



esipap...

European School of Instrumentation
in Particle & Astroparticle Physics

2-3 February 2014, Archamps

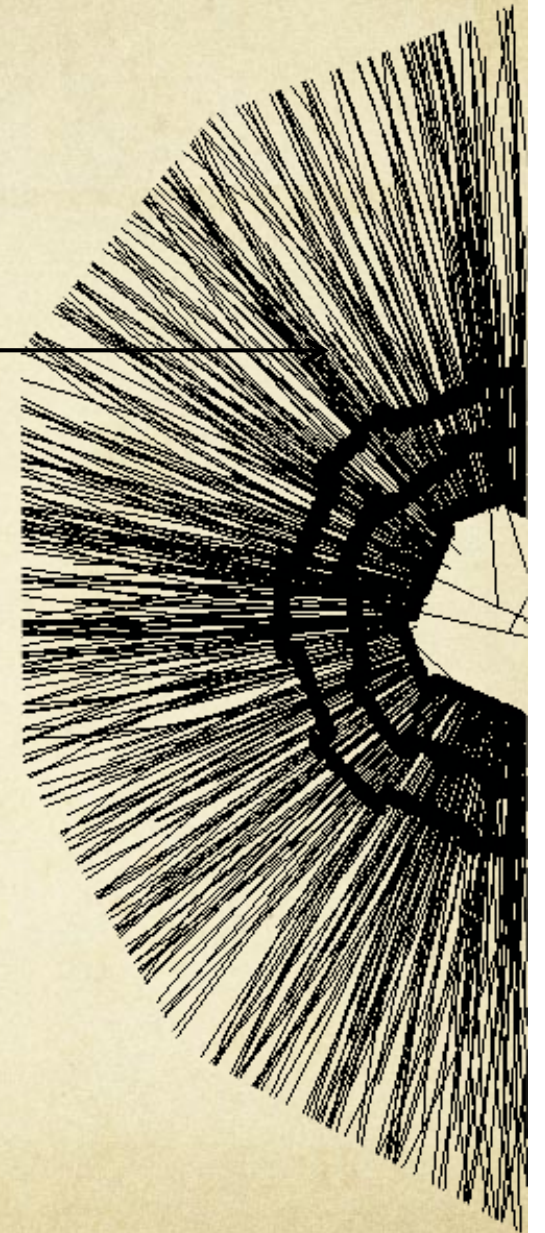
Tracking

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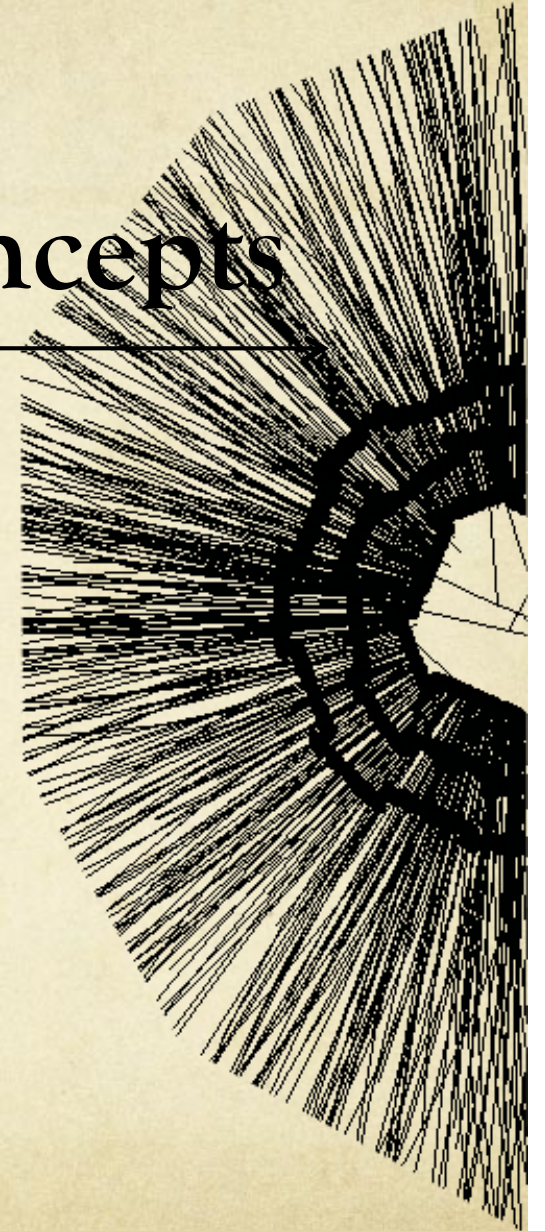
Lecture outline

1. Basic concepts
2. Position sensitive detectors
3. Standard algorithms
4. Advanced algorithms
5. Optimizing a tracking system
6. References



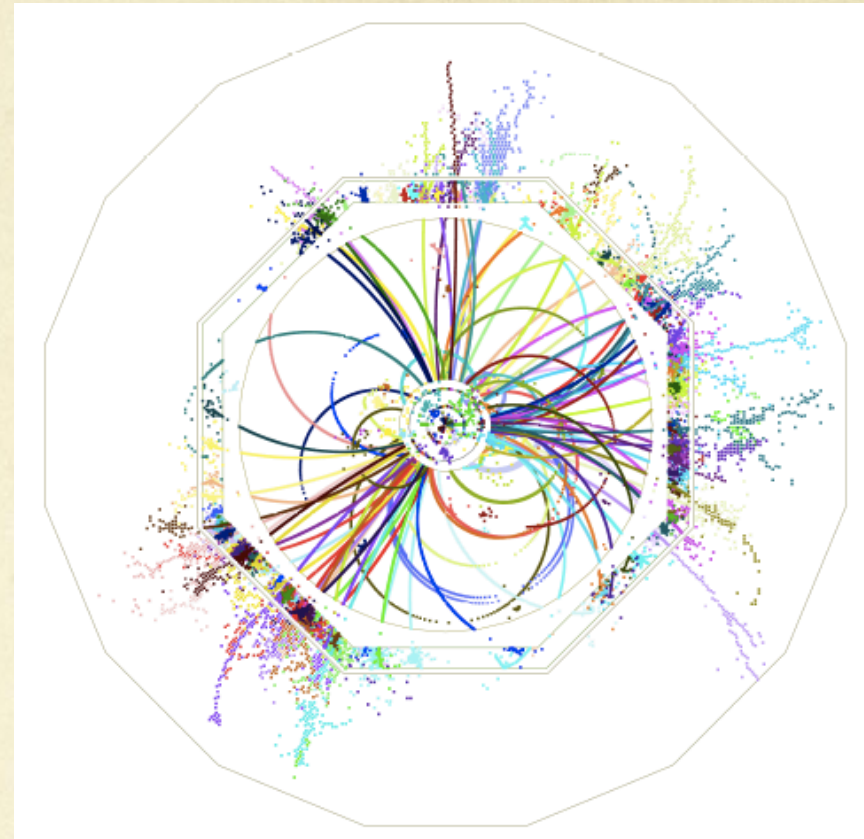
1. Motivations & basic concepts

- Motivations
- The 2 main tasks
- Environmental considerations



- Understanding an event
 - Individualize tracks \approx particles
 - Measure their properties
 - LHC: ~ 1000 particles per 25 ns “event”

- Track properties
 - Momentum
 - Reconstruct invariant masses
 - Energy
 - Mass \Leftrightarrow identification
 - Origin \Leftrightarrow vertexing (track merging)
 - Identify decays
 - Measure flight distance



8 jets event ($t\bar{t}h$) @ 1 TeV ILC

1. Motivations & Basic Concepts

Momentum measurement

○ Magnetic field curves trajectories $\frac{d\vec{p}}{dt} = q\vec{v} \times \vec{B}$

→ Rewritten with position (x) and path length (l) = basic equation $\frac{d^2\vec{r}}{d^2l} \propto \frac{q\vec{B}(\vec{x})}{\|\vec{p}\|} \frac{d\vec{r}}{dl}$

→ In B=4T a 1 GeV/c particle will get a sagitta of 1.5 mm

○ Fixed-target experiments

- Dipole magnet
- Measurement of deflection (angle variation)

○ Collider experiment

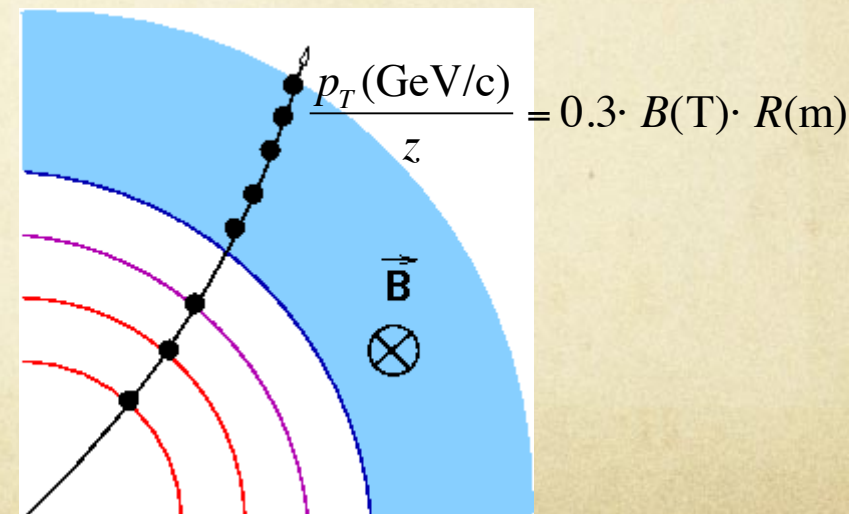
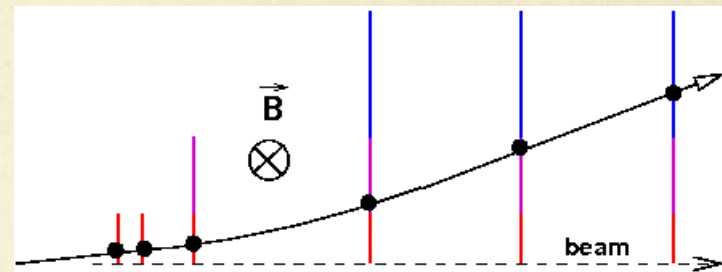
- Barrel-type with axial B
- Measurement of curvature (sagitta)

○ Other arrangements

- Toroidal B... not covered

○ **Two consequences**

- Position sensitive detectors needed
- Any perturbation effects on trajectories is a pain



Multiple scattering - 1/2

○ Reminder on the physics (see other courses)

- Coulomb scattering mostly on nuclei
- Molière theory description as a **centered** gaussian process
 - the thinner the material, the less true → large tails

○ In-plane description (defined by vectors \mathbf{p}_{in} , \mathbf{p}_{out})

- Corresponds to (ϕ, θ) with $\mathbf{p}_{in} = \mathbf{p}_z$ and $p_{out}^2 = p_{out,z}^2 + p_{out,T}^2$

$$\begin{cases} p_{out,z} \cos\theta \approx p_{out,z} \\ p_{out,T} \sin\theta \approx p_{out,T} \end{cases}$$

$$\sigma_\theta = \frac{13.6 \text{ (MeV/c)}}{\beta p} \cdot z \cdot \sqrt{\frac{\text{thickness}}{X_0}} \cdot \left[1 + 0.038 \ln\left(\frac{\text{thickness}}{X_0}\right) \right]$$

○ In-space description (defined by fixed x/y axes)

- Corresponds to (θ_x, θ_y) with $p_{out,T}^2 = p_{out,x}^2 + p_{out,y}^2$

$$\begin{cases} p_{out,x} \sin\theta_x \approx p_{out,T} \theta_x \\ p_{out,y} \sin\theta_y \approx p_{out,T} \theta_y \end{cases} \Rightarrow \theta^2 = \theta_x^2 + \theta_y^2$$

- θ_x and θ_y are independent gaussian processes $\sigma_\theta^2 = \sigma_{\theta_x}^2 + \sigma_{\theta_y}^2$ and $\sigma_{\theta_y} = \sigma_{\theta_x} = \frac{\sigma_\theta}{\sqrt{2}}$

Multiple scattering - 2/2

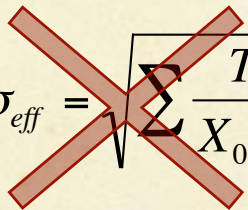
○ Important remark when combining materials

→ Total thickness $T = \sum T_i$, each material (i) with $X_0(i)$

→ Definition of effective radiation length $\Rightarrow X_{0,eff} = \frac{\sum T_i \times X_0(i)}{T}$

→ Consider single gaussian process $\sigma_{eff} \propto \sqrt{\frac{T}{X_{0,eff}}}$

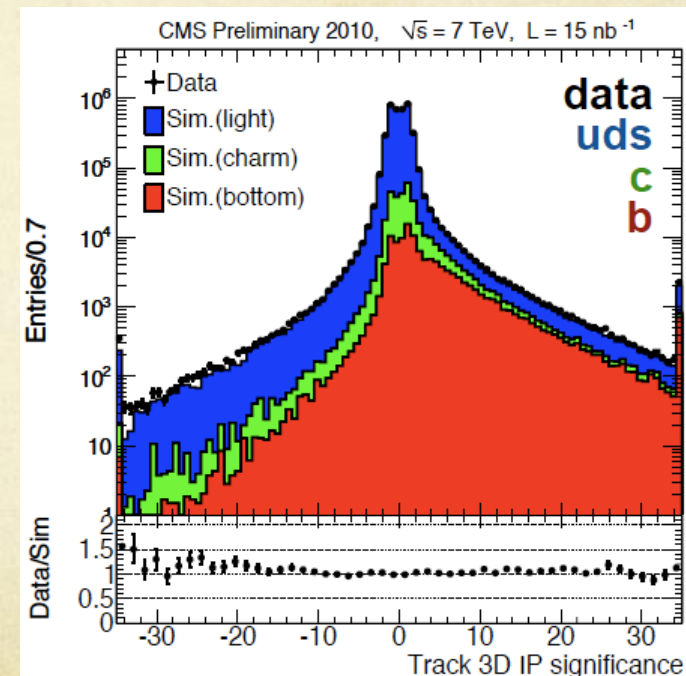
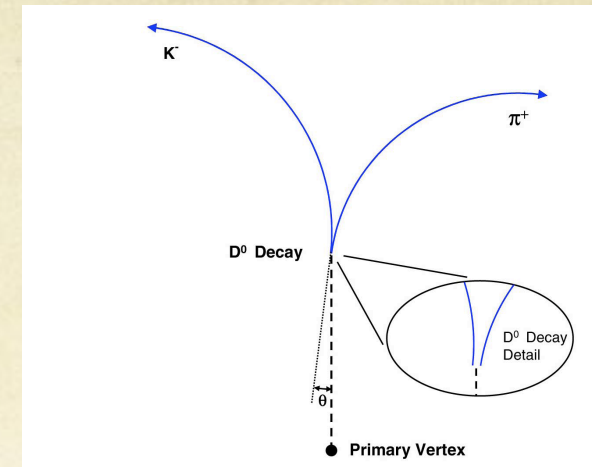
and never do variance addition

$$\sigma_{eff} = \sqrt{\sum \frac{T_i}{X_0(i)}}$$


1. Motivations & Basic Concepts

Vertexing

- Identifying through topology
 - Short-lived weakly decaying particles
 - Charm c $\tau \sim 120 \mu\text{m}$
 - Beauty b $\tau \sim 470 \mu\text{m}$
 - Exclusive reconstruction
 - Decay topology with secondary vertex
 - Inclusive reconstruction
 - Flavor tagging partly based on impact parameter
 - $\sigma_{\text{IP}} \sim 20\text{-}100 \mu\text{m}$ requested
- Finding the origin
 - Where did the collision did occur?
 - Primary vertex (could be multiple)
 - (life)Time dependent measurements
 - CP-asymmetries @ B factories ($\Delta z \approx 60\text{-}120 \mu\text{m}$)
- Remarks:
 - Usually no measurement below 1-2 cm / vertex
 - Requires extrapolation



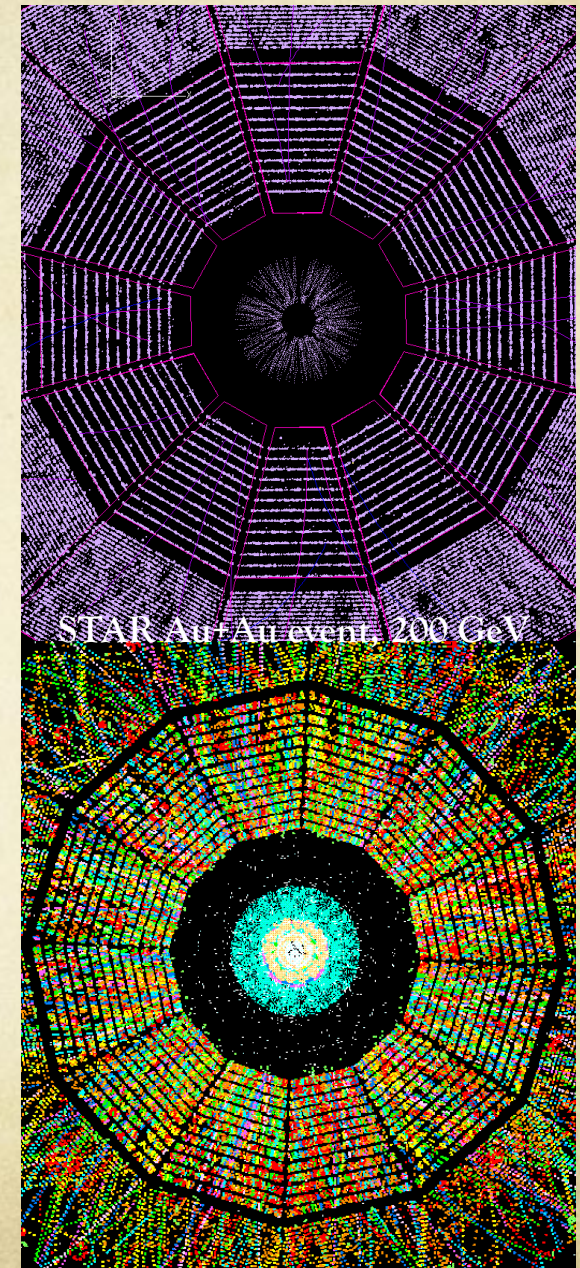
- Usually not a tracker task
 - CALORIMETERS (see lecture by Isabelle)
 - Indeed calorimeters gather material to stop particles while trackers try to avoid material (multiple scattering)
 - however...calorimetry tries to improve granularity
- Particle flow algorithm
 - LHC / ILC
- Energy evaluation by counting particles
 - Clearly heretic from calorimetry experts
 - Required to separate $E_{deposit}$ in dense environment
- Range measurement for low energy particles
 - Stack of tracking layers
 - Modern version of nuclear emulsion

NOT COVERED

1. Motivations & Basic Concepts

The two man tasks

- Basic inputs from detectors
 - Succession of 2D or 3D points (or track segments)
 - Who's who ?
- 2 steps process
 - Step 1: track identification = **finding** = pattern recognition
 - Associating a set of points to a track
 - Step 2: track **fitting**
 - Estimating trajectory parameters ➔ momentum
- Both steps require
 - **Track model** (signal, background)
 - Knowledge of **measurement uncertainties**
 - Knowledge of **materials traversed** (Eloss, mult. Scattering)
- Vertexing needs same 2 steps
 - Identifying tracks belonging to same vertex
 - Estimating vertex properties (position + 4-vector)



- Life in a real experiment is tough (for detectors of course)
 - Chasing small cross-sections → large luminosity and/or energy
 - Short interval between collisions
 - LHC: 25 ns
 - CLIC: 5 ns (but not continuous)
 - Large amount of particles → background, radiation
 - makes the finding more complicated
 - Vacuum could be required (space, very low momentum particles (CBM, LHCb))

- Radiation tolerance
 - Two types of energy loss
 - Ionizing (generate charges): dose in Gy = 100 Rad
 - Non-ionizing (generate defects in solid): fluence in $n_{\text{eq}}(1\text{MeV})/\text{cm}^2$
 - The more inner the detection layer, the harder the radiation (radius² effect)
 - Examples for most inner layers:
 - LHC: 10^{15} to $<10^{17}$ $n_{\text{eq}}(1\text{MeV})/\text{cm}^2$ with 50 to 1 MGy
 - ILC: $<10^{12}$ $n_{\text{eq}}(1\text{MeV})/\text{cm}^2$ with 5 kGy

○ Timing consideration

- Readout speed limits dead time
- Time resolution offers time-stamping of tracks
 - Tracks in one “acquisition event” could be associated to their proper collisions event if several have piled-up

○ Heat concerns

- Spatial resolution → segmentation
- Readout speed → power dissipation/channel
- Efficient cooling techniques exist BUT add material budget and may not work everywhere (space)

} Hot cocktail!

