

# Higgs pair production at the LHC at NLO

Eleni Vryonidou

Université catholique de Louvain

With R. Frederix, S. Frixione, V. Hirschi, F.  
Maltoni, P. Torrielli and M. Zaro  
Based on arxiv:1401.7340

Pheno2014

Pittsburgh, 5/5/14

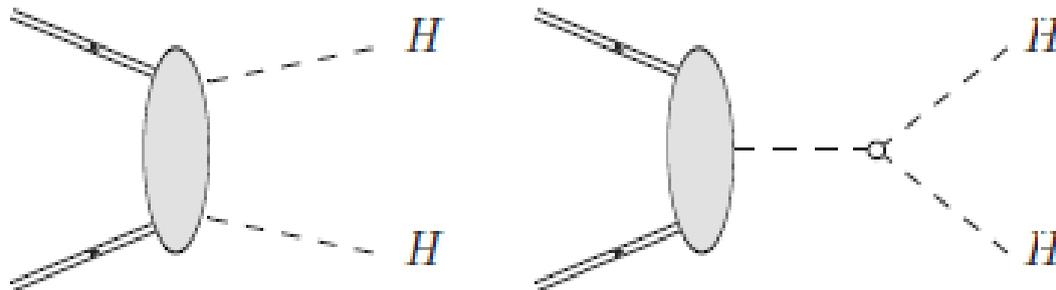
# Outline

- Motivation
- HH in gluon gluon fusion
- HH results at NLO
- Outlook

# Motivation

- Higgs discovery  SM Higgs?
- Higgs couplings measurements:
  - Couplings to fermions and gauge bosons
- **Higgs self couplings**
  - Higgs potential:

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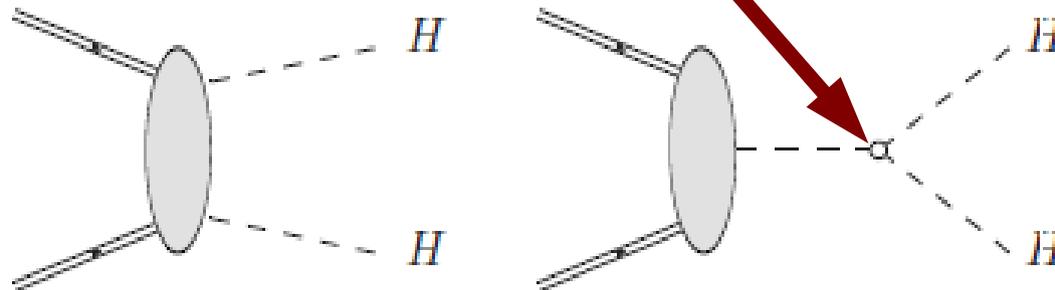


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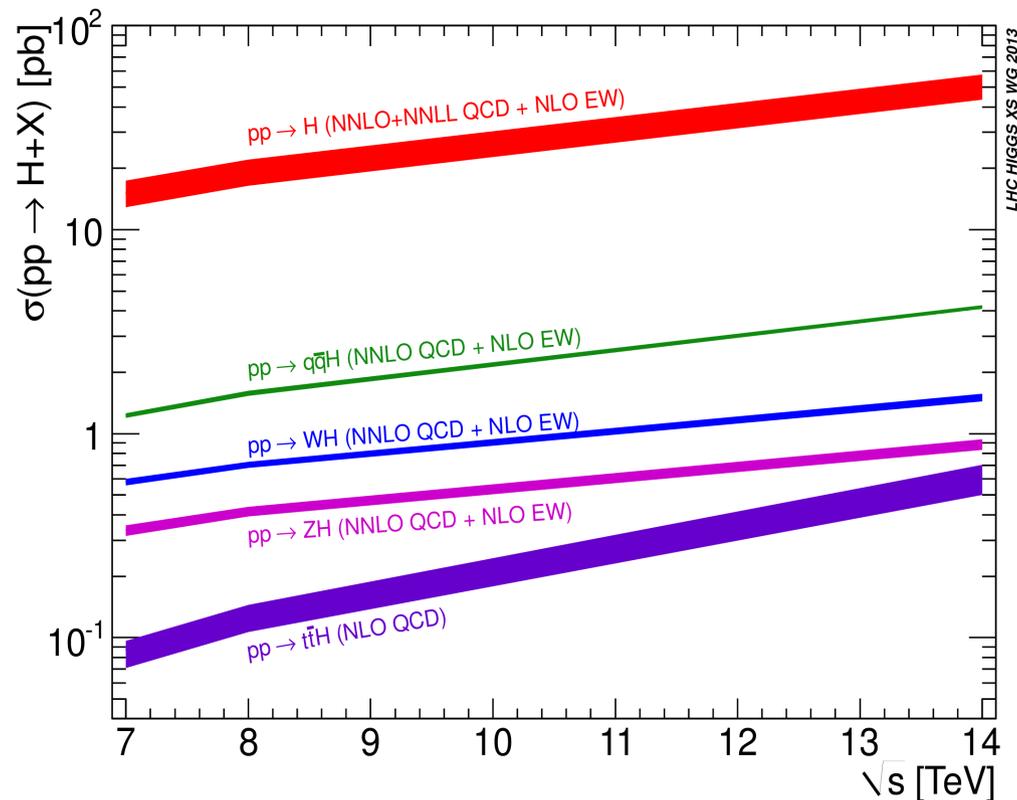


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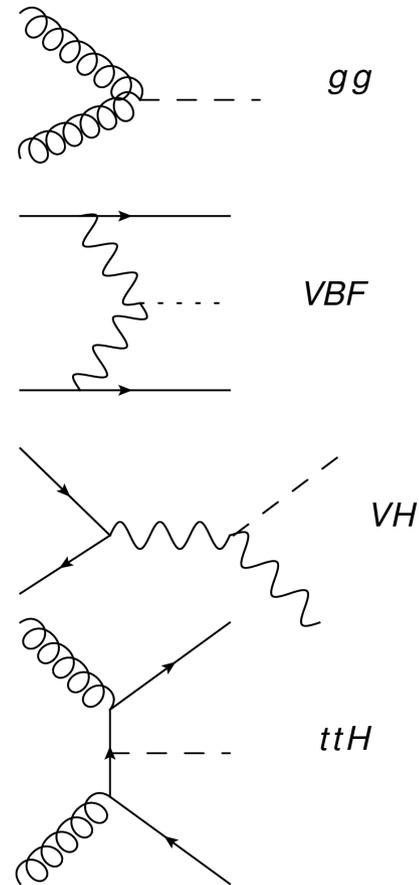
# Higgs Pair Production channels

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- Vector boson fusion
- VHH associated production
- ttHH



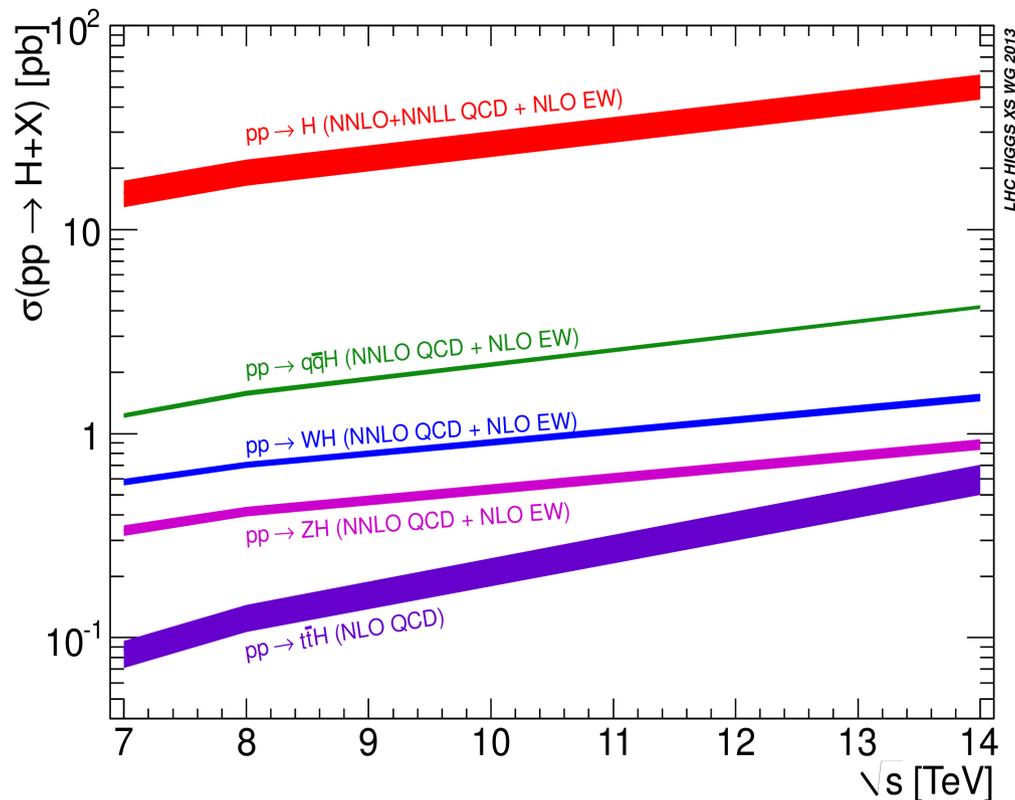
LHC Higgs Cross Sections Working Group



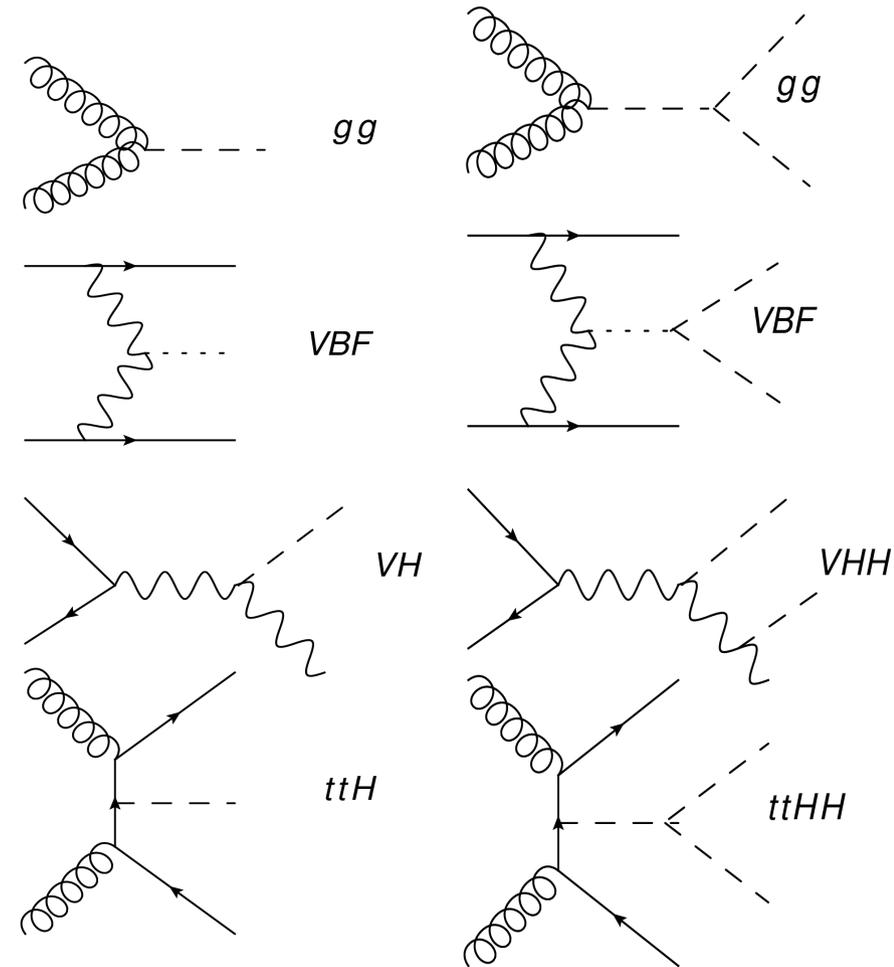
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*Schematically*

# Questions about HH

- How does the hierarchy of the channels change for HH at 14TeV? Is gluon fusion the dominant one?
- How does the cross section change with the centre of mass energy?
- How does the cross section depend on the value of the trilinear Higgs coupling?
- Do we have NLO predictions for all the channels?
- Do we have an efficient fully differential Monte Carlo implementation of the process?

