

Status of Z' Analysis in $e^- e^+$ channel

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WP1 group (FP7 project)

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(1) Angular distributions:

People involved

Sh. Elgammal (BUE),
P. Miné (LLR)
B. Clerbaux (ULB),
L. Thomas (ULB).

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(2) Recovery of Saturated ECAL crystals using MVA Method:

People involved

Sh. Elgammal (BUE),
P. Miné (LLR)
B. Clerbaux (ULB).

AN on going

(3) ECAL Spike in 14 TeV C.M.E:

People involved

M. Eshra (BUE),
Sh. Elgammal (BUE),
P. Miné (LLR)
A. Zabi (LLR).

BSM Models



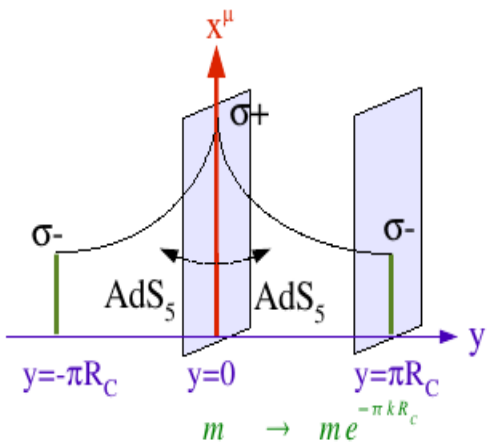
RS model of extra – dimensions



[Phys.Rev.Lett. 83 (1999) 3370 - hep-ph/9905221]

1 ED compactified, constant and negative curvature space (AdS₅):

bounded by 2 branes: Planck brane (y=0) and TeV or SM brane (y=±πR_C)



metric: (non factorizable)

$$ds^2 = e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2$$

$$R_5 = -20 k^2$$

Gauss law: relates M_D to M_{pl}:

$$\bar{M}_{pl}^2 = \frac{M_D^3}{k} (1 - e^{-2\pi k R_C})$$

No hierarchy: k ~ M_D ~ M_{pl}

consistency SM:

$$k < M_D \quad (k \leq 0.1 M_D)$$

$$k < 0.1 M_{pl}$$

$$\Lambda_\pi = \bar{M}_{pl} e^{-k\pi R_C}$$

The scale of phys. phen. as realized

by 4D flat metric ⊥ to 5th dim:

$$\sim 10^{18} \text{ GeV} \rightarrow 1 \text{ TeV need } kR_C \sim 11$$

$$\rightarrow R_C \sim 10^{-32} \text{ m (very small)}$$

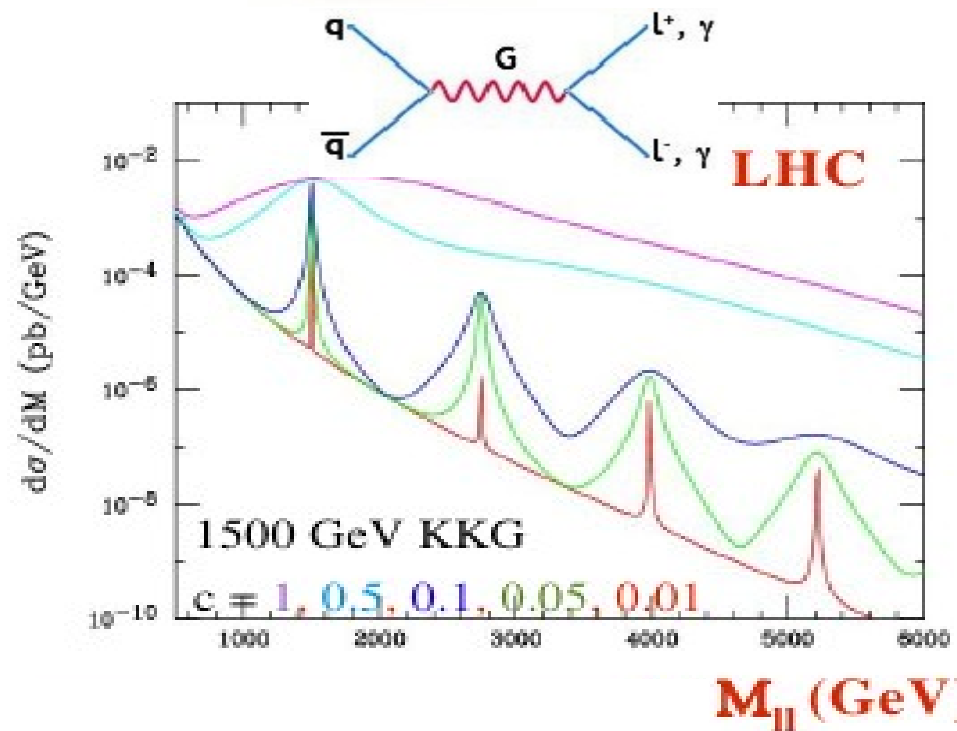
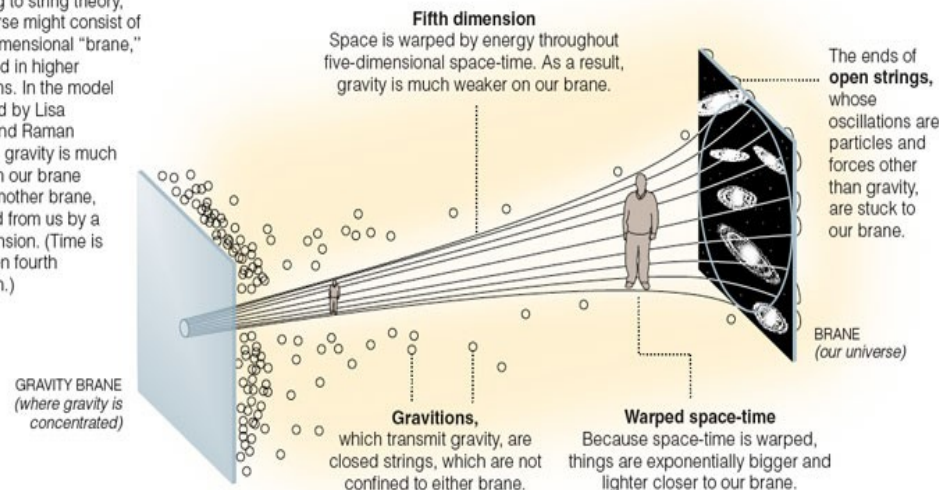
2 free parameters: m₁ or Λ_π and k/M_{pl} = c

$$\text{width: } \sim (k/M_{pl})^2$$

$$\sim m_n^3$$

Island Universes in Warped Space-Time

According to string theory, our universe might consist of a three-dimensional "brane," embedded in higher dimensions. In the model developed by Lisa Randall and Raman Sundrum, gravity is much weaker on our brane than on another brane, separated from us by a fifth dimension. (Time is the unseen fourth dimension.)



E_6 is GUT group of rank 6:

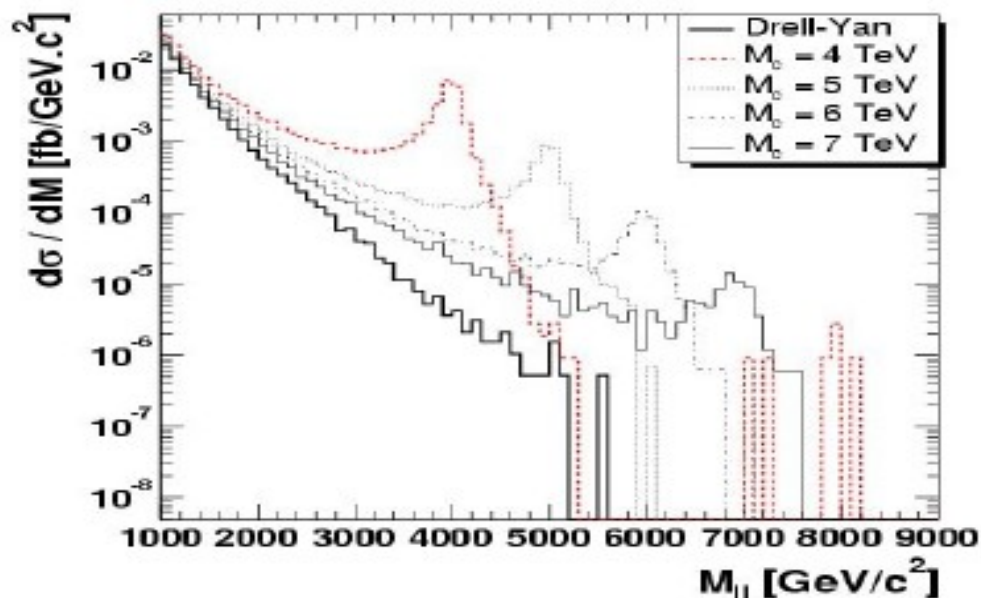
$$\begin{aligned}
 E_6 &\rightarrow SO(10) \times U(1)_\psi \rightarrow SU(5) \times U(1)_\chi \times U(1)_\psi \\
 &\rightarrow SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)', \quad (2.2)
 \end{aligned}$$

where $U(1)'$ is a linear combination of $U(1)_\chi$ and $U(1)_\psi$, thus

$$U(1)' = U(1)_\chi \cos(\theta) + U(1)_\psi \sin(\theta), \quad (2.3)$$

where θ , for E_6 , is a free parameter [17]; if $\theta = 0$, one extra gauge boson Z'_χ exists from $SO(10)$, while for $\theta = \pi/2$ only Z'_ψ from E_6 is obtained. Finally, $U(1)_\eta$ is a particular combination of $U(1)_\chi$ and $U(1)_\psi$, i.e., $\theta = 2\pi - \tan^{-1} \sqrt{5/3}$, which produces Z'_η [17]. The additional neutral Z boson is more massive than the SM

[Rizzo, PRD61(2000) 055005]



ADD: Arkadi-Hamed, Dimopoulos and Dvali

[Phys.Lett. B429 (1998) 263 - hep-ph/9803315]

Gauss law: relates M_D to M_{Pl} :

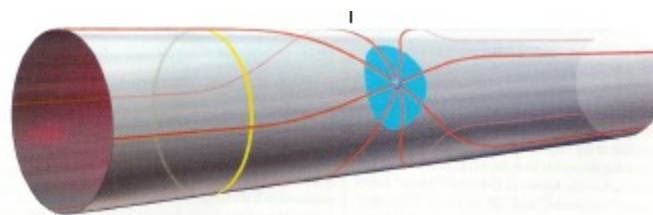
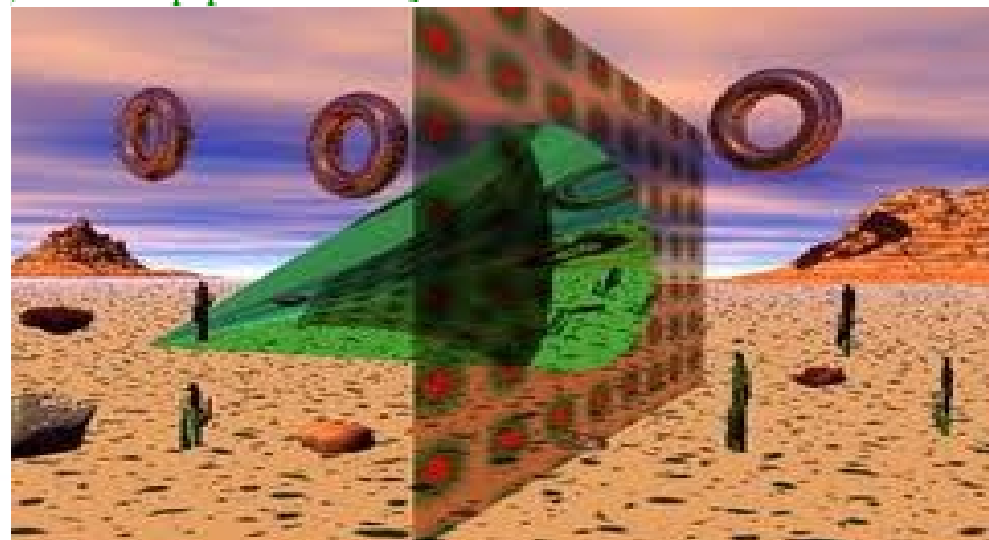
$$r \ll R_c \rightarrow V_{4+\delta}(r) = -\frac{1}{M_D^{2+\delta}} \frac{m}{r^{\delta+1}}$$

$$r \gg R_c \rightarrow V_4(r) = -\frac{1}{M_D^{2+\delta} (2\pi R)^\delta} \frac{m}{r}$$

$$M_{Pl}^2 = V_\delta M_D^{2+\delta}$$

$$V = (2\pi R_c)^\delta$$

Dimension



Coupling $\sim 1/M_{Pl}$ - but $N = (ER_c)^\delta$

for $\delta=2$ and $E=1$ TeV $\rightarrow 10^{30}$ KK gravitons

if $M_D = 1$ TeV : $R \sim 10^{(30/d-17)}$ cm

Experim. searches: - high energy collider

[- astrophysics]

- short range gravity experiments

The differential cross section corresponding to the combination of a single term in Eq. **1** with DY production can be written as

$$\frac{d\sigma^{\text{CI/DY}}}{dM_{\mu\mu}} = \frac{d\sigma^{\text{DY}}}{dM_{\mu\mu}} - \eta_{ij} \frac{\mathcal{I}}{\Lambda^2} + \eta_{ij}^2 \frac{\mathcal{C}}{\Lambda^4}, \quad (2)$$

