

Radiative Neutrino Masses Linked to $0\nu\beta\beta$ Decay



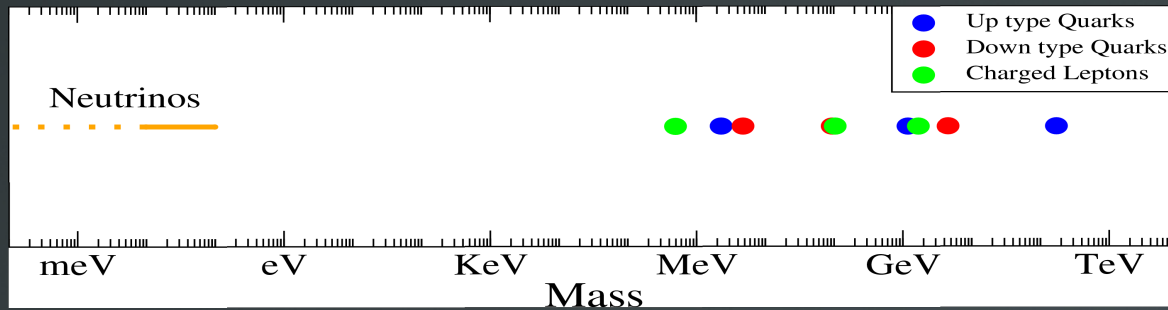
Jose Miguel No (Sussex U.)



FLASY14, Sussex, June 18th 2014



(Naturally small) Neutrino Masses

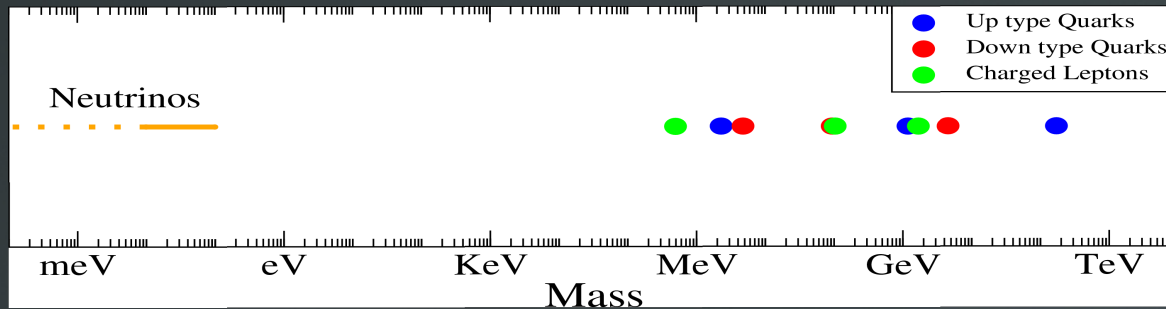


$m_\nu < 0.1 \text{ eV}$ **Why So Small?**

*Suggests Alternative Mechanism
for Neutrino Mass Generation*



(Naturally small) Neutrino Masses



Suggests Alternative Mechanism for Neutrino Mass Generation

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⇒ See-Saw Mechanism

⇒ Radiative Neutrino Masses

Loop suppression

Symmetry (e.g. Z_2) Connection to DM

Ma, Aoki, Kanemura, Morisi, Valle, Nasri, Peinado, Lineros, Okada, Kajiyama, Lindner, Suematsu, Watanabe, Seto, Pilafsis, Gustafsson, No, Kubo, Hirsch, McDonald, Farzan, Schmidt, Sugiyama...

(\supset Radiative See-Saw)

New EW States (+ Lepton Number Violation)

A. Zee, *Phys. Lett. B* **93** (1980) 389

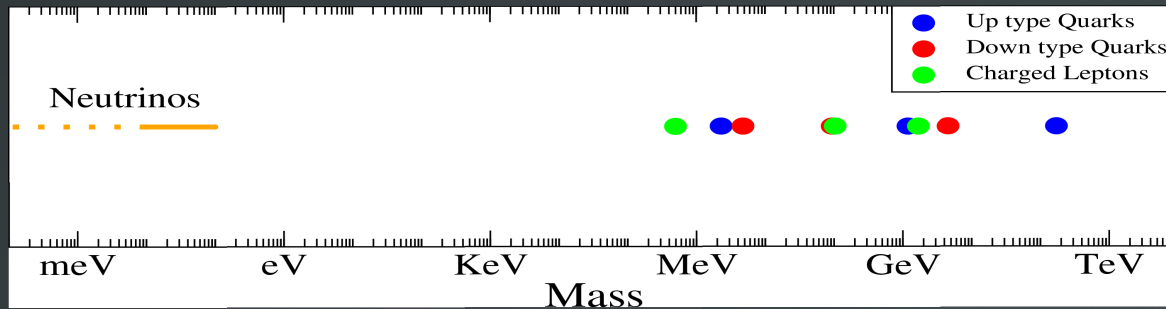
K. S. Babu, *Phys. Lett. B* **203** (1988) 132

...

Connection to EW Physics



(Naturally small) Neutrino Masses



Suggests Alternative Mechanism for Neutrino Mass Generation

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New EW States (+ Lepton Number Violation)

*A. Zee, Phys. Lett. B **93** (1980) 389*

*K. S. Babu, Phys. Lett. B **203** (1988) 132*

Connection to EW Physics

Rich Phenomenology:

- Possible Collider Signatures at LHC & ILC (Potential LNV!)
- Potentially large Lepton Flavour Violation signals
- Potentially large $0\nu\beta\beta$ decay signals



Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

(A Systematic Approach to Structure)

A Systematic Approach to $0\nu\beta\beta$?

