

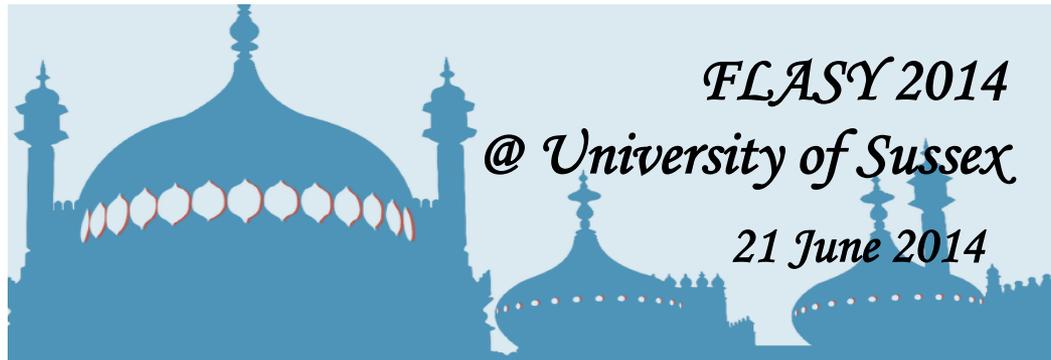
Squark flavor mixing in B decays

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Based on: [arXiv:1404.0520](https://arxiv.org/abs/1404.0520) with M. Tanimoto (Niigata Univ.)

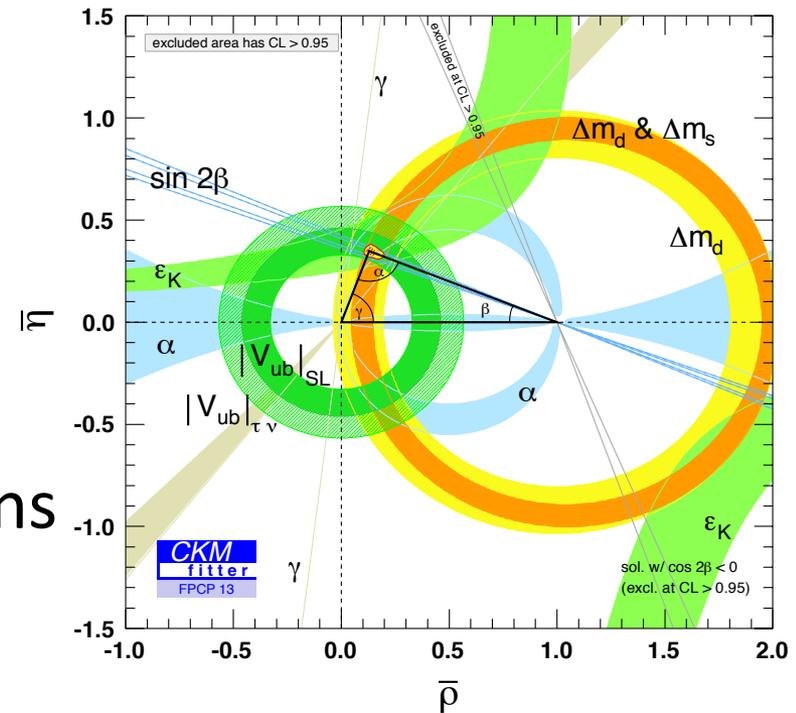


1. Introduction

- Higgs Discovery 2012 $m_H \simeq 126\text{GeV}$
- No evidence of SUSY
SUSY scale may be much higher than 1 TeV
- We need indirect Search for SUSY
 ➔ Flavor physics

1. Introduction

- SM explains CP violation of K and B mesons successfully
- No significant deviation, but
 - a number of tensions
 - future measurements can improve a lot
- $\mathcal{O}(20\%)$ New Physics contributions to loop processes are still possible



We examine the sensitivity of **High Scale SUSY** in the **CP violations of K and B mesons**

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2. Squark Mass Spectrum

**3. CP violations of K and B
chromo-EDM of strange quark**

4. Summary

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2. Squark Mass Spectrum

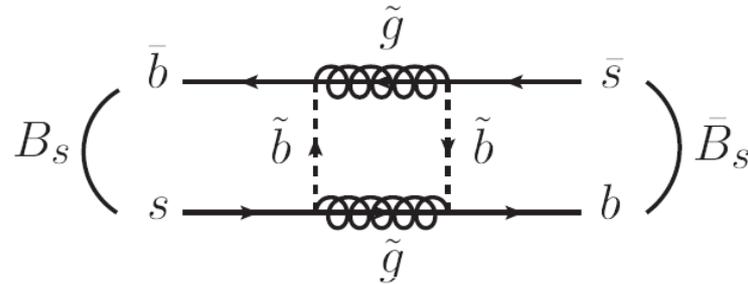
3. CP violations of K and B
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2. Squark Mass Spectrum

- We consider **squark-gluino interactions** in B meson system

Ex) ΔM_s



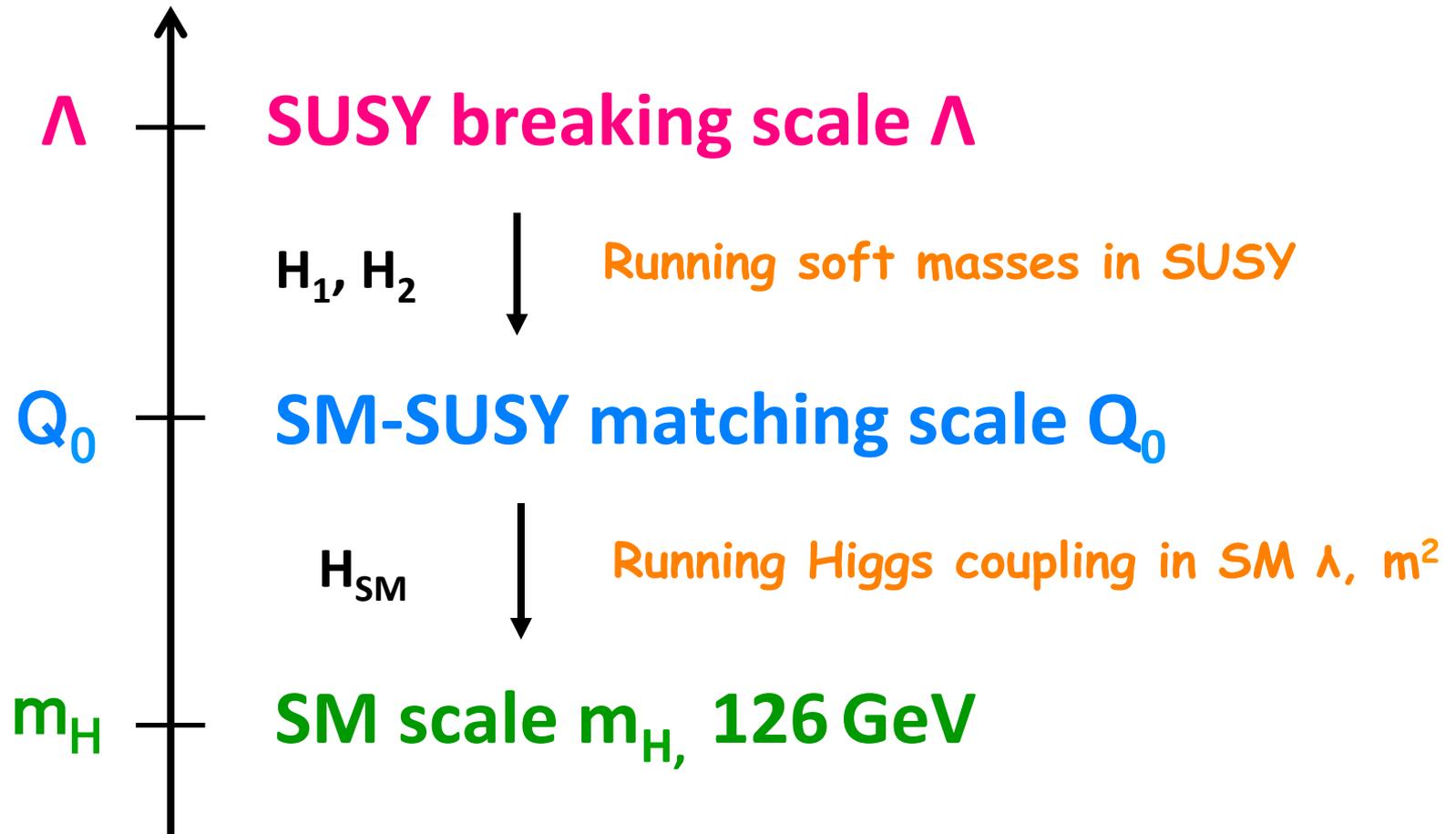
which depends on the squark and gluino mass spectrum

◇ SUSY-GIM works

◇ Left-right mixing of sbottom is important

◇ Loop functions depend on sbottom-gluino mass ratio

We should consider SUSY particle spectrum, which is consistent with Higgs Discovery.



The quadratic terms in the MSSM potential

Λ

$$V_2 = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 + m_3^2 (H_1 \cdot H_2 + h.c.)$$

$$m_1^2 = m_{H_1}^2 + |\mu|^2 \quad m_2^2 = m_{H_2}^2 + |\mu|^2$$

$$m_{\pm}^2 = \frac{m_1^2 + m_2^2}{2} \pm \sqrt{\left(\frac{m_1^2 - m_2^2}{2}\right)^2 + m_3^2}$$

Q_0

Below Q_0 scale, SM

$$V_{\text{SM}} = -m^2 |H|^2 + \frac{\lambda}{2} |H|^4$$

We put the matching condition

$$m_-^2 = -m^2(Q_0) \quad \text{and} \quad m_+^2 = m_1^2 + m_2^2 + m^2 \equiv m_{\mathcal{H}}^2$$

by the fixing $m_3^4 = (m_1^2 + m^2)(m_2^2 + m^2)$

Q_0

$$m^2 = \frac{m_1^2 - m_2^2 \tan^2 \beta}{\tan^2 \beta - 1}$$

$$\lambda = \frac{1}{4} (g^2 + g'^2) \cos^2 2\beta + \frac{3h_t^2}{8\pi^2} X_t^2 \left(1 - \frac{X_t^2}{12} \right)$$

$$m_{\mathcal{H}}^2 = Q_0^2$$

$$\mu(Q_0) = Q_0$$

$$X_t = \frac{A_t(Q_0) - \mu(Q_0) \cot \beta}{Q_0}$$

RGE's

SM Higgs	$H = \cos \beta H_1 + \sin \beta \tilde{H}_2$
Heavy Higgs	$\mathcal{H} = -\sin \beta H_1 + \cos \beta \tilde{H}_2$

m_H

$$m_H^2 = \lambda(m_H) v^2 = 2m^2(m_H), \quad v = 246 \text{ GeV}$$

(126 GeV)²

$$\left(\begin{array}{l} \text{where} \quad \langle H_1 \rangle = v_d = v \cos \beta \\ \quad \quad \langle H_2 \rangle = v_u = v \sin \beta \end{array} \Rightarrow \begin{array}{l} \langle H \rangle = v \\ \langle \mathcal{H} \rangle = 0 \end{array} \right)$$

- Taking universal soft parameters at SUSY breaking scale Λ (gravity mediated-like model)

$$m_{\tilde{Q}_i}^2(\Lambda) = m_{\tilde{U}_i^c}^2(\Lambda) = m_{\tilde{D}_i^c}^2(\Lambda) = m_0^2 \quad (i = 1, 2, 3) ,$$

$$M_1(\Lambda) = M_2(\Lambda) = M_3(\Lambda) = m_{1/2} ,$$

$$m_{H_1}^2(\Lambda) = m_{H_2}^2(\Lambda) = m_0^2 ,$$

$$A_U(\Lambda) = A_0 y_U(\Lambda), \quad A_D(\Lambda) = A_0 y_D(\Lambda), \quad A_E(\Lambda) = A_0 y_E(\Lambda).$$