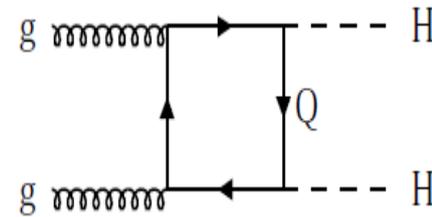
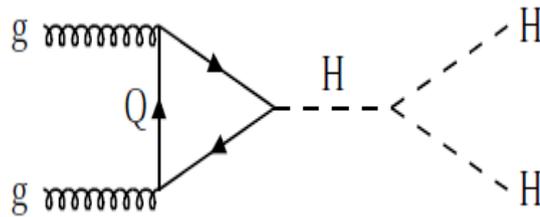
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Let's focus on gluon-gluon fusion...

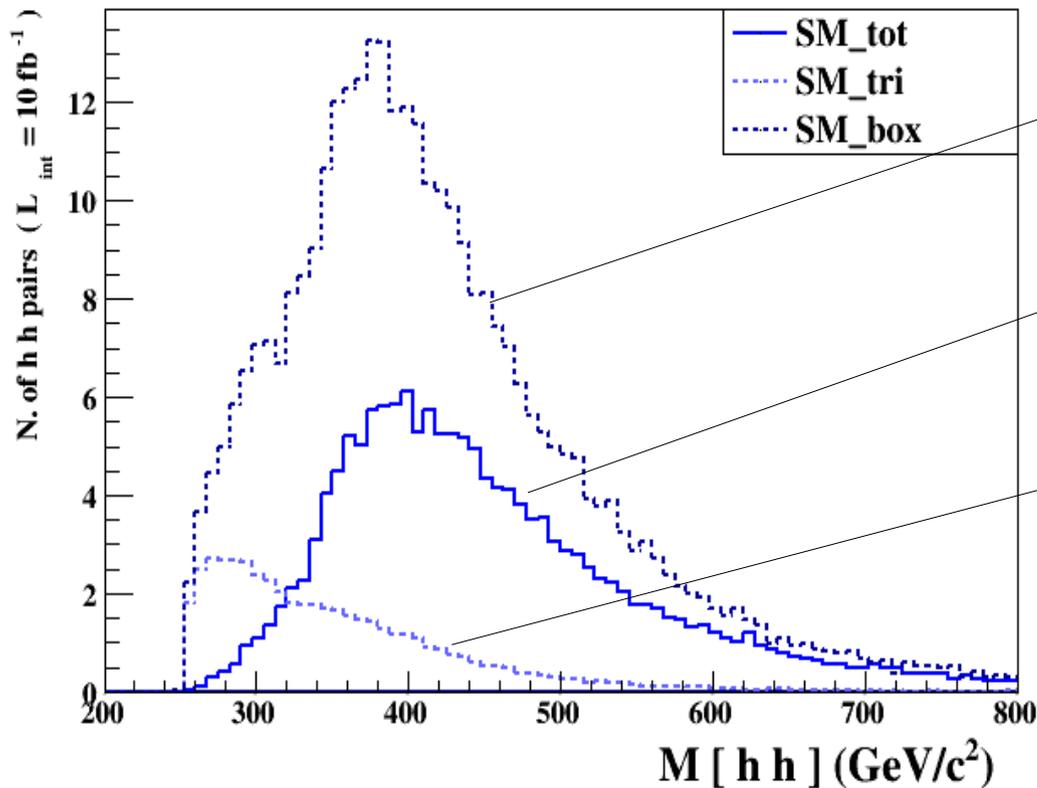
# Focussing on gluon-gluon fusion...

- At LO...



Only loop induced channel

How much does each diagram contribute?



Box

Total

Triangle

Significant cancellation between the two diagrams

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Loop induced process: not yet automated in MC

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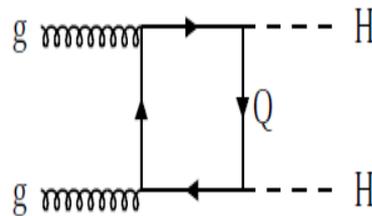
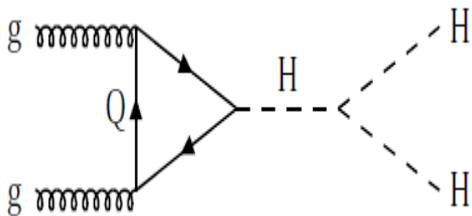
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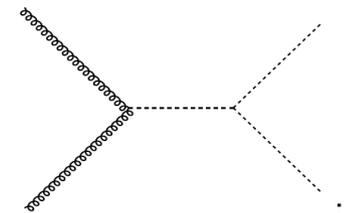
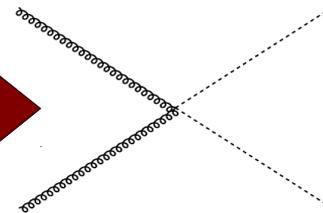
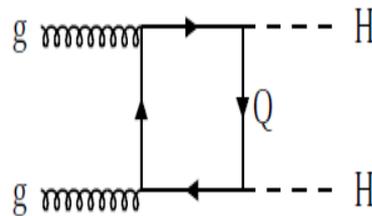
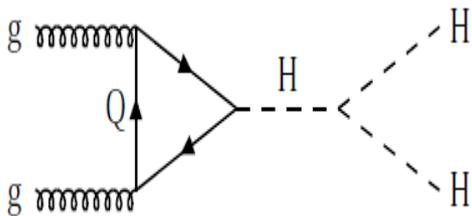
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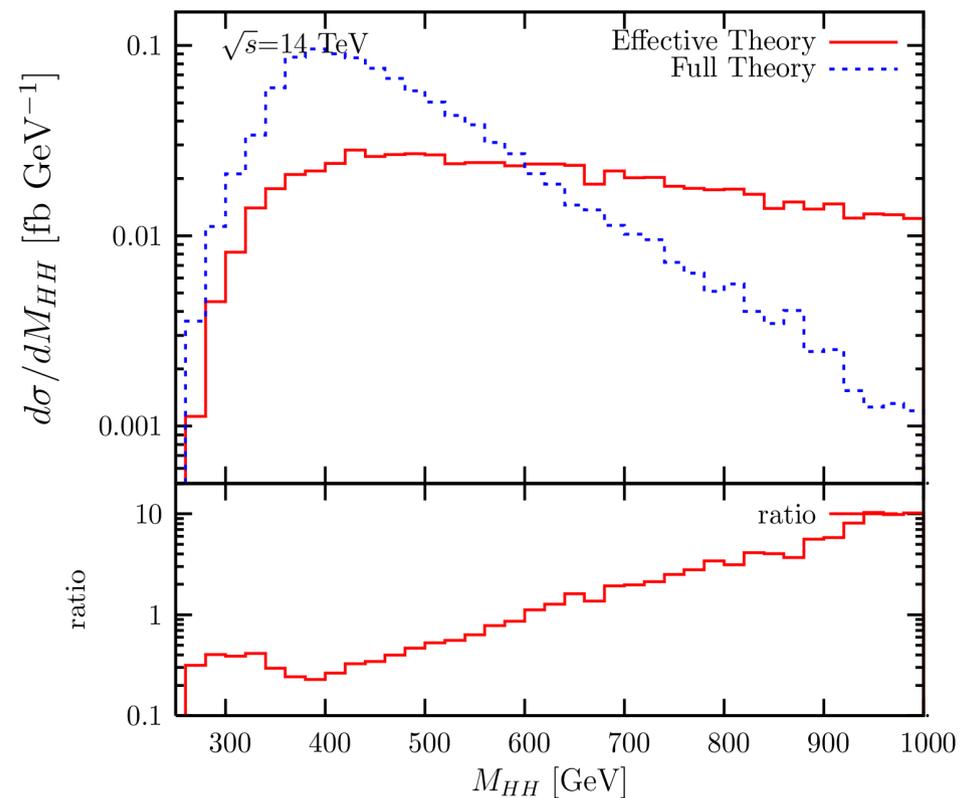
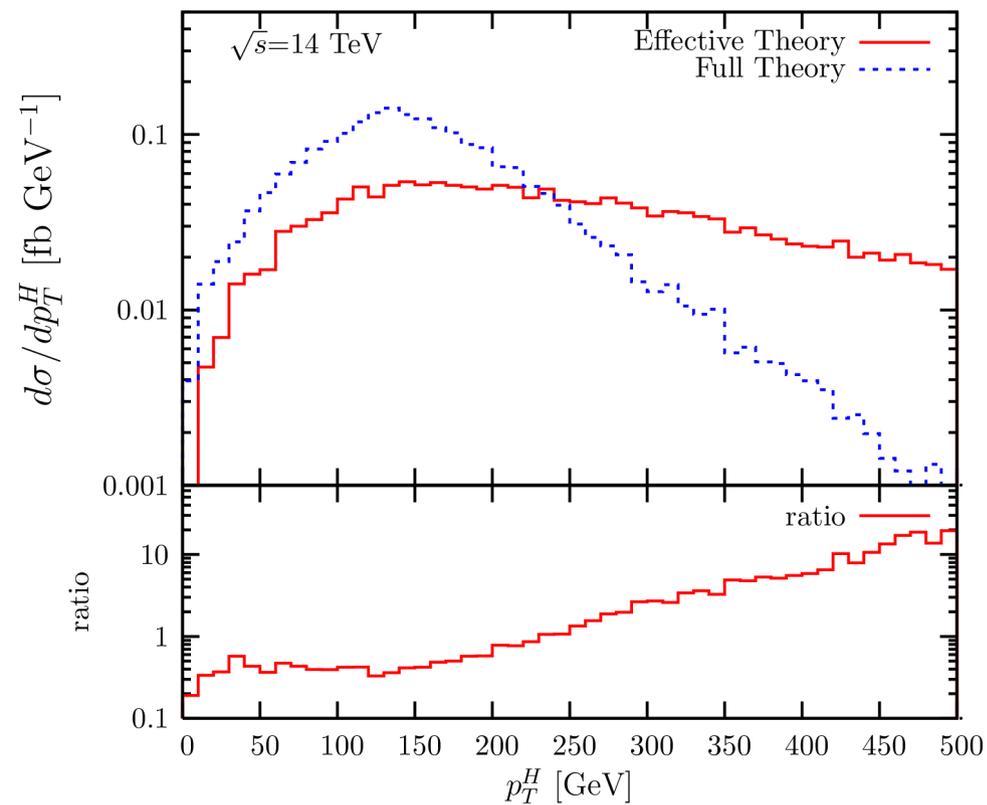
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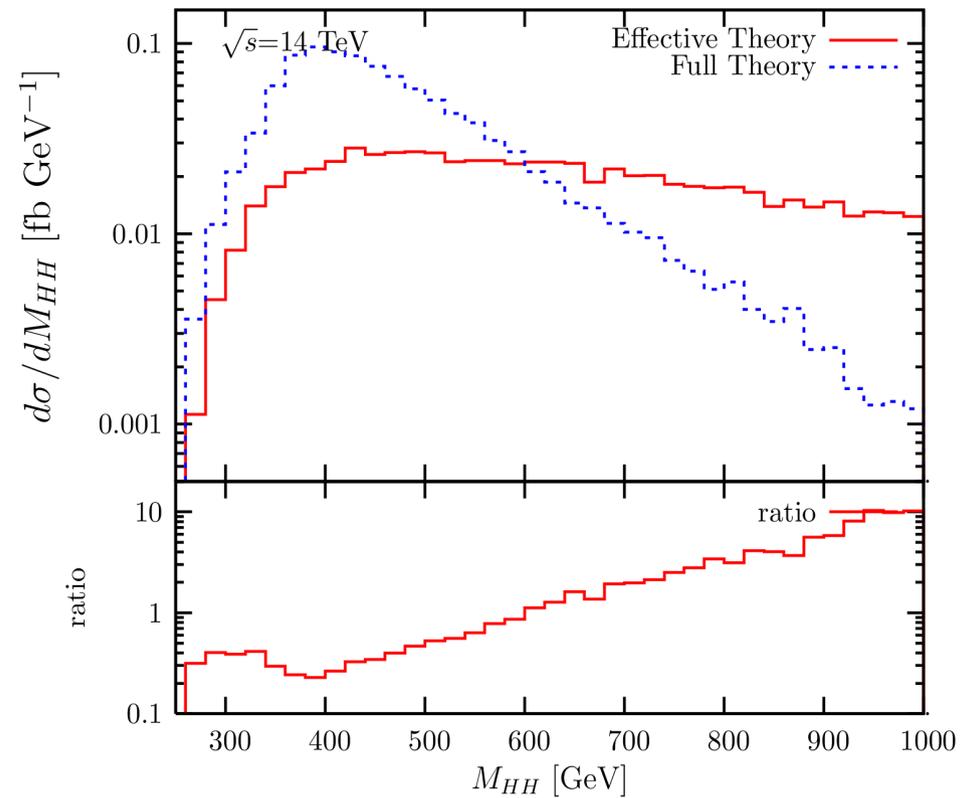
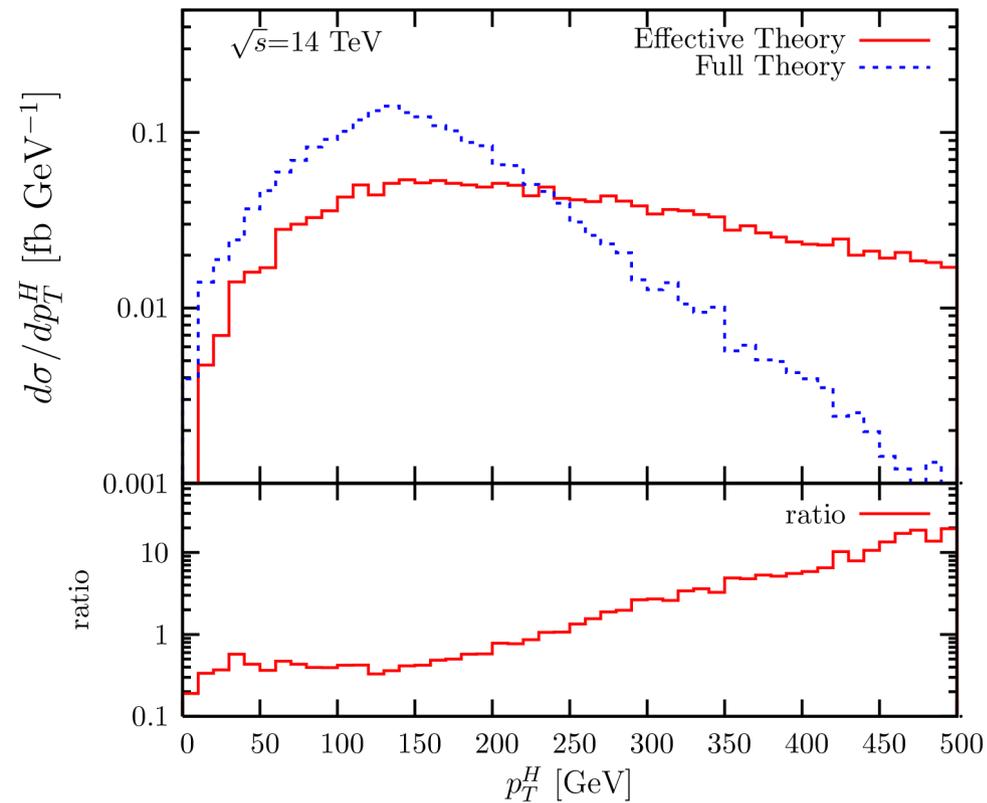
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Using MadGraph5  
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Low energy theory fails to  
reproduce kinematic distributions<sup>17</sup>