⇒ Classify LNV Non-Renormalizable SM Operators ($\Delta L = 2$)

K. S. Babu, C. N. Leung, Nucl. Phys. B **619** (2001) 667

A. de Gouvea, J. Jenkins, Phys. Rev. D **77** (2008) 013008

F. Bonnet, M. Hirsch, T. Ota, W. Winter, JHEP **1303** (2013) 055

P. W. Angel, N. L. Rodd, R. R. Volkas, Phys. Rev. D **87** (2013) 7, 073007

$N_{\text{operators}} > 20$ $N_{\text{operators}} > 75$
($D \leq 9$) ($D \leq 11$)



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Assume:

⇒ LNV New (BSM) Physics Only Couples Directly to Leptons (not to quarks)

⇒ No New Gauge Symmetries (below a few TeV)

Construct Lowest Order LNV SM Operator (O_{SM})

Lepton
Chirality



Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

(A Systematic Approach to Structure)

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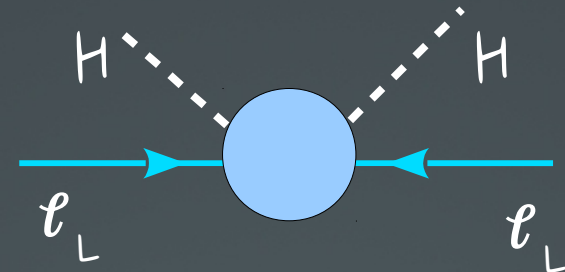
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Construct Lowest Order LNV SM Operator (O_{SM}) → Lepton Chirality

① If O_{SM} Involves 2 ℓ_L :

$D = 5$
Weinberg Operator



→ No Structure in Neutrino Mass Matrix m_{ab}^ν

→ $0\nu\beta\beta$ Dominated by Light Neutrino Exchange

J. Lopez-Pavon, S. Pascoli, C. Wong, Phys. Rev. D **87** (2013) 9, 093007



Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

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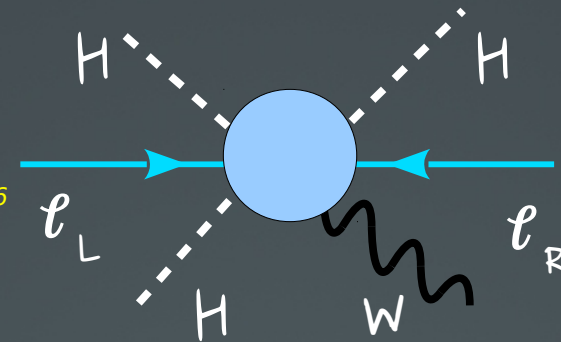
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Construct Lowest Order LNV SM Operator (O_{SM}) → Lepton Chirality

② If O_{SM} Involves 1 ℓ_R and 1 ℓ_L : $D = 7$

F. del Aguila, A. Aparici, S. Bhattacharya, A. Santamaria, J. Wudka, JHEP **1206** (2012) 146



$$(H^\dagger D_\mu \tilde{H}) (H^\dagger \bar{\ell}_R \gamma_\mu \tilde{\ell}_L)$$



Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

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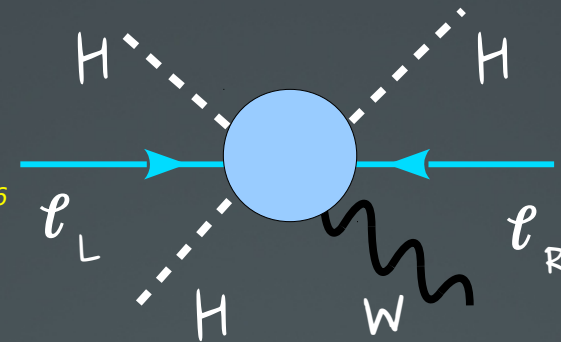
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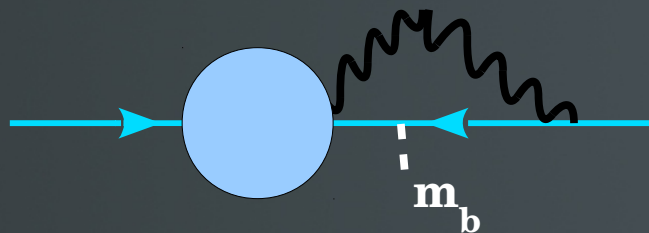
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F. del Aguila, A. Aparici, S. Bhattacharya, A. Santamaria, J. Wudka, JHEP **1206** (2012) 146



→ Structure in Neutrino Mass Matrix m_{ab}^ν → ($m_{ee}^\nu \approx 0$)



$$m_{ab}^\nu \sim \frac{\nu C_{ab} (m_a + m_b)}{(16\pi^2) \Lambda}$$

Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

(A Systematic Approach to Structure)

