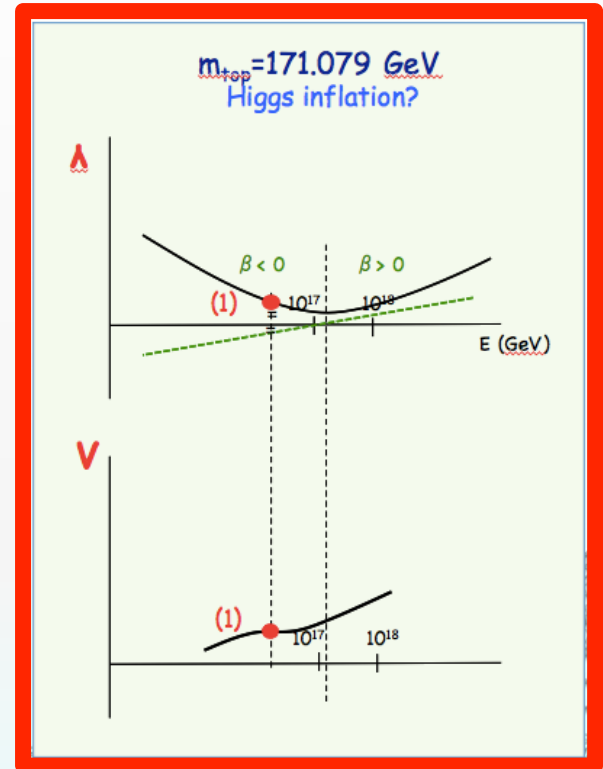




$m_H = 125.9 \pm 0.4 \text{ GeV}$ ,  $m_{\text{top}} = 171.83 \sim 174.31 \text{ GeV}$  in the SM



$\lambda(M_{\text{Pl}}) = \beta(M_{\text{Pl}}) = 0$   
( $V(M_{\text{Pl}}) = 0$ )



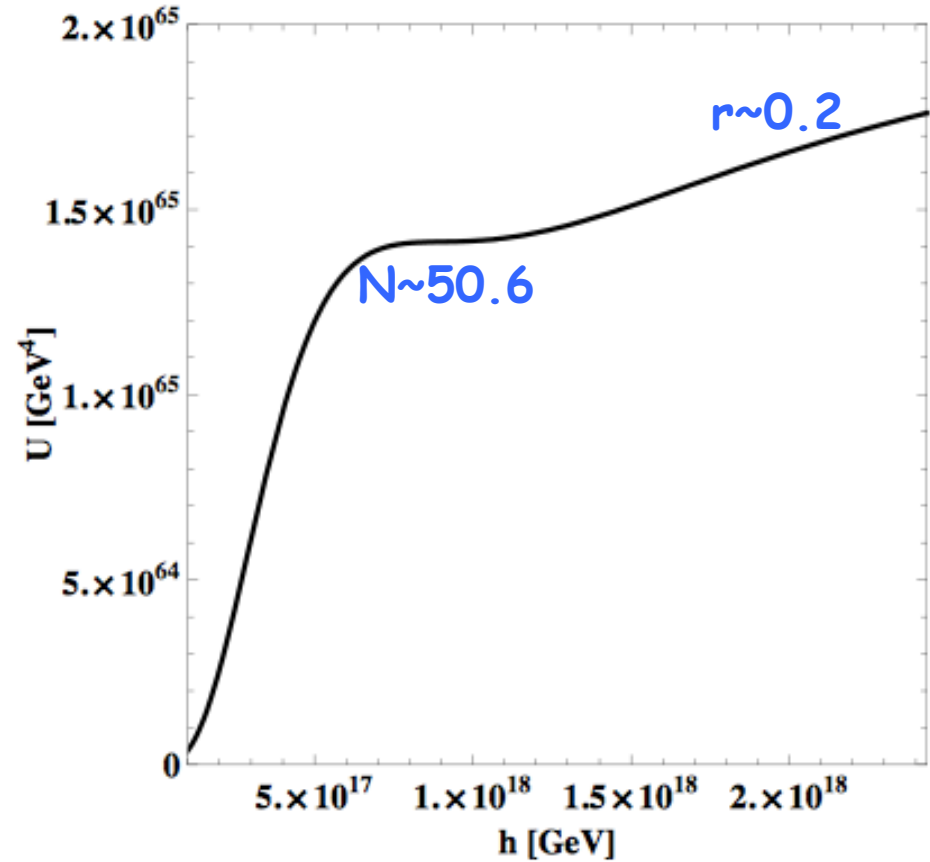
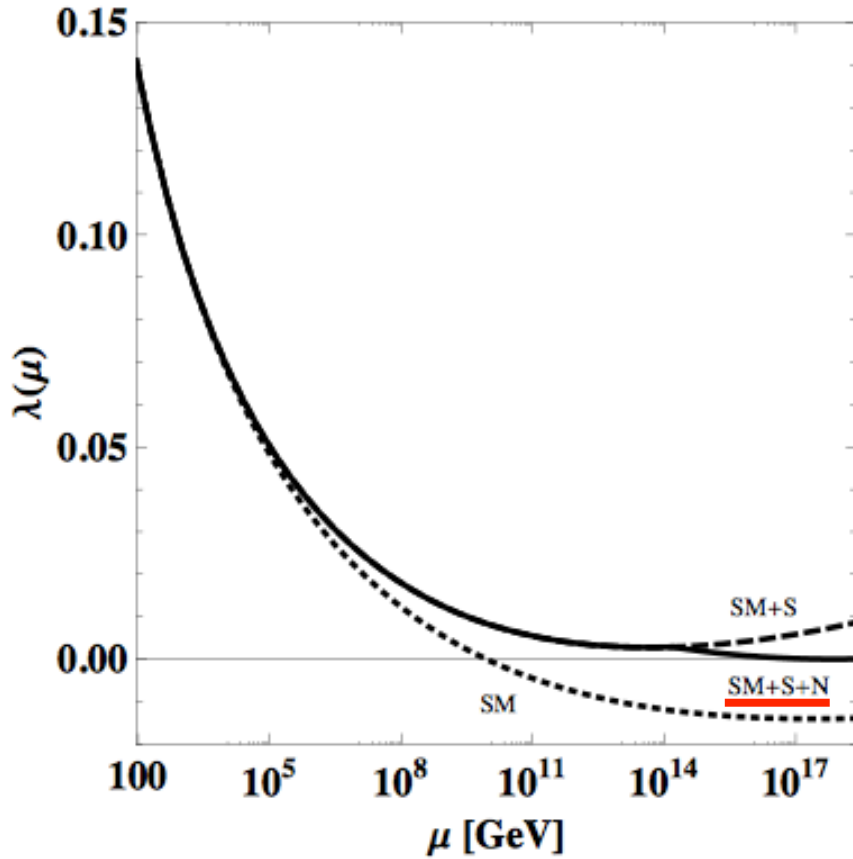
Higgs inflation