6 parameters taking with $\mu = Q_0$

$\Lambda, Q_0, \tan\beta, m_0, m_{1/2}, A_0$

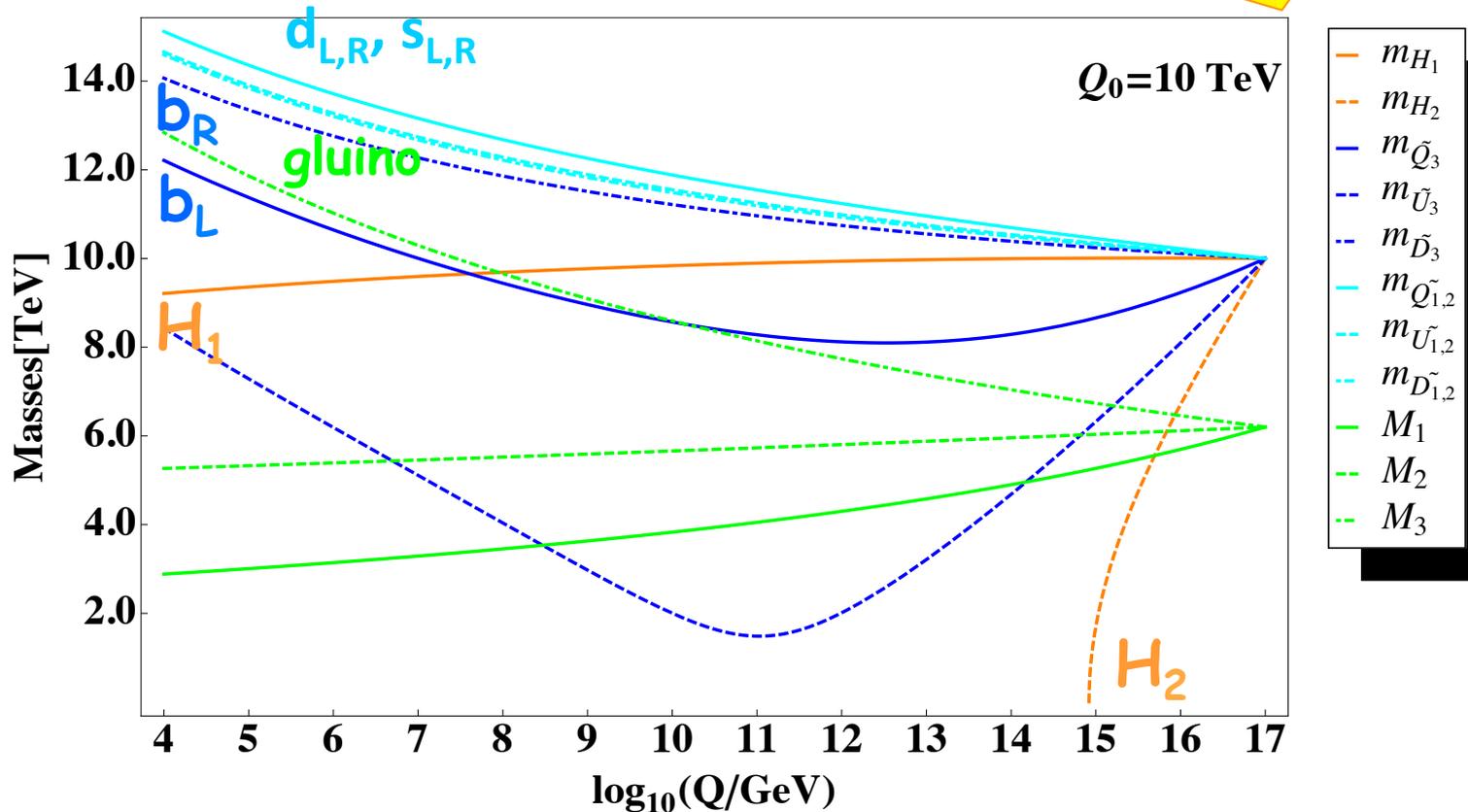
- We tune $m_{1/2}$ and A_t to give $m_H = 126$ GeV

$$Q_0 = 10 \text{ TeV} \quad \Lambda = 10^{17} \text{ TeV}$$

RGE running

at $Q_0 = 10$ TeV,
 $\mu = 10$ TeV,
 $\tan \beta = 10$

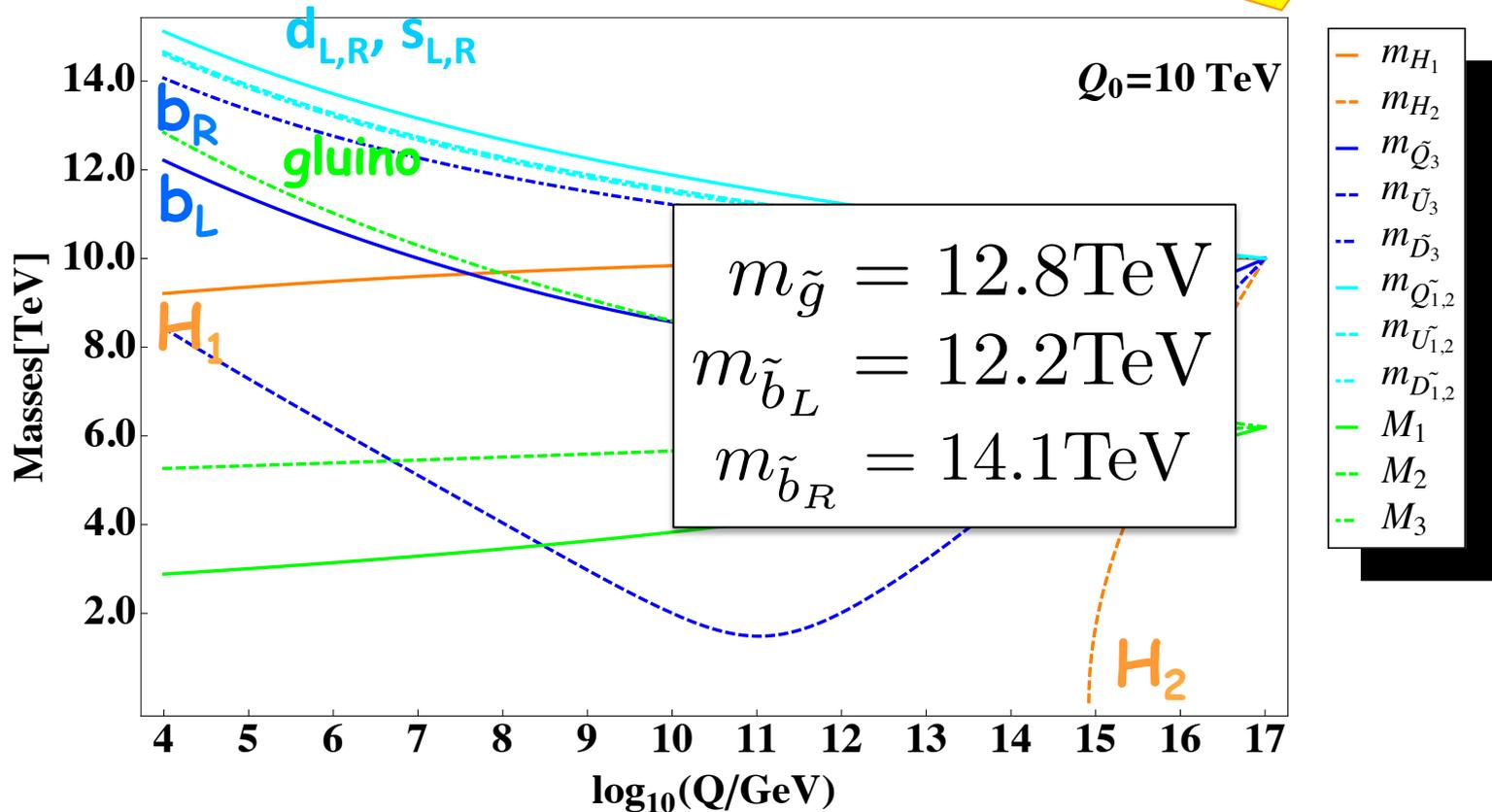
at $\Lambda = 10^{17}$ GeV,
 $m_0 = 10$ TeV,
 $m_{1/2} = 6.2$ TeV,
 $A_0 = 25.803$ TeV;



RGE running

at $Q_0 = 10$ TeV,
 $\mu = 10$ TeV,
 $\tan \beta = 10$

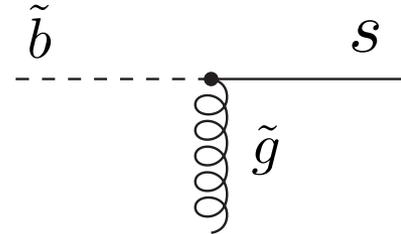
at $\Lambda = 10^{17}$ GeV,
 $m_0 = 10$ TeV,
 $m_{1/2} = 6.2$ TeV,
 $A_0 = 25.803$ TeV;



Squark flavor mixing

- The gluino-squark-quark interaction

$$\mathcal{L}_{\text{int}}(\tilde{g}q\tilde{q}) = -i\sqrt{2}g_s \sum_{\{q\}} \tilde{q}_i^* (T^a) \overline{\tilde{G}}^a \left[(\Gamma_{GL}^{(q)})_{ij} \mathbf{L} + (\Gamma_{GR}^{(q)})_{ij} \mathbf{R} \right] q_j + \text{h.c.}$$



Rotation matrix :

$$\Gamma_{GL}^{(d)} = \begin{pmatrix} c_{13}^L & 0 & s_{13}^L e^{-i\phi_{13}^L} c_\theta & 0 & 0 & -s_{13}^L e^{-i\phi_{13}^L} s_\theta e^{i\phi} \\ -s_{23}^L s_{13}^L e^{i(\phi_{13}^L - \phi_{23}^L)} & c_{23}^L & s_{23}^L c_{13}^L e^{-i\phi_{23}^L} c_\theta & 0 & 0 & -s_{23}^L c_{13}^L e^{-i\phi_{23}^L} s_\theta e^{i\phi} \\ -s_{13}^L c_{23}^L e^{i\phi_{13}^L} & -s_{23}^L e^{i\phi_{23}^L} & c_{13}^L c_{23}^L c_\theta & 0 & 0 & -c_{13}^L c_{23}^L s_\theta e^{i\phi} \end{pmatrix} \quad \mathbf{q}_L$$

6 squarks

$$\Gamma_{GR}^{(d)} = \begin{pmatrix} 0 & 0 & s_{13}^R s_\theta e^{-i\phi_{13}^R} e^{-i\phi} & c_{13}^R & 0 & s_{13}^R e^{-i\phi_{13}^R} c_\theta \\ 0 & 0 & s_{23}^R c_{13}^R s_\theta e^{-i\phi_{23}^R} e^{-i\phi} & -s_{13}^R s_{23}^R e^{i(\phi_{13}^R - \phi_{23}^R)} & c_{23}^R & s_{23}^R c_{13}^R e^{-i\phi_{23}^R} c_\theta \\ 0 & 0 & c_{13}^R c_{23}^R s_\theta e^{-i\phi} & -s_{13}^R c_{23}^R e^{i\phi_{13}^R} & -s_{23}^R e^{i\phi_{23}^R} & c_{13}^R c_{23}^R c_\theta \end{pmatrix} \quad \mathbf{q}_R$$

- 1st and 2nd family squarks are degenerate: $s_{12}=0$

- Parameters

Setup

$$\text{Mixing parameter: } s_{23}^L, s_{23}^R, s_{13}^L, s_{13}^R \longrightarrow |s_{23}^L| = |s_{23}^R| \quad |s_{13}^L| = |s_{13}^R|$$

Phase: ϕ

Left-Right mixing angle: θ

Left-Right mixing angle θ

- Remark:

Dominant contributions of C_{8G} , $C_{7\gamma}$ and cEDM come from Left-Right mixing θ

$$M_{\tilde{q}}^2 = \begin{pmatrix} m_{\tilde{d}_L}^2 & m_b(A_b - \mu \tan\beta) \\ m_b(A_b - \mu \tan\beta) & m_{\tilde{d}_R}^2 \end{pmatrix} \quad \text{Third family}$$

$$\tan 2\theta = \frac{2m_b(A_b - \mu \tan\beta)}{m_{\tilde{d}_L}^2 - m_{\tilde{d}_R}^2}$$

$$\theta = 0.35^\circ$$

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Our strategy

$\Delta F=2$: Mixing

K meson

$$|\epsilon_K|$$

$\Delta F=1$: Time dependent CP asymmetry

B meson

$$\Delta M_d$$
$$S_{J/\psi K_S}$$
$$S_{\phi K_S}, S_{\eta' K^0}$$
$$a_{sl}^d$$

Bs meson

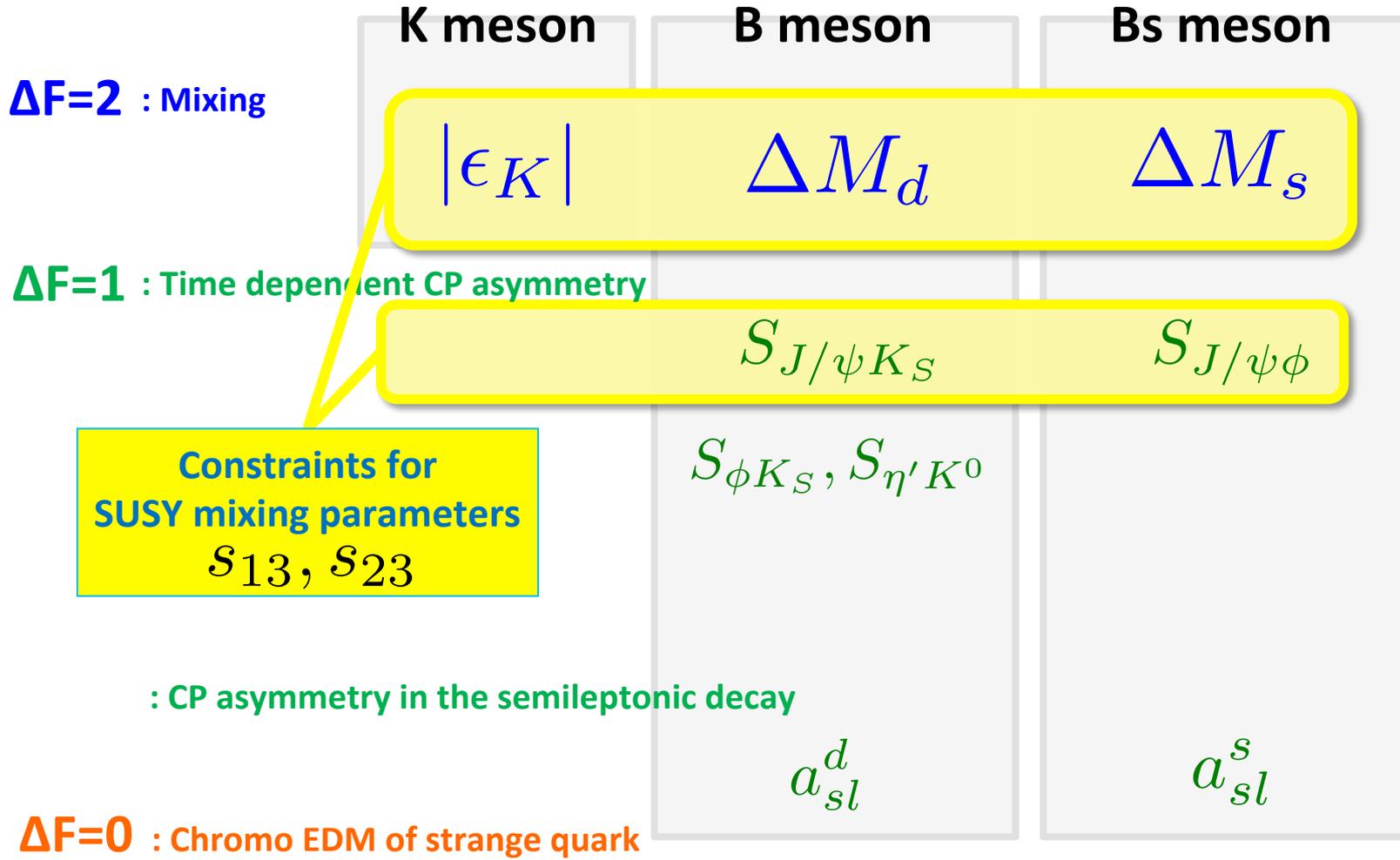
$$\Delta M_s$$
$$S_{J/\psi\phi}$$
$$a_{sl}^s$$