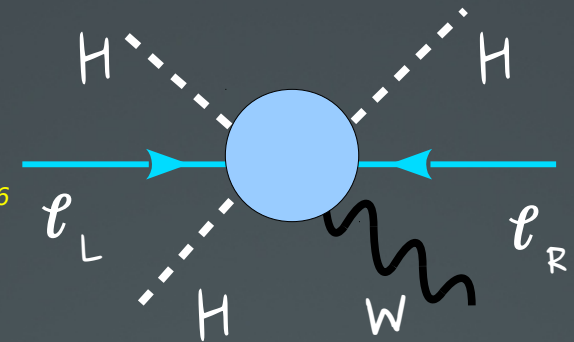
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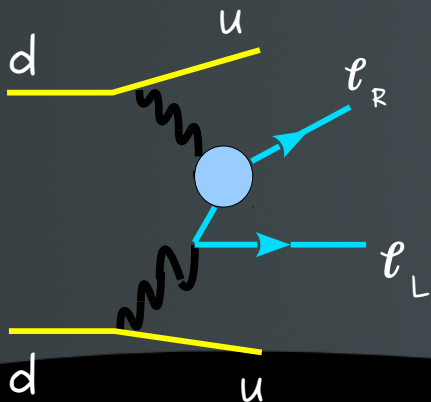
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F. del Aguila, A. Aparici, S. Bhattacharya, A. Santamaria, J. Wudka, JHEP **1206** (2012) 146



→ Short-Distance Contribution from O_{SM} Important for $0\nu\beta\beta$



- **Light Neutrino Exchange Contribution Suppressed** ($m_{ee}^\nu \approx 0$)
... but SD contribution has $16\pi^2 v/m_e$ "enhancement"
- **Electrons of Opposite Chirality**

Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

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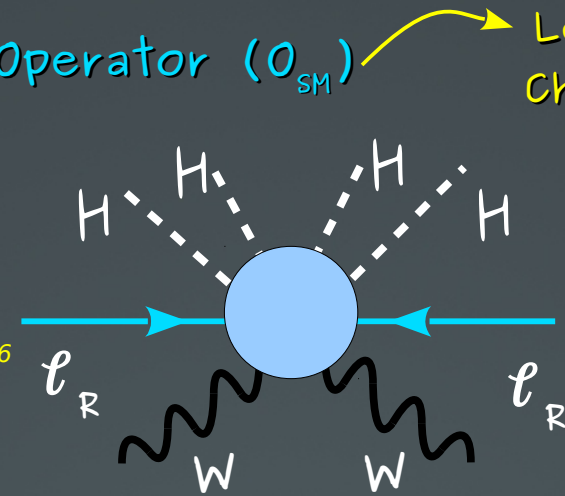
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③ If O_{SM} Involves 2 ℓ_R :

$$D = 9$$

F. del Aguila, A. Aparici, S. Bhattacharya, A. Santamaria, J. Wudka, JHEP 1206 (2012) 146

M. Gustafsson, J.M.N., M. Rivera, arXiv:1402.0515



$$\bar{\ell}_R \ell_R^c (H^\dagger D_\mu \tilde{H})^2$$



Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

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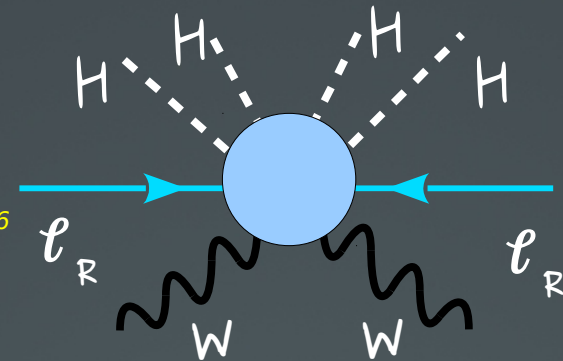
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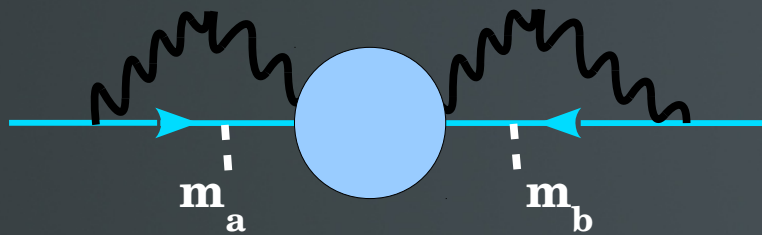
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→ Structure in Neutrino Mass Matrix m_{ab}^ν → ($m_{ee}^\nu \simeq 0, m_{e\mu}^\nu \simeq 0?$)



$$m_{ab}^\nu \sim \frac{C_{ab} m_a m_b}{(16\pi^2)^2 \Lambda}$$

Radiative ν -Masses & $0\nu\beta\beta$ (& Neutrino Mixing)

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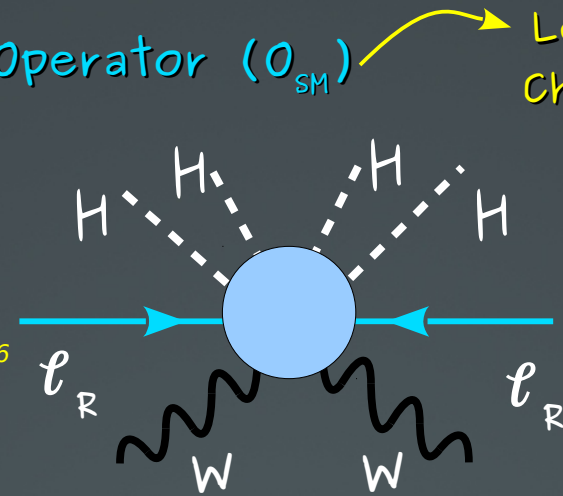
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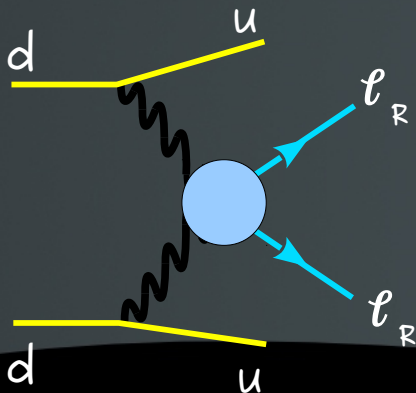
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M. Gustafsson, J.M.N, M. Rivera, arXiv:1402.0515

