

# Multicomponent dark matter in radiative seesaw model

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**Collaboration with**

**J. Kubo (Kanazawa U.), H. Takano (IPMU)**

[arXiv:1406.xxxx [hep-ph]]

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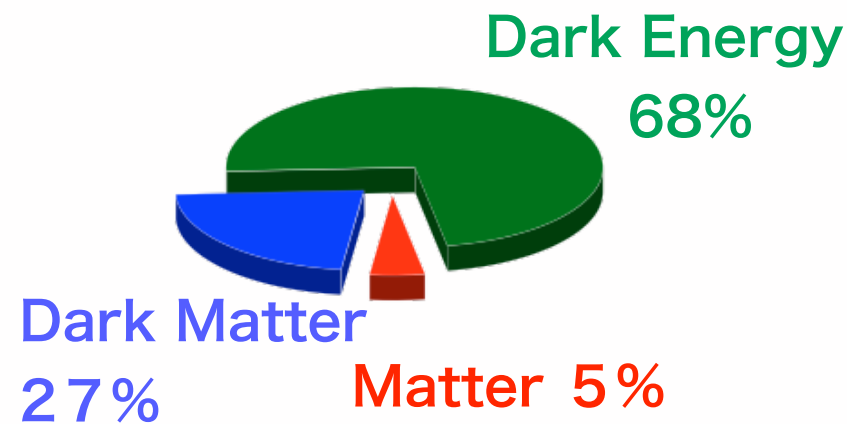
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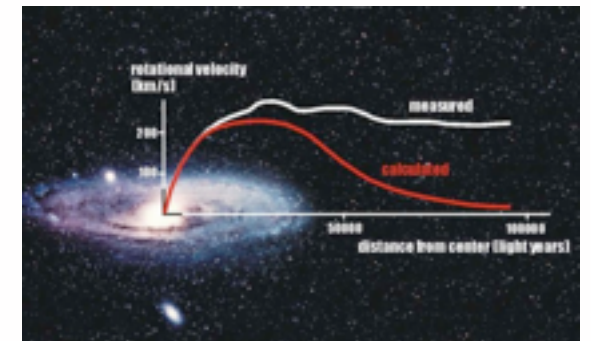
# Introduction

## Dark Matter

The existence of DM has been confirmed by astronomy, but the origin of DM is still unknown.



Gravitational lens



Galaxy rotation curves



Bullet Cluster

- Stability of the DM can be guaranteed by an unbroken symmetry.
- The simplest possibility is a  $Z_2$  symmetry.
- If the DM stabilizing symmetry is larger than  $Z_2$ , **a multicomponent DM system can be realized.**

e.g.)  $Z_N$  ( $N \geq 4$ )

a product of two or more  $Z_2$ 's

:

Boehm, Fayet and Silk, PRD69 (2004); D'Eramo and Thaler, JHEP 1006 (2010); Belanger et al, JCAP 1204 (2012), arXiv:1403.4960 [hep-ph]; Ivanov and Keus, Phys. Rev. D 86, (2012), etc.

# Introduction

## Multicomponent DM system

e.g.)

- Model with  $Z_2 \times Z_2'$

$$\underline{m_3 > m_2 > m_1}$$

- $m_3 > m_1 + m_2$

$$\chi_3 \rightarrow \chi_1 \chi_2$$

2 DM particle

- $m_3 < m_1 + m_2$

3 DM particles

	$Z_2$	$Z_2'$
$\chi_1$	-	+
$\chi_2$	+	-
$\chi_3$	-	-

- Model with  $Z_4$  symmetry

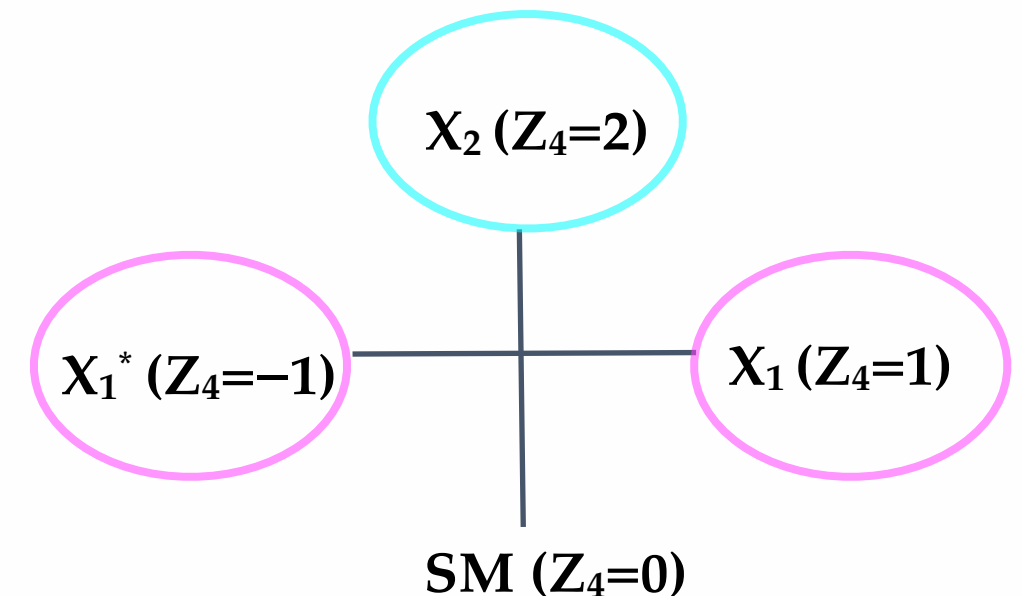
- $m_2 > m_1 + m_1$

$$\chi_2 \rightarrow \chi_1 \chi_1$$

1 DM particle

- $m_2 < m_1 + m_1$

2 DM particles

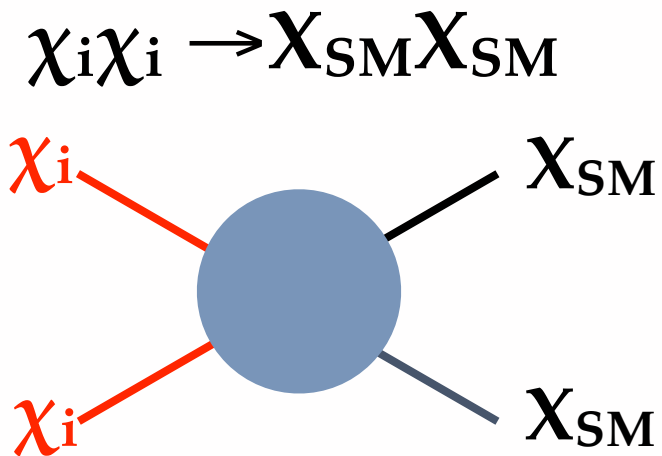


# Introduction

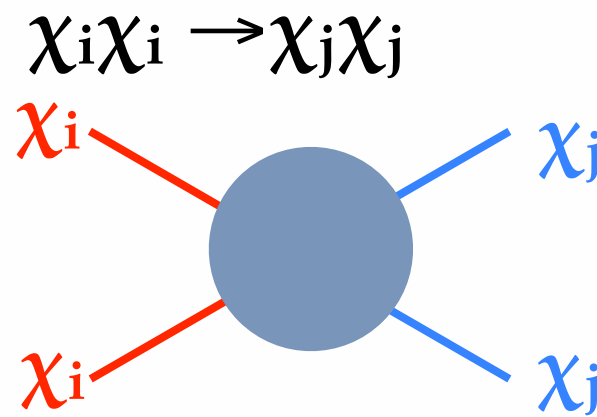
## DM annihilation processes

In addition to the standard annihilation processes, there can be nonstandard DM annihilation processes.

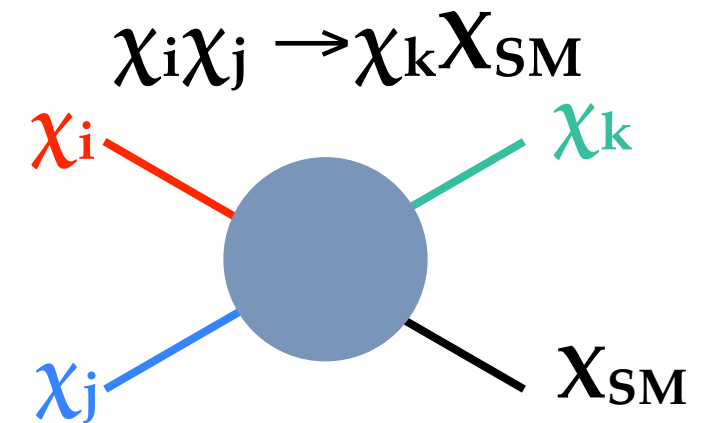
Standard



DM Conversion



Semi-annihilation



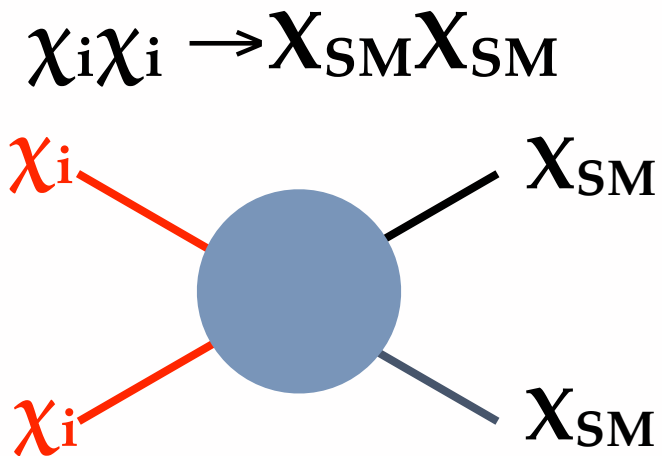
$$\dot{n}_{\chi_1} + 3Hn_{\chi_1} = - \left\{ \underbrace{\langle \sigma_{\chi_1 \chi_1 \rightarrow X_{SM} X_{SM}} |v| \rangle (n_{\chi_1}^2 - \bar{n}_{\chi_1}^2)}_{\text{standard}} + \underbrace{\langle \sigma_{\chi_1 \chi_1 \rightarrow \chi_2 \chi_2} |v| \rangle (n_{\chi_1}^2 - \bar{n}_{\chi_1}^2 \frac{n_{\chi_2}^2}{\bar{n}_{\chi_2}^2})}_{\text{DM conversion}} + \underbrace{\langle \sigma_{\chi_1 \chi_2 \rightarrow \chi_3 X_{SM}} |v| \rangle (n_{\chi_1} n_{\chi_2} - \bar{n}_{\chi_1} \bar{n}_{\chi_2} \frac{n_{\chi_3}}{\bar{n}_{\chi_3}})}_{\text{semi-annihilation}} \right\}$$

