## **Higher Order Generators: Which One Where?**

"Status, new developments, (some) issues and dusty corners of present higher-order Monte Carlo generators"





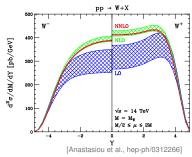
Simone Alioli LBNL & UC Berkeley

28 January 2014

**US ATLAS Workshop on LHC Searches** 

## What are higher-order generators?

- NLO is the first order at which rates and associated theoretical uncertainties are reliably predicted.
- NLO and NNLO gives non-negligible contributions in several cases (e.g.  $gg \rightarrow H \approx 100\%$  at NLO and  $\approx 30\%$  at NNLO).
- Theoretical uncertainties further reduced by including NLO and NNLO corrections.

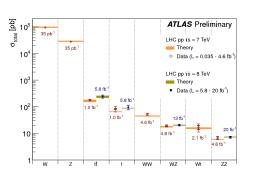


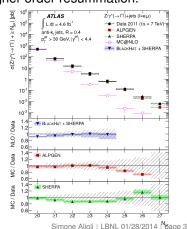
- ► Shapes are generically better described increasing the parton multiplicity: new channels at NLO, and NNLO, larger *K*-factors and noticeable shape distorsions.
- Fixed-order results are only at the parton level. No immediate way to estimate detector effects. Singular regions are poorly described.
- Resummation improve sing. region but requires to define the observable in advance, no fully-exclusive events.
- Higher-order generators are tools that aim to incorporate all these effects in a consistent way. Examples:

MC@NLO, POWHEG, SHERPA, Geneva, Herwig++, Vincia ...

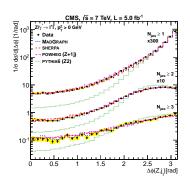


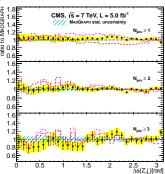
- It strongly depends on the obervable under study!
- ▶ Multijet shapes are usually ok with CKKW/MLM. Large scale uncertainties.
- Normalizations are given better in NLO+PS, but spectrum is still LO only. If normalized, one looses the need for NLO.
- For studying pure shower effects, just use a standard SMC
- ▶ In many cases what we really want is higher order resummation.



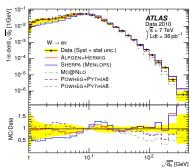


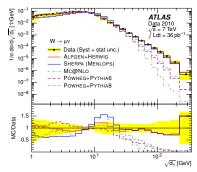
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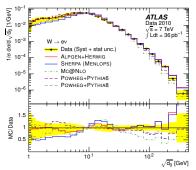
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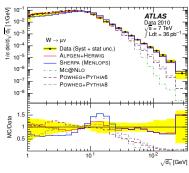




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Lesson: always keep in mind limit of validity of each MC



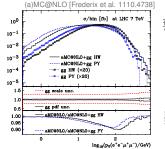
## **Estimating theoretical uncertainties**

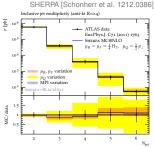
- Monte Carlo event distributions are theoretical predictions!
- They should always be accompanied by theoretical uncertainties. If not, demand for them!
- Typical procedure for accuracy of generator = accuracy of the observable, e.g. NLO
  - Independent  $\mu_R, \mu_F$  variations.
  - PDF error set envelope (PDF4LHC recommendation?)
  - Matching to a different parton shower(Herwig vs. Pythia), MPI on/off
  - Caveat: The shower only preserves the total probability. After acceptance cuts, rates and distributions can change drastically.

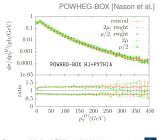


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- Machinery do exist for fast reweighting in many MC. Make use of them!









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- For process which are already divergent at LO, explicit independence on generation cuts/suppression factors must be enforced. This is not a theoretical unc.
- ► For observables that don't have NLO accuracy, showers effect are more marked. Different shower starting scales within the same generator can give very different results.