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→ Short-Distance Contribution from O_{SM} Crucial for $0\nu\beta\beta$



→ **Light Neutrino Exchange Contribution Negligible** ($m_{ee}^\nu \approx 0$)

... but SD contribution has $(16\pi^2)^2 v^2/m_e^2$ "enhancement"

① O_7 & O_9 give *Tree-Level* $0\nu\beta\beta$ vs *Loop-Level* m^ν

F. del Aguila, A. Aparici, S. Bhattacharya, A. Santamaria, J. Wudka, *JHEP* **1206** (2012) 146

M. Gustafsson, J.M.N, M. Rivera, *arXiv:1402.0515*

(Known to be possible for Effective Operators involving Quarks)

K. S. Babu, R. N. Mohapatra, *Phys. Rev. Lett.* **75** (1995) 2276

K. S. Babu, C. N. Leung, *Nucl. Phys. B* **619** (2001) 667



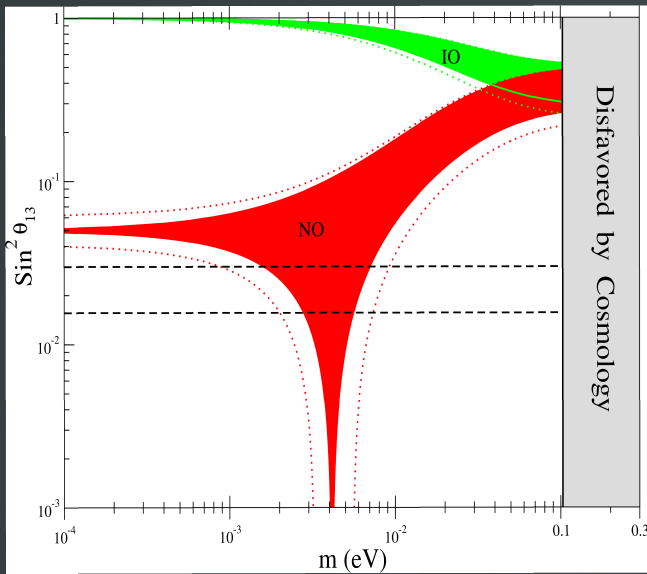
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② O_7 & O_9 give structure to m^ν \rightarrow $m_{ee}^\nu \simeq 0$

(A Word on Neutrino Mixing...)

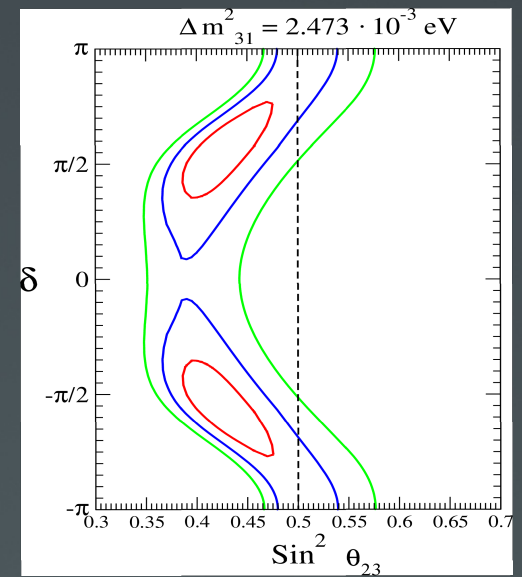
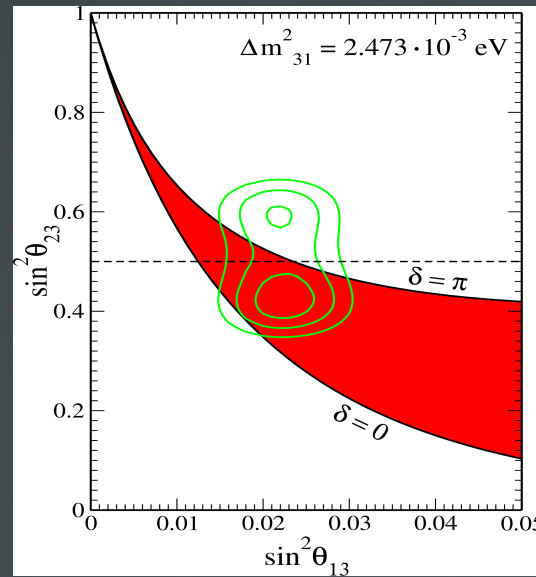
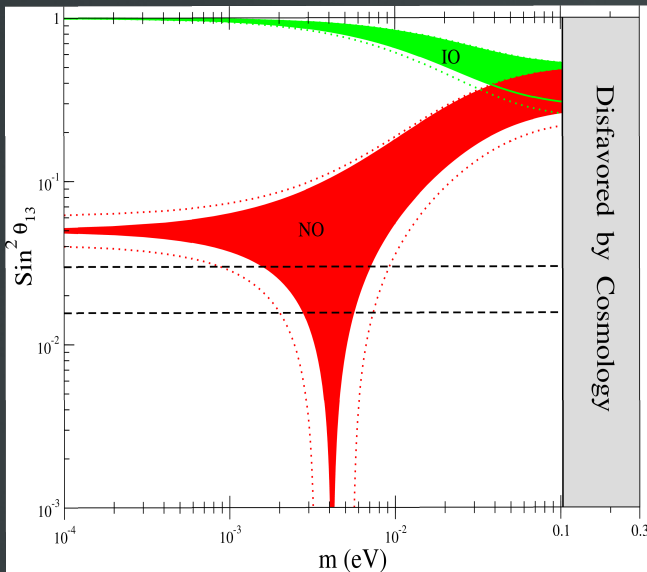


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 (A Word on Neutrino Mixing...)