: CP asymmetry in the semileptonic decay

$\Delta F=0$: Chromo EDM of strange quark

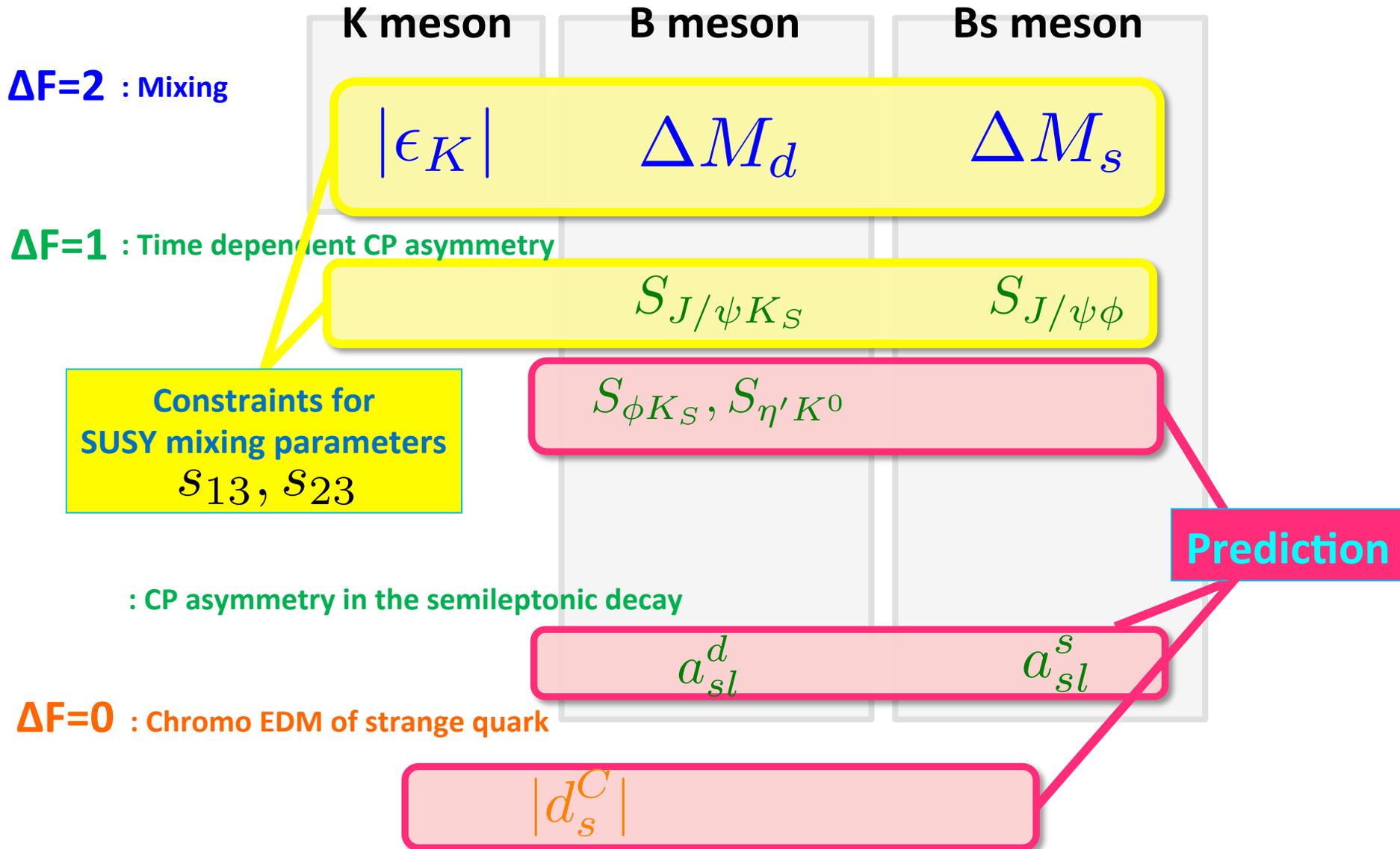
$$|d_s^C|$$

Our strategy

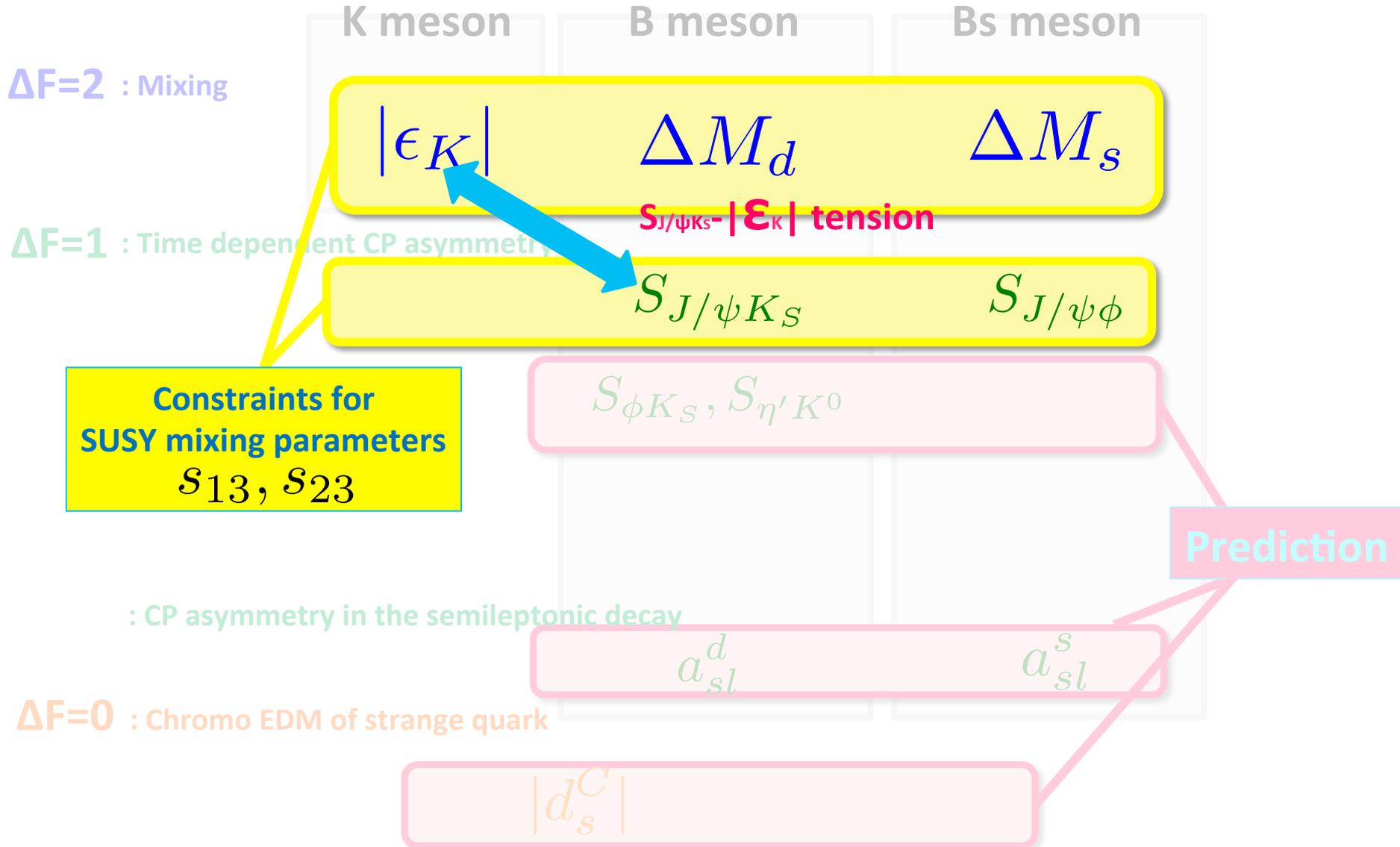


$$|d_s^C|$$

Our strategy



Our strategy



$S_{J/\psi K_S} - |\epsilon_K|$ tension

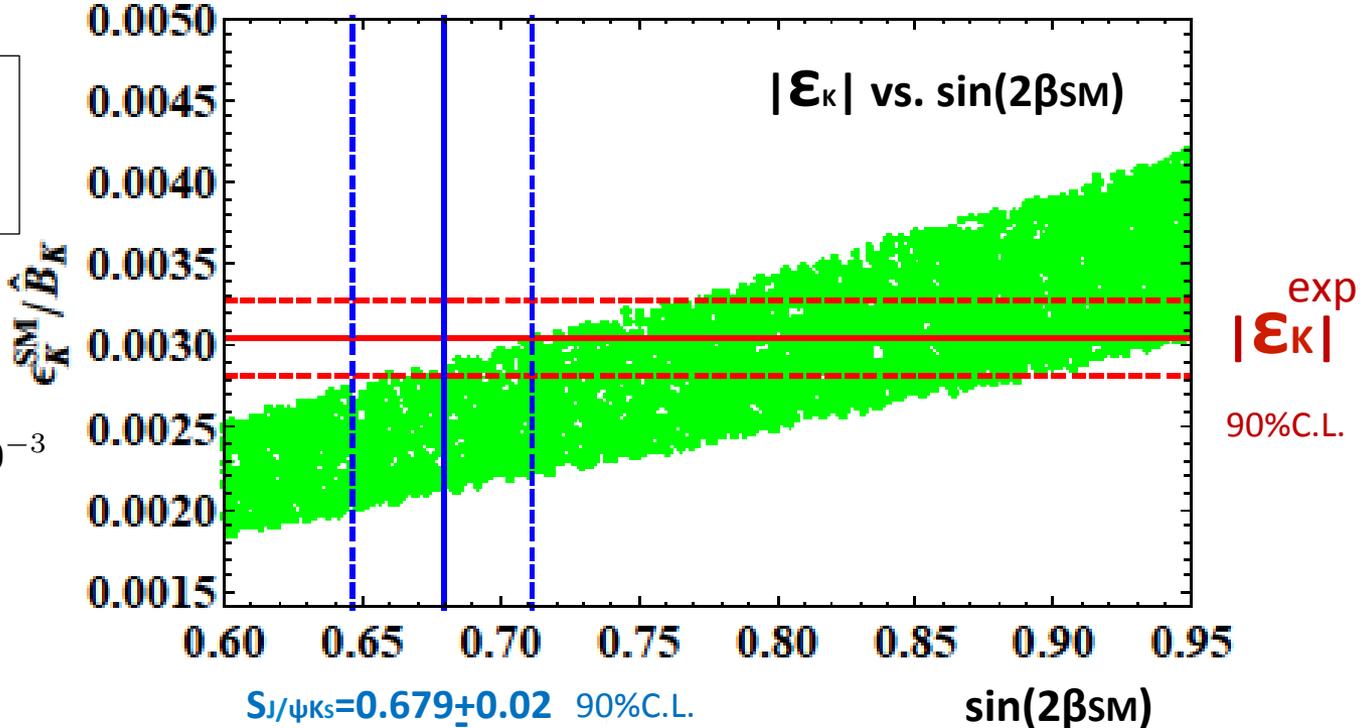
[Andrzej J. Buras and Diego Guadagnoli ,2008]
[Andrzej J. Buras ,2011]

- $|\epsilon_K|$ is given in terms of $\sin(2\beta)$ because there is only one CP violating phase in the SM.

SM $|\epsilon_K| \propto \hat{B}_K |V_{cb}|^4 \sin(2\beta_{SM})$ $S_{J/\psi K_S} = \sin(2\beta_{exp}) = \sin(2\beta_{SM})$

B_K : Lattice calculation
 $\hat{B}_K = 0.73 \pm 0.03$
[JM.Gerard, 2011]

$|\epsilon_K^{exp}| = (2.228 \pm 0.011) \times 10^{-3}$



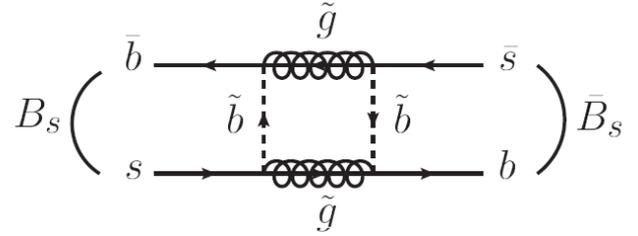
- It is noticed that the consistency between the SM prediction and the experimental data in $\sin(2\beta)$ and $|\epsilon_K^{SM}|/\hat{B}_K$ is marginal.