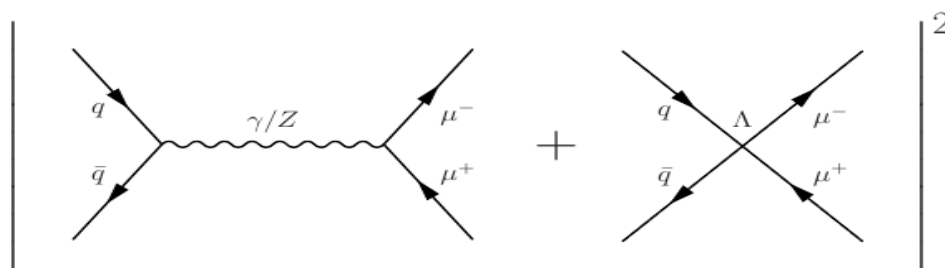
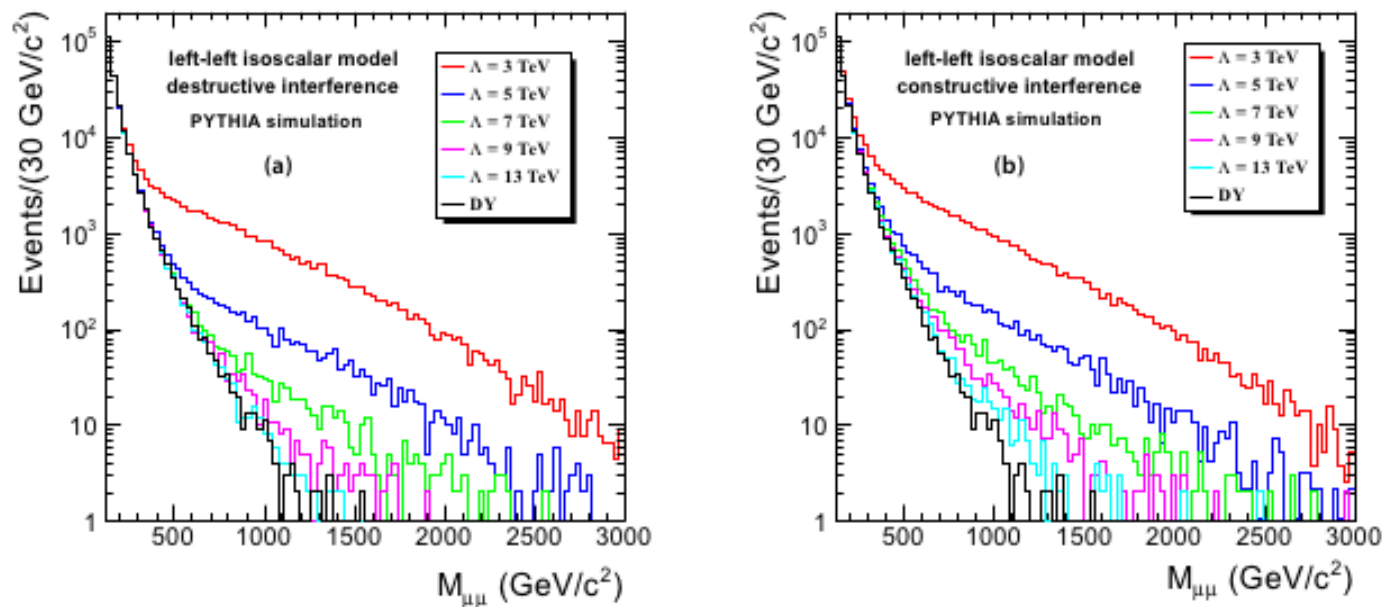


Figure 1: Schematic representation of the addition of DY (left) and CI (right) amplitudes, for common helicity states, contributing to the total cross section for $pp \rightarrow X + \mu^+ \mu^-$.



The Summer12 (reconstructed with CMSSW software, version 5.3.x) Monte Carlo simulated samples are used:

(1) for background samples;

/DYToEE-M-20-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-120-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-200-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-400-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-500-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-700-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-800-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToEE-M-1000-TuneZ2star-8TeV-pythia6/Summer12-PU-S7-START52-V9-v1/AODSIM,
 /DYToEE-M-2000-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /TT-CT10-TuneZ2star-8TeV-powheg-tauola/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /WW-TuneZ2star-8TeV-pythia6-tauola/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /WZ-TuneZ2star-8TeV-pythia6-tauola/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /ZZ-TuneZ2star-8TeV-pythia6-tauola/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /DYToTauTau-M-20-CT10-TuneZ2star-8TeV-powheg-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
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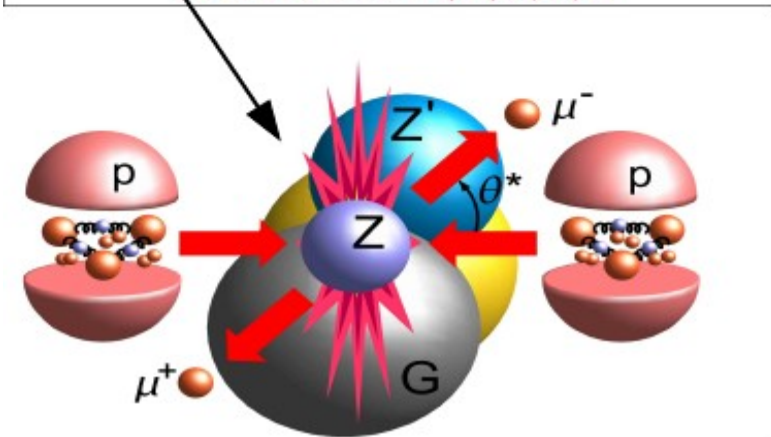
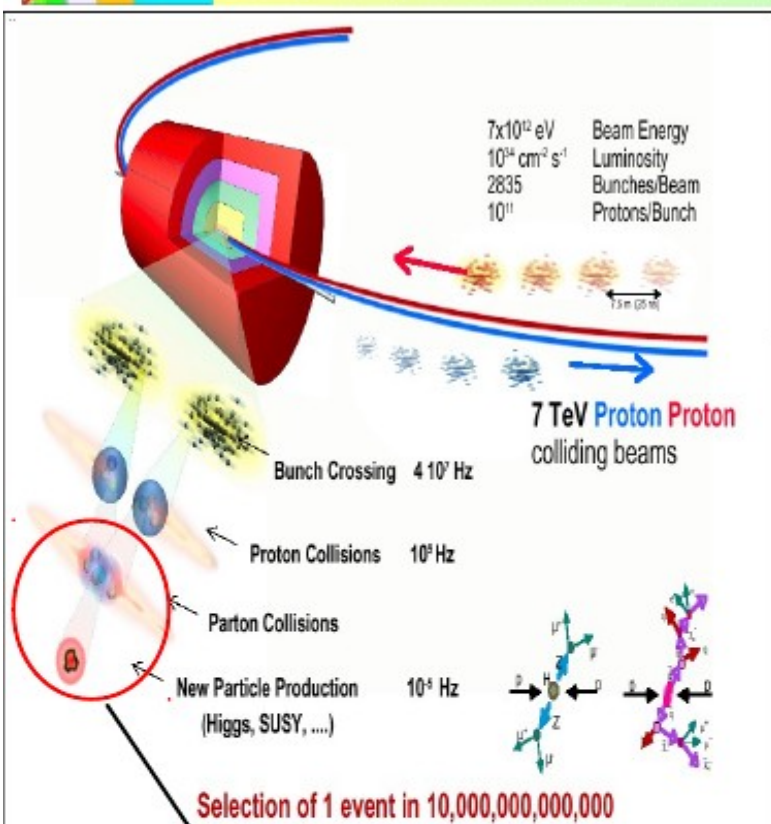
(2) for signales samples;

/RSGravEE-kMpl001-M-2000-TuneZ2star-8TeV-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /ZprimePSIToEE-M-2000-TuneZ2star-8TeV-pythia6/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
 /ADDdiLepton-LambdaT-2000-Tune4C-8TeV-pythia8/Summer12-DR53X-PU-S10-START53-V7A-v1/AODSIM,
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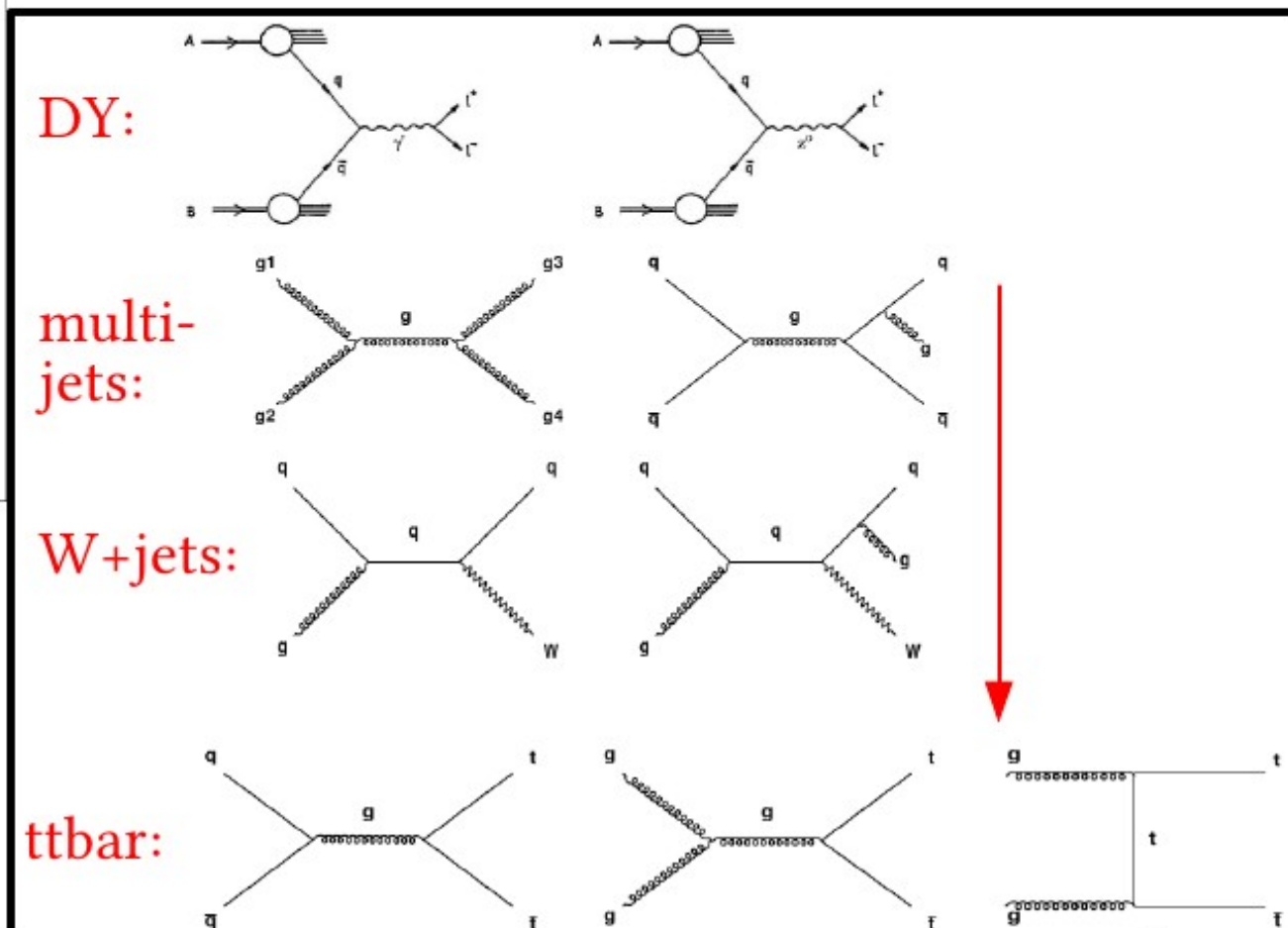
| Dataset | run range | json file |
|--|---------------|---|
| Run2012A-13Jul2012 | 190456-193621 | Cert_190456-196531_8TeV_13Jul2012ReReco_Collisions12_JSON_v2.txt |
| Run2012A-recover-06Aug2012 | 190782-190949 | Cert_190782-190949_8TeV_06Aug2012ReReco_Collisions12_JSON.txt |
| Run2012B-13Jul2012 | 193833-196531 | Cert_190456-196531_8TeV_13Jul2012ReReco_Collisions12_JSON_v2.txt |
| Run2012C-ReReco | 198022-198913 | Cert_198022-198523_8TeV_24Aug2012ReReco_Collisions12_JSON.txt |
| Run2012C-PromptReco-v2 | 198934-203746 | Cert_190456-203002_8TeV_PromptReco_Collisions12_JSON_v2.txt |
| Run2012C-EcalRecover ₁ 1Dec2012 | 201191-201191 | Cert_201191-201191_8TeV_11Dec2012ReReco-recover_Collisions12_JSON.txt |
| Run2012D-PromptReco-v1 | 203768-208686 | Cert_190456-206098_8TeV_PromptReco_Collisions12_JSON.txt |

| | variable | barrel | endcap |
|-------------------|-----------------------|--|--|
| | E_T | $> 35 \text{ GeV}$ | $> 35 \text{ GeV}$ |
| | $ \eta_{SC} $ seed | < 1.442 ECAL seeded | $1.56 < \eta < 2.5$ ECAL seeded |
| Kinematics cuts | missing hits | ≤ 1 | ≤ 1 |
| | $ d_{xy} $ | < 0.02 | < 0.05 |
| | $\Delta\eta_{in}$ | < 0.005 | < 0.007 |
| | $\Delta\phi_{in}$ | < 0.06 | < 0.06 |
| | H/E | < 0.05 | < 0.05 |
| Shower shape cuts | E^{2x5} / E^{5x5} | > 0.94 OR $E^{1x5} / E^{5x5} > 0.83$ | - |
| | $\sigma_{in\eta}$ | - | < 0.03 |
| Isolation cuts | isol Em + Had Depth 1 | $< 2 + 0.03 \times E_T + \rho \times 0.28 \text{ GeV}$ | $< 2.5 \text{ GeV} + \rho \times 0.28$ for $E_T < 50 \text{ GeV}$ $< 2.5 + 0.03 \times (E_T - 50) + \rho \times 0.28 \text{ GeV}$ |
| | isol Pt Tracks | $< 5 \text{ GeV}/c$ | $< 5 \text{ GeV}/c$ |

- * **HEEP** events are selected with 2 opposite sign electrons
- * Events with 2 electrons reco in EE are excluded



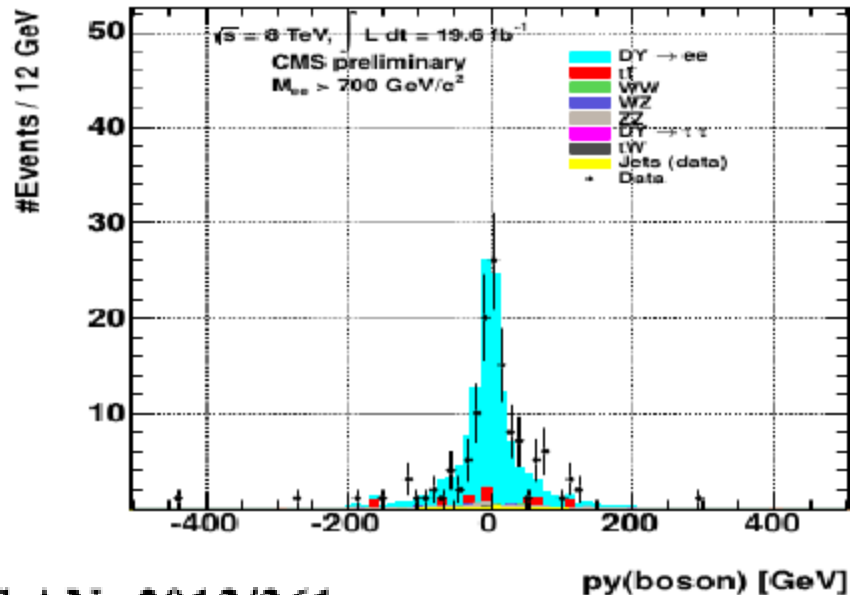
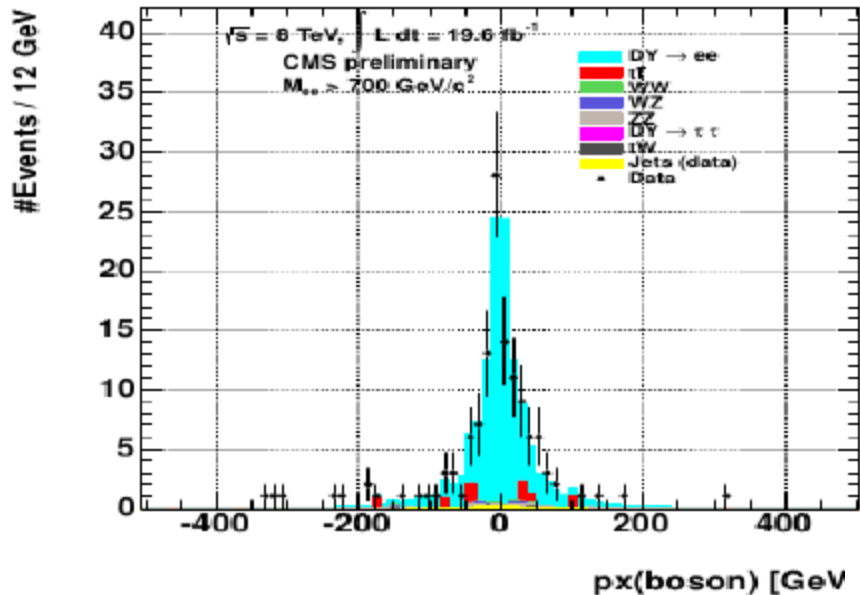
Backgrounds



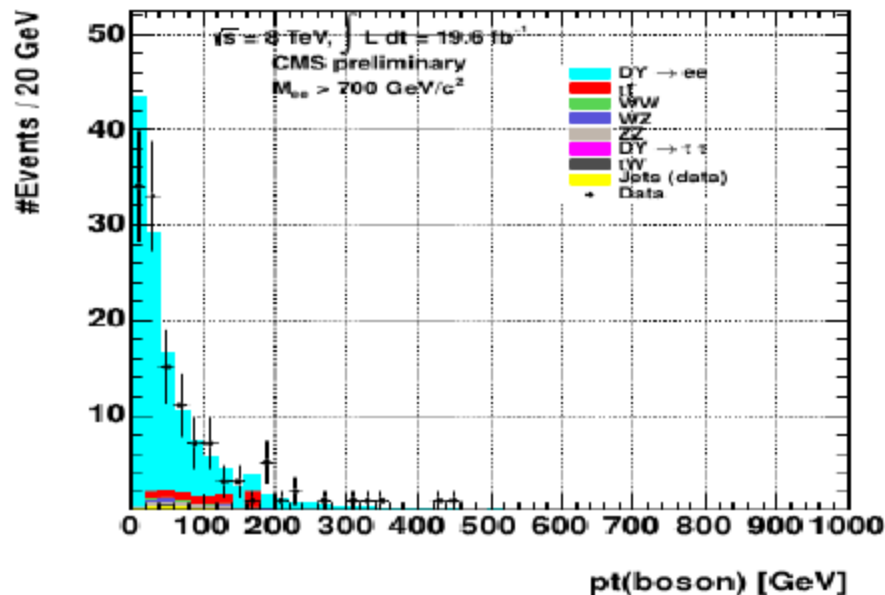
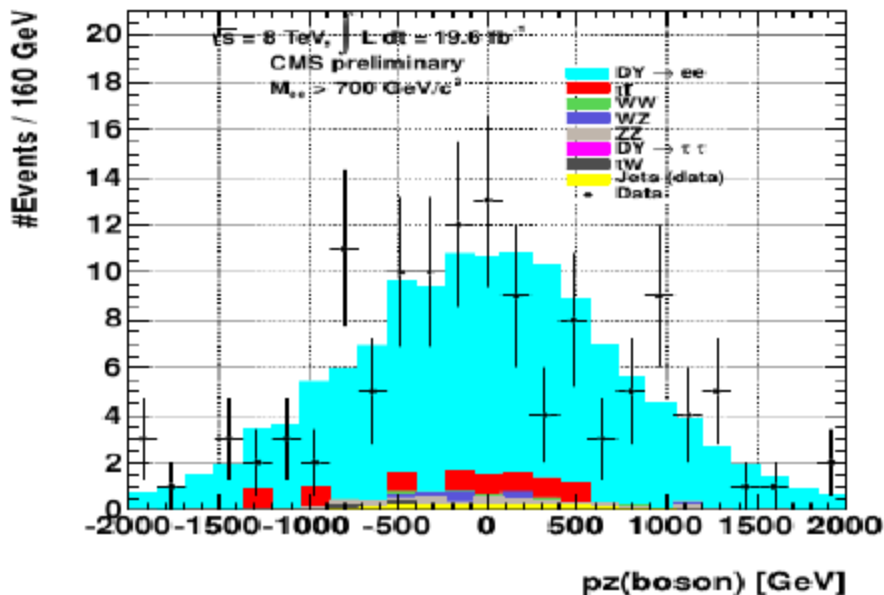
Bosons Kinematics at Lab Frame



Boson kinematics at high mass



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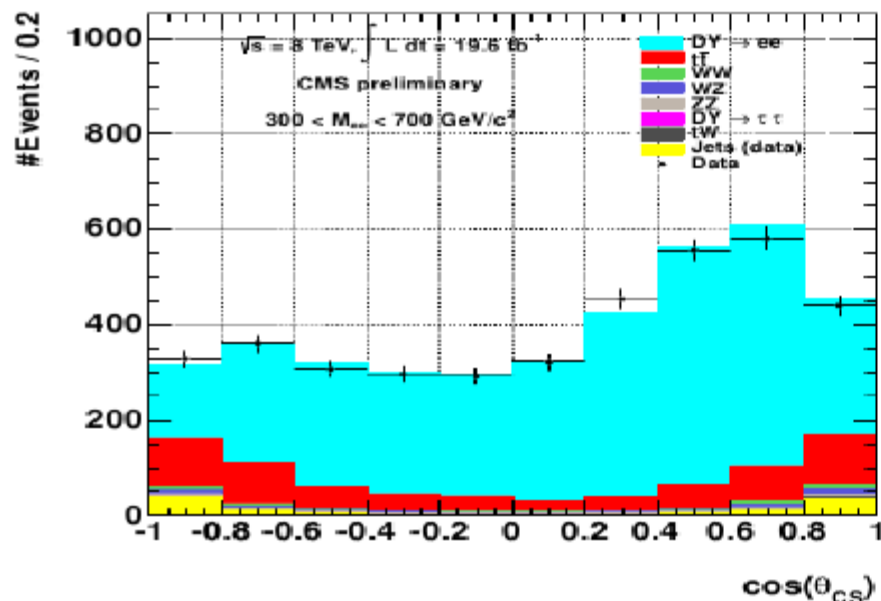
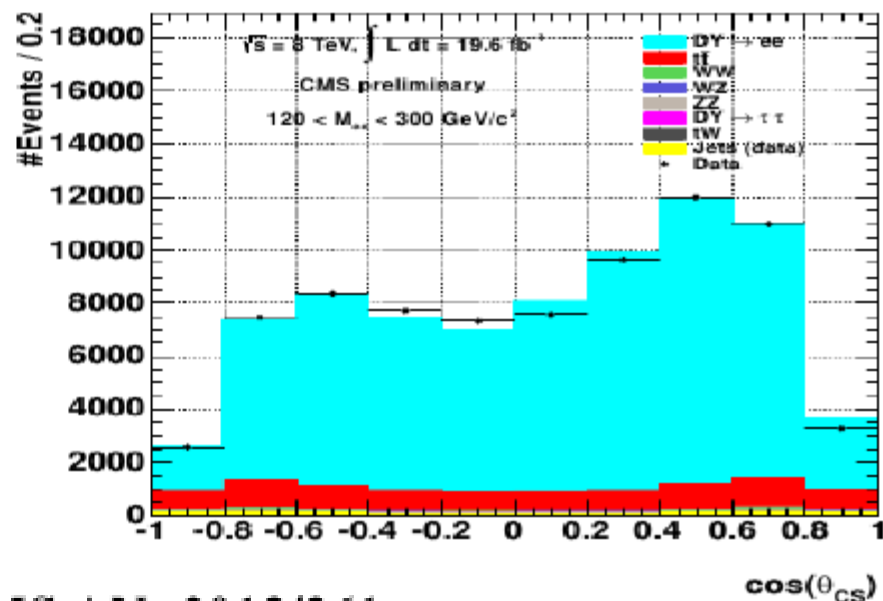
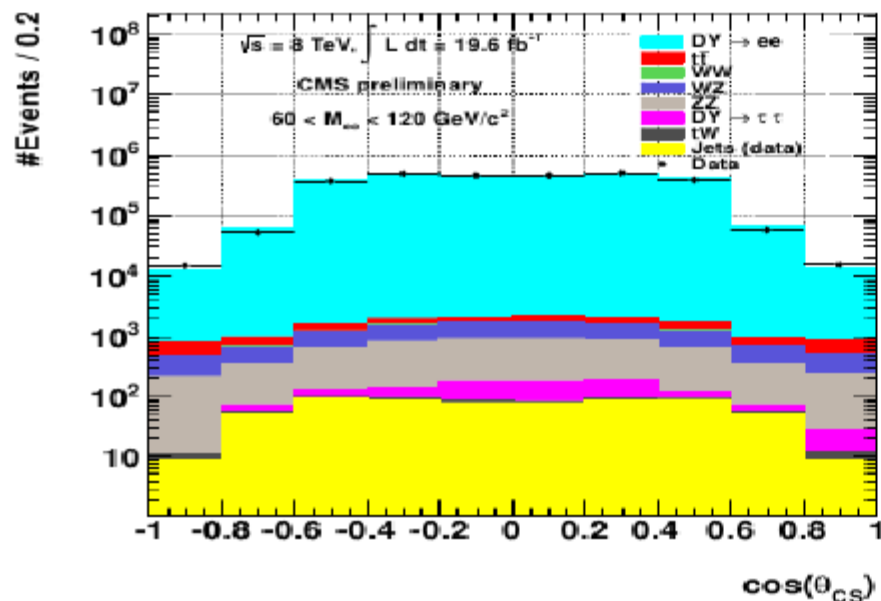
<http://arxiv.org/pdf/1207.3973v1.pdf>

Figure 5: Collins Soper frame is characterized by 2 properties; the y axis is perpendicular to the plane spanned by the two hadron momenta P_1 and P_2 , the z -axis bisects the proton and minus the other proton directions in the boson rest frame.

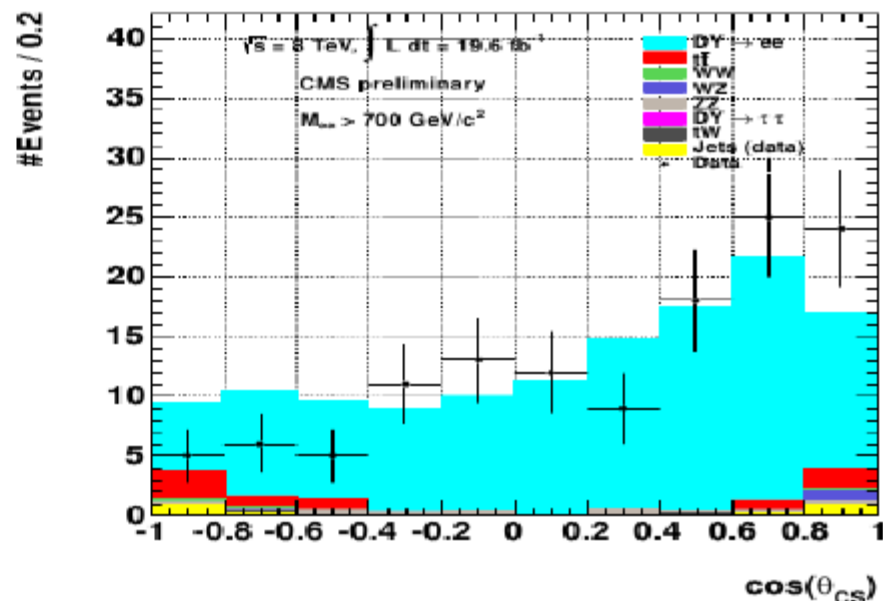
$$\cos \theta_{CS}^* = \frac{Q_z}{|Q_z|} \frac{2(P_1^+ P_2^- - P_1^- P_2^+)}{|Q| \sqrt{Q^2 + Q_T^2}}, \quad (3)$$

where Q is the four-momentum of the dilepton and Q_T and Q_z are the transverse and longitudinal components of the dilepton momentum with respect to the beam axis; P_1 (P_2) represents the four-momentum of the lepton (antilepton); and $P_i^\pm = (P_i^0 \pm P_i^3)/\sqrt{2}$. The quark direction is not determined a priori at the Large Hadron Collider (LHC) [13] because both beams consist of protons. However, because the antiquark is necessarily a sea quark, on average we expect it to carry less momentum than the valence quark, and therefore the dilepton system is usually boosted in the direction of the valence quark [5, 14, 15]. This assumption is taken into account by including the sign of the longitudinal boost in the definition of $\cos \theta_{CS}^*$.