Compatible with Current Oscillation Data
 Predictive (NO , θ_{23} Octant, δ_{CP})



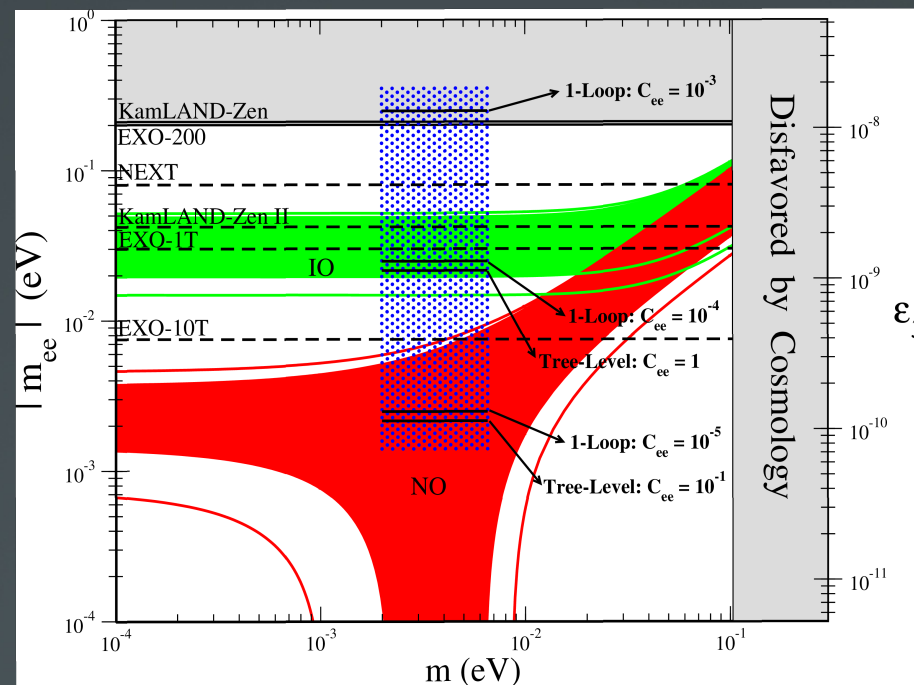
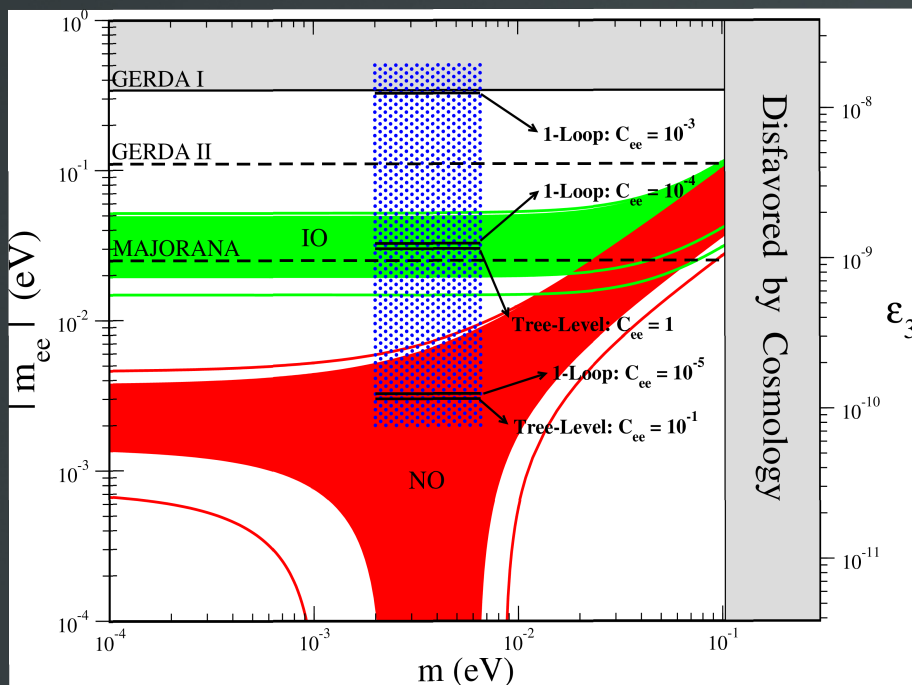
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M. Gustafsson, J.M.N, M. Rivera, arXiv:1402.0515

Short-Distance

$$\mathcal{L}_{0\nu\beta\beta} = \frac{G_F^2}{2 m_p} \epsilon_3 J^\mu J_\mu \bar{e}(1 - \gamma_5)e^c$$



