



Track Reconstruction for Mu3e based on a Multiple Scattering Fit

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on behalf of the Mu3e collaboration

Outline



- The Mu3e experiment
- Multiple scattering fit
- Tracking performance
- Reconstruction on GPU

Mu3e Experiment

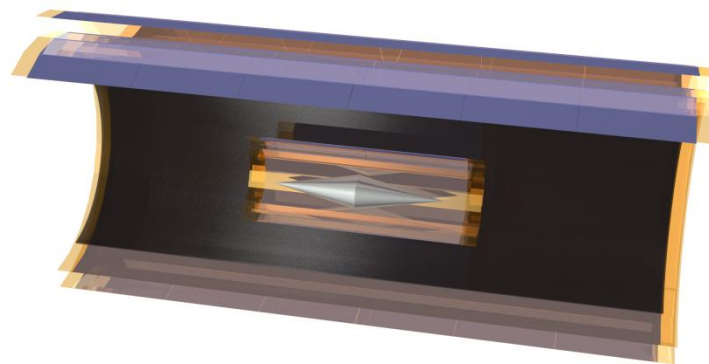


- Search for $\mu^+ \rightarrow e^+e^+e^-$ decay at PSI
- Current experimental status:
 - SINDRUM (PSI, 1988)
 - $\text{Br}(\mu^+ \rightarrow e^+e^+e^-) < 10^{-12}$ at 90% c.l.
- Sensitivity goal:
 - phase I @ $10^8 \mu^+/s$: $\text{Br} < 10^{-15}$
 - phase II @ $10^9 \mu^+/s$: $\text{Br} < 10^{-16}$
- Requirements:
 - Beam: $O(10^9) \mu^+/s$
 - Good momentum and timing resolution
 - Good vertex resolution
 - Fast readout

Mu3e Collaboration:

- DPNC Geneva University
- Paul Scherrer Institute (PSI)
- Zurich University, ETH
- Heidelberg Physics Inst & KIP
- Mannheim ZITI

Experiment approved in 2013.



Mu3e Experiment



$$\mu^+ \rightarrow e^+e^+e^-:$$

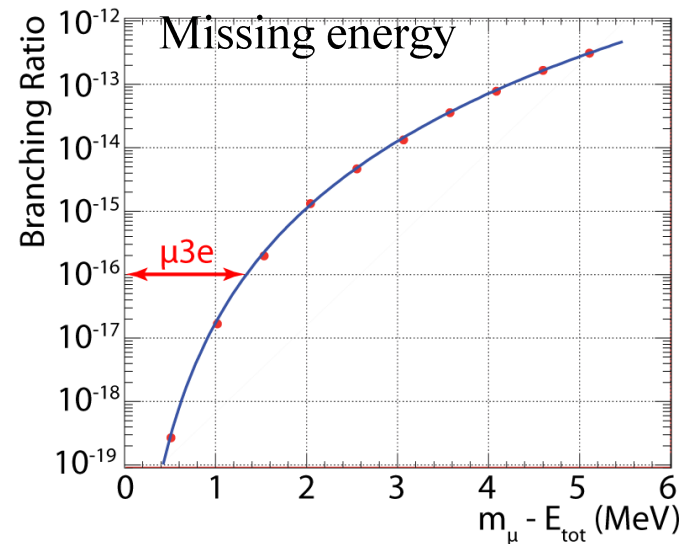
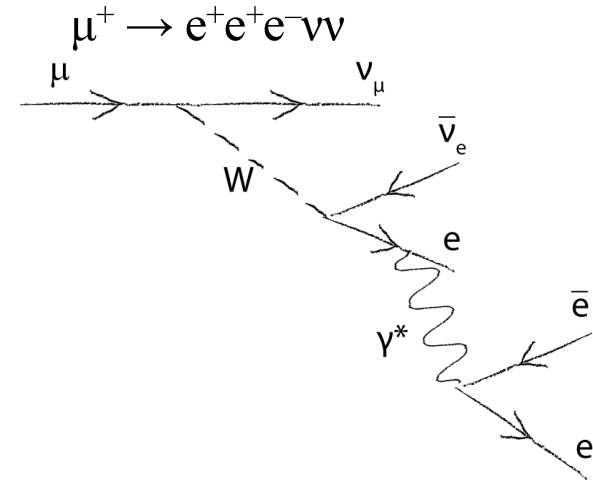
- Muons stopped on target and decay at rest
- Maximum e^\pm energy = 53 MeV
- Missing Energy = 0

Main background:

- $\mu \rightarrow e^+e^+e^-$
- photon conversion
- mis-reconstruction
- $\mu \rightarrow e\nu + \text{combinations}$

For $O(10^{-16})$ sensitivity:

- Momentum resolution: < 0.5 MeV
- Vertex resolution: 200 μm
- Low material budget
- High acceptance & efficiency



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R.M.Djilkibaev, R.V.Konoplich

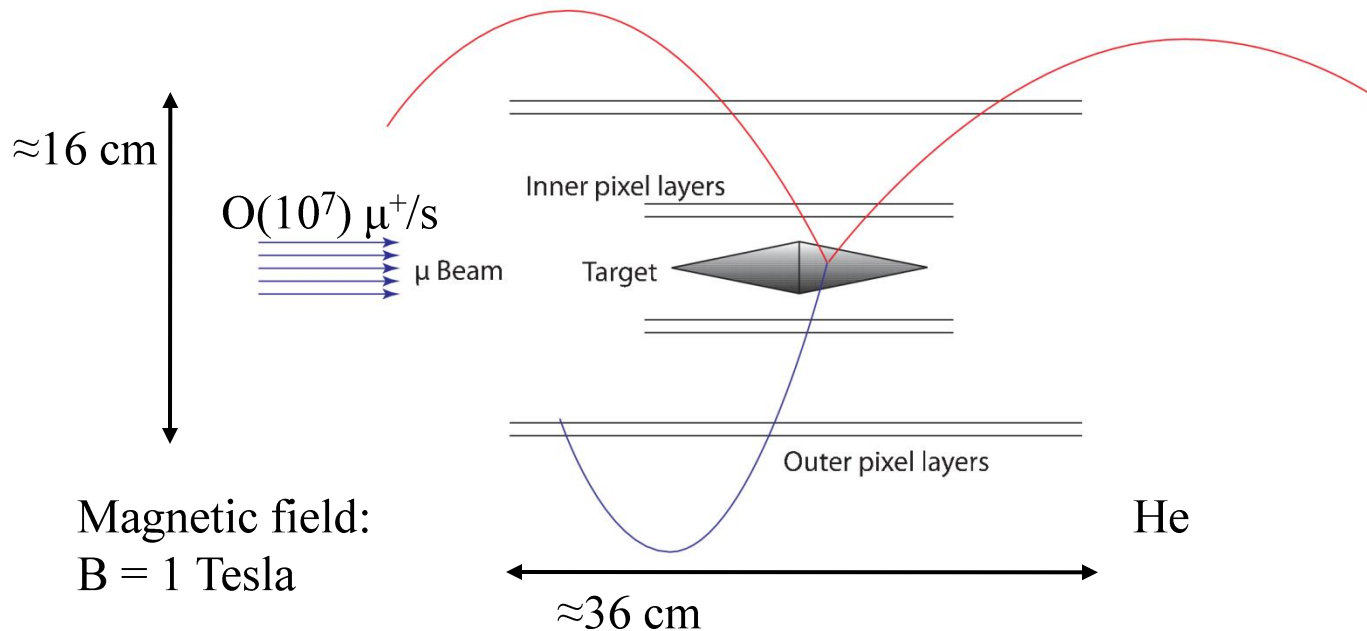
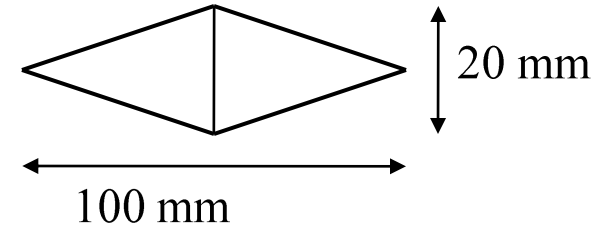
Detector design: phase Ia