Constraints

K- \bar{K} , B- \bar{B} , Bs- \bar{B}_s mixing: $|\epsilon_K|$ ΔM_d ΔM_s

$$M_{12}^q = \langle B_q | H_{\text{eff}} | \bar{B}_q \rangle = M_{12}^{q,\text{SM}} + M_{12}^{q,\text{SUSY}}$$

$$\Delta M_d = 2 |M_{12}^d| \quad \epsilon_K \propto \text{Im}(M_{12}^K)$$

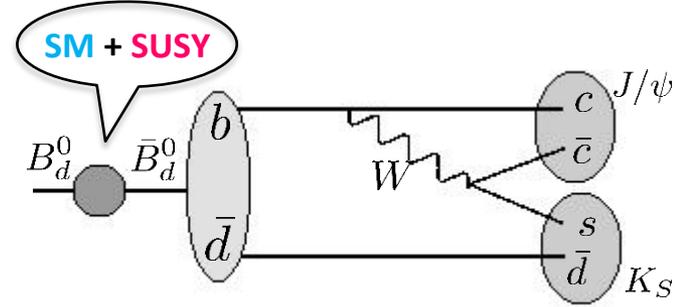


$$|\epsilon_K| \propto s_{13}s_{23} \quad \Delta M_d \propto s_{13} \quad \Delta M_s \propto s_{23}$$

Time dependent CP asymmetry : $S_{J/\psi K_S}$ $S_{J/\psi \phi}$

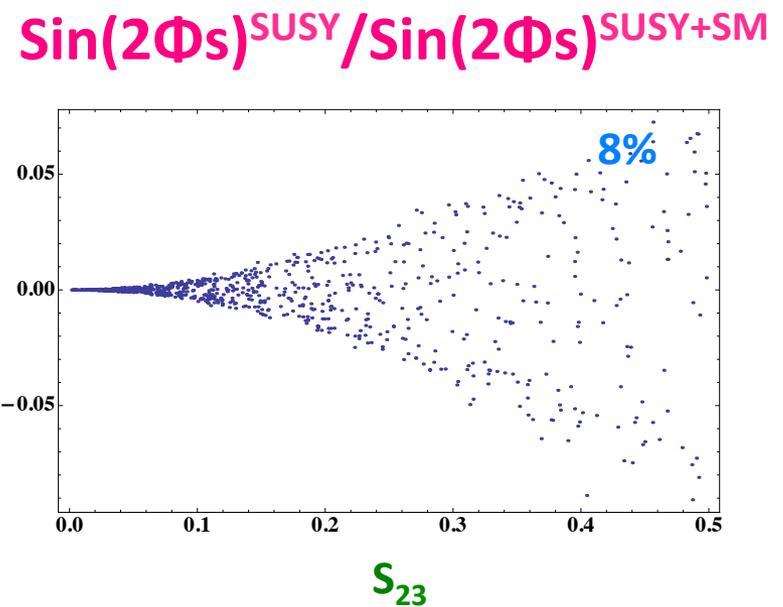
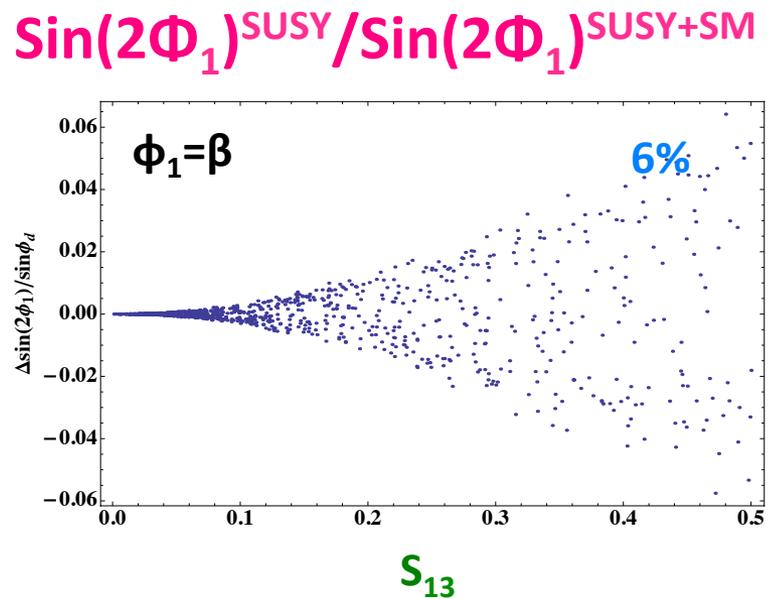
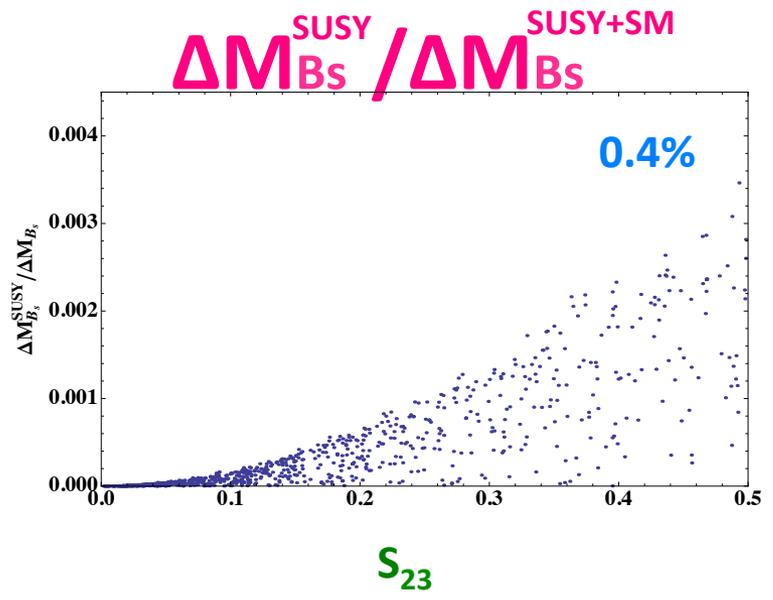
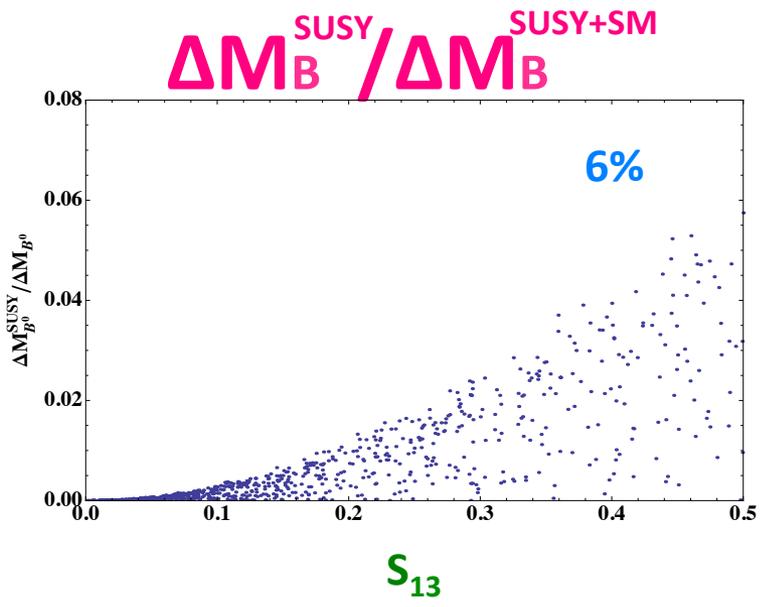
$$S_{J/\psi K_S} \rightarrow \sin(2\beta_{\text{SM}} + \text{Arg}(1 + \left| \frac{M_{12}^{\text{SM}}}{M_{12}^{\text{SUSY}}} \right| e^{2i\sigma}))$$

$$S_{J/\psi \phi} \rightarrow \sin(-2\beta_{s,\text{SM}} + \text{Arg}(1 + \left| \frac{M_{s,12}^{\text{SM}}}{M_{s,12}^{\text{SUSY}}} \right| e^{2i\sigma_s}))$$

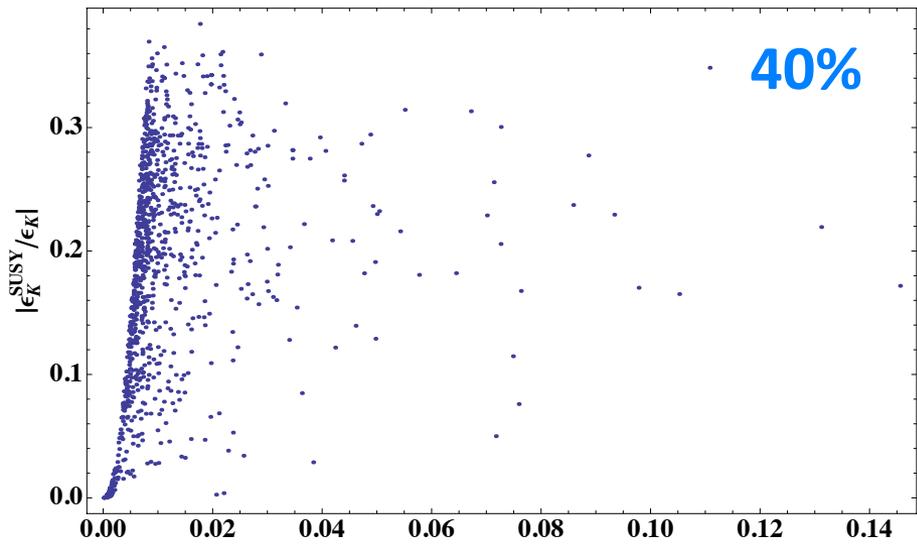


$$S_{J/\psi K_S} \propto s_{13} \quad S_{J/\psi \phi} \propto s_{23}$$

We scan s_{ij} randomly in the region of $0 \sim 0.5$ with taking $|s_{ij}^L| = |s_{ij}^R|$