○ Conclusion

- Tracker technology driven by environmental conditions: hadron colliders (LHC)
- Tracker technology driven by physics performances: lepton colliders (B factories, ILC)
- Of course, some intermediate cases: superB factories, CLIC

○ For detection layer

- Detection efficiency
 - Mostly driven by Signal/Noise
 - Note: Noise = signal fluctuation \oplus readout (electronic) noise
- Intrinsic spatial resolution
 - Driven by segmentation (not only)
 - Useful tracking domain $\sigma < 1\text{mm}$
- Material budget
- “Speed” (integration time, count rate, ...)

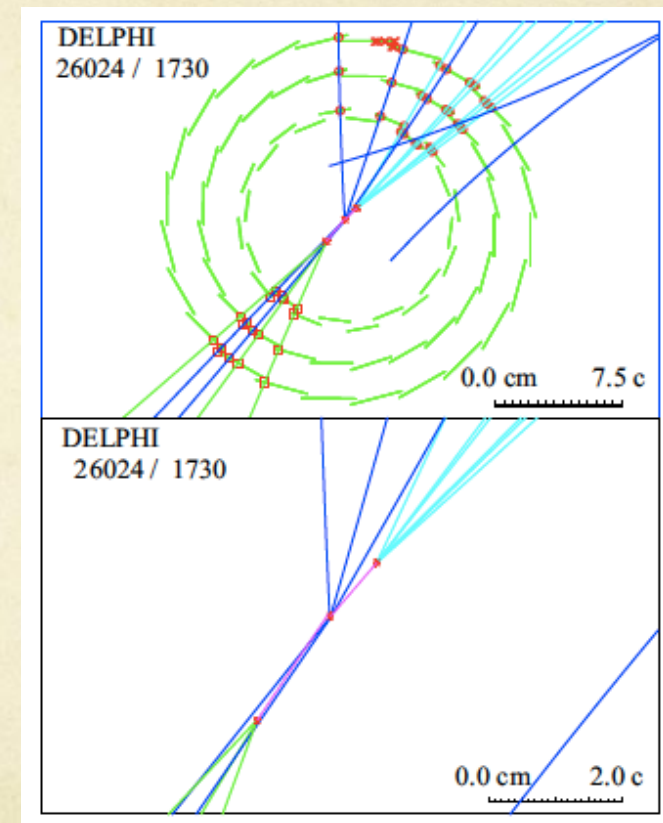
○ Two-track resolution

- Ability to distinguish to nearby trajectories
- Mostly governed by signal spread

○ Momentum resolution $\frac{\sigma(p)}{p}$

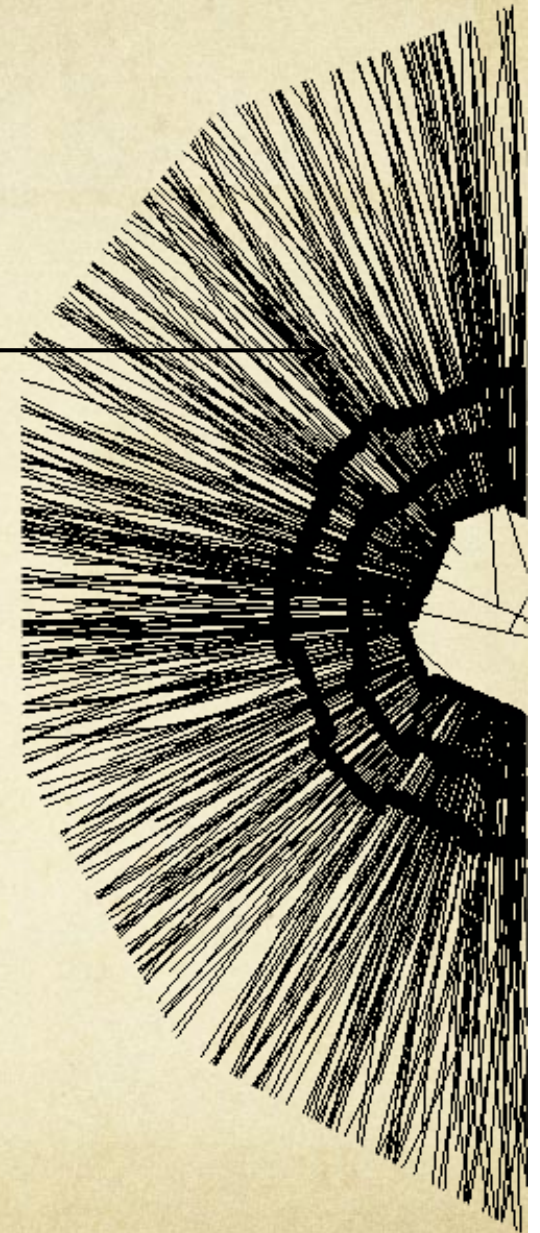
○ Impact parameter resolution

- Sometimes called “distance of closest approach” to a vertex



2. Detection technologies

- Intrinsic resolution
- Single layer systems
 - Silicon, gas sensors
- Multi-layer systems
 - Drift chamber and TPC
- Tentative comparison
- Magnets
- Leftovers



1. Motivations & Basic Concepts:

Intrinsic resolution

○ Position measurement comes from segmentation

→ Pitch

○ Digital resolution $\sigma = \frac{\text{pitch}}{\sqrt{12}}$

○ Improvement from signal sharing

→ Position = charge center of gravity

$$\sigma \propto \frac{\text{pitch}}{\text{signal/noise}}$$

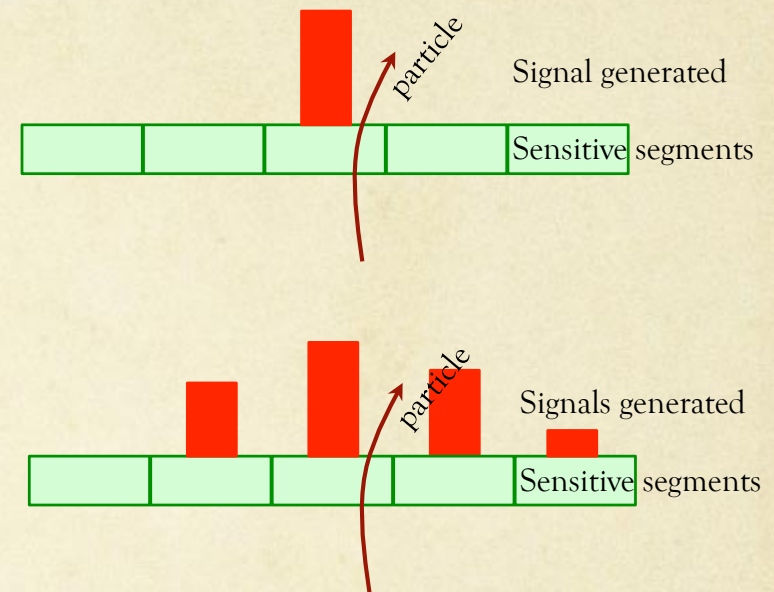
→ Effects generated by

- Secondary charges spread inside volume
- Inclined tracks (however, resol. limited at large angles)

→ Potential optimization segmentation / sharing

→ Warnings:

- Lorentz force from B mimick the effect
- counterproductive / 2-track resolution

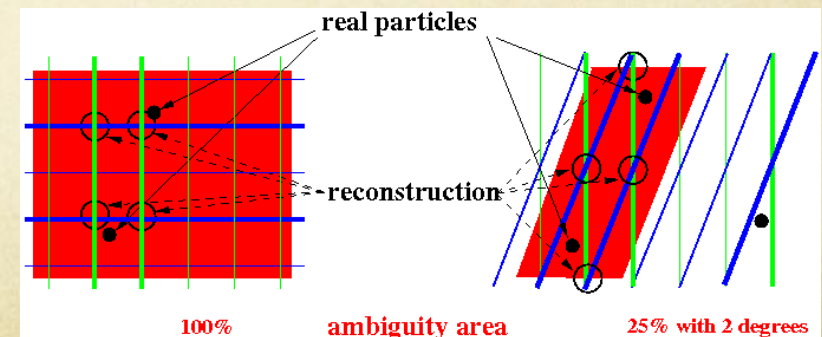
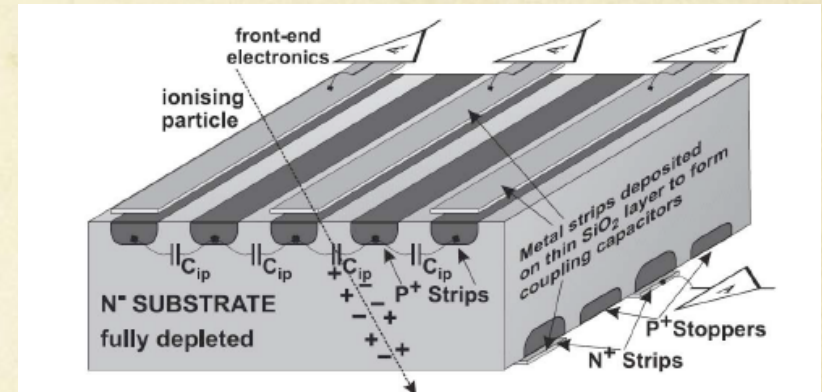


○ Basic sensitive element

- E-h pairs are generated by ionization in silicon
 - 3.6 eV needed
 - 300 μm thick Si generates ~ 22000 charges for MIP
BUT beware of Landau fluctuation
- Collection: P-N junction = diode
 - Depletion (10 to 0.5 kV)
generates a drift field (10^4 V/cm)
 - Collect time ~ 15 ps/ μm

○ Silicon strip detectors

- sensor “easily” manufactured
with pitch down to ~ 25 μm
- 1D if single sided
- Pseudo-2D if double-sided
 - Stereo-angle useful against ambiguities
- Difficult to go below 100 μm thickness

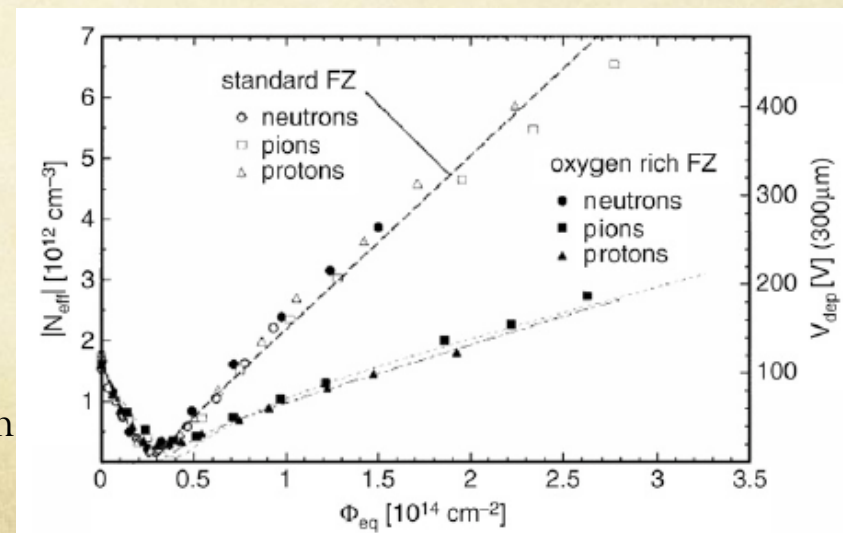
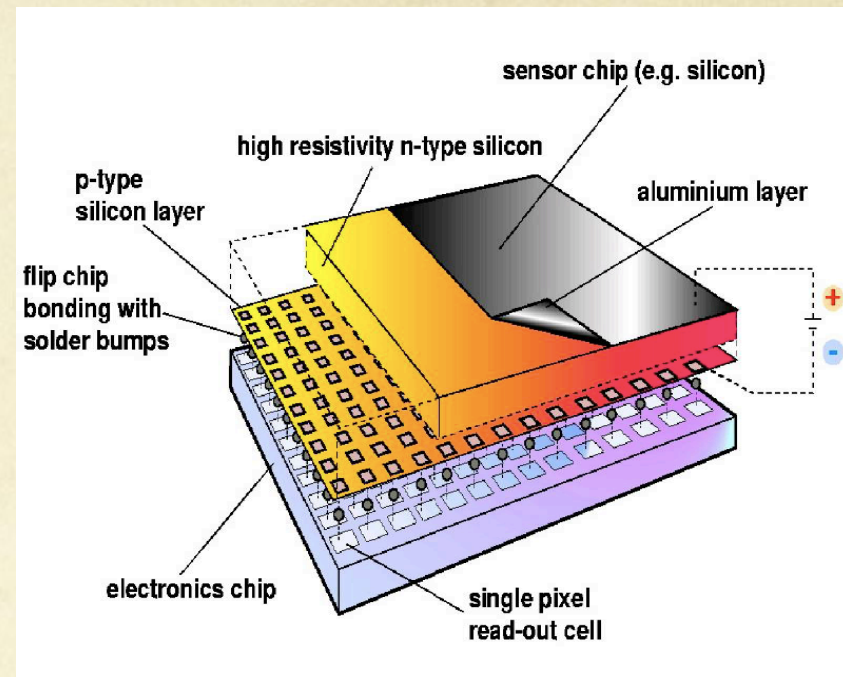


○ Concept

- Strips → pixels on sensor
- One to one connection from electronic channels to pixels

○ Performances

- Real 2D detector & keep performances of strips
 - Can cope with LHC rate (speed & radiation)
- Pitch size limited by physical connection and #transistors for treatment
 - minimal (today): $50 \times 50 \mu\text{m}^2$
 - typical: $100 \times 150 / 400 \mu\text{m}^2$
 - spatial resolution about $10 \mu\text{m}$
- Material budget
 - Minimal(today): $100(\text{sensor}) + 100(\text{elec.}) \mu\text{m}$
- Power budget: $10 \mu\text{W}/\text{pixel}$



2. Detector Technologies:

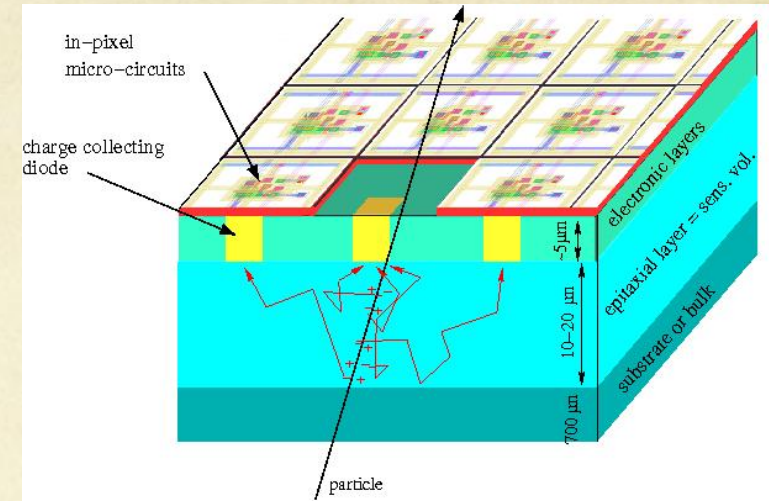
CMOS Pixel Sensor

○ Concept

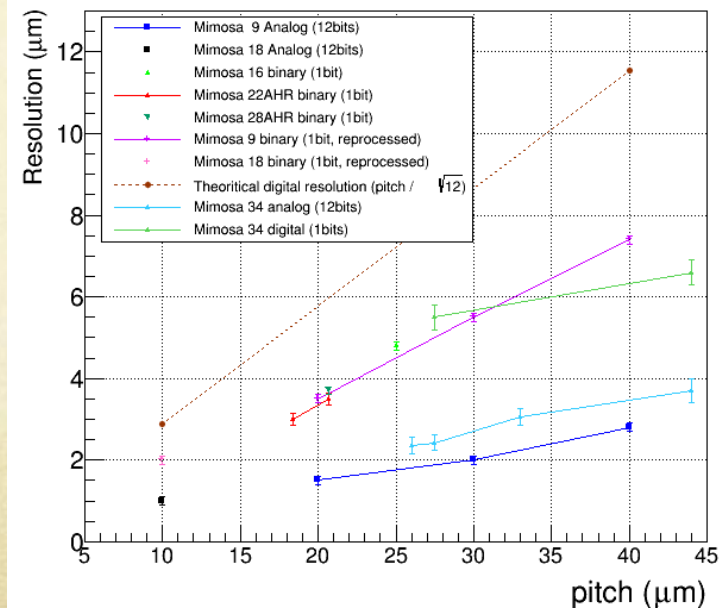
- Use industrial CMOS process
 - Implement an array of sensing diode
 - Amplify the signal with transistors near the diode
- Gain in granularity: pitch down to $\sim 10 \mu\text{m}$
- Gain in sensitive layer thickness $\sim 10\text{-}20 \mu\text{m}$
- BEWARE: depletion not systematically available
 - Slow (100 ns) thermal drift

○ Performances

- Spatial resolution 1-10 μm (in 2 dimensions)
- Material budget: $\lesssim 30 \mu\text{m}$
- Power budget: 1-5 $\mu\text{W}/\text{pixel}$
- Integration time $\sim 50\text{-}100 \mu\text{s}$ demonstrated
 - 1 μs in development



Mimosa resolution vs pitch

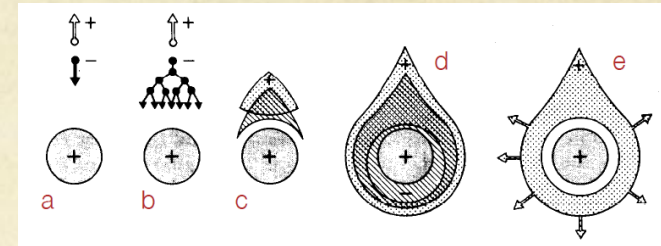


2. Detector Technologies:

Wire chambers

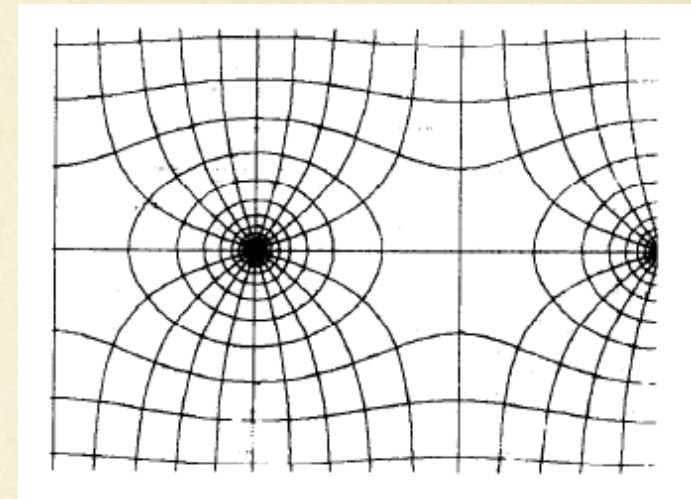
○ Basic sensitive element

- Metallic wire, 1/r effect generated an avalanche
- Signal depends on gain (proportional mode) typically 10^4
- Signal is fast, a few ns



