

DARK MATTER IN SUSY DFSZ AXION MODEL

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based on

KJB, Baer, Chun 1309.0515, 1309.5365

KJB, Baer, Lessa, Serce, in progress

Pheno2014@Pittsburgh

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OVERVIEW

SUSY & PQ

Fine-tuning problems in SM:

- quadratic divergence: $\Delta m_h^2 = \Lambda_{\text{cut-off}}^2 + \dots$ removed by SUSY
- Strong CP problem: $\bar{\theta} G \tilde{G} \Rightarrow \left(\bar{\theta} + \frac{a}{f_a} \right) G \tilde{G} \Rightarrow \left\langle \frac{a}{f_a} \right\rangle = -\bar{\theta}$ axion

SUSY axion

SUSY partner saxion, axino:

- thermal production: scattering, decay & inverse decay
- late decay: might decay after neutralino freeze-out

affects the neutralino density \longrightarrow augmented WIMP density

also axion CDM

two DM scenario

DFSZ AXION MODEL

Effective Interaction:

$$W = Z(XY - v_{PQ}^2) + \frac{X^2}{M_P} H_u H_d$$

$$X = (v_{PQ} + \rho_1)e^{A/v_{PQ}}, \quad Y = (v_{PQ} + \rho_1)e^{-A/v_{PQ}}, \quad Z = \rho_2$$



$$W_{\text{eff}} = \mu e^{2A/v_{PQ}} H_u H_d \quad \mu \sim v_{PQ}^2/M_P \quad \text{Kim-Nilles mechanism}$$

Interactions via Higgs sector:

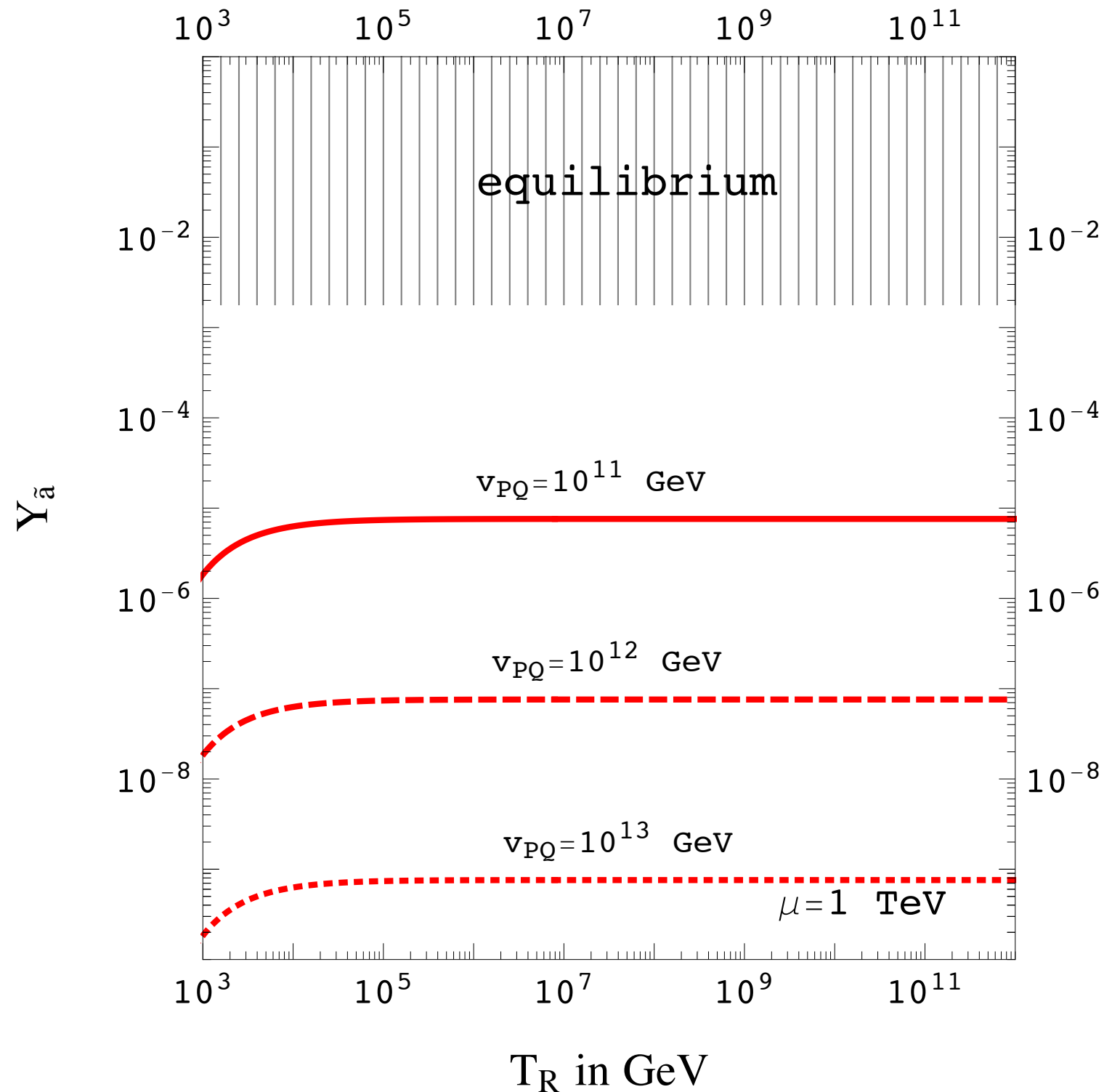
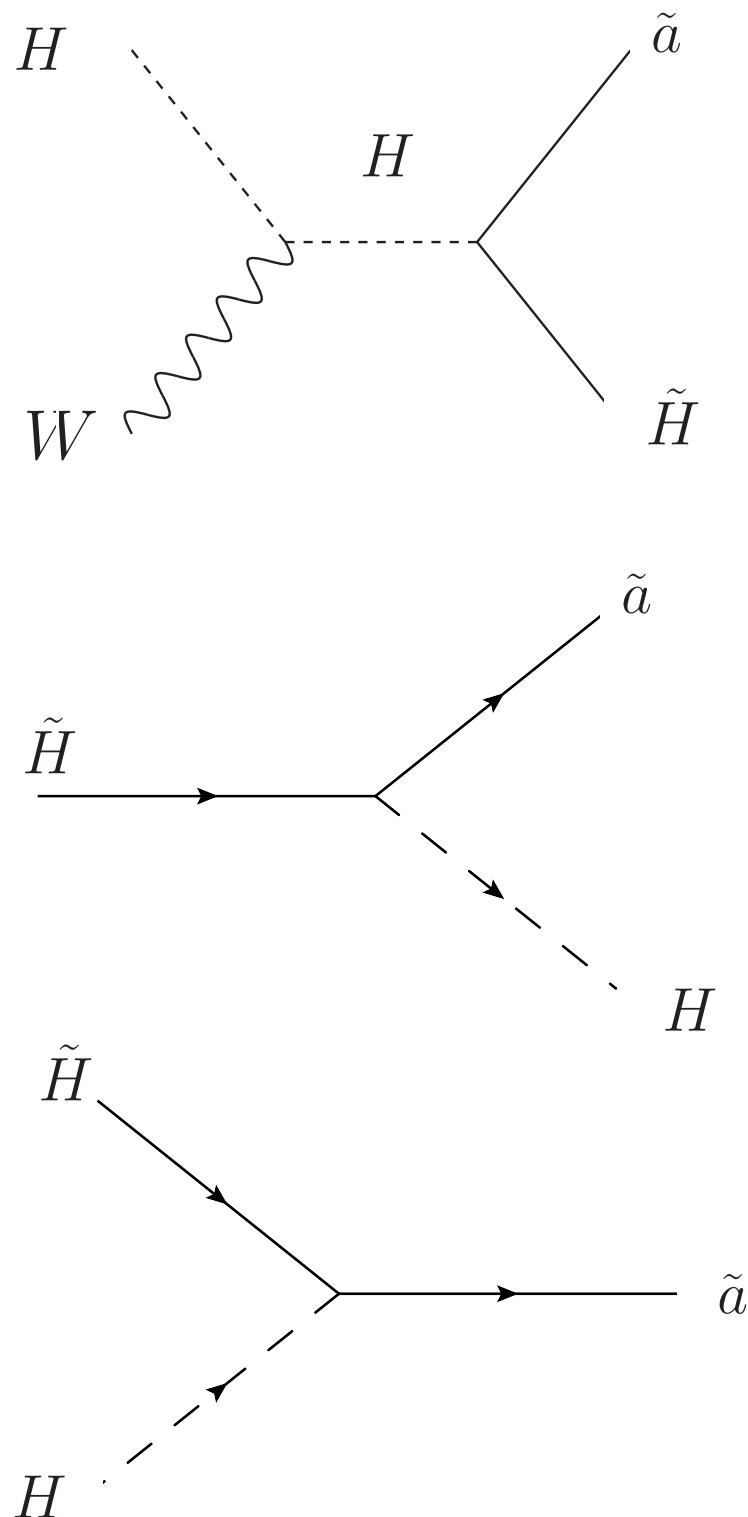
- **AHH** trilinear int.
- **mixing** with higgs & higgsino

Production of axino/saxion:

scattering/decay/inverse-decay of particles in thermal equilibrium:

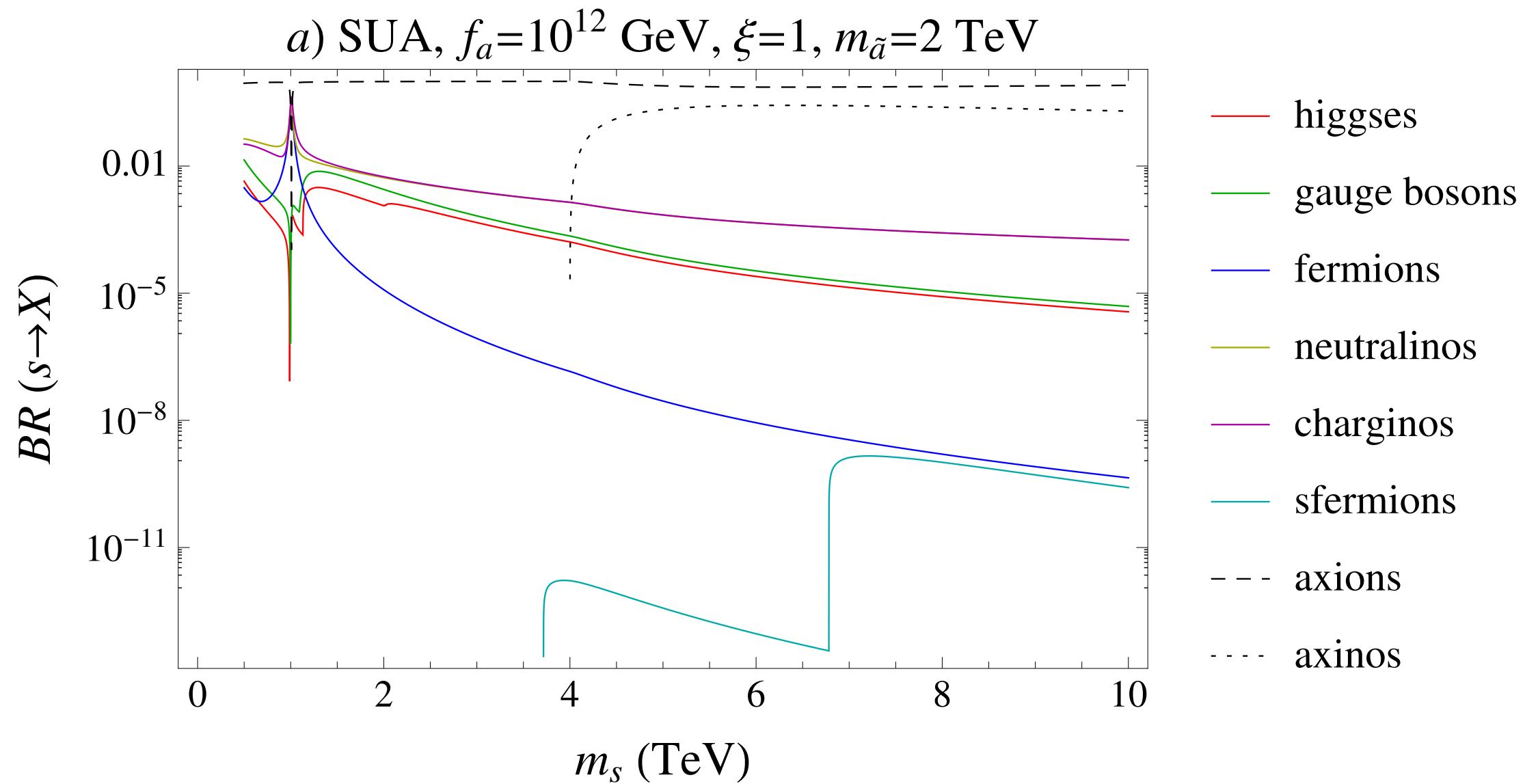
“Freeze-In”

Chun; KJB, Choi, Im; KJB, Chun, Im

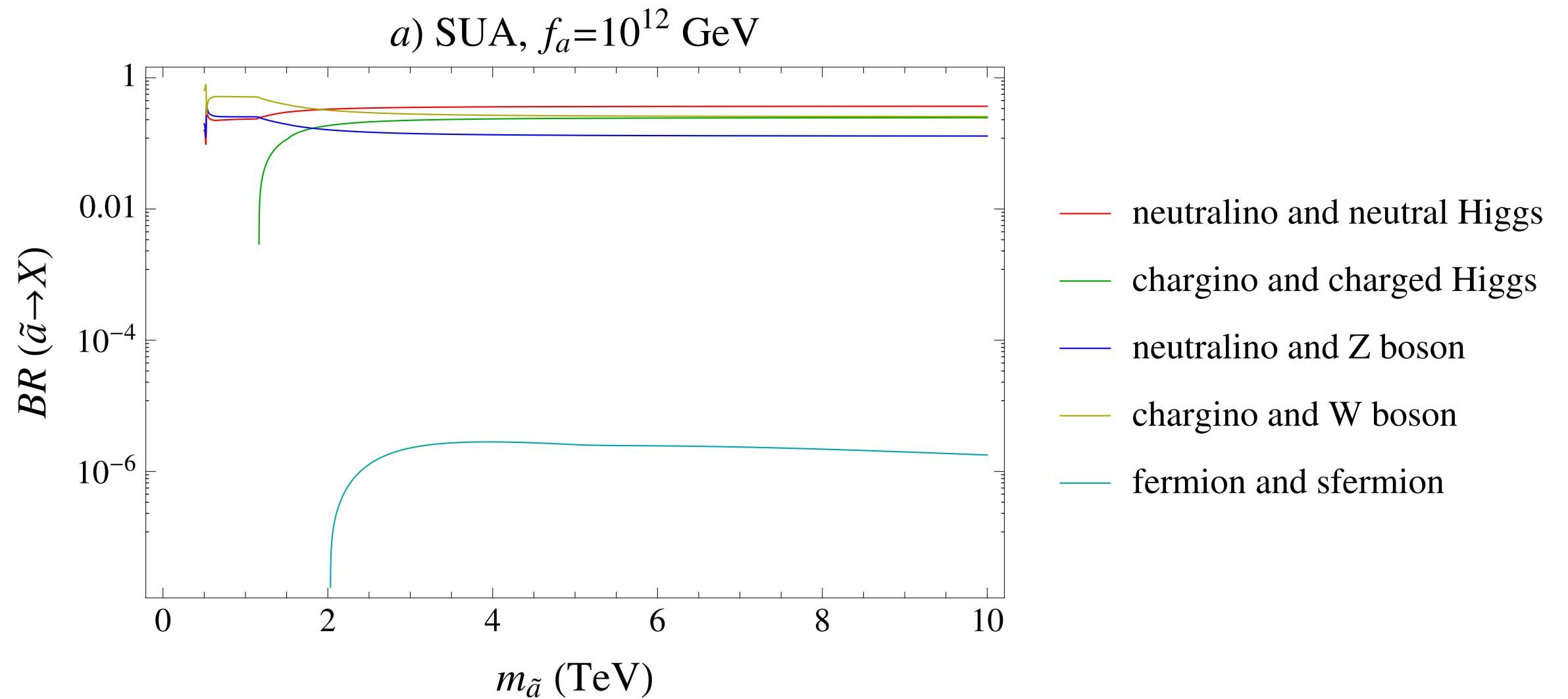


Decay of saxion: $T_D^s = \mathcal{O}(10^{-4}) - \mathcal{O}(10^4)$ GeV

KJB, Baer, Chun



Decay of axino: $T_D^{\tilde{a}} = \mathcal{O}(10^{-4}) - \mathcal{O}(10^4)$ GeV



BOLTZMANN EQS.

8 Coupled Boltzmann eqs:

- 1) rad
- 2) neutralino
- 3) axion TP
- 4) axion CO
- 5) saxion TP
- 6) saxion CO
- 7) axino
- 8) gravitino

$$\begin{aligned} \frac{dn_i}{dt} + 3Hn_i &= \langle \sigma v \rangle (\bar{n}_i^2 - n_i^2) \\ &- \Gamma_i m_i \frac{n_i}{\rho_i} \left(n_i - \bar{n}_i \sum_{i \rightarrow \dots} B_{ab\dots} \frac{n_a n_b \dots}{\bar{n}_a \bar{n}_b \dots} \right) \\ &+ \sum_a \Gamma_a B_i m_a \frac{n_a}{\rho_a} \left(n_a - \bar{n}_a \sum_{a \rightarrow i\dots} \frac{B_{ib\dots}}{B_i} \frac{n_i n_b \dots}{\bar{n}_i \bar{n}_b \dots} \right) \end{aligned}$$

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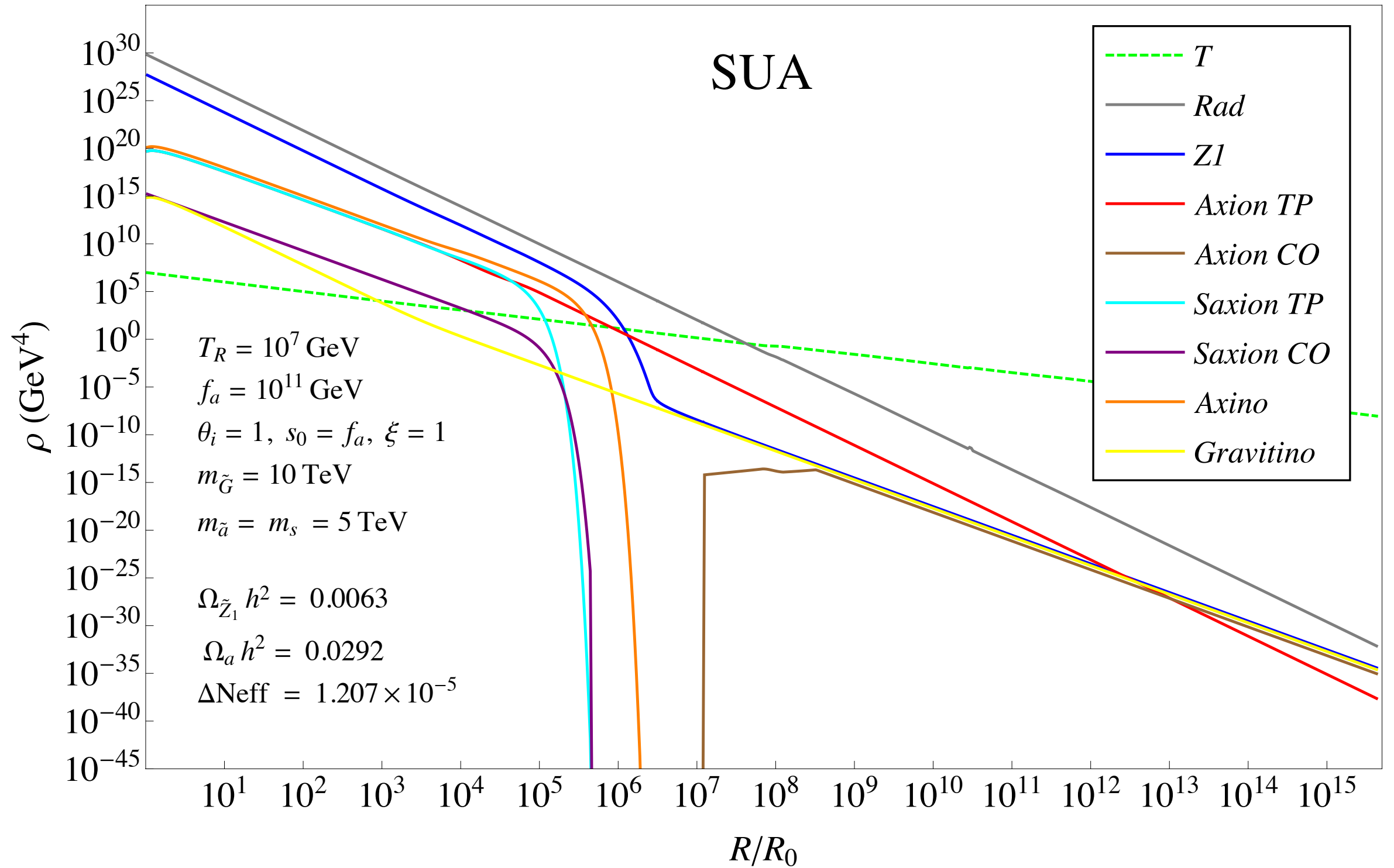
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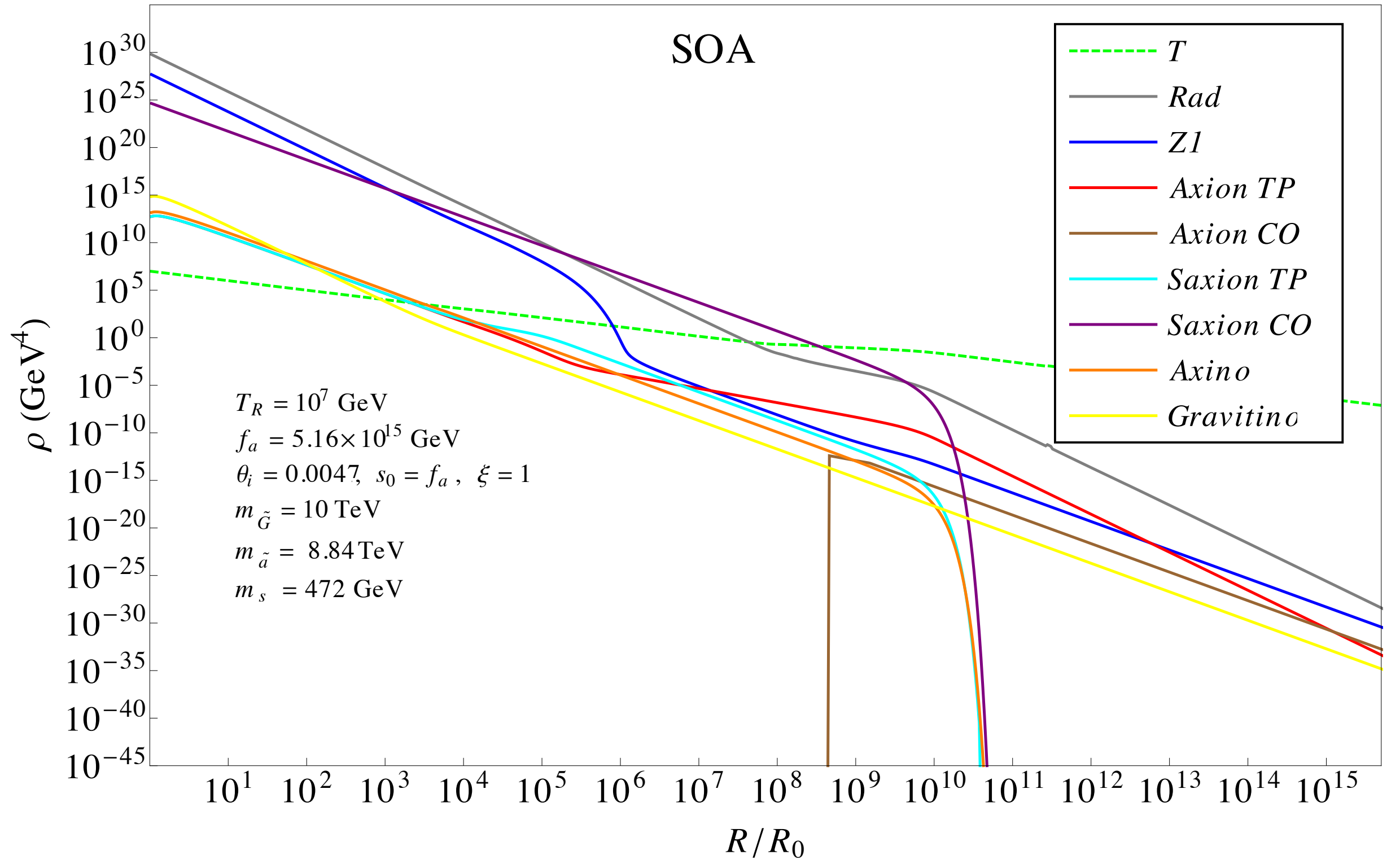
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 \frac{d\rho_i}{dt} + 3H(\rho_i + P_i) &= \langle \sigma v \rangle \frac{\rho_i}{n_i} (\bar{n}_i^2 - n_i^2) \\
 &- \Gamma_i m_i \left(n_i - \bar{n}_i \sum_{i \rightarrow \dots} B_{ab\dots} \frac{n_a n_b \dots}{\bar{n}_a \bar{n}_b \dots} \right) \\
 &+ \sum_a \Gamma_a B_i \frac{m_a}{2} \left(n_a - \bar{n}_a \sum_{a \rightarrow i\dots} \frac{B_{ib\dots}}{B_i} \frac{n_i n_b \dots}{\bar{n}_i \bar{n}_b \dots} \right)
 \end{aligned}$$

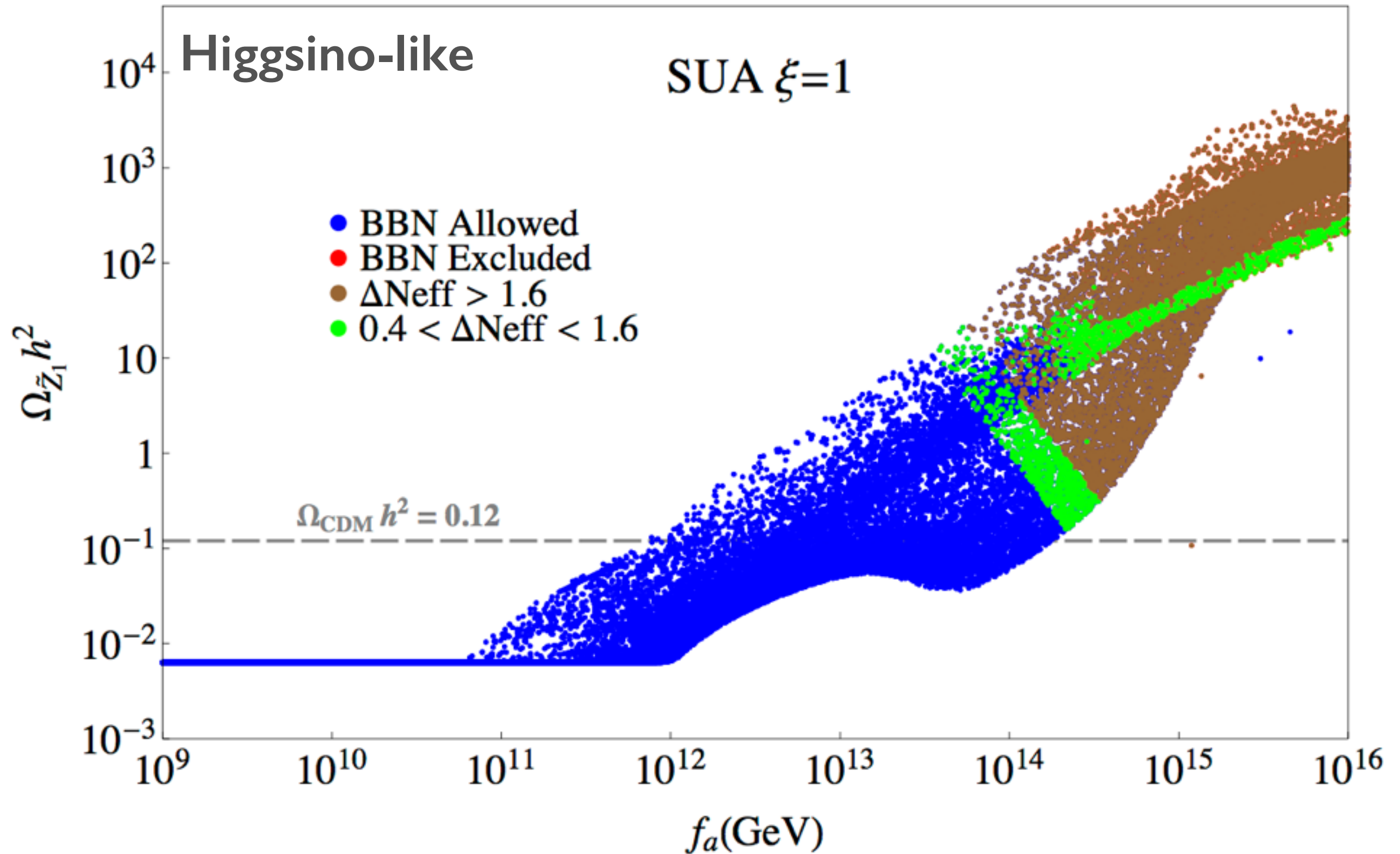
EVOLUTION



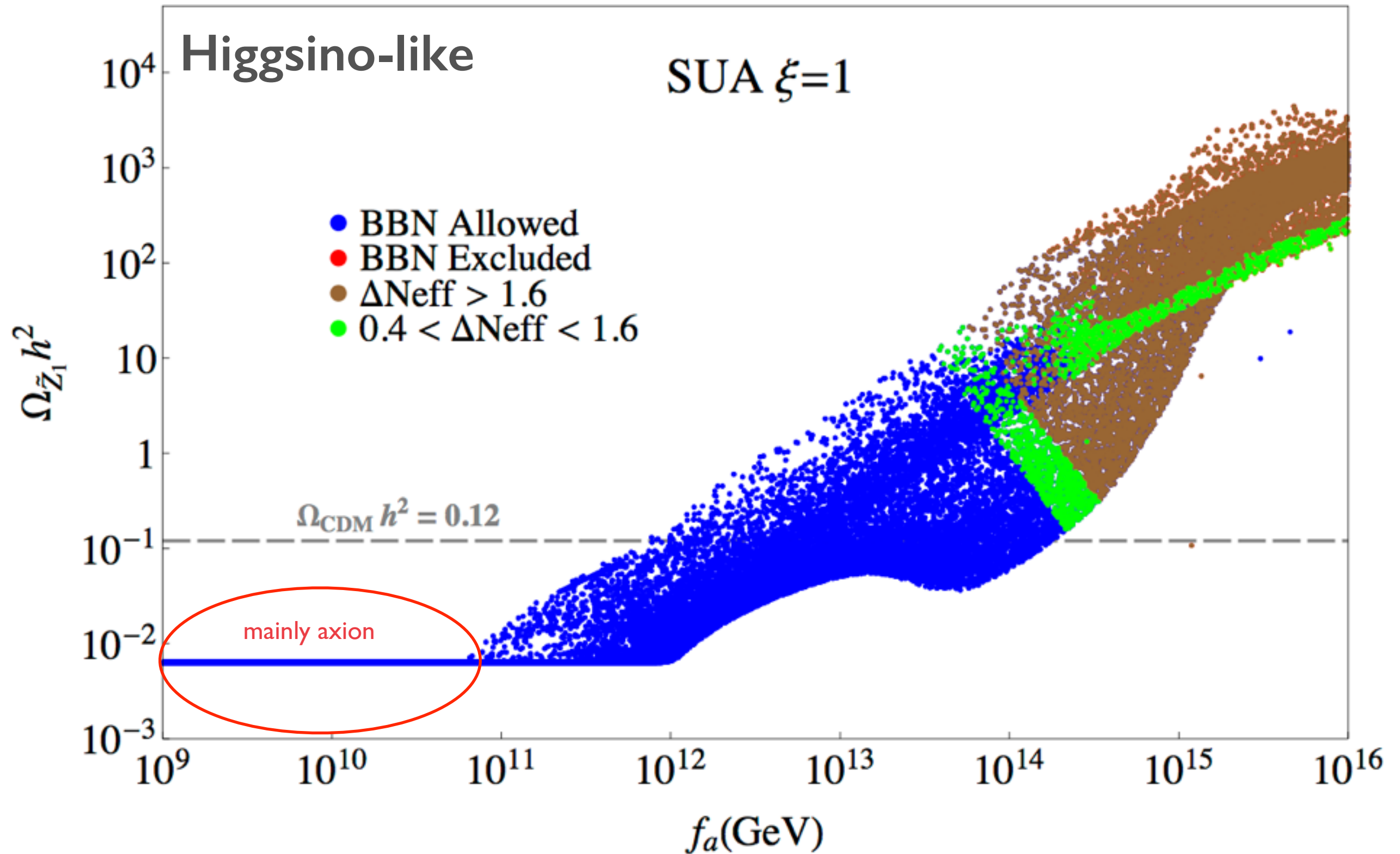
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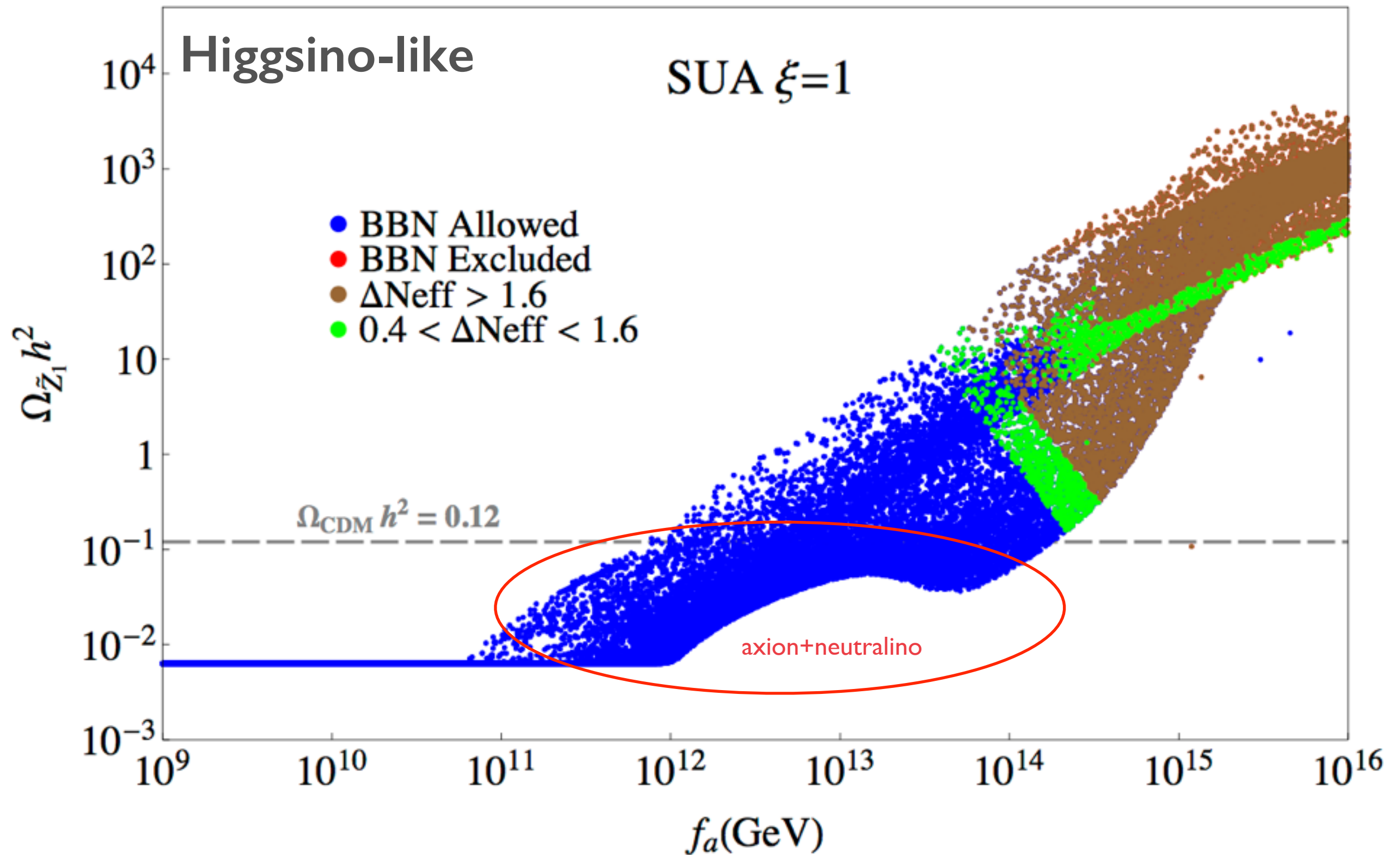
RESULTS



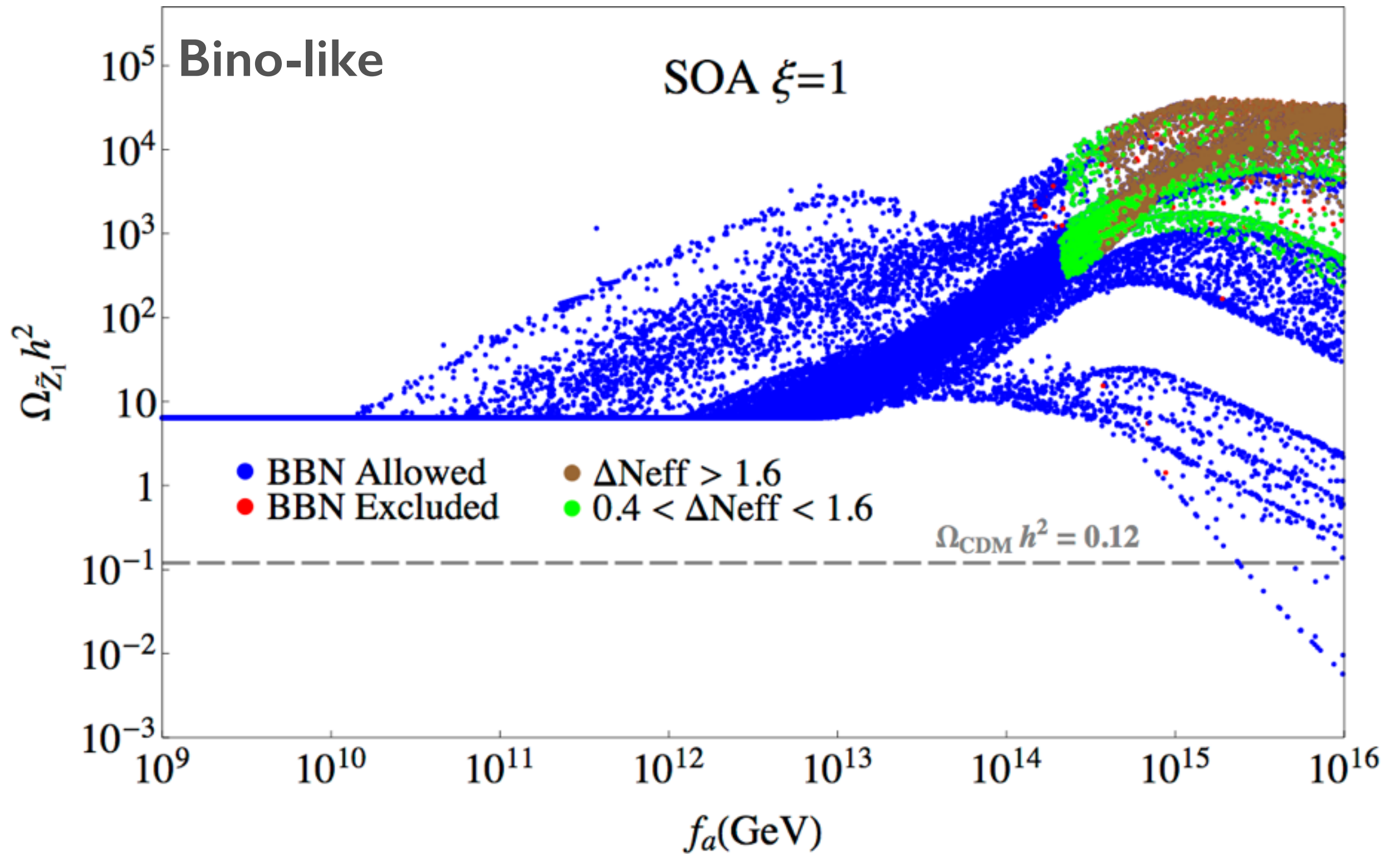
RESULTS



RESULTS



RESULTS



COMMENTS ON BICEP2

BICEP2 result:

$r \sim 0.16$ with $H_I \sim 10^{14}$ GeV implies

1) PQ broken during & after inflation ($f_a > H_I$):

Marsh, Grin, Hlozek, Ferreira;
Visinelli, Gondolo

massless axion \rightarrow isocurvature perturb.

$$\mathcal{P}_a \sim 4 \left(\frac{\Omega_a}{\Omega_{CDM}} \right)^2 \left(\frac{H_I}{2\pi f_a \theta_i} \right)^2 \lesssim 0.04 \mathcal{P}_{\mathcal{R}}$$

Planck 2013

$$f_a \gtrsim 10^{28} \text{ GeV} \times \left(\frac{\Omega_a h^2}{0.12} \right)^{1.22}$$

2) PQ restored after inflation ($f_a < H_I$):

no isocurvature perturb.

domain wall problem arises, $N_{DW}=6$ for DFSZ

Possible solutions:

1) Explicit PQ breaking during inflation: [Higaki, Jeong, Takahashi](#)

massive axion \rightarrow no isocurvature perturb.

$$m_a^2(t = t_I) \sim H_I^2$$

2) PQ scale during inflation : $f_a(t_I) \gg f_a(t_0)$ [Choi, Jeong, Seo; Chun](#)

$$f_a(t_I) \sim (H_I M_P^n)^{1/(n+1)}$$

$$\frac{\mathcal{P}_a}{\mathcal{P}_{\mathcal{R}}} \sim \left(\frac{H_I}{2\pi f_a(t_I)} \right)^2 \ll \left(\frac{H_I}{2\pi f_a(t_0)} \right)^2$$

SUMMARY

- SUSY axion models solves 2 fine-tuning problems in SM.
- DFSZ realization provides μ -term solution and effective interactions of axion sector.
- For small $f_a < 10^{11}$ GeV, axion is dominant DM, while for $f_a > 10^{11}$ GeV, DM is a mixture of axion & neutralino.
- BICEP2 constrains DFSZ axion models but can be avoided in the extension of PQ sector.