Minimum configuration

- Target
- Si-pixel detectors (inner & outer layers).
 - pixel size: $80 \times 80 \mu\text{m}^2$
 - Efficiency: $> 99\%$
- Sensitivity: $O(10^{-14})$

Hollow double cone target.



Si-pixel layer detector



HV-MAPS:

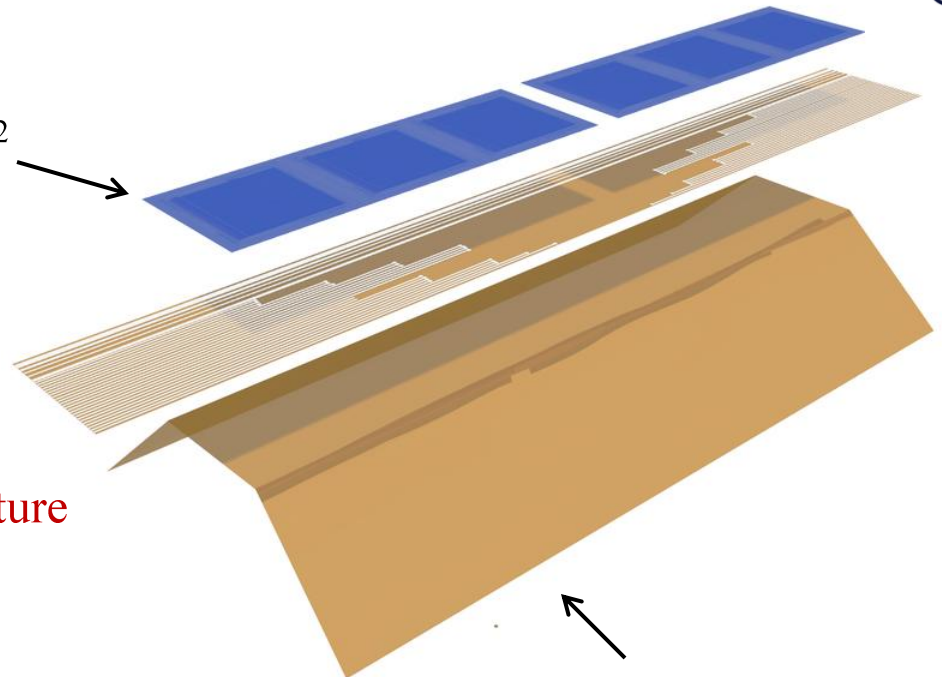
- Thinned to 50 μm
- Sensor size: 1x2 or 2x2 cm^2

Kapton flex print:

- 25 μm kapton
- 12.5 μm Alu traces

- Self supporting, ultra-light structure
- Material: $O(10^{-3}X_0)$

Prototype of inner
two layers



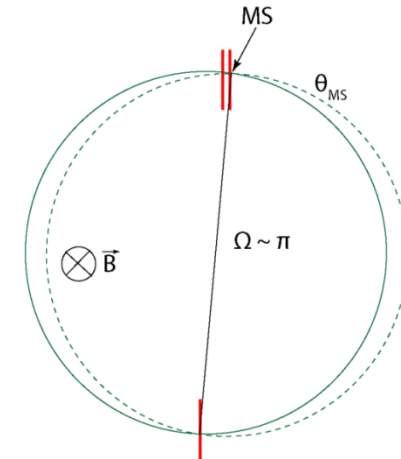
Kapton frame:

- 25 μm foil
- Self supporting

Detector design: phase Ib



- Recurl stations (double layers)
 - Increase acceptance
 - **Much better (x5-x10) momentum resolution (~ 0.2 MeV)**
- Fiber & tile detectors
- Sensitivity: $O(10^{-15})$

