

# Vector Boson Scattering: A Theory Perspective



**Higgs Couplings Workshop**

**Torino – October 2014**

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**University of Tübingen**

vector boson fusion (VBF) &  
vector boson scattering (VBS)

Standard Model:

- ❖ important production mode for the Higgs boson
- ❖ sensitive to Higgs couplings and CP properties

the big advantage:

- ✓ experimentally clean signature
- ✓ perturbatively well under control

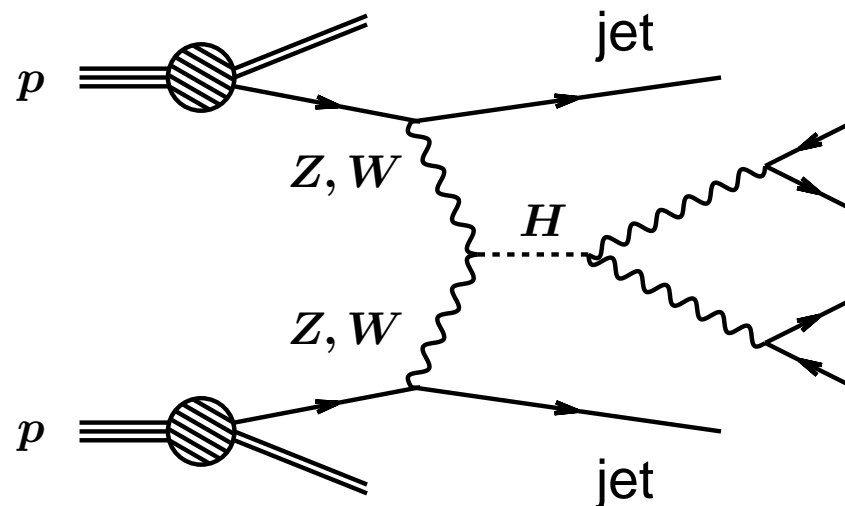
beyond the Standard Model:

sensitive to the mechanism of electroweak symmetry breaking



strongly interacting weak sector,  
new resonances, ... ?

# VBF / VBS event topology



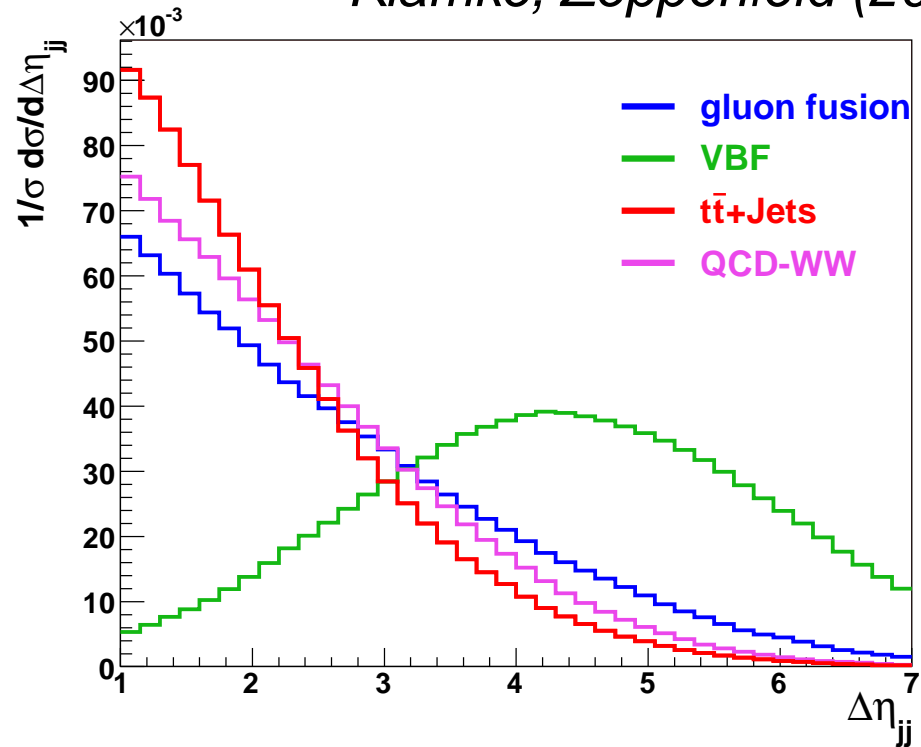
suppressed color exchange between quark lines gives rise to

- ❖ little jet activity in central rapidity region
- ❖ scattered quarks  $\rightarrow$  two forward tagging jets (energetic; large rapidity)
- ❖ decay products of the weak-boson system typically between tagging jets

# tagging jets: properties

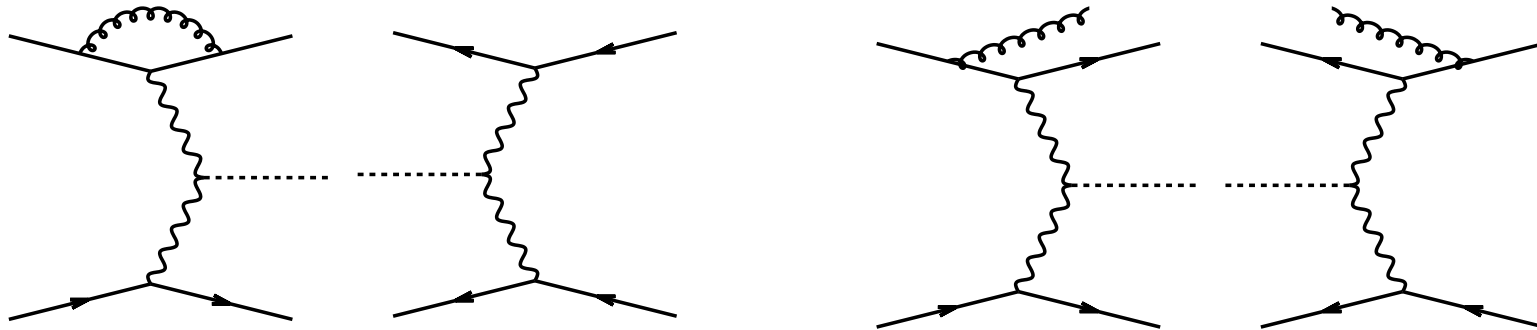
rapidity separation of the tagging jets

*Klämke, Zeppenfeld (2007)*



**jets more central** in QCD- than in EW-induced production processes

# Higgs production in VBF @ NLO QCD



NLO QCD:

inclusive cross section:

*Han, Valencia, Willenbrock (1992)*

distributions:

*Figy, Oleari, Zeppenfeld (2003)*

*Berger, Campbell (2004)*



**NLO QCD corrections  
moderate**

and well under control  
(order 10% or less)