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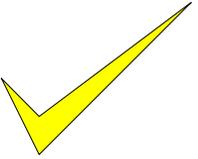
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  - Virtual corrections: Including 2-loop amplitudes

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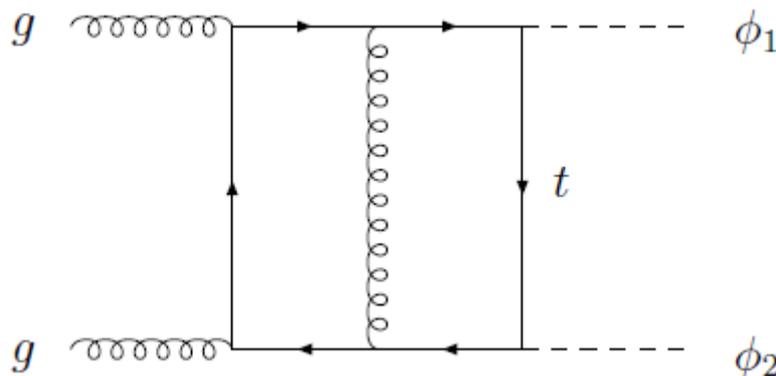
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e.g.



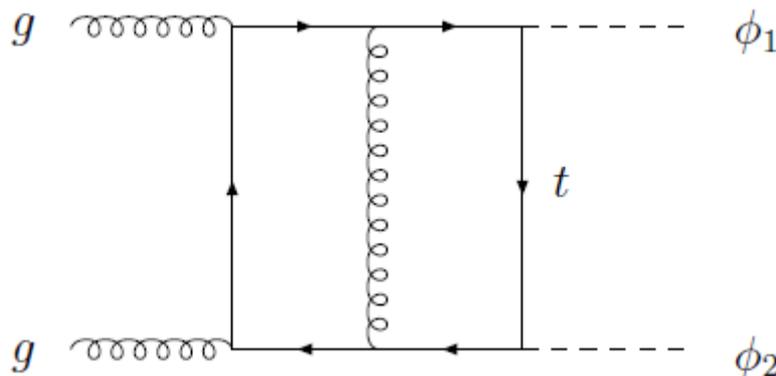
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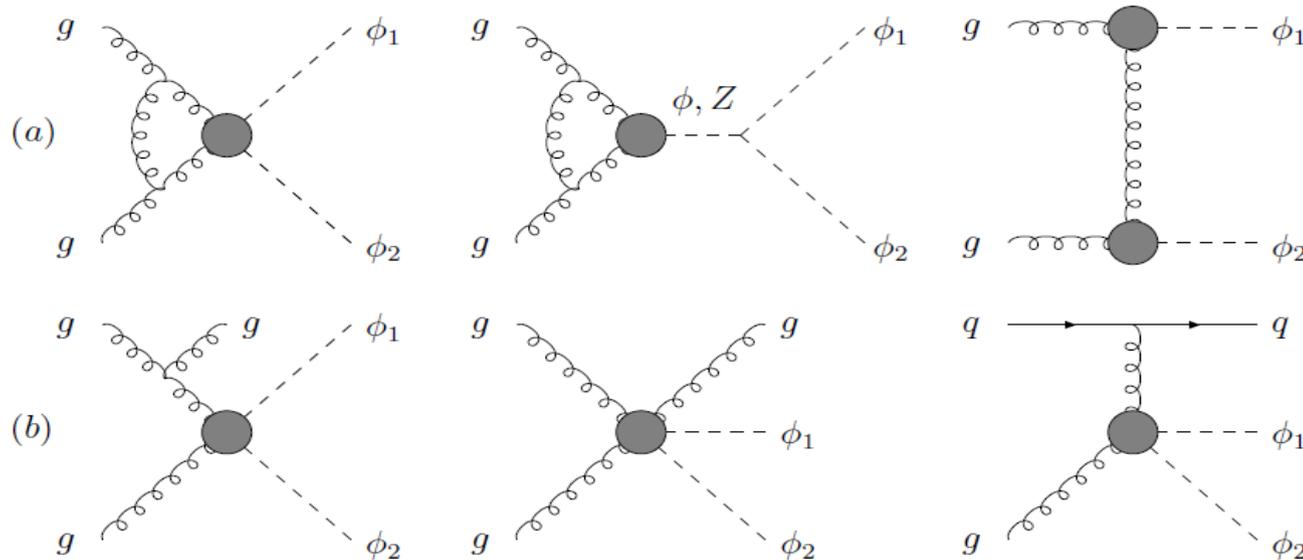
e.g.



**Beyond  
current loop  
technology**

# NLO corrections

- What did we have instead of the full NLO corrections?
- Corrections in the low energy theory:  
Dawson et al. hep-ph/9805244

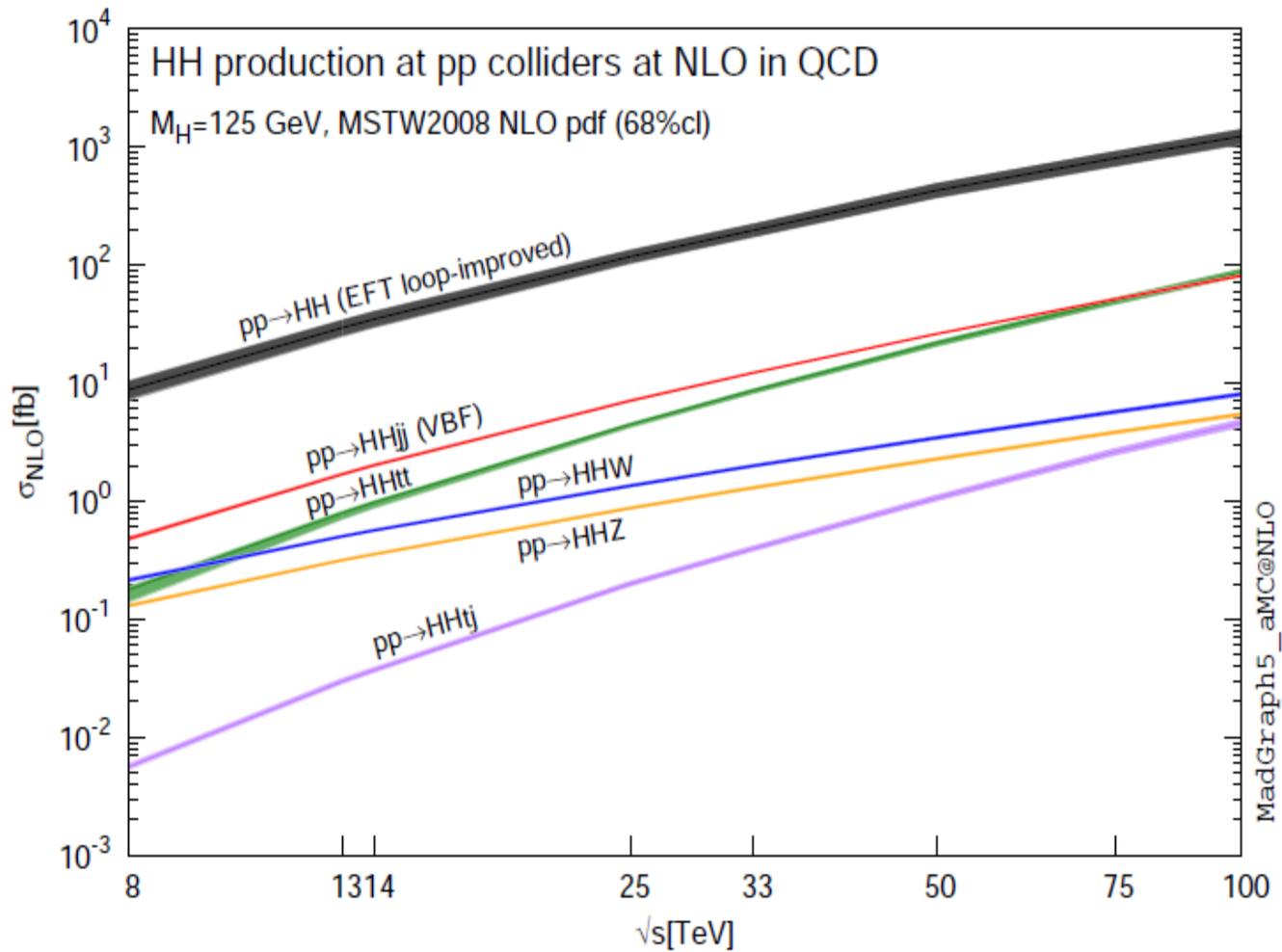


- Improved by using the full loop results for the Born cross section and available in Hpair code (total cross section)