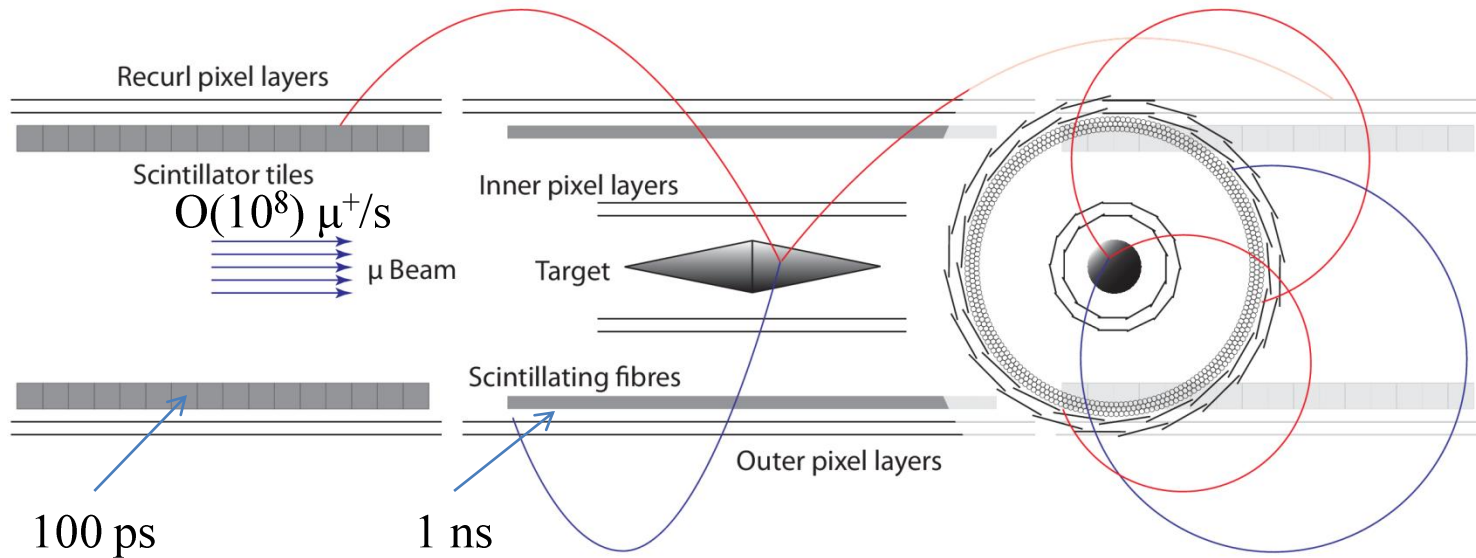


Scintillating fiber tracker:

- Time resolution: 1 ns

Tile detector:

- Time resolution: 100 ps



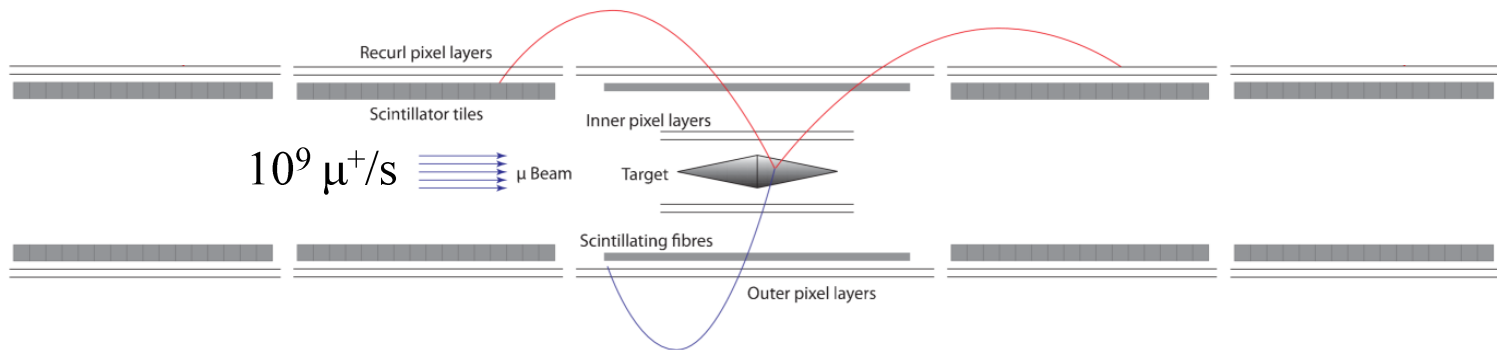
Detector design: phase II



- Additional recurl stations on both sides
- **High track acceptance: $\sim 90\%$**
- New beam line: $10^9 \mu^+/\text{s}$
- Sensitivity: $O(10^{-16})$

Tracker:

- 300M pixels
- **Readout at 20 MHz (50 ns frame)**
- Total data rate: $O(1)$ Tbit/s



Track reconstruction & Event filtering

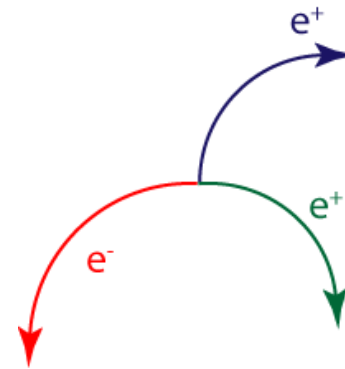


Triggerless system:

- Very high data rate: **1 Tbit/s**
- Online data reduction required

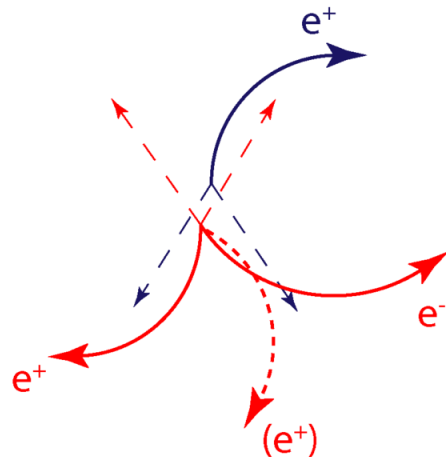
Online reconstruction & filtering:

- Reduce rate by factor **1000**
- **Perform “full” reconstruction** & vertex fit
- Strong requirements on the tracking performance

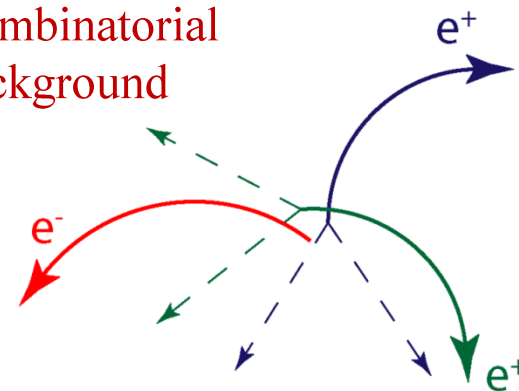


Mu3e signal:

- 3 tracks
- **common vertex**
- **Missing Energy ≈ 0**



Combinatorial background



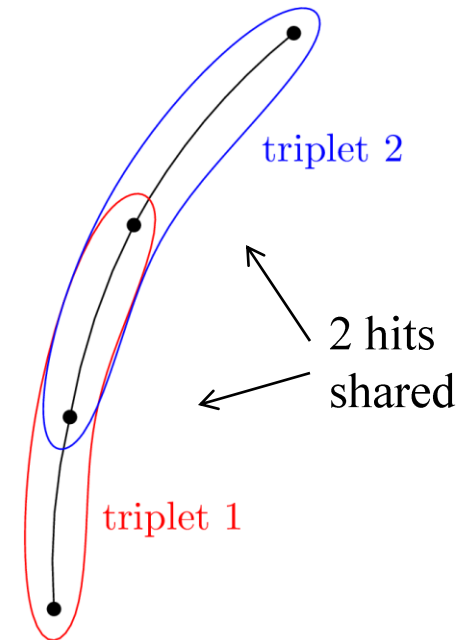
Multiple Scattering fit



- Kalman filter and broken line fits are relatively slow:
 - Both require matrix inversion
- At Mu3e e^+/e^- have low momenta (< 53 MeV)
 - Multiple Scattering (MS) dominates resolution