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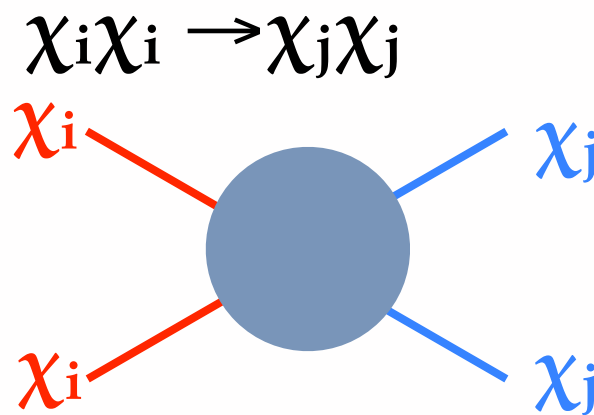
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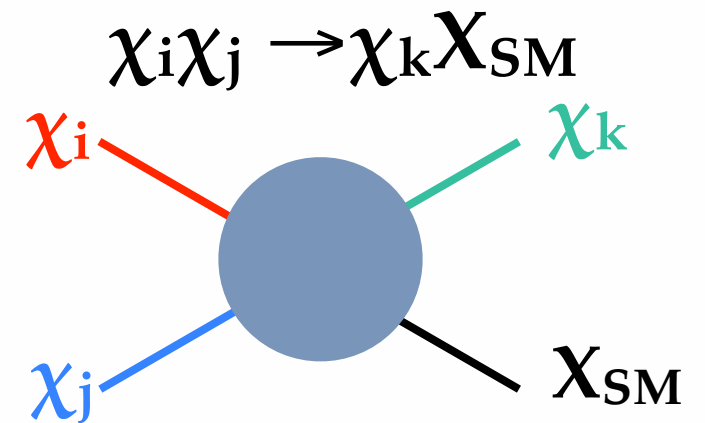
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Semi-annihilation in the single component DM system

Single component DM:  $\chi\chi \rightarrow \chi^* X_{SM}$

$Z_3$  symmetric DM, New Vector boson DM

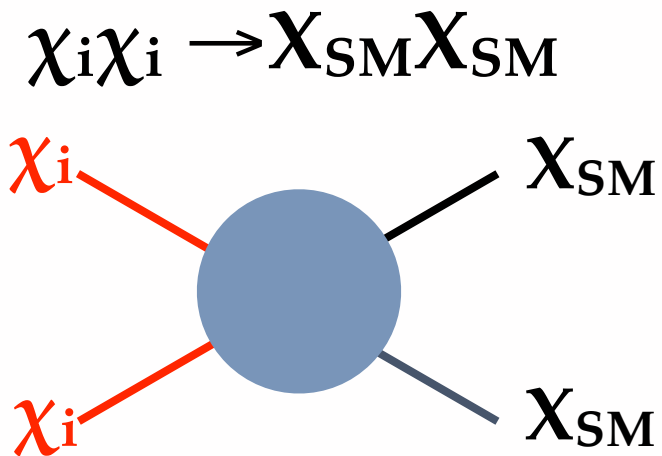
D'Eramo and Thaler, JHEP1006(2010); Belanger et al, JCAP1204(2012), JCAP(2013), arXiv:1403.4960 [hep-ph]; Hambye, JHEP0901(2009); Arina et al, JCAP1003(2010), etc.

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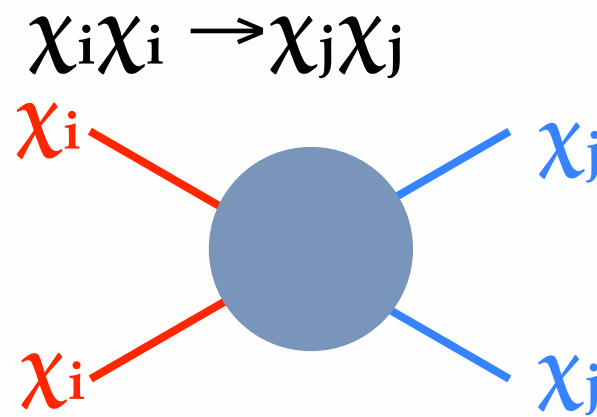
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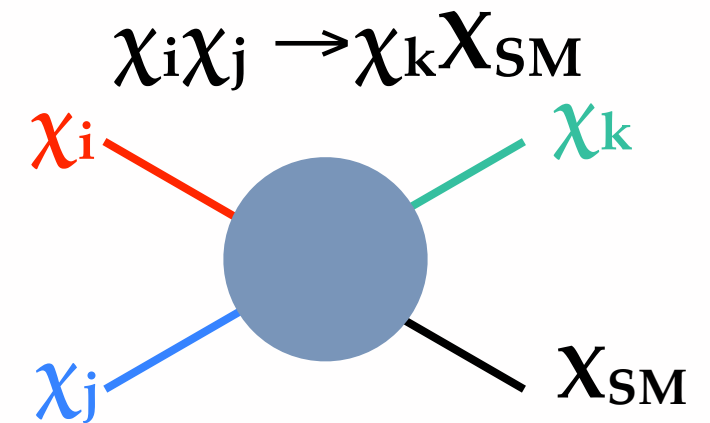
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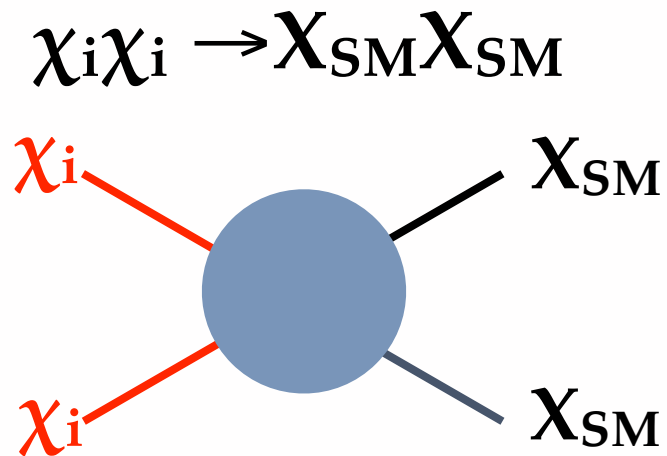


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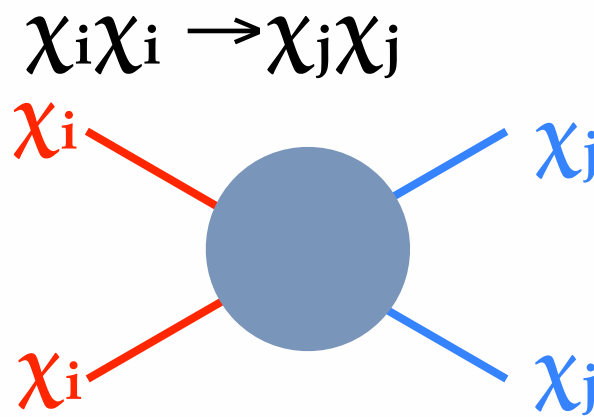
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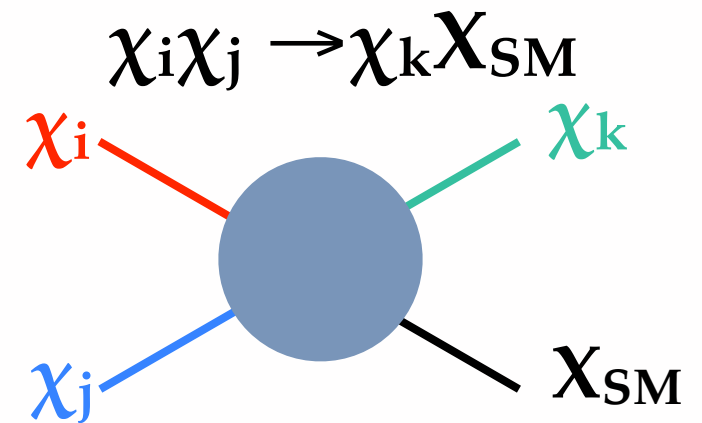
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Impact on the indirect signals :

- PAMELA/Fermi positron excess,
- Fermi-Lat  $\gamma$ -line,
- Fermi-Lat diffuse  $\gamma$  from the Galactic center
- :

Boehm, Fayet, Silk, PRD69 (2004); Cao et al, arXiv:0711.3881 [hep-ph]; Huh, Kim, Kyae, PRD79 (2009); Zurek, PRD79 (2009); D'Eramo, McCullough, Thaler, JCAP1304, (2013); Biswas et al, arXiv:1301.3668 [hep-ph]; MA, Kubo, Takano, PRD87 (2013); Gu, Phys.Dark Univ. 2 (2013), etc



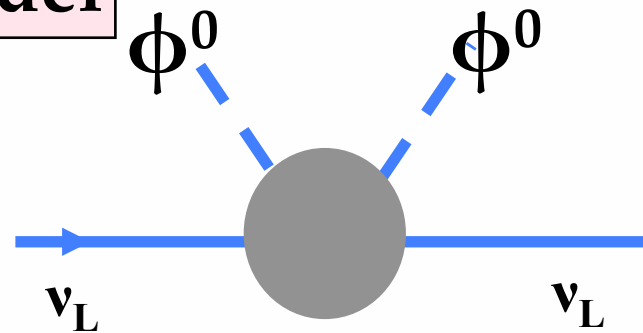
# Introduction

DM stabilizing symmetry



Neutrino mass generation mechanism

Radiative seesaw model



**N-loop:** 
$$m_{\nu}^{ij} = \left( \frac{1}{16\pi^2} \right)^N \frac{f_{ij}}{\Lambda} \langle \phi^0 \rangle^2$$

Neutrino masses are generated via the radiative effect.

⇒ Due to the loop suppression factor,  $\Lambda$  can be lower.

**Neutrino masses would be explained by the TeV-scale physics.**

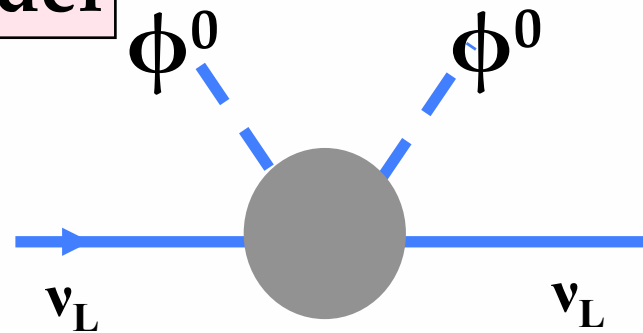
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Zee, PLB93,389 (1980),  
PLB161,141 (1985)

Zee, NPB264,99 (1986)  
Babu, PLB203,132 (1988)

Ma, PRD73, 077301 (2006)

Krauss, Nasri, Trodden  
PRD67,085002 (2003)

Exact discrete symmetry is imposed.