## Recent developments and new directions

- POWHEG and MC@NLO methods are by now well established methods for NLO+PS.
- Several implementations by different groups available

POWHEG-BOX, (a)MC@NLO, SHERPA, Herwig++, POWHEL, ...

Where to move from here? Three main directions:

Merge NLO samples with different jet multiplicities. Increase the fixed-order accuracy beyond NLO. Improve the resummation accuracy beyond (N)LL of parton showers.



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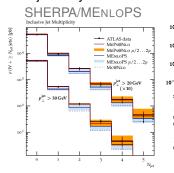
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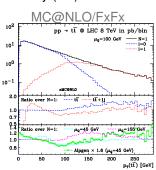


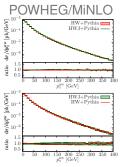
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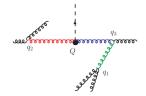




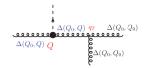




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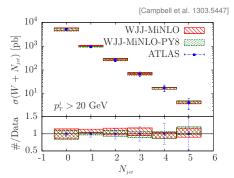
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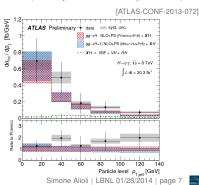
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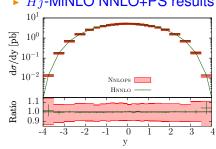
### POWHEG/MiNLO as a path to NNLO+PS.

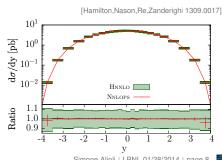
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- Integrates back to NNLO cross-section by construction
- NLO accuracy of Hj is maintained. Corrections start at  $\mathcal{O}(\alpha_a^5)$ .
- Need to reweight after generation, for each independent LO variable







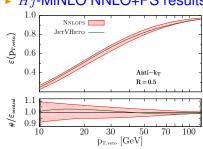
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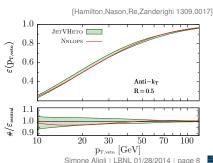
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Is this the only way to NNLO+PS?

See Christian's talk next ....



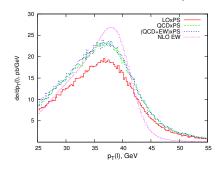
## Interplay between NLO QCD and NLO QED corrections

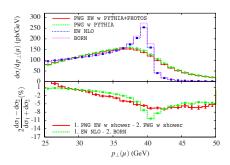
- First examples in single vector boson production
- ▶ Two separate implementations for  $W^{\pm}$ :

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- NLO QCD + NLO EW, only 1st QCD emission by POWHEG. Interfaced to QCD parton shower (PYTHIA / HERWIG). No photon-induced nor multiple photon radiation.
- Simultaneous NLO QCD and QED correction on first emission by POWHEG, interfaced to QCD (PYTHIA) and QED (PHOTOS) parton showers.
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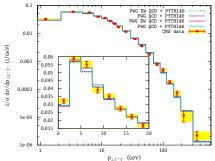
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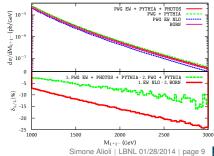
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- ► Simultaneous NLO QCD and QED also available for DY [Barzé et al., arXiv:1302.4606]



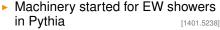




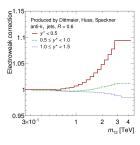
### EW Sudakov logs and weak emissions in PS

- ▶ EW logs don't cancel as QCD, partonic processes are not EW singlets
- ► Sizeable effects at LHC

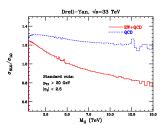


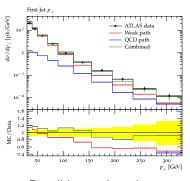


Interleaved QCD-EW evolution, matched to QCD and EW ME, better agreement with data



► Huge at future colliders [1308.1430]

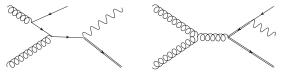




Possible to take advantage of this for EW-improved ME merging?

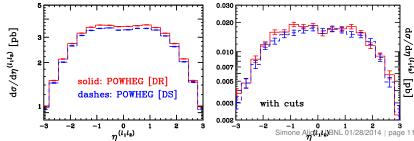
# Interference issues in the SM: single top $\mathit{Wt}$ -channel

- ▶ In general, LO QCD + NLO EW must be treated as LO EW + NLO QCD
- ▶ In the SM, a prime example is  $gg o W^+b\bar{t}$  vs.  $gg o t\bar{t} o W^+b\bar{t}$  at NLO



- Contributions from doubly resonant seem to spoil perturbative convergence. • DR removes  $|\mathcal{M}_r|^2$  ( $\pm 2\mathcal{R}e\{\mathcal{M}_r \ \mathcal{M}^*_{nr}\}$ ). Not gauge invariant (but violations
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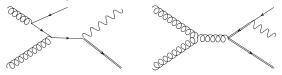
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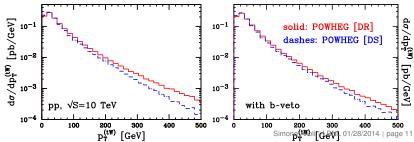


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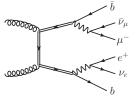
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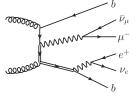


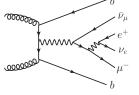


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- ► Complete  $pp \to e^+ \nu_e \mu^- \nu_\mu b \bar{b} + X$  at NLO in 4F scheme  $(m_b \neq 0)$



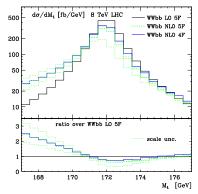


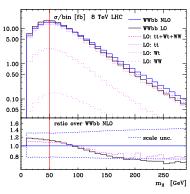


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- ▶ Includes SR,DR, and NR contributions, off-shell effects and interferences
- ▶ Results show moderate NLO corrections and scale unc. ( $\pm 20 30\%$ ).

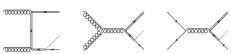




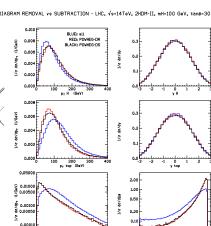
Extremely challenging calculation, NLO only for now. Shower Matching?

## Interference issues beyond the SM: $H^{\pm}t$

Same issue present in  $H^{\pm}t$  associate production with  $m_H^{\pm} < m_t$ 



- ► Implemented in both POWHEG and MC@NLO [Klasen et al. 1203.1341]
  - [Weydert et al. 0912.3430]
- ▶ DR vs. DS differences seems smaller in his case, compared to doubly resonant contributions



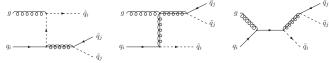
0.00005

# Interference issues beyond the SM: $\tilde{q}\tilde{q}$

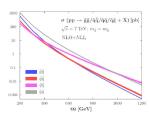
Same effect studied also in squark-squark production

[Gavin et al. 1305,4061]

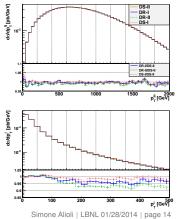
Interference with  $\tilde{q}\tilde{g}$  when gluino is resonant



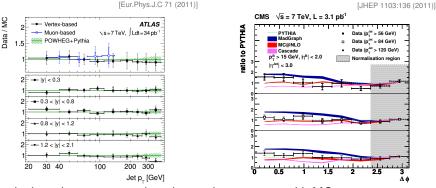
Dominant channel in the high mass region



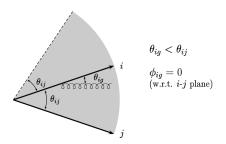
Inclusive effects small, again more pronounced in particular distributions



## Heavy quarks in the final state

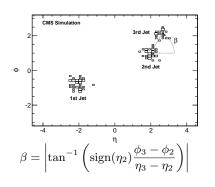


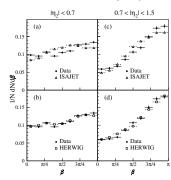
- Inclusive b-jets cross sections in good agreement with MC
- As the two b-jets become closer MC start to show disagreements. Disagreement grows with  $p_{\rm T}$ , where  $g \to b \bar b$  dominates.
- ► Use Heavy Quark Fragmenting Jet Functions for simultaneous resummation of jet resolution and quark mass logs [Bauer, Mereghetti 1312.5605]
- How to include these resummations into a fully exclusive Montecarlo? Geneva...



► At Tevatron collinear approx. + angular-ordering provided good modeling of color-coherence effects.

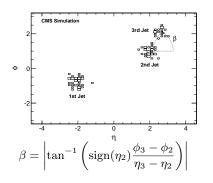
[D0 Phys. Lett. B 414 419 (1997)]

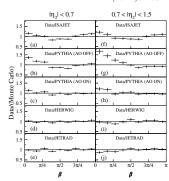




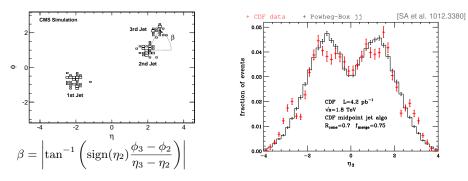
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- Shower Monte Carlo needed to take angular-ordering into account.

[D0 Phys. Lett. B 414 419 (1997)]



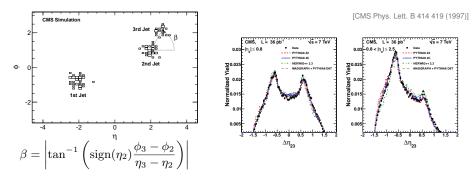


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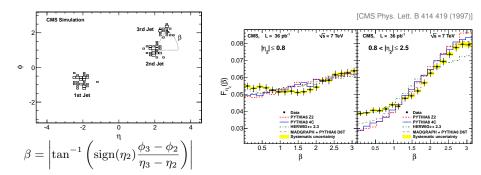


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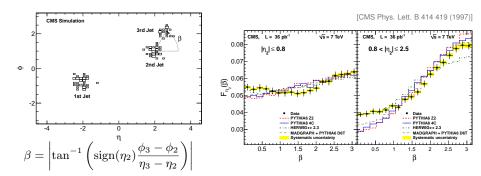


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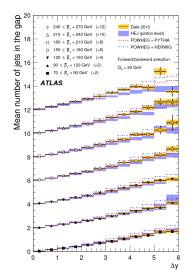


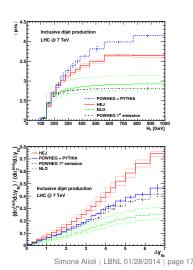


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- Shower Monte Carlo needed to take angular-ordering into account.
- At LHC, general features are still described fairly
- But larger coherence effects start to show up in angular correlation between 2nd and 3rd jet
- Can we learn something from 3-jets at NLO?

# Jets gap and BFKL dynamics

- ► Study of effects beyond NLO at large rapidity separations, comparison between POWHEG+SMC and HEJ [SA et al., 1202.1475]
- Indentified few other observables with larger difference in radiation patterns





#### **Conclusions and outlook**

- Monte Carlo's have been tested across a wide range of energies and phase spaces.
- In general, NLO SMC's are performing remarkably well to describe LHC data.
- When looking into extreme areas of phase space or in high multiplicity regions, we start seeing (expected) disagreements.
- ► NLO+PS automation is now mature and helpful for new analysises.
- Care must still be taken for selected processes: interference effects, new regimes, BSM physics . . .
- New developments and theoretical ideas are pushing MC forward in three main directions
  - Merge NLO sample with different NLO multiplicities.
  - Increase the fixed-order accuracy beyond NLO.
  - Increase the resummation accuracy beyond parton showers.
- Many other interesting subjects that have not been covered: MPI, soft-QCD, MC tunes . . .

# Thank you for your attention!