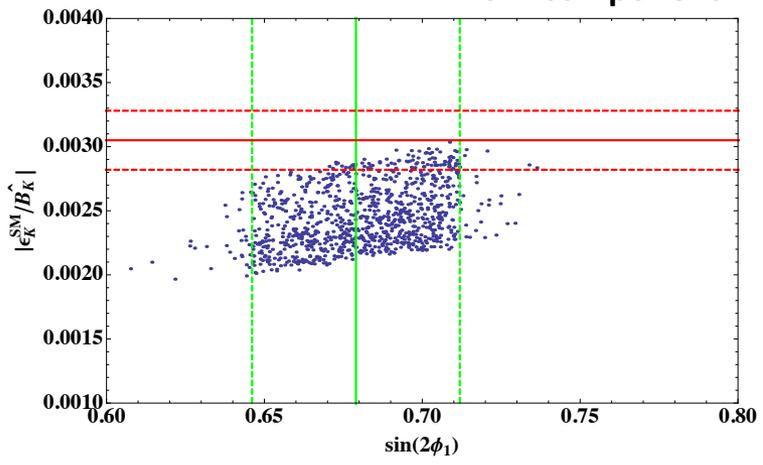
SUSY / SUSY+SM
 ϵ_K / ϵ_K



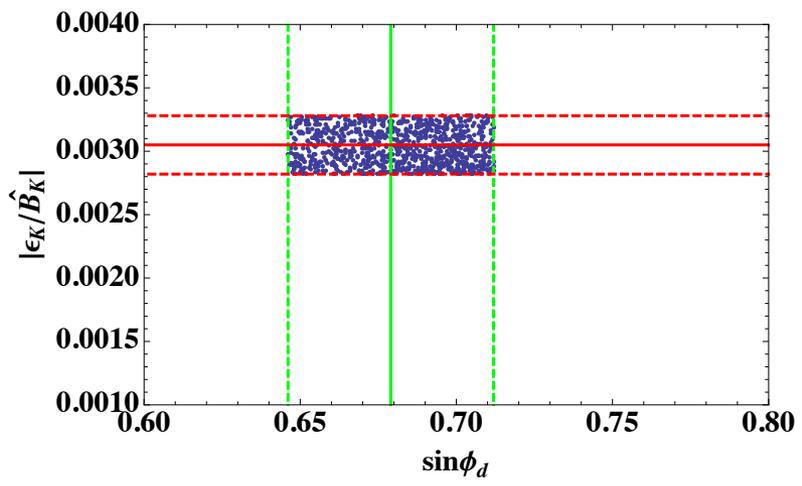
sensitive

$S_{13}S_{23}$

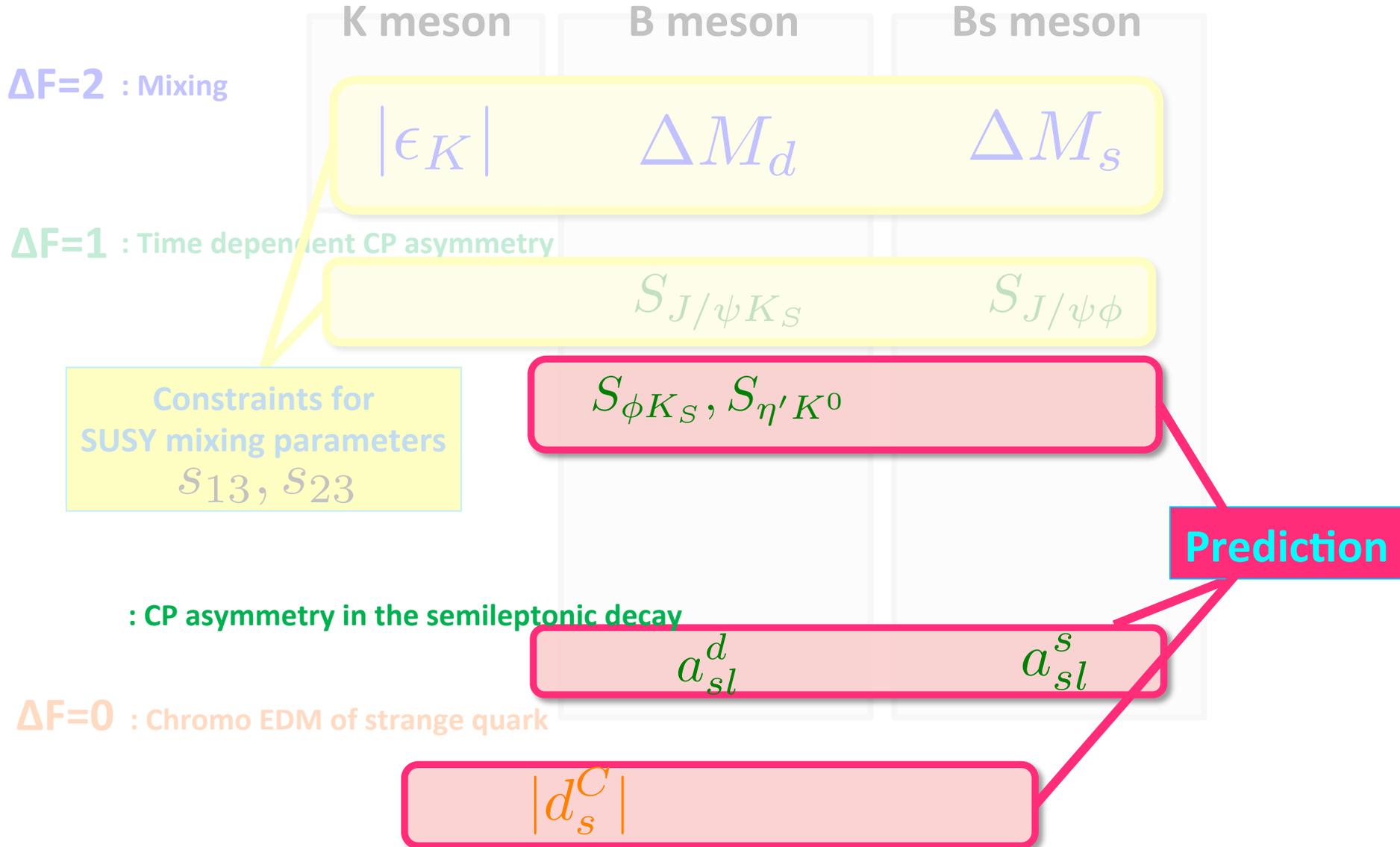
SM component



Taking account
of Gluino squark
interaction



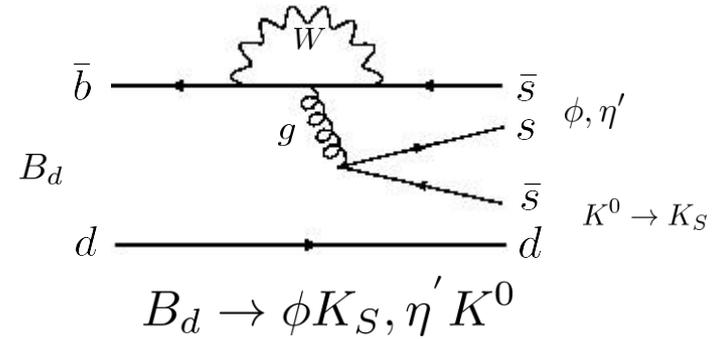
Our strategy



Time dependent CP asymmetry $S_{\phi K_S}, S_{\eta' K^0}$ ^{16/23}

Time dependent CP asymmetry

$$\begin{aligned}
 \mathcal{A} &= \frac{\Gamma(B^0(t) \rightarrow f) - \Gamma(\bar{B}^0(t) \rightarrow f)}{\Gamma(B^0(t) \rightarrow f) + \Gamma(\bar{B}^0(t) \rightarrow f)} \\
 &= \frac{|\lambda|^2 - 1}{|\lambda|^2 + 1} \cos(\Delta m_B t) + \underbrace{\frac{2\text{Im}\lambda}{|\lambda|^2 + 1}}_{S_f} \sin(\Delta m_B t) \\
 &\quad \left(\lambda = \frac{q}{p} \frac{\bar{A}}{A} \right)
 \end{aligned}$$



SM prediction

$$S_{J/\psi K_S} \simeq S_{\phi K_S, \eta' K_S}$$

Both CP violations come from CP phase in the $B_d^0 - \bar{B}_d^0$ mixing.

SUSY contribution [S. Khalil, E. Kou(2003), A.L. Kagan(2002), M.Endo, S.Mishima, M.Yamaguchi (2005)]

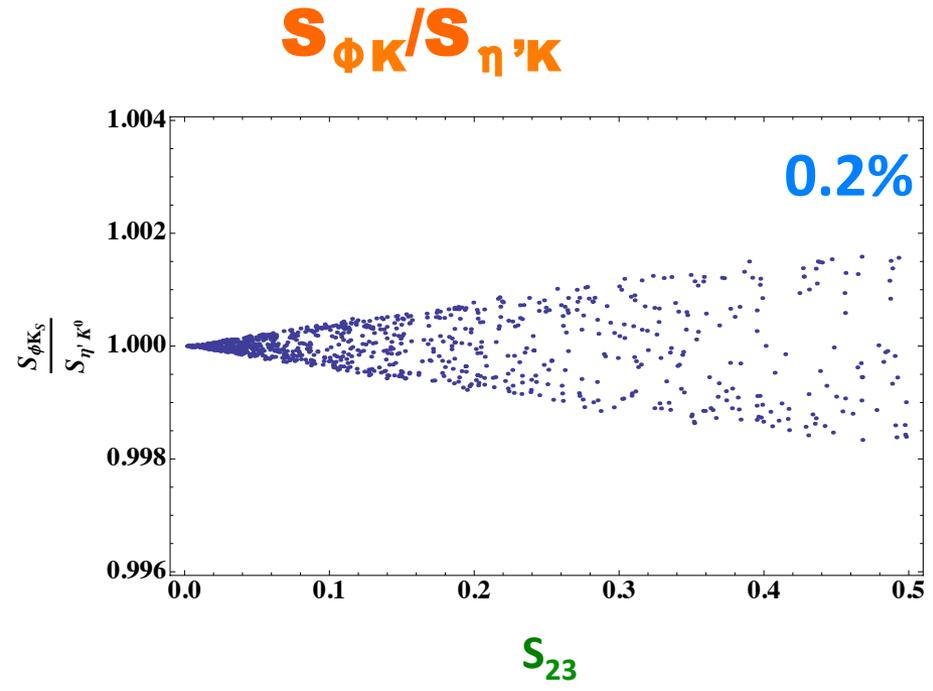
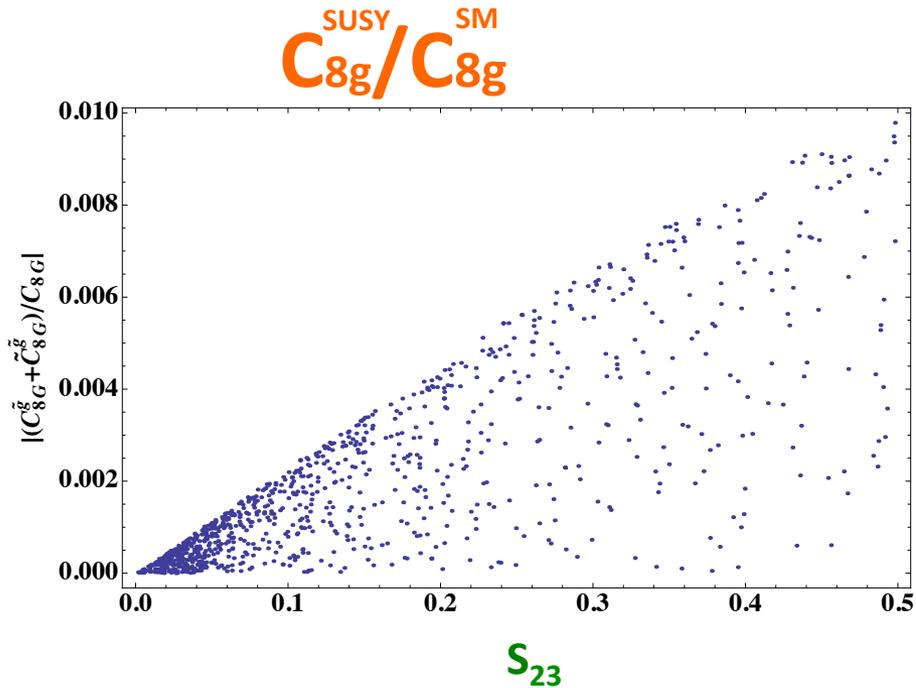
$$O_{8G} = \frac{g_s}{16\pi^2} m_b \bar{s}_i \sigma^{\mu\nu} P_R T_{ij}^a b_j G_{\mu\nu}^a$$

$$A^{SUSY}(\bar{B}_d \rightarrow \phi K_S) \propto C_{8G}^{\tilde{g}}(m_b) + \tilde{C}_{8G}^{\tilde{g}}(m_b) \quad \tilde{C} : C(L \Leftrightarrow R)$$

$$A^{SUSY}(\bar{B}_d \rightarrow \eta' K_S) \propto C_{8G}^{\tilde{g}}(m_b) - \tilde{C}_{8G}^{\tilde{g}}(m_b)$$

- $C_{8G}^{\tilde{g}}$ is depend on S_{23}
- Difference of sign comes from parity of final state

Time dependent CP asymmetry $S_{\phi K_S}, S_{\eta' K^0}^{17/23}$

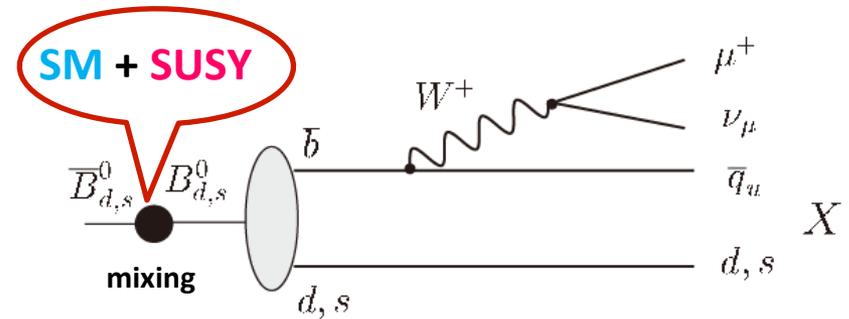


insensitive...

- CP asymmetry in the semileptonic decay in $\bar{B}_q^0 \Rightarrow B_q^0 \rightarrow \mu^+ X$

$$a_{sl}^q \equiv \frac{\Gamma(\bar{B}_q^0 \rightarrow \mu^+ X) - \Gamma(B_q^0 \rightarrow \mu^- X)}{\Gamma(\bar{B}_q^0 \rightarrow \mu^+ X) + \Gamma(B_q^0 \rightarrow \mu^- X)}$$

$$= \frac{1 - \left| \frac{p}{q} \right|^4}{1 + \left| \frac{p}{q} \right|^4} = -\text{Im} \left(\frac{\Gamma_{12}}{M_{12}} \right)$$



SM predictions

[A.Lenz and U.Nierste, arXiv:1102.4274 [hep-ph]]

$$a_{sl}^{s, \text{SM}} = (1.9 \pm 0.3) \times 10^{-5}$$

$$a_{sl}^{d, \text{SM}} = -(4.1 \pm 0.6) \times 10^{-4}$$

Experimental results [PDG 2012]

$$a_{sl}^s = (-0.24 \pm 0.54 \pm 0.33) \times 10^{-2}$$

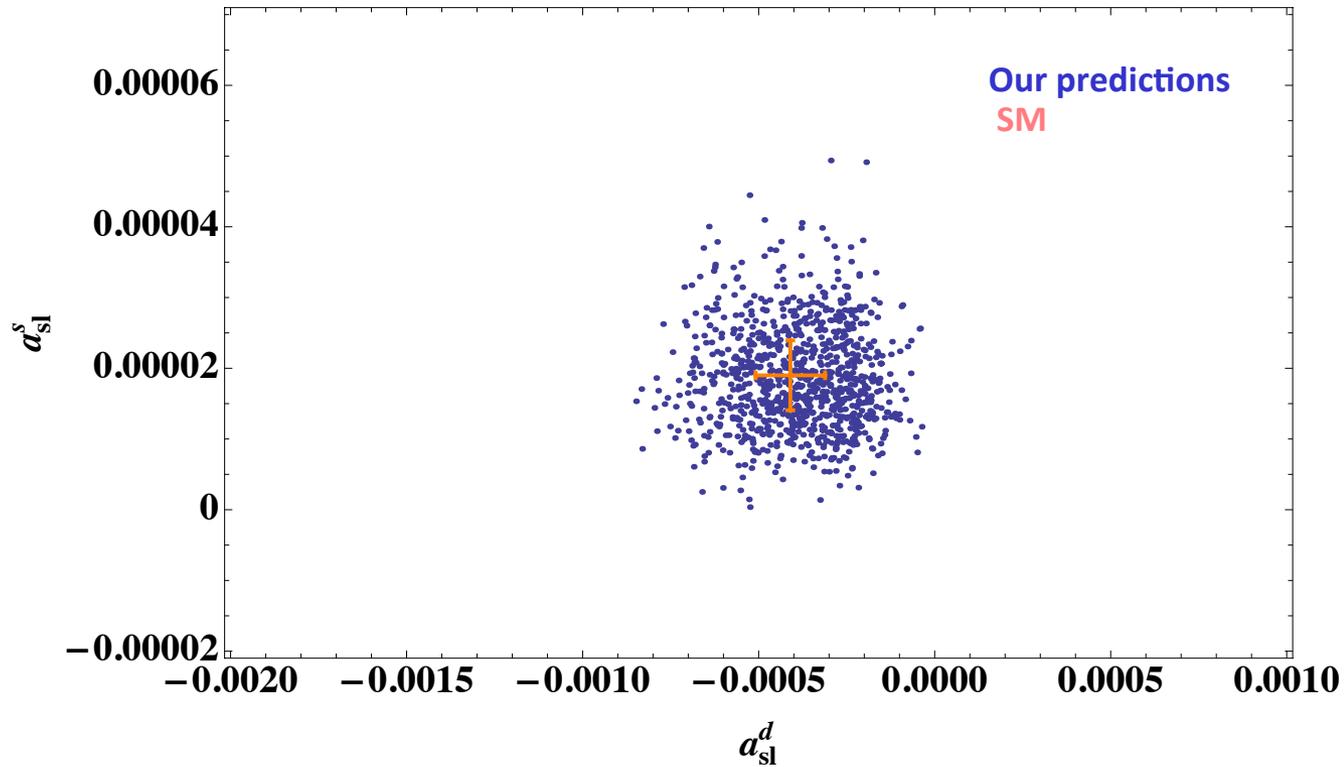
$$a_{sl}^d = (-0.3 \pm 2.1) \times 10^{-3}$$

- a_{sl}^d is depend on S_{13} , a_{sl}^s is depend on S_{23}

Semi-leptonic CP asymmetry

$$a_{sl}^d, a_{sl}^s$$

a_{sl}^s vs. a_{sl}^d



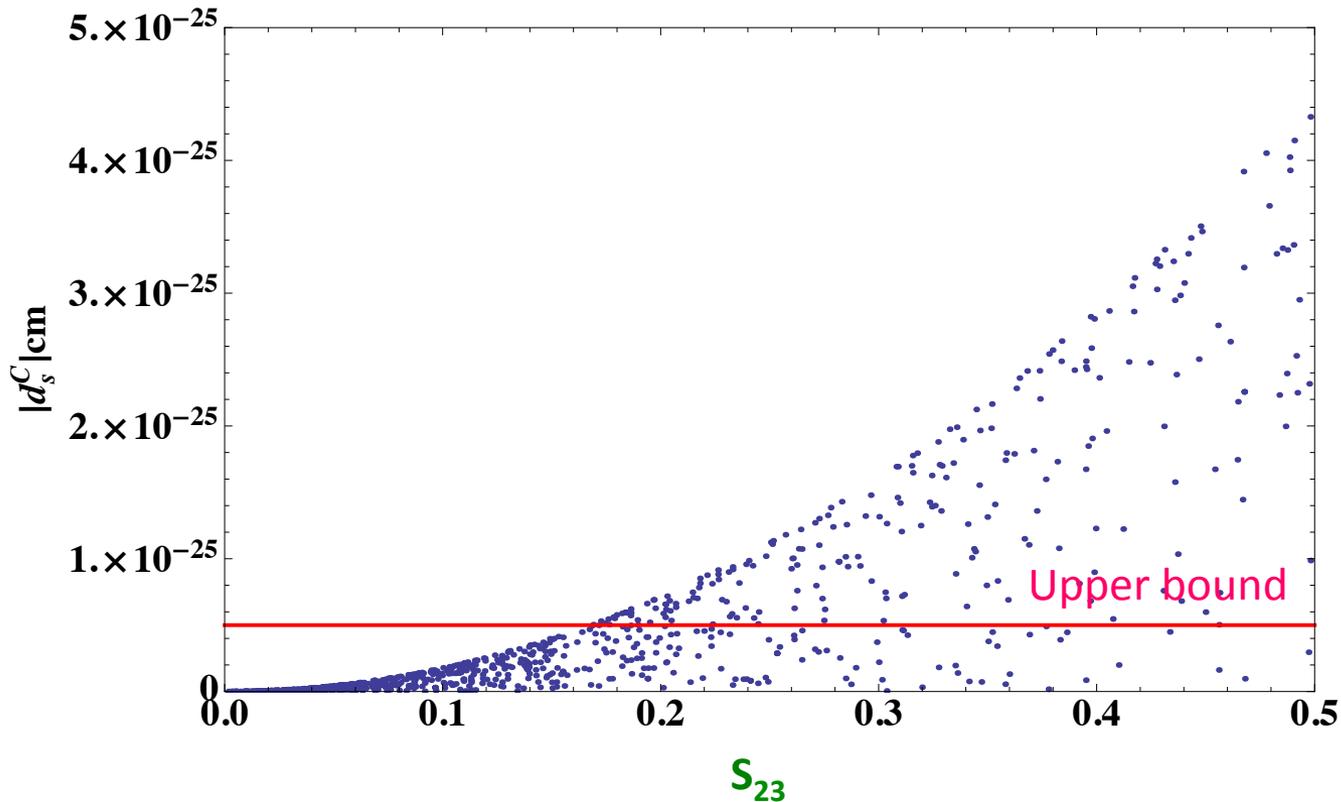
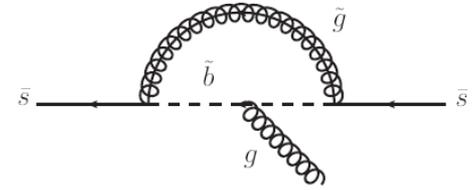
$$a_{sl}^d < 1 \times 10^{-3}, \quad a_{sl}^s < 5 \times 10^{-5}$$

insensitive...

Chromo-EDM of strange quark

$$e|d_s^C| < 0.5 \times 10^{-25} \text{ ecm} \quad [\text{K.Fuyuto, J.Hisano and N.Nagata, 2013}]$$

$$|d_s^C| \propto s_{23}^L c_{13}^L s_{23}^R c_{13}^R \sin(2\theta) e^{-i(\phi_{23}^L + \phi_{23}^R + \phi)}$$

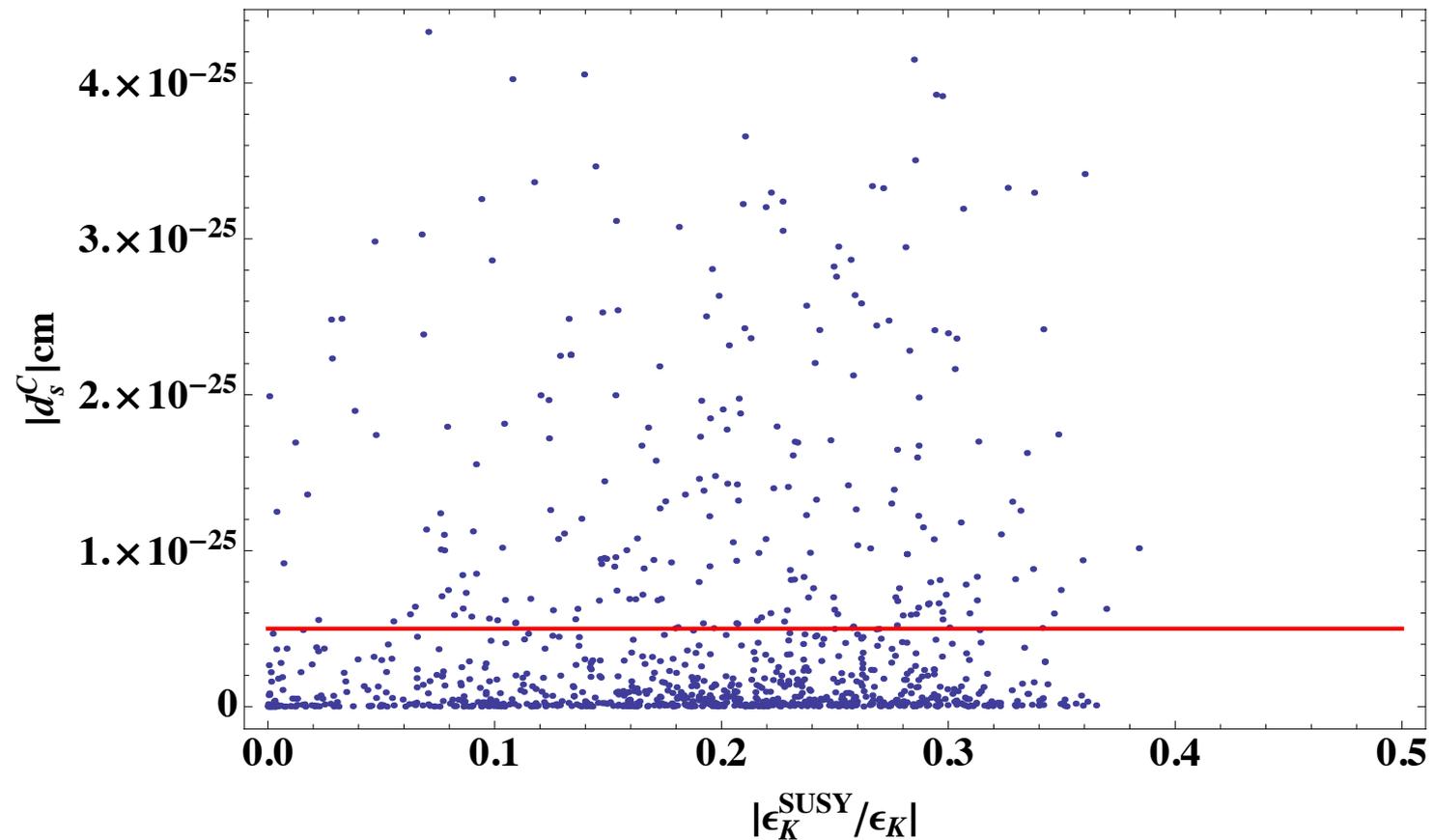


$$|d_s^C| < 4 \times 10^{-25} \text{ cm}$$

sensitive

Chromo-EDM of strange quark vs. ϵ_K

$$|d_s^C| \propto s_{23}^L c_{13}^L s_{23}^R c_{13}^R \sin(2\theta) e^{-i(\phi_{23}^L + \phi_{23}^R + \phi)}$$

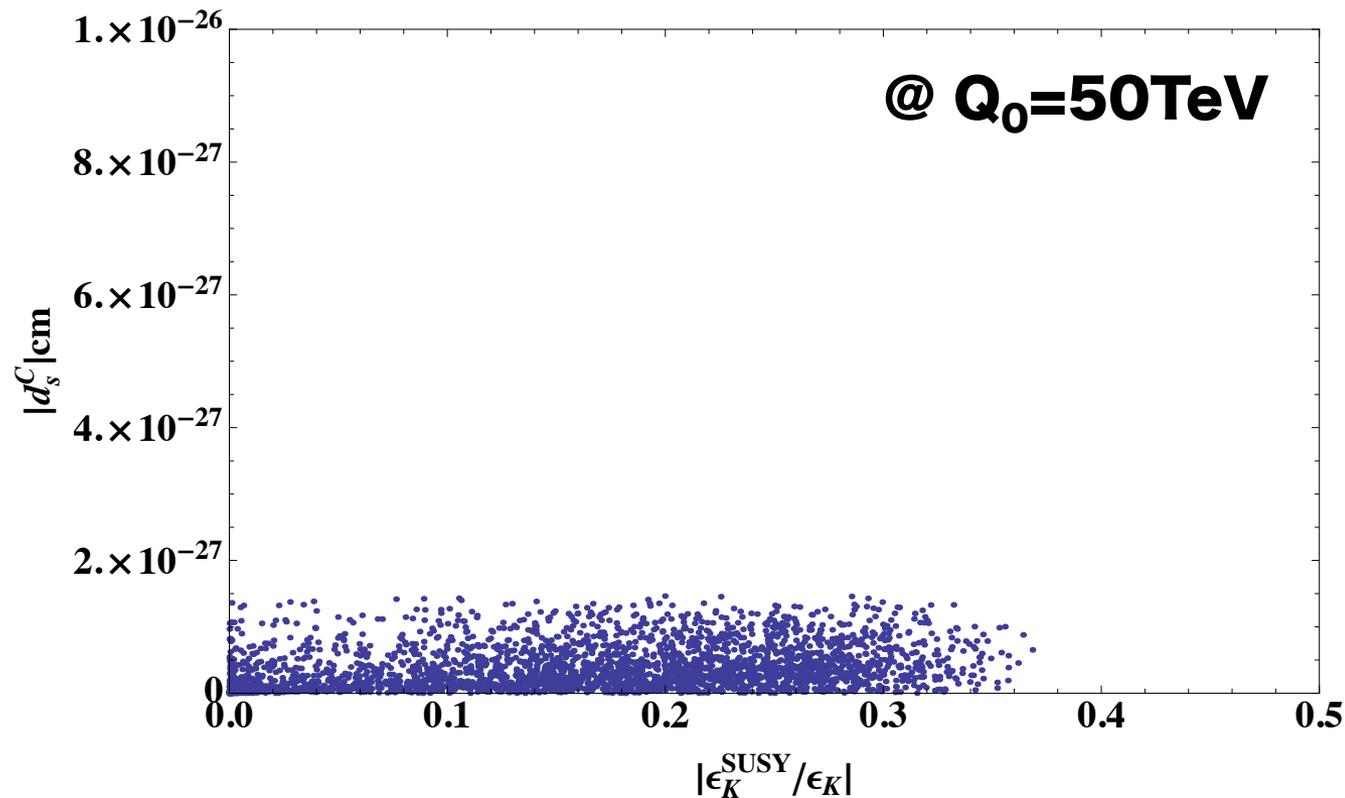


Chromo-EDM of strange quark vs. ϵ_K

$$|d_s^C| \propto s_{23}^L c_{13}^L s_{23}^R c_{13}^R \sin(2\theta) e^{-i(\phi_{23}^L + \phi_{23}^R + \phi)}$$

$$Q_0 = 10 \text{ TeV} \rightarrow Q_0 = 50 \text{ TeV}$$

$$\theta = 0.35^\circ \quad \theta = 0.05^\circ$$



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- We examined the sensitivity of High scale SUSY, in which squark spectrum is consistent with Higgs mass