We study the multicomponent DM system in the extended Ma model.

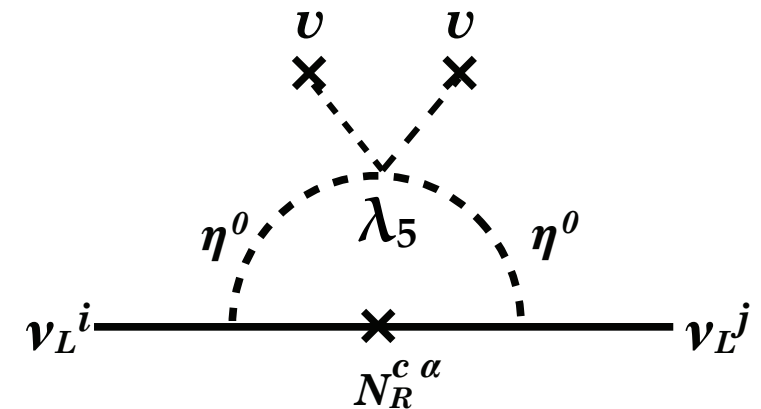
# Ma model

## Ma model

SM +  $N_R$  +  $\eta$

Ma, PRD73, 077301 (2006)

field	$SU(2)_L$	$U(1)_Y$	$Z_2$
$(\nu_{Li}, l_i)$	2	-1/2	+
$l_i^c$	1	1	+
$N_i^c$	1	0	-
$H = (H^+, H^0)$	2	1/2	+
$\eta = (\eta^+, \eta^0)$	2	1/2	-



- Inert doublet scalar

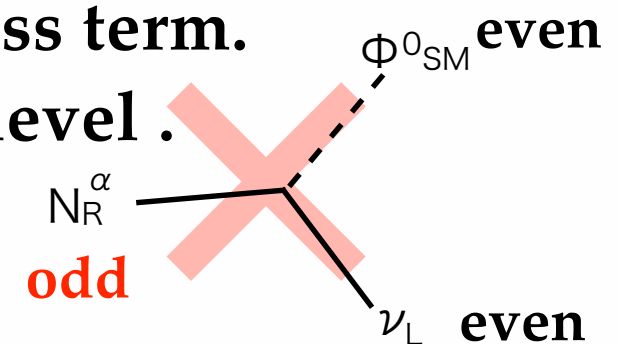
$$\eta = \begin{pmatrix} \eta^+ \\ (\eta_R^0 + i\eta_I^0)/\sqrt{2} \end{pmatrix}, \quad \langle \eta \rangle = 0$$

-  $Z_2$  symmetry is introduced to forbid the Dirac neutrino mass term.

→ Then the neutrino masses are generated at the one-loop level.

- Relevant Lagrangian

$$\mathcal{L} = Y_{ik}^\nu L_i \epsilon \eta N_k^c - \left[ \frac{1}{2} M_k N_{Rk}^c N_{Rk}^c + \frac{1}{2} \lambda_5 (H^\dagger \eta)^2 + h.c. \right]$$



- Single component DM

$$N_R, \eta_R^0 \text{ or } \eta_I^0$$

# Ma model

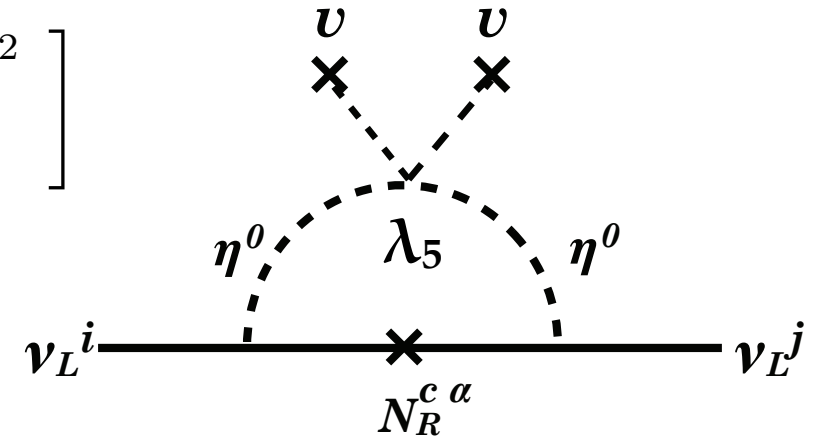
## • Neutrino masses

$$(\mathcal{M}_\nu)_{ij} = \sum_k \frac{Y_{ik}^\nu Y_{jk}^\nu M_k}{16\pi^2} \left[ \frac{m_{\eta_R^0}^2}{m_{\eta_R^0}^2 - M_k^2} \ln \left( \frac{m_{\eta_R^0}}{M_k} \right)^2 - \frac{m_{\eta_I^0}^2}{m_{\eta_I^0}^2 - M_k^2} \ln \left( \frac{m_{\eta_I^0}}{M_k} \right)^2 \right]$$

- small  $\lambda_5$  case ( $\lambda_5 \ll m_0$ )

$$2\lambda_5 v^2 = m_{\eta_R}^2 - m_{\eta_I}^2 \quad m_0^2 = \frac{m_{\eta_R^0}^2 + m_{\eta_I^0}^2}{2}$$

$$(\mathcal{M}_\nu)_{ij} \simeq \frac{Y_{ik} Y_{jk} \lambda_5 v^2}{8\pi^2} \frac{M_k}{m_0^2 - M_k^2} \left\{ 1 - \frac{M_k^2}{m_0^2 - M_k^2} \ln \frac{m_0^2}{M_k^2} \right\}$$



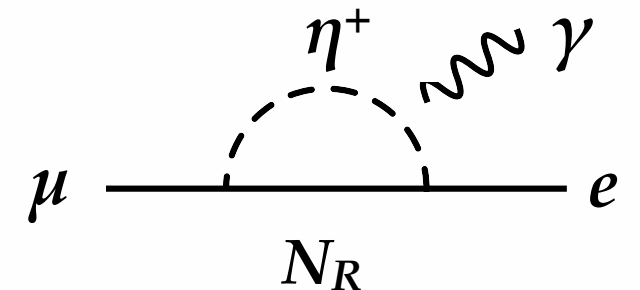
→  $M\nu = 0.1 \text{ eV}$ , New masses  $\sim \text{O}(100) \text{ GeV} \rightarrow |Y_\nu Y_\nu \lambda_5| \sim 10^{-10}$

## • Lepton Flavor Violation :

-  $\mu \rightarrow e\gamma$  constraint :

$$B(\mu \rightarrow e\gamma)^{\text{exp}} \lesssim 5.7 \times 10^{-13} \quad \text{MEG(2013)}$$

→  $Y_\nu Y_\nu \lesssim 10^{-4}$

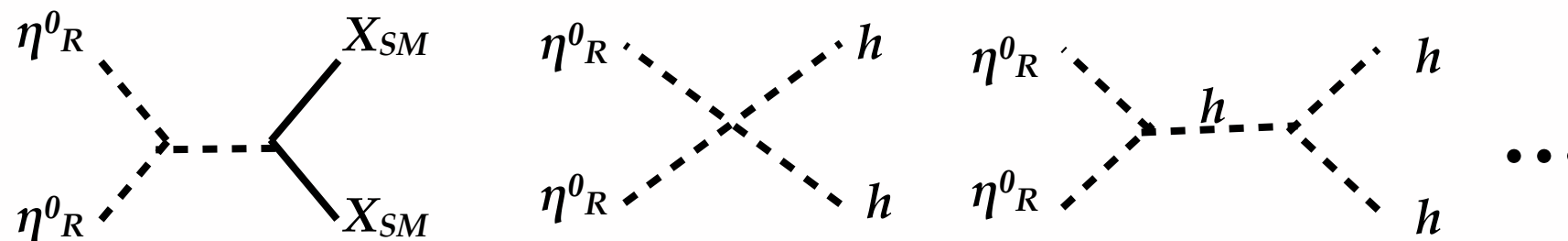


# Ma model

- Dark Matter

$$N_R, \eta^0_R \text{ or } \eta^0_I$$

$\eta$  DM :



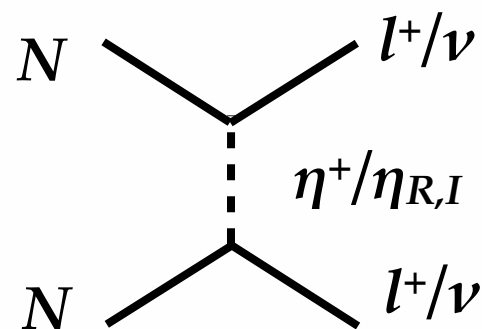
Two mass regions of DM consistent with the data.

- low-mass region (  $40 \text{ GeV} < m_\eta < 80 \text{ GeV}$  ) [Lopez Honorez et al., JCAP0702\(2007\);](#)
- high-mass region (  $> 500 \text{ GeV}$  ) [Gustafsson et al. PRD86 \(2012\)](#)

$N_R$  DM :

$$\Omega h^2 \sim 0.12 \rightarrow Y_\nu \sim 1$$

[Kubo et al. PLB642 \(2006\)](#)



# Ma model

- Neutrino masses :  $|Y_\nu Y_\nu \lambda_5| \sim 10^{-10}$

- LFV :  $Y_\nu Y_\nu \lesssim 10^{-4}$

-  $N_R$  DM relic abundance :  $Y_\nu \sim 1$

- There is **the tension between the LFV and the relic abundance.**
- We need some **fine tuning to obtain the small  $\lambda_5$  for  $Y_\nu \sim 0.01$ .**

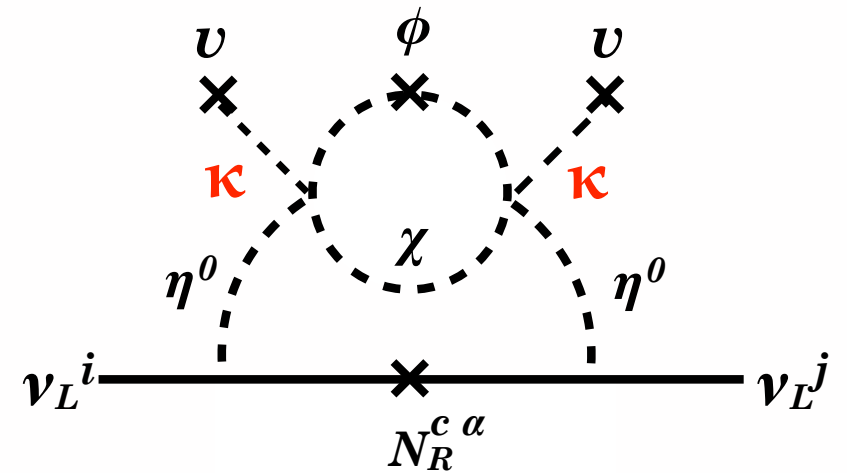
$$\lambda_5 \sim 10^{-5} \text{ for } Y_\nu \sim 0.01$$