Multiple scattering fit:

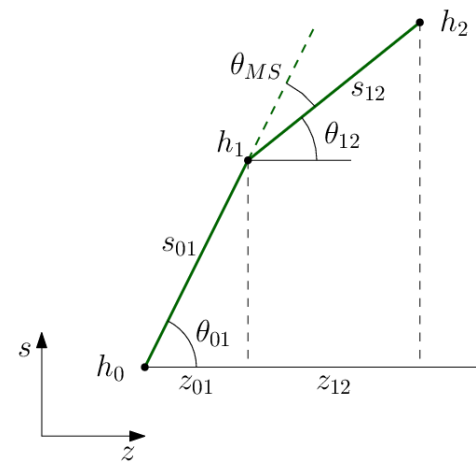
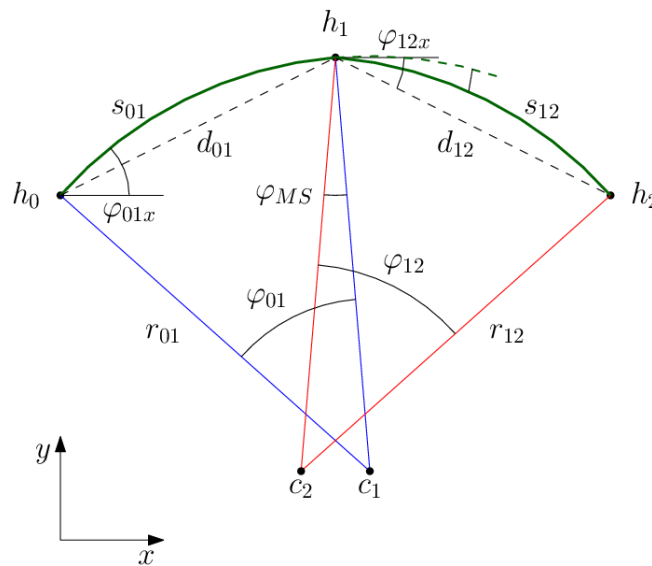
- Assume zero measurement uncertainties
- Describe tracks as a sequence of hit triplets:
 - MS takes place in middle hit of each triplet
 - Track parameters are calculated by taking a weighted mean over all triplets



Multiple Scattering fit



- Each triplet is described by 10 parameters
 - three 3D points (fixed)
 - momentum (3D curvature)
 - 2 helical trajectories (h_0h_1 and h_1h_2)
 - Same 3D radius (energy conservation)
- Two strategies to solve triplet equations:
 - numerical
 - linearization around circle solution



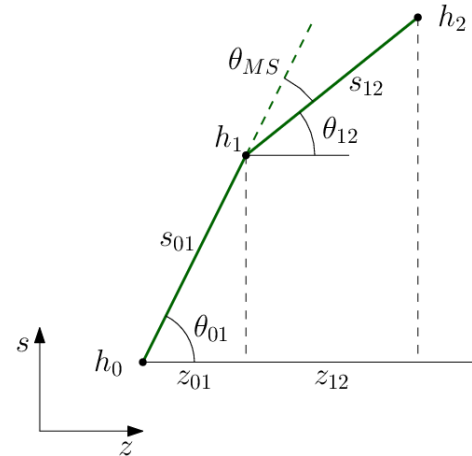
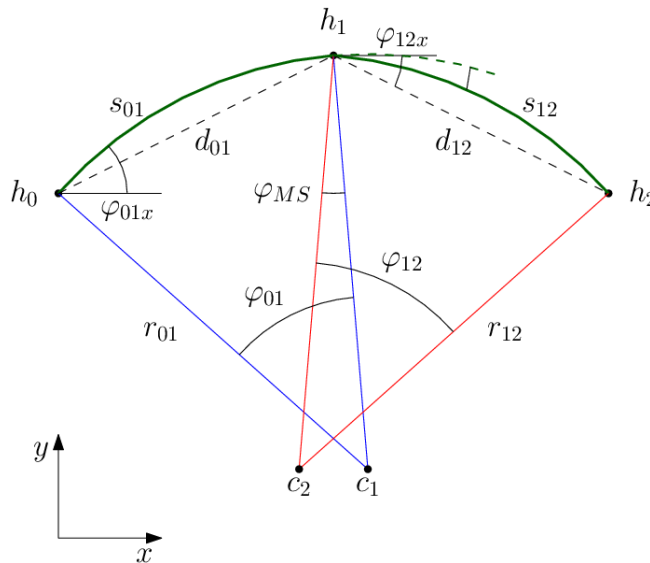
2 helixes:
 $\varphi_{01,12}(\mathbb{R}_{3D})$
 $\theta_{01,12}(\mathbb{R}_{3D})$

MS angles:
 $\varphi_{MS}(\mathbb{R}_{3D})$
 $\theta_{MS}(\mathbb{R}_{3D})$

Multiple Scattering fit



- Minimize $\chi^2 = \frac{\varphi_{MS}^2(R_{3D})}{\sigma_{MS}^2} + \frac{\theta_{MS}^2(R_{3D})}{\sigma_{MS}^2}$
- MS angles are small:
 - use linearization around circle solution
 - very simple equations
- $$\mathbf{R}_{3D} = - \frac{\frac{d\theta_{MS}}{dR_{3D}} \theta_{MS,0} + \frac{d\varphi_{MS}}{dR_{3D}} \varphi_{MS,0}}{\left(\frac{d\theta_{MS}}{dR_{3D}}\right)^2 + \left(\frac{d\varphi_{MS}}{dR_{3D}}\right)^2}$$
- Note: all parameters (including derivatives) are easily calculated from position of 3 hits.