seem special

$$(4\pi)^2 \frac{d\lambda}{dt} = \underline{12\lambda^2} + 12\lambda y_t^2 - \underline{12y_t^4} - 3\lambda(g'^2 + 3g^2) + \frac{3}{8}[2g^4 + (g'^2 + g^2)^2]$$

↗ scalar eff.  
↘ fermion eff.

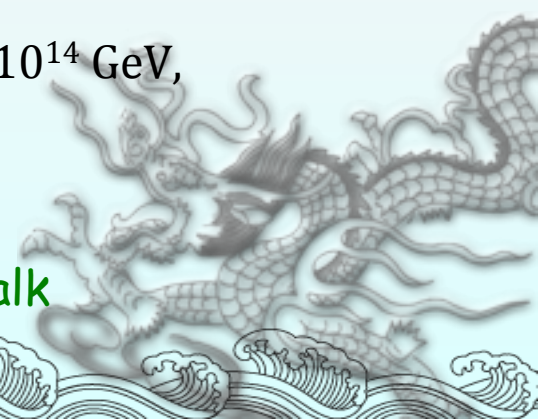
# suitable Higgs inflation



$m_{\text{top}} = 173.34$  GeV,  $m_H = 125.6$  GeV,  $m_S \simeq 1029$  GeV,  $M_R \simeq 1.58 \times 10^{14}$  GeV,  
 $k(M_Z) \simeq 0.325$ , and  $y_N(M_Z) = [m_\nu M_R]^{1/2}/v \simeq 0.512$ ,  $\xi=10.1$

$$S_G = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \frac{\xi h^2}{2} R \right\}$$

→ R. Takahashi's talk



# §5 summary



# summary

SM Higgs & top mass roughly implies

$\lambda \sim 0, \beta \sim 0$  @  $M_p$  ( $\leftarrow$  expect  $M_p$  scale physics(?))

but, not accurate (current top mass), nor no DM (tiny  $m_\nu$ , BAU) in SM  
(& still no evidence of BSM @ LHC)

$\rightarrow$  SM + scalar DM +  $\nu_R$  model

$\lambda = \beta = 0$  @  $M_p \rightarrow$  determine  $m_S$  &  $M_R$ , and

$M_p = 10^{18}$  GeV:  $m_S = 800$  GeV  $\sim 1.2$  TeV,  $M_R = 6.3 \times 10^{13} \sim 1.6 \times 10^{14}$  GeV

$M_p = 10^{19}$  GeV:  $m_S = 850$  GeV  $\sim 1.4$  TeV,  $M_R = 5.5 \times 10^{13} \sim 1.2 \times 10^{14}$  GeV

$\rightarrow$  Higgs inflation (consistent with BICEP2)  
can also possible in another option.