○ Gas proportional counters

- Multi-Wire Proportional Chamber
 - Array of wires
 - 1 or 2D positioning depending on readout
 - Wire spacing (pitch) limited to 1-2 mm
- Straw or drift tube
 - One wire in One tube
 - Extremely fast (compared to Drift Chamber)
 - Handle high rate
 - Spatial resolution $<200 \mu\text{m}$
 - Left/right ambiguity



Electric fields line
around anode wires

2. Detector Technologies:

Wire chambers “advanced”

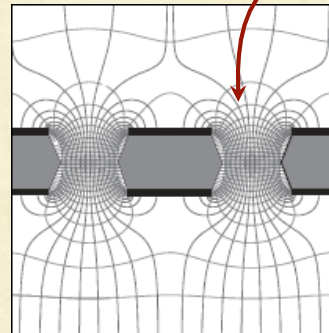
○ Micro-pattern gas multipliers

→ MSGC

- Replace wires with lithography micro-structures
- Smaller anodes pitch 100-200 μm
- BUT Ageing difficulties due to high voltage and manufacturing not so easy

→ GEM

- Gain 10^5
- Hit rate 10^6 Hz/cm^2

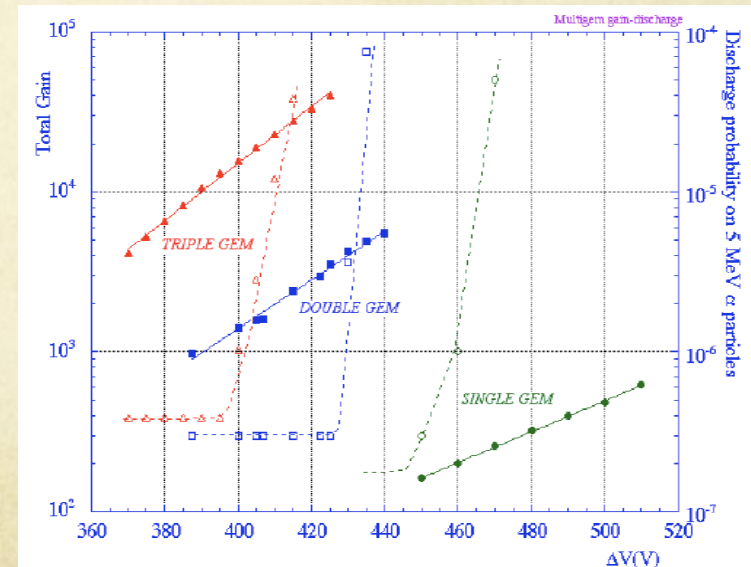
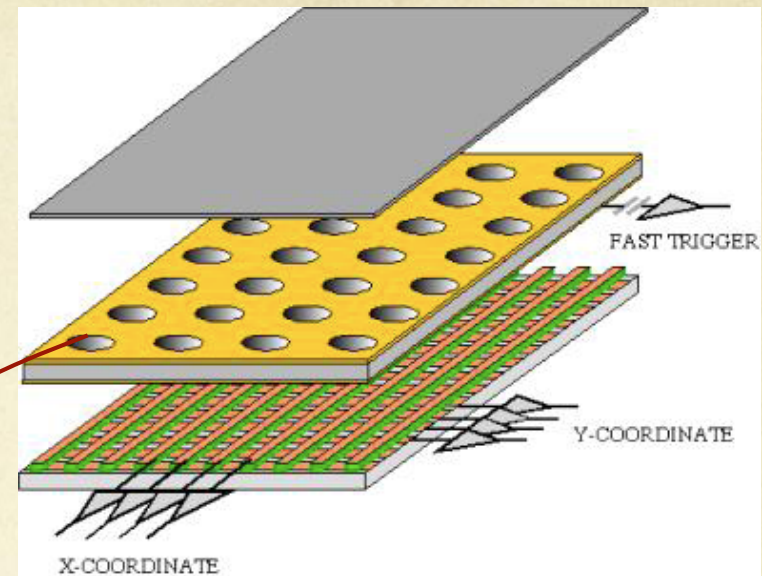


→ MICROME GAS

- Even smaller distance anode-grid
- Hit rate 10^9 Hz/cm^2

→ More development

- Electron emitting foil working in vacuum!



2. Detector Technologies:

Drift chambers

○ Basic principle

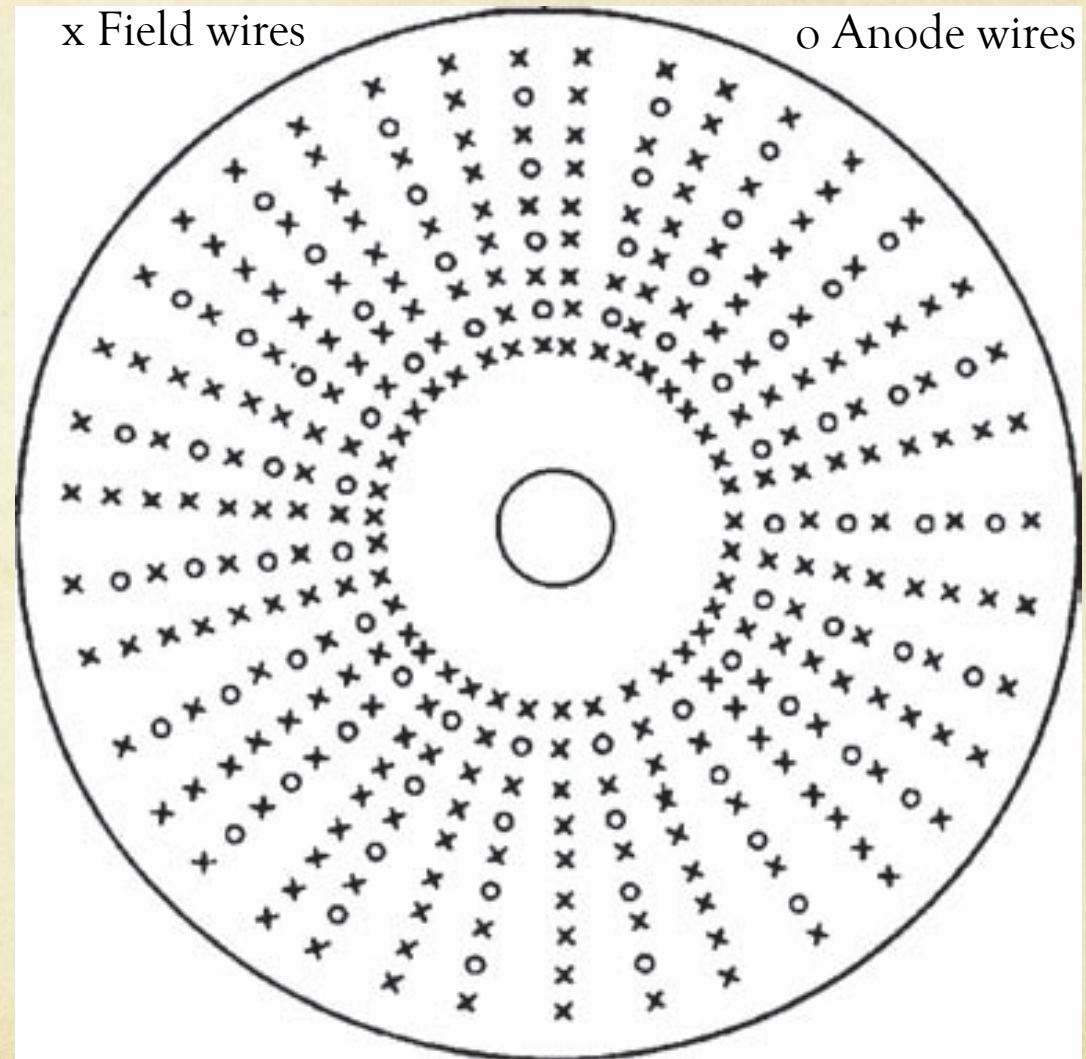
- Mix field and anode wires
 - Generate a drift
- Pressurize gas to increase charge velocity (few atm)
- 3D detector
 - 2D from wire position
 - 1D from charge sharing at both ends

○ Spatial Resolution

- Related to drift path
$$\sigma \propto \sqrt{\text{drift length}}$$
- Typically 100-200 μm

○ Remarks

- Could not go to very small radius

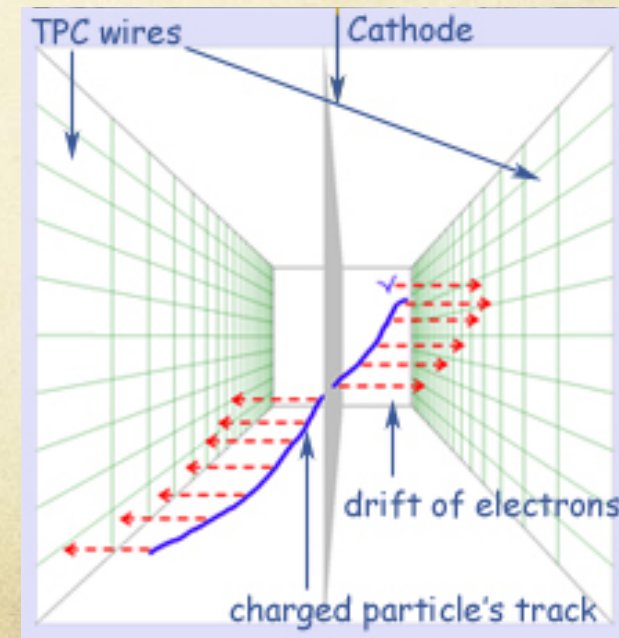
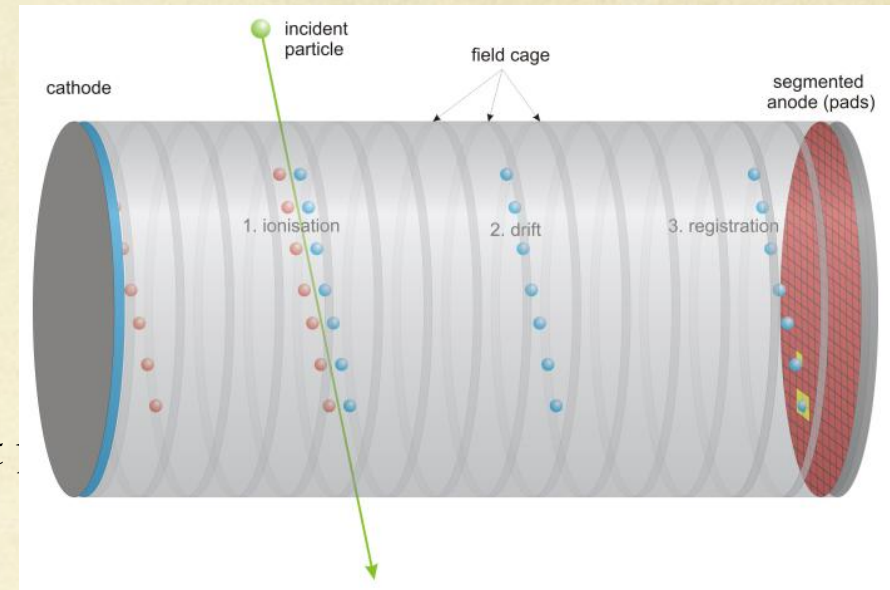


○ Benefits

- Large volume available
- Multi-task: tracking + Part. Identification

○ Basic operation principle

- Gas ionization → charges
- Electric field → charge drift along straight
- End cap readout
 - wire proportional chamber - type
- Information collected
 - 2D position of charges at end-cap
 - 3rd dimension from drift time
 - Energy deposited from #charges
- Different shapes:
 - rectangles (ICARUS)
 - Cylinders (colliders)
 - Volumes can be small or very large

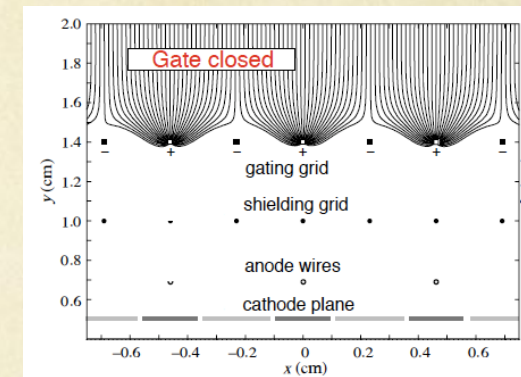
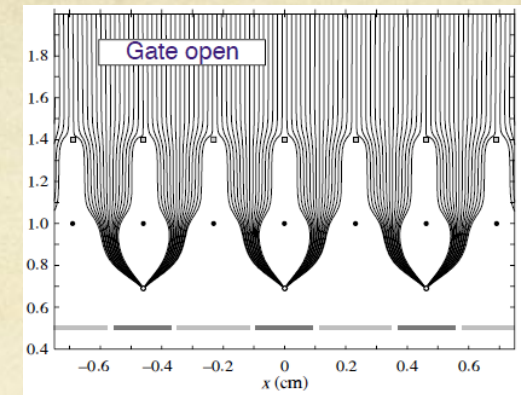


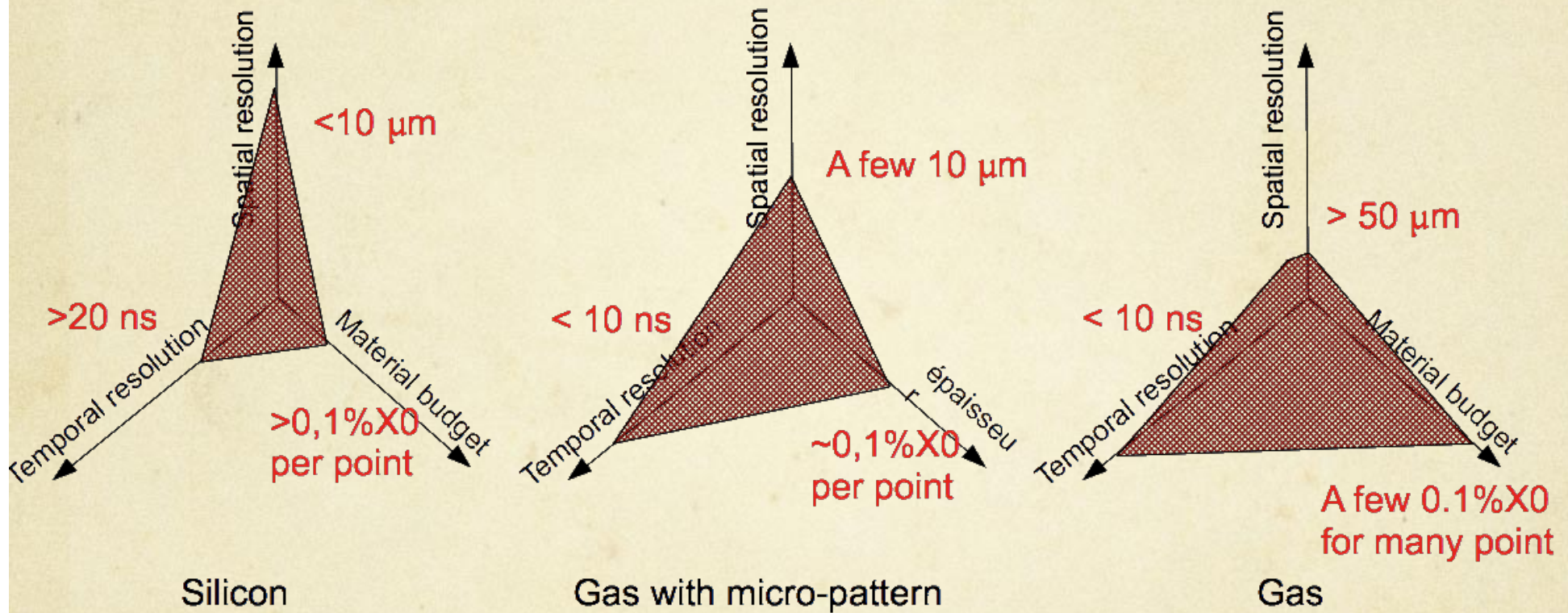
Time Projection Chambers 2/2

○ End cap readout

○ Performances

- Two-track resolution $\sim 1\text{cm}$
- Transverse spatial resolution $\sim 100 - 200\ \mu\text{m}$
- Longitudinal spatial resolution $\sim 0.2 - 1\ \text{mm}$
- Longitudinal drift velocity: 5 to 7 cm/ μs
 - ALICE TPC (5m long): 92 μs drift time
 - Limiting usage with respect to collision rate





○ Solenoid

- Field depends on current I , length L , # turns N
 - on the centerline
$$B = \frac{\mu_0 NI}{\sqrt{L^2 + 4R^2}}$$
 - Typically: 1 T needs 4 to 8 kA → **superconducting** metal to limit heat
- Field uniformity needs flux return (iron structure)
 - Mapping is required for fitting (remember $B(\mathbf{x})$?)
 - Usually performed with numerical integration
- Calorimetry outside → limited material → **superconducting**
- Fringe field calls for compensation

	Field (T)	Radius (m)	Length (m)	Energy (MJ)
ALICE	0.5	6		150
ATLAS	2	2.5	5.3	700
CMS	4	5.9	12.5	2700
ILC	4	3.5	7.5	2000

○ Superconduction

- cryo-operation → quenching possible !
- Magnetic field induces energy: $E \propto B^2 R^2 L$
 - Cold mass necessary to dissipate heat in case of quench

- From a detection principle to a detector
 - Build large size or many elements
 - Manufacture infrastructures
 - Characterization capabilities
 - Production monitoring
 - Integration in the experiment
 - Mechanical support
 - Electrical services (powering & data transmission)
 - Cooling (signal treatment dissipates power)
 - Specific to trackers
 - Internal parts of multi-detectors experiment → limited space
 - Material budget is ALWAYS a concern
 - ⇔ trade-offs required

○ Silicon drift detectors

- Real 2D detectors made of strips
- 1D is given by drift time

○ Diamond detectors

- Could replace silicon for hybrid pixel detectors
- Very interesting for radiation tolerance

○ Plasma sensor panels

- Derived from flat television screen
- Still in development

○ Charge Coupled Devices (CCD)