2 helixes:

$$\varphi_{01,12}(\mathbf{R}_{3D})$$

$$\theta_{01,12}(\mathbf{R}_{3D})$$

MS angles:

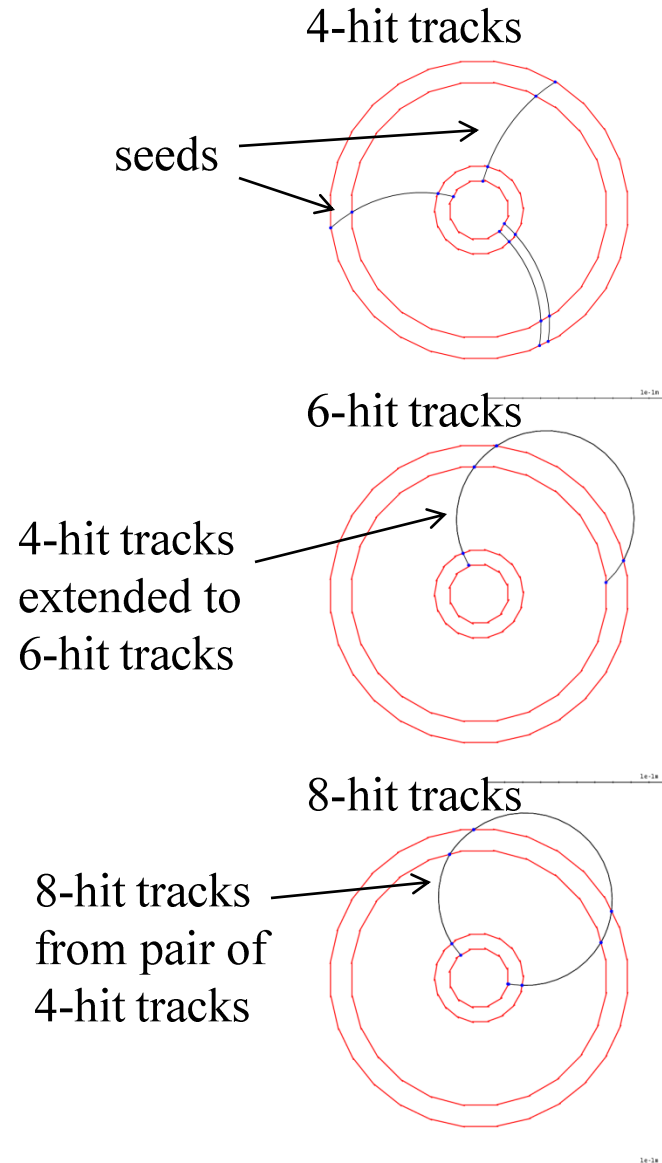
$$\varphi_{MS}(\mathbf{R}_{3D})$$

$$\theta_{MS}(\mathbf{R}_{3D})$$

Track reconstruction



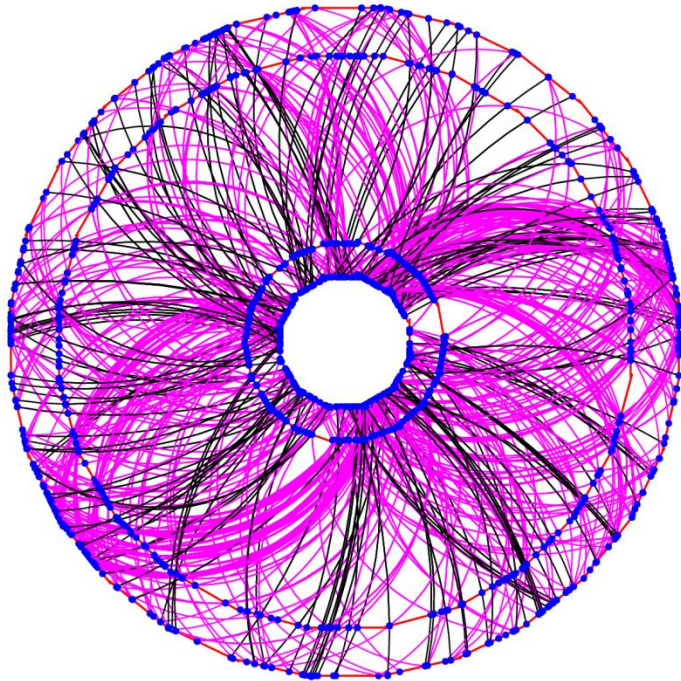
- Fully reconstructed tracks:
 - triplets & 4-hit tracks – seeds.
 - recurls: 6- and 8-hit tracks
- Finding first triplet (first 3 layers) is most expensive operation:
 - No beam line constraint due to extended target
 - $O(n^3)$, n – number of hits in layer
- Triplets & 4-hit tracks used online
- Long tracks are used for offline analysis:
 - Strong constraint on 3D radius
 - $\sigma_p \approx 0.2$ MeV