	(a) $Q_0 = 10$ TeV	(b) $Q_0 = 50$ TeV
✓ $ \epsilon_K $	40%	35%
$S_{J/\psi K_S}$	6%	0.1%
$S_{J/\psi \phi}$	8%	0.1%
ΔM_{B^0}	6%	0.1%
ΔM_{B_s}	0.4%	0.005%
$ S_{\phi K_S}/S_{\eta' K^0} - 1$	0.2%	0.001%
$\text{BR}(b \rightarrow s\gamma)$	0.3%	0.001%
$ a_{sl}^d $	$\leq 1 \times 10^{-3}$	$\leq 8 \times 10^{-4}$
$ a_{sl}^s $	$\leq 5 \times 10^{-5}$	$\leq 4 \times 10^{-5}$
✓ $ d_s^C $	$\leq 4 \times 10^{-25}$ cm	$\leq 1 \times 10^{-27}$ cm

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- We examined the sensitivity of High scale SUSY, in which squark spectrum is consistent with Higgs mass

	(a) $Q_0 = 10$ TeV	(b) $Q_0 = 50$ TeV
✓ $ \epsilon_K $	40%	35%
$S_{J/\psi K_S}$	6%	0.1%
$S_{\eta' K^0}$	8%	0.1%
$\Delta M_{B_s}^{\text{th}} / \Delta M_{B_s}^{\text{expt}}$	6%	0.1%
$ \mathcal{S}_{\phi K_S} / \mathcal{S}_{\eta' K^0} - 1$	0.4%	0.005%
$\text{BR}(b \rightarrow s\gamma)$	0.2%	0.001%
$\text{BR}(b \rightarrow s\gamma)$	0.3%	0.001%
$ a_{sl}^d $	$\leq 1 \times 10^{-3}$	$\leq 8 \times 10^{-4}$
$ a_{sl}^s $	$\leq 5 \times 10^{-5}$	$\leq 4 \times 10^{-5}$
✓ $ d_s^C $	$\leq 4 \times 10^{-25}$ cm	$\leq 1 \times 10^{-27}$ cm

ϵ_K has sensitivity of squark flavor mixing on the present experimental data even if SUSY scale is higher than 50 TeV

4. Summary

- We examined the sensitivity of High scale SUSY, in which squark spectrum is consistent with Higgs mass

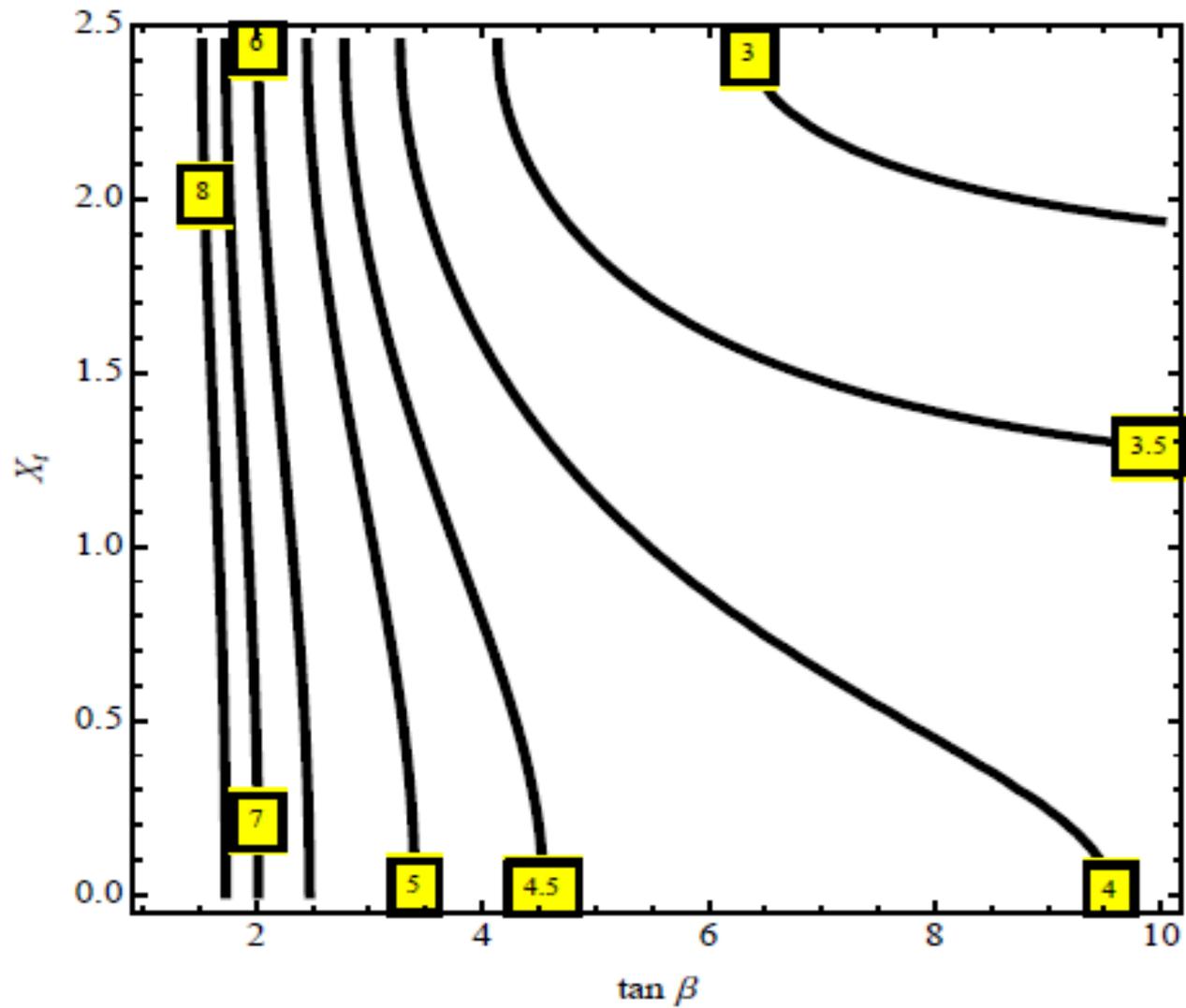
	(a) $Q_0 = 10 \text{ TeV}$	(b) $Q_0 = 50 \text{ TeV}$
✓ $ \epsilon_K $	40%	35%
$S_{J/\psi K_S}$	6%	0.1%
ϵ_K has sensitivity of squark flavor mixing on the present experimental data even if SUSY scale is higher than 50 TeV		
$ S_{\phi K_S}/S_{\eta' K^0} - 1$	0.2%	0.001%
cEDM has sensitivity at 10-50 TeV		
$ d_s^C $	$\leq 5 \times 10^{-5}$ $\leq 4 \times 10^{-25} \text{ cm}$	$\leq 8 \times 10^{-4}$ $\leq 4 \times 10^{-5}$ $\leq 1 \times 10^{-27} \text{ cm}$

Backup

	Input at Λ and Q_0	Output at Q_0
Case (a)	at $\Lambda = 10^{17}$ GeV, $m_0 = 10$ TeV, $m_{1/2} = 6.2$ TeV, $A_0 = 25.803$ TeV; at $Q_0 = 10$ TeV, $\mu = 10$ TeV, $\tan \beta = 10$	$m_{\tilde{g}} = 12.8$ TeV, $m_{\tilde{W}} = 5.2$ TeV, $m_{\tilde{B}} = 2.9$ TeV $m_{\tilde{b}_L} = m_{\tilde{t}_L} = 12.2$ TeV $m_{\tilde{b}_R} = 14.1$ TeV, $m_{\tilde{t}_R} = 8.4$ TeV $m_{\tilde{s}_L, \tilde{d}_L} = m_{\tilde{c}_L, \tilde{u}_L} = 15.1$ TeV $m_{\tilde{s}_R, \tilde{d}_R} \simeq m_{\tilde{c}_R, \tilde{u}_R} = 14.6$ TeV, $m_{\mathcal{H}} = 13.7$ TeV $A_t = -1.2$ TeV, $A_b = 5.1$ TeV, $X_t = -0.22$ $\lambda_H = 0.126$, $\theta = 0.35^\circ$
Case (b)	at $\Lambda = 10^{16}$ GeV, $m_0 = 50$ TeV, $m_{1/2} = 63.5$ TeV, $A_0 = 109.993$ TeV; at $Q_0 = 50$ TeV, $\mu = 50$ TeV, $\tan \beta = 4$	$m_{\tilde{g}} = 115.6$ TeV, $m_{\tilde{W}} = 55.4$ TeV, $m_{\tilde{B}} = 33.45$ TeV $m_{\tilde{b}_L} = m_{\tilde{t}_L} = 100.9$ TeV $m_{\tilde{b}_R} = 104.0$ TeV, $m_{\tilde{t}_R} = 83.2$ TeV $m_{\tilde{s}_L, \tilde{d}_L} = m_{\tilde{c}_L, \tilde{u}_L} = 110.7$ TeV, $m_{\tilde{s}_R, \tilde{d}_R} = 110.7$ TeV $m_{\tilde{c}_R, \tilde{u}_R} = 105.0$ TeV, $m_{\mathcal{H}} = 83.1$ TeV $A_t = -20.2$ TeV, $A_b = 4.7$ TeV, $X_t = -0.65$ $\lambda_H = 0.1007$, $\theta = 0.05^\circ$

Table 1: Input parameters at Λ and obtained the SUSY spectra in the cases of (a) and (b).

$$\overline{m}_t(m_t) = 163.5 \pm 2 \text{ GeV}$$



[Delgado, Garcia, Quiros, arXiv:1312.3235]

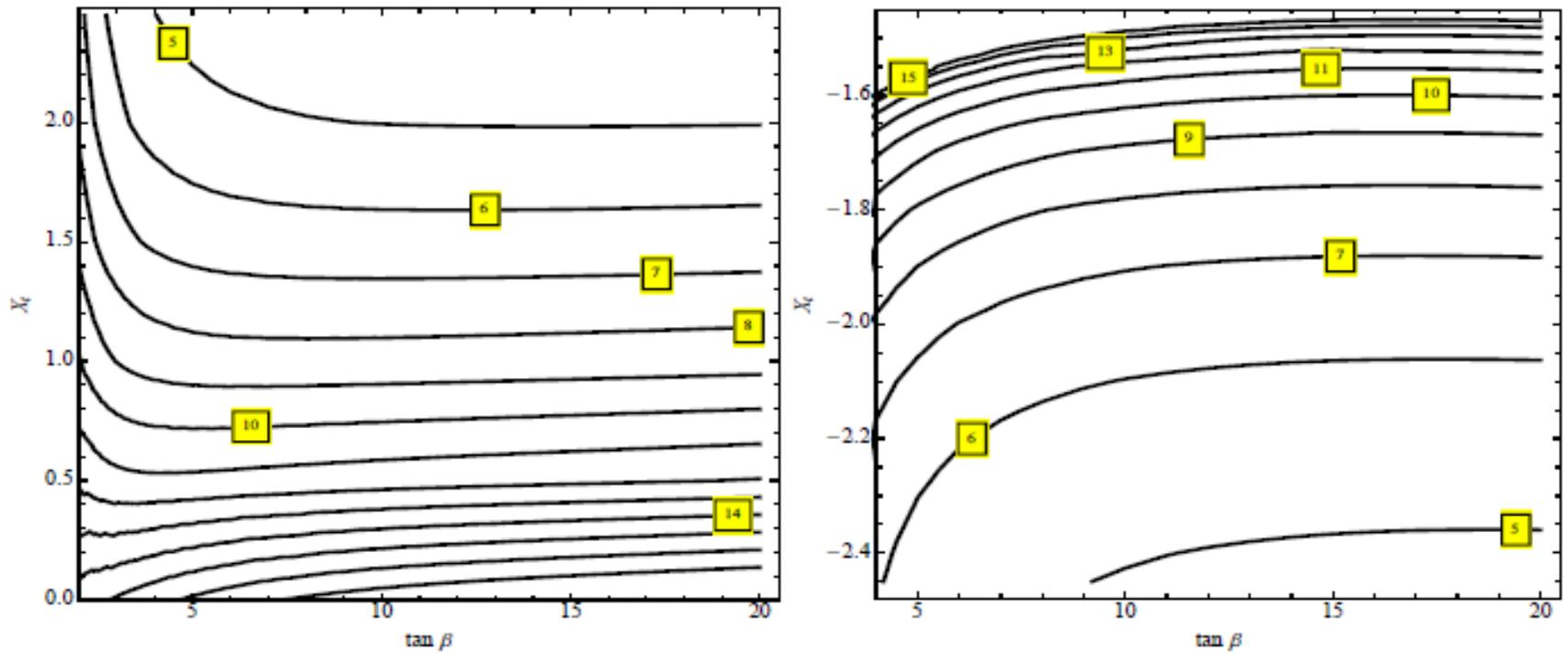
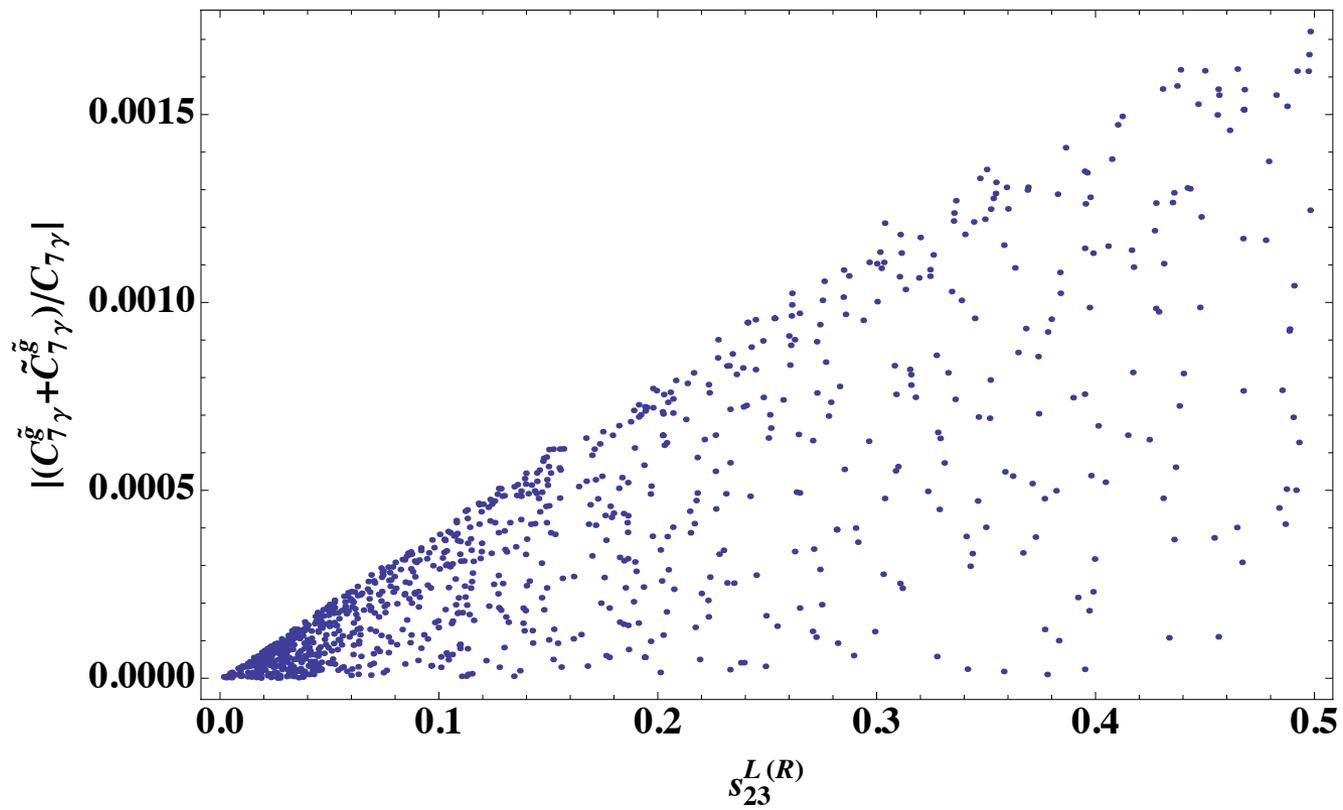


Figure 4: Contour lines of constant $\log_{10}[\mathcal{M}/\text{GeV}]$ in the $(\tan \beta, X_t)$ plane for $X_t \geq 0$ (left panel) and $X_t < 0$ (right panel).

$C_{7\gamma}^{\text{SUSY}}/C_{7\gamma}^{\text{SM}}$



$\Delta F=2$ process : $K-\bar{K}$, $B-\bar{B}$, $B_s-\bar{B}_s$ mixing $|\epsilon_K|$ ΔM_d ΔM_s

$$|\epsilon_K^{exp}| = (2.228 \pm 0.011) \times 10^{-3}$$

$$\Delta M_s = (116.942 \pm 0.1564) \times 10^{-13} \text{GeV}$$

$$\Delta M_d = (3.337 \pm 0.033) \times 10^{-13} \text{GeV}$$

$\Delta F=1$ process : Time dependent CP asymmetry $S_{J/\psi K_S}$ $S_{J/\psi \phi}$

$$S_{J/\psi K_S} = 0.679 \pm 0.020$$

$$S_{J/\psi \phi} \quad \phi_s = 0.07 \pm 0.09 \pm 0.01$$

Complementarity of Belle II and LHCb

Observable	Expected th. accuracy	Expected exp. uncertainty	Facility
CKM matrix			
$ V_{cs} [K \rightarrow \pi \ell \nu]$	**	0.1%	<i>K</i> -factory
$ V_{cb} [B \rightarrow X_c \ell \nu]$	**	1%	Belle II
$ V_{ub} [B_d \rightarrow \pi \ell \nu]$	*	4%	Belle II
$\sin(2\phi_1) [c\bar{c}K_S^0]$	***	$8 \cdot 10^{-3}$	Belle II/LHCb
ϕ_2		1.5°	Belle II
ϕ_3	***	3°	LHCb
CPV			
$S(B_s \rightarrow \psi\phi)$	**	0.01	LHCb
$S(B_s \rightarrow \phi\phi)$	**	0.05	LHCb
$S(B_d \rightarrow \phi K)$	***	0.05	Belle II/LHCb
$S(B_d \rightarrow \eta' K)$	***	0.02	Belle II
$S(B_d \rightarrow K^* (\rightarrow K_S^0 \pi^0) \gamma)$	***	0.03	Belle II
$S(B_s \rightarrow \phi \gamma)$	***	0.05	LHCb
$S(B_d \rightarrow \rho \gamma)$		0.15	Belle II
A_{SL}^d	***	0.001	LHCb
A_{SL}^s	***	0.001	LHCb
$A_{CP}(B_d \rightarrow s\gamma)$	*	0.005	Belle II
rare decays			
$\mathcal{B}(B \rightarrow \tau \nu)$	**	3%	Belle II
$\mathcal{B}(B \rightarrow D \tau \nu)$		3%	Belle II
$\mathcal{B}(B_d \rightarrow \mu \nu)$	**	6%	Belle II
$\mathcal{B}(B_s \rightarrow \mu \mu)$	***	10%	LHCb
zero of $A_{FB}(B \rightarrow K^* \mu \mu)$	**	0.05	LHCb
$\mathcal{B}(B \rightarrow K^{(*)} \nu \nu)$	***	30%	Belle II
$\mathcal{B}(B \rightarrow s \gamma)$	KEK-PH2013 F=10%		Belle II
$\mathcal{B}(B_s \rightarrow \gamma \gamma)$		$0.25 \cdot 10^{-6}$	Belle II (with 5 ab^{-1})

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Type	Observable	Current precision	LHCb 2018	Upgrade (50 fb ⁻¹)	Theory uncertainty
B_s^0 mixing	$2\beta_s (B_s^0 \rightarrow J/\psi \phi)$	0.10 [9]	0.025	0.008	~ 0.003
	$2\beta_s (B_s^0 \rightarrow J/\psi f_0(980))$	0.17 [10]	0.045	0.014	~ 0.01
	$A_{FB}(B_s^0)$	6.4×10^{-3} [18]	0.6×10^{-3}	0.2×10^{-3}	0.03×10^{-3}
Gluonic penguin	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\phi)$	–	0.17	0.03	0.02
	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow K^{*0}\bar{K}^{*0})$	–	0.13	0.02	< 0.02
	$2\beta_s^{\text{eff}}(B^0 \rightarrow \phi K_S^0)$	0.17 [18]	0.30	0.05	0.02
Right-handed currents	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\gamma)$	–	0.09	0.02	< 0.01
	$\tau^{\text{eff}}(B_s^0 \rightarrow \phi\gamma)/\tau_{B_s^0}$	–	5%	1%	0.2%
Electroweak penguin	$S_3(B^0 \rightarrow K^{*0}\mu^+\mu^-; 1 < q^2 < 6 \text{ GeV}^2/c^4)$	0.08 [14]	0.025	0.008	0.02
	$s_0 A_{FB}(B^0 \rightarrow K^{*0}\mu^+\mu^-)$	25% [14]	6%	2%	7%
	$A_I(K\mu^+\mu^-; 1 < q^2 < 6 \text{ GeV}^2/c^4)$	0.25 [15]	0.08	0.025	~ 0.02
	$\mathcal{B}(B^+ \rightarrow \pi^+\mu^+\mu^-)/\mathcal{B}(B^+ \rightarrow K^+\mu^+\mu^-)$	25% [16]	8%	2.5%	$\sim 10\%$
Higgs penguin	$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	1.5×10^{-9} [2]	0.5×10^{-9}	0.15×10^{-9}	0.3×10^{-9}
	$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)$	–	$\sim 100\%$	$\sim 35\%$	$\sim 5\%$
Unitarity triangle angles	$\gamma (B \rightarrow D^{(*)} K^{(*)})$	$\sim 10\text{--}12^\circ$ [19, 20]	4°	0.9°	negligible
	$\gamma (B_s^0 \rightarrow D_s K)$	–	11°	2.0°	negligible
	$\beta (B^0 \rightarrow J/\psi K_S^0)$	0.8° [18]	0.6°	0.2°	negligible
Charm	A_F	2.3×10^{-3} [18]	0.40×10^{-3}	0.07×10^{-3}	–
CP violation	ΔA_{CP}	2.1×10^{-3} [5]	0.65×10^{-3}	0.12×10^{-3}	–

Table 1: Statistical sensitivities of the LHCb upgrade to key observables. For each observable the current sensitivity is compared to that which will be achieved by LHCb before the upgrade, and that which will be achieved with 50 fb⁻¹ by the upgraded experiment. Systematic uncertainties are expected to be non-negligible for the most precisely measured quantities.

The cEDM of the strange quark from gluino contribution is given by [65]

$$d_s^C(Q_0) = -2\sqrt{4\pi\alpha_s(m_{\tilde{g}})}\text{Im}[A_s^{g22}(Q_0)], \quad (64)$$

where

$$A_s^{g22}(Q_0) = -\frac{\alpha_s(m_{\tilde{g}})}{4\pi} \frac{1}{3} \left[\frac{1}{2m_{\tilde{d}_3}^2} \left\{ \left(m_s(\lambda_{GLL}^{(d)})_3^{22} + m_s(\lambda_{GRR}^{(d)})_3^{22} \right) \left(9F_1(x_{\tilde{g}}^3) + F_2(x_{\tilde{g}}^3) \right) \right. \right. \\ \left. \left. + m_{\tilde{g}}(\lambda_{GLR}^{(d)})_3^{22} \left(9F_3(x_{\tilde{g}}^3) + F_4(x_{\tilde{g}}^3) \right) \right\} \right. \\ \left. + \frac{1}{2m_{\tilde{d}_6}^2} \left\{ \left(m_s(\lambda_{GLL}^{(d)})_6^{22} + m_s(\lambda_{GRR}^{(d)})_6^{22} \right) \left(9F_1(x_{\tilde{g}}^6) + F_2(x_{\tilde{g}}^6) \right) + m_{\tilde{g}}(\lambda_{GLR}^{(d)})_6^{22} \left(9F_3(x_{\tilde{g}}^6) + F_4(x_{\tilde{g}}^6) \right) \right\} \right]. \quad (65)$$

Including the QCD correction, we get

$$d_s^C(2\text{GeV}) = d_s^C(Q_0) \left(\frac{\alpha_s(Q_0)}{\alpha_s(m_{\tilde{g}})} \right)^{\frac{14}{15}} \left(\frac{\alpha_s(m_{\tilde{g}})}{\alpha_s(m_t)} \right)^{\frac{14}{21}} \left(\frac{\alpha_s(m_t)}{\alpha_s(m_b)} \right)^{\frac{14}{23}} \left(\frac{\alpha_s(m_b)}{\alpha_s(2\text{GeV})} \right)^{\frac{14}{25}}. \quad (66)$$

Factorization relation

$$\langle O_3 \rangle = \langle O_4 \rangle = \left(1 + \frac{1}{N_c}\right) \langle O_5 \rangle, \quad \langle O_6 \rangle = \frac{1}{N_c} \langle O_5 \rangle,$$

$$\langle O_{8G} \rangle = \frac{\alpha_s(m_b)}{8\pi} \left(-\frac{2m_b}{\sqrt{\langle q^2 \rangle}} \right) \left(\langle O_4 \rangle + \langle O_6 \rangle - \frac{1}{N_c} (\langle O_3 \rangle + \langle O_5 \rangle) \right),$$

[R. Harnik, D. T. Larson, H. Murayama and A. Pierce (2004)]