- Fragile/ radiation tolerance

○ Signal generation

- see Ramo's theorem

○ DEPFET

- Depleted Field Effect Transistor detector
- Real 2D and partly monolithic

○ Nuclear emulsions

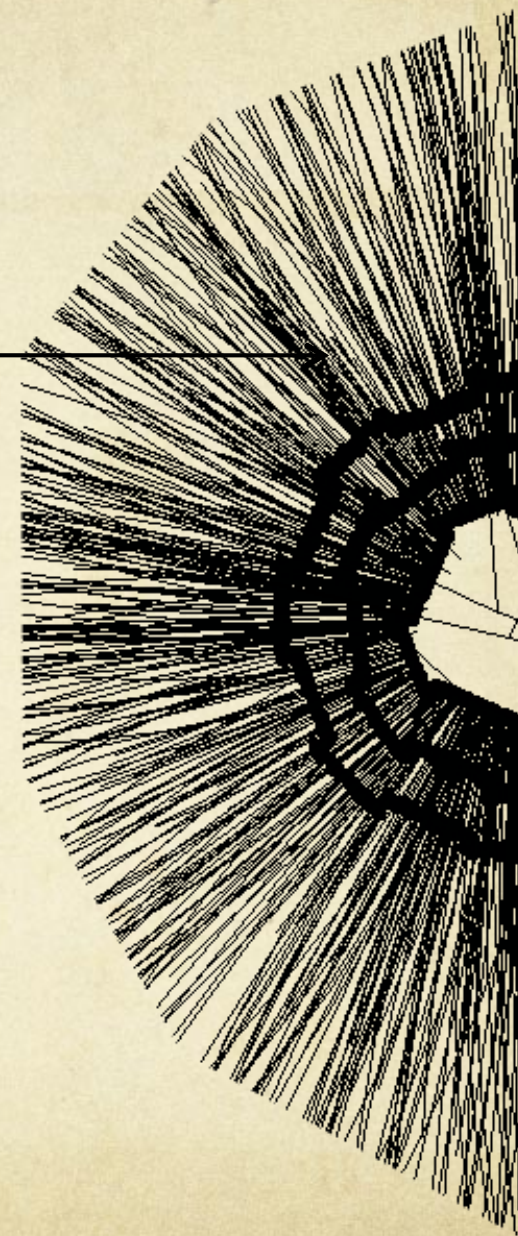
- One of the most precise $\sim 1\mu\text{m}$
- No timing information → very specific applications

○ Scintillators

- Extremely fast (100 ps)
- Could be arranged like straw tubes
- But quite thick ($X_0 \sim 2\text{ cm}$)

3. Standard algorithms

- Finders
- First evaluation of momentum resolution
- Fitters
- Alignment



○ Global methods

- Transform the coordinate space into pattern space
 - “pattern” = parameters used in track model
- Identify the “best” solutions in the new phase space
- Use all points at a time
 - No history effect
- Well adapted to evenly distributed points with same accuracy

○ Local methods

- Start with a track seed = restricted set of points
- Then extrapolate to next layer-point
 - And so on...**iterative procedure**
- “Wrong” solutions discarded at each iteration
- Possibly sensitive to “starting point”
- Well adapted to redundant information

**FINDING drives
tracking efficiency**

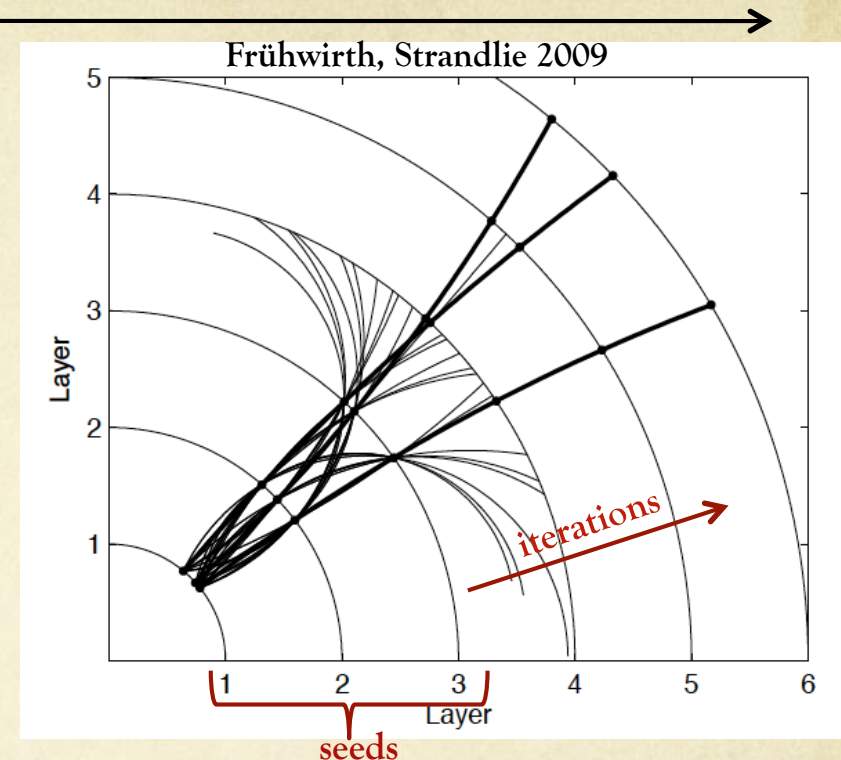
3. Reconstruction algorithm:

Local method

- Track seed = initial segment
 - Made of few (2 to 4) points
 - One point could be the expected primary vtx
 - Allows to initialize parameter for track model
 - Farther from primary interaction
 - At lowest density
 - Limit mixing points from different tracks
 - Variant: choose inner layers first to benefit from precision

○ Extrapolation step

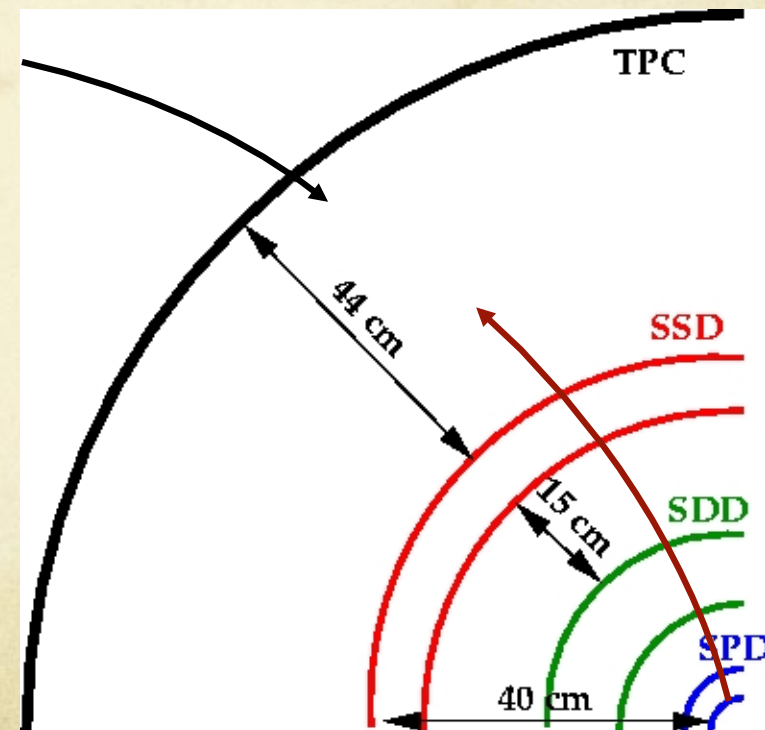
- Usually inward (toward primary vtx) onto the next layer
- Not necessarily very precise, especially **only local model** needed
 - Extrapolation uncertainty \lesssim layer point uncertainty
 - Computation speed important
- Match (associate) nearest point on the new layer
 - Might skip the layer if point missing
 - Might reject a point on 2 basis



3. Reconstruction algorithm:

Local method

- Variant with track segments
 - First build “tracklets” on natural segments
 - Sub-detectors, or subparts with same resolution
 - Then match segments together
 - Typical application:
 - Segments large tracker (TPC) with vertex detector (Si)
 - layers dedicated to matching
- Variant with track roads
 - Full track model used from start
- Variant with Kalman filter
 - See later



3. Reconstruction algorithm:

Global methods

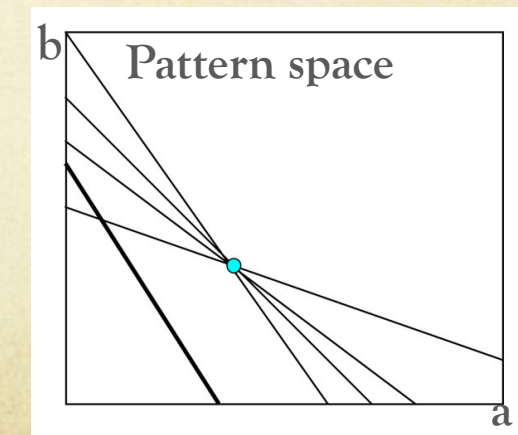
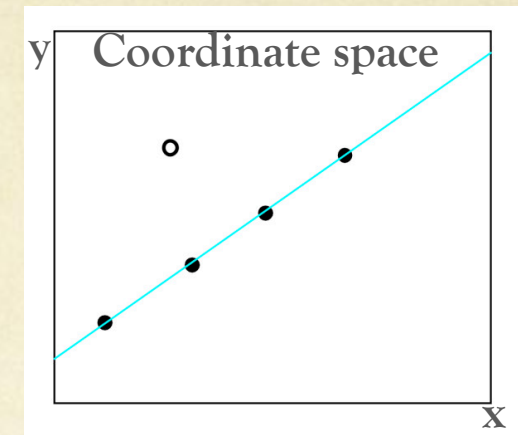
○ Brute force = combinatorial way

- Consider all possible combination of points to make a track
- Keep only those compatible with model
- Usually too time consuming...

○ Hough transform

→ Example straight track:

- Coord. space $y = a*x + b \Leftrightarrow$ pattern space $b = y - x*a$
- Each point (y,x) defines a line in pattern space
- All lines, from points belonging to same straight-track, cross at same point (a,b)
- In practice:
discretize pattern space and search for maximum
- Applicable to circle finder
 - needs two parameters as well $(r, \phi$ of center)
if track is assumed to originate from $(0,0)$
- More difficult for more than 2 parameters...



3. Reconstruction algorithm:

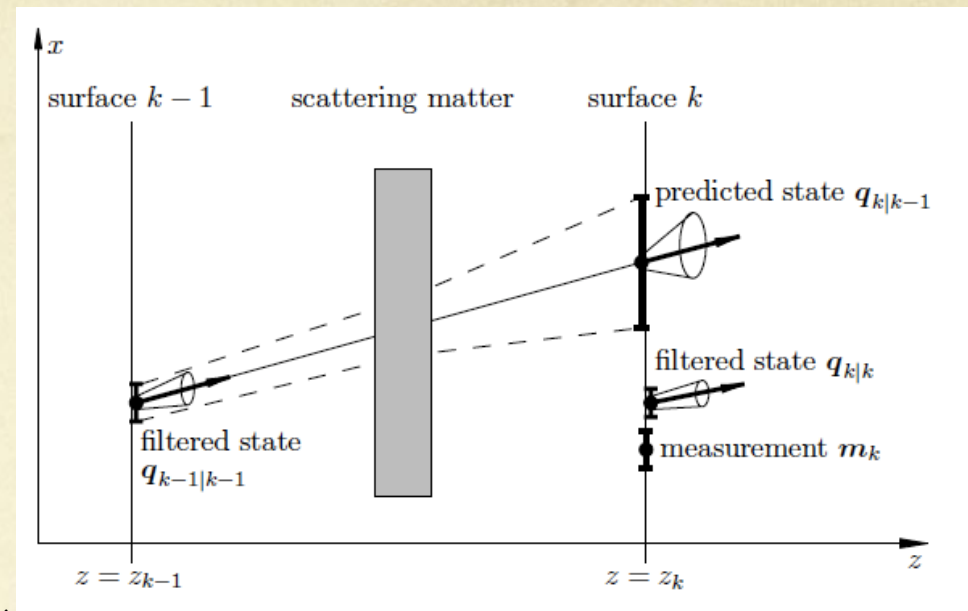
FITTING

○ Why do we need to fit?

- Measurement error
- Multiple scattering error

○ Recursive method (linear χ^2 and Kalman filter)

- Start from an initial set of parameters:
- Propagate to next layer:
 - New parameters
 - AND new covariance matrix
- Update the covariance matrix with additional uncertainties from
 - Material budget between layers
- Use new point to update (FIT) parameters and covariance
- Iterate...



○ Notes

- The method is only matrix computation
- Can be used for finding as well after propagation step (local finder)
- Some points can be discarded if considered as outliers in the fit (use χ^2 value)

**FITTING drives
track extrapolation
& momentum res.**

3. Reconstruction algorithm:

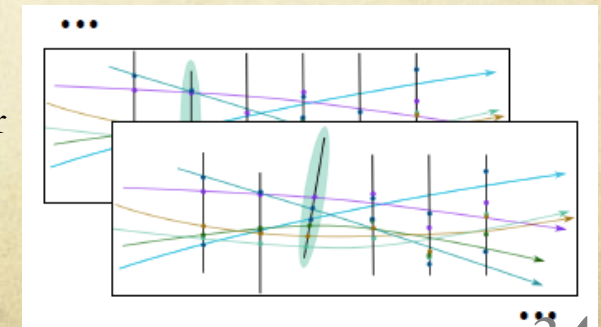
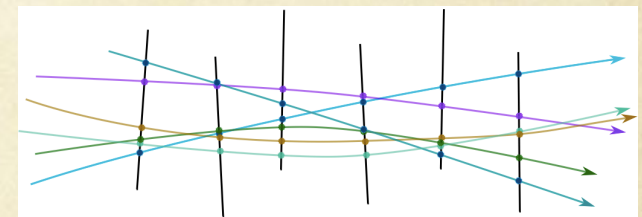
Alignment strategy

○ Let's come back to one hypothesis

- We know where the points are located
- True to the extent we know where the detector is!
- BUT, mechanical instability (magnetic field, temperature, air flow...) and also drift speed variation (temperature, pressure, field inhomogeneity...) limit our knowledge
- Periodic determination of positions and deformations needed = alignment

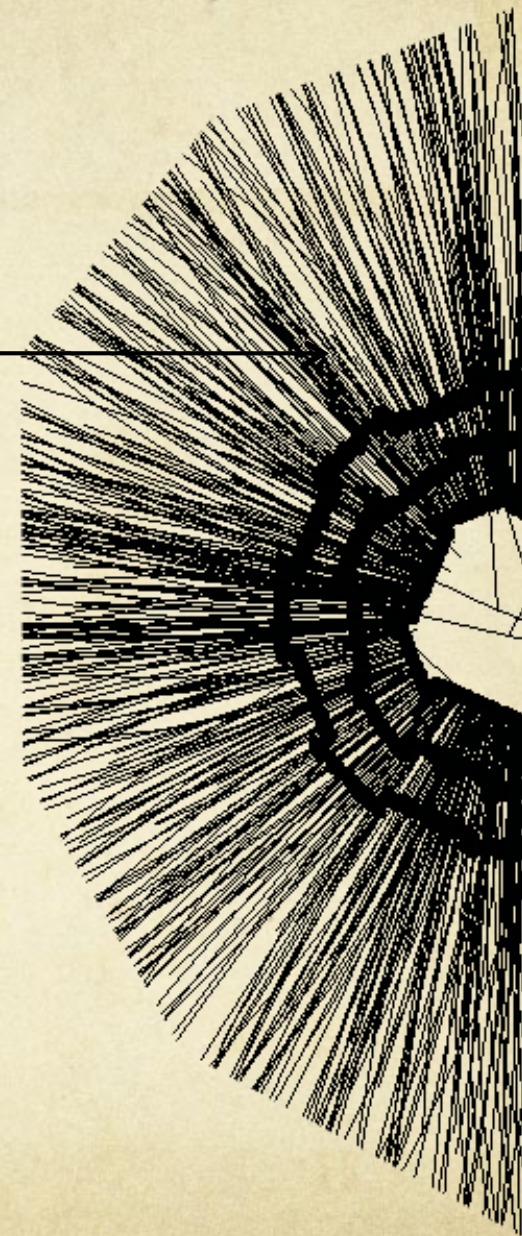
○ Methods

- Track model depends on new “free” parameters, i.e. the alignment
- Global alignment:
 - Fit the new params. to minimize the overall χ^2 of a set of tracks (Millepede algo.)
 - Beware: many parameters could be involved (few 10^3 can easily be reached)
- Iterative alignment:
 - Use tracks reconstructed with reference detectors and align other detectors by minimizing the “residual” (track-hit distance) width
- Use a set of well know tracks and tracking-“friendly” environment to avoid bias



4. Advanced methods

- Neural network
- Cellular automaton



3. Reconstruction algorithm:

Adaptive methods

○ Shall we do better?

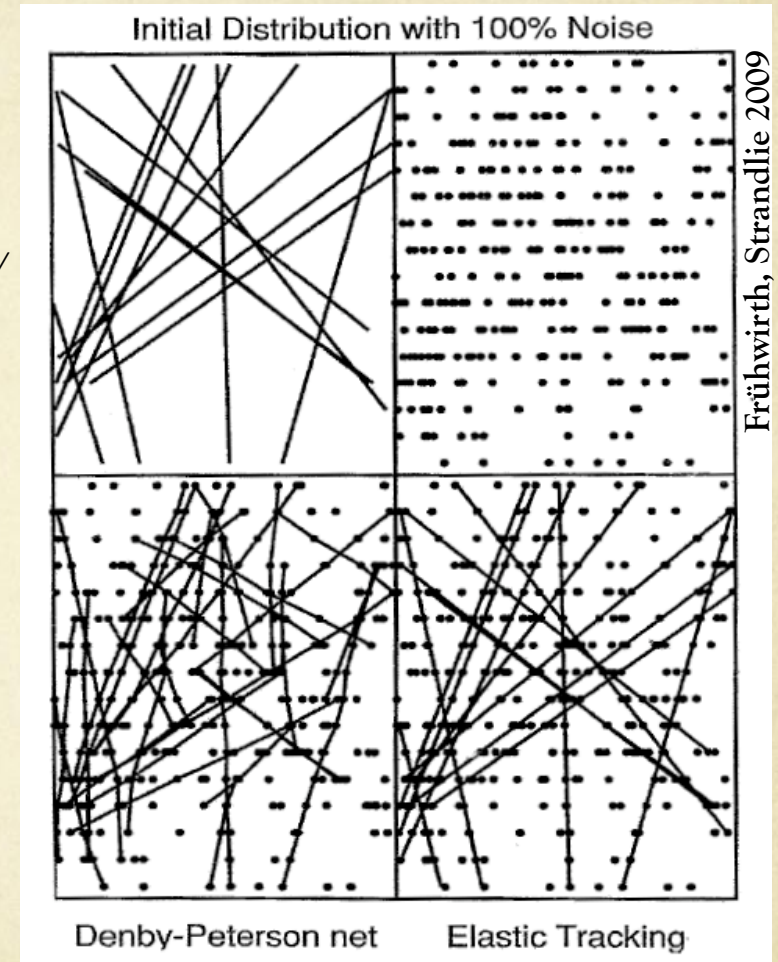
- Higher track/vertex density, less efficient the classical method
- Allows for many options and best choice

○ Adaptive features

- Dynamic change of track parameters during finding/fitting
- Measurements are weighted according to their uncertainty
 - Allows to take into account several “normally excluding” info
- Many hypothesis are handled simultaneously
 - But their number decrease with iterations (annealing like behavior)
- Non-linearity
- Often CPU-time costly (is that still a problem?)