Reconstruction performance



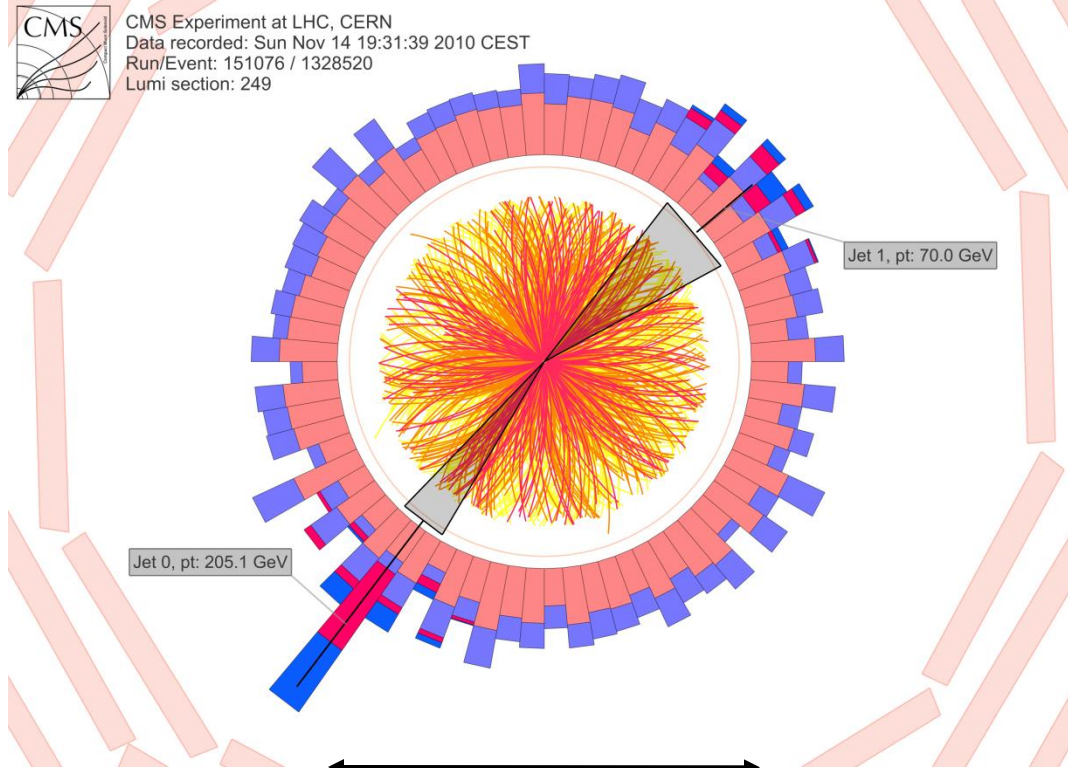
Mu3e: reconstructed 4-hit tracks



≈16 cm

Readout in frames of 50 ns

E ~ 10-50 MeV



≈2.5 m

Collision every 25 ns

E ~ 200 GeV

Performance

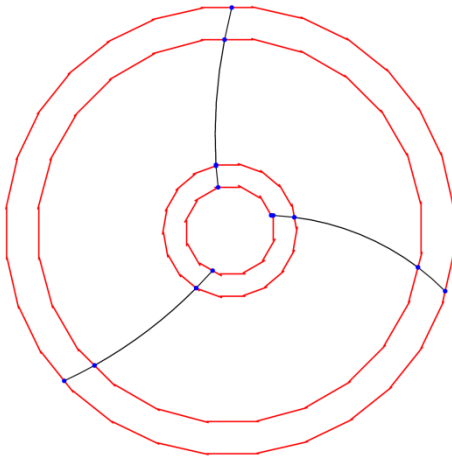


Monte Carlo study:

- Final detector geometry
- Geant4 full detector simulation
- Track reconstruction with Multiple Scattering fit
- Different beam intensities

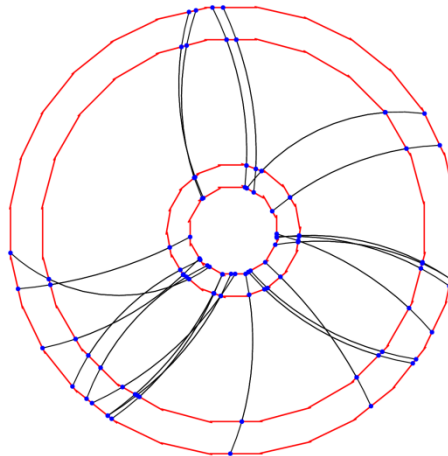
Ia: beam $10^7 \mu^+$ /s:

- 3 track candidates/frame
- fake candidates $\sim 5\%$



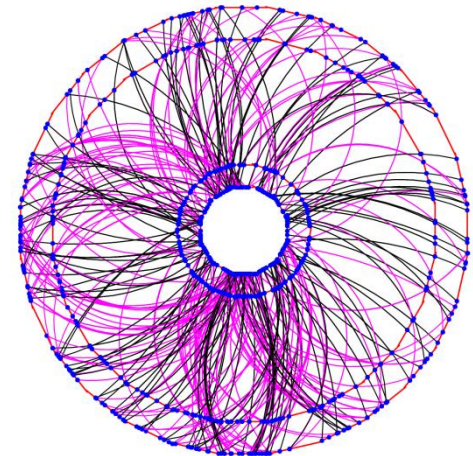
Ib: beam $10^8 \mu^+$ /s:

- 30 candidates/frame
- fake candidates $\sim 5\%$



II: Beam $2 \cdot 10^9 \mu^+$ /s:

- 300 track candidates/frame
- $\sim 50\%$ fake candidates



Performance



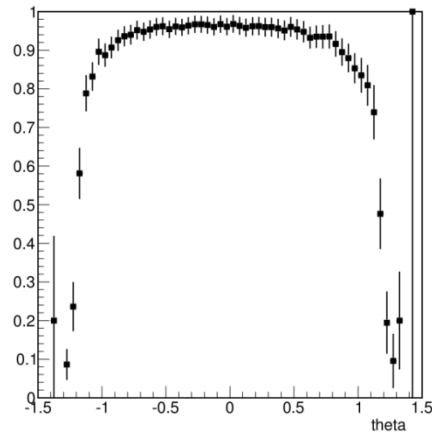
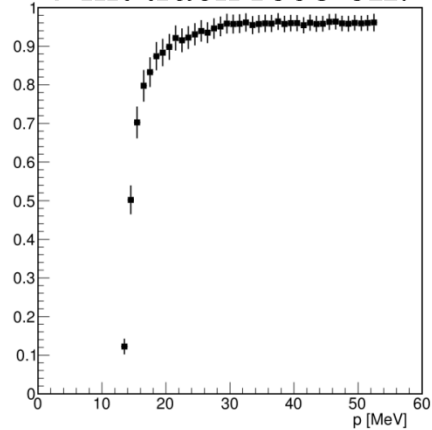
Good reconstruction efficiency:

- **90-95%** for 4-hit and 6-hit tracks
- Defined by χ^2 cuts

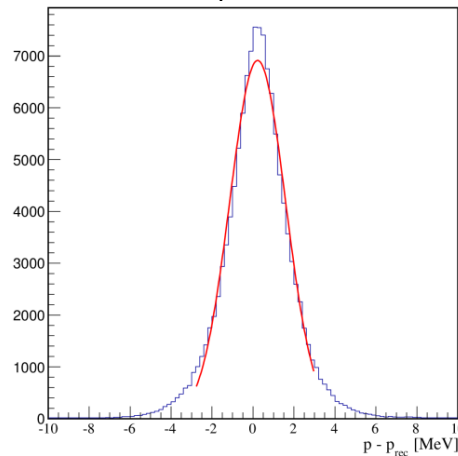
Momentum resolution:

- **1.5 MeV** for triplets (layers 1,2,3)
- **0.2 MeV** for 6-hit tracks (recurlers)

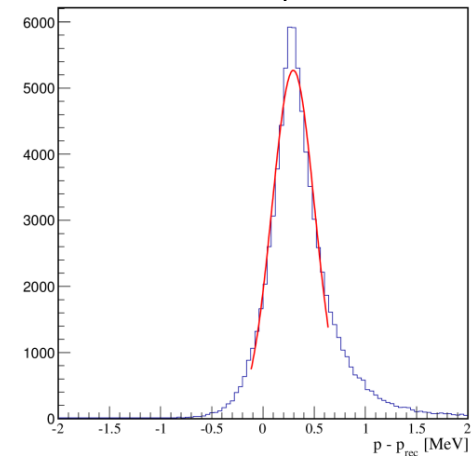
4-hit track reco eff.