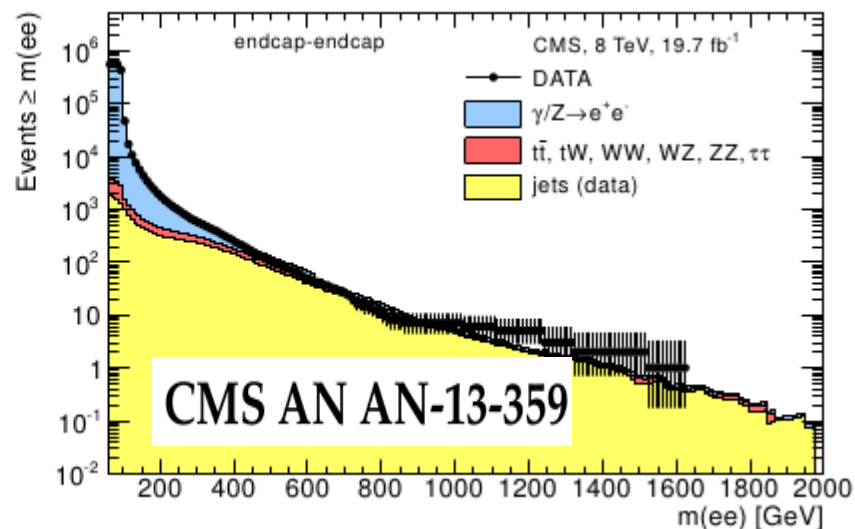
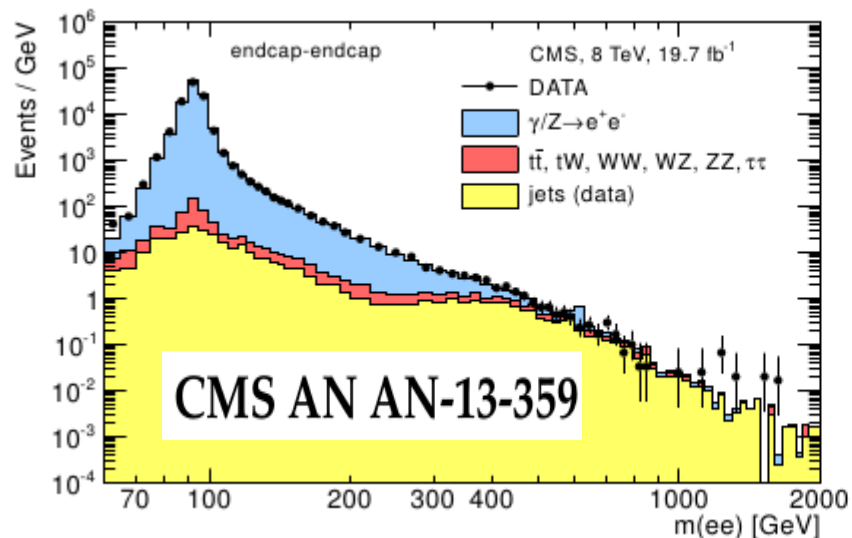
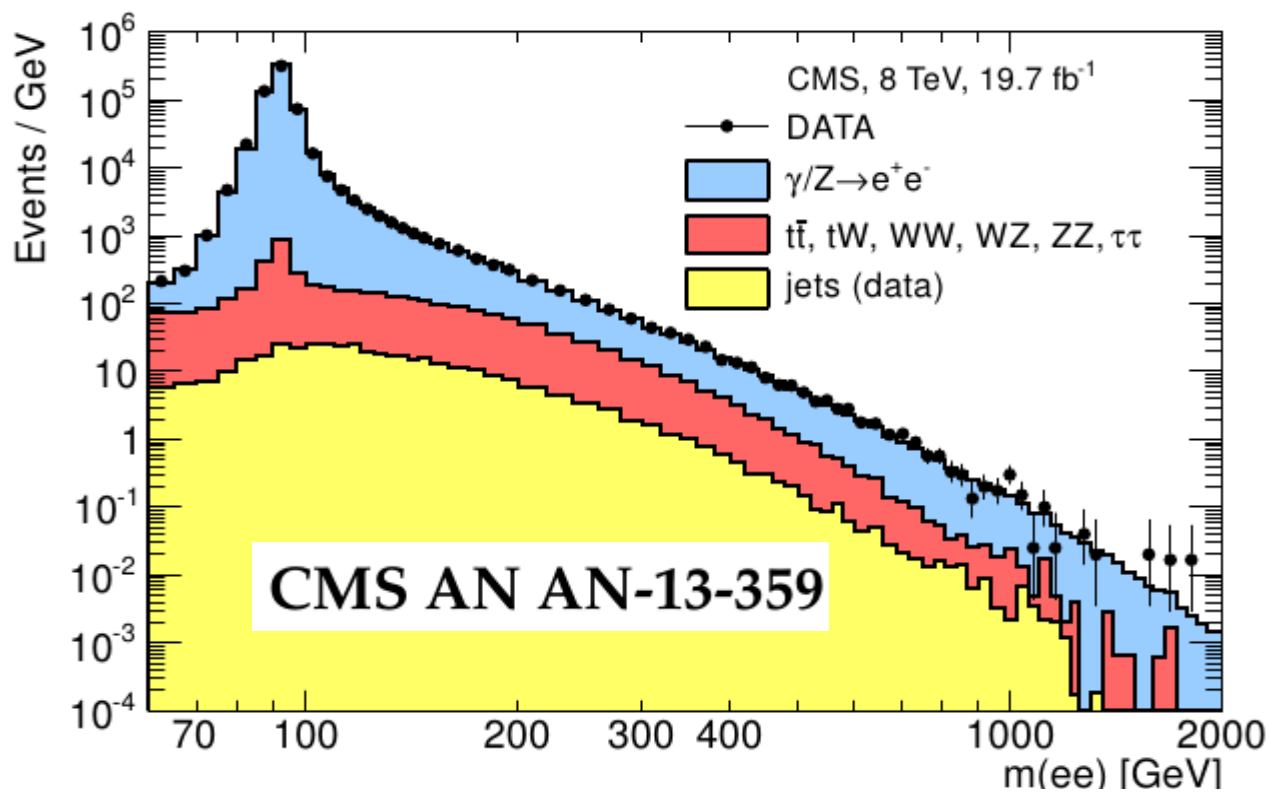
Angular distributions for DY dist



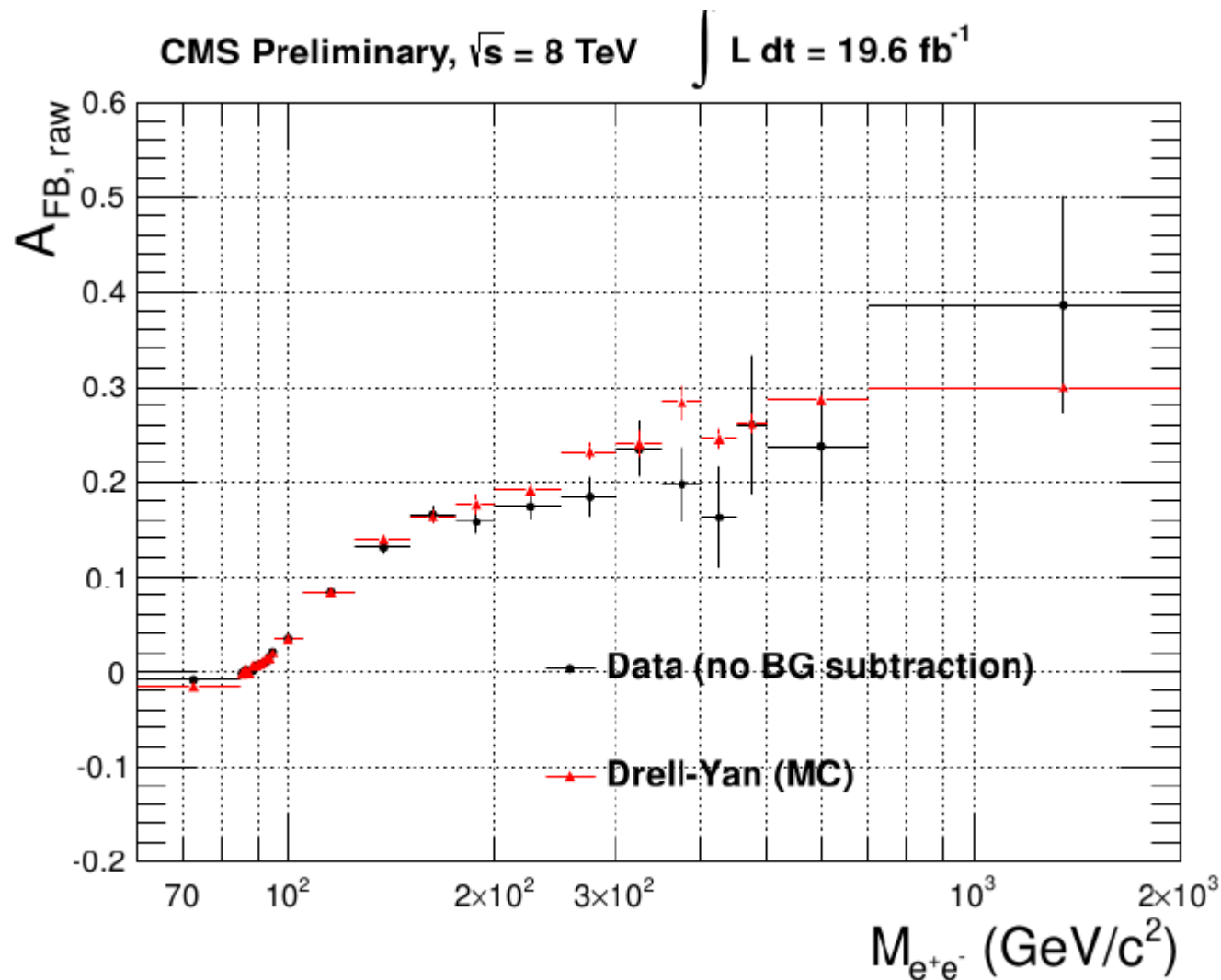
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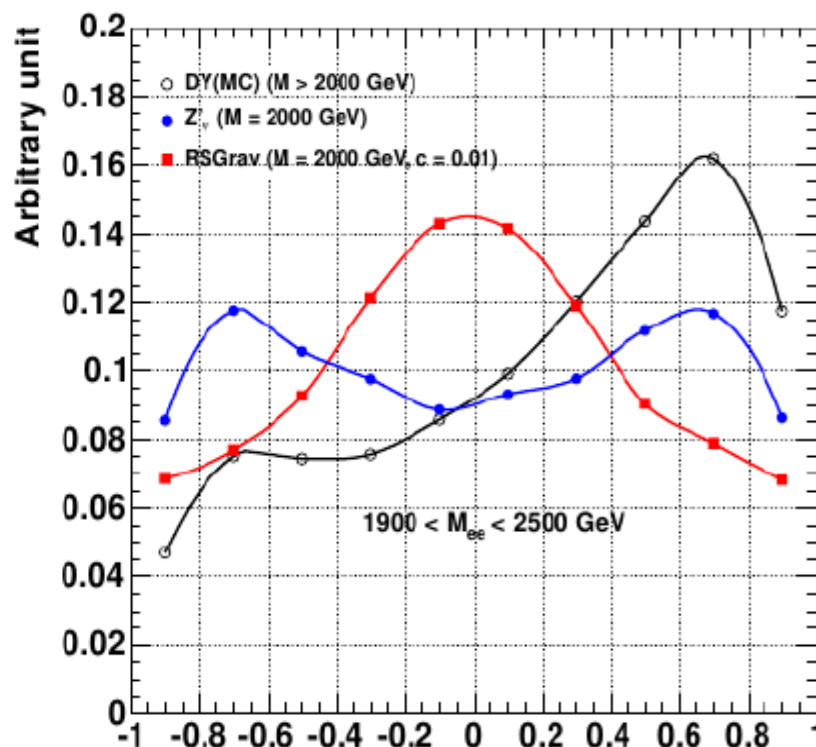
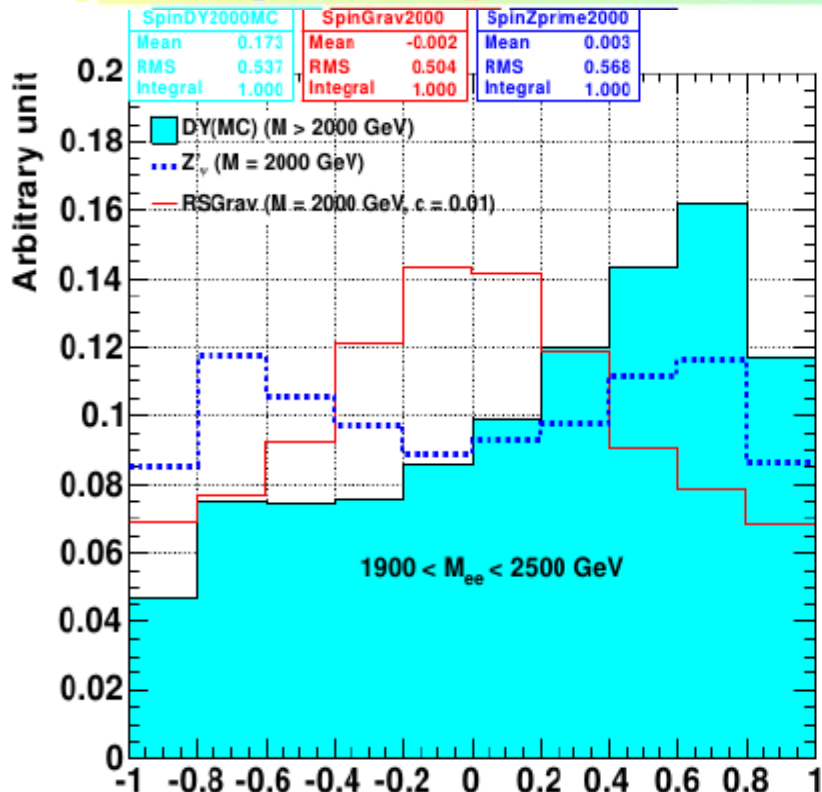
Invariant Mass Plots in Di-Electron Channel



Forward Backward asymmetry



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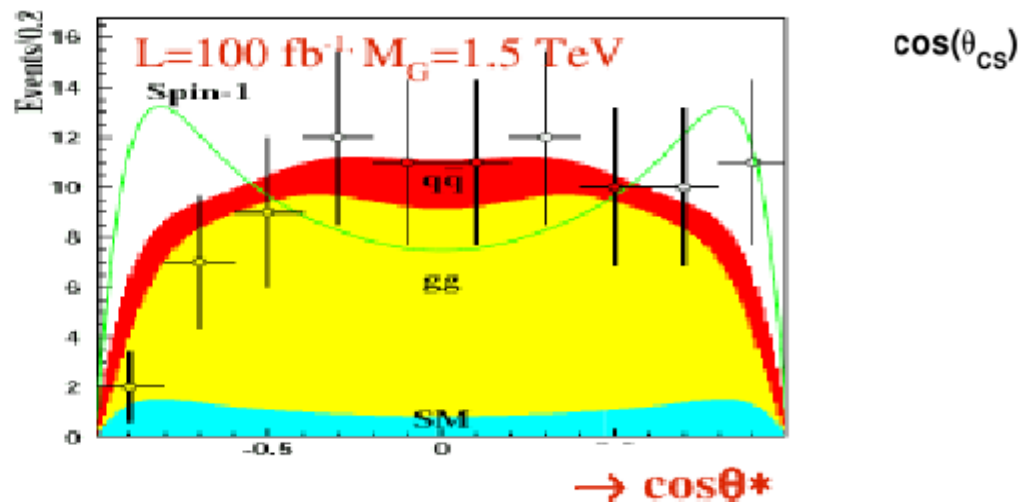


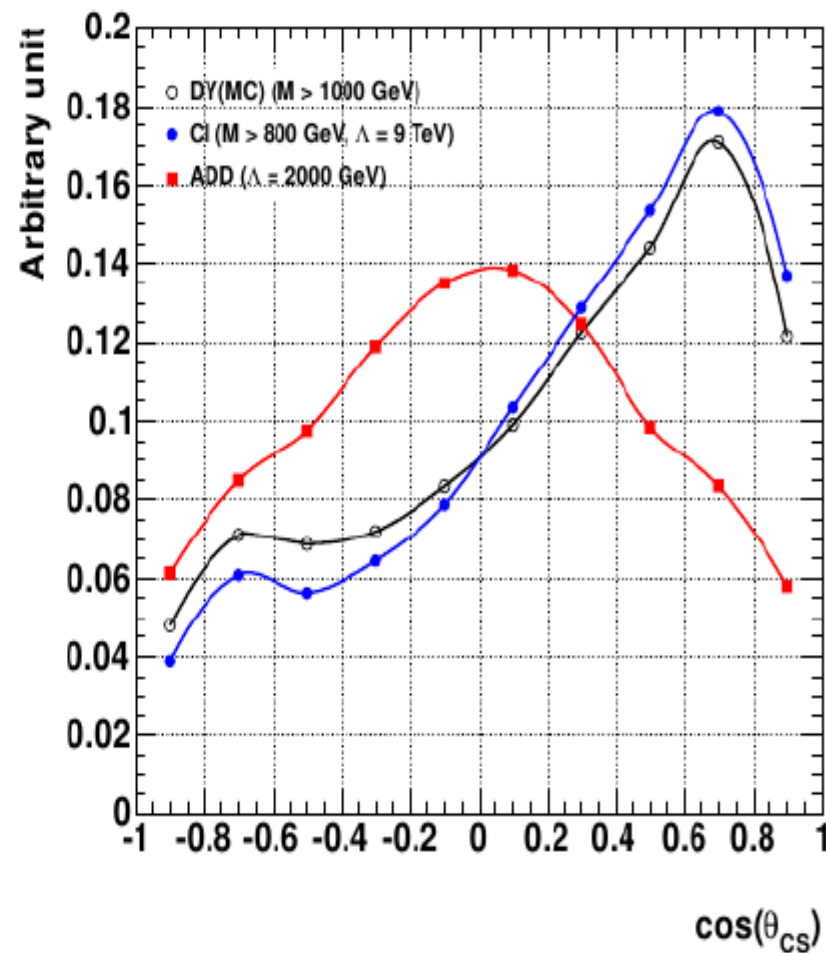
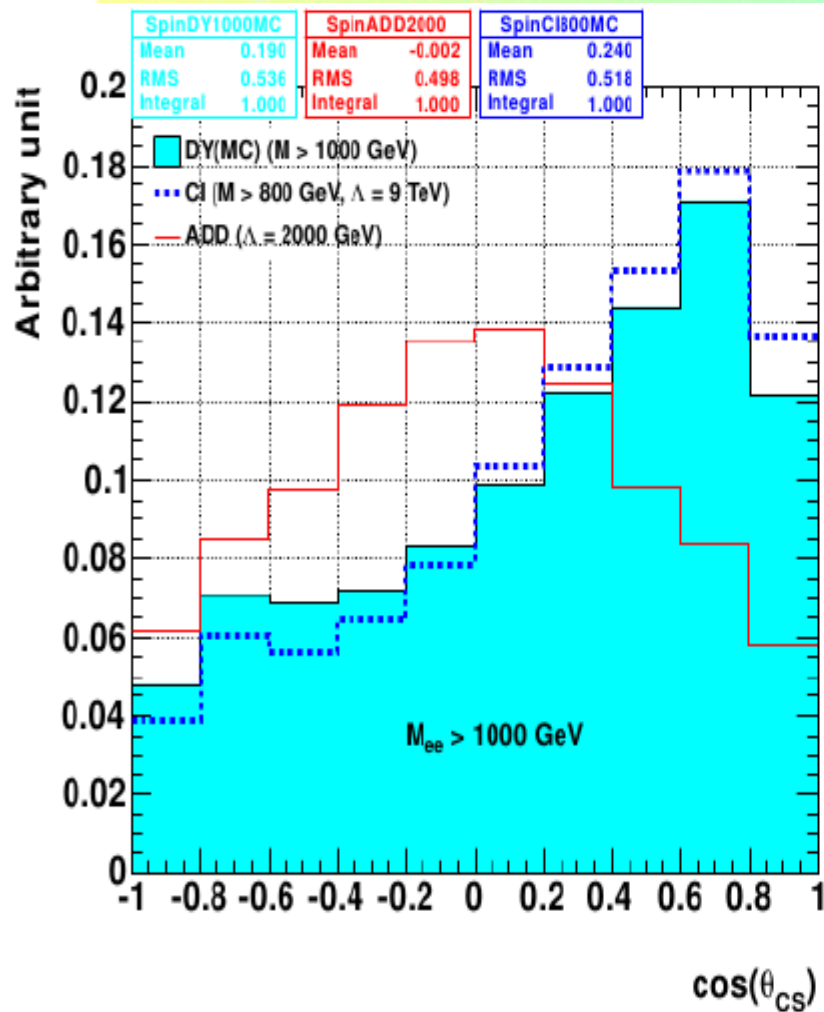
$DY \ M_{ee} > 2 \text{ TeV}/c^2$

$Z' \ M_{ee} = 2 \text{ TeV}/c^2$

$RS \ G \ M_{ee} = 2 \text{ TeV}/c^2$

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DY $M_{ee} > 1 \text{ TeV}/c^2$

CI $M_{ee} > 0.8 \text{ TeV}/c^2$

RS $G = 2 \text{ TeV}/c^2$

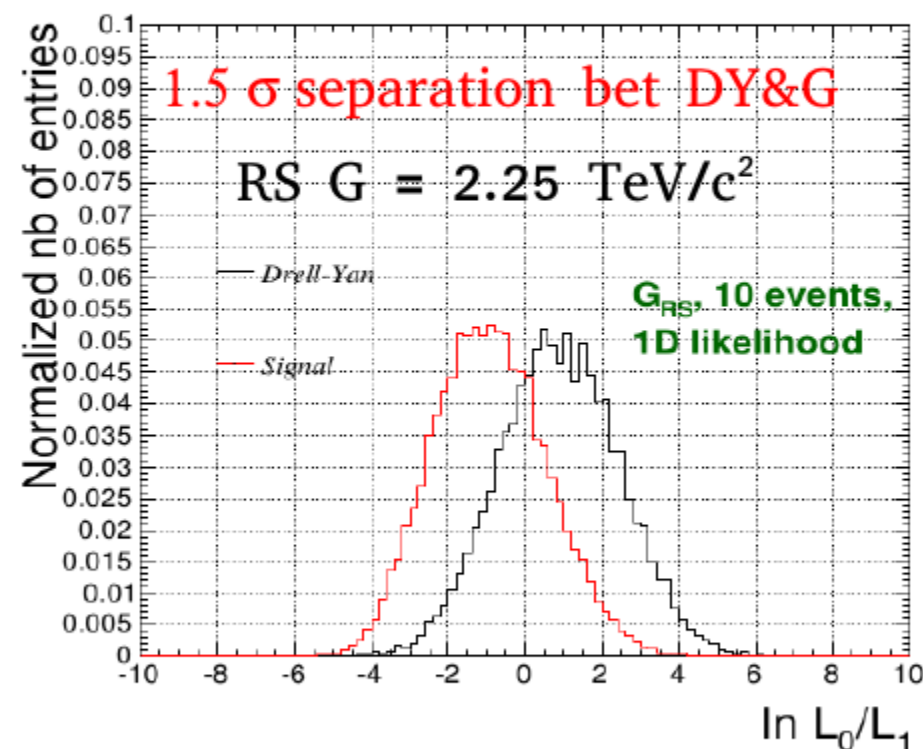
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the log likelihood ratio, Q , as:

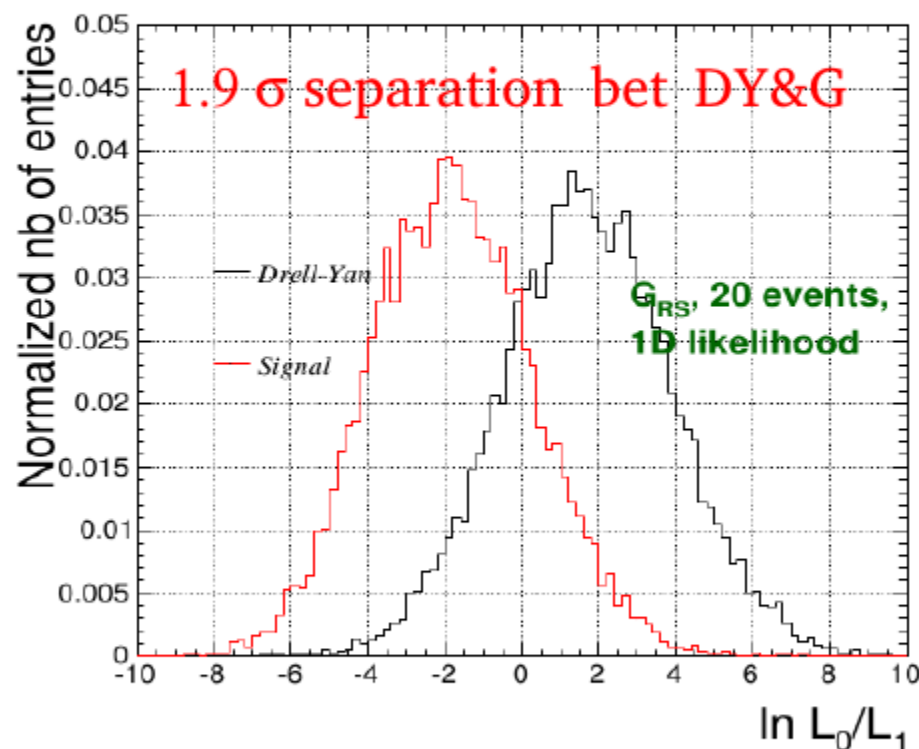
$$Q = \ln \frac{\mathcal{L}_0}{\mathcal{L}_1} = \ln \frac{\prod_{i=1}^n p_0(\vec{x}_i)}{\prod_{i=1}^n p_1(\vec{x}_i)}$$

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CMS Simulation, $\sqrt{s} = 8$ TeV



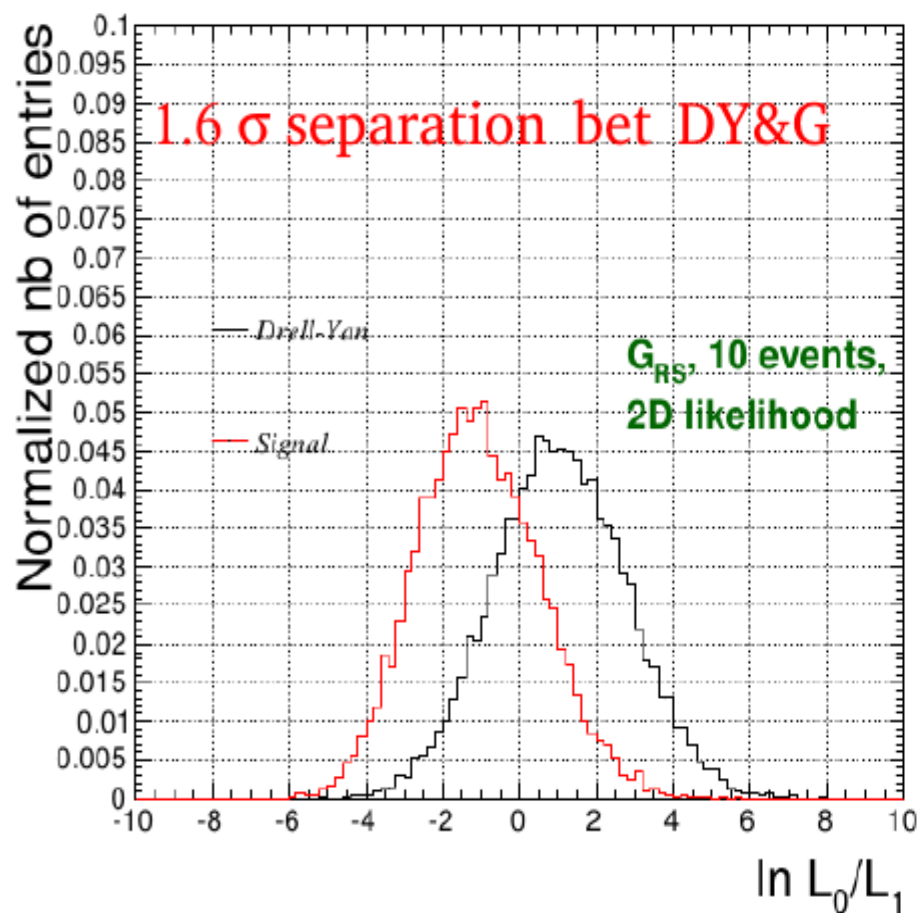
CMS Simulation, $\sqrt{s} = 8$ TeV



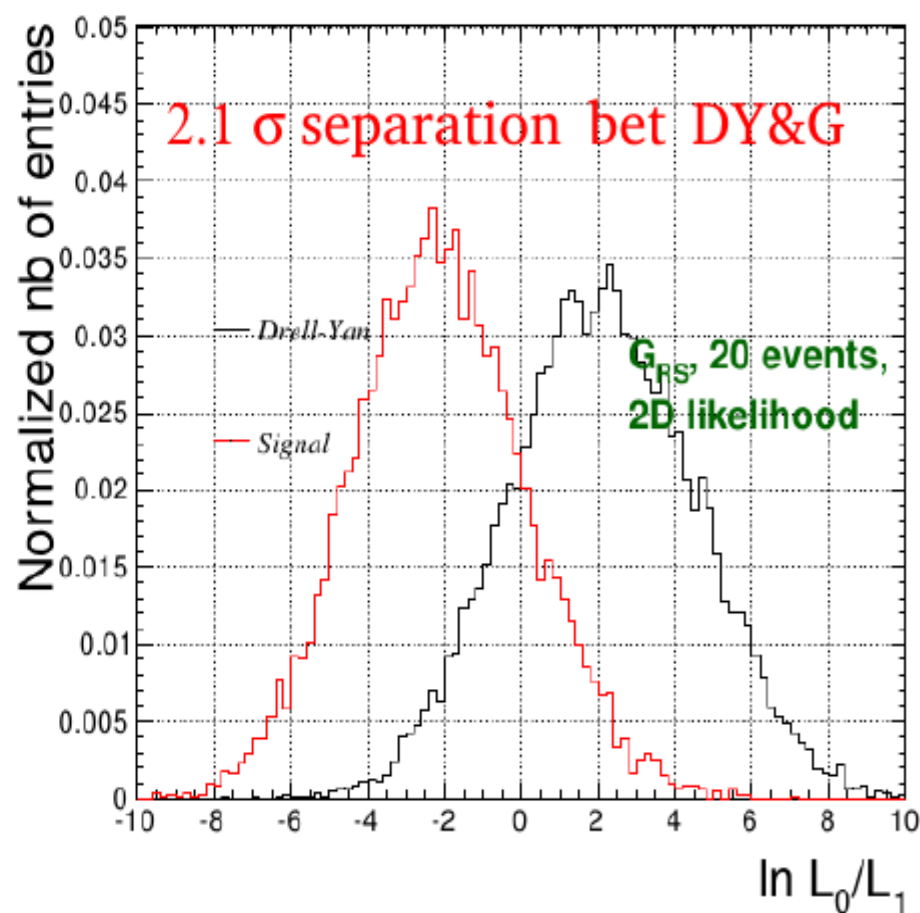
In this analysis, the pdf $p_0(\vec{x})$ and $p_1(\vec{x})$ are binned and obtained from the Monte Carlo simulations. In order to avoid a possible bias due to the limited statistics, separate events are used to generate the pdf used for the pseudo-experiments generation and those used in the likelihood calculation.

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CMS Simulation, $\sqrt{s} = 8$ TeV



CMS Simulation, $\sqrt{s} = 8$ TeV

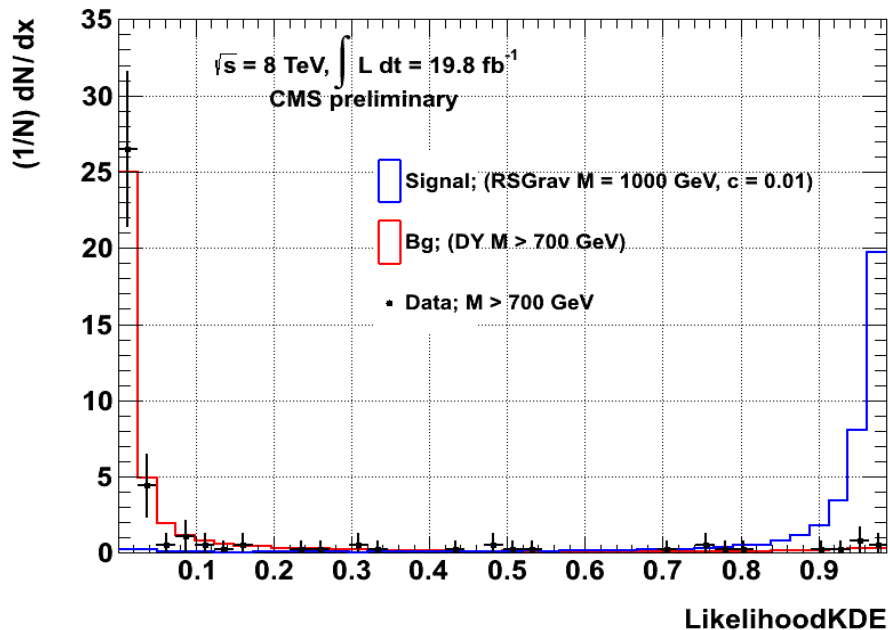
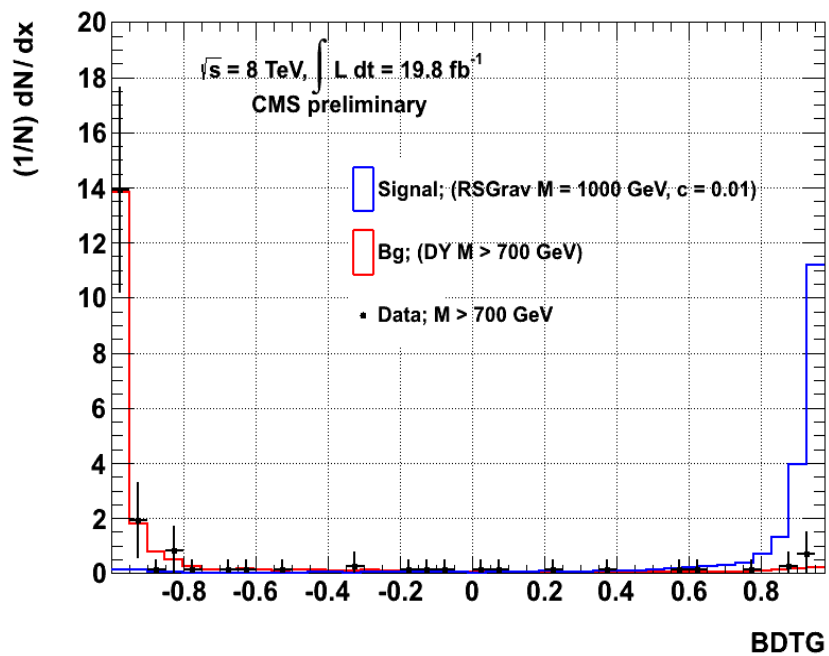
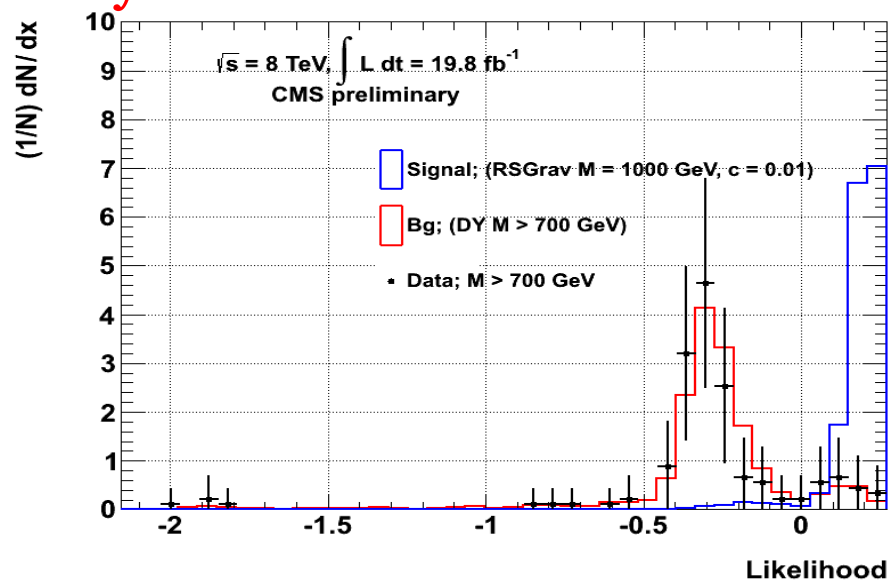
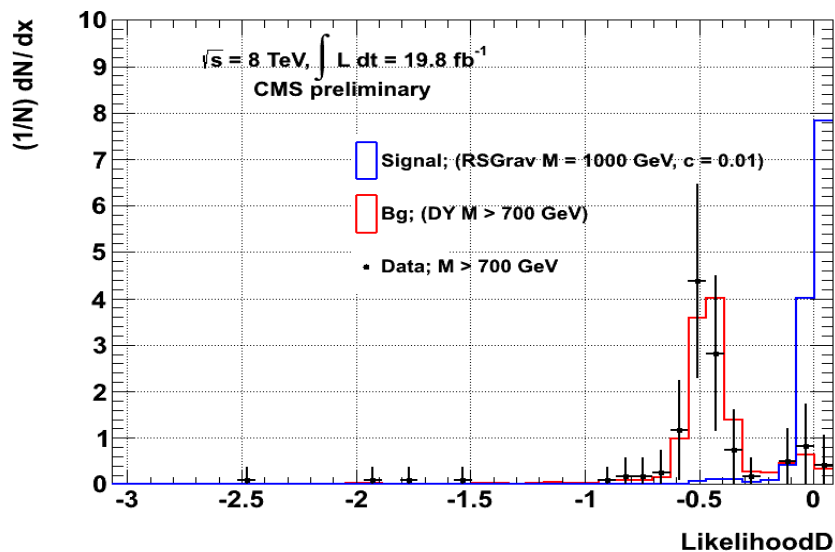


New Study

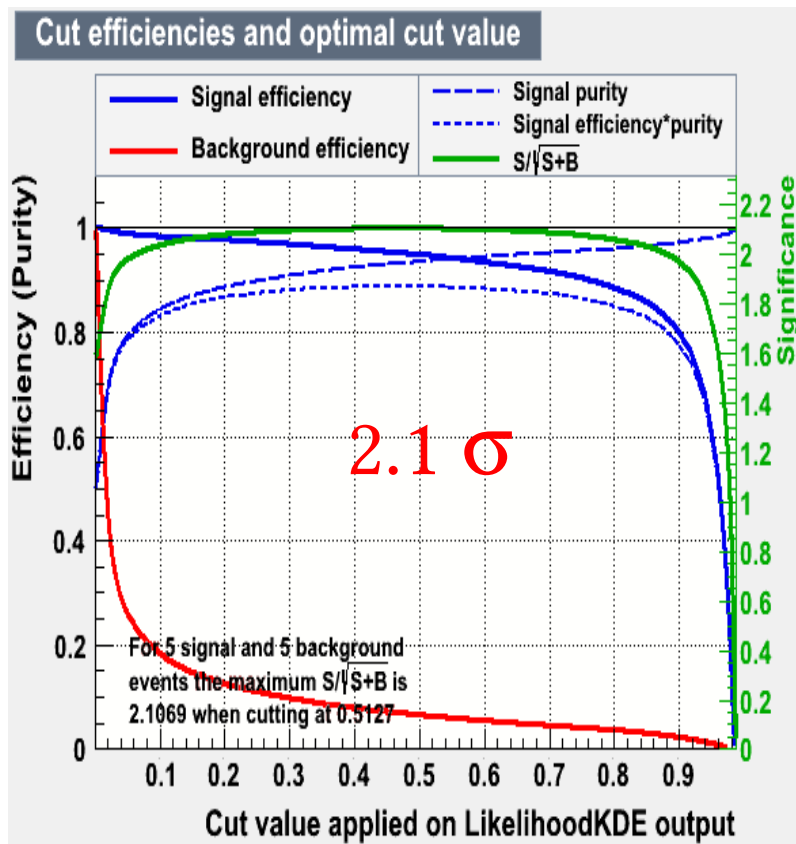
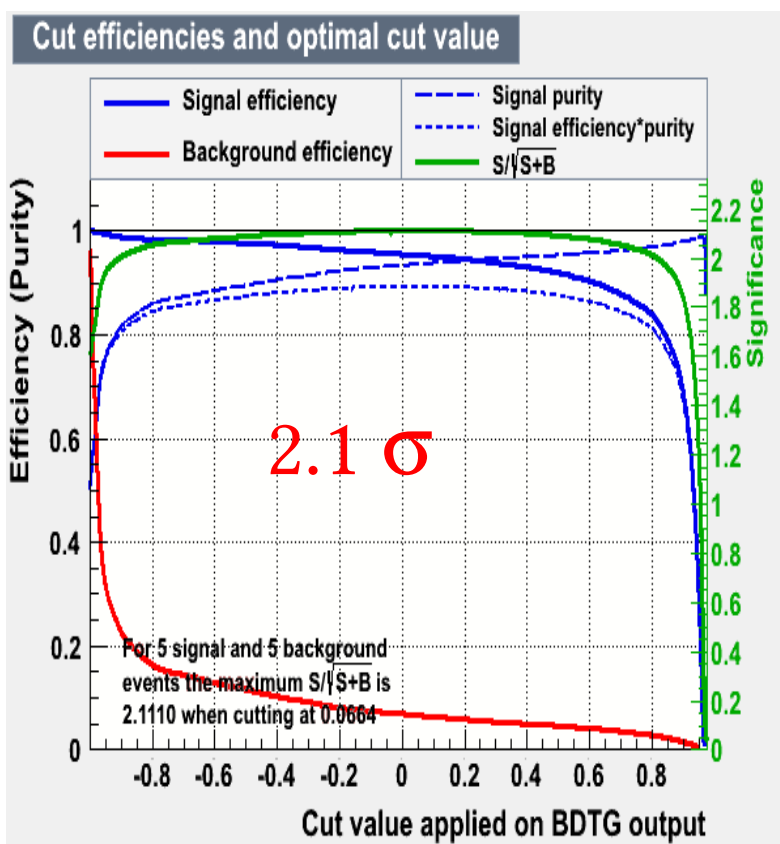
*Suppose we have
access at 1 TeV*

- (1) the chosen set variables are only loosely correlated to each other.
- (2) then we can develop a likelihood discriminant using chosen set of variables $\{x_i\}$:
- (3) Likelihood shows good separation between signal and background
- (4) can be applied to the selected events from data

New Study



| Classifier | #signal | Optimal-cut | S/sqrt(S+B) | NSig | NBkg | EffSig | EffBkg |
|-----------------------|----------|---------------|----------------|-----------------|------------------|---------------|----------------|
| Likelihood: | 5 | 0.0423 | 2.09854 | 4.789803 | 0.4197713 | 0.958 | 0.08395 |
| LikelihoodD: | 5 | -0.1101 | 2.08826 | 4.784287 | 0.4645813 | 0.9569 | 0.09292 |
| LikelihoodPCA: | 5 | 0.7228 | 2.07049 | 4.79348 | 0.5663908 | 0.9587 | 0.1133 |
| LikelihoodKDE: | 5 | 0.5127 | 2.10694 | 4.742616 | 0.3241424 | 0.9485 | 0.06483 |
| BDTG: | 5 | 0.0664 | 2.11101 | 4.762839 | 0.3275761 | 0.9526 | 0.06552 |

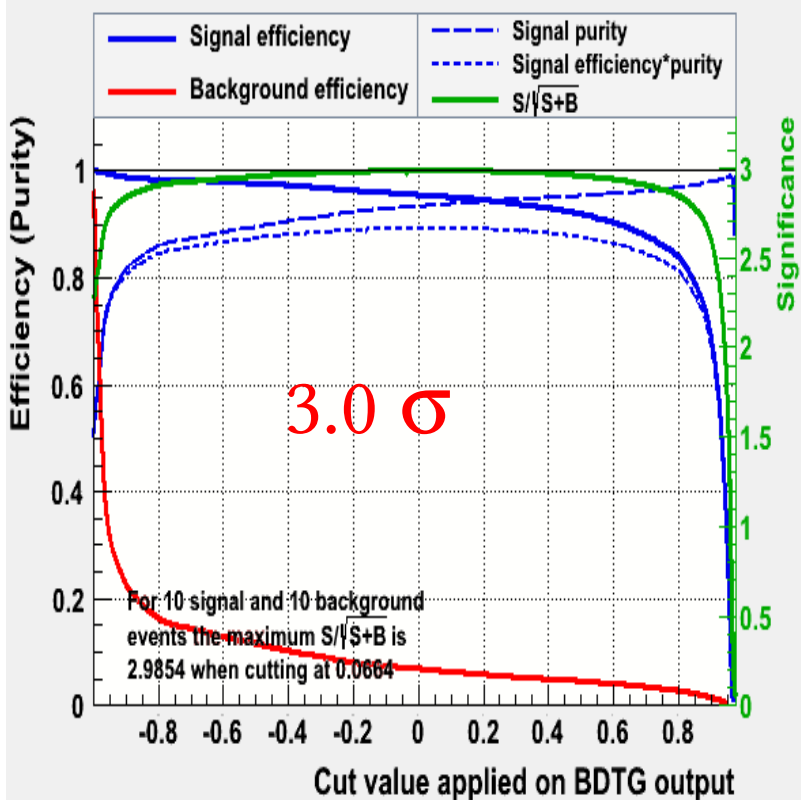


Signal is G^*
Background is $DY(M > 700 \text{ GeV})$

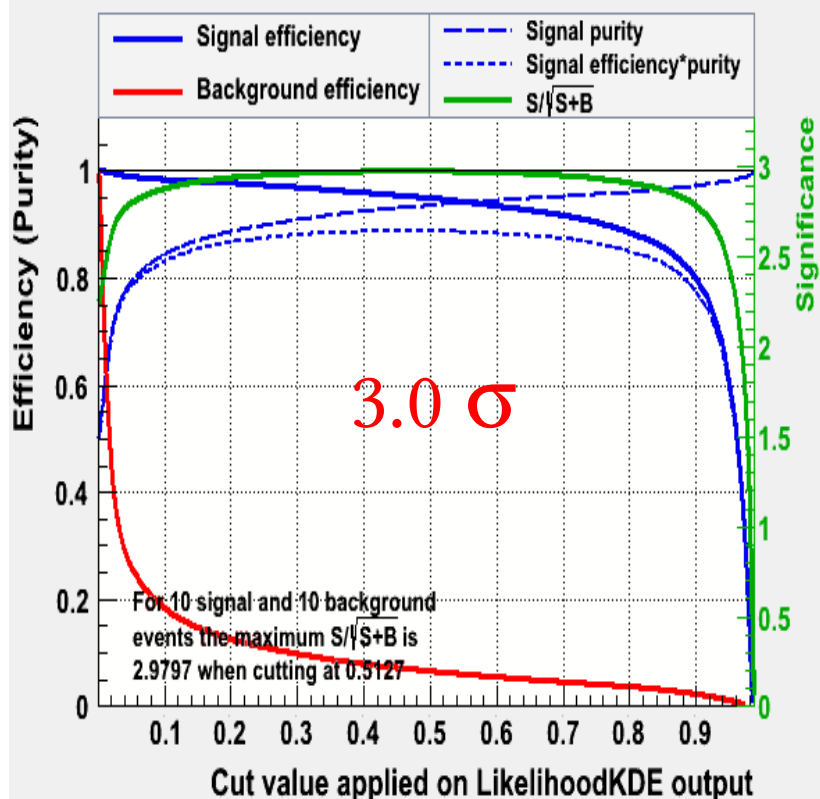
New Study

| Classifier | #signal | Optimal-cut | S/sqrt(S+B) | NSig | NBkg | EffSig | EffBkg |
|-----------------------|-----------|---------------|----------------|-----------------|------------------|---------------|----------------|
| Likelihood: | 10 | 0.0423 | 2.96778 | 9.579605 | 0.8395426 | 0.958 | 0.08395 |
| LikelihoodD: | 10 | -0.1101 | 2.95324 | 9.568575 | 0.9291625 | 0.9569 | 0.09292 |
| LikelihoodPCA: | 10 | 0.7228 | 2.92812 | 9.586959 | 1.132782 | 0.9587 | 0.1133 |
| LikelihoodKDE: | 10 | 0.5127 | 2.97967 | 9.485231 | 0.6482849 | 0.9485 | 0.06483 |
| BDTG: | 10 | 0.0664 | 2.98541 | 9.525677 | 0.6551523 | 0.9526 | 0.06552 |

Cut efficiencies and optimal cut value



Cut efficiencies and optimal cut value

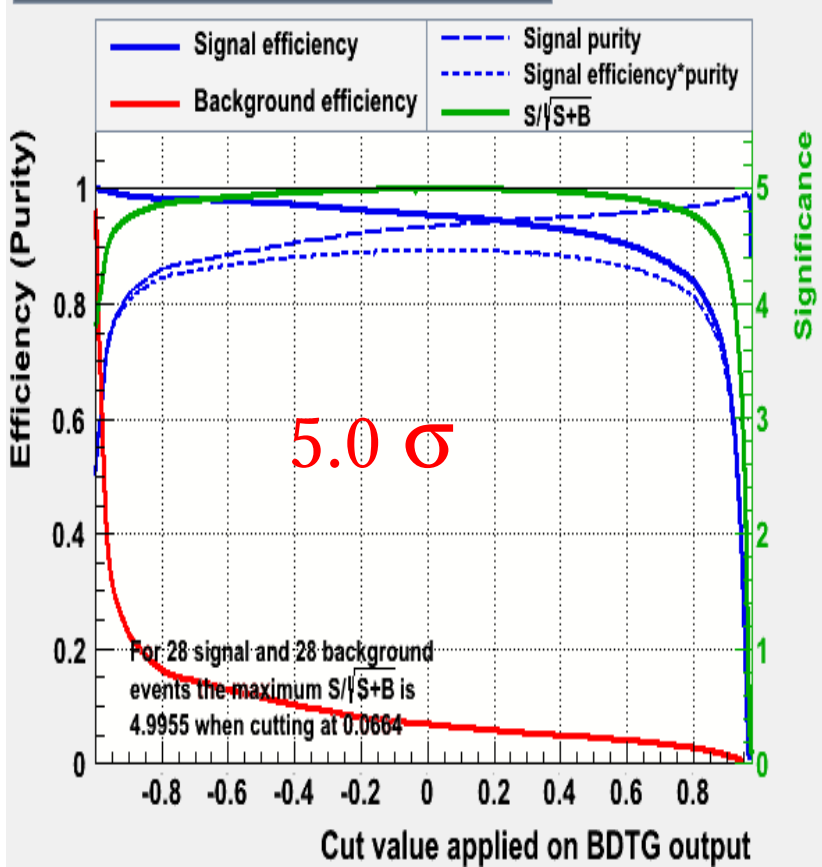


Signal is G^*
Background is $DY(M > 700 \text{ GeV})$

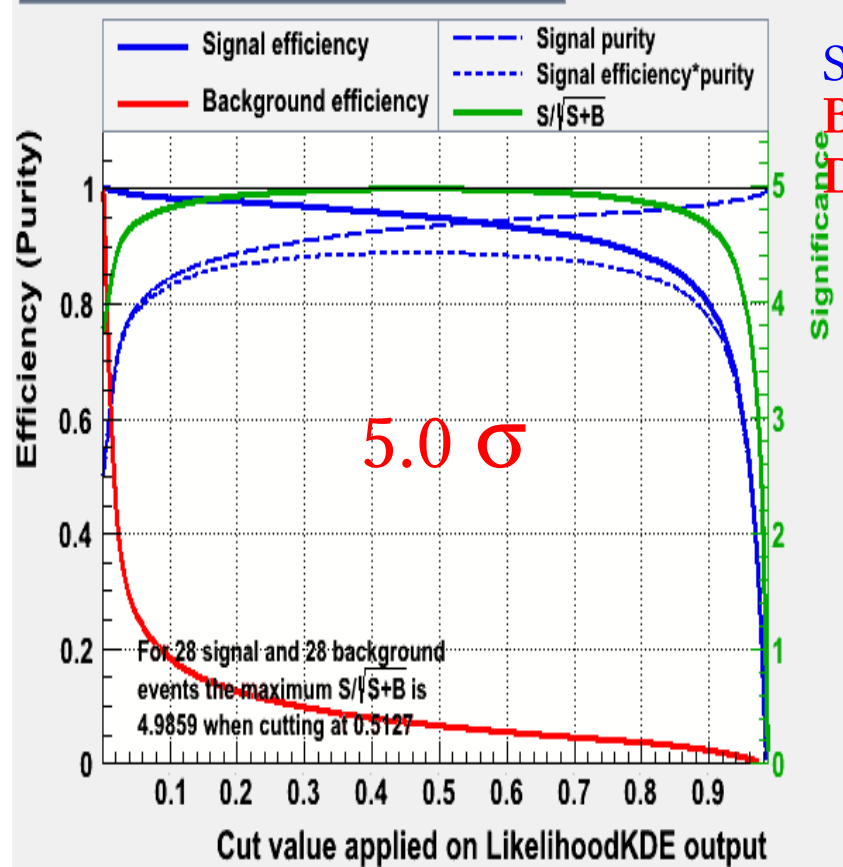
New Study

| Classifier | #signal | Optimal-cut | S/sqrt(S+B) | NSig | NBkg | EffSig | EffBkg |
|--------------------------|---------|-------------|----------------|----------|----------|--------|---------|
| Likelihood: | 28 | 0.0423 | 4.96604 | 26.82289 | 2.350719 | 0.958 | 0.08395 |
| LikelihoodD: | 28 | -0.1101 | 4.94172 | 26.79201 | 2.601655 | 0.9569 | 0.09292 |
| LikelihoodPCA: | 28 | 0.7228 | 4.89968 | 26.84349 | 3.171789 | 0.9587 | 0.1133 |
| LikelihoodKDE: 28 | | 0.5127 | 4.98594 | 26.55865 | 1.815198 | 0.9485 | 0.06483 |
| BDTG: 28 | | 0.0664 | 4.99555 | 26.6719 | 1.834426 | 0.9526 | 0.06552 |

Cut efficiencies and optimal cut value



Cut efficiencies and optimal cut value



Signal is G^*
Background is $DY(M > 700 \text{ GeV})$

New Study

- (1) The angular distributions $[\cos(\theta^*)]$ have been studied in the framework of HEEP selection (v4.1) using **MC DY(M > 2000 GeV)**, **RSgrav(M = 2000 GeV)** and **Z' psi(M = 2000 GeV)**, using **CMSSW_5_3_X** and **full 2012 data**
- (2) It was found that the CS polar angles $\cos(\theta_{cs})$ is good variable to distinguish between the BSM bosons [G (ADD or RS) and Z'] and the DY b.g. Process.
- (3) Good agreements are seen between data and DY MC(M > 120 GeV).
- (4) we can reach 2σ separation bet G (M=2.25TeV) & DY at high mass with 20 events.
- (5) In the preparation for 2015 data taking, with the use of topological likelihood, with the hypothesis of having excess of data at **1 TeV/c²**
 - (a) **5 events** allows **2.1 σ** discrimination betw. **G* & DY**
 - (b) to reach **5.0 σ** discrimination **28 events** are needed

***Thanks to FP7
Project***

Backup

[1] In this study I used MVA Version 4.2.0, Sep 19, 2013

[2] Likelihood

The likelihood ratio $y_{\mathcal{L}}(i)$ for event i is defined by

$$y_{\mathcal{L}}(i) = \frac{\mathcal{L}_S(i)}{\mathcal{L}_S(i) + \mathcal{L}_B(i)},$$

where

$$\mathcal{L}_{S(B)}(i) = \prod_{k=1}^{n_{\text{var}}} p_{S(B),k}(x_k(i)),$$

[3] LikelihoodD

the "D" extension indicates decorrelated input variables (see option strings)

[4] Likelihood KDE

3.1 Kernel Density Estimator (KDE)

KDE is a non-parametric technique to estimate a probability density function $p(\mathbf{x})$ defined on \mathbb{R}^d from its i.i.d. samples $\{\mathbf{x}_i\}_{i=1}^n$. For the Gaussian kernel, KDE is expressed as

$$\hat{p}(\mathbf{x}) = \frac{1}{n(2\pi\sigma^2)^{d/2}} \sum_{i=1}^n \exp\left(-\frac{\|\mathbf{x} - \mathbf{x}_i\|^2}{2\sigma^2}\right).$$

[5] Likelihood PCA (Principle Component Analysis)

2.2 Maximum **Likelihood PCA** (MLPCA)

MLPCA estimates the model that maximizes the likelihood of estimating the true principal components and projection directions given the measured variables, or equivalently maximizing the probability density function of the measurements given the noise-free principal components, projection directions, and the true rank of the data matrix “ $\tilde{\mathbf{p}}$ ”, as

$$\{\hat{\mathbf{a}}, \hat{\mathbf{Z}}\}_{\text{MLPCA}} = \arg \max_{\tilde{\mathbf{a}}, \tilde{\mathbf{Z}}} L(\tilde{\mathbf{a}}, \tilde{\mathbf{Z}}, \tilde{\mathbf{p}}; \mathbf{X}) = \arg \max_{\tilde{\mathbf{a}}, \tilde{\mathbf{Z}}} P(\mathbf{X} | \tilde{\mathbf{a}}, \tilde{\mathbf{Z}}, \tilde{\mathbf{p}}) \quad (7)$$

[7] Boosted decision tree Gradient (BDTG)

- **Output(or response)**: a random variable y
- **Input(or explanatory)**: a set of random variables $\mathbf{x} = \{x_1, \dots, x_n\}$
- **Goal**: using a training sample $\{y_i, \mathbf{x}_i\}_1^N$ of known (y, \mathbf{x}) values to obtain an estimate $\hat{F}(\mathbf{x})$ of the function $F^*(\mathbf{x})$ mapping \mathbf{x} to y
- **Minimizing the expected value of some specified loss function $L(y, F(\mathbf{x}))$:**

$$F^* = \arg \min_{\underline{F}} E_{y, \mathbf{x}} L(y, F(\mathbf{x})). \quad (1)$$

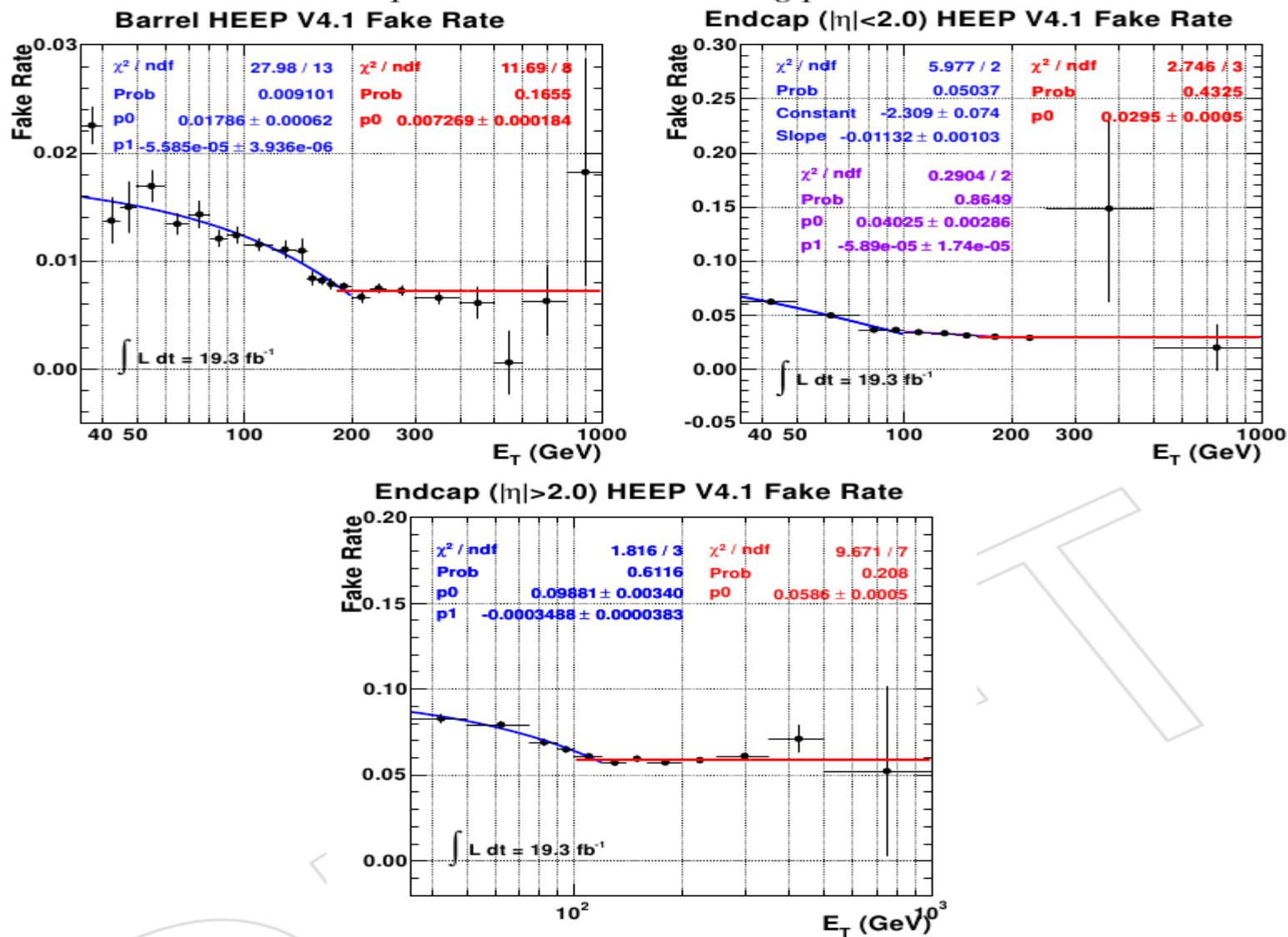
- Take a **non-parametric** approach
- Apply **numerical optimization** in function space
- Consider $\mathbf{F}(\mathbf{x})$ evaluated at each point \mathbf{x} to a **parameter** and seek to minimize $\Phi(F) = E_{y, \mathbf{x}} L(y, F(\mathbf{x})) = E_{\mathbf{x}} [E_y (L(y, F(\mathbf{x}))) | \mathbf{x}]$ at each individual \mathbf{x} , directly with respect to $F(\mathbf{x})$
- Numerical optimization paradigm:

$$F^*(\mathbf{x}) = \sum_{m=0}^M f_m(\mathbf{x}),$$

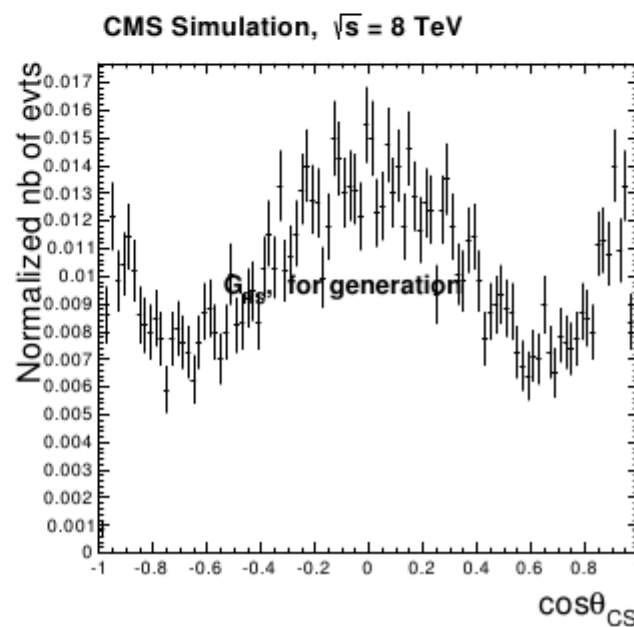
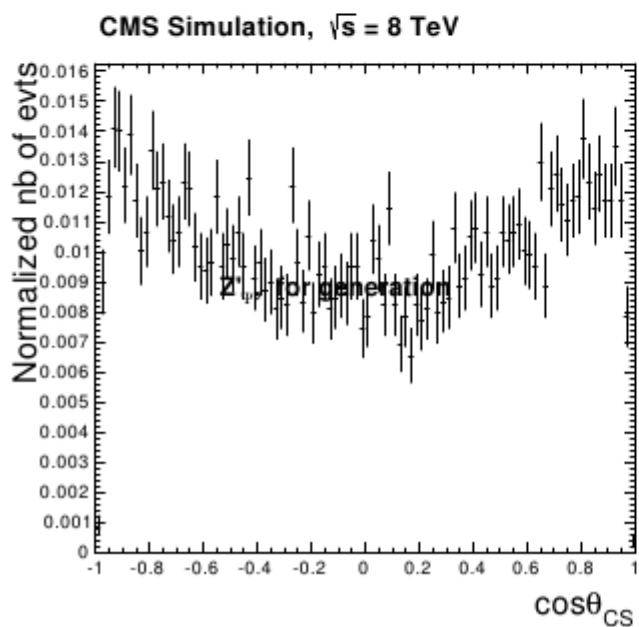
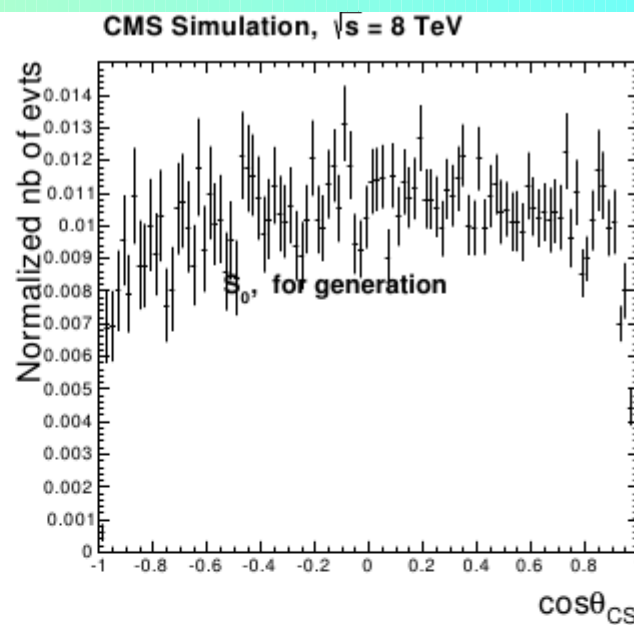
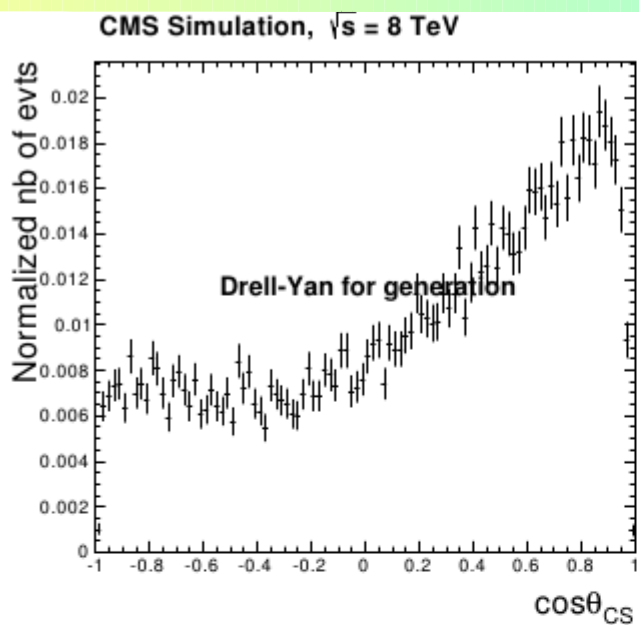
where $f_0(\mathbf{x})$ is an initial guess, and $\{f_m(\mathbf{x})\}_1^M$ are incremental functions (steps or boosts) defined by the optimization method

| variable | barrel | endcap |
|------------------------|----------|----------|
| $\sigma_{i\eta i\eta}$ | <0.013 | <0.034 |
| H/E | <0.15 | <0.10 |
| nr. missing hits | ≤ 1 | ≤ 1 |
| $ dxy $ | < 0.02 | < 0.05 |

Table 13: The selection requirements for the starting point of the fake rate calculation.



Pdf in 1D analysis



Pdf in 2D analysis

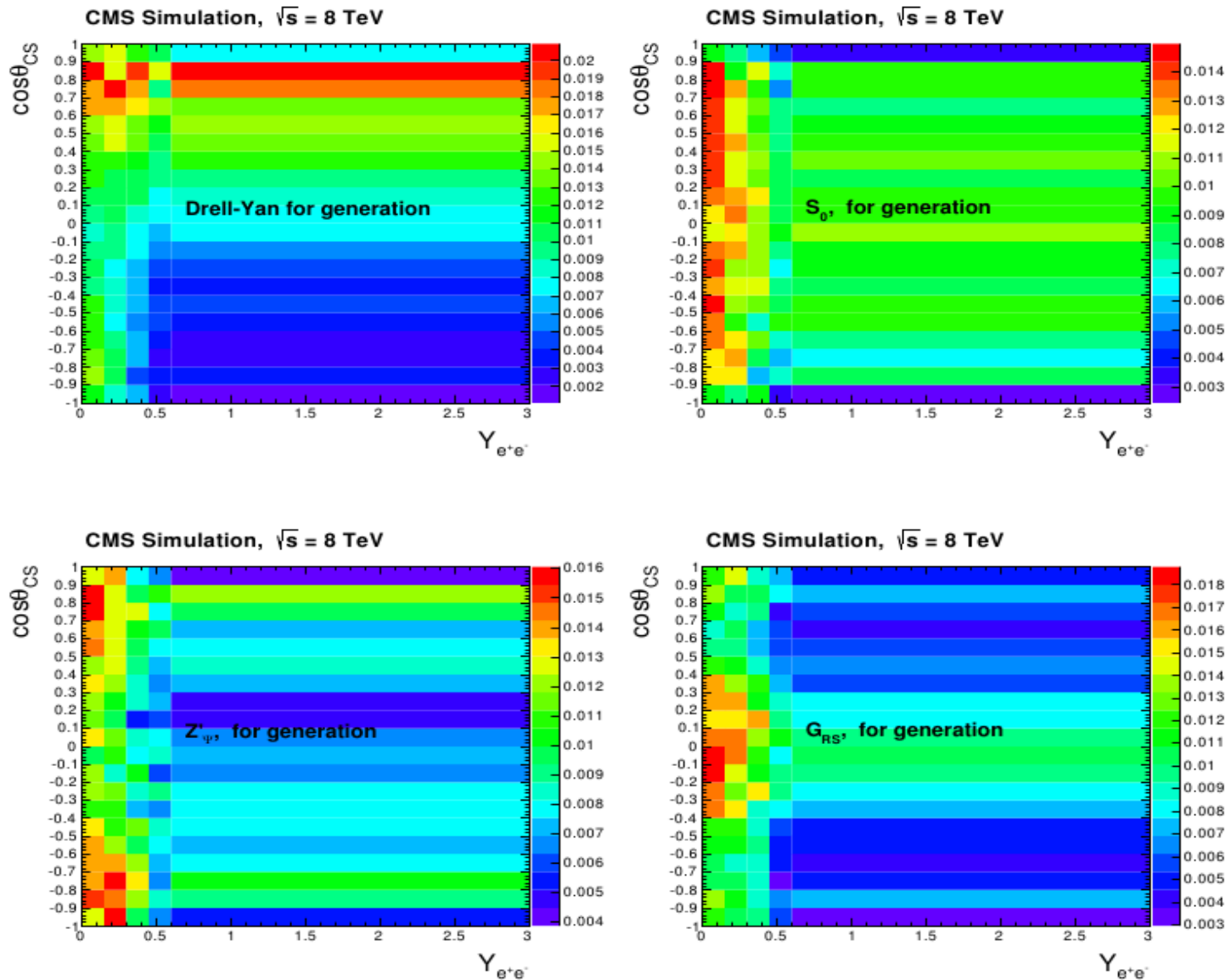


Figure 14: The normalized distributions of $(\cos \theta_{CS}, |y_{e^+e^-}|)$ defining the pdf in the 2D analysis for background (top left) and three signal samples, namely an isotropic model (top right), Z'_{ψ} (bottom left), a Randall-Sundrum graviton (bottom right).

| Signal sample, nb of evts, method | Exp. separation (in σ), (H_0 true) | Exp. separation (in σ) (H_1 true) |
|--------------------------------------|--|---|
| Spin 0, 10evts, 1D | 1.0 | 1.3 |
| Spin 0, 10evts, 2D | 1.1 | 1.4 |
| Spin 0, 20evts, 1D | 1.4 | 1.6 |
| Spin 0, 20evts, 2D | 1.6 | 1.9 |
| RSGrav, 10evts, 1D | 1.2 | 1.5 |
| RSGrav, 10evts, 2D | 1.3 | 1.6 |
| RSGrav, 20evts, 1D | 1.6 | 1.9 |
| RSGrav, 20evts, 2D | 1.8 | 2.1 |
| Z' Psi, 10evts, 1D | 0.8 | 1.1 |
| Z' Psi, 10evts, 2D | 1 | 1.3 |
| Z' Psi, 20evts, 1D | 1.1 | 1.5 |
| Z' Psi, 20evts, 2D | 1.5 | 1.8 |

Table 4: Expected separation (in σ) obtained using the angular information of dielectron pairs between the Drell-Yan model and different models of new physics in case the background hypothesis (first column) or the signal hypothesis (second column) is true for different number of events and likelihood functions (1D or 2D).