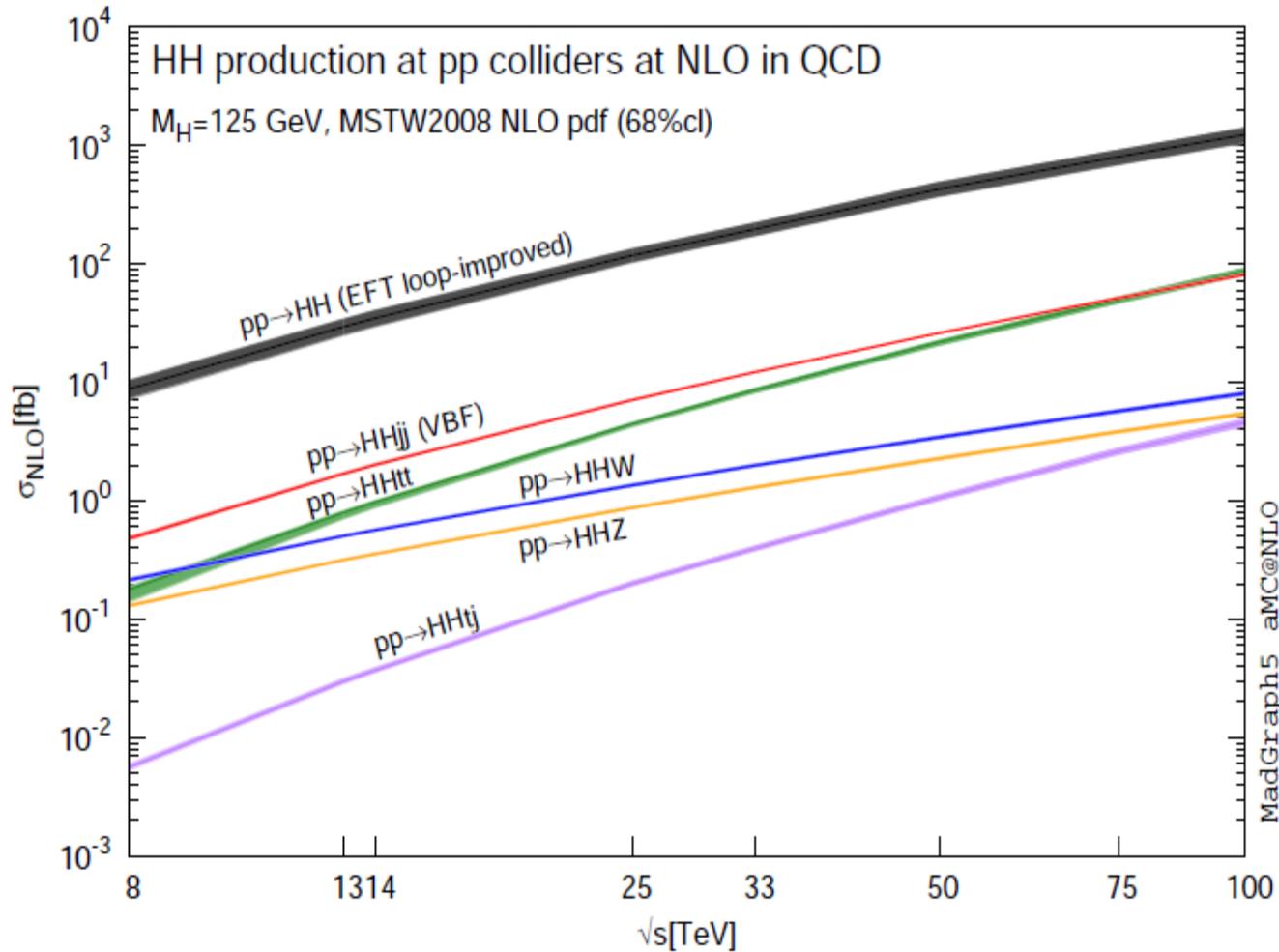
# How did we improve this?

- What we have done:
  - Implementation of gluon fusion channel in aMC@NLO
  - Use LET to generate events
  - Reweigh on an event by event basis using the results of loop matrix elements, obtained from MadLoop for both Born and real emission kinematics
- When done consistently improves previous results, because of better description of real emission processes not included in previous results

# aMC@NLO results

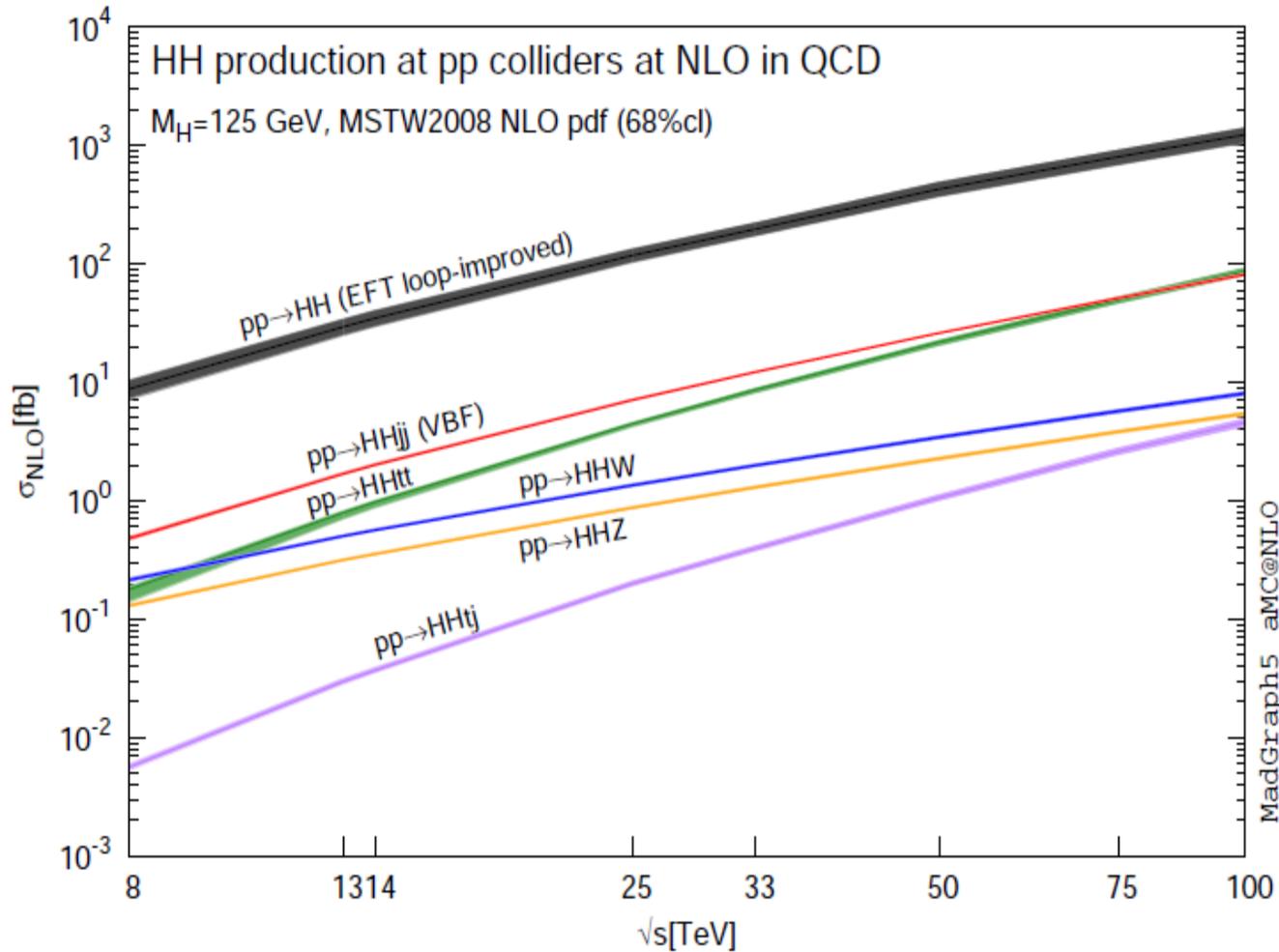


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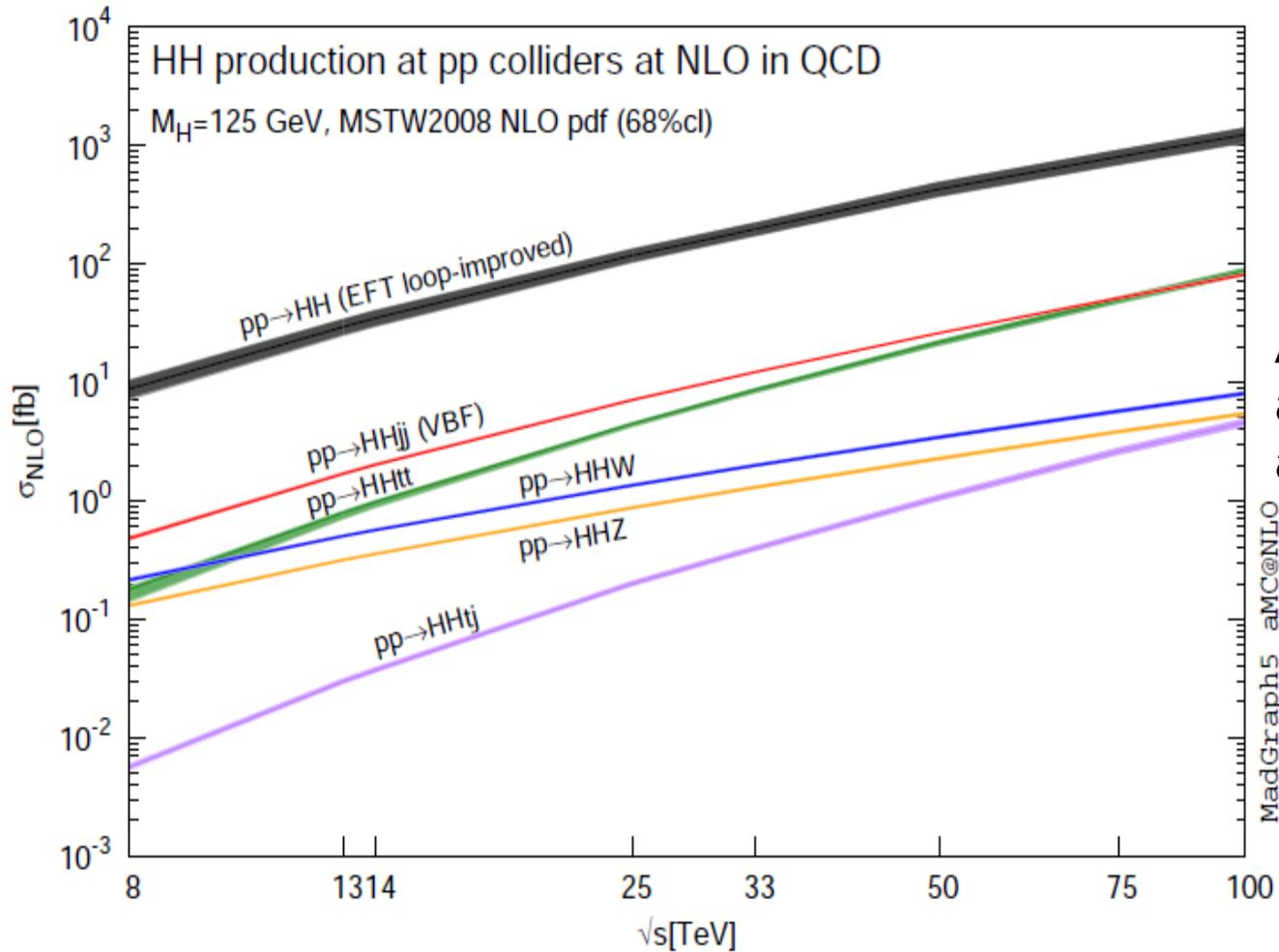
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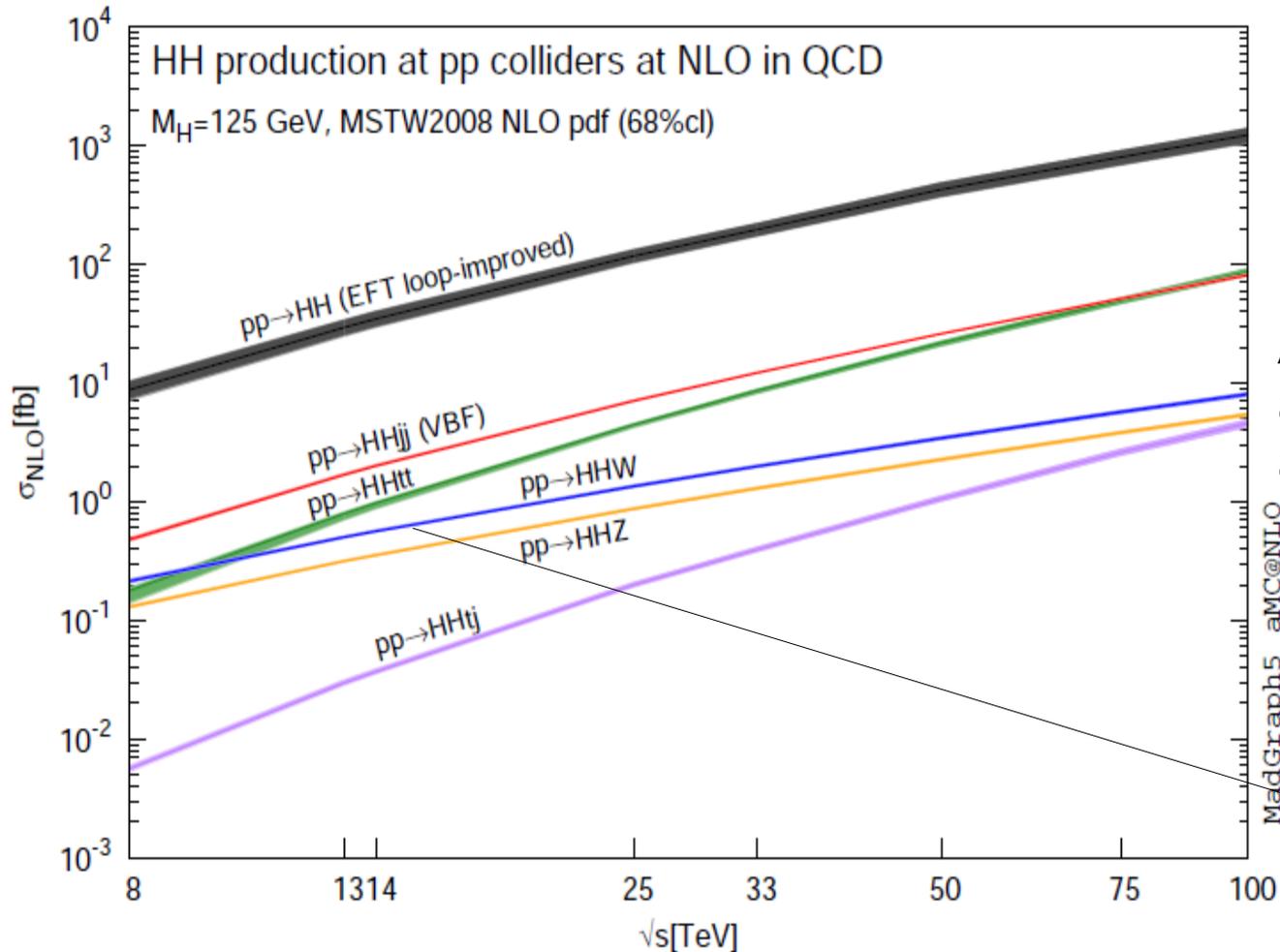
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arXiv:1405.0301

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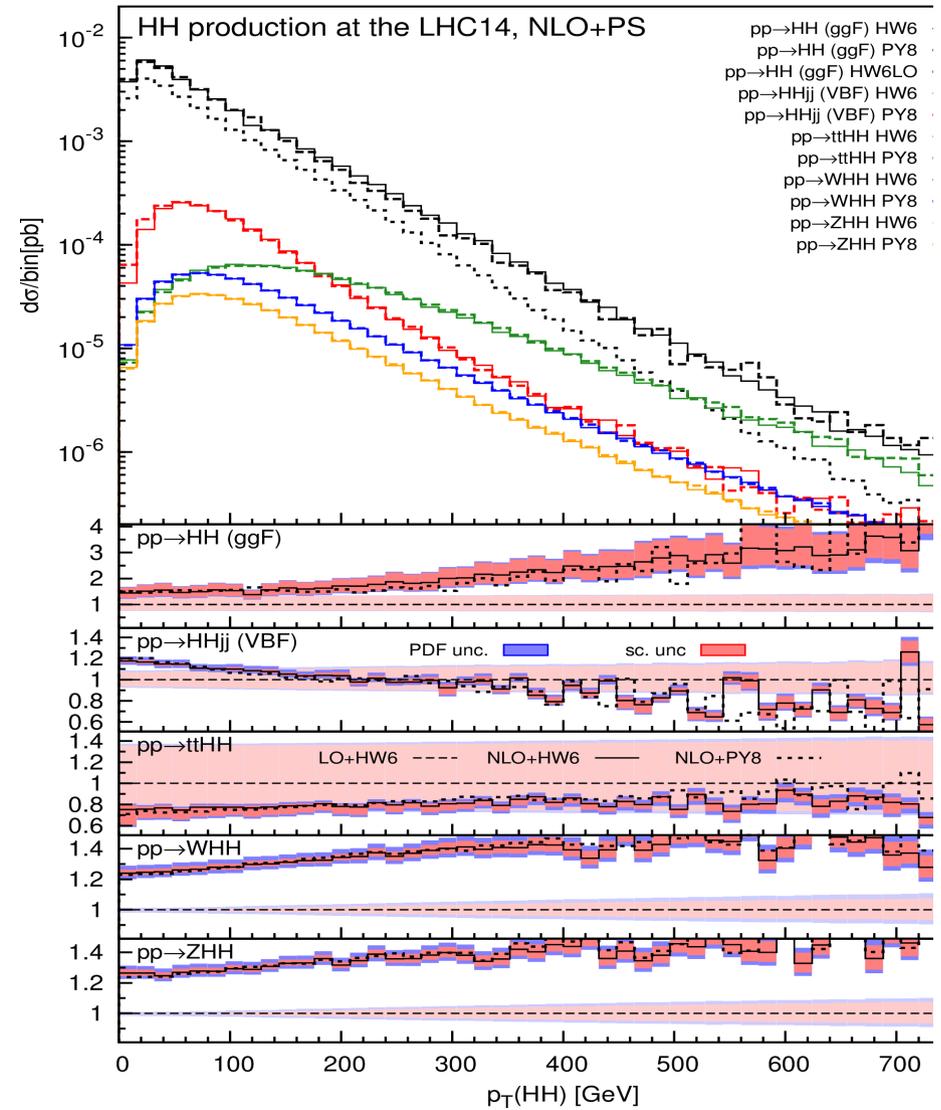
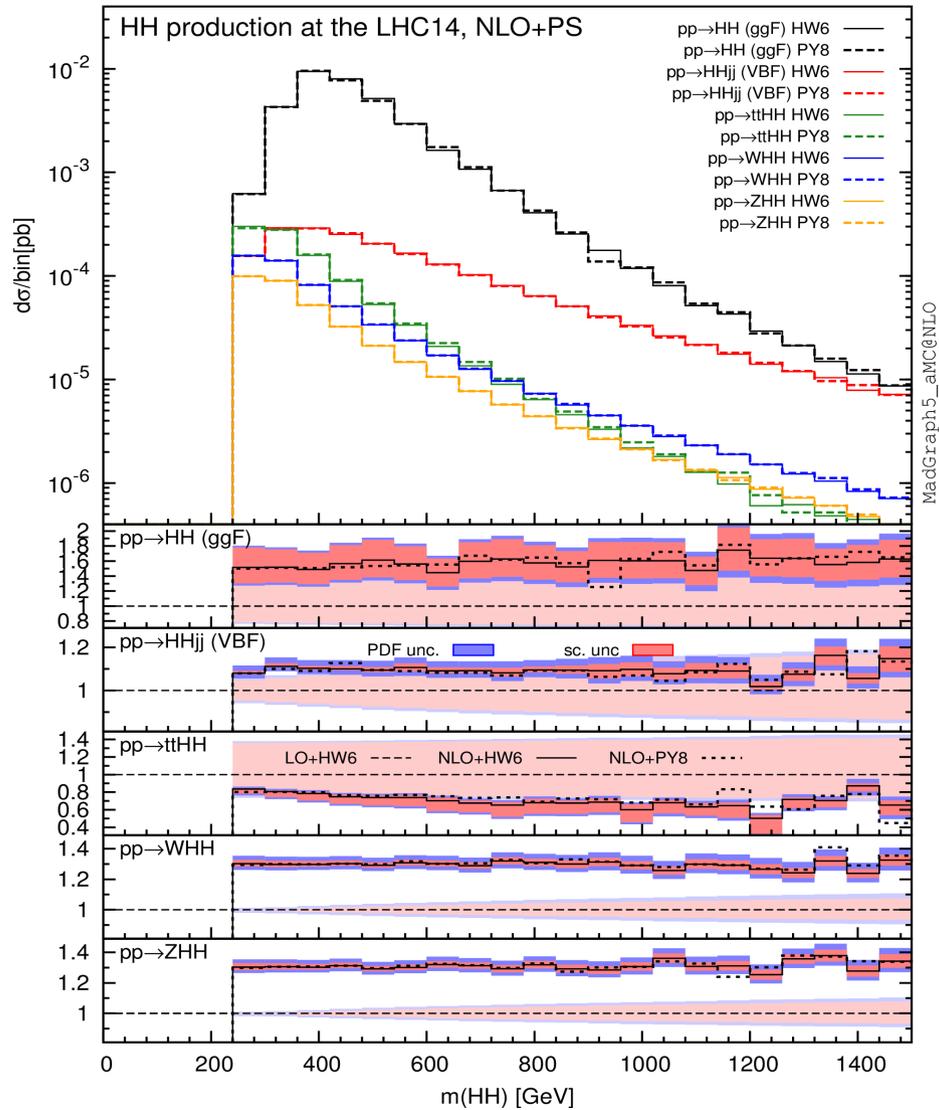


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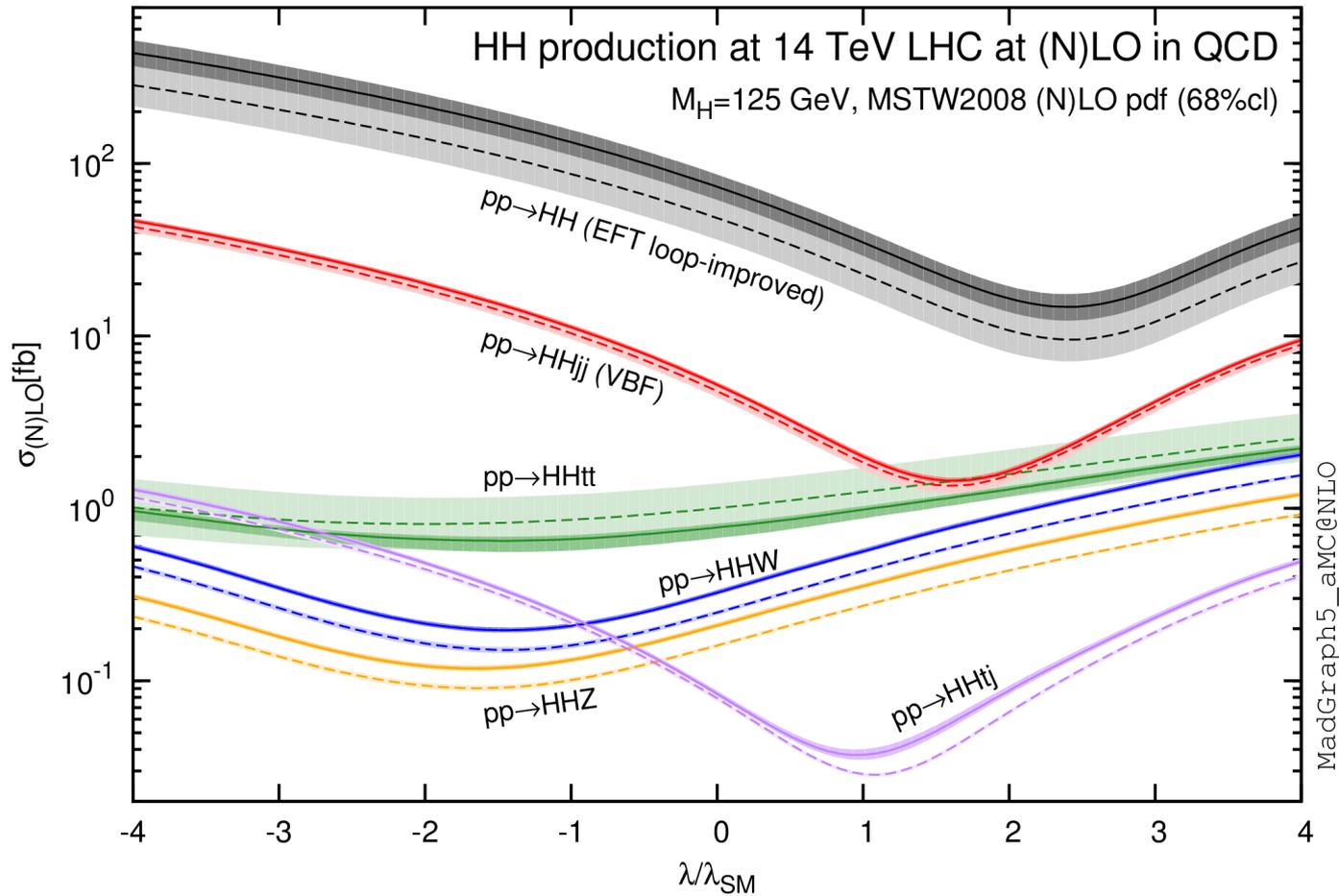
Small difference from  
single Higgs at 14  
TeV:  
Vector boson  
associated  
production and ttHH  
hierarchy reversed

# Differential distributions



Including NLO and PS effects: **best available predictions**<sup>32</sup>

# Dependence on the trilinear Higgs coupling



Sensitivity of  
different  
channels to  $\lambda$

# Conclusions and future plans

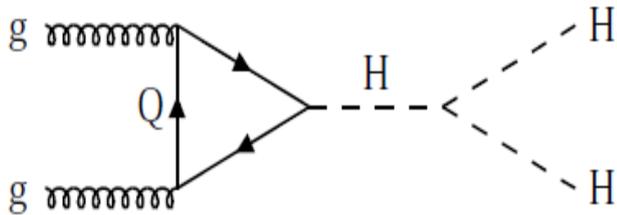
- Higgs pair production key to the measurement of triple Higgs coupling
- Presented results of an efficient MC implementation of the process at NLO provided in an automated way by aMC@NLO
- Results can now be used for phenomenological studies
- Extend to HH production in BSM scenarios like the 2HDM

**Thanks for your attention...**

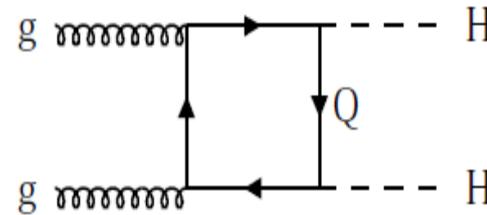
# **ADDITIONAL SLIDES**

# Gluon-gluon fusion

- What do these form factors mean? Why do we have 3?



$$S_z = 0 \quad F_{\Delta}$$

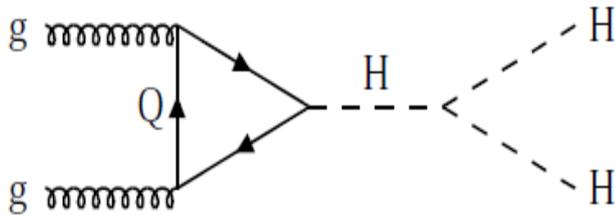


$$S_z = 0 \text{ or } S_z = 2$$

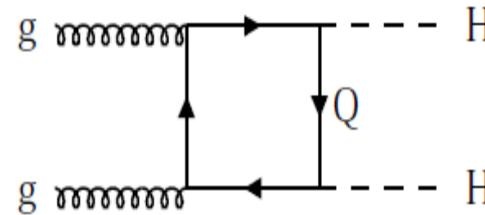
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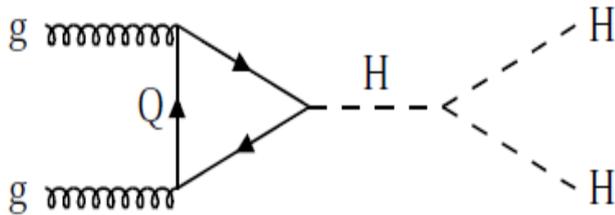
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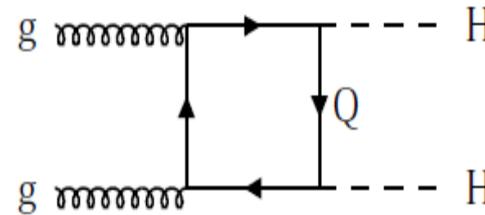
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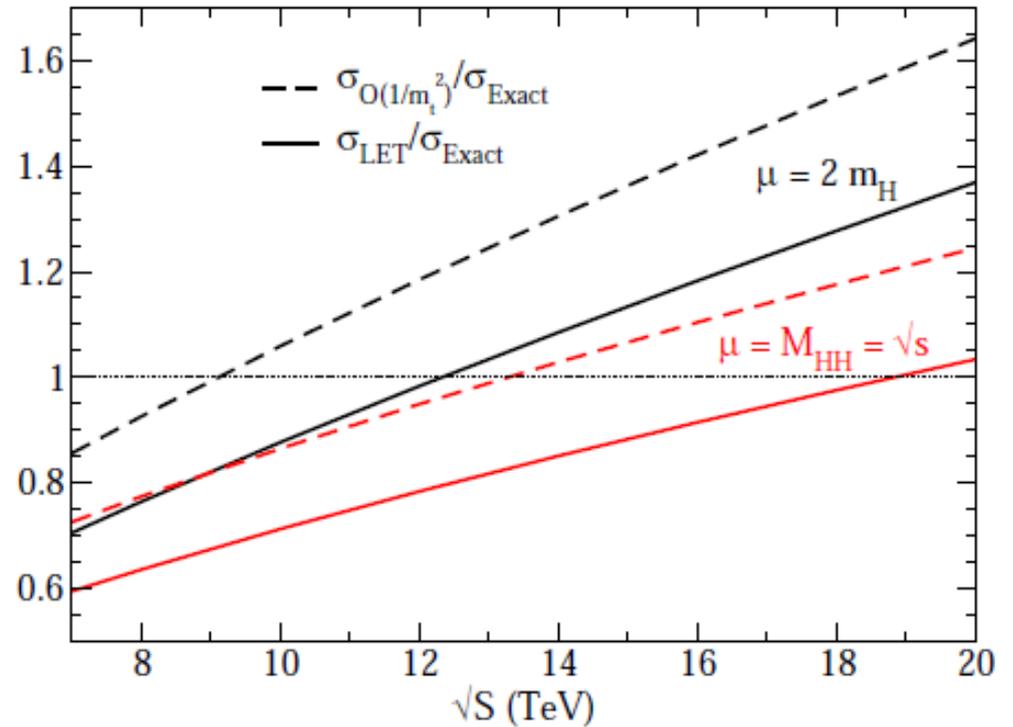
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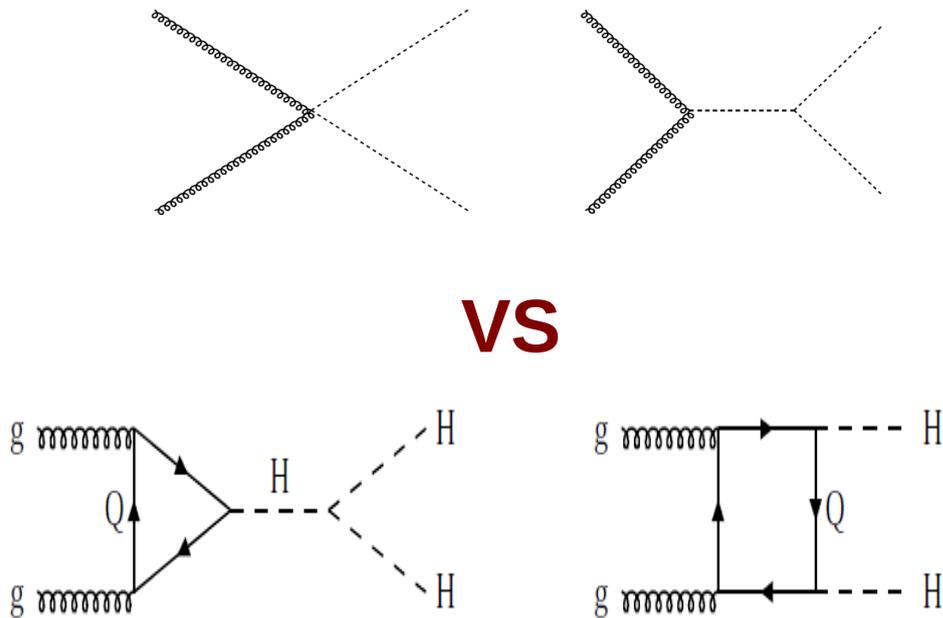
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# Does the effective theory work?

$pp \rightarrow HH, m_H = 125 \text{ GeV}$   
CT10 NLO PDFs

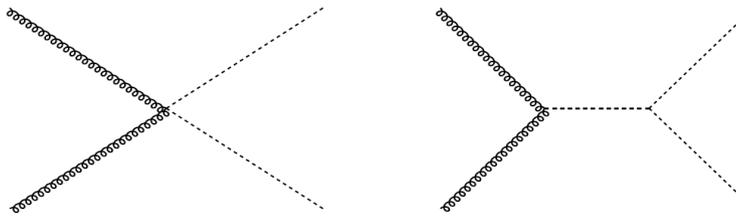


Dawson et al 1206.6663

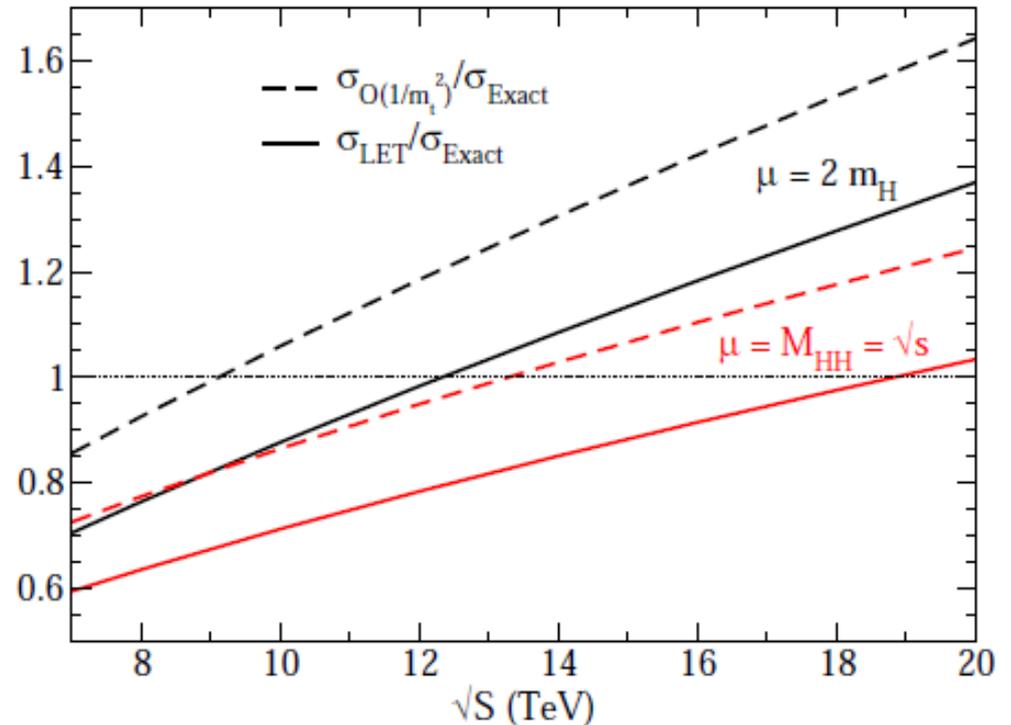
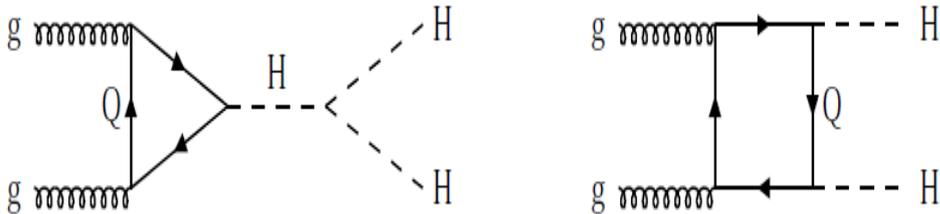


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**VS**

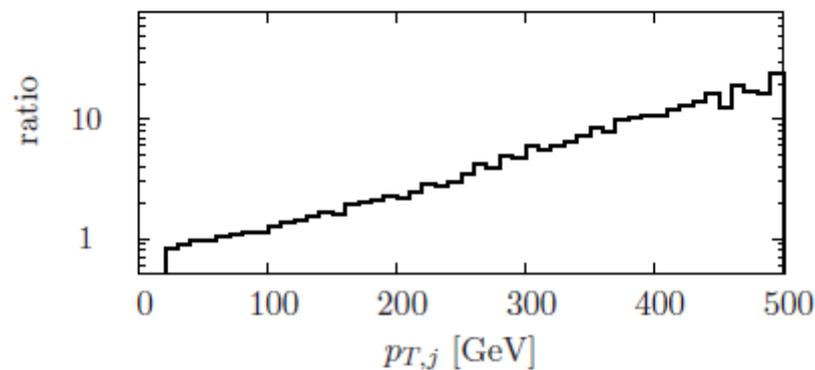
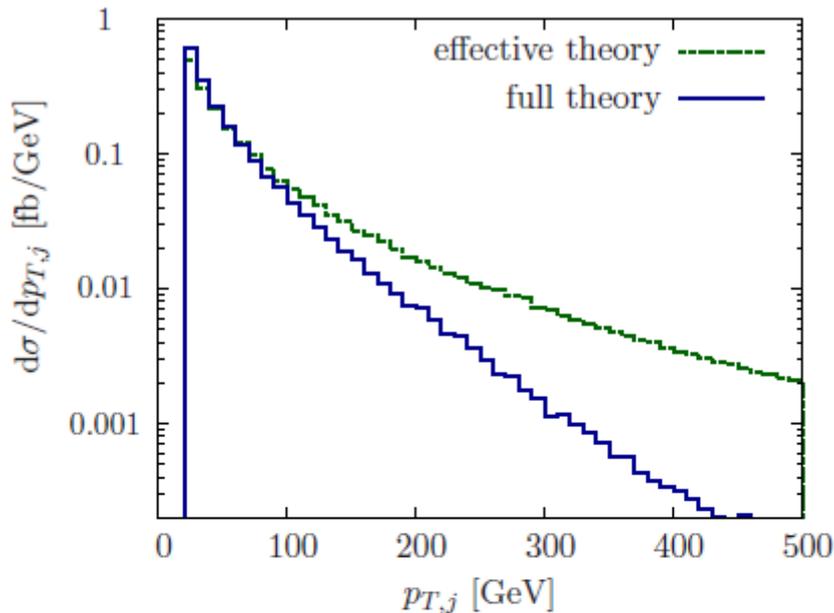


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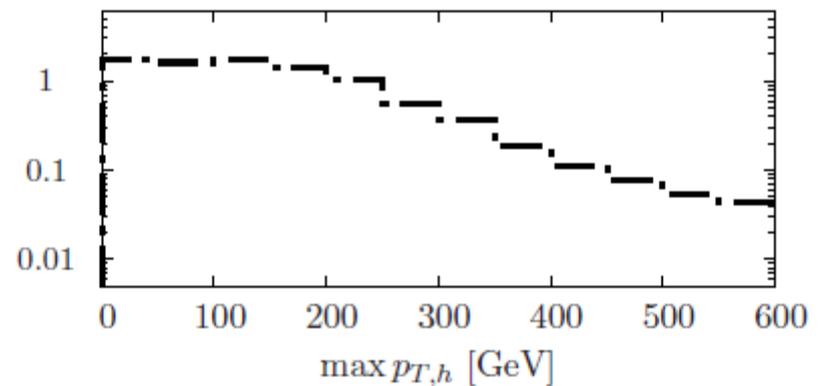
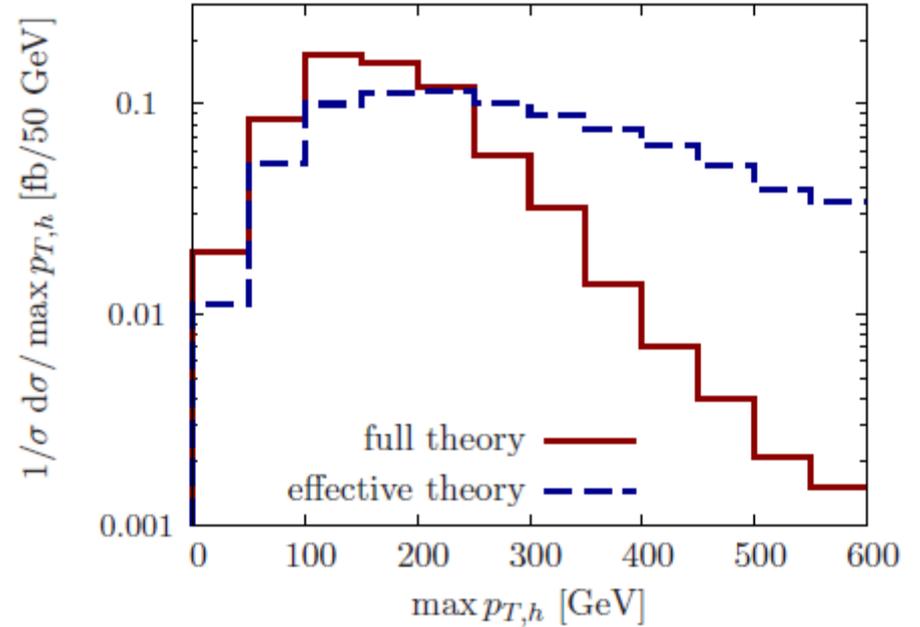
10-20% difference in the total cross section at 14 TeV (depending on the scale choice)

# Higgs pair plus 1,2 jets

How good or bad is the LET?



Dolan et al. 1206.5001



Dolan et al. 1310.1084

# BSM physics in HH

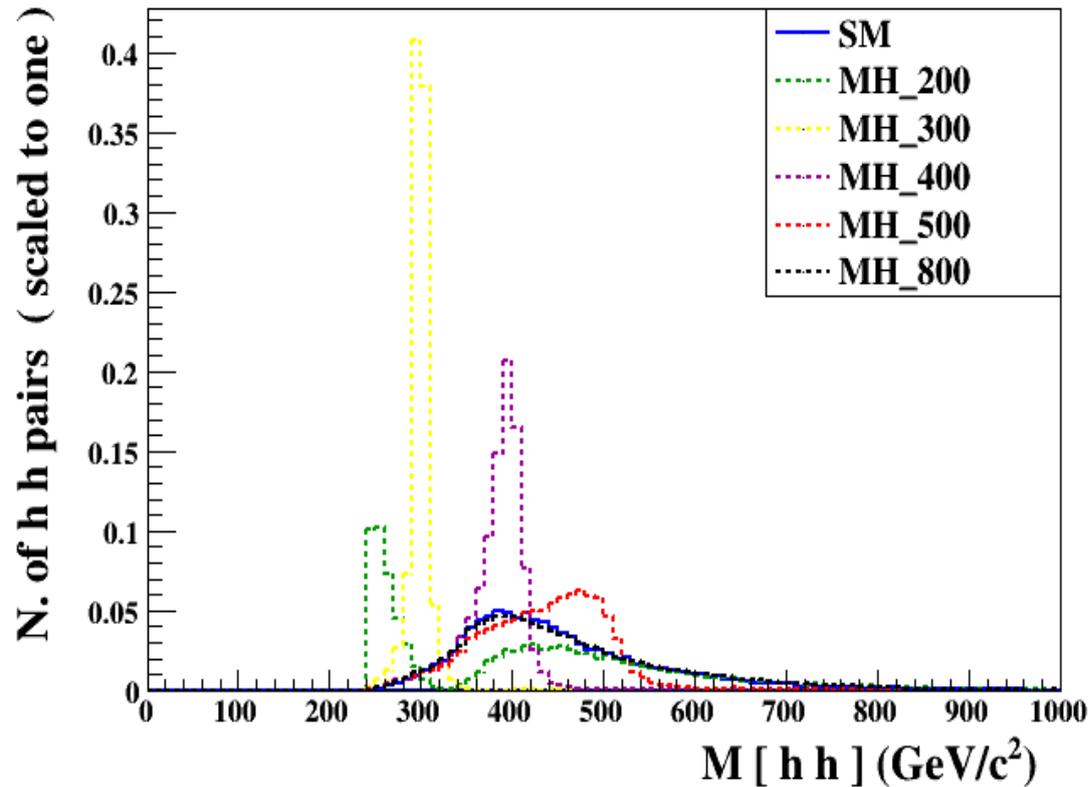
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  - ttHH interactions (1205.5444)
  - Resonances from extra dimensions (1303.6636)
  - Vector-like quarks (1009.4670, 1206.6663)
  - THDM (1009.4670, 1210.8166)
  - Light coloured scalars (1207.4496)

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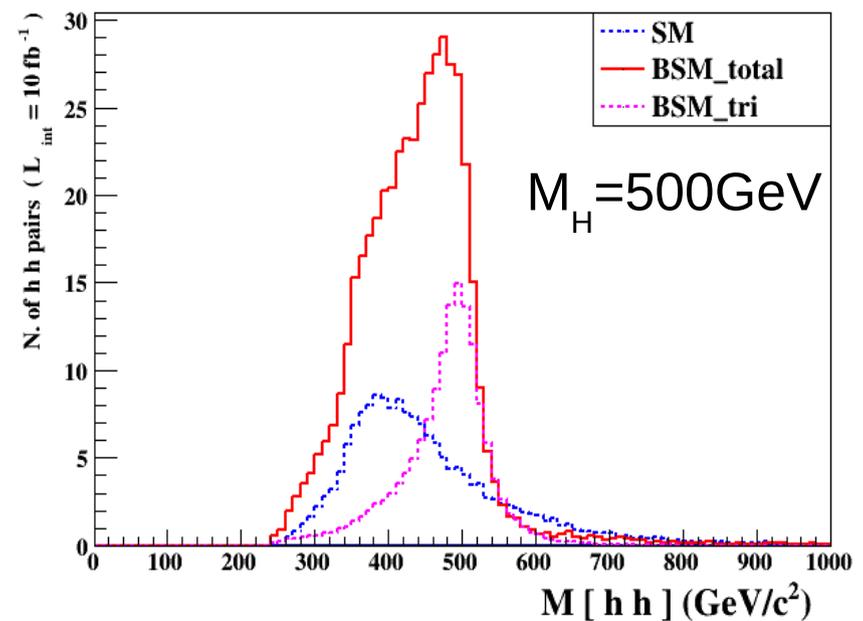
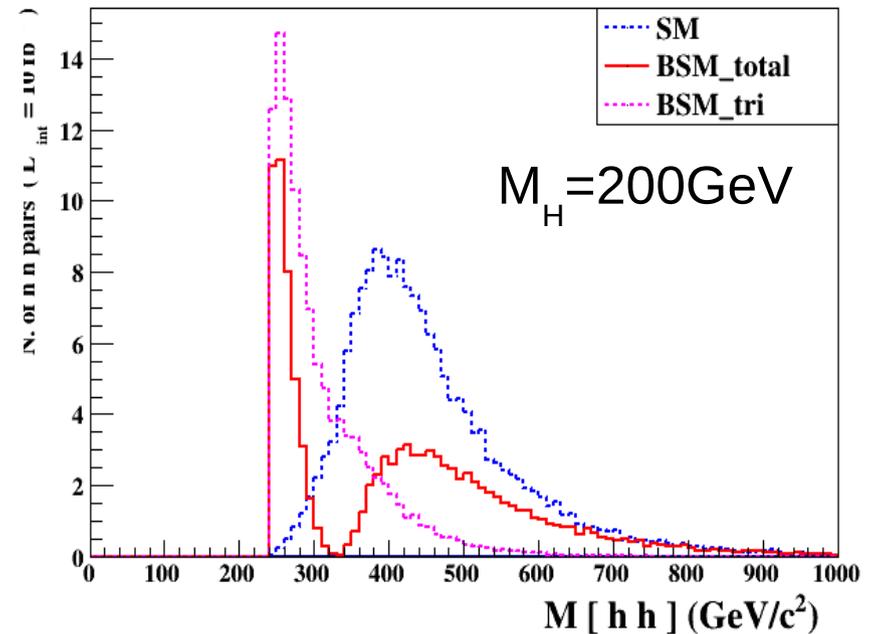
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RICH PHENOMENOLOGY

# Additional scalar with SM couplings Toy model



Interference  
changing sign for  
different masses

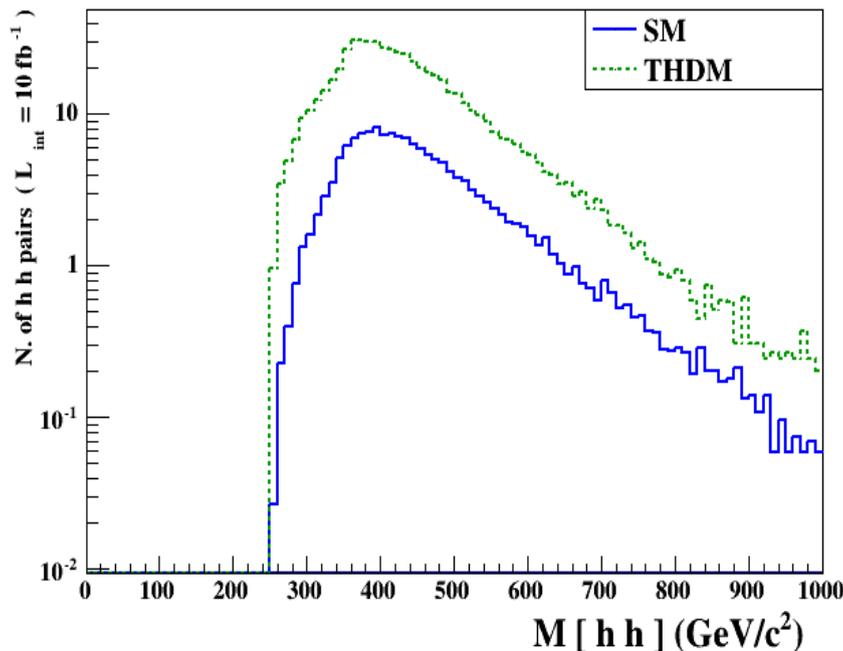


# THDM

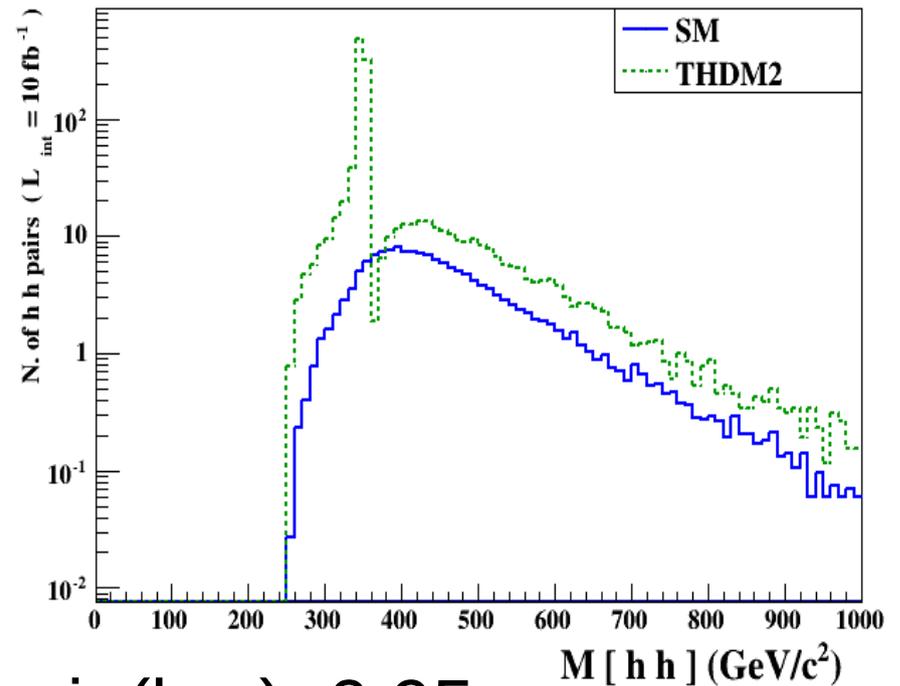
Results for 2 THDM benchmark points (provided by David Lopez Val)

$$M_H = 350 \text{ GeV}$$

Results strongly depend on the modification of the light Higgs couplings and the suppression of heavy Higgs couplings



$$\sin(b-a) = 0.8$$



$$\sin(b-a) = 0.95$$

# Results from aMC@NLO?

## Total cross-section results

	$\sqrt{s} = 8 \text{ TeV}$ (LO) NLO		$\sqrt{s} = 13 \text{ TeV}$ (LO) NLO		$\sqrt{s} = 14 \text{ TeV}$ (LO) NLO	
$HH$ (reweighted)	$(5.44^{+38}_{-26})$	$8.73^{+17+2.9}_{-16-3.7}$	$(19.1^{+33}_{-23})$	$29.3^{+15+2.1}_{-14-2.5}$	$(22.8^{+32}_{-23})$	$34.8^{+15+2.0}_{-14-2.5}$
$HH$ (EFT loop-improved)	$(5.04^{+37}_{-25})$	$9.68^{+21+4.1}_{-17-5.0}$	$(16.6^{+32}_{-23})$	$32.6^{+19+3.0}_{-16-3.8}$	$(20.3^{+32}_{-23})$	$38.5^{+18+2.9}_{-16-3.7}$
$HHjj$ (VBF)	$(0.436^{+12}_{-10})$	$0.479^{+1.8+2.8}_{-1.8-2.0}$	$(1.543^{+9.4}_{-8.0})$	$1.684^{+1.4+2.6}_{-0.9-1.9}$	$(1.839^{+8.9}_{-7.7})$	$2.017^{+1.3+2.5}_{-1.0-1.9}$
$t\bar{t}HH$	$(0.265^{+41}_{-27})$	$0.177^{+4.7+3.2}_{-1.9-3.3}$	$(1.027^{+37}_{-25})$	$0.792^{+2.8+2.4}_{-1.0-2.9}$	$(1.245^{+36}_{-25})$	$0.981^{+2.3+2.3}_{-9.0-2.8}$
$W^+HH$	$(0.111^{+4.0}_{-3.9})$	$0.145^{+2.1+2.5}_{-1.9-1.9}$	$(0.252^{+1.4}_{-1.7})$	$0.326^{+1.7+2.1}_{-1.2-1.6}$	$(0.283^{+1.1}_{-1.3})$	$0.364^{+1.7+2.1}_{-1.1-1.6}$
$W^-HH$	$(0.051^{+4.2}_{-4.0})$	$0.069^{+2.1+2.6}_{-1.9-2.2}$	$(0.133^{+1.5}_{-1.7})$	$0.176^{+1.6+2.2}_{-1.2-2.0}$	$(0.152^{+1.1}_{-1.4})$	$0.201^{+1.7+2.2}_{-1.1-1.8}$
$ZHH$	$(0.098^{+4.2}_{-4.0})$	$0.130^{+2.1+2.2}_{-1.9-1.9}$	$(0.240^{+1.4}_{-1.7})$	$0.315^{+1.7+2.0}_{-1.1-1.6}$	$(0.273^{+1.1}_{-1.3})$	$0.356^{+1.7+1.9}_{-1.2-1.5}$
$tjHH$ ( $\cdot 10^{-3}$ )	$(5.057^{+2.0}_{-3.2})$	$5.606^{+4.4+3.9}_{-2.3-4.2}$	$(23.20^{+0.0}_{-0.8})$	$29.77^{+4.8+2.8}_{-2.8-3.2}$	$(28.79^{+0.0}_{-1.2})$	$37.27^{+4.7+2.6}_{-2.7-3.0}$

Significant decrease of scale and PDF uncertainties for the NLO results

All results apart from gluon fusion are completely automated

# What was available?

- Hpair: Fortran code by Spira
  - Parton level full theory LO and approximate (LET) NLO results
  - Total cross section
- MadGraph 5
  - Exact LO matrix elements for pair production
  - Some information in:
    - <https://cp3.irmp.ucl.ac.be/projects/cp3admin/wiki/UsersPage/Physics/Exp/HHproduction>