Triplets: $\sigma_p \approx 1.5$ MeV



6-hit tracks: $\sigma_p \approx 0.2$ MeV



Note: no correction for energy loss

GPU event filter farm



Readout (FPGA):

- Directly copy data (DMA) to GPU
- High parallelism but limited memory
- Sort/group hits (time, geometry)
- Simple pre-selections

Filter Farm (GPU):

- Find 3 triplets/4-hit tracks & Fit vertex
 - Process all combinations of hits from first 3 layers
- For each frame give decision (write/drop)
- Main limitations:
 - Slow memory access
 - Total bandwidth

GPU reconstruction/performance



- First implementation of GPU reconstruction
- **Result: ~10G triplet combinations per second**

	Low beam intensity (phase Ib, $10^8 \mu^+/s$)	High intensity (phase II, $2 \cdot 10^9 \mu^+/s$)
Number of hits per layer	50-100	200-500
Number of combinations per 50 ns frame	100K-1M	10M-100M
Single GPU reconstruction performance [frames/s]	50K	500
Filter Farm (48 GPU units) [frames/s]	2.5M	25K

- Current limitation: internal memory throughput
- Room for improvement:
 - Memory access pattern
 - FPGA pre-processing, associative memory
 - **Expect another factor 10 improvement**
 - But still factor 100 missing for phase II (work in progress)

Summary



Mu3e experiment:

- Search for LFV with 10^{16} muons (Br fraction at 10^{-16})
- HV-MAPS based silicon tracker
 - ~300M pixels
 - High precision & efficiency
 - Large data rates

Triplet fit for track fitting in MS dominated environment

- Fast: O(1M) fits/s on CPU
- Algorithm easily portable to GPU
- Simple GPU implementation x100 faster than CPU

Work ongoing:

- Optimization of detector design
- Detector R&D (pixels, fibers, tiles)
- Optimization of GPU reconstruction
- Implementation of vertex fit on GPU

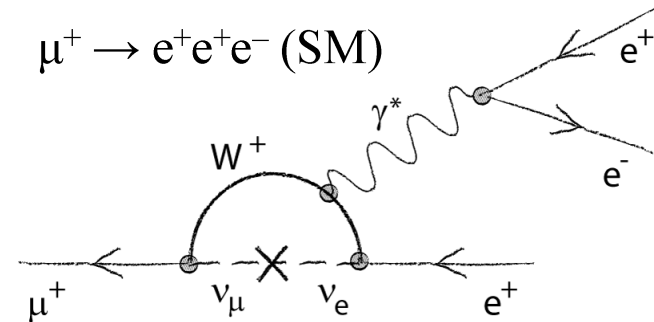
Backup



Lepton Flavor Violation



- There is no LFV in SM:
 - Neutrino mixing
 - Br ratio suppressed by 10^{50}
- Can be enhanced in SUSY, GUT, EDIM, extended Higgs models, etc.
- Current experimental status:
 - SINDRUM (PSI, 1988):
 - $\text{Br}(\mu^+ \rightarrow e^+e^+e^-) < 10^{-12}$
- Search for $\mu \rightarrow 3e$:
 - Test of current models where LFV is expected
 - Complementary to other searched ($\mu \rightarrow e\gamma$, etc.)
- To set limit at the level of $O(10^{-15})$:
 - Need at least 10^{16} muon decays



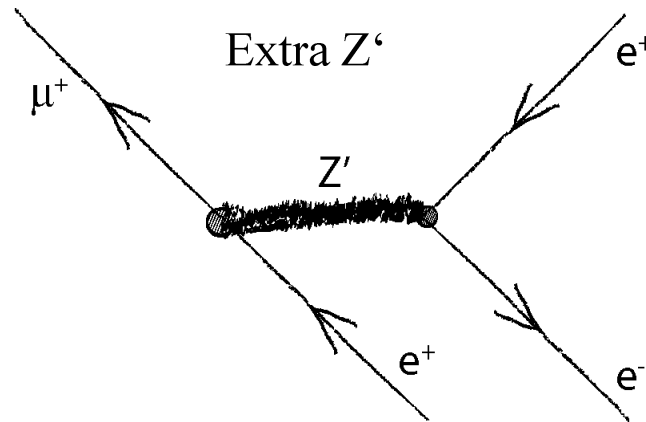
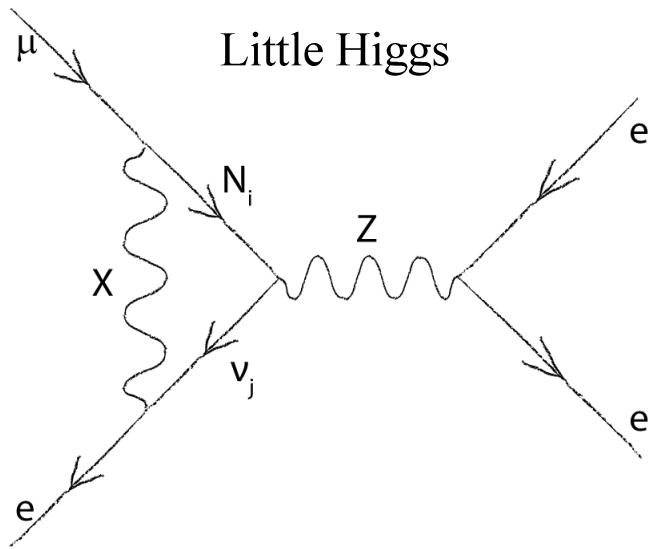
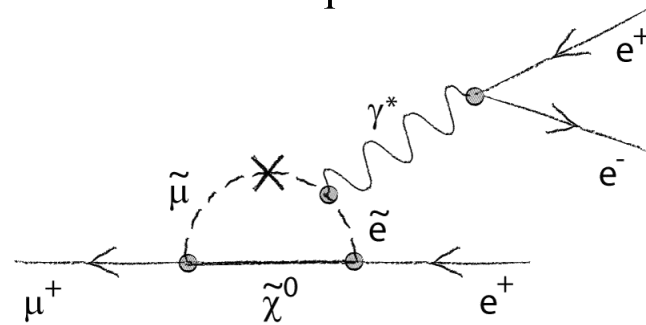
Lepton Flavor Violation



Other models:

- SUSY and other BSM models
- GUT models (leptoquarks)
- Extended Higgs models
- Extra dimensions
- New heavy bosons
- Many other models

SUSY loop

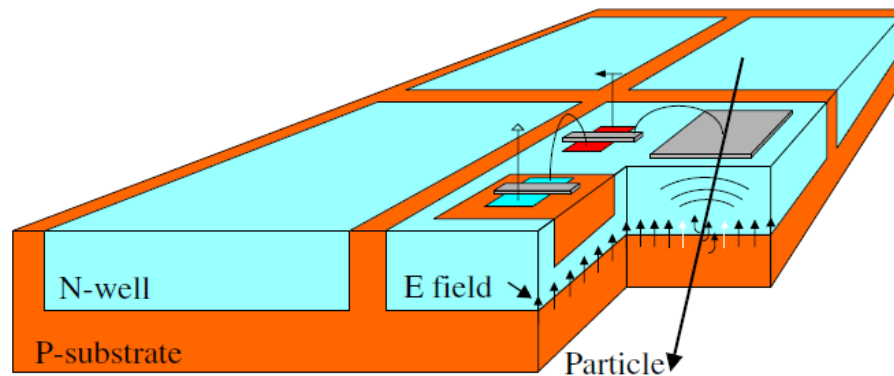


HV-MAPS



High Voltage Monolithic Active Pixel Sensor:

- HV CMOS technology
- N-well in p-substrate
- Reverse bias $\approx 60V$
- Charge collection via drift
- Fast: < 1 ns charge collection
- Thinned down to $50 \mu m$
- Integrated readout electronics



MuPix chip prototype

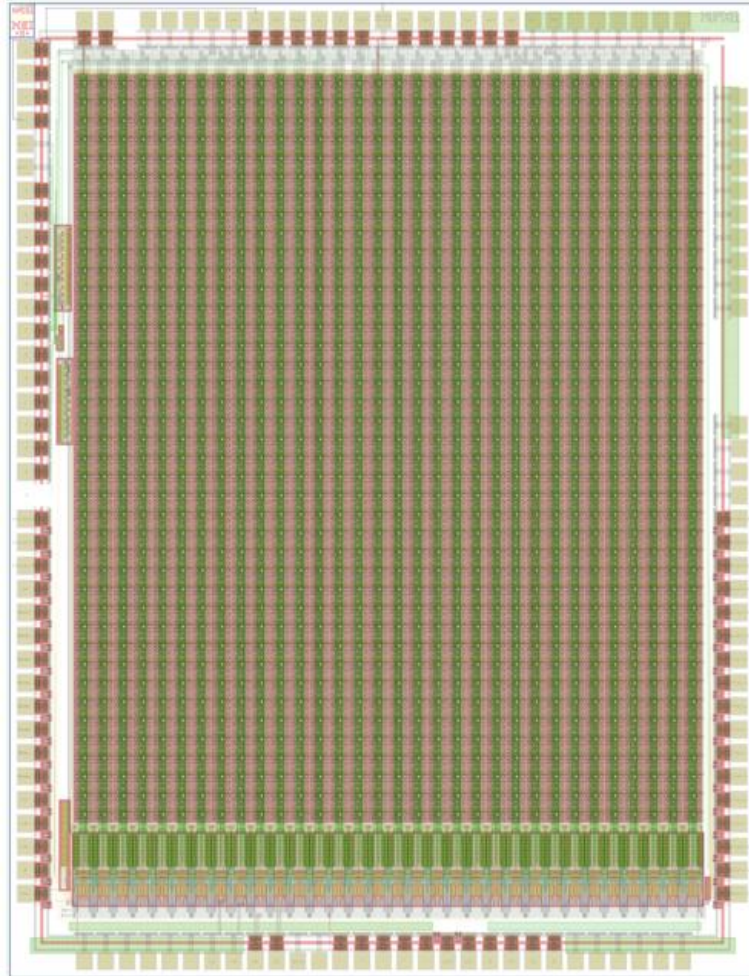


MuPix4:

- 180 nm HV-CMOS
- Matrix:
 - 40x32 pixels
 - pixel size: $98 \times 80 \mu\text{m}^2$

MuPix6:

- Matrix:
 - 40x32 pixels
 - pixel size: $103 \times 80 \mu\text{m}^2$

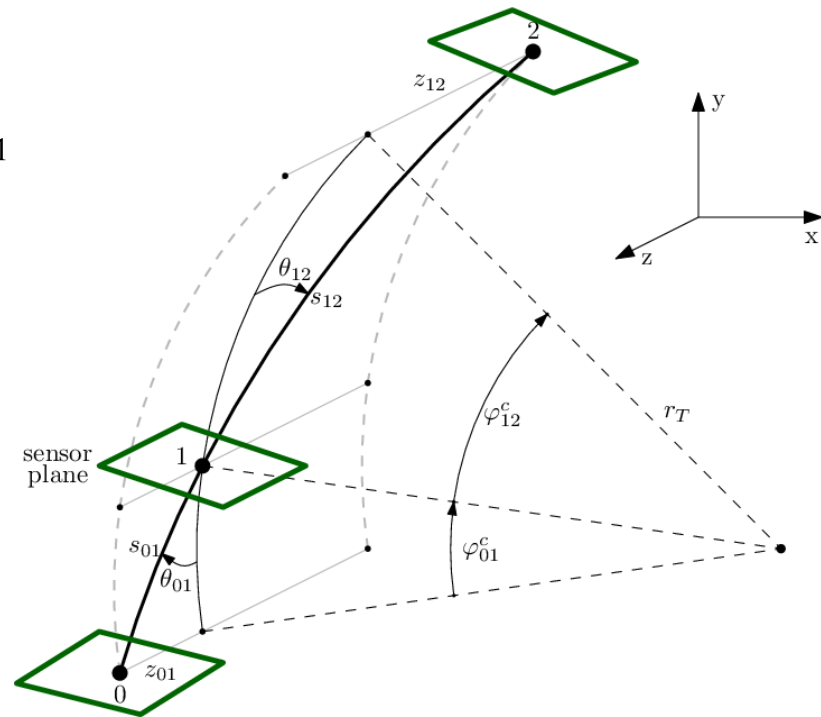


Triplet fit



First step:

- Start with circle solution in XY-plane (hit triplet 012)
 - transverse radius: r_T
 - $r_T = r_{T01} = r_{T12}$
- r_T, z_{01}, z_{12} :
 - path lengths in 3D: s_{01} & s_{12}
 - 3D radii:
 - $r_{01} = r_{T01} / \cos(\theta_{01})$
 - helix angles: θ_{01} & θ_{12}
 - MS angle $\theta_{MS} = \theta_{12} - \theta_{01}$
- Note:
 - MS angle $\varphi_{MS} = 0$
 - No energy conservation
 - $r_{01} \neq r_{12}$



Triplet fit



Second step:

- Solving $r_T \cdot \sin(\varphi_{01}/2) = d_{01}/2$:
 - $d\varphi_{01} = \alpha_{01} \cdot dr_{01}$ & $d\varphi_{12} = \alpha_{01} \cdot dr_{01}$
 - $d\theta_{01} = \beta_{01} \cdot dr_{01}$ & $d\theta_{01} = \beta_{01} \cdot dr_{01}$
 - $2 \cdot \varphi_{MS} = \alpha_{12} \cdot (r - r_{12}) + \alpha_{01} \cdot (r - r_{01})$
- Fit:
 - vary $\mathbf{r} \Rightarrow$ changes r_{T01} , r_{T12} , etc.
 - minimize $\chi^2 = (\varphi_{MS}^2(r) + \theta_{MS}^2(r)) / \sigma_{MS}^2$