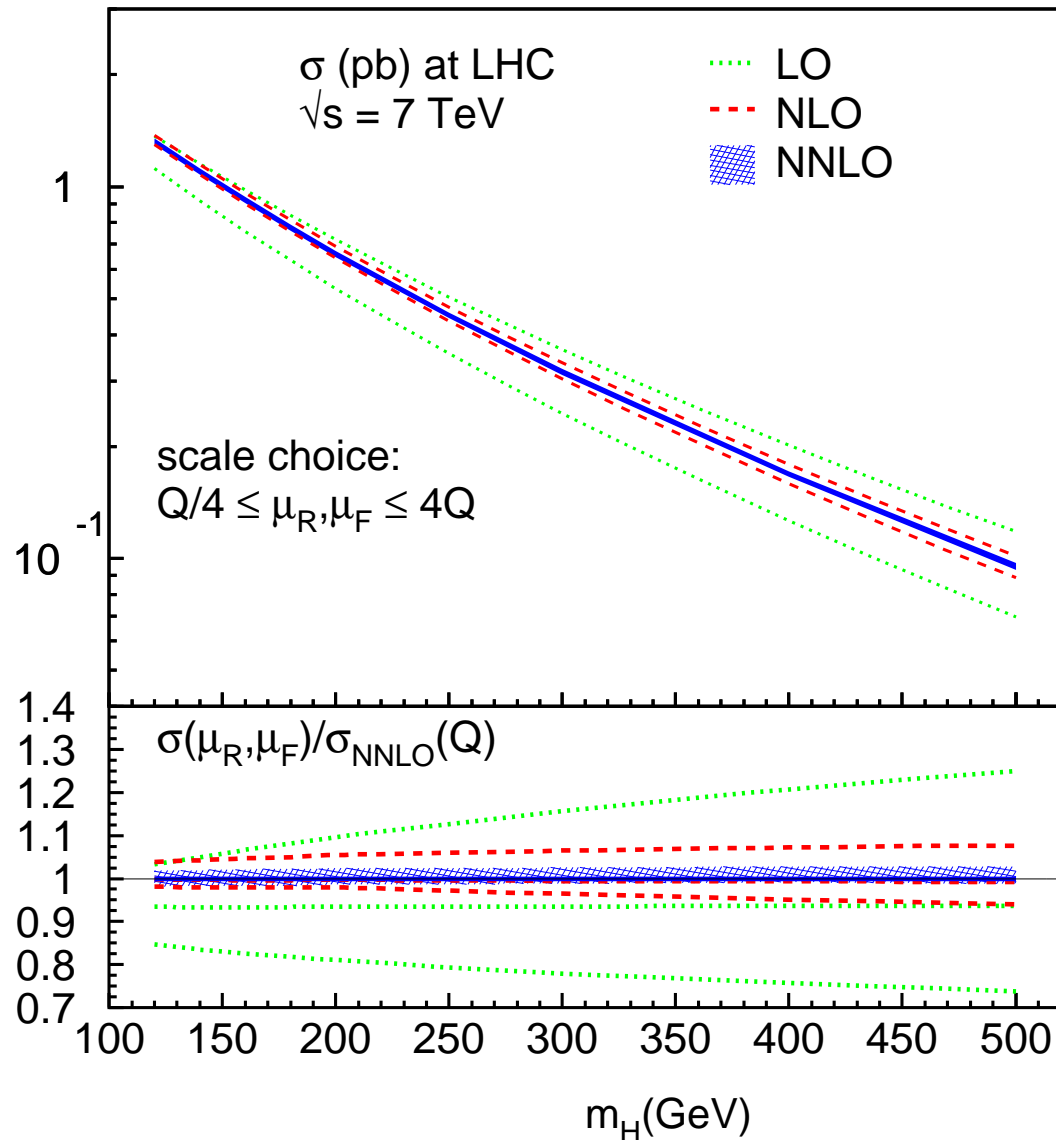
publicly available  
parton-level Monte Carlos:

VBFNLO

MCFM

# higher orders of QCD in VBF

*Bolzoni et al. (2011)*



partial NNLO-QCD results:

$gg \rightarrow q\bar{q}H$ :

*Harlander, Vollinga, Weber (2007)*

$qq \rightarrow qqH$ :

*Bolzoni, Maltoni, Moch, Zaro (2019)*

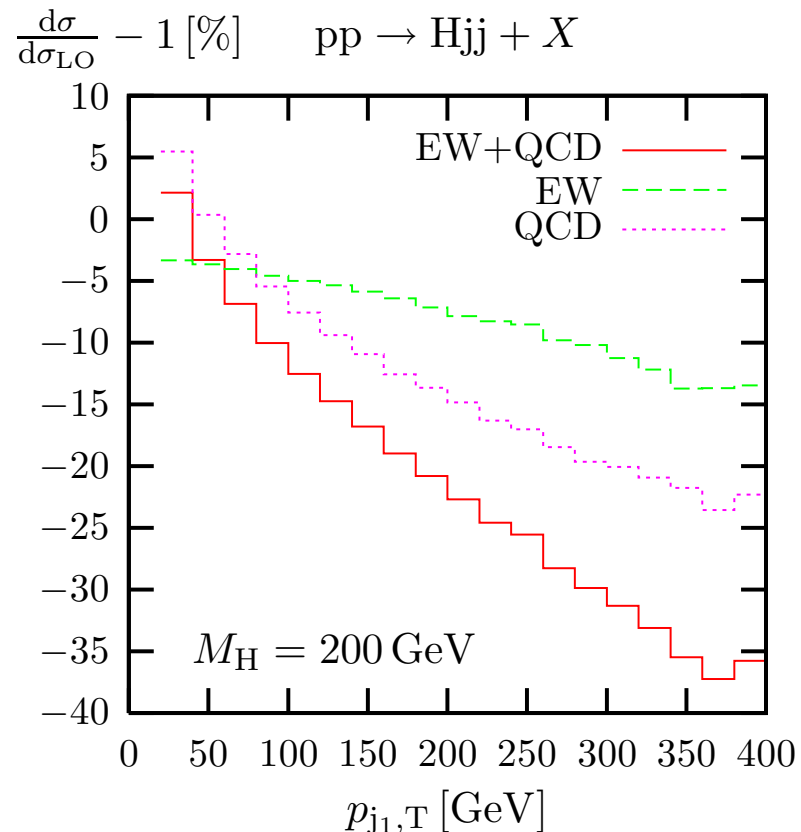
- ◆ NNLO predictions are in full agreement with NLO results
- ◆ residual scale uncertainties are reduced from  $\sim 4\%$  to  $2\%$
- ◆ NNLO PDF uncertainties are at the  $2\%$  level

# Higgs production in VBF @ NLO EW

*Ciccolini, Denner, Dittmaier (2007):*

NLO EW corrections to inclusive cross sections and distributions

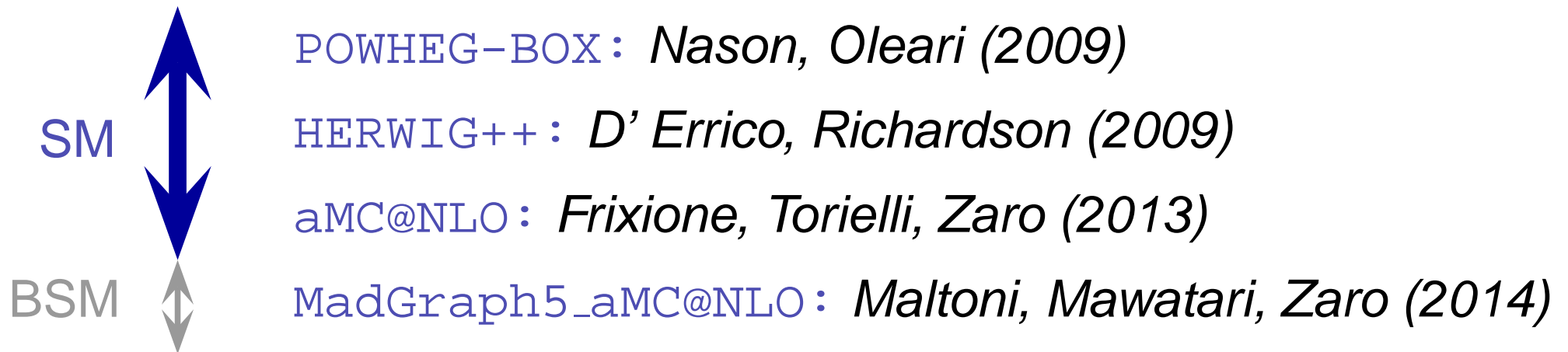
- 👉 **NLO EW corrections non-negligible**, modify  $K$  factors and distort distributions by up to 10%



publicly available  
parton-level Monte Carlo:  
HAWK  
*[Denner, Dittmaier, Mück]*

# $pp \rightarrow Hjj$ via VBF @ NLO QCD with parton shower

various implementations in different frameworks available:

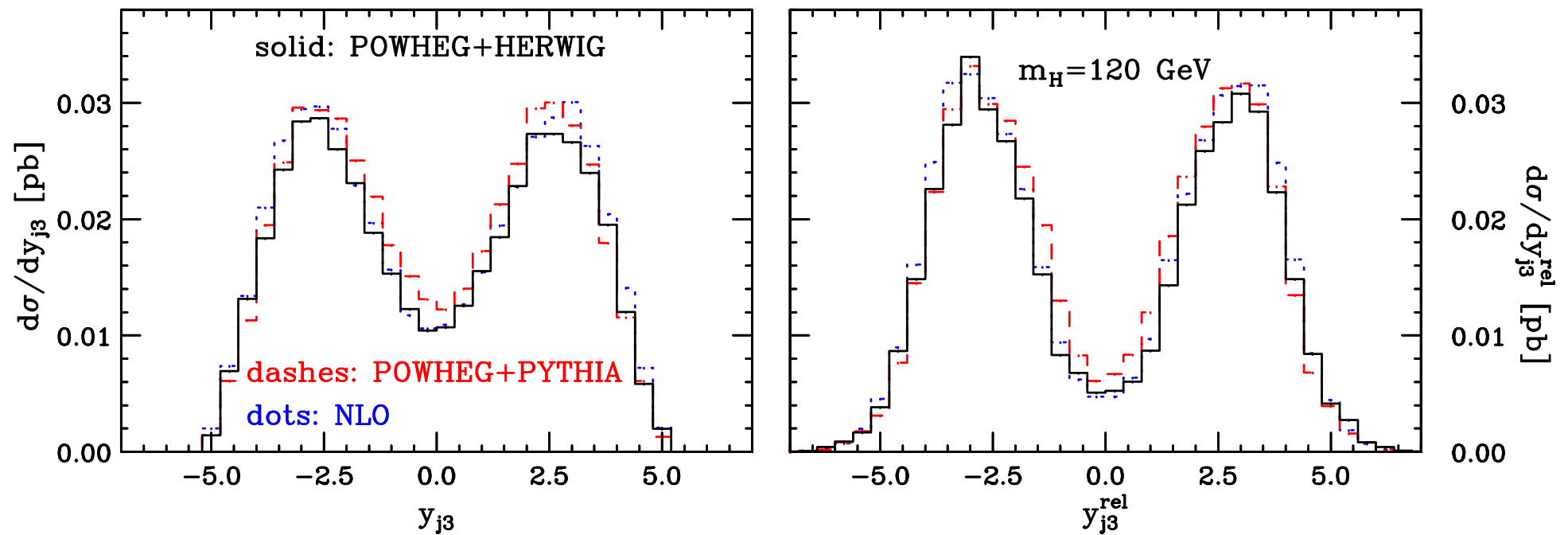


generally **parton shower does not significantly modify**  
distributions related to **tagging jets**



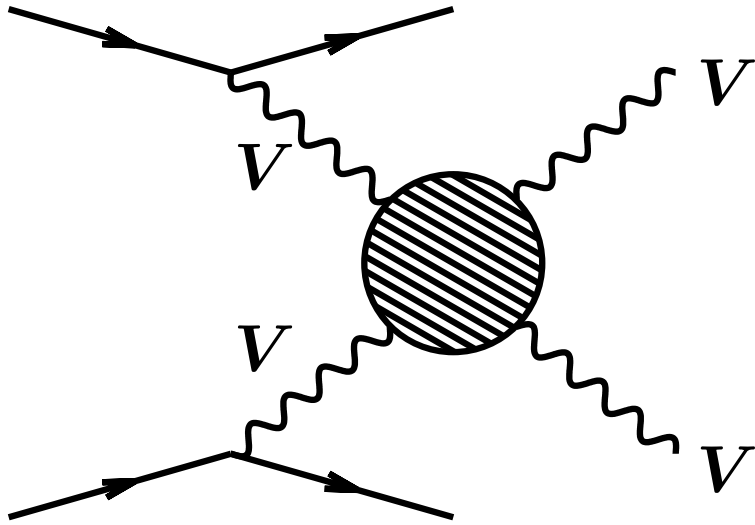
# $pp \rightarrow Hjj$ via VBF @ NLO QCD with parton shower

Nason, Oleari (2009)



distributions related to the **third jet** are more **sensitive to parton shower effects** and details of the **implementation**

# vector boson scattering: $VV \rightarrow VV$



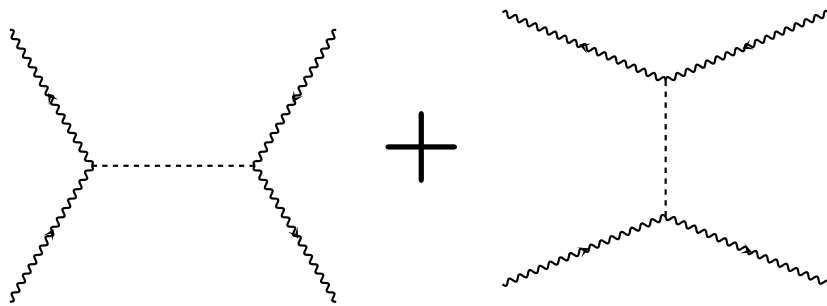
vector-boson scattering processes  
are extremely **sensitive to**  
**new interactions in the**  
**gauge boson sector**

# vector boson scattering & unitarity

$$W_L^+ W_L^- \rightarrow W_L^+ W_L^- \quad \text{with } \epsilon_L^\mu \sim \frac{\sqrt{s}}{M_W}$$

$$\mathcal{M} = \text{[s-channel diagram]} + \text{[t-channel diagram]} + \text{[u-channel diagram]} \sim \frac{s}{M_W^2}$$

growth violates unitarity  $\rightarrow$  need:



Higgs with  $M_H \lesssim 1$  TeV  
or new physics at TeV scale

# implications of unitarity in VBS

historic speculations:

❖ **heavy Higgs** boson?

challenging: in TeV range  $\Gamma_H \sim M_H$

❖ **no Higgs** boson?

- strong interactions of  $V_L$  modes?
- resonances in TeV range?
- spectacular signals ?

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- ❖ heavy Higgs bosons  
couplings in TeV range  $\Gamma_H \sim M_H$
- ❖ no Higgs boson
  - strong interactions of  $V_L$  modes?
  - resonances in TeV range?
  - spectacular signals ?

... OUTDATED!!

# approaches to VBS today

experimental fact:  $M_H = 125 \text{ GeV} \ll 1 \text{ TeV}$

➡ BSM effects expected to be small

- ❖ specific models with one or more Higgs boson(s)
- ❖ model-independent effective analysis

based on particle content of the SM:

$$\mathcal{L}_{\text{eff}} = \sum \frac{c_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)} = \mathcal{L}_{\text{SM}} + \sum \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$$

higher-dim operators may give rise to  
anomalous triple and quartic gauge couplings

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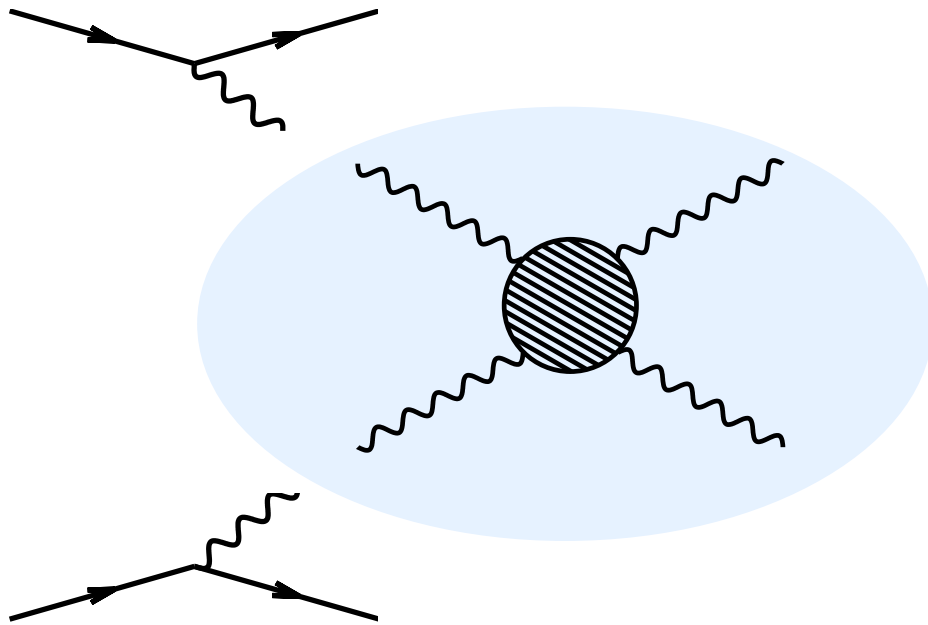
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precision in theory and experiment needed  
to identify small deviations from SM

# vector boson scattering in hadronic collisions



$$\sigma_{pp} \sim f_{V_1/p_1} \otimes f_{V_2/p_2} \otimes \hat{\sigma}_{V_1 V_2 \rightarrow V_3 V_4}$$

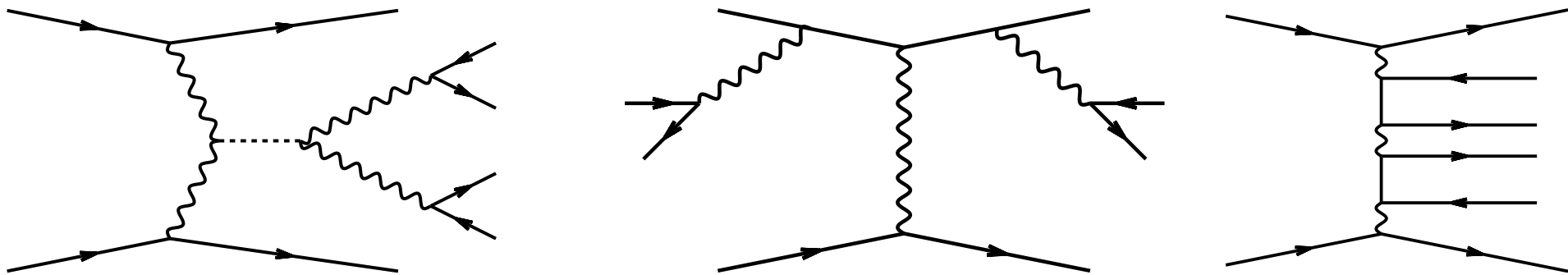
poor man's approach:

consider heavy gauge bosons as  
effective constituents of the proton

“effective  $V$  boson approximation”



# $pp \rightarrow VVjj$ : the full picture



note: effective  $V$  boson approximation expected to work only in high-energy domain, but

still **uncertainties of several 10%** at 3 TeV !

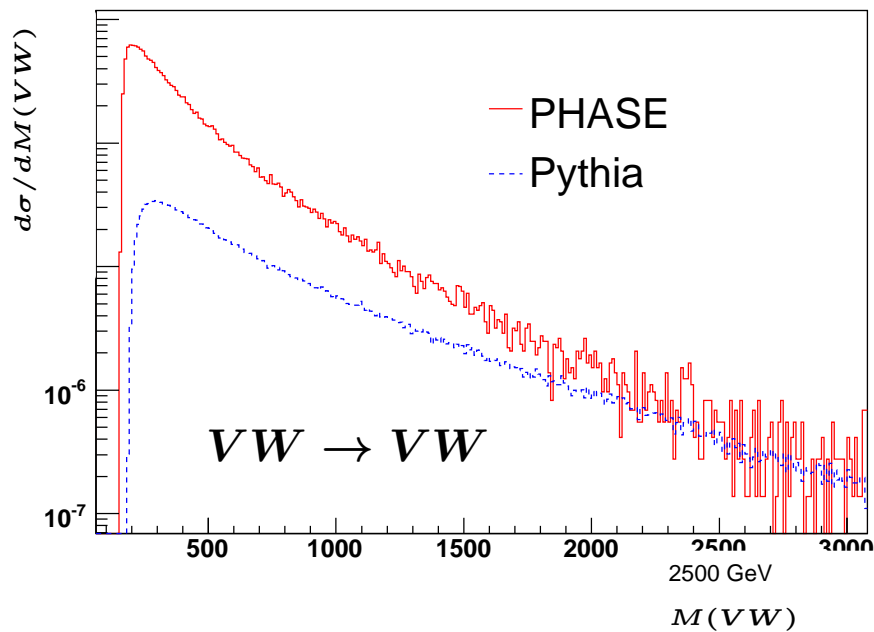
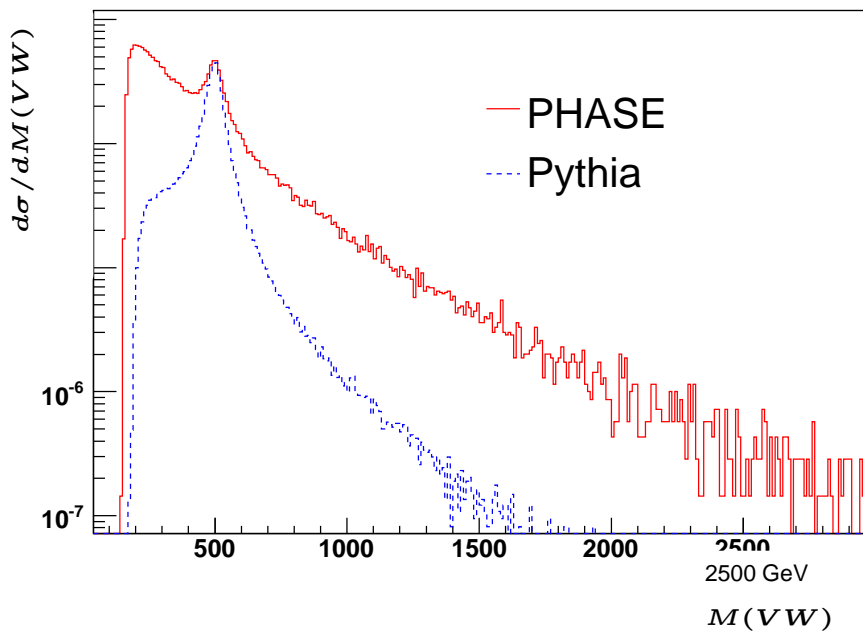
[ *Accomando, Denner, Pozzorini (2006)* ]

in **realistic calculation** need to consider:

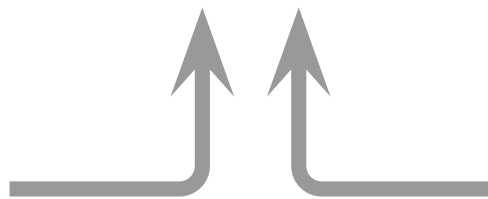
- ❖ non-resonant contributions
- ❖ off-shell effects

# first step: full $2 \rightarrow 6$ amplitudes

PHASE: LO event generator for six fermion physics at the LHC  
*Accomando, Ballestrero, Maina (2004)*



PHASE:  
off-shell effects fully  
considered



PYTHIA:  
EWA with longitudinal  
vector bosons

Accomando et al. (2005)

# EW $VVjj$ production at NLO-QCD

**NLO-QCD** calculation for VBF production of

$$pp \rightarrow W^+W^-jj, ZZjj, W^\pm Zjj, \text{ and } W^\pm W^\pm jj$$

(including off-shell effects and leptonic decay correlations)

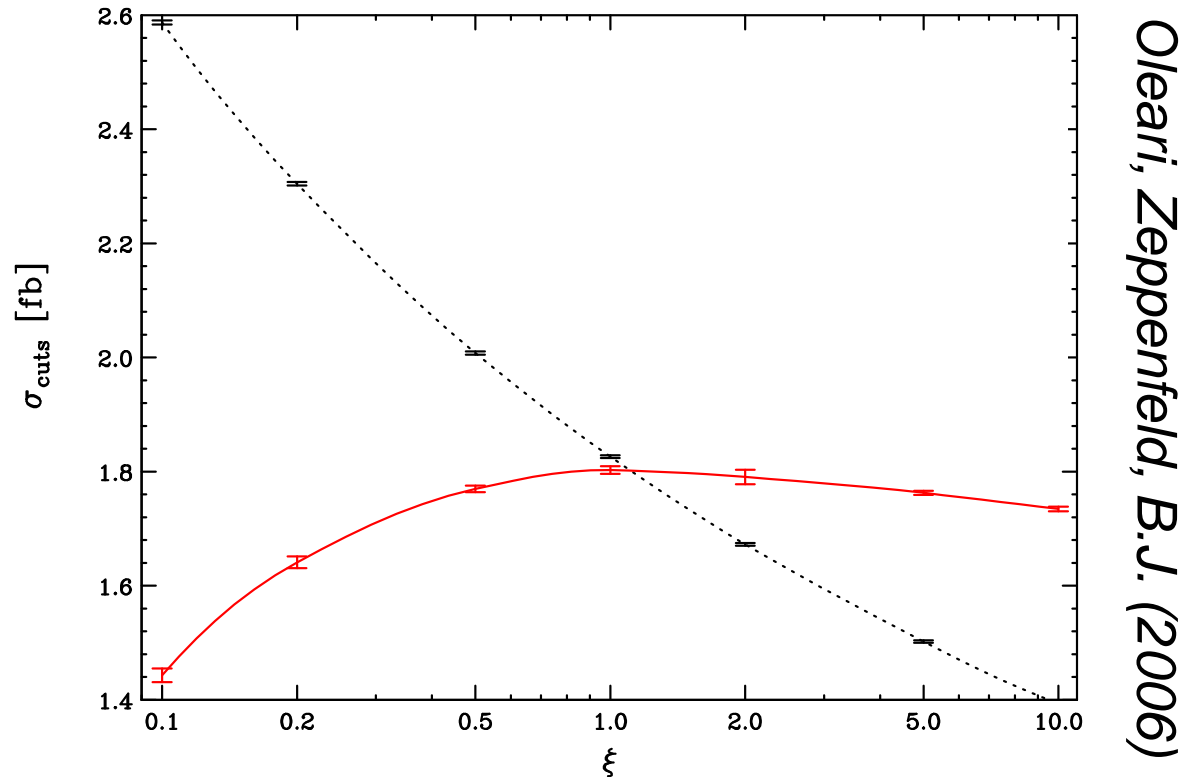
available in [VBFNLO](#) Monte Carlo program

*G. Bozzi, C. Oleari, D. Zeppenfeld, B. J. (2006-2009)*

*A. Denner, L. Hosekova, S. Kallweit (2012)*

# EW $W^+W^-jj$ production: theoretical uncertainty

estimate theoretical uncertainty by studying dependence of cross section on unphysical scale parameter  $\mu = \xi M_W$



LO: no control on scale

NLO QCD: scale dependence strongly reduced

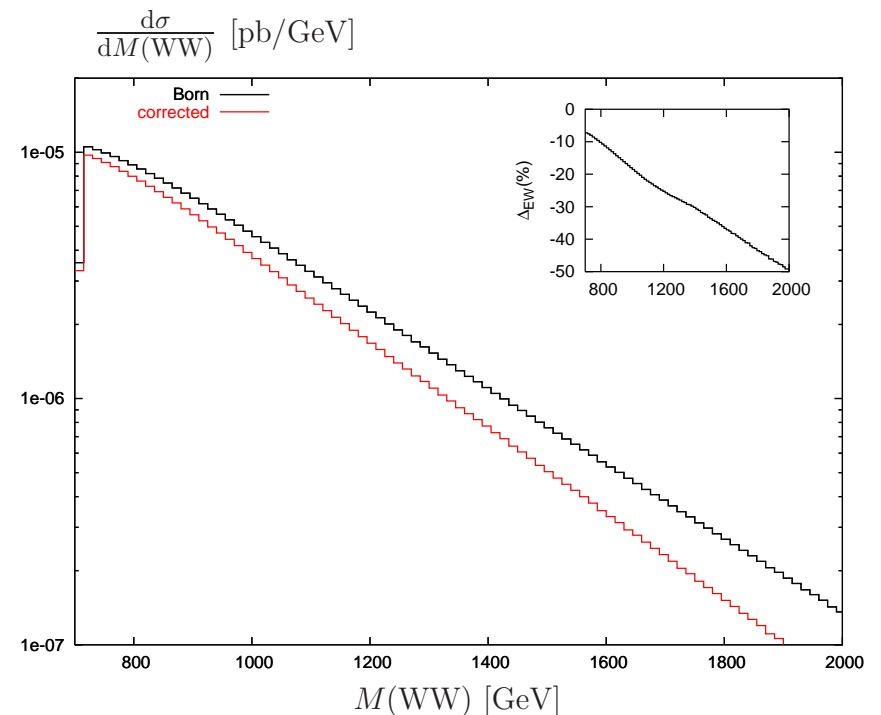
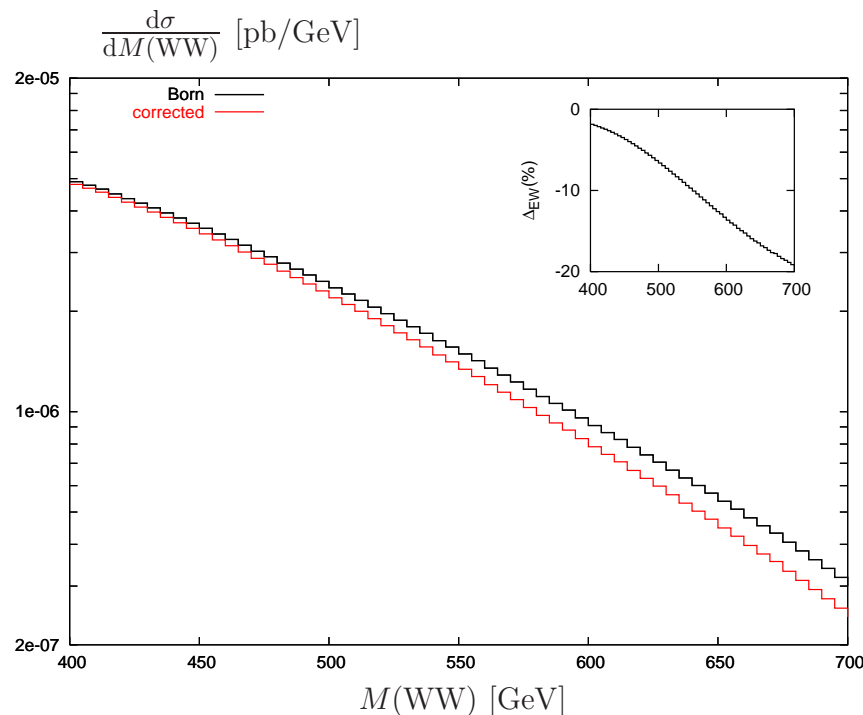
# $pp \rightarrow VVjj$ via VBF: electroweak corrections

very tough – no calculations available to date

related case of  $e^+e^- \rightarrow \nu_e\bar{\nu}_e W^+W^-$ :

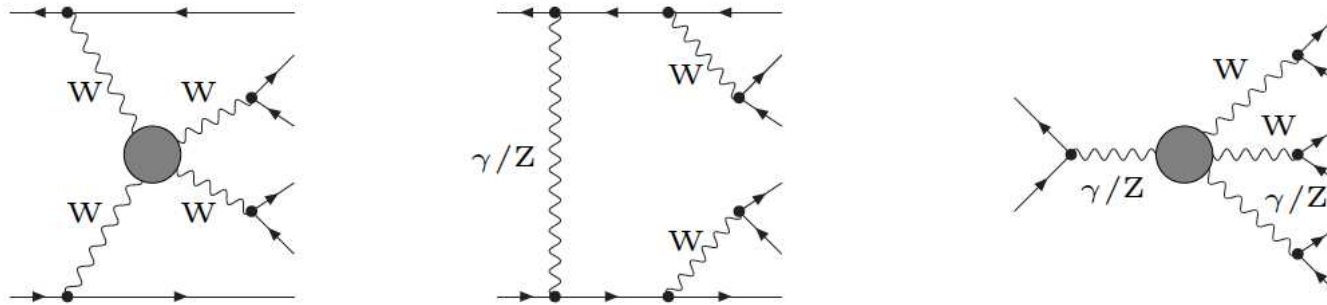
dominant EW corrections can be as **large** as 50% in TeV range

[Accomando, Denner, Pozzorini (2006) ]



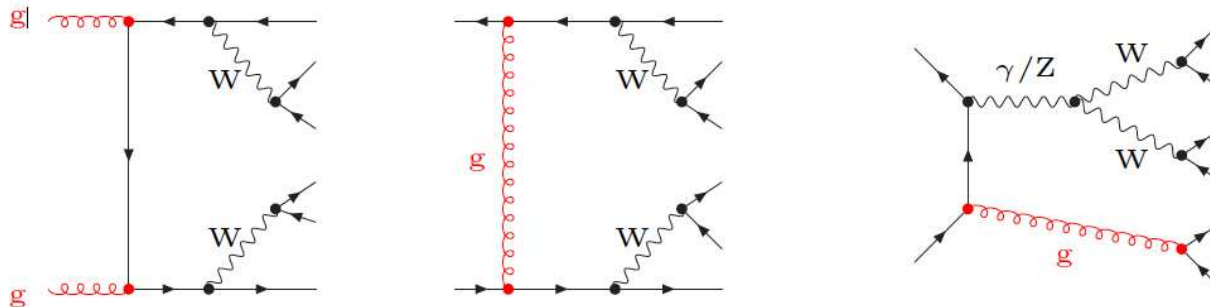
# the various contributions to the VVjj final state

EW channels:



$$|\mathcal{M}_{EW}|^2 \propto \alpha^6$$

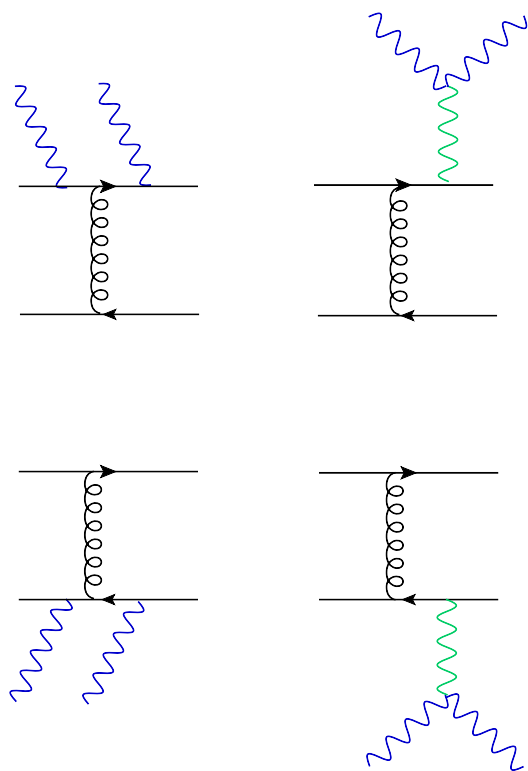
QCD channels:



$$|\mathcal{M}_{QCD}|^2 \propto \alpha_s^2 \alpha^4$$

interference between QCD and EW channels:  
possible, but suppressed

# QCD-induced $VVjj$ production



QCD-induced  $VVjj$  production  
constitutes irreducible background to  
EW  $VVjj$  production

NLO-QCD predictions available for

$W^+W^+jj$  (★),  $W^+W^-jj$  (\*),  
 $WZjj$  (◆),  $ZZjj$  (◆):

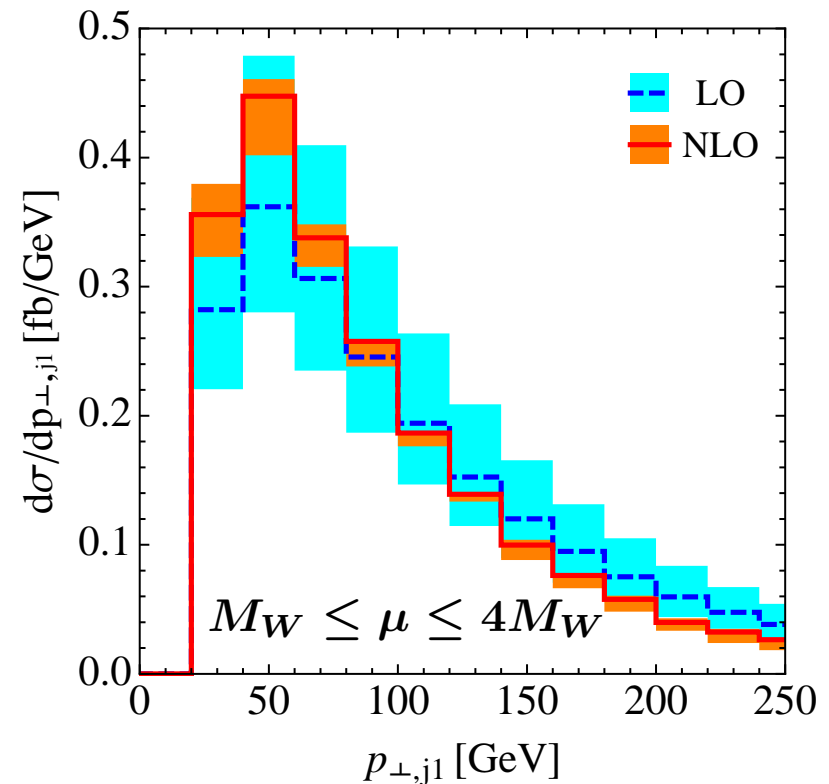
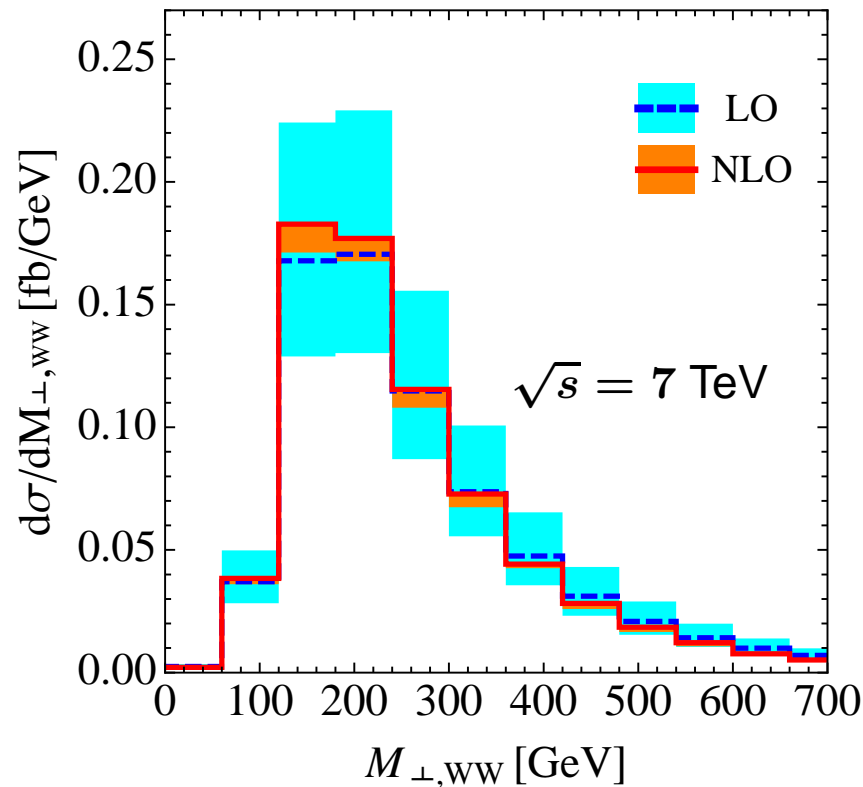
★, \* *Melia et al. (2010, 2011)*

\* *Greiner et al. (2012)*

◆ *Campanario et al. (2013,2014)*

# QCD-induced $W^+W^-jj$ production at NLO

*Melia, Melnikov, Rontsch, Zanderighi (2011)*



NLO-QCD corrections significantly reduce  
scale uncertainty



# $VVjj$ matched with parton showers & NLO-QCD

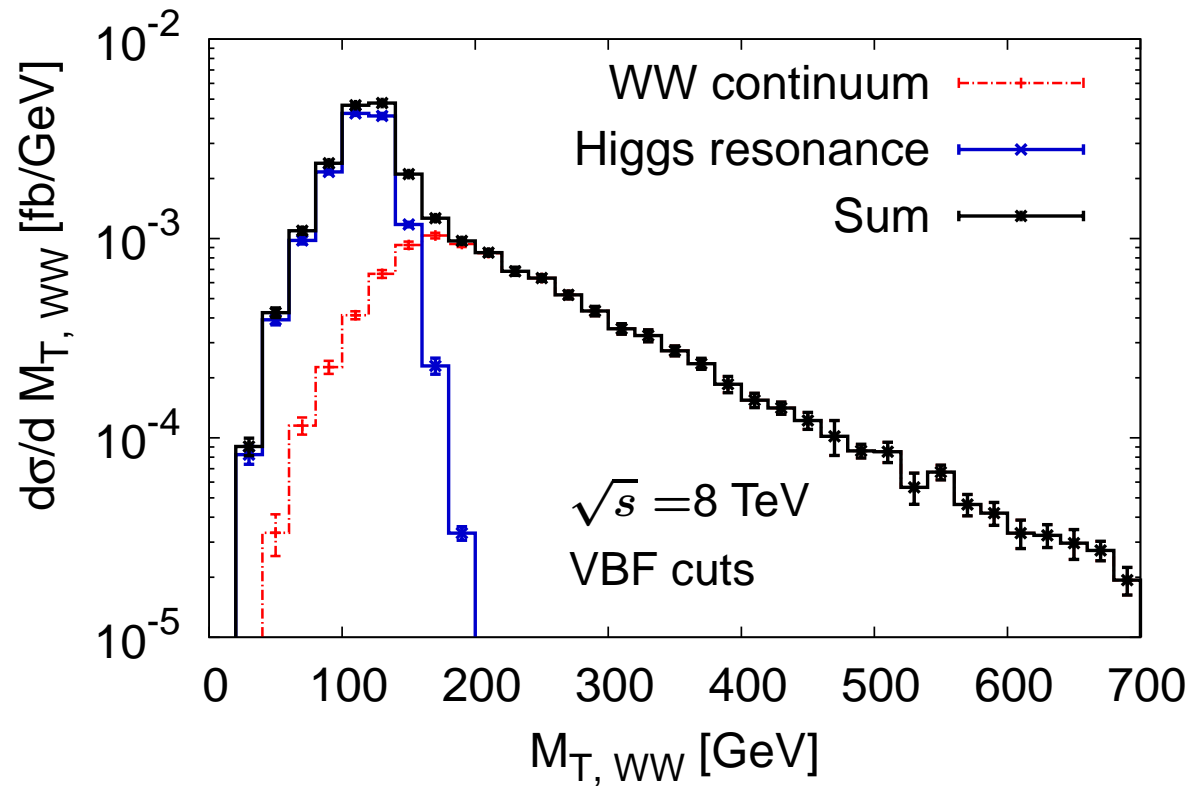
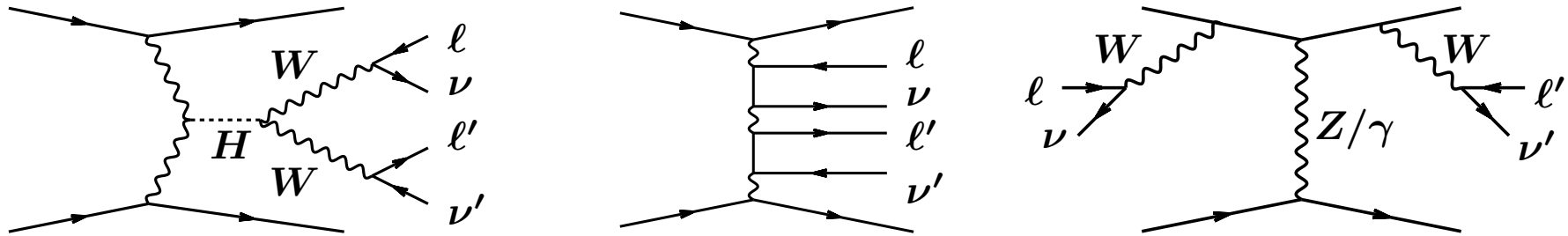
so far only implementation of EW- and QCD-induced  $VVjj$  production processes available in the POWHEG-BOX:

<http://powhegbox.mib.infn.it/>



- ❖ QCD  $W^+W^+jj$  production [Melia, Nason, Rