# LHCb Status & Plans for Yellow Report



Ronan McNulty (UCD Dublin) on behalf of the LHCb collaboration

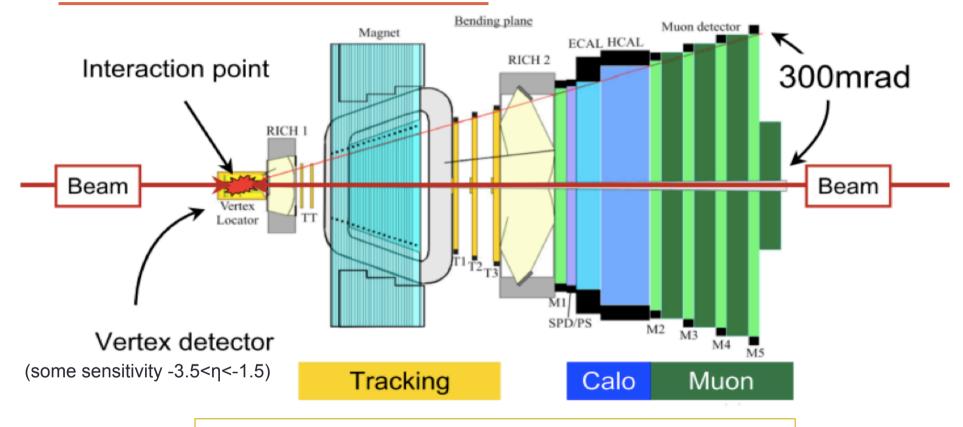


LHC Forward physics & diffraction. 19<sup>th</sup> February 2013

## **Outline**

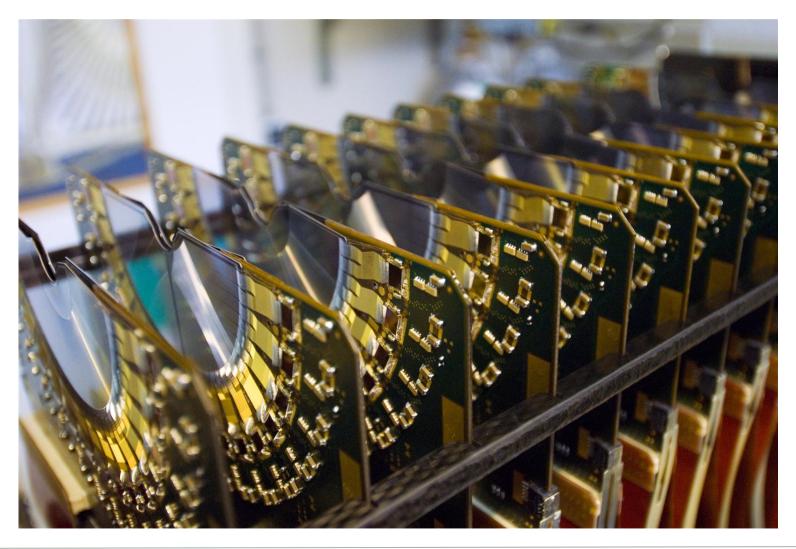
- General comments on LHCb
- Recent results on Central Exclusive Production
- Detector improvements
- Plans for Yellow Report
  - Focus on Chapter 5: Future CEP measurements

## The LHCb detector

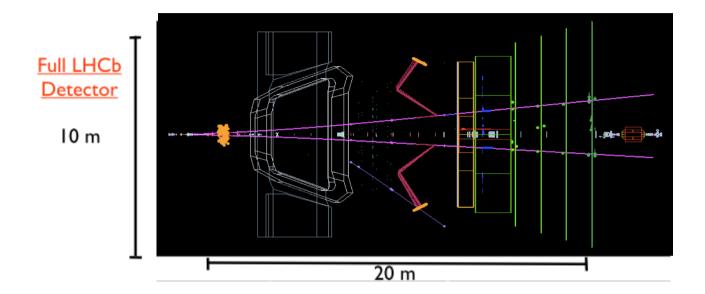


Fully instrumented from  $2 < \eta < 5$ Trigger on e,h, $\mu$ , $\gamma$  of few 100 MeV Low pile-up Ideal for low mass CEP

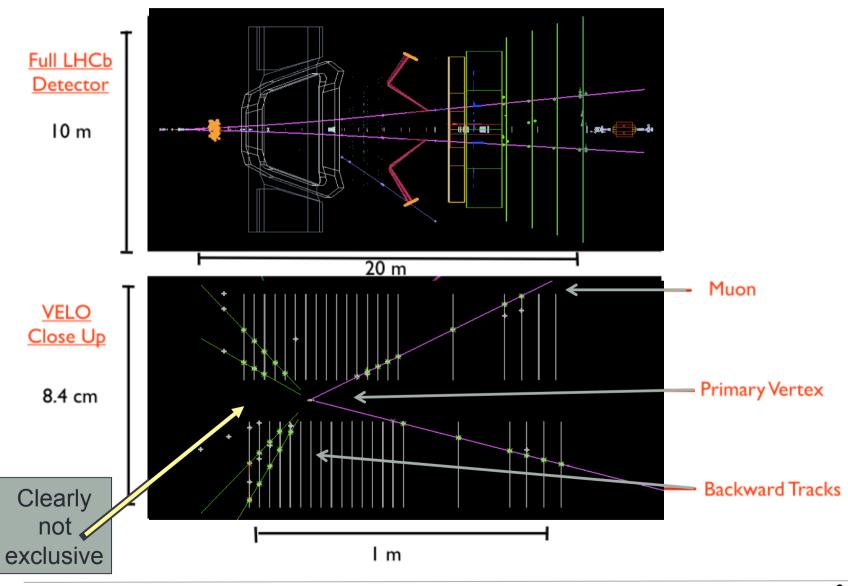
## VELO sub-detector



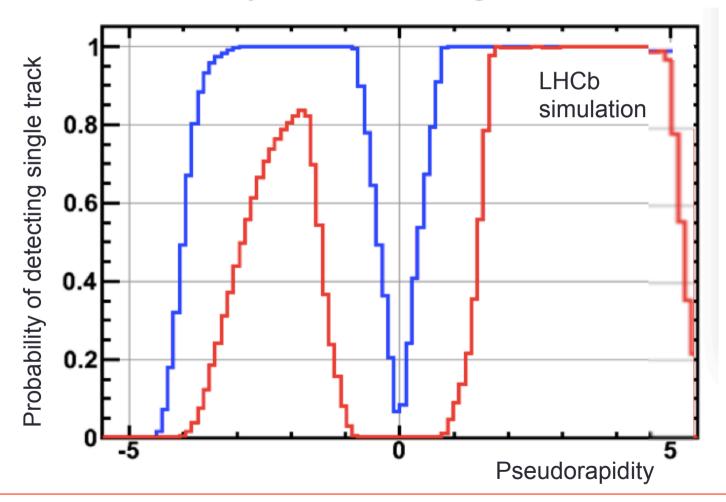
## **Use of backwards tracks**



## **Use of backwards tracks**

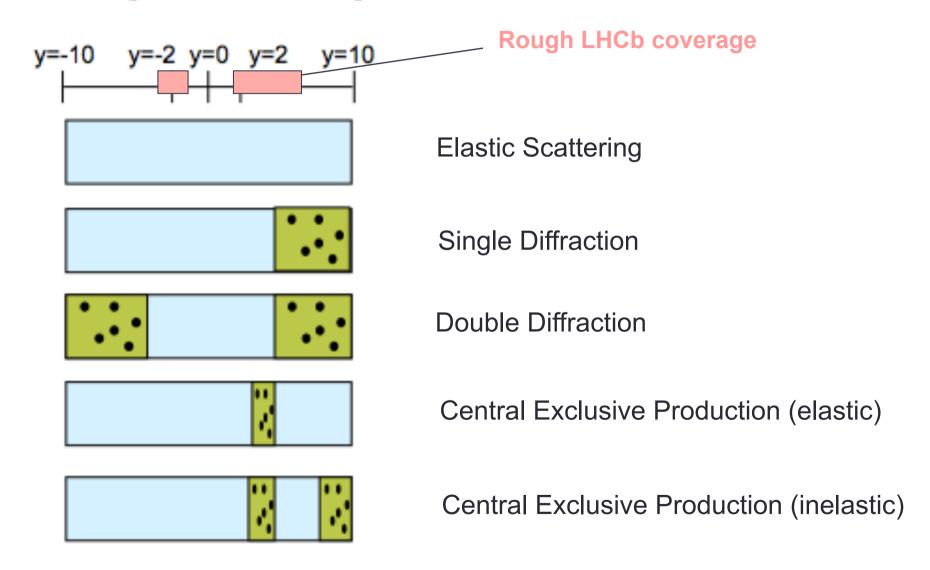


## Pseudorapidity veto range

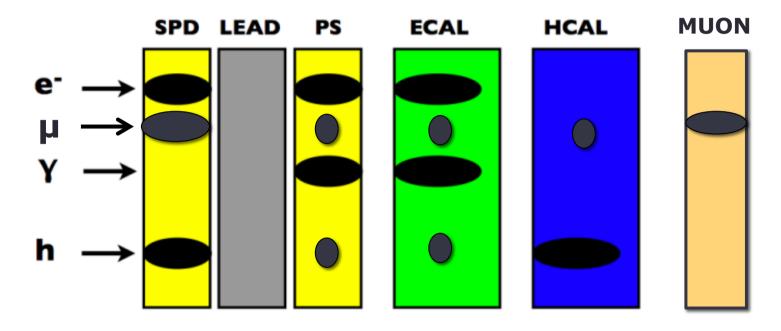


All results I show imply red region void, (except for muons from signal).

## **Graphical Representation**



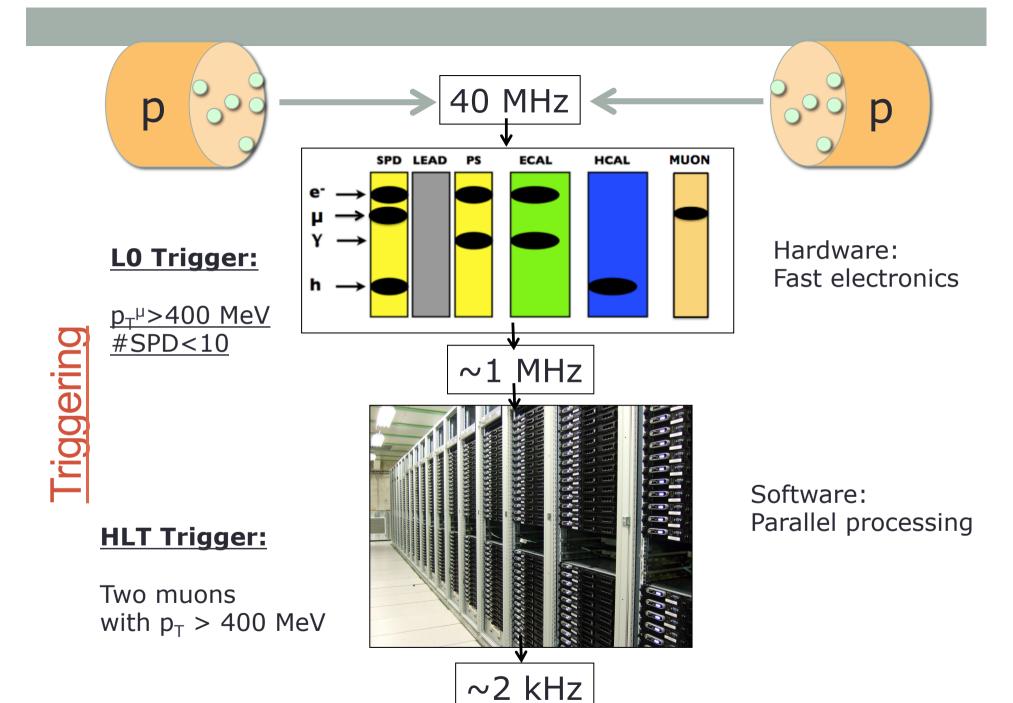
## Calorimeter System in LHCb



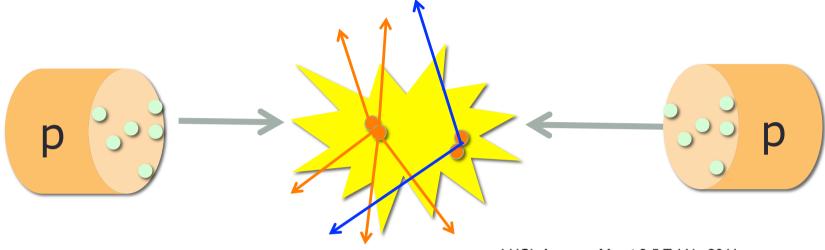
#### **Scintillation Pad Detector.**

If a charged particle goes through, we get a signal. Rough count of number of charged particles.

Use in trigger to select **low multiplicity** events for CEP. <10 hits



## Beam pile-up



High luminosity requires multiple proton interactions per beam-crossing.

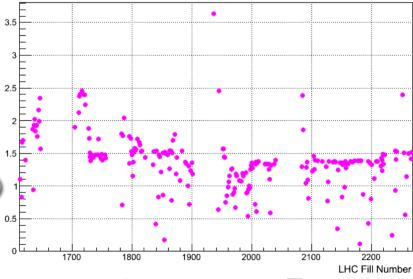
Number of interactions (N) /crossings, distributed

Average

#interactions

$$f(N) = \frac{e^{\mu} \mu^{N}}{N!}$$

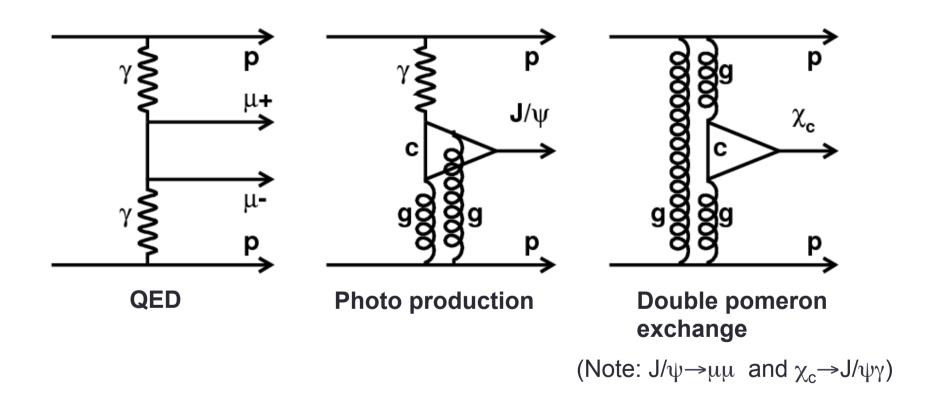
LHCb Average Mu at 3.5 TeV in 2011



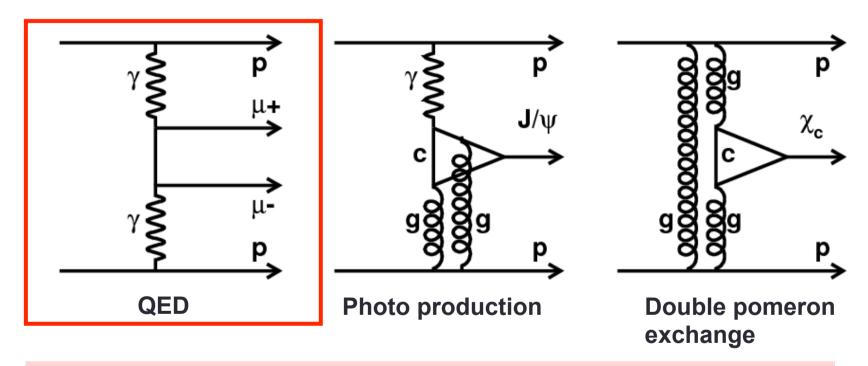
For LHCb in 2011,  $\overline{\mu}$ =1.4

## Central Exclusive Production of J/ψ and ψ(2S) mesons

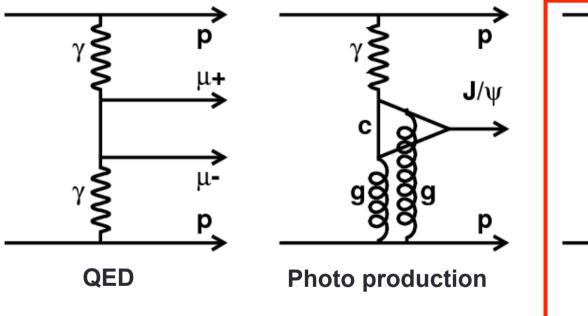
Data-taking year	Energy	Integrated Luminosity	Paper
2010	7 TeV	37pb <sup>-1</sup>	JPG 40 (2013) 045001
2011	7 TeV	930pb <sup>-1</sup>	arXiv: 1401.3288 (accepted by JPG)

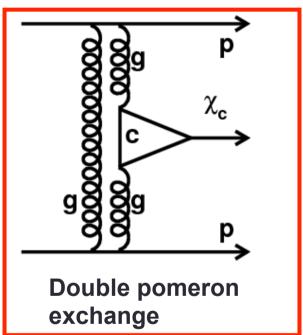


Related phenomena where the colourless object creates a particle

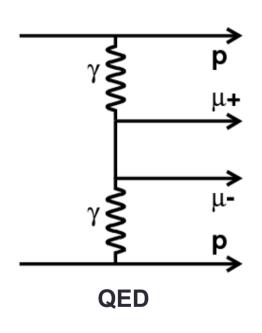


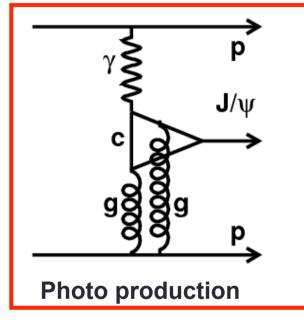
- QED process. Can be predicted with high accuracy (~1%)
- Candidate process for very precise luminosity determination at LHC

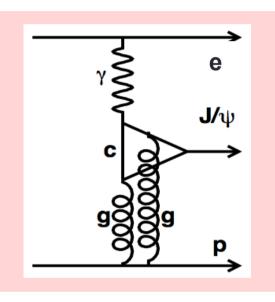




- Double pomeron exchange.
- Unambiguous evidence for pomeron
- 'Standard Candle' for other DPE processes, in particular, Higgs.







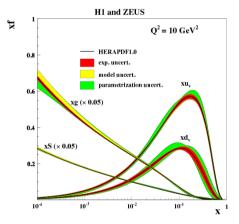
- Test of QCD and pomeron in clean environment
- Sensitive to diffractive PDF at very low x (to 5x10<sup>-6</sup>)
- Search for the odderon and saturation effects
- Measured at HERA/Tevatron but at different photon-proton energy, W

## Photo-production cross-section

$$\frac{\mathrm{d}\sigma}{\mathrm{d}t}\left(\gamma^*p\to J/\psi\ p\right)\Big|_{t=0} = \frac{\Gamma_{ee}M_{J/\psi}^3\pi^3}{48\alpha}\ \left[\frac{\alpha_s(\bar{Q}^2)}{\bar{Q}^4}xg(x,\bar{Q}^2)\right]^2\left(1+\frac{Q^2}{M_{J/\psi}^2}\right)\ \underline{\hspace{1cm}}$$

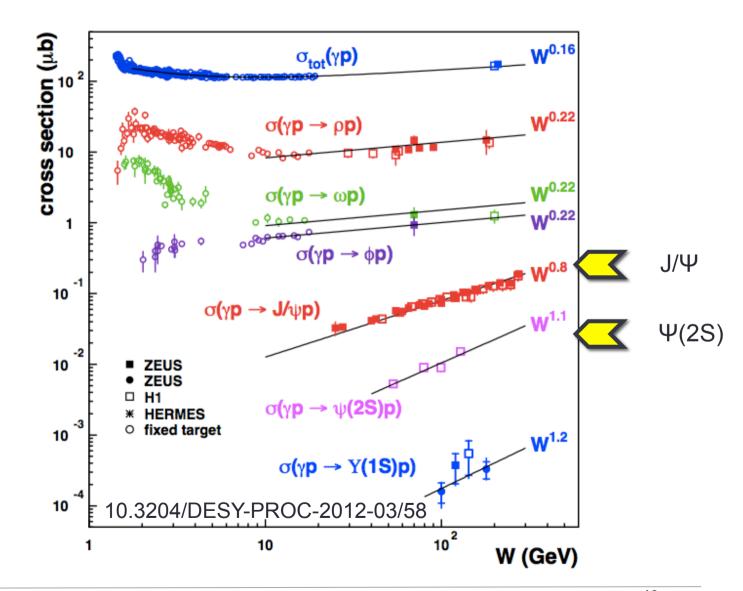
$$ar{Q}^2 = (Q^2 + M_{J/\psi}^2)/4, \qquad x = (Q^2 + M_{J/\psi}^2)/(W^2 + M_{J/\psi}^2)$$

Cross-section proportional to gluon<sup>2</sup>  $\sigma \sim (xg)^2$ and so  $\sigma \sim x^{\lambda}$ 



- [1] Martin A D, Nockles C, Ryskin M and Teubner T 2008 Small x gluon from exclusive  $J/\psi$  production Phys. Lett. B 662 252 (arXiv:0709.4406)
- [2] Ryskin M G 1993 J/ψ electroproduction in LLA QCD Z. Phys. C 57 89
- [3] Ryskin M G, Roberts R G, Martin A D and Levin E M 1997 Diffractive  $J/\psi$  photoproduction as a probe of the gluon density Z. Phys. C 76 231 (arXiv:hep-ph/9511228)
- [4] S. Jones, A. Martin, M. Ryskin, and T. Teubner, Probes of the small x gluon via exclusive  $J/\psi$  and  $\Upsilon$  production at HERA and the LHC, JHEP 1311 (2013) 085, arXiv:1307.7099.

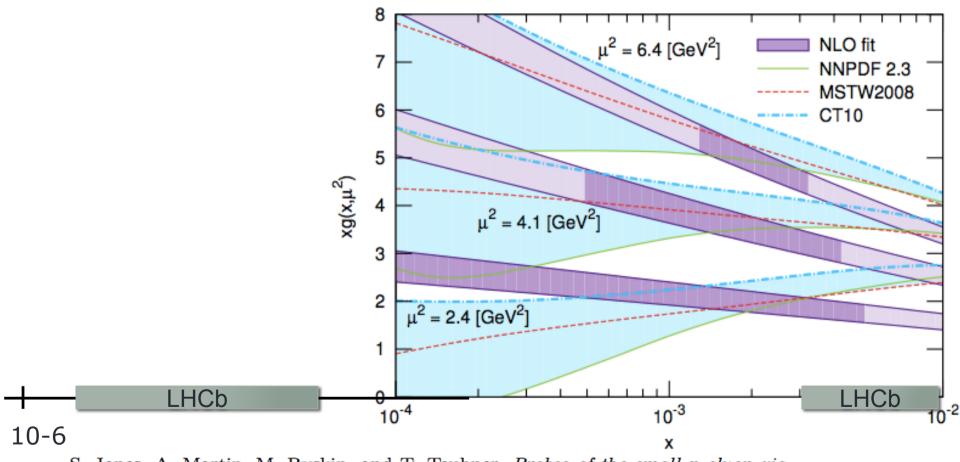
### HERA vector meson photo-production results



#### Note:

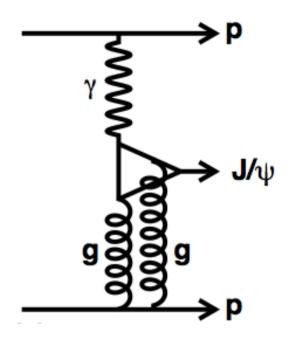
- $\sigma \sim x^{\lambda}$
- soft/hard
- $g(x,Q^2)$

## Sensitivity to gluon pdf (arXiv: 1307.7099)



S. Jones, A. Martin, M. Ryskin, and T. Teubner, *Probes of the small x gluon via exclusive J/\psi and \Upsilon production at HERA and the LHC, JHEP 1311 (2013) 085, arXiv:1307.7099.* 

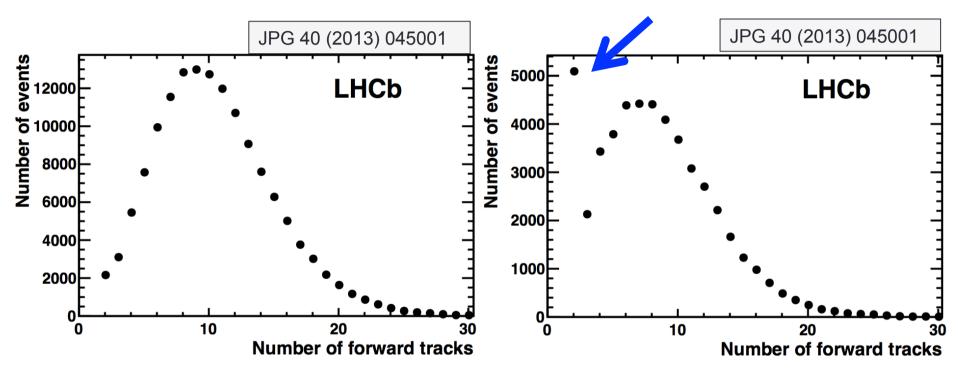
## Simple Selection Criteria



- Precisely two forward muons
- No backward tracks
- No photons
- p<sub>T</sub><sup>2</sup> of dimuon < 0.8 GeV<sup>2</sup>
- Mass of dimuon within 65 MeV of J/ψ or ψ(2S)

2 forward gaps that sum to 3.5 units of rapidity + a backward <gap> of 1.7

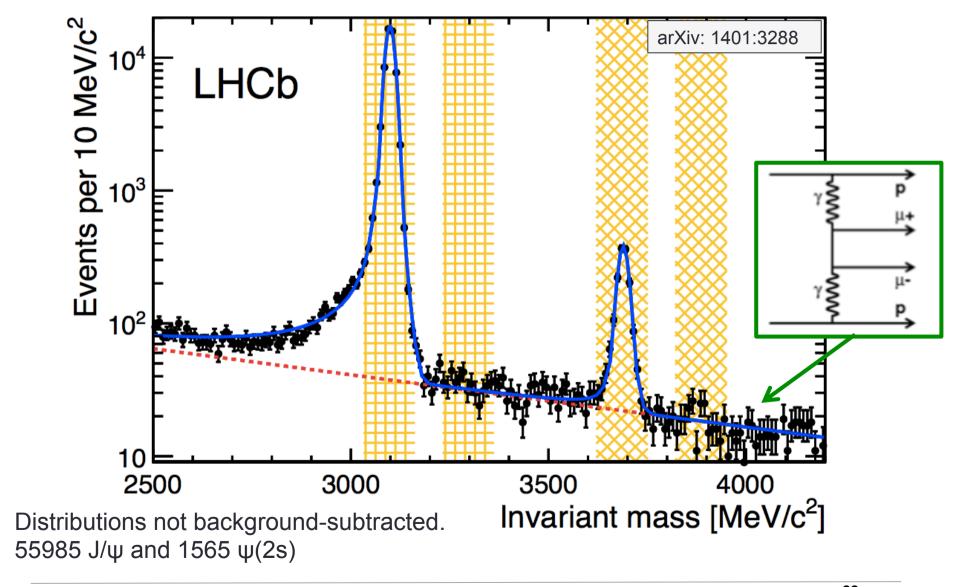
# Effect of rapidity gap requirement on low multiplicity muon triggered events



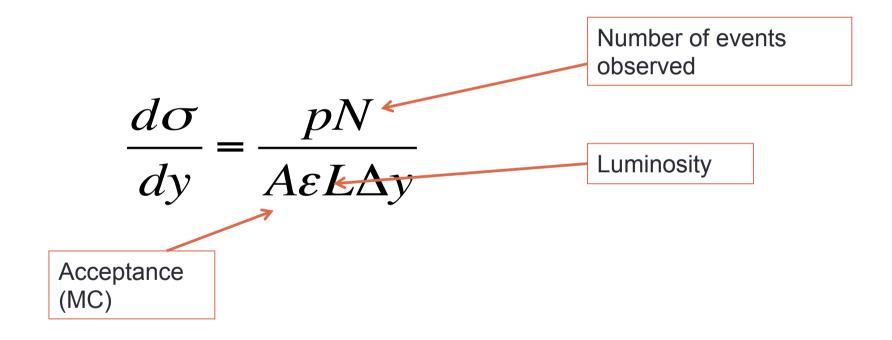
All triggered events

With veto on backward tracks

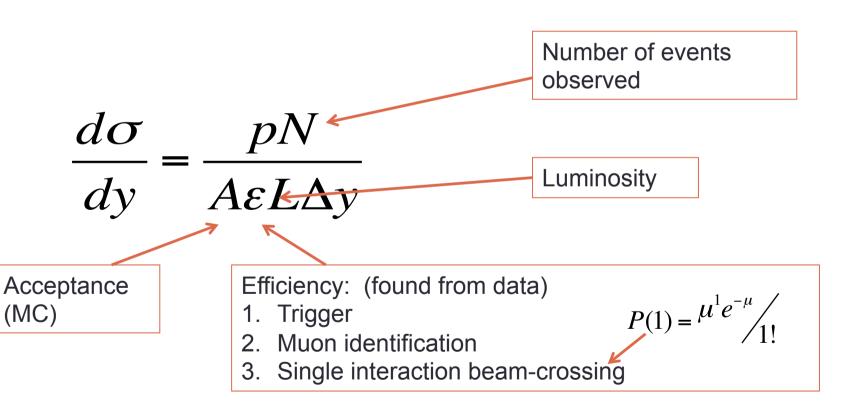
## Non-resonant background very small



## Cross-section measurement J/ $\psi$ / $\psi$ (2S)



## Cross-section measurement J/ $\psi$ / $\psi$ (2S)



## Cross-section measurement J/ψ / ψ(2S)

Purity: (found from data)

- 1. non-resonant bkg (1% / 17%)
- 2. Feeddown (10% / 2%)
- 3. Inelastic Jpsi production (40% / 40%)

Number of events observed

$$\frac{d\sigma}{dy} = \frac{pN}{A\varepsilon L\Delta y}$$

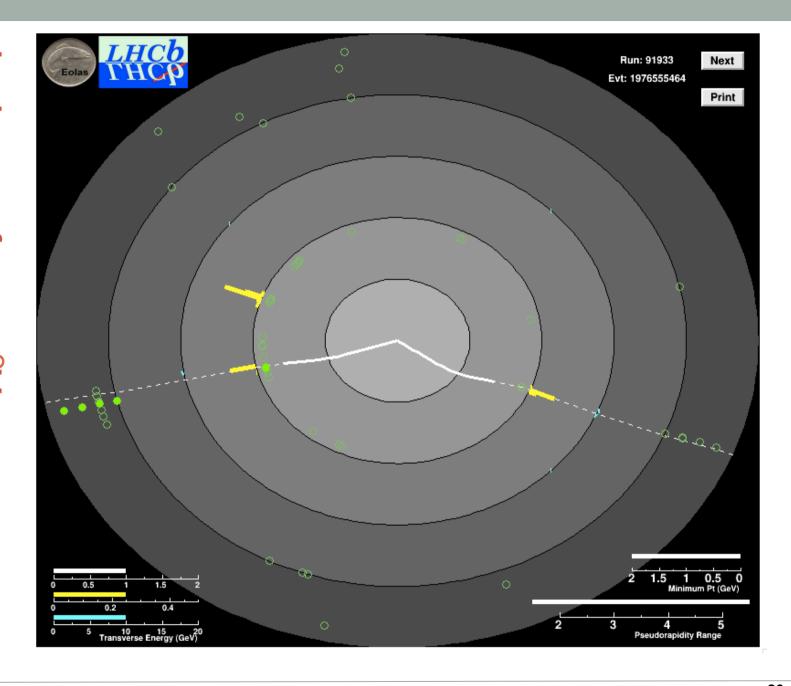
Luminosity

Acceptance (MC)

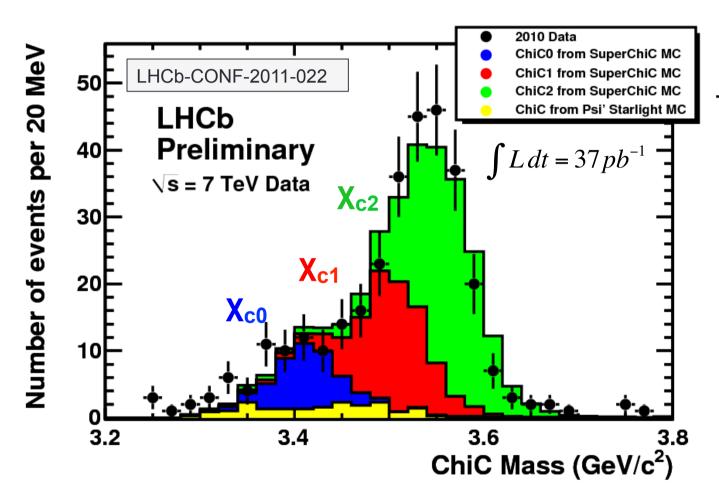
Efficiency: (found from data)

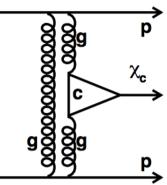
- 1. Trigger
- 2. Tracking & muon id.
- 3. Single interaction beam-crossing

# Sandidate for $\chi_c$ decay to $J/\psi + \gamma$

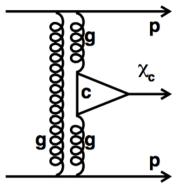


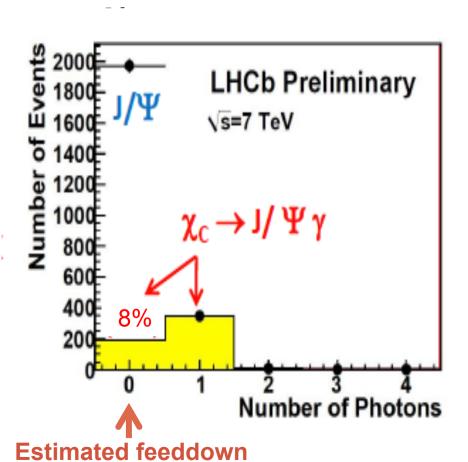
## Selected $\chi_{c0,1,2}$ candidates

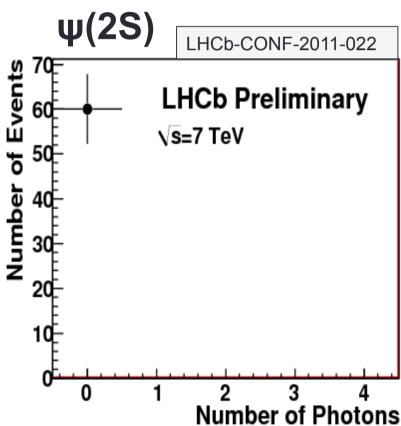




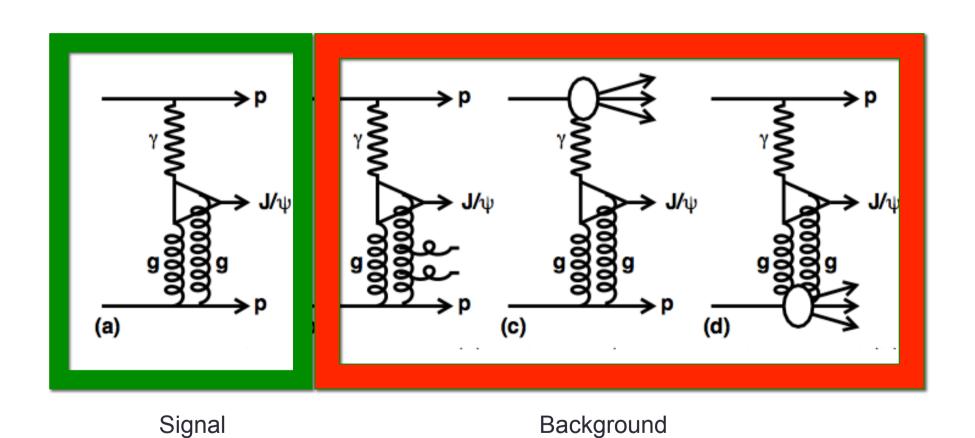
## Feed-down background



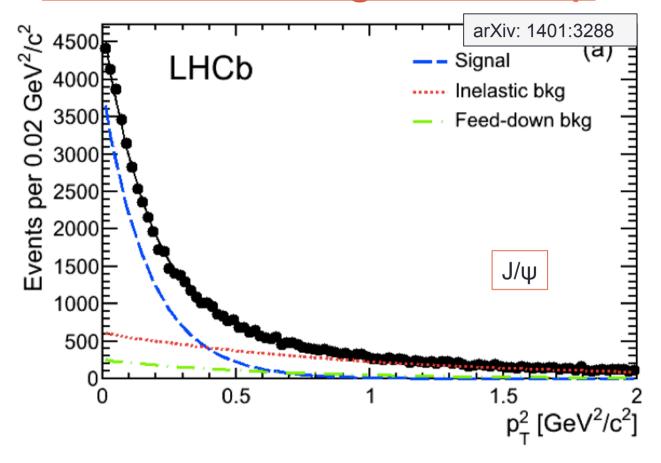




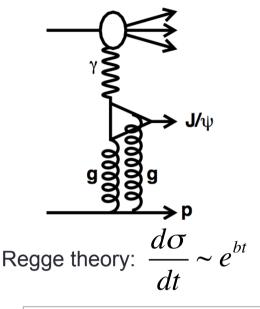
## Inelastic background



## Inelastic background J/ψ



Systematic: Change signal to  $\,(1+b_{
m pd}p_{
m T}^2/n)^{-n}$ 



#### **HERA** measured:

 $b_s$ =4.9 GeV<sup>-2</sup>

 $b_{pd}$ =1.1 GeV<sup>-2</sup>

#### LHCb Expect:

 $b_s \sim 6 \text{ GeV}^{-2}$ 

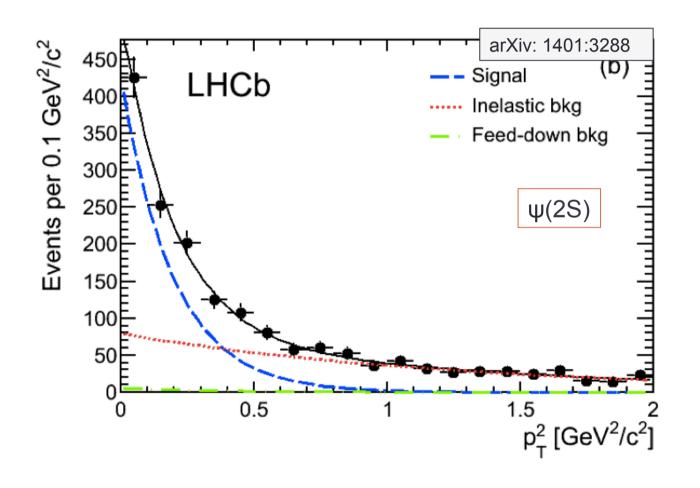
 $b_{pd}$ ~ 1 GeV<sup>-2</sup>

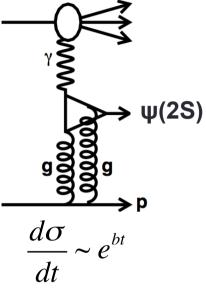
#### LHCb Fit:

 $b_s = 5.70 \pm 0.11 \text{ GeV}^{-2}$ 

 $b_{pd}$ =0.97±0.04 GeV<sup>-2</sup>

## Inelastic background ψ(2S)





HERA measured:  $b_s$ =4.2 GeV<sup>-2</sup>  $b_{pd}$ =0.6 GeV<sup>-2</sup> LHCb Expect:  $b_s \sim 5.5$  GeV<sup>-2</sup>  $b_{pd} \sim 0.6$  GeV<sup>-2</sup> LHCb Fit:  $b_s$ =5.1±0.7 GeV<sup>-2</sup>  $b_{pd}$ =0.8±0.2 GeV<sup>-2</sup>

Table 1: Quantities entering the cross-section calculations as a function of meson rapidity.

$y$ range $(J/\psi)$	[2.00, 2.25]	[2.25, 2.50]	[2.50, 2.75]	[2.75,3.00]	[3.00,3.25]	
# Events	798	3911	6632	8600	9987	
Acceptance	$0.467 \pm 0.009$	$0.653 \pm 0.013$	$0.719 \pm 0.014$	$0.718 \pm 0.014$	$0.713 \pm 0.014$	
$\epsilon_{\mathrm{id}}^{\psi} \times \epsilon_{\mathrm{trig}}^{\psi}$	$0.71 \pm 0.03$	$0.78 \pm 0.02$	$0.81 \pm 0.01$	$0.84 \pm 0.01$	$0.85 \pm 0.01$	
Purity	$0.592 \pm 0.012 \pm 0.030$					
$y$ range $(J/\psi)$	[3.25, 3.50]	[3.50, 3.75]	[3.75, 4.00]	[4.00, 4.25]	[4.25,4.50]	
# Events	9877	7907	5181	2496	596	
Acceptance	$0.739 \pm 0.015$	$0.734 \pm 0.015$	$0.674 \pm 0.014$	$0.566\pm0.011$	$0.401\pm0.008$	
$\epsilon_{\mathrm{id}}^{\psi} \times \epsilon_{\mathrm{trig}}^{\psi}$	$0.87 \pm 0.01$	$0.88 \pm 0.01$	$0.87 \pm 0.01$	$0.83 \pm 0.02$	$0.81 \pm 0.03$	
Purity	$0.592 \pm 0.012 \pm 0.030$					
y range $(\psi(2S))$	[2.00, 2.25]	[2.25, 2.50]	[2.50, 2.75]	[2.75,3.00]	[3.00, 3.25]	
# Events	31	111	208	1287	268	
Acceptance	$0.678 \pm 0.013$	$0.800 \pm 0.016$	$0.834 \pm 0.01$	$7  0.787 \pm 0.016$	$0.755 \pm 0.015$	
$\epsilon_{\mathrm{id}}^{\psi} \times \epsilon_{\mathrm{trig}}^{\psi}$	$0.80 \pm 0.03$	$0.83 \pm 0.02$	$0.86 \pm 0.01$	$0.88 \pm 0.01$	$0.88 \pm 0.01$	
Purity $(\psi(2S))$	$0.52 \pm 0.07 \pm 0.03$					
$y \operatorname{range}(\psi(2S))$	[3.25, 3.50]	[3.50, 3.75]	[3.75, 4.00]	[4.00, 4.25]	[4.25, 4.50]	
# Events	282	201	105	61	11	
Acceptance	$0.748 \pm 0.015$	$0.702\pm0.014$	$0.628 \pm 0.013$	$0.524 \pm 0.010$	$0.384 \pm 0.008$	
$\epsilon_{\mathrm{id}}^{\psi} \times \epsilon_{\mathrm{trig}}^{\psi}$	$0.90 \pm 0.01$	$0.89 \pm 0.01$	$0.87 \pm 0.01$	$0.84 \pm 0.02$	$0.77 \pm 0.03$	
Purity $(\psi(2S))$	$0.52 \pm 0.07 \pm 0.03$					
$y$ range $(J/\psi)$ an	$\mathrm{id}\;\psi(2S))$		[2.00, 4.50]			
$\epsilon_{ m sel}$	$0.87 \pm 0.01$					
$\epsilon_{ m single}$	$0.241 \pm 0.003$					
$L  ext{ (pb}^{-1})$	$929 \pm 33$					

Cross-section\*BR for both muons in pseudorapidity range  $2 < \eta < 4.5$ :

[2.00, 2.25]	[2.25, 2.50]	[2.50, 2.75]	[2.75, 3.00]	[3.00, 3.25]
$29.3 \pm 1.7$	$92.5 \pm 2.4$	$137.8 \pm 2.4$	$173.1 \pm 2.6$	$198.0 \pm 2.7$
$0.56 \pm 0.11$	$1.75 \pm 0.17$	$3.06 \pm 0.22$	$4.41 \pm 0.26$	$4.24 \pm 0.26$
[3.25, 3.50]	[3.50, 3.75]	[3.75, 4.00]	[4.00, 4.25]	[4.25, 4.50]
$187.6 \pm 2.6$	$148.9 \pm 2.4$	$107.4 \pm 2.1$	$65.3 \pm 2.0$	$21.9 \pm 1.3$
4 51 1 0 05	0.40   0.05	0.05   0.00	1 47   0 10	$0.36 \pm 0.11$
	$0.56 \pm 0.11$ $[3.25, 3.50]$ $187.6 \pm 2.6$	$29.3 \pm 1.7$ $92.5 \pm 2.4$ $0.56 \pm 0.11$ $1.75 \pm 0.17$ [3.25, 3.50] $[3.50, 3.75]187.6 \pm 2.6 148.9 \pm 2.4$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

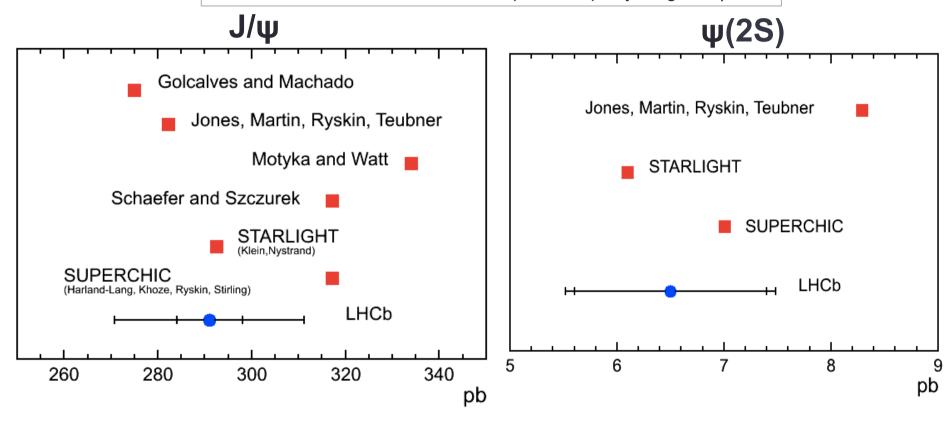
Correlated uncertainties expressed as a percentage	of the final resu	lt
$\epsilon_{ m sel}$	1.4%	
Purity determination $(J/\psi)$	2.0%	(2C)
Purity determination $(\psi(2S))$	13.0%	ψ(2S)
$^*\epsilon_{ m single}$	1.0%	
*Acceptance	2.0%	J/ψ
*Shape of the inelastic background	5.0%	σ, φ
*Luminosity	3.5%	
Total correlated statistical uncertainty $(J/\psi)$	2.4%	
Total correlated statistical uncertainty $(\psi(2S))$	13.0%	
Total correlated systematic uncertainty	6.5%	

## Comparison to theory

- V. P. Gonçalves and M. V. T. Machado, Vector meson production in coherent hadronic interactions: an update on predictions for RHIC and LHC, Phys. Rev. C84 (2011) 011902, arXiv:1106.3036.
- S. Jones, A. Martin, M. Ryskin, and T. Teubner, *Probes of the small x gluon via exclusive J/\psi and \Upsilon production at HERA and the LHC, JHEP 1311 (2013) 085, arXiv:1307.7099.*
- L. Motyka and G. Watt, Exclusive photoproduction at the Fermilab Tevatron and CERN LHC within the dipole picture, Phys. Rev. **D78** (2008) 014023, arXiv:0805.2113.
- W. Schäfer and A. Szczurek, Exclusive photoproduction of  $J/\psi$  in proton-proton and proton-antiproton scattering, Phys. Rev. **D76** (2007) 094014, arXiv:0705.2887.
- S. R. Klein and J. Nystrand, *Photoproduction of quarkonium in proton proton and nucleus nucleus collisions*, Phys. Rev. Lett. **92** (2004) 142003, arXiv:hep-ph/0311164.
- L. A. Harland-Lang, V. A. Khoze, M. G. Ryskin, and W. J. Stirling, Central exclusive  $\chi_c$  meson production at the Tevatron revisited, Eur. Phys. J. C65 (2010) 433, arXiv:0909.4748.

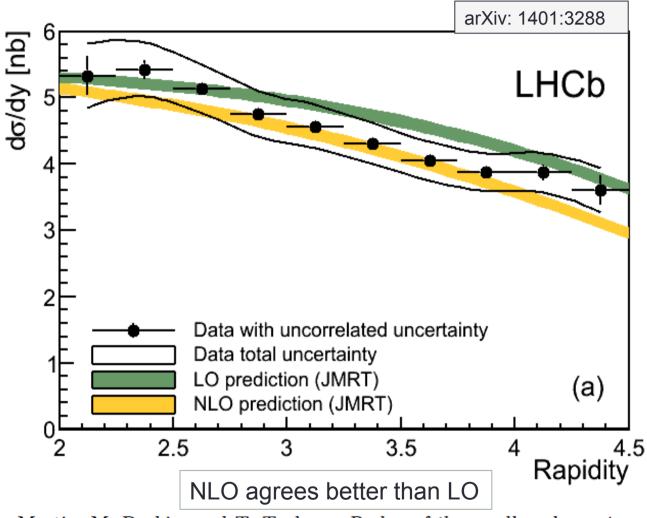
## **Integrated Cross-sections**

Cross-section\*BR for both muons in pseudorapidity range 2<η<4.5:



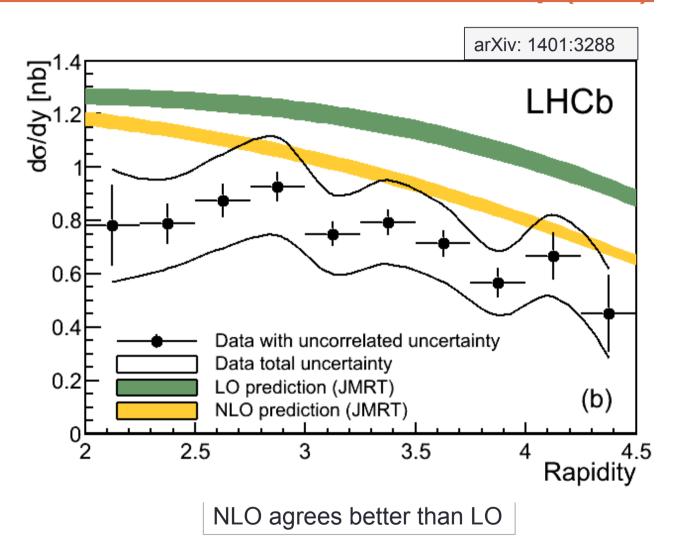
Good agreement with all theory estimates

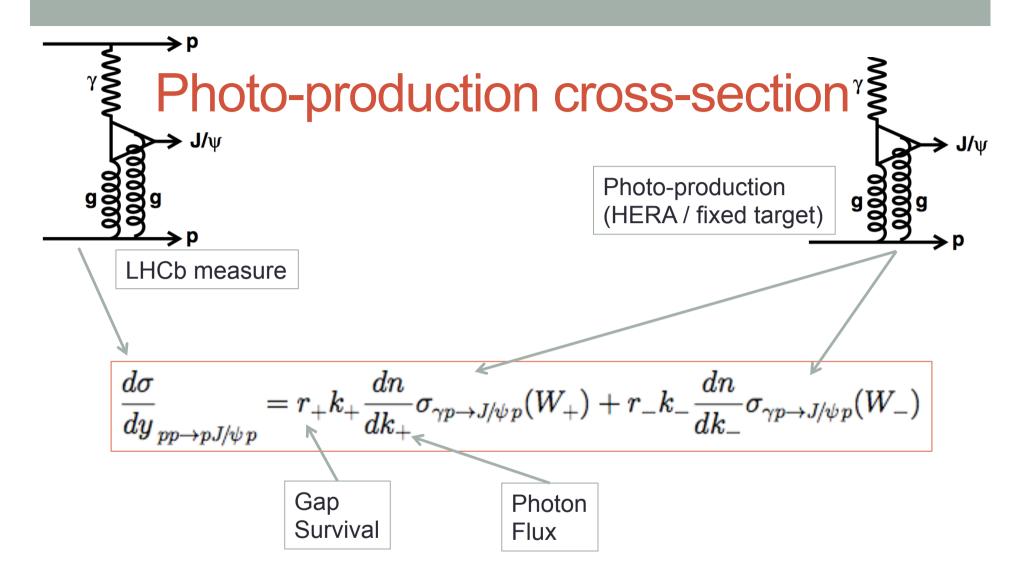
## Differential cross-sections J/ψ



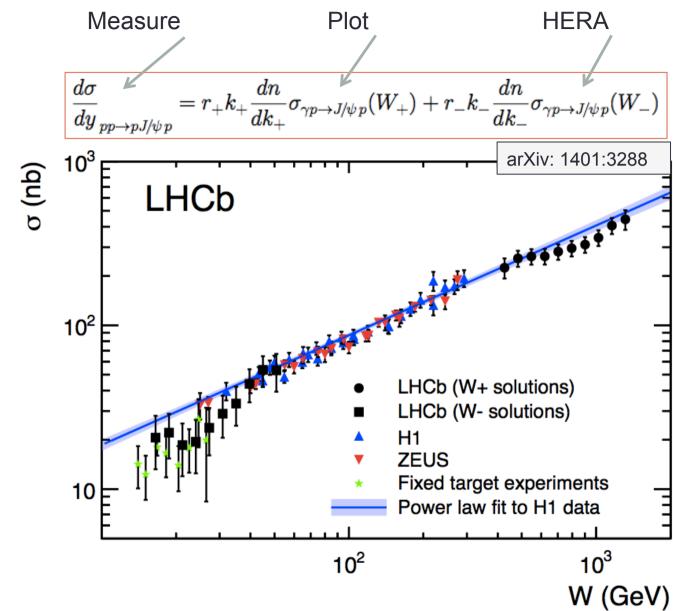
S. Jones, A. Martin, M. Ryskin, and T. Teubner, *Probes of the small x gluon via exclusive J/\psi and \Upsilon production at HERA and the LHC, JHEP 1311 (2013) 085, arXiv:1307.7099.* 

### Differential cross-sections ψ(2S)

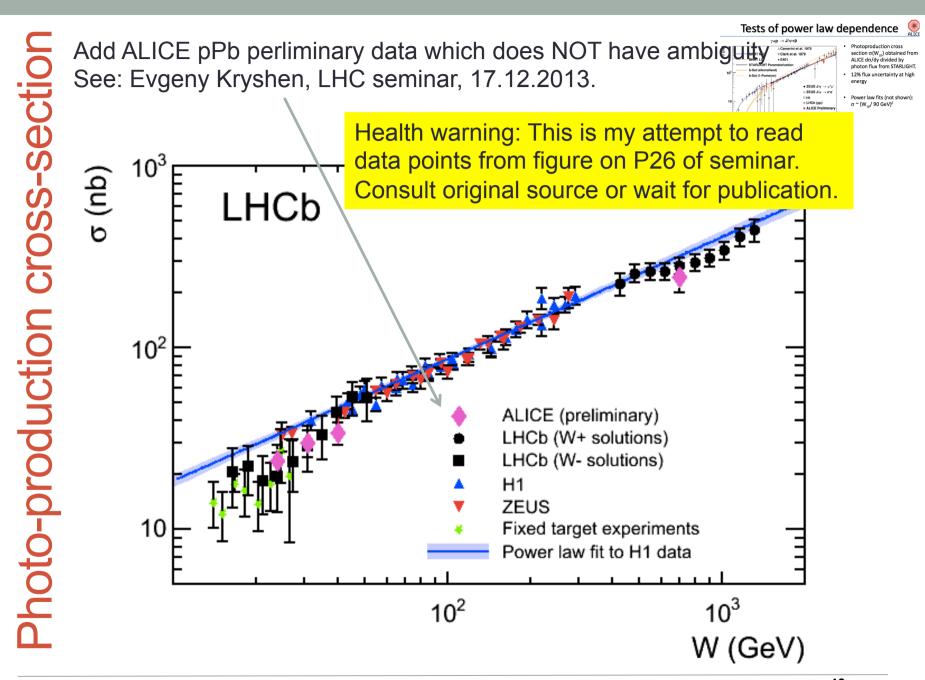




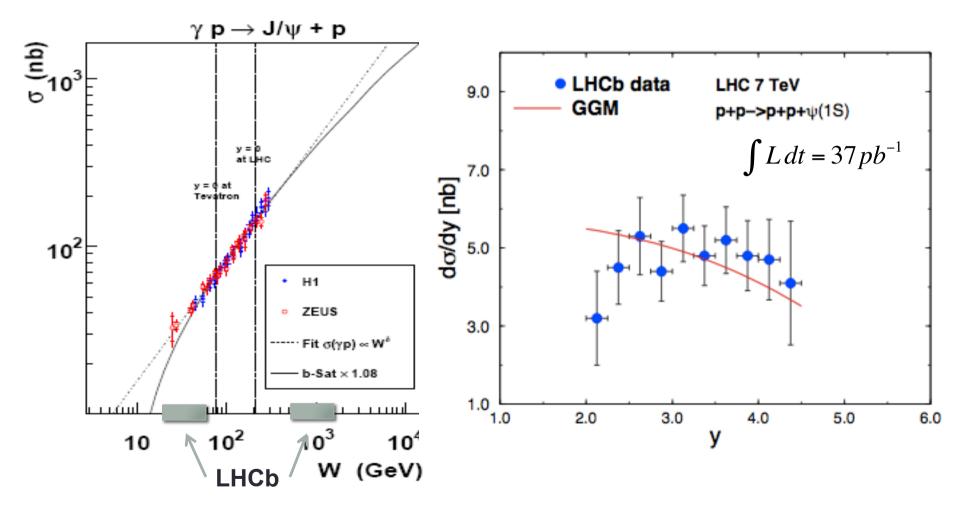
HERA measured power-law:  $\sigma_{\gamma p \to J/\psi p}(W) = 81(W/90 \, \text{GeV})^{0.67} \, \text{nb}$ Use this for one cross-section on RHS – LHCb measure the other solution



Deviation from pure power-law. i.e. NLO required or only power-law for W>W<sub>0</sub>



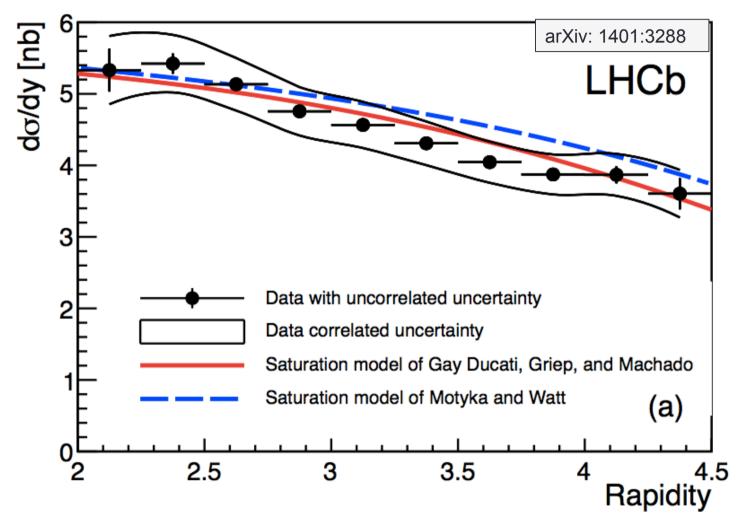
### Sensitivity to saturation effects



Motyka, Watt: PRD 78, 014023 (2008)

Gay Ducati et al., arXiv: 1305.4611

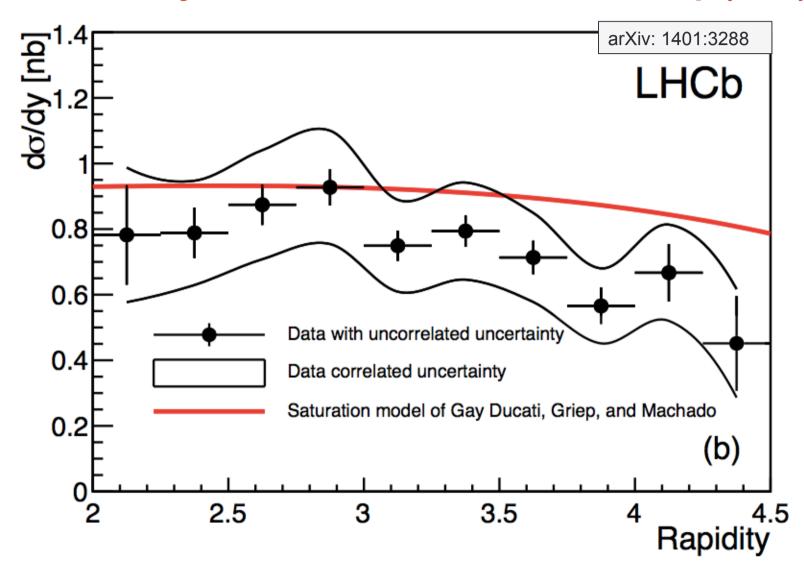
### Sensitivity to saturation effects: J/ψ



L. Motyka and G. Watt, Exclusive photoproduction at the Fermilab Tevatron and CERN LHC within the dipole picture, Phys. Rev. D78 (2008) 014023, arXiv:0805.2113.

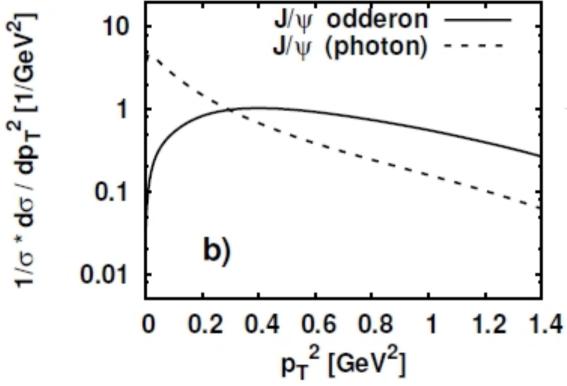
M. B. Gay Ducati, M. T. Griep, and M. V. T. Machado, Exclusive photoproduction of  $J/\psi$  and  $\psi(2S)$  states in proton-proton collisions at the CERN LHC, arXiv:1305.4611.

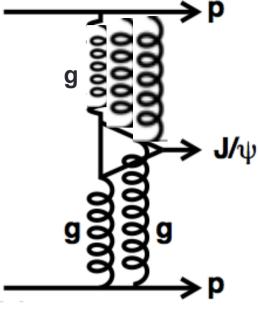
# Sensitivity to saturation effects: ψ(2S)



### Search for odderon

Motyka, DIS 2008.





#### **Detector Improvements**

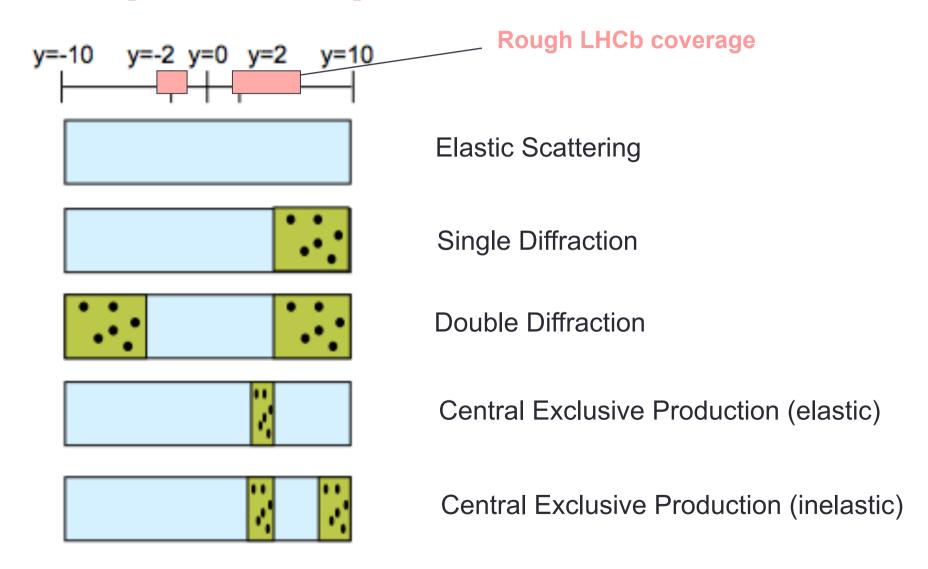
#### What we have learnt from the past:

Inelastic background limits measurement and search for new phenomena

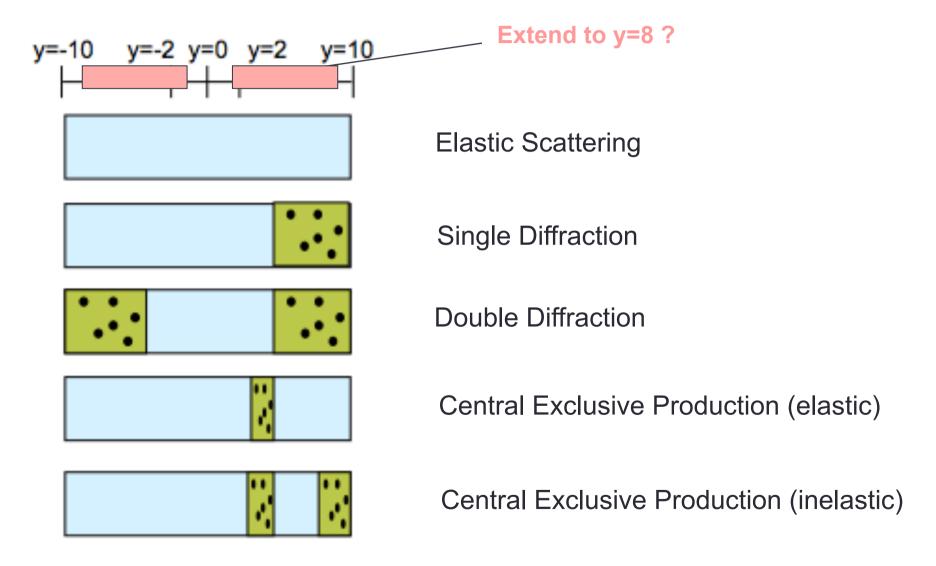
#### How we can improve for future:

Extend rapidity gap: currently ~ 5 units; future ~12 units?

## **Graphical Representation**



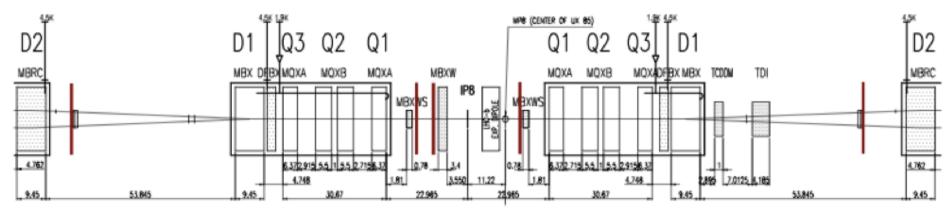
## **Graphical Representation**



#### High rapidity shower counters for LHCb

- Increase rapidity gap with scintillators in forward region
- Use existing electronics

LHC-b



#### Left

- 1. z ~ -7.5 m (after MBXW)
- 2.  $z \sim -19m$  (before MBXWS)
- 3.  $z \sim -114m$  (after BRANS)

#### Right

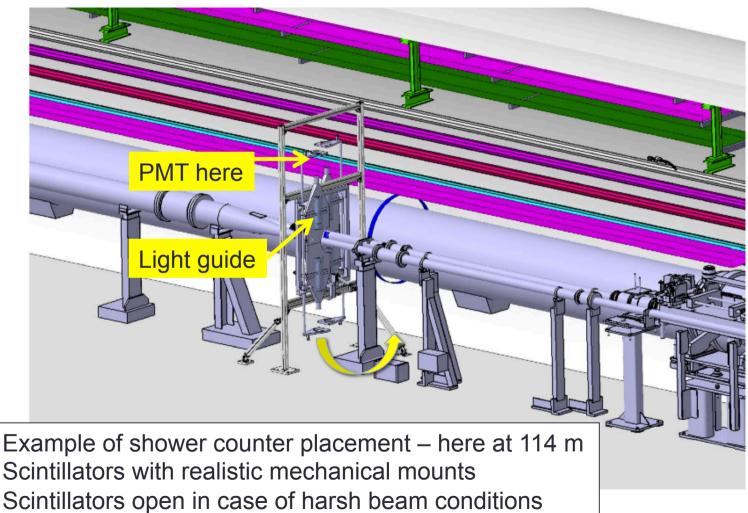
- 1.  $z \sim 19$  m (close to MBXWS)
- 2. z ~ 114m (after BRANS)

First simulations suggest veto region for charged and neutral particles can be extended to include  $5<|\eta|<8$ 

# Herschel Integration inside Tunnel

Implantation LHCb shower counter

C4R8 114m /IP 8



#### Summary LHCb contributions for yellow report

Yellow report contributions will have contributions from LHCb; contact persons Dima (<a href="mailto:Dmytro.Volyanskyy@cern.ch">Dmytro.Volyanskyy@cern.ch</a>), Victor (<a href="mailto:Victor.Coco@cern.ch">Victor.Coco@cern.ch</a>), Katharina (<a href="mailto:kmueller@physik.uzh.ch">kmueller@physik.uzh.ch</a>), Ronan (<a href="mailto:Ronan.Mcnulty@cern.ch">Ronan.Mcnulty@cern.ch</a>), Paula (<a href="mailto:Paula.Collins@cern.ch">Paula.Collins@cern.ch</a>), Heinrich (Heinrich.Schindler@cern.ch) plus many more contributors.

We plan to produce contributions for the following aspects:

- Chapter 1: Simulation of conditions in tunnel
  - For scintillator tagging of proton disassociation background for running after LS2, for CEP, possibly jets, and single diffractive physics (Paula)
  - Possible proton tagging in LS3 running
- Chapter 2: MC performance in the forward region (Dima, Victor)
- Chapter 3: Prospects for soft diffractive production studies with LHCb (Dima)
- Chapter 4: Prospects for diffractive electroweak boson production studies (Katharina)
- Chapter 5: Results and Prospects for central exclusive production (Ronan, Paula)
- Chapter 6: Results and prospects for Drell-Yan studies (Katharina)
- Results and prospects for inclusive jet studies (Victor)
- Chapter 7: Results and prospects for charged particle multiplicities and forward energy flow (Dima)
- Chapter 8: Results and prospects for pA studies (Heinrich)
- Chapter 9: HERSCHEL: High rapidity shower counters (Paula)

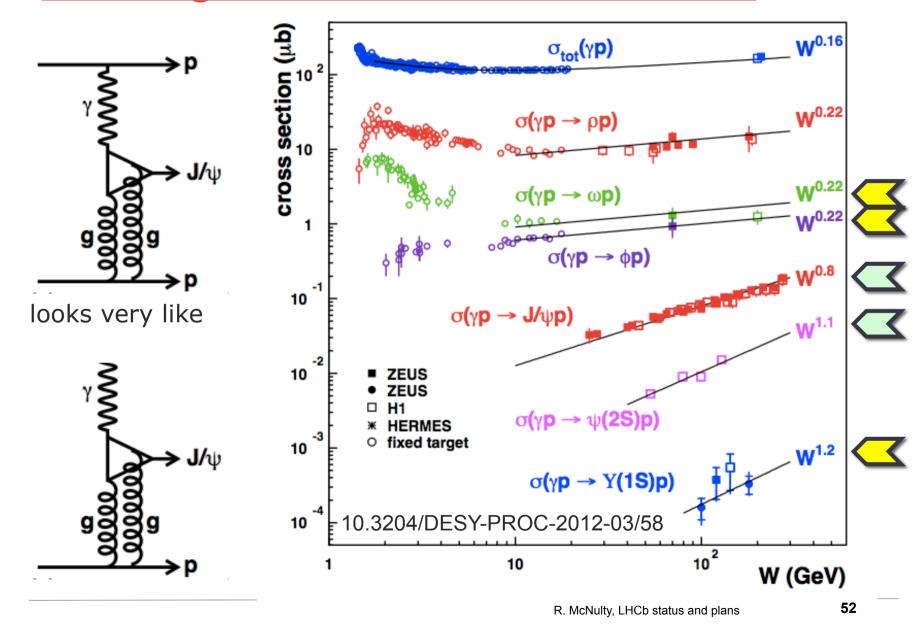
# Chapter 5: CEP Future physics measurements

CEP of vector mesons in leptonic modes

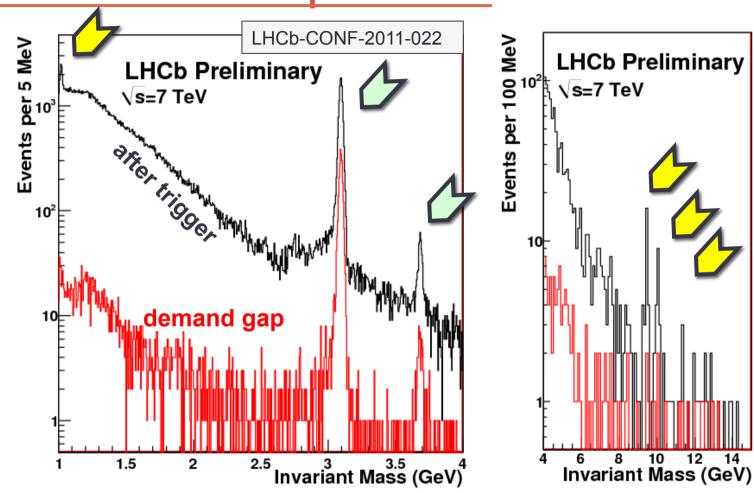
CEP of mesons in hadronic modes

CEP of pairs of mesons

### Investigate other vector mesons



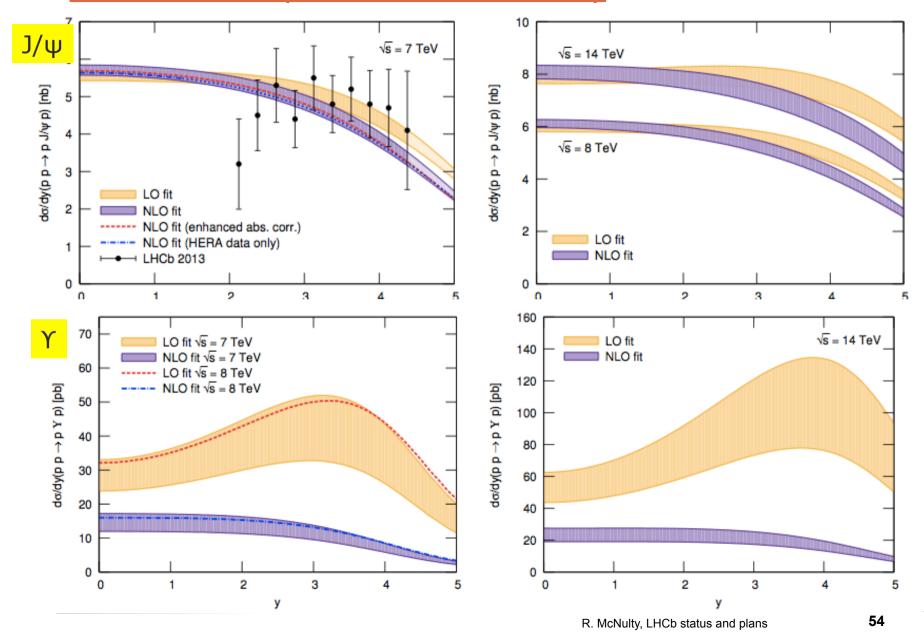
#### Dimuon Mass Spectrum



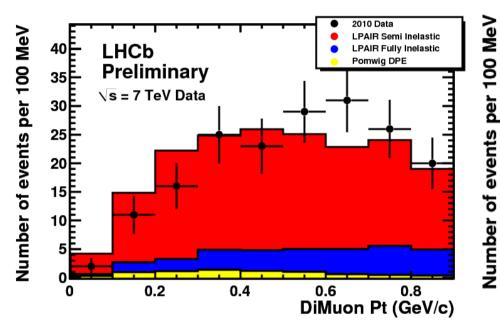
Factor ~ \*100 data now available with 2011+2012 (~3fb<sup>-1</sup>)

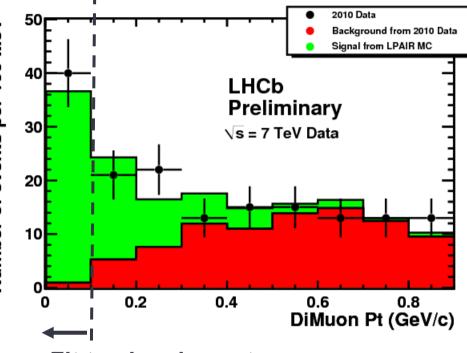
#### Predictions (arXiv: 1307.7099)

(Jones, Martin, Ryskin, Teubner)



# QED: pp->pµµp di-photon fusion





#### **Shape for inelastic events**

Note: this time we have simulation that predicts the shape for the three contributions.

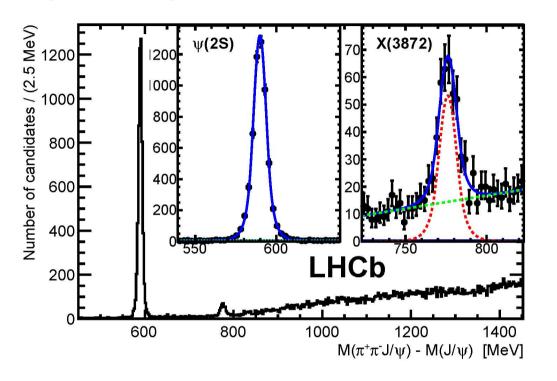
Fit to signal events

Background shape from data Signal shape from simulation.

Measured cross-section pμμp: 67 +- 19 pb

LPAIR (J. Vermaseren) 42 pb

# X(3872)



X(3872) observed inclusively. (arXiv:1112.5310) Could it be produced exclusively?

- JPC of X(3872) shown by LHCb to be 1++ (arXiv:1302.6269)
- χ<sub>c(1++)</sub> has been observed `exclusively' ?
- If X(3872) is a bound cc state, might expect to observe it in central exclusive production

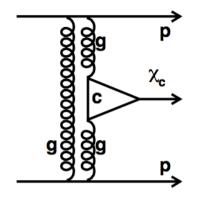
#### <u>x<sub>c</sub> meson</u>

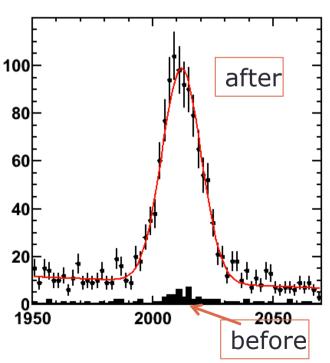
- Observation in J/ψ+γ suffers
  - Large proton-dissociation background
  - Poor resolution to distinguish  $\chi_{c0} \chi_{c1} \chi_{c2}$



- $\chi_{c0}$ -> $\pi\pi$  / KK ~1% while  $\chi_{c2}$ -> $\pi\pi$  / KK ~0.1%
- Backgrounds ok? (arXiv: 1105.1626)
- New low pt trigger for 2012 to access hadronic modes

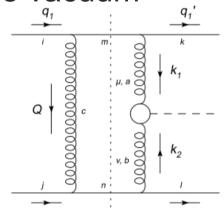
Example of D\*-> $K\pi\pi$  reconstruction in low multiplicity events



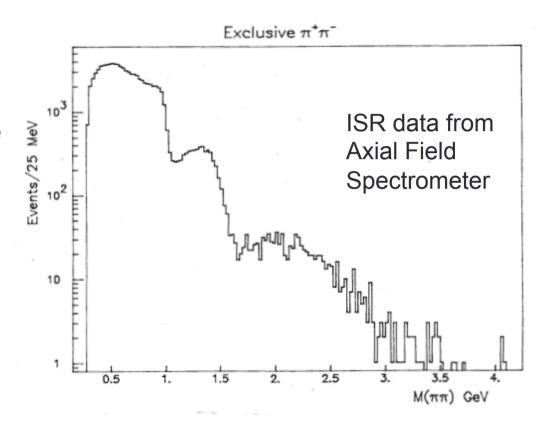


## Low mass spectroscopy + glueballs

- Data from ISR/Tevatron
- Accessible at LHCb
- DPE, probing the nature of the vacuum



Glue laboratory

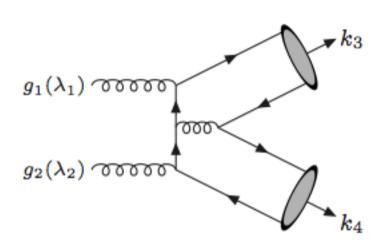


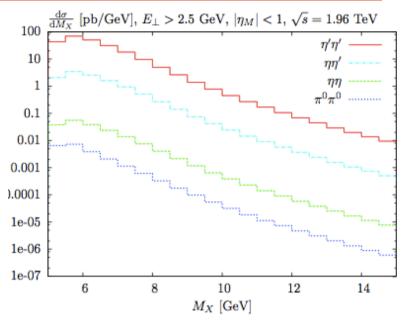
M.G. Albrow, T.D. Coughlin, and J.R. Forshaw, Prog. Part. Nucl. Phys. 65, 149 (2010). arXiv: 1006.1289

[101] T. Akesson, et al., A search for glueballs and a study of double pomeron exchange at the CERN Intersecting Storage Rings, Nucl. Phys. B264 (1986) 154.

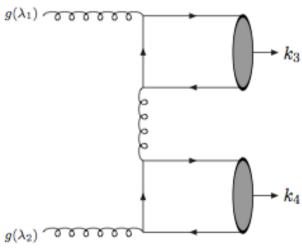
(Harland-Lang, Khoze, Ryskin, Stirling)

#### CEP meson-meson production arXiv:1105.1626





- Vanishing cs when gluons in  $J_z=0$
- Flavour non-singlet mesons suppressed (thus ππ/KK small)
- Flavour singlet (e.g. η'η' production)
   can proceed via



#### Some approximate yields for Yellow Report

Assume 6fb<sup>-1</sup> at 13 TeV with  $<\mu>=1$ 

Note: LHCb can use 40-100% of this luminosity, depending on whether crossings with single or few interactions are used.

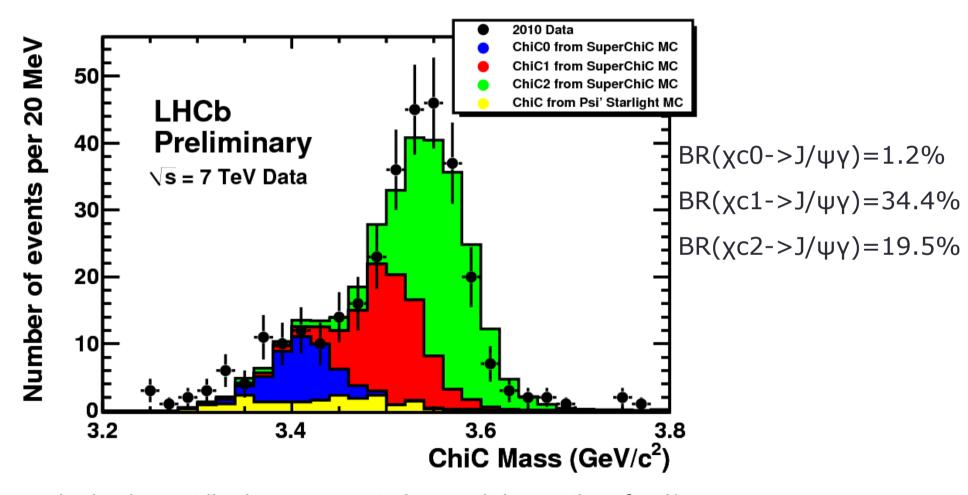
J/Ψ	2,500,000
Ψ(2S)	37,500
Y(1S)	2,000
Y(2S)	1,000
Y(3S)	500
рр->рµµр	20,000
$\chi_{c0}$ ->J/ $\Psi\gamma$	20,000
χ <sub>c0</sub> ->ππ	80,000
$\chi_{c0}$ ->KK	40,000
η'η'->(ππγγ)(ππγγ)	10000

#### **Conclusions**

- Two published measurements in CEP
- Several more in the pipeline
- Improvements to rapidity gap identification critical
- Yellow Report to include CEP + much more physics that will be discussed at Trento workshop.

# Backup

## X<sub>c</sub>: DiMuon+Photon Invariant Mass



Inelastic contribution appears to be much larger than for  $J/\psi$ . In a first approximation it should be square of bkg in  $J/\psi$  process.

## Theory v experiment

$$\sigma_{\chi_{c0-}\mu+\mu-\gamma} = 9.3 +/- 2.2 +/- 3.5 +/- 1.8 \text{ pb}$$
  
 $\sigma_{\chi_{c1-}\mu+\mu-\gamma} = 16.4 +/- 5.3 +/- 5.8 +/- 3.2 \text{ pb}$   
 $\sigma_{\chi_{c2-}\mu+\mu-\gamma} = 28.0 +/- 5.4 +/- 9.7 +/- 5.4 \text{ pb}$ 

LHCb preliminary results with 2010 data

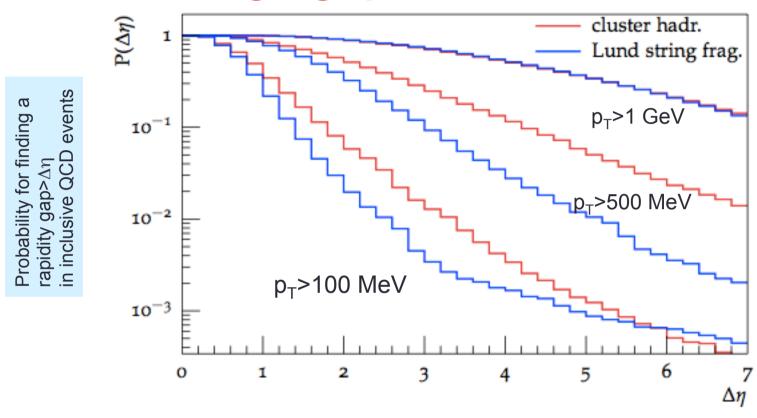
```
\chi_0: 9.3 +- 4.5 pb \chi_1: 16.4 +- 7.1 pb \chi_2: 28.0 +-12.3 pb
```

SuperChic: 14 pb 10 pb 3 pb

Large contribution due to  $X_{c0}$  is confirmed.

 $\chi_{c2}$  larger than expected but note that non-elastic background has been assumed same for each resonance. More precise data required.

#### What's a large gap?



- Khoze, Kraus, Martin, Ryskin, Zapp, "Diffraction and correlations at the LHC: definitions and observables", arXiv:1005.4839v2
- Probability for inclusively produced J/ $\psi$  to give two muons and nothing else inside LHCb is < ~10<sup>-5</sup>