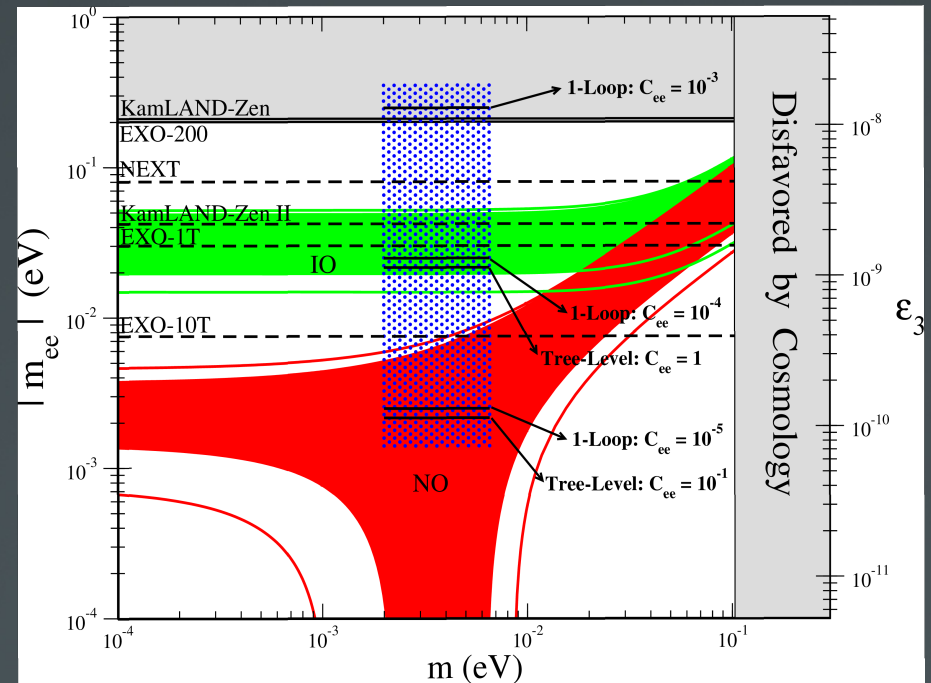
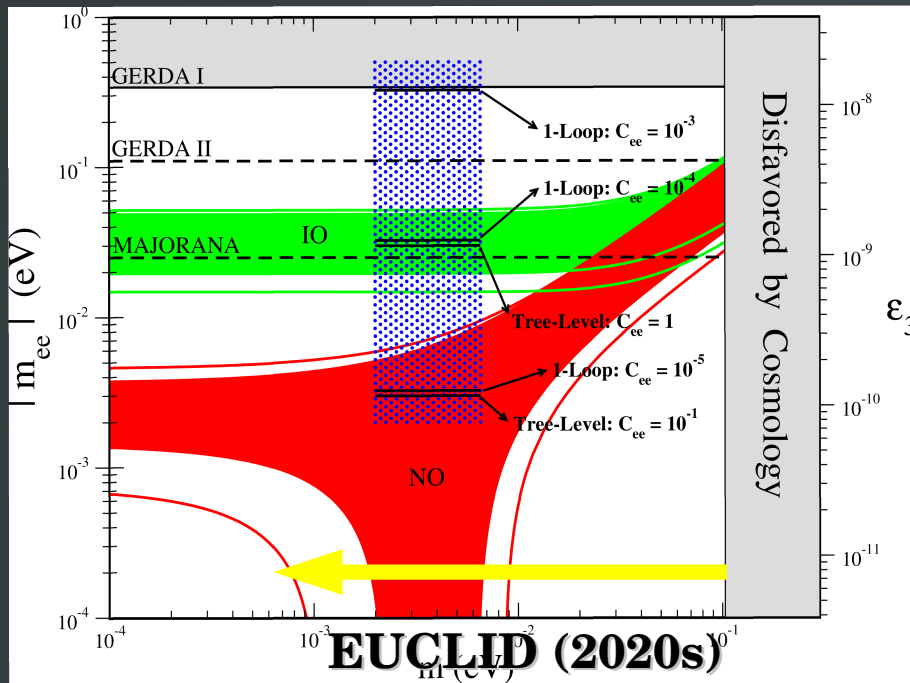
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Positive signal in $0\nu\beta\beta$ combined with NO (hierarchical) as a way to test O_7/O_9

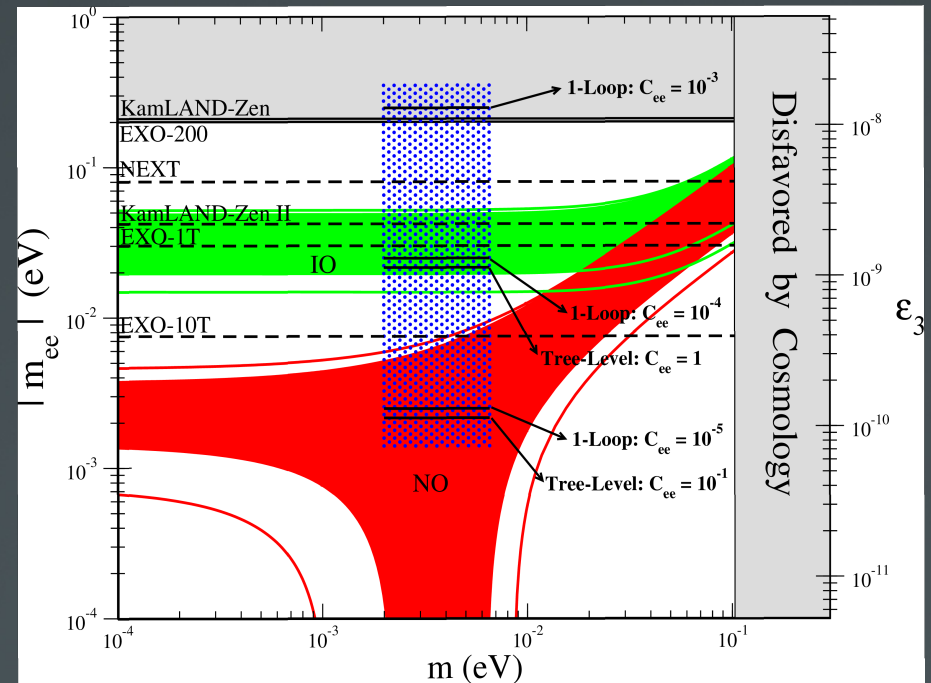
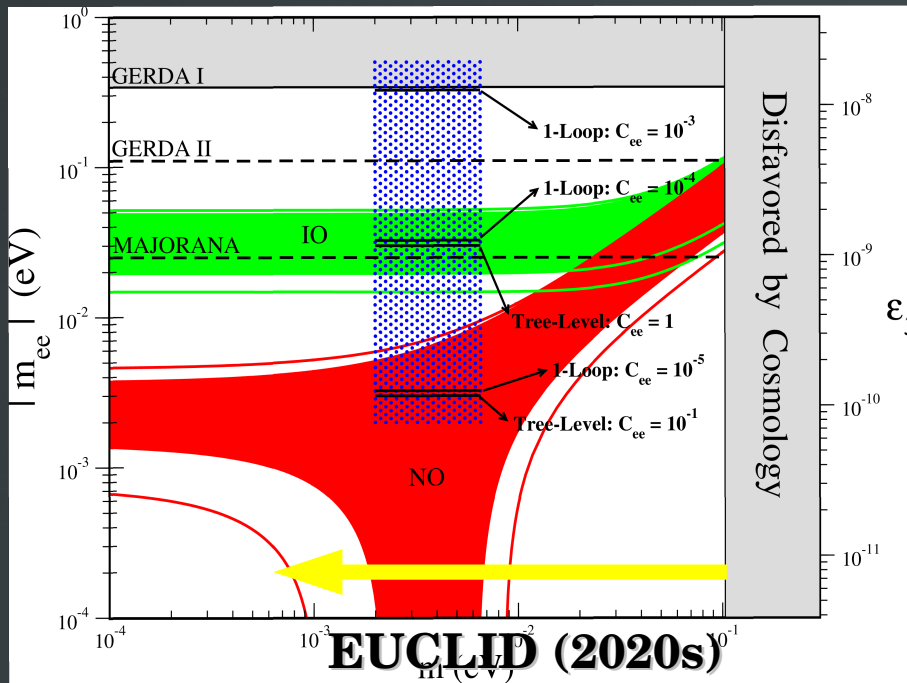
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Angular Distribution in SuperNEMO?

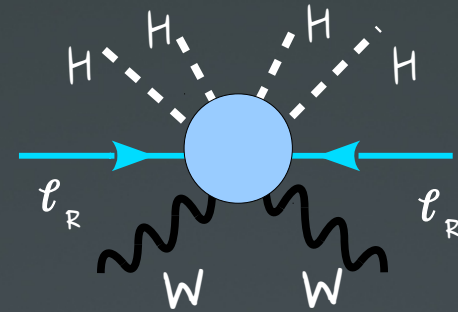
Electrons of Opposite Chirality

A Word for the Model Builder...



A Word for the Model Builder...

Renormalizable Completions of O_9



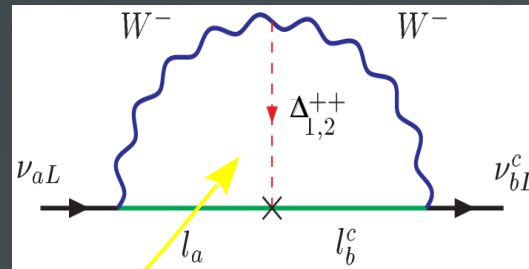
Tree-Level (2-Loop Neutrino Masses)

C. S. Chen, C. Q. Geng, J. N. Ng, *Phys. Rev. D* **75** (2007) 053004

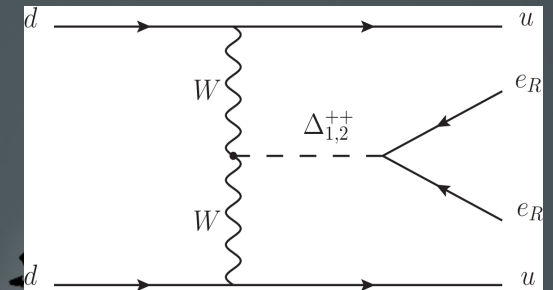
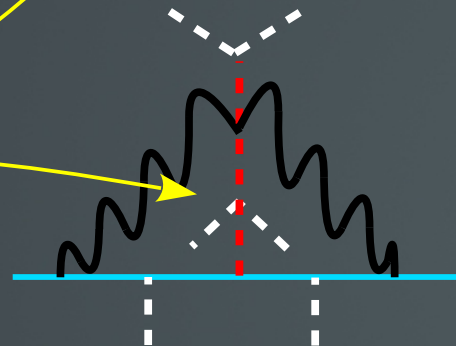
F. del Aguila, A. Aparici, S. Bhattacharya, A. Santamaria, J. Wudka, *JHEP* **1205** (2012) 133

$$C_{ab} \bar{l}_{Ra} l_{Rb}^c \rho^{--}$$

(+ Complex SU(2) Triplet Δ)



ρ^{++} and Δ^{++} Mix

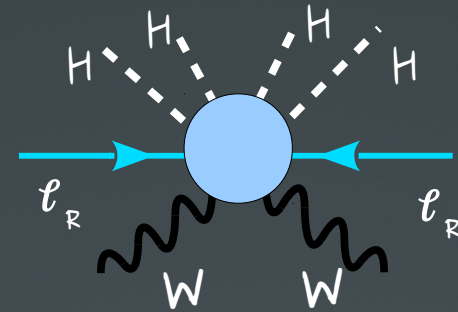


A Word for the Model Builder...