○ Examples

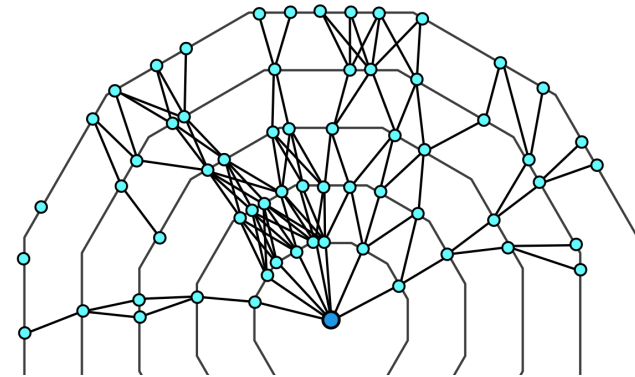
- Neural network, Elastic nets, Gaussian-sum filters, Deterministic annealing



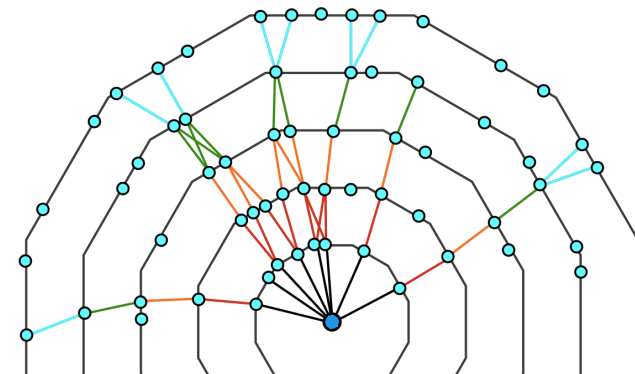
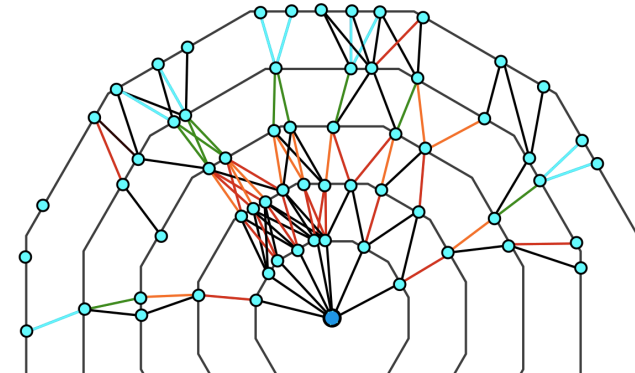
○ Cellular automaton

- Initialization
 - built any cell (= segment of 2 points)
- Iterative step
 - associate neighbour cells (more inner)
 - Raise “state” with associated celled
 - Kill lowest state cells

J. Lettenbichler *et al.*, 2013

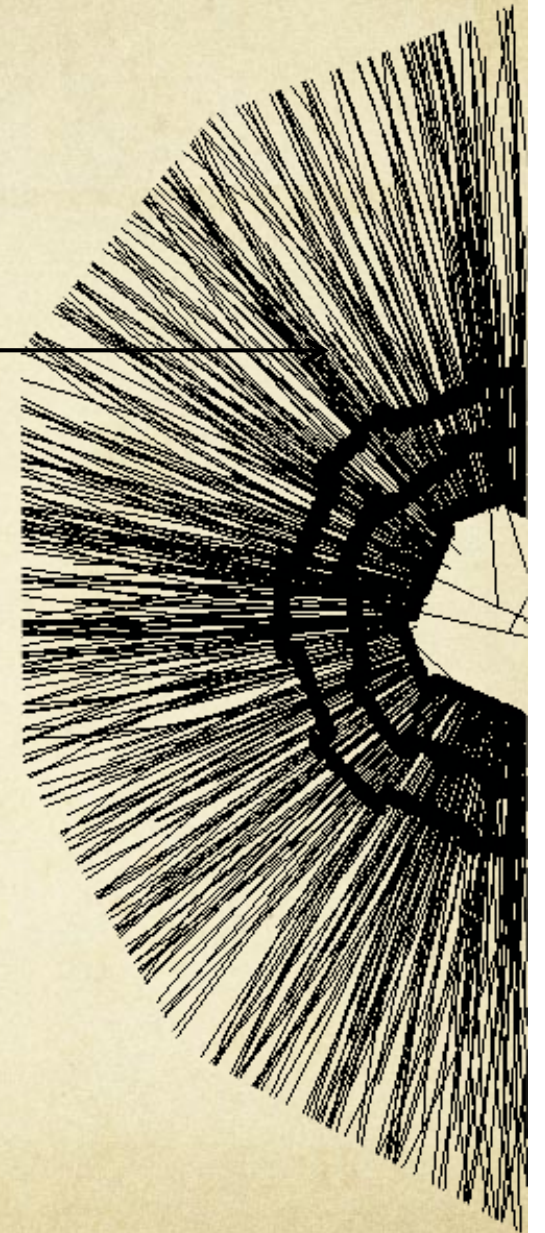


0 (black), 1 (red), 2 (orange), 3 (green), 4 (cyan)



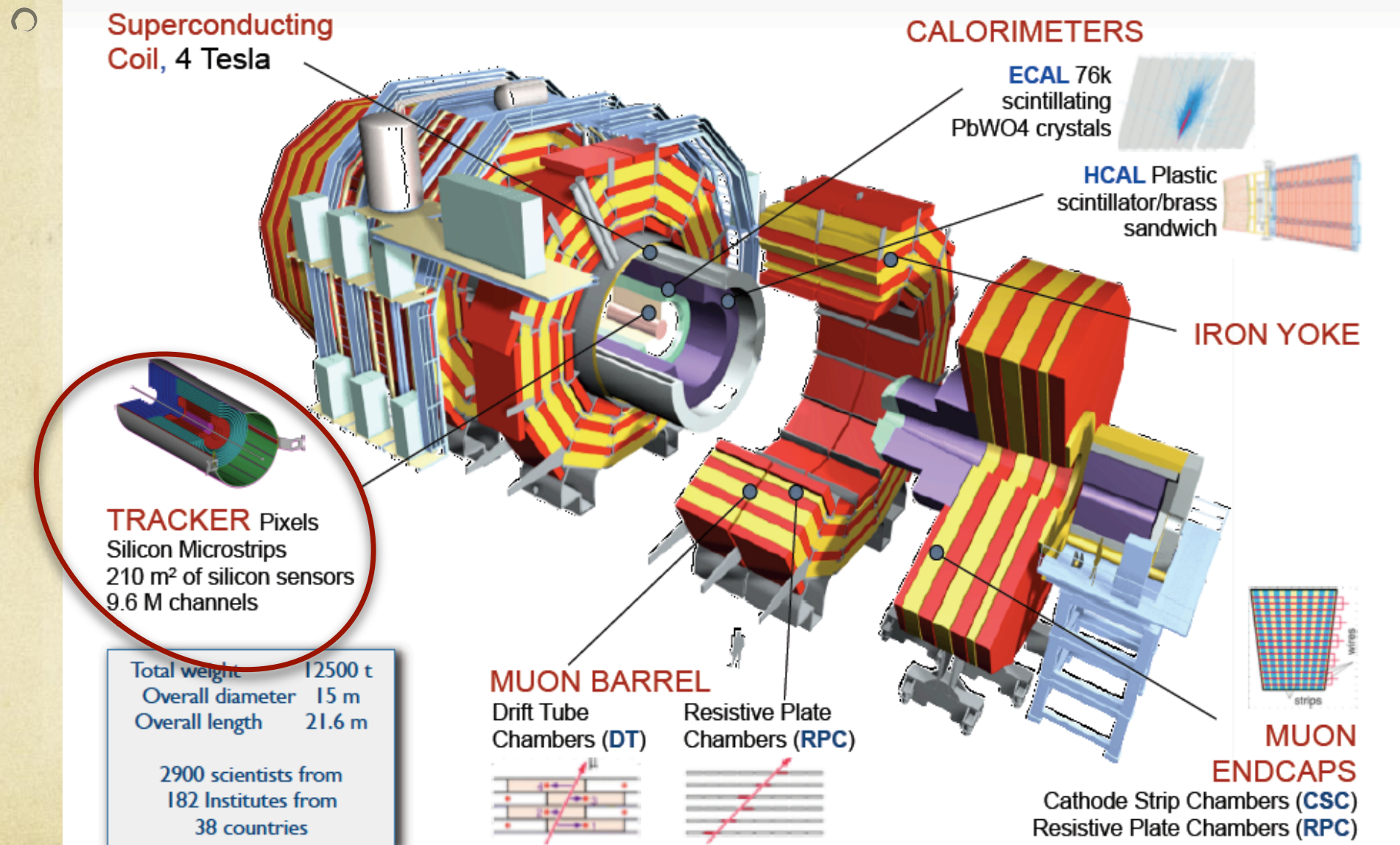
4. Deconstructing some tracking systems

- CMS
- AMS



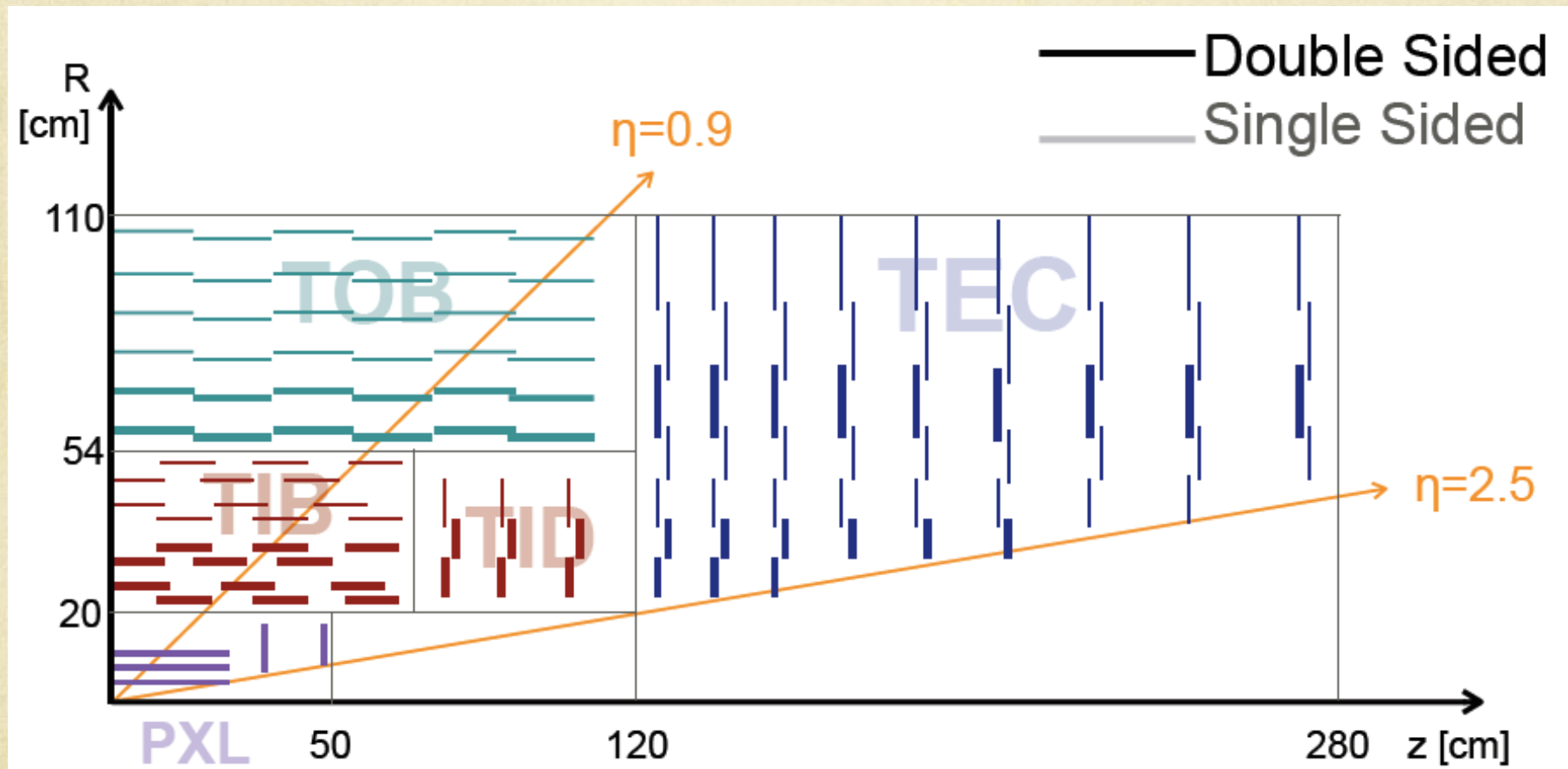
4. Some tracking systems:

CMS



4. Some tracking systems:

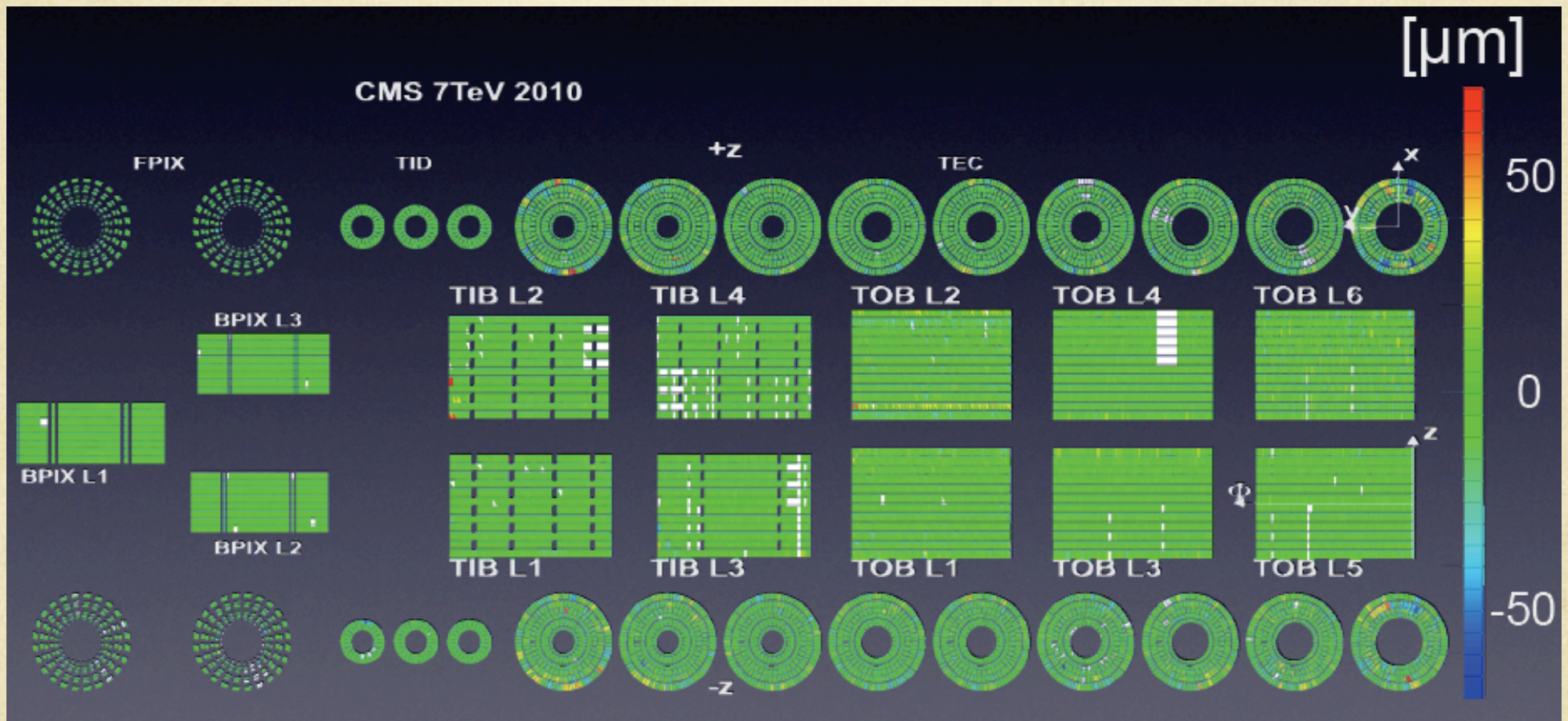
CMS



4. Some tracking systems:

CMS

- Alignment residual width

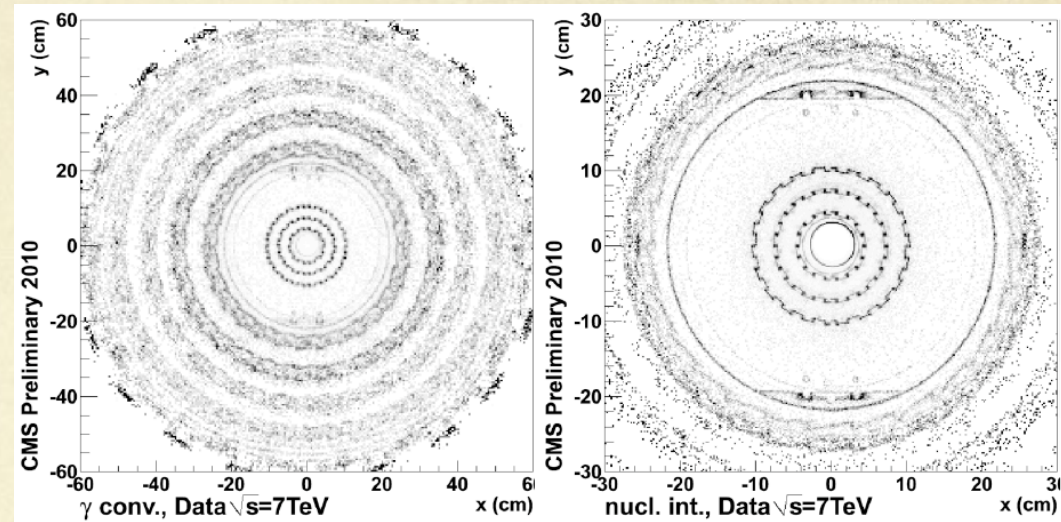


4. Some tracking systems:

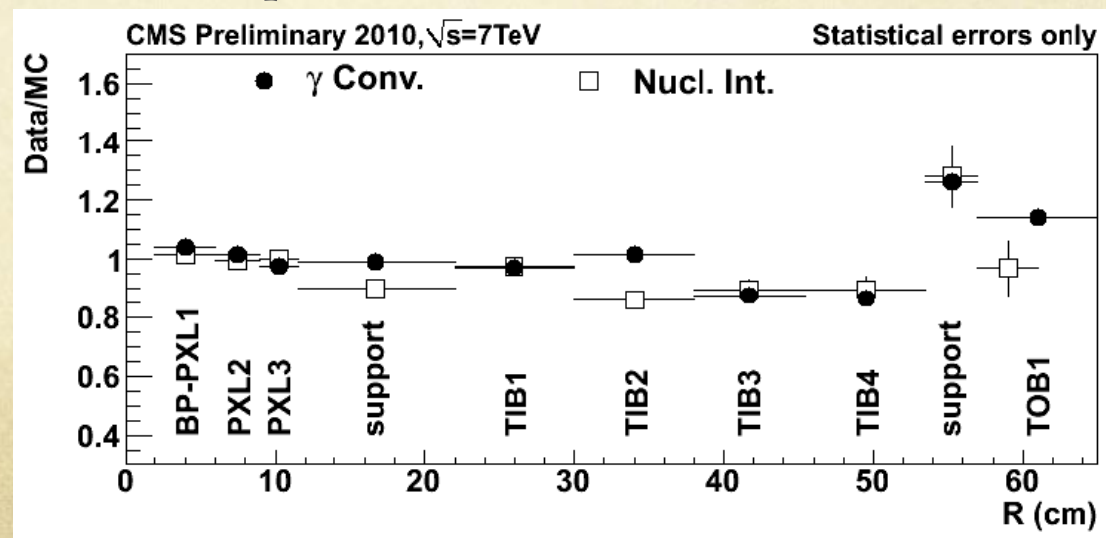
CMS

○ Taking a picture of the material budget

- Using secondary vertices from
photon conversion
nuclear interaction



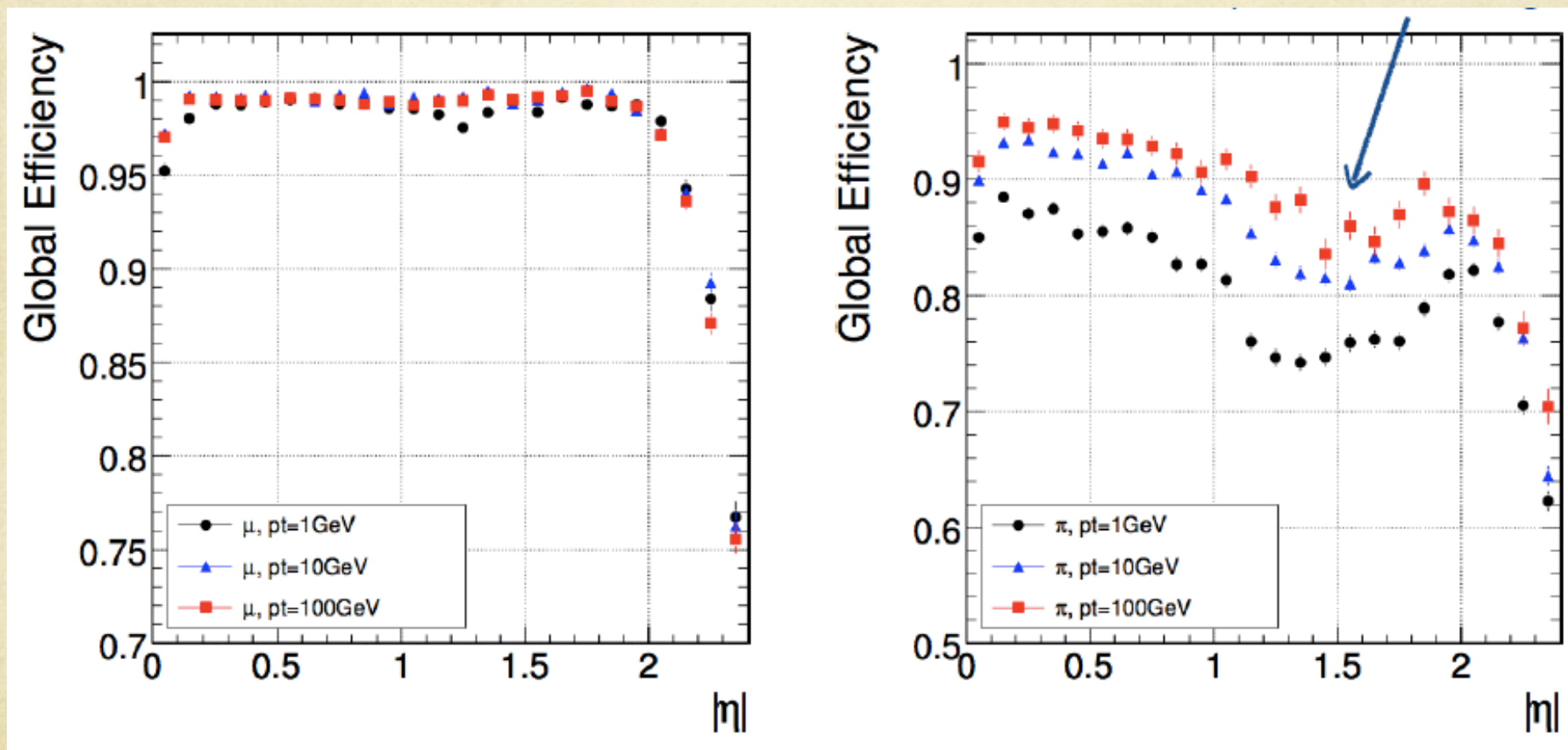
○ Measuring it by data/simulation comparison



4. Some tracking systems:

CMS

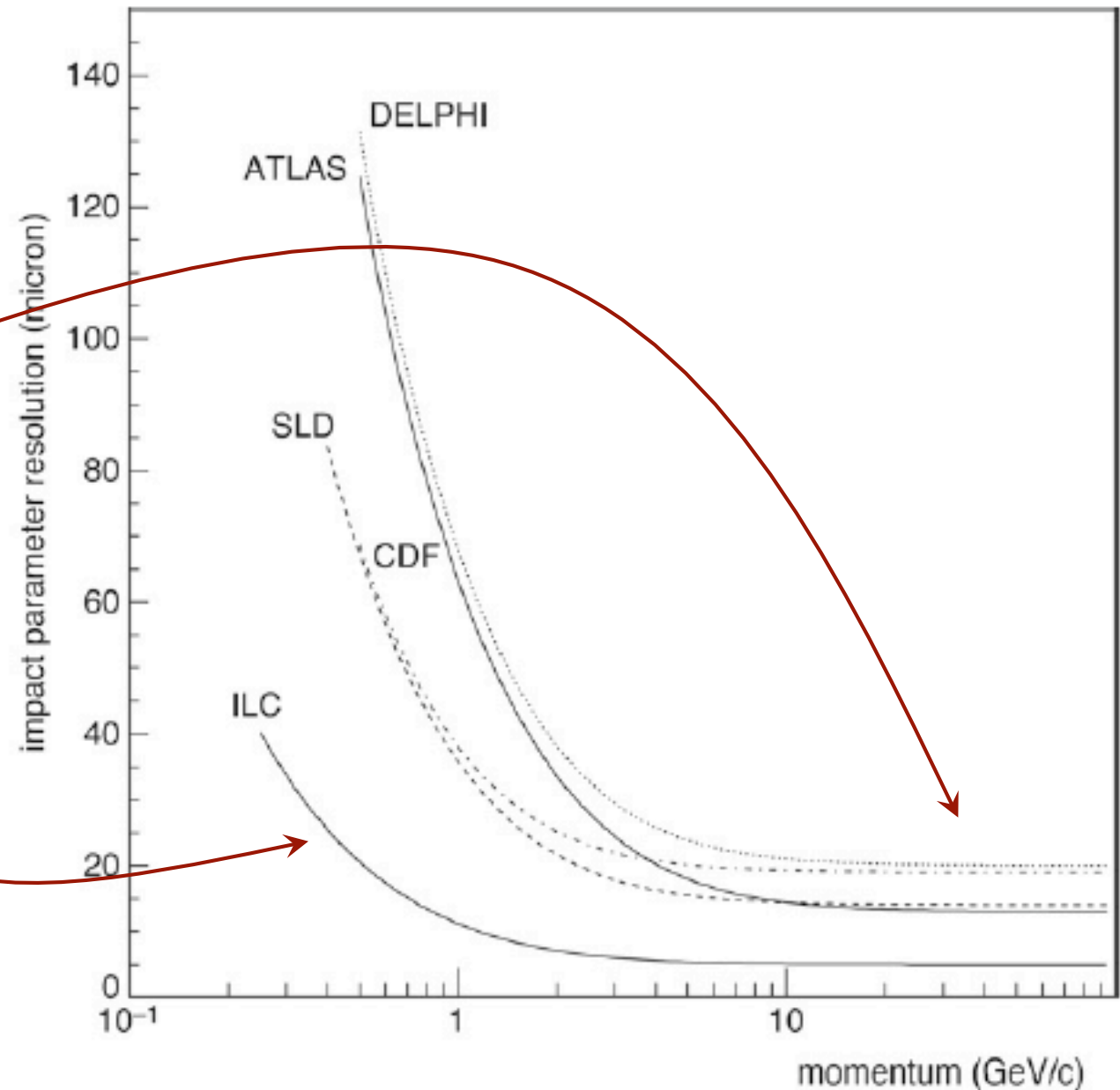
○ Tracking efficiency



4. Some tracking systems:

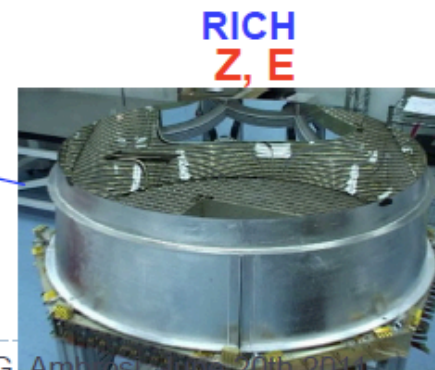
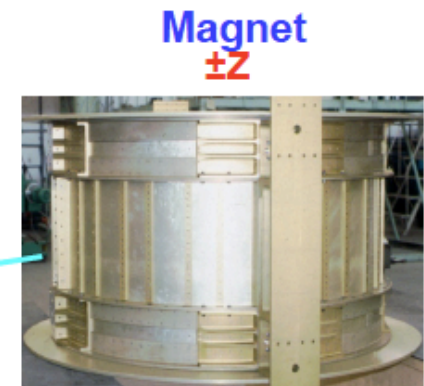
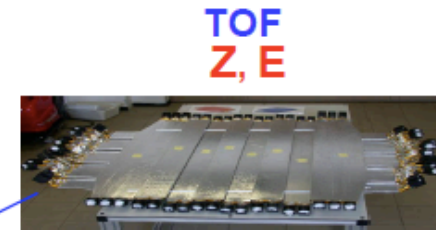
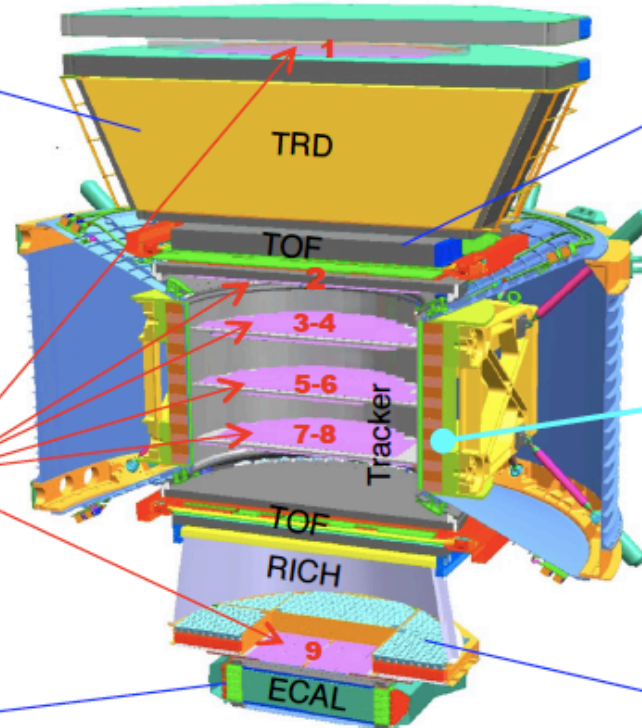
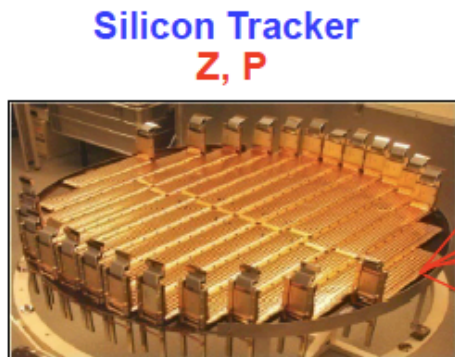
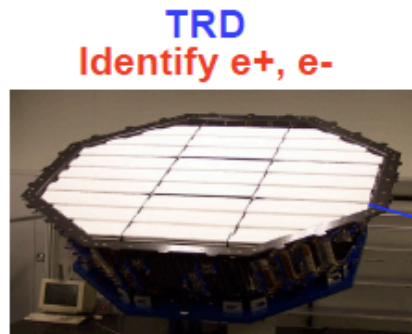
Impact parameter resolution

$$\sigma_{IP} \propto \frac{\sqrt{R_{\text{ext}}^2 \sigma_{\text{int}}^2 - R_{\text{int}}^2 \sigma_{\text{ext}}^2}}{R_{\text{ext}} - R_{\text{int}}} \oplus \frac{R_{\text{int}} \sigma_{\theta(\text{ms})}}{p \sin^{3/2}(\theta)}$$



AMS: A TeV precision, multipurpose particle physics spectrometer in space.

Particles and nuclei are defined by their charge (Z) and energy ($E \sim P$)

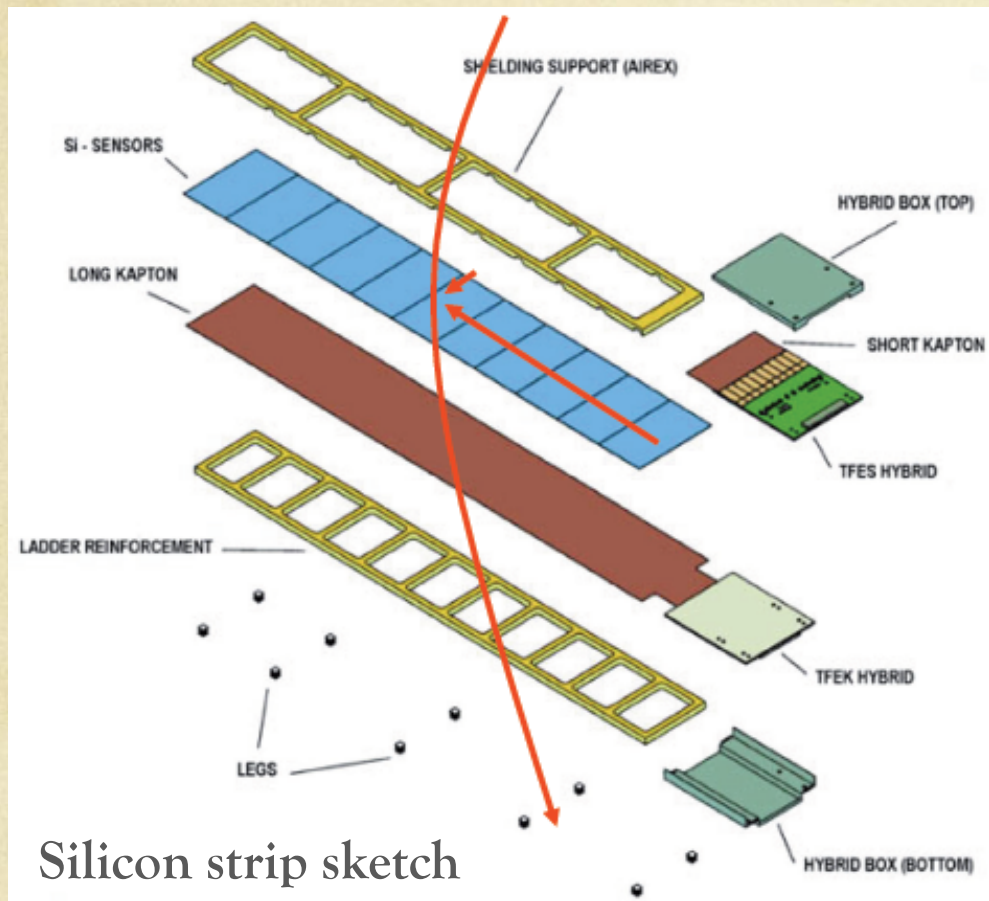


Z, P are measured independently by the Tracker, RICH, TOF and ECAL

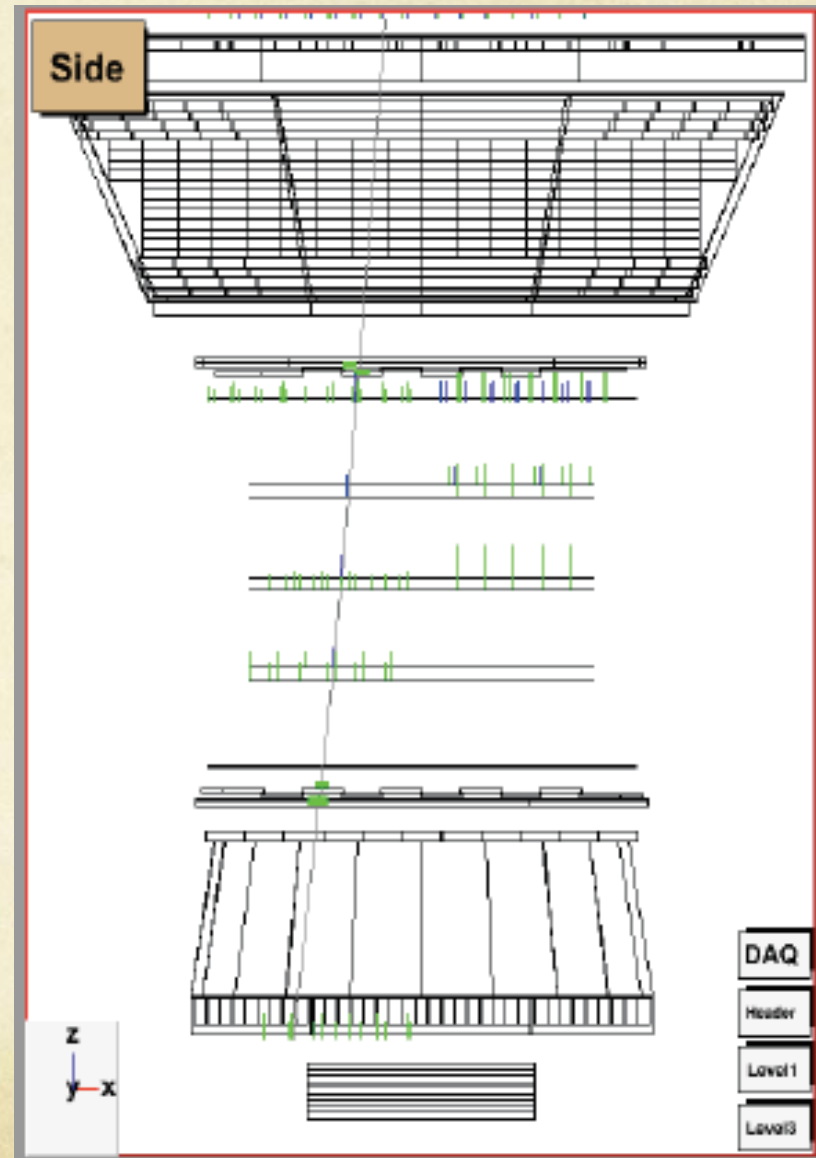
G. Ambrosi, June 20th 2011

4. Some tracking systems:

AMS



Silicon strip sketch



Summary

- **Fundamental characteristics of any tracking & vertexing device:**
 - (efficiency), granularity, material budget, power dissipation, “timing”, radiation tolerance
 - All those figures are intricated: each technology has its own limits

- **Many technologies available**
 - None is adapted to all projects (physics + environment choose, in principle)
 - Developments are ongoing for upgrades & future experiments
 - Goal is to extent limits of each techno. → convergence to a single one?

- **Reconstruction algorithms**
 - Enormous boost (variety and performances) in the last 10 years
 - Each tracking system has its optimal algorithm

- **Development trend**
 - Always higher hit rates call for more data reduction
 - Tracking info in trigger → high quality online tracking/vertexing

- **Link with:**
 - PID: obvious with TPC, TRD, topological reco.
 - Calorimetry: Particle flow algorithm, granular calo. using position sensors

References

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Data Analysis Techniques for High-Energy Physics
Cambridge University Press, 2nd edition 2000
- P. Billoir
Statistics for trajectometry,
proceedings of SOS 2012, [doi:10.1051/epjconf/20135503001](https://doi.org/10.1051/epjconf/20135503001)

- **Detector technologies**

- Lecture serie
- H.G.Moser: *Silicon detector systems in high energy physics*, Progress in Particle and Nuclear Physics 63 (2009) 186237, [doi:10.1016/j.pnpnp.2008.12.002](https://doi.org/10.1016/j.pnpnp.2008.12.002)
- V.Lepeltier: Review on TPC's, Journal of Physics: Conference Series 65 (2007) 012001, [doi:10.1088/1742-6596/65/1/012001](https://doi.org/10.1088/1742-6596/65/1/012001)

- **Reconstruction algorithm**

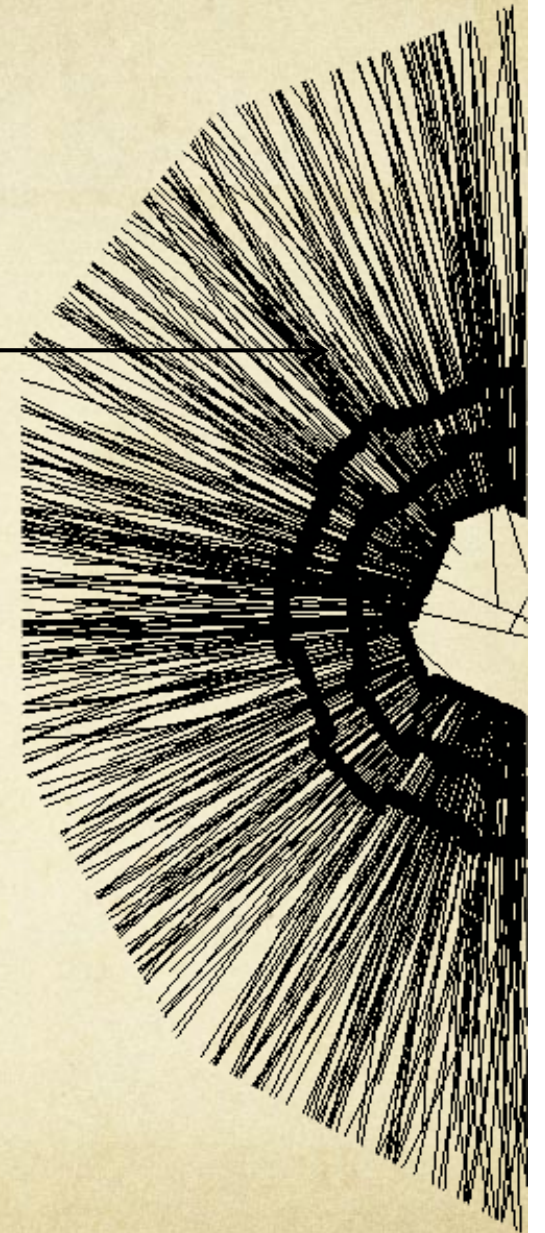
- A.Strandlie & R.Frühwirth : *Track and Vertex Reconstruction: From Classical to Adaptive Methods*, Rev. Mod. Phys. 82 (2010) 1419-1458, [doi:10.1103/RevModPhys.82.1419](https://doi.org/10.1103/RevModPhys.82.1419) and many references therein.
- R Mankel : *Pattern recognition and event reconstruction in particle physics experiments*, Rep. Prog. Phys. 67 (2004) 553-622, [doi:10.1088/0034-4885/67/4/R03](https://doi.org/10.1088/0034-4885/67/4/R03)
- Proceedings of the first LHC Detector Alignment Workshop, report CERN-2004-007, cdsweb.cern.ch/search?p=reportnumber%3ACERN-2007-004 also consult lhcdetector-alignment-workshop.web.cern.ch

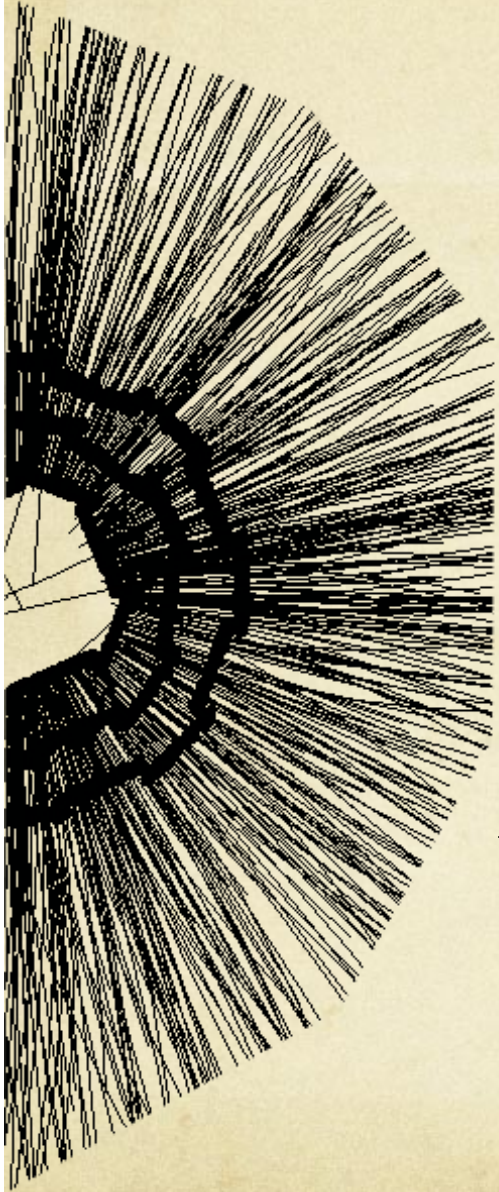
○ Contributions from experiments

- S.Haino et al., *The performance of the AMS-02 silicon tracker evaluated during the pre-integration phase of the spectrometer*, Nuclear Instruments and Methods in Physics Research A 630 (2011) 78–81, [doi:10.1016/j.nima.2010.06.032](https://doi.org/10.1016/j.nima.2010.06.032)
- G.Piacquadio, ATLAS Alignment, Tracking and Physics Performance Results, proceedings of VERTEX 2010, [PoS\(VERTEX 2010\)015](#)
- A.Venturi, CMS Alignment, Tracking and Physics Performance Results, proceedings of VERTEX 2010, [PoS\(VERTEX 2010\)016](#)
- J.Aguilar et al., A fast algorithm for muon track reconstruction and its application to the ANTARES neutrino telescope, J. Astro. Phys. 34 (2011) 652-662, [doi10.1016/j.astropartphys.2011.01.003](https://doi.org/10.1016/j.astropartphys.2011.01.003)
- S.Amerio, Online Track Reconstruction at Hadron Collider, Proceedings of ICHEP 2010, [PoS\(ICHEP 2010\)481](#)
- F.Arneodo et al., **Performance of a liquid argon time projection chamber exposed to the CERN West Area Neutrino Facility neutrino beam**, Phys.Rev. D 74(2006)112001, [doi:10.1103/PhysRevD.74.112001](https://doi.org/10.1103/PhysRevD.74.112001)

Was not discussed

- Particle interaction with matter
- The readout electronics
- Cooling systems
- The magnets to produce the mandatory magnetic field for momentum measurement





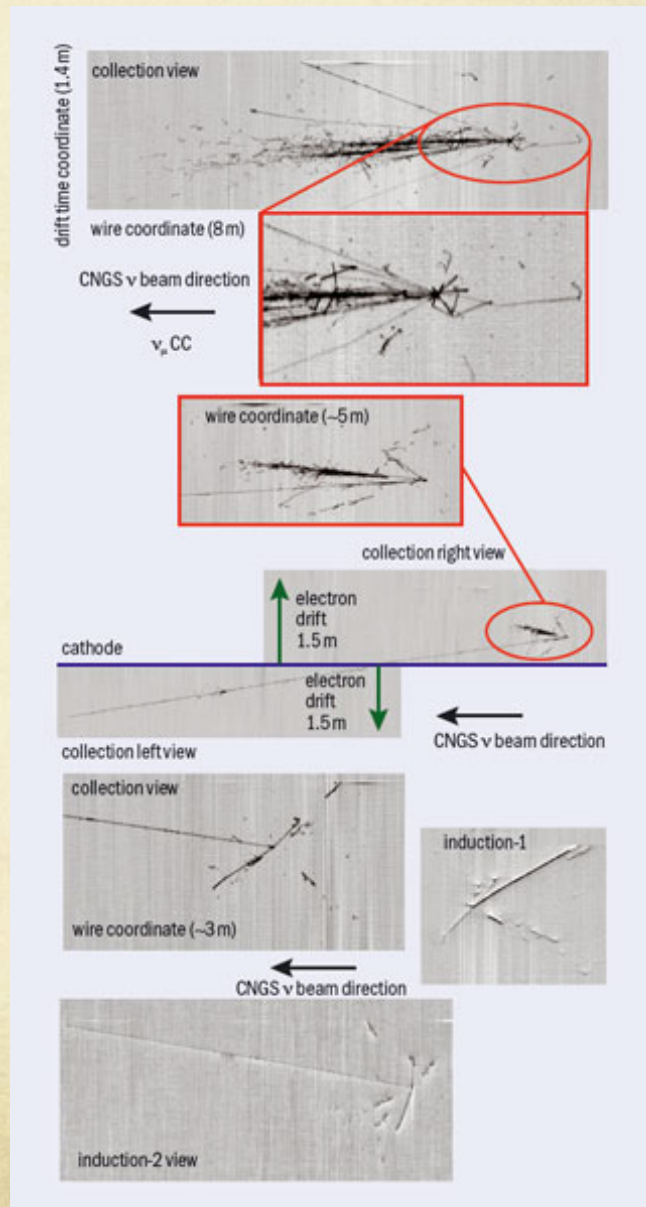
Backups

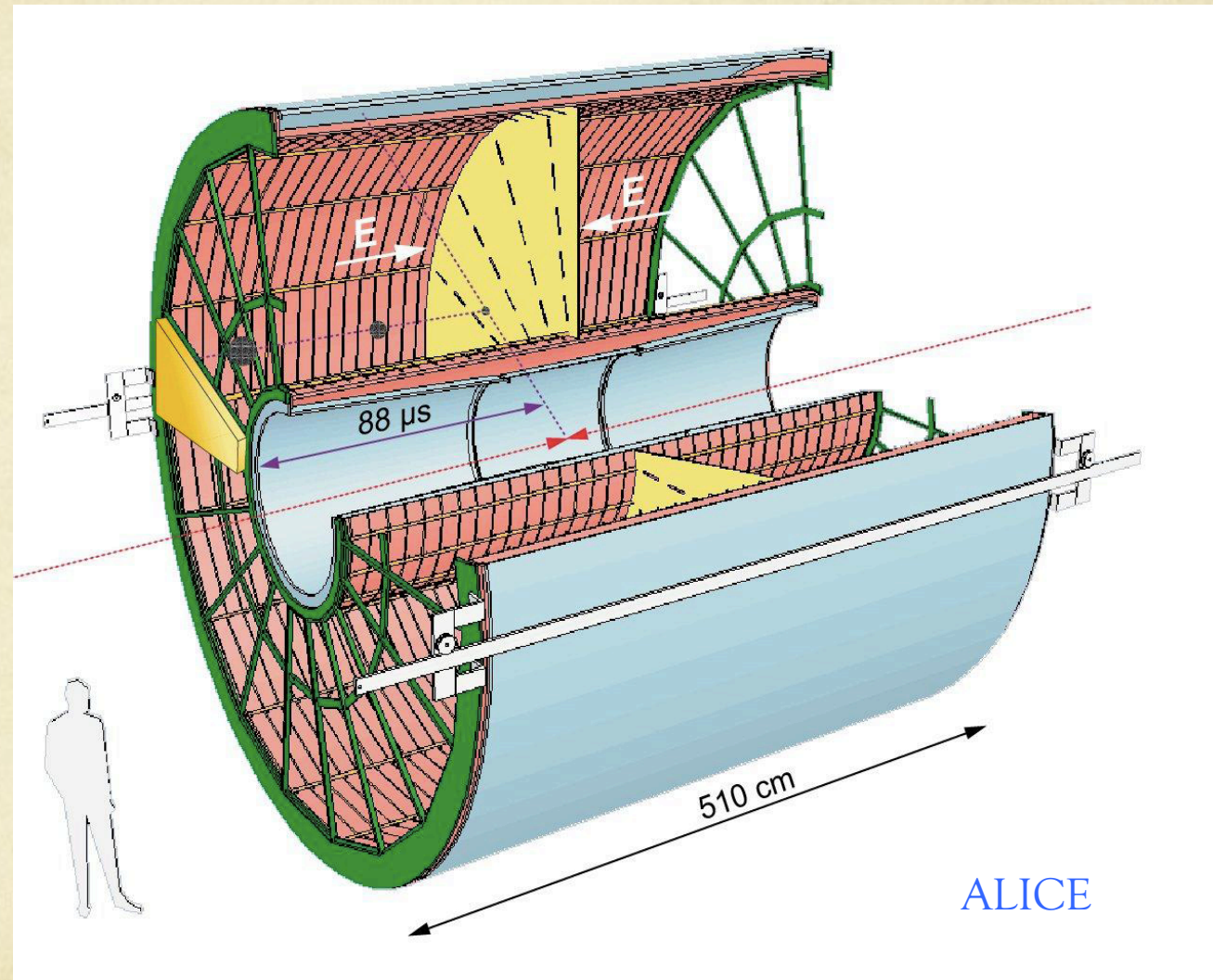
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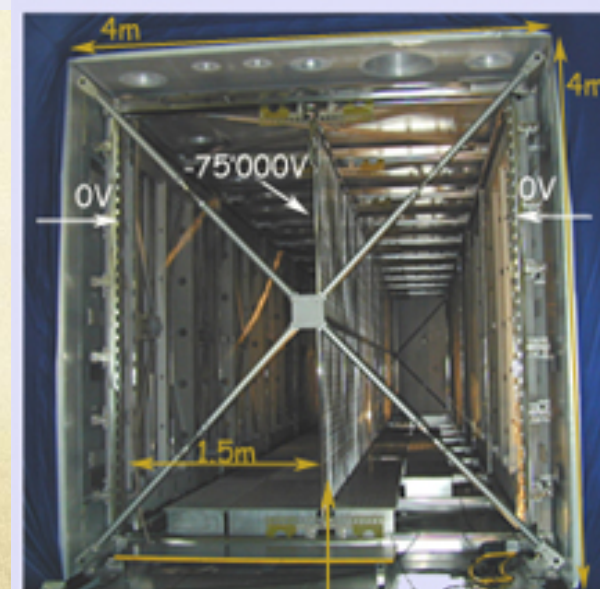
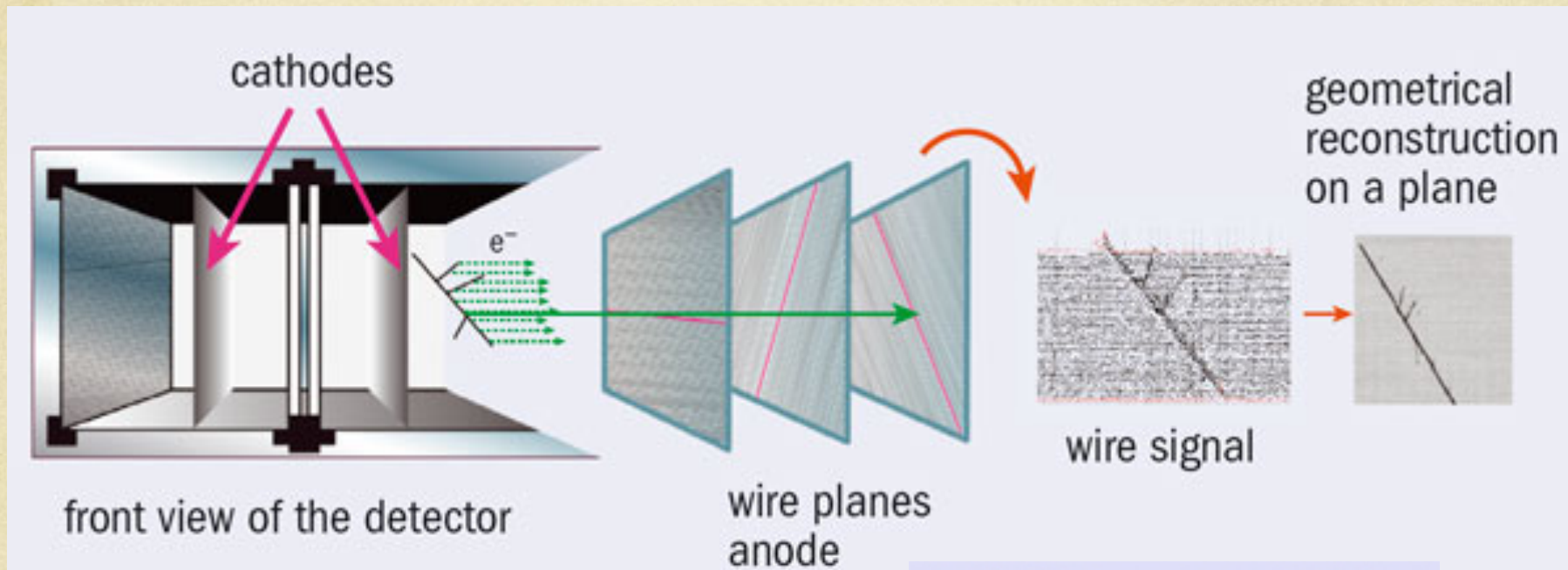
OPAL drift chamber

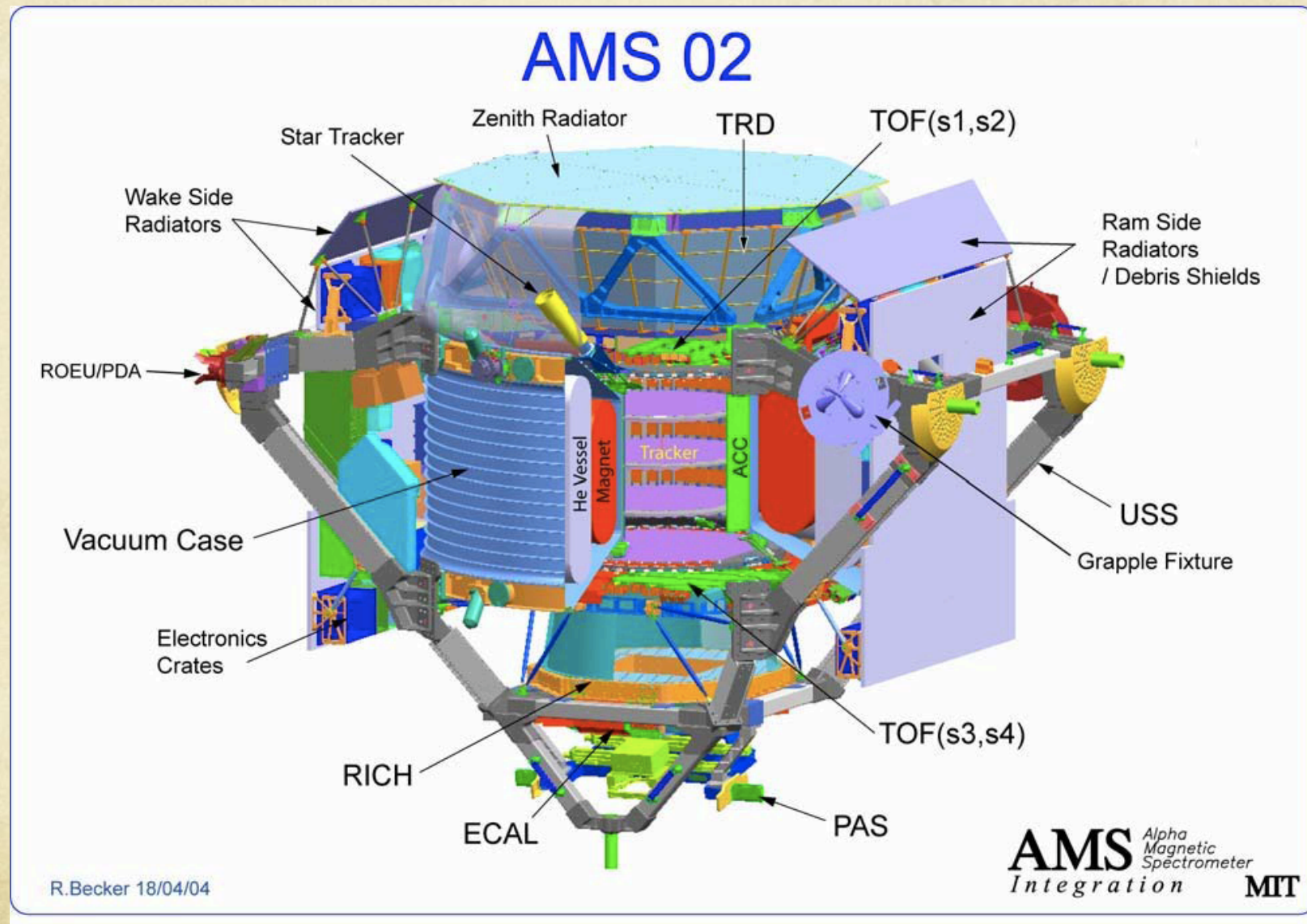
○

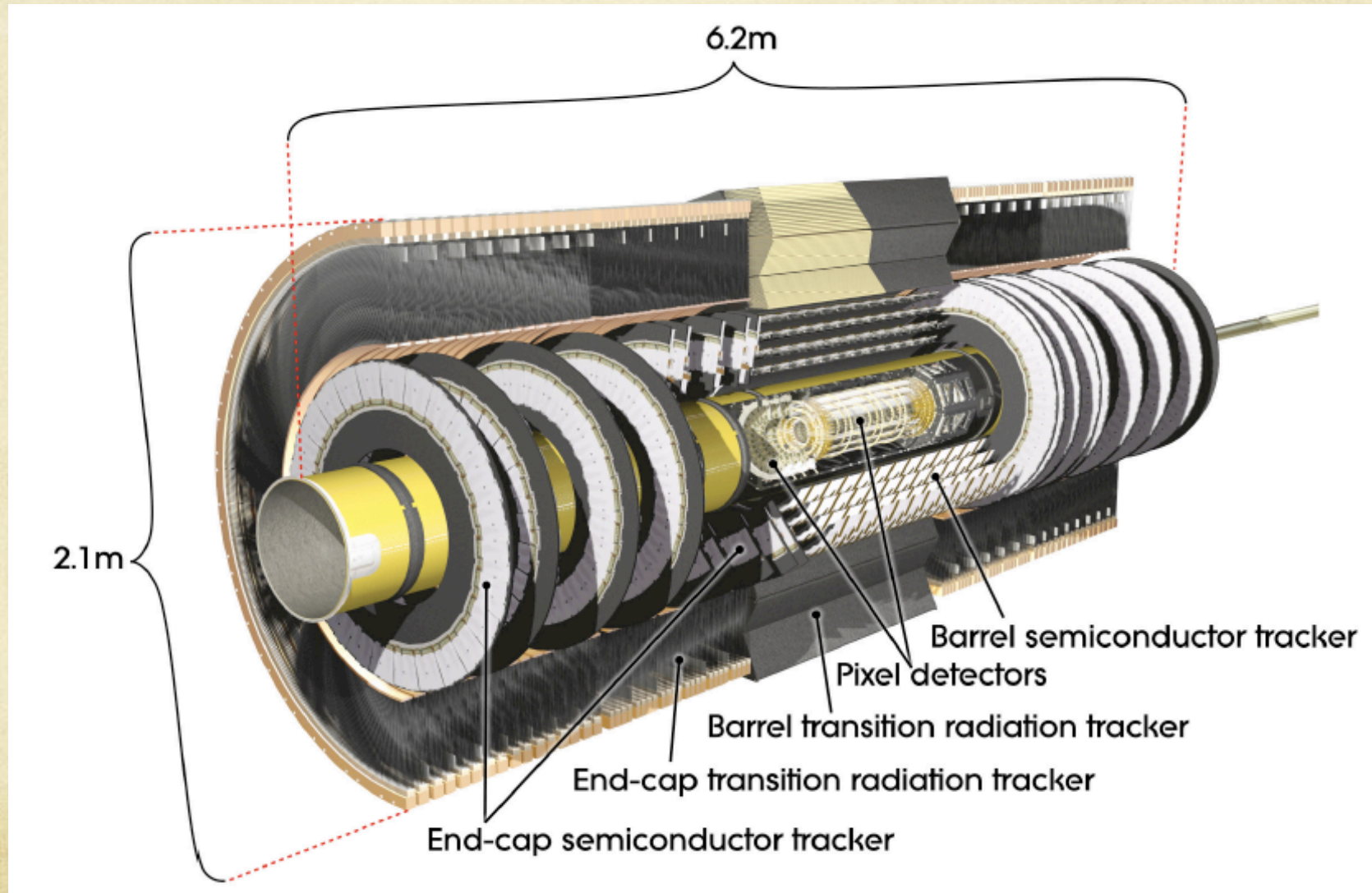


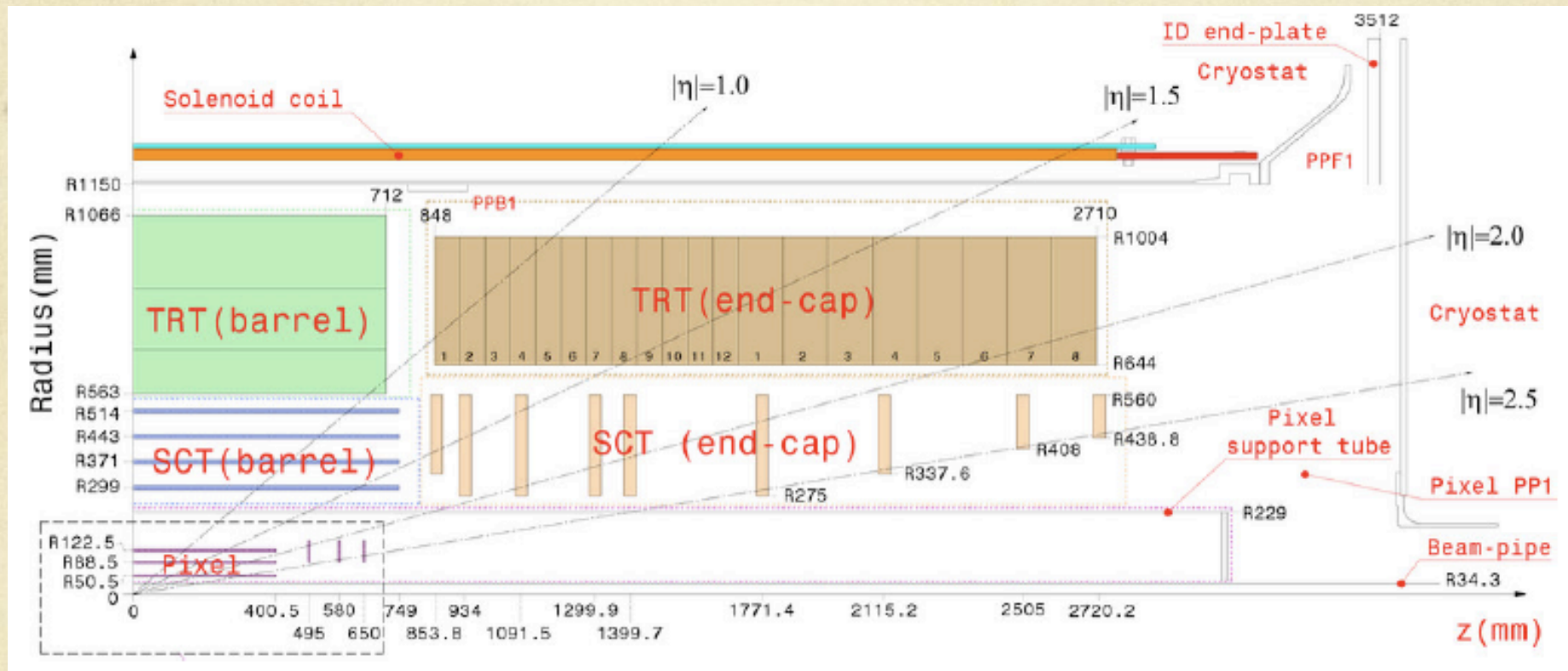


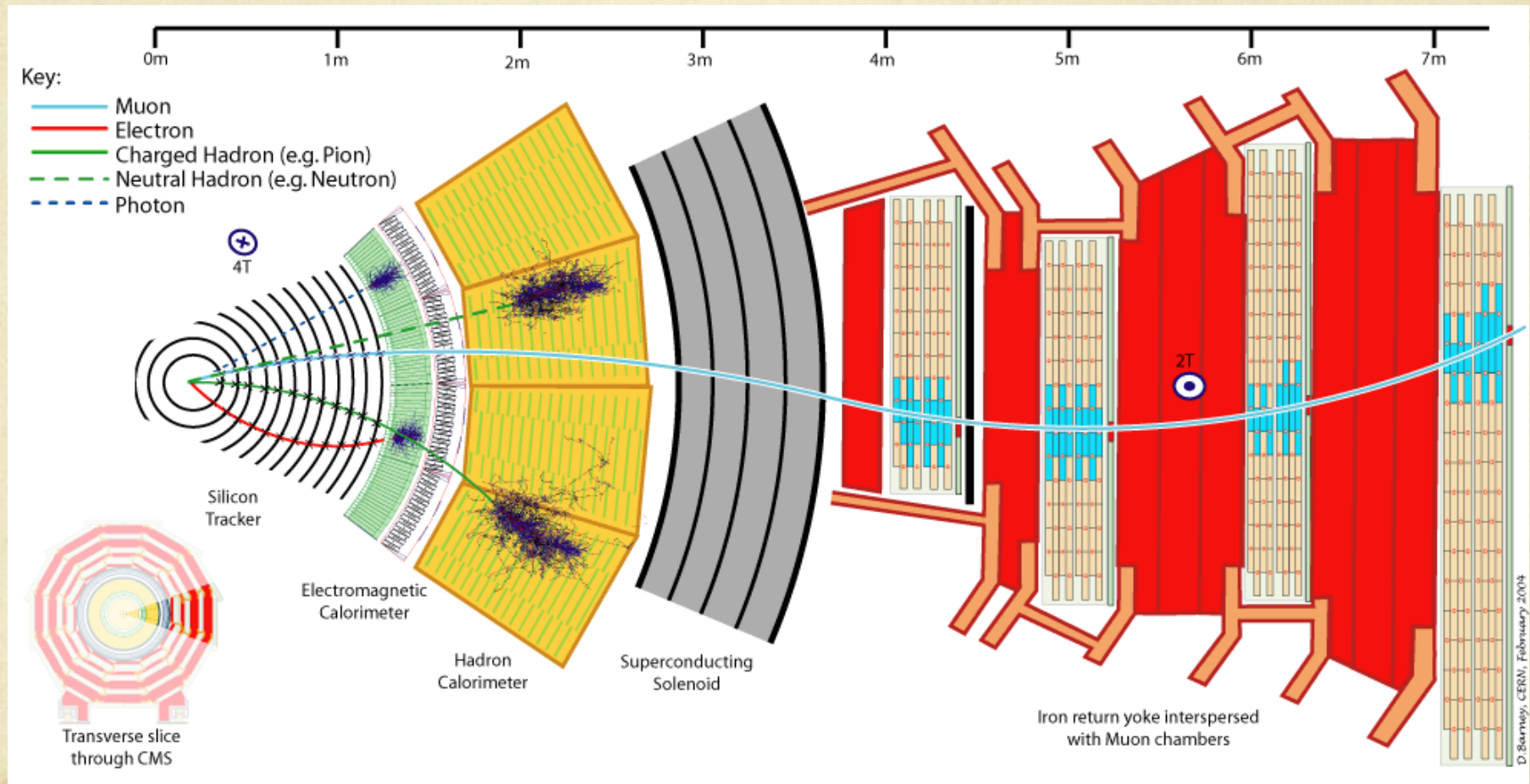


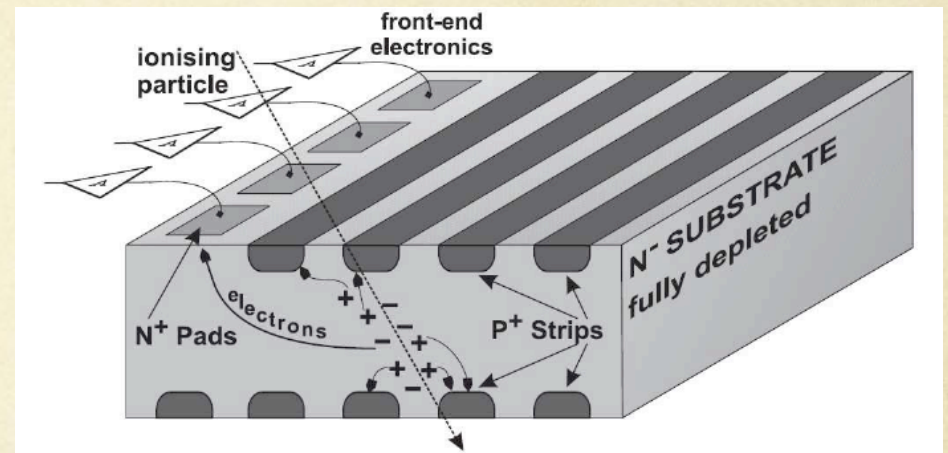


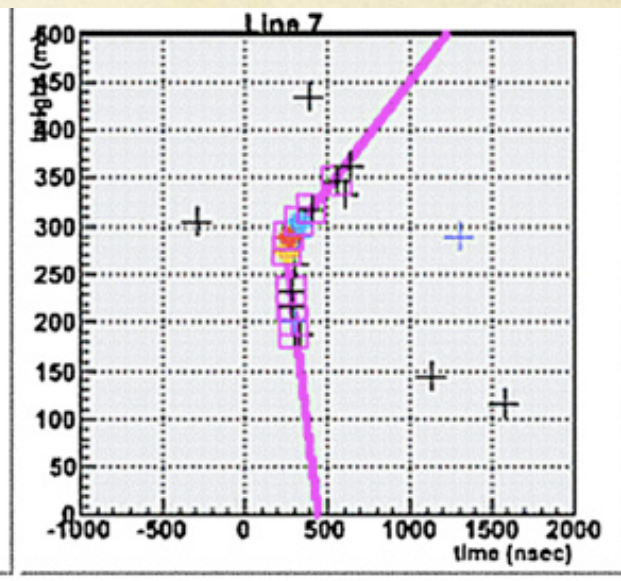
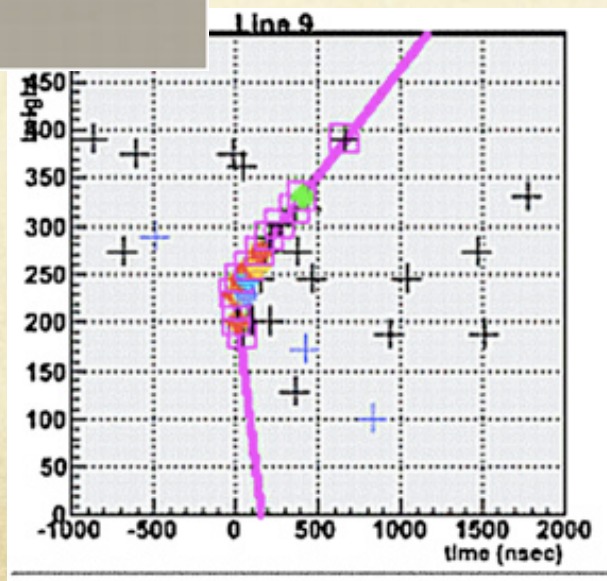
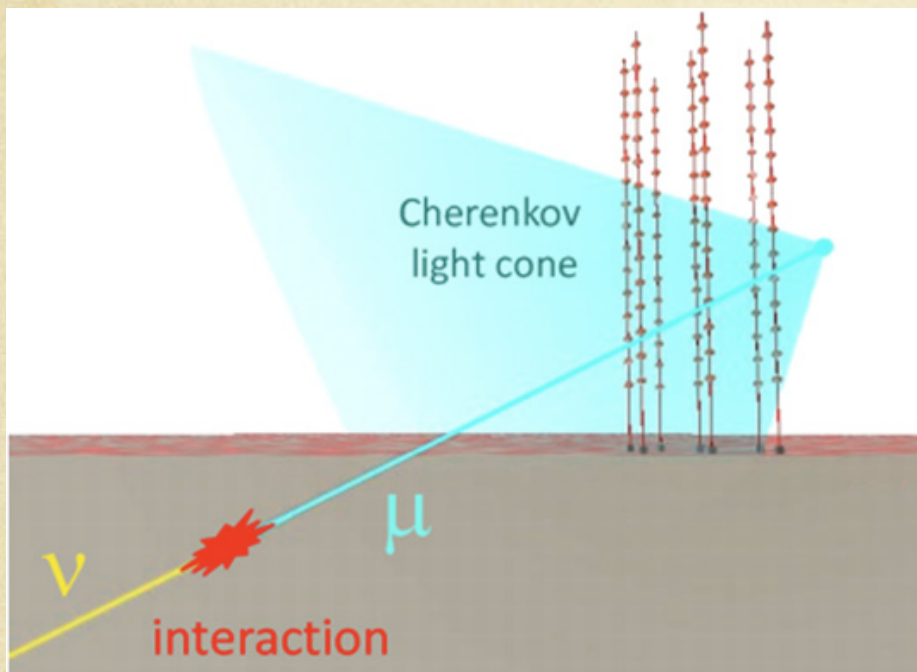












3. Reconstruction algorithm:

Resolution on P: fixed target

○ Hypothesis

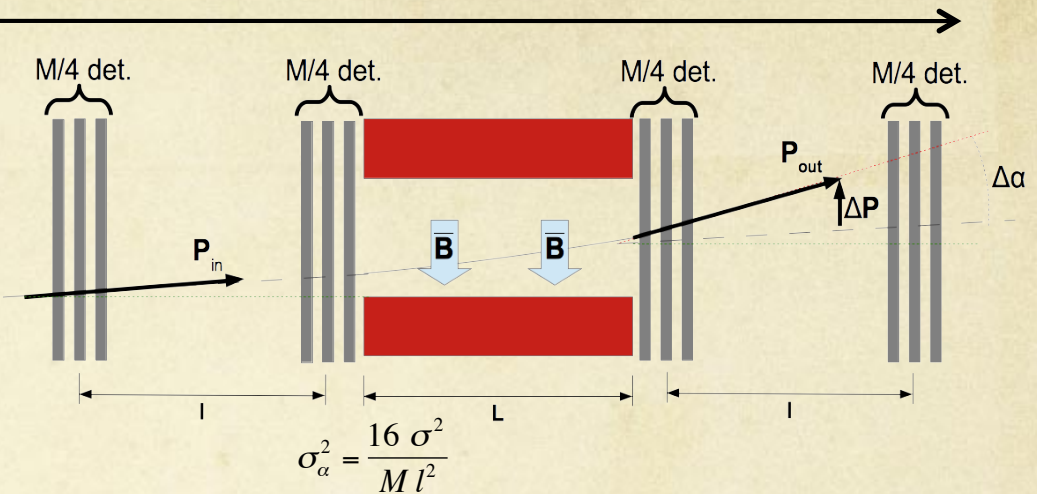
- M detectors, each with σ single point accuracy

- Uniform field over L from dipole

- Trajectory: $\Delta p = p \Delta\alpha$ $\Delta\alpha = \left| \frac{0.3qBL}{p} \right|$
- Bending:

- Geometrical arrangement optimized for resolution

- Angular determination on input and output angle:



○ Without multiple scattering $\Delta\alpha = \left| \frac{0.3qBL}{p} \right|$

- Uncertainty on momentum