→ Extension the Ma model

# Model

## Two-loop radiative seesaw model

field	$SU(2)_L$	$U(1)_Y$	$Z_2$	$Z'_2$	$L$
$(\nu_L, l_L)$	2	-1/2	+	+	1
$l_R^c$	1	1	+	+	-1
$N_R^c$	1	0	-	+	0
$H = (H^+, H^0)$	2	1/2	+	+	0
$\eta = (\eta^+, \eta^0)$	2	1/2	-	+	-1
$\chi$	1	0	+	-	0
$\phi$	1	0	-	-	1



$$\phi = (\phi_R + i\phi_I)/\sqrt{2}.$$

- The  $\lambda_5$  term,  $\lambda_5 (H^\dagger \eta)^2 + h.c.$ , in Ma model is forbidden by  $\#L$ .
- The  $\lambda_5^{\text{eff}}$  is generated at the 1-loop level.
- New relevant terms for neutrino mass :

$$V \supset \frac{\kappa}{2} [(H^\dagger \eta) \chi \phi + h.c.] + \frac{1}{2} m_5^2 [\phi^2 + (\phi^*)^2]$$

- $\#L$  is softly violated at  $m_5^2$  term.
- $m_{\eta R} = m_{\eta I}$  at the tree level. The degeneracy is lifted by  $\lambda_5^{\text{eff}}$ .
- DM candidates are  $N_R, \eta^0_{R/I}, \chi, \phi^0_{R/I}$  **Multicomponent DM system**

$$(Z_2, Z_2') = (-,+), (+,-), (-,-)$$

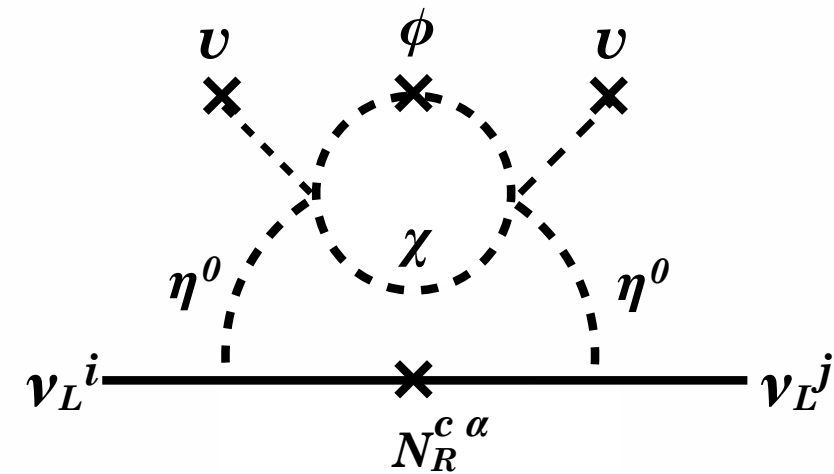


# Neutrino mass

- Neutrino mass

$$(\mathcal{M}_\nu)_{ij} \simeq -\frac{\lambda_5^{\text{eff}} v_h^2}{8\pi^2} \sum_k \frac{Y_{ik}^\nu Y_{jk}^\nu M_k}{m_{\eta^0}^2 - M_k^2} \left[ 1 - \frac{M_k^2}{m_{\eta^0}^2 - M_k^2} \ln \frac{m_{\eta^0}^2}{M_k^2} \right].$$

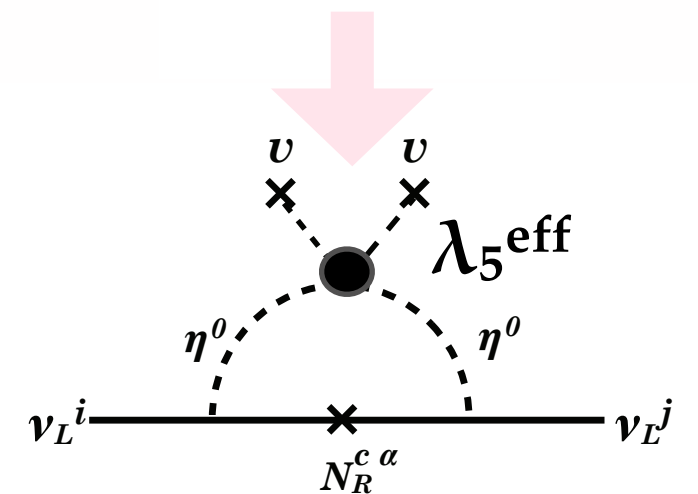
$$m_{\eta^0} = m_{\eta_R^0} \simeq m_{\eta_I^0}$$



$\lambda_5^{\text{eff}}$  term (for  $m_5^2 = m_{\phi R}^2 - m_{\phi I}^2 \ll m_{\phi R}^2$ )

$$\lambda_5^{\text{eff}} \simeq -\frac{\kappa^2}{64\pi^2} \frac{m_5^2}{m_{\phi R}^2 - m_\chi^2} \left[ 1 - \frac{m_\chi^2}{m_{\phi R}^2 - m_\chi^2} \ln \frac{m_{\phi R}^2}{m_\chi^2} \right]$$

- The neutrino mass is proportional to  $|Y_\nu \kappa|^2 m_5^2$ .
- $M_\nu = 0.1$  eV, New physical masses  $\sim \mathcal{O}(100)$  GeV  $\rightarrow \kappa Y_\nu m_5 \sim 10^{-2}$  GeV
- $\kappa \sim 0.1, Y_\nu \sim 0.01 \rightarrow m_5 \sim 10$  GeV,  $\lambda_5^{\text{eff}} \sim 10^{-5}$



➔ The smallness of  $\lambda_5$  is explained by the radiative generation.

# Dark matter

We assume  $N_R$ ,  $\chi$  and  $\phi_R$  are the DM.  $\rightarrow$  Three-component DM system.

## DM annihilation processes:

We assume  $m_\phi > m_\chi$ .

Standard annihilation :  $NN \rightarrow XX'$ ,  $\phi_R\phi_R \rightarrow XX'$ ,  $\chi\chi \rightarrow XX'$ ,

DM conversion :  $\phi_R\phi_R \rightarrow \chi\chi$ ,

Semiannihilation :  $N\phi_R \rightarrow \chi\nu$ ,  $\chi N \rightarrow \phi_R\nu$ ,  $\phi_R\chi \rightarrow N\nu$ ,

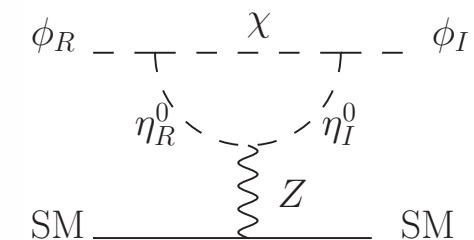
## - Annihilation processes of $\phi_I$

Standard annihilation :  $\phi_I\phi_I \rightarrow XX'$ ,

DM conversion :  $\phi_I\phi_I \rightarrow \chi\chi$ ,

Semiannihilation :  $N\phi_I \rightarrow \chi\nu$ ,  $\chi N \rightarrow \phi_I\nu$ ,  $\phi_I\chi \rightarrow N\nu$ .

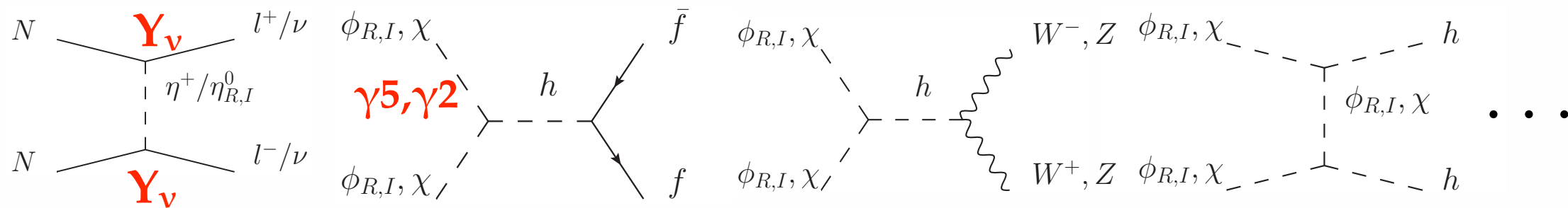
## - Conversion between $\phi_I \rightleftharpoons \phi_R$



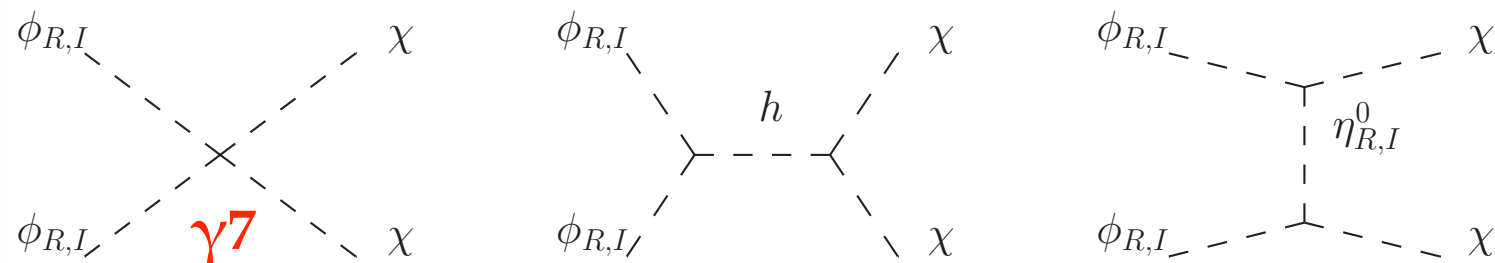
- We sum up the number densities of  $\phi_I$  and  $\phi_R$ ,  $n_\phi = n_{\phi_I} + n_{\phi_R}$ , and solve the Boltzmann equation of  $n_N$ ,  $n_\phi$  and  $n_\chi$ .

# Dark matter

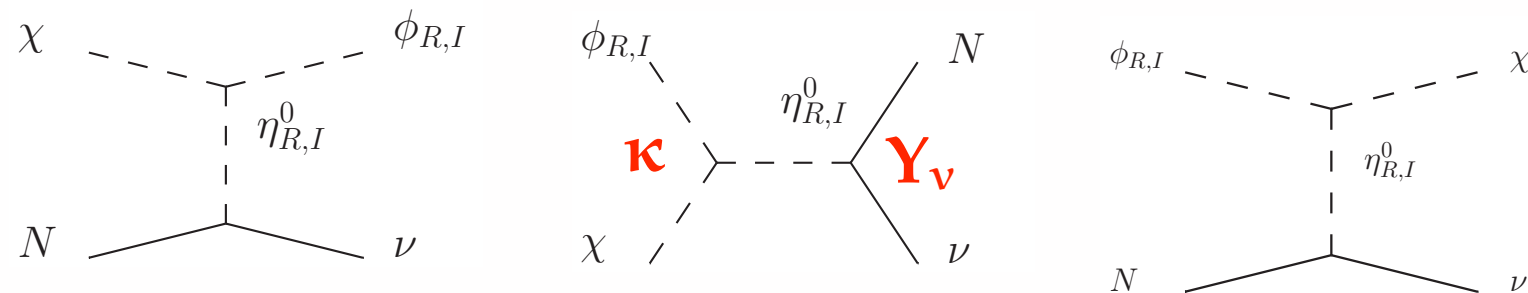
**Standard**



**DM Conversion:**

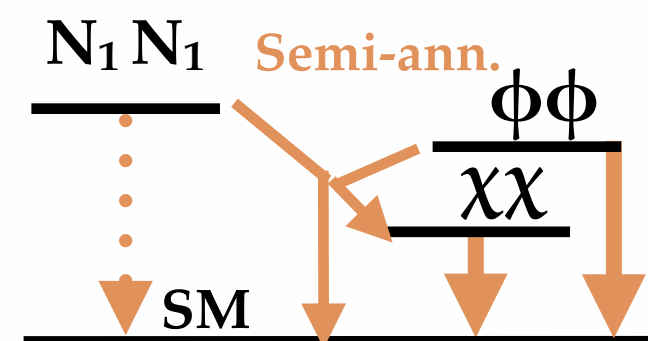


**Semi-annihilation:**



- In the Ma model, the  $\Omega_N h^2$  tends to be larger than 0.12. However, in this model, the contribution from the semi-annihilation can enhance the annihilation rate for  $N_R$ .

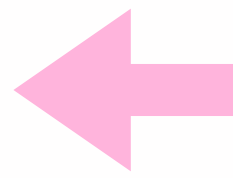
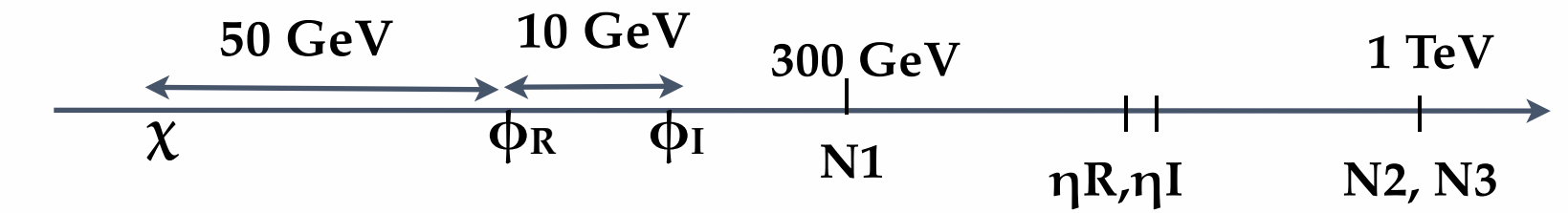
➔ **The tension between the constraints of LFV and  $\Omega_N h^2$  becomes mild.**



# Relic abundance

## Benchmark Point

$M_1$	300 GeV
$m_{\eta_R^0}$	$m_\chi + m_{\phi_R} - 10$ GeV
$m_{\phi_I}$	$m_\chi + 60$ GeV
$m_{\phi_R}$	$m_\chi + 50$ GeV
$\gamma \equiv \gamma_{2,5,7}$	0.1
$\kappa$	0.4

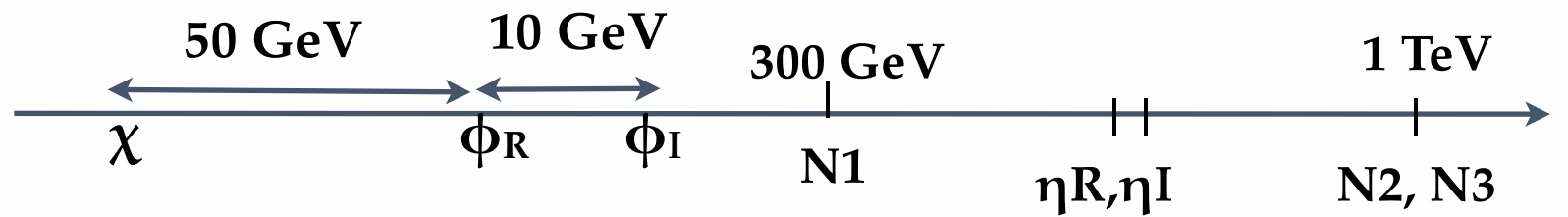


- Neutrino mass scale
- Vacuum stability
- Perturbativity  $|\lambda_i|, |\gamma_i|, |\kappa| < 1$

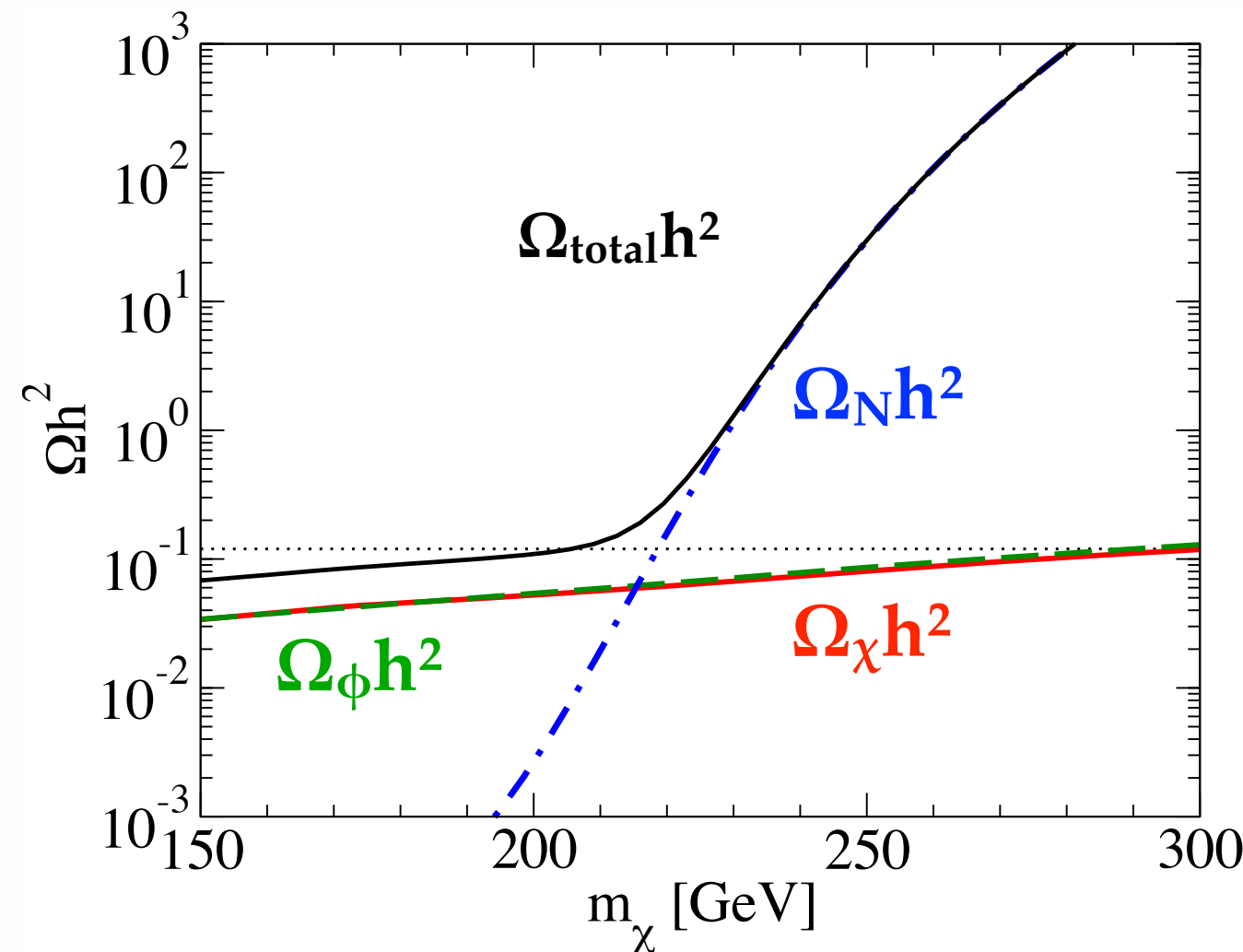
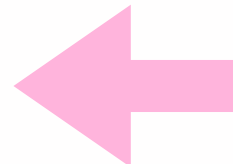
# Relic abundance

## Benchmark Point

$M_1$	300 GeV
$m_{\eta_R^0}$	$m_\chi + m_{\phi_R} - 10$ GeV
$m_{\phi_I}$	$m_\chi + 60$ GeV
$m_{\phi_R}$	$m_\chi + 50$ GeV
$\gamma \equiv \gamma_{2,5,7}$	0.1
$\kappa$	0.4



- Neutrino mass scale
- Vacuum stability
- Perturbativity  $|\lambda_i|, |\gamma_i|, |\kappa| < 1$



Semi-annihilation tends to decrease the relic density of the N DM.

-  $\gamma=0.1 \rightarrow m_\chi \sim 200$  GeV for  $\Omega h^2 \sim 0.12$  **Scalar DM**

-  $\gamma > 0.2 \rightarrow m_\chi \sim 220$  GeV **N DM**

-  $\gamma \sim 0.08 \rightarrow m_\chi \sim 150$  GeV **Scalar DM**

-  $m_\chi > 220$  GeV  $\rightarrow \Omega_N h^2 > 0.12$

# *Direct detection*

The current upper bound for the DM-nucleon cross section is estimated assuming the single component DM scenario.

→ Constraint on the detection rate in the multicomponent DM scenario.

effective cross section :  $\sigma_i^{\text{eff}} = \sigma_i \left( \frac{\Omega_i h^2}{\Omega_{\text{total}} h^2} \right)$

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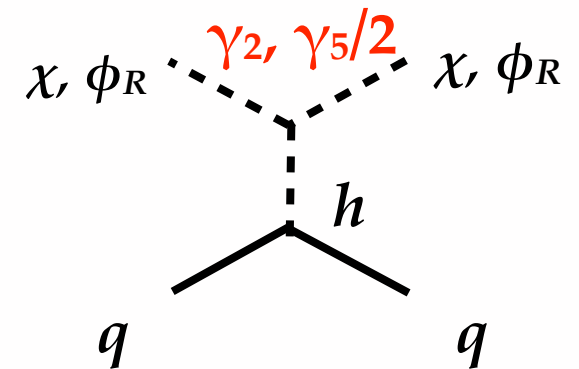
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Our model

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- $\chi$  and  $\phi_R$  have interactions to the quarks.
- The effective cross sections :

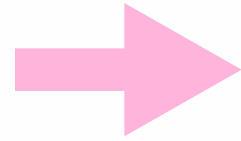
$$\sigma_{\phi_R}^{\text{eff}} = \sigma_{\phi_R} \left( \frac{\Omega_{\phi_R} h^2}{\Omega_{\text{tot}} h^2} \right) \quad \sigma_{\chi}^{\text{eff}} = \sigma_{\chi} \left( \frac{\Omega_{\chi} h^2}{\Omega_{\text{tot}} h^2} \right)$$





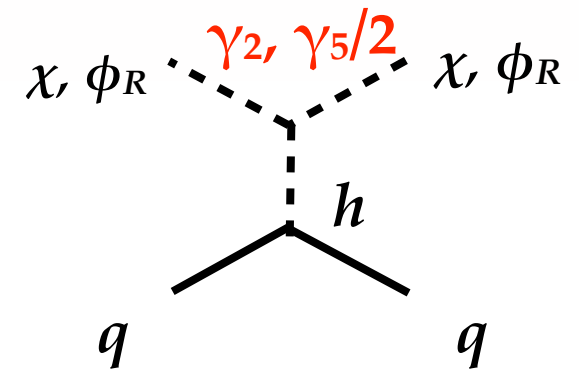
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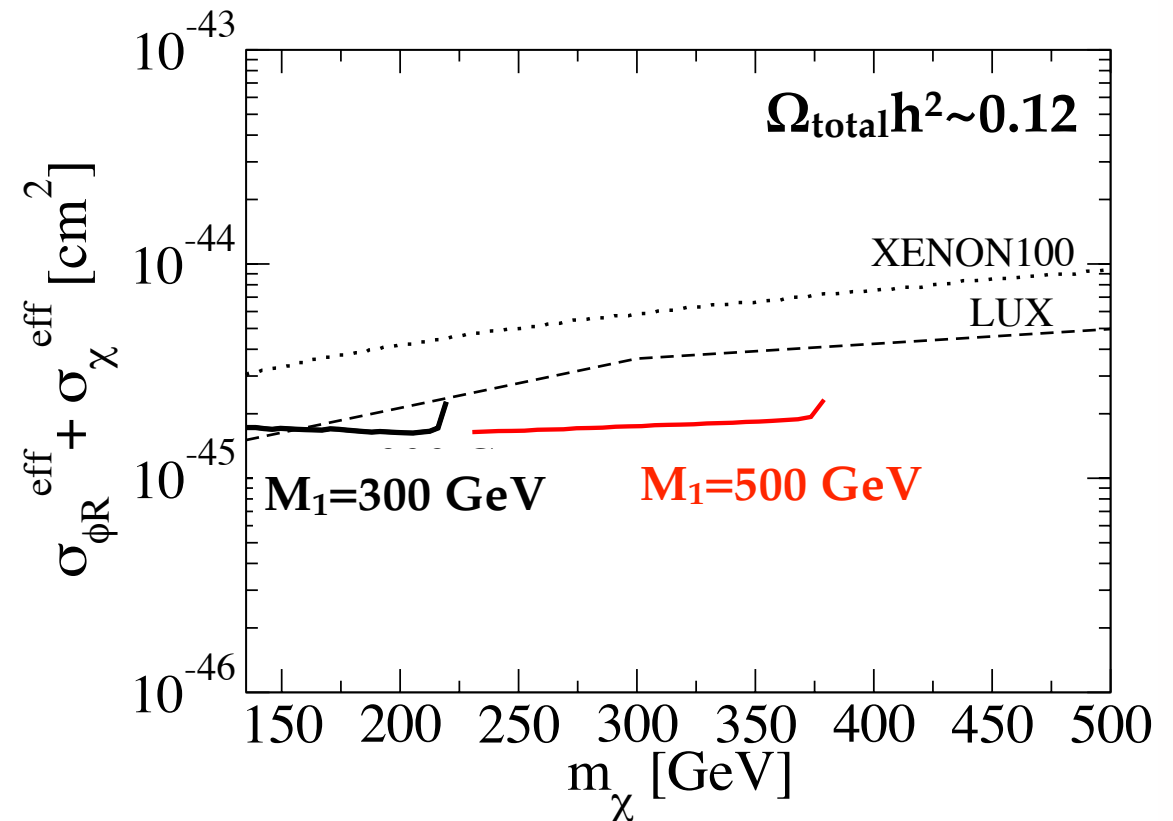


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- At  $m_{\chi}=220$  (380) GeV for  $M_1=300$  (500) GeV  
 $\rightarrow$  large  $\gamma$ , small  $\Omega_{\chi, \phi}$
- The obtained cross section is accessible to XENON1ton.

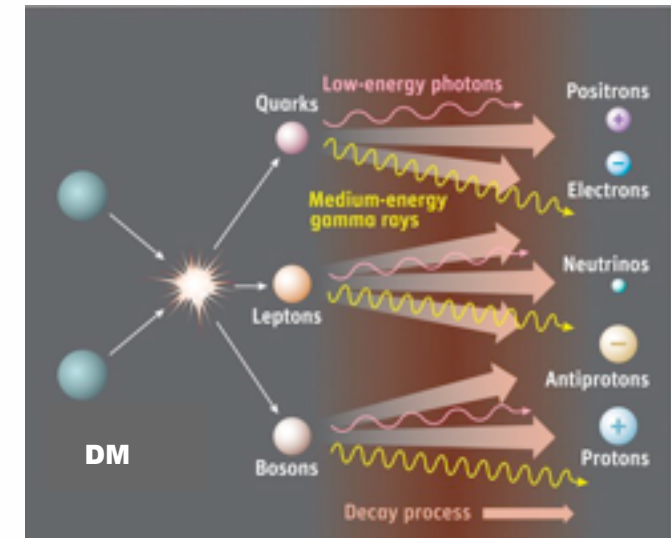


# Indirect detection

Cosmic ray from the DM annihilation.

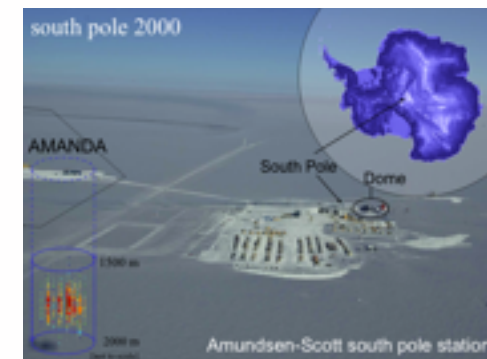
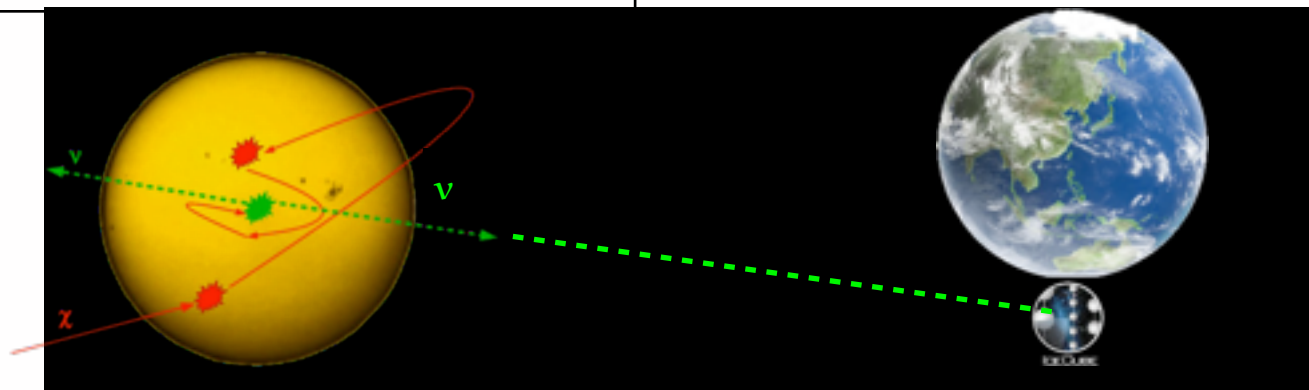


Indirect signals



We discuss the neutrinos from the annihilation of captured DM in the Sun.

Neutrino from the Sun



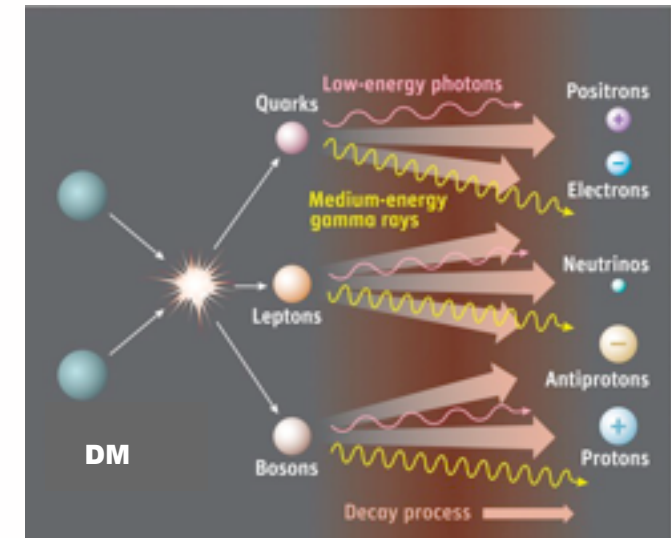
IceCUBE

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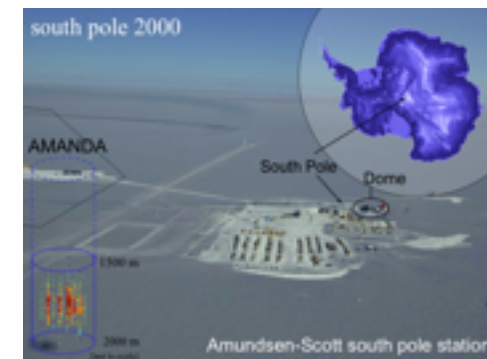
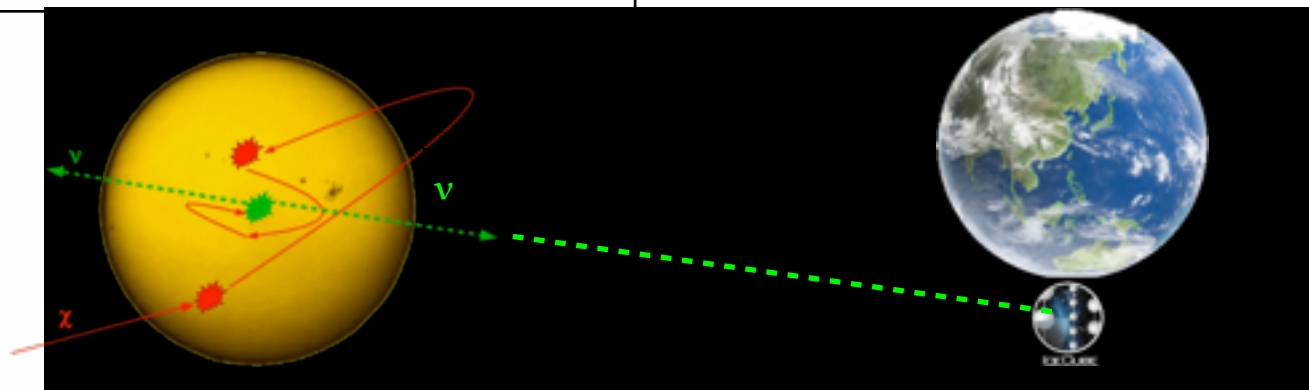


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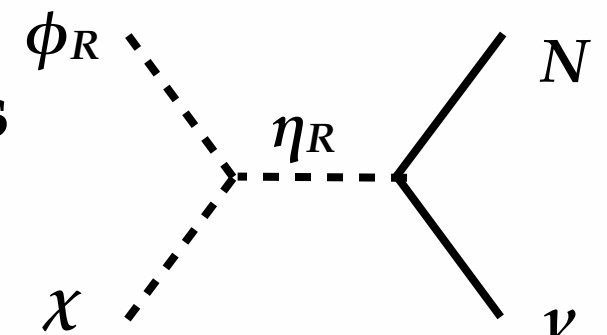
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Neutrino from the Sun



IceCUBE

In our model, the semi-annihilation process produces **a monochromatic neutrino.**

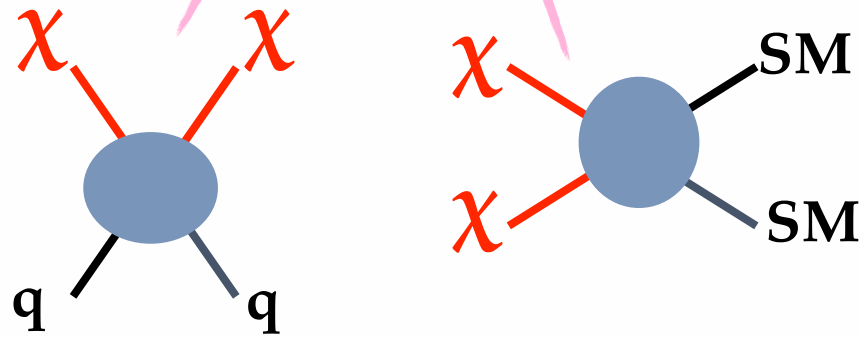


# Indirect detection

## Single component DM : $\chi$

- Time evolution of  $n_\chi$  in the Sun

$$\dot{n}_\chi = C - C_A n_\chi^2$$



$n_\chi$  : Number of DM in the Sun

$C$  : Capture rate in the Sun.

$C_A$  : Annihilation rate  $C_A = \langle \sigma v \rangle / V_{\text{eff}}$

$$C_A(\chi\chi \leftrightarrow XX') = \frac{\langle \sigma(\chi\chi \rightarrow XX')v \rangle}{V_{\text{eff}}}$$

$V_{\text{eff}}$  : Effective Volume of the Sun

$$V_{\text{eff}} = 5.7 \times 10^{27} \left( \frac{100 \text{ GeV}}{m_\chi} \right)^{3/2} \text{ cm}^3$$

- At the time of birth of the Sun the  $n_\chi$  were zero.
- The  $n_\chi$  increase with time and approach the fixed point values.

Fixed point at  $C = C_A n_\chi^2$

→ equilibrium → The number of DM reaches its **maximal** value.

- DM annihilation rate :  $\Gamma = C_A n_\chi^2 / 2 = C / 2$ .

- Neutrino production rate :  $\Gamma_\nu = \Gamma \text{ Br}(\chi\chi \rightarrow XX'\nu\nu)$

# Indirect detection

IceCube Collaboration  
Phys.Rev.Lett. 110 (2013) 13, 131302

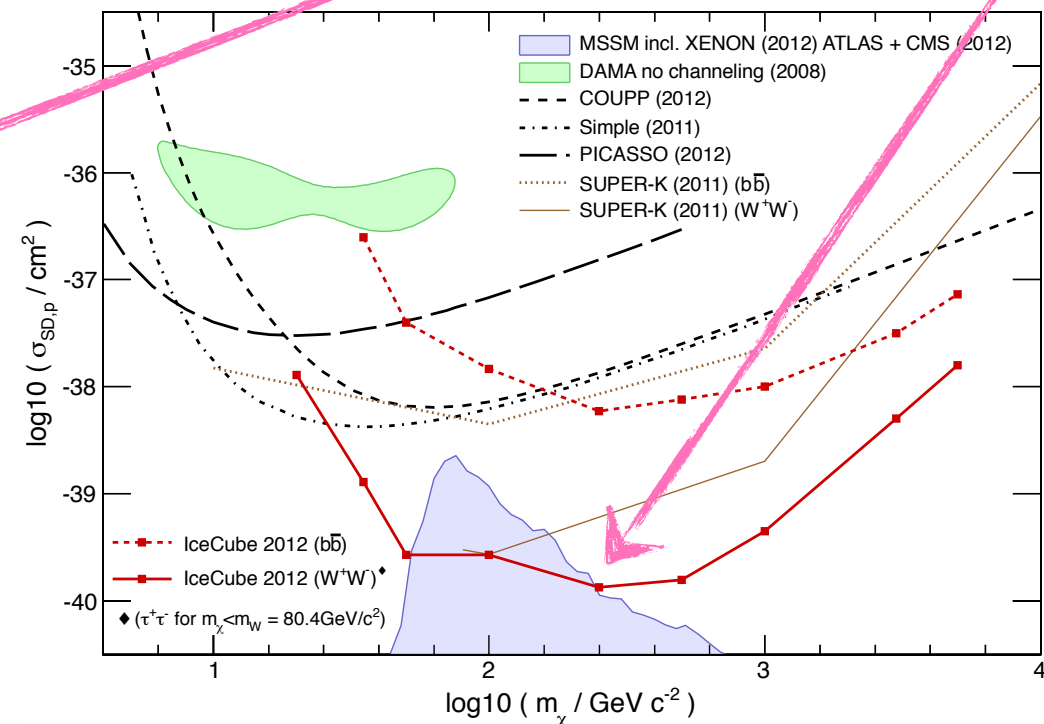
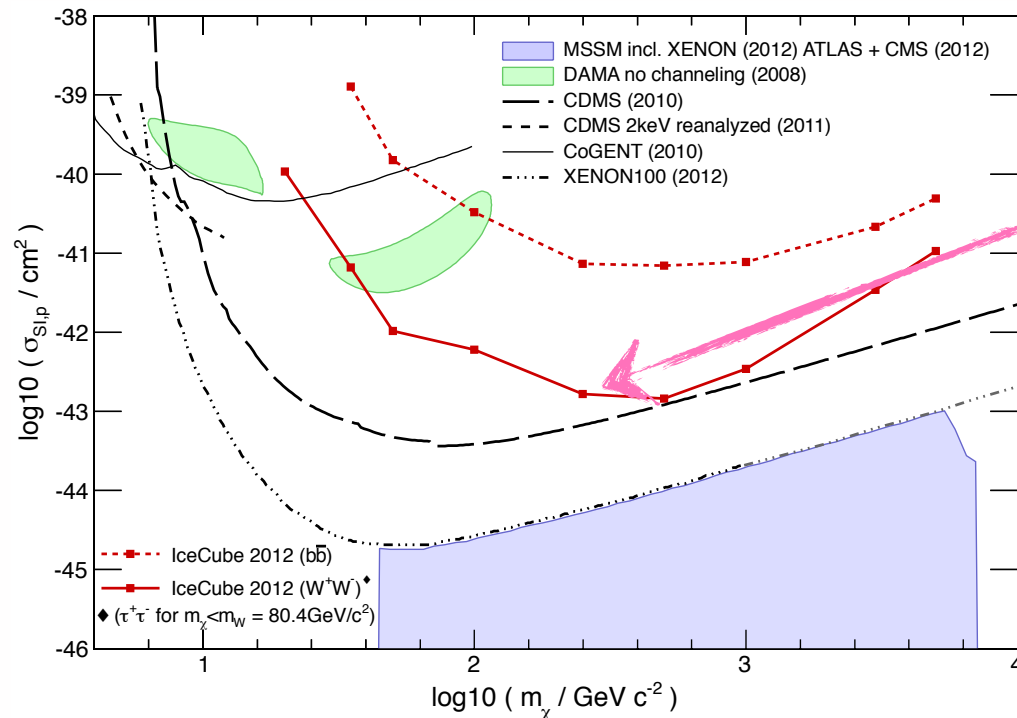
IceCUBE (2013)

## Neutralino DM

$$\chi\chi \rightarrow WW \rightarrow XX'vv$$

$m_\chi = 250 \text{ GeV}$  :

$m_\chi$ (GeV/c <sup>2</sup> )	Channel	$\Phi_\nu$ (km <sup>-2</sup> y <sup>-1</sup> )	$\sigma_{SI,p}$ (cm <sup>2</sup> )	$\sigma_{SD,p}$ (cm <sup>2</sup> )
20	$\tau^+\tau^-$	$2.35 \times 10^{15}$	$1.08 \times 10^{-40}$	$1.29 \times 10^{-38}$
35	$\tau^+\tau^-$	$1.02 \times 10^{14}$	$6.59 \times 10^{-42}$	$1.28 \times 10^{-39}$
35	$b\bar{b}$	$6.29 \times 10^{15}$	$1.28 \times 10^{-39}$	$2.49 \times 10^{-37}$
50	$\tau^+\tau^-$	$1.17 \times 10^{13}$	$1.03 \times 10^{-42}$	$2.70 \times 10^{-40}$
50	$b\bar{b}$	$5.64 \times 10^{14}$	$1.51 \times 10^{-40}$	$3.96 \times 10^{-38}$
100	$W^+W^-$	$1.23 \times 10^{12}$	$6.01 \times 10^{-43}$	$2.68 \times 10^{-40}$
100	$b\bar{b}$	$6.34 \times 10^{13}$	$3.30 \times 10^{-41}$	$1.47 \times 10^{-38}$
250	$W^+W^-$	$9.72 \times 10^{10}$	$1.67 \times 10^{-43}$	$1.34 \times 10^{-40}$
250	$b\bar{b}$	$4.59 \times 10^{12}$	$7.37 \times 10^{-42}$	$5.90 \times 10^{-39}$



# Indirect detection

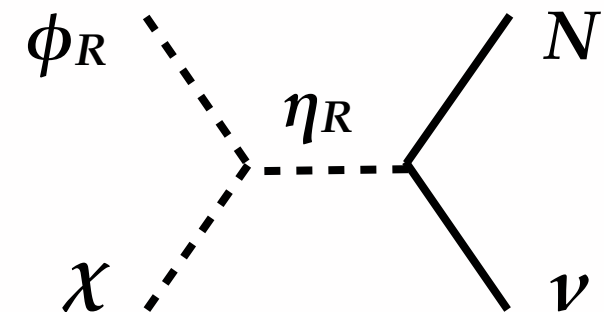
Multicomponent DM :  $\phi_R, \chi, N_R$

$$\dot{n}_i = C_i - \underbrace{C_A(ii \rightarrow \text{SM})n_i^2}_{\text{Standard}} - \sum_{m_i > m_j} \underbrace{C_A(ii \rightarrow jj)n_i^2}_{\text{Conversion}} - \underbrace{C_A(ij \rightarrow k\nu)n_i n_j}_{\text{Semi-annihilation}}$$

- Since  $C_N=0$ , the  $n_N$  cannot increase.
- $\phi\chi \rightarrow N\nu$  is the only  $\nu$  production process.
- Monochromatic  $\nu$  production rate :

$$\Gamma_\nu = C_A(\chi\phi \rightarrow N_R^c\nu)n_\chi n_\phi$$

- Neutrino flux :  $\Phi_\nu = \Gamma_\nu / (4\pi R^2)$   
 $R$ : the distance to the Sun





# Indirect detection

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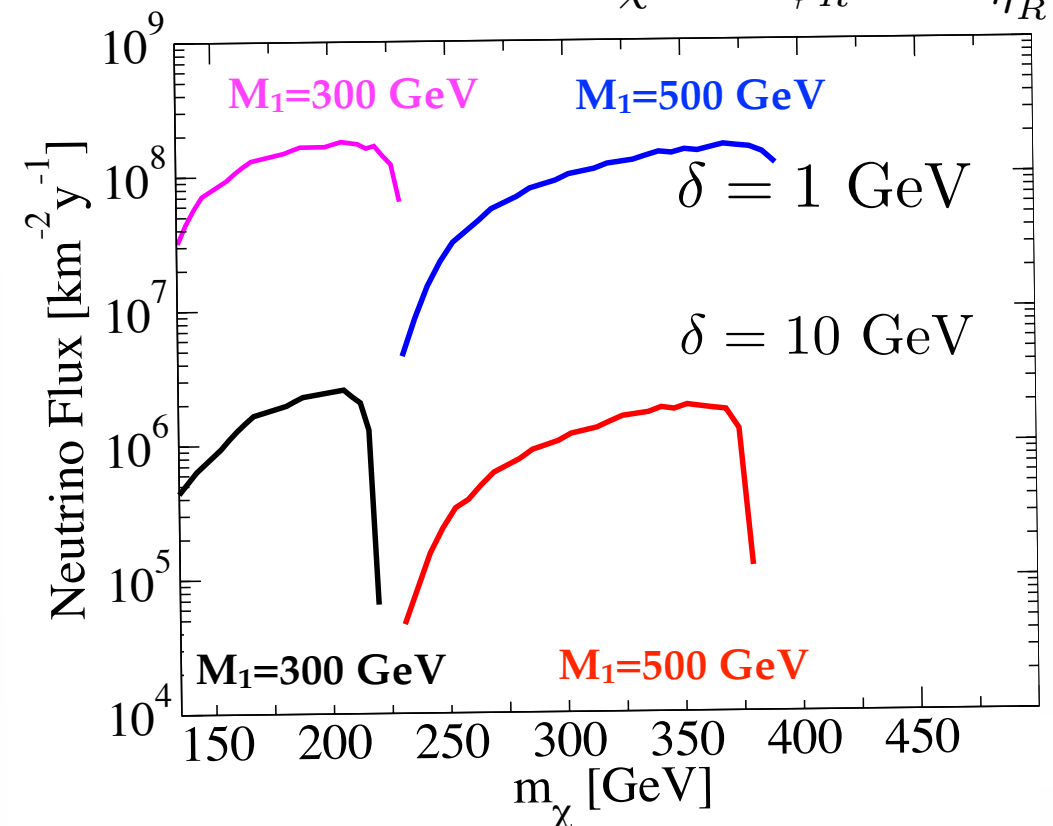
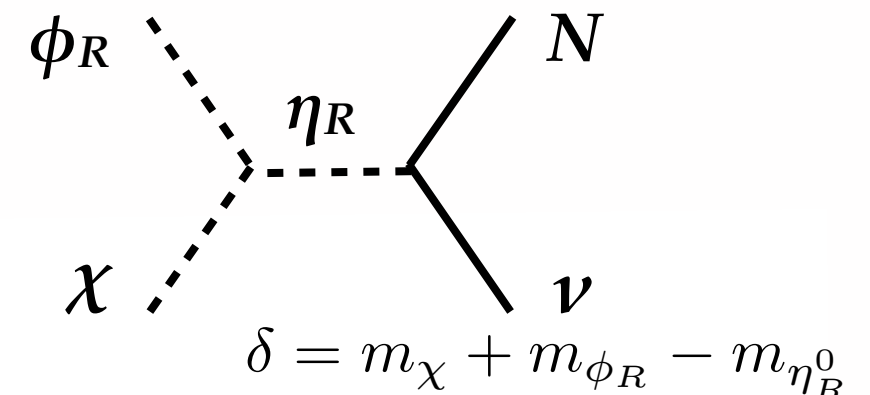
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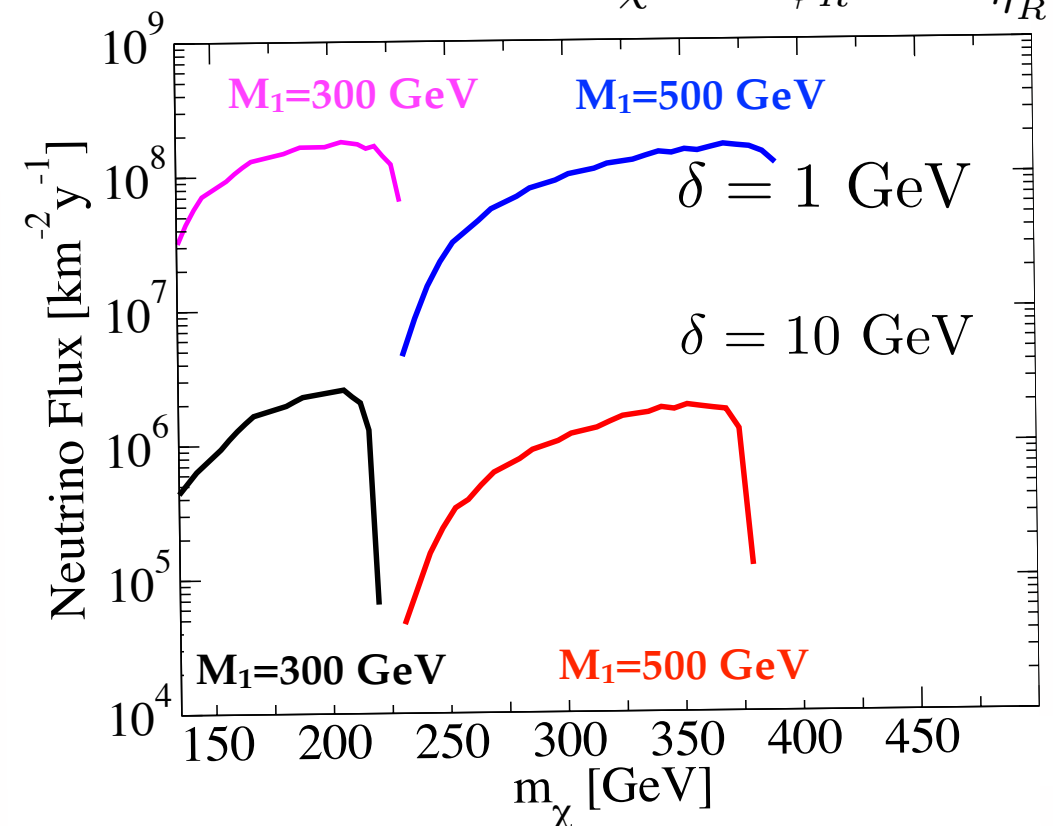
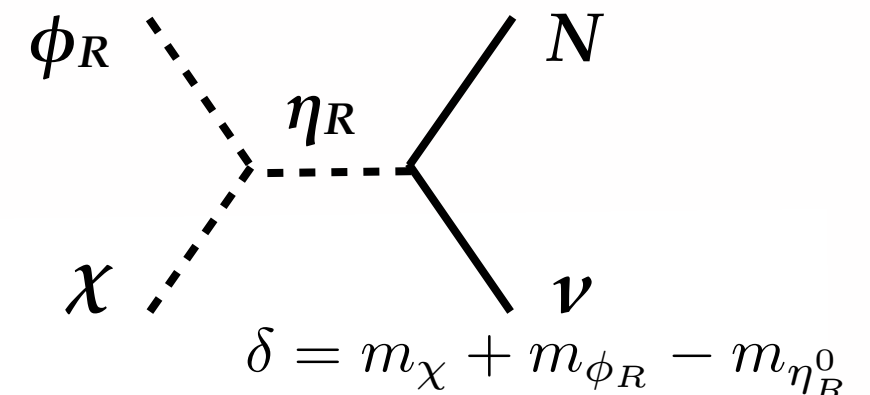
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- When  $\delta=1\text{GeV}$ , the larger neutrino flux can be obtained.
- The IceCUBE limit is at least  $10^3$  times larger than these results.



# Summary

We have proposed the radiative seesaw model with multicomponent DM system.

**Two-loop extension of Ma model with  $Z_2 \times Z_2$  symmetry.**

- The small  $\lambda_5$  coupling is realized by the radiative correction.

**Three-component  $(N, \chi, \phi_R)$  DM system.**

- $\Omega_N h^2$  is reduced by the semi-annihilation processes.
- For the direct detection, the predicted value will be covered by XENON1T.
- The monochromatic neutrino is produced by the semi-annihilation.
- The neutrino flux from the Sun is enhanced by the resonant effect. However, the flux is very small compared with the IceCUBE sensitivity.

**Thank you for your attention.**