Renormalizable Completions of O_9

1-Loop (3-Loop Neutrino Masses)

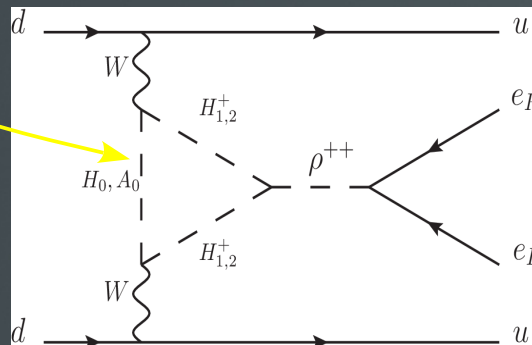
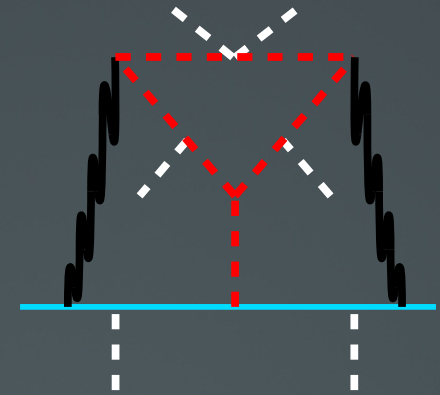
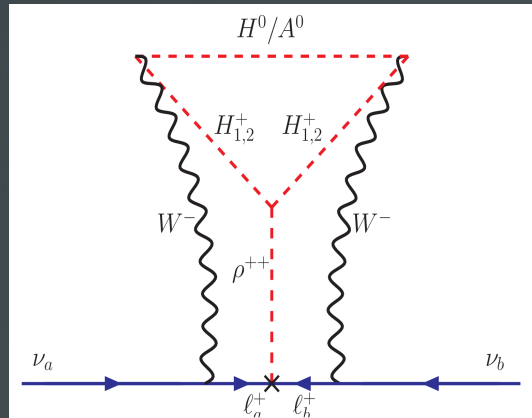
M. Gustafsson, J. M. N., M. Rivera, *Phys. Rev. Lett* **110** (2013) 211802



The "Cocktail" Model

$$C_{ab} \bar{\ell}_{Ra} \ell_{Rb}^c \rho^{--}$$

(+ DM Running in the Loop)



Conclusions

$0\nu\beta\beta$ Decay  *Standard Mechanism* (Light-neutrino Exchange)
New Particles (Short-Distance Physics)

Effective  *Operators*

If LNV New Physics Couples Only to Leptons (not Quarks),
few Operators (e.g. O_7 & O_9)

There exist attractive ways to connect Radiative Neutrino Mass
Generation to $0\nu\beta\beta$ Decay Probes of the Majorana Nature of
Neutrinos

Ultimate Answer: $0\nu\beta\beta$ + LHC + Cosmology



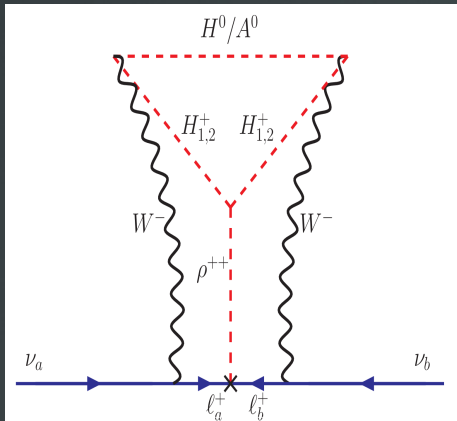
Thanks!





The "Cocktail" Model

Inert Doublet Model "&" inspired by Zee/Babu



$$\Phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG_0}{\sqrt{2}} \end{pmatrix} + \begin{pmatrix} 0 \\ v \end{pmatrix} \quad \Phi_2 = \begin{pmatrix} \Lambda^+ \\ \frac{H_0+iA_0}{\sqrt{2}} \end{pmatrix} \quad S^+ \quad \rho^{++}$$

$$-\Delta\mathcal{L} = C_{ab} \overline{l_{R_a}^c} l_{R_b} \rho^{++} + V(|\Phi_1|^2, |\Phi_2|^2, |S|^2, |\rho|^2) + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 \\ + \kappa_1 \Phi_1^T i\sigma_2 \Phi_2 S^- + \lambda_{\rho S} \Phi_1^T i\sigma_2 \Phi_2 S^+ \rho^{--} + \kappa_2 S^- S^- \rho^{++} + \text{h.c.}$$

Lepton Number Breaking

Need $C_{ab} \neq 0, \lambda_5 \neq 0, (\kappa_1 \neq 0)$

Need $\lambda_{\rho S}$ or $\kappa_2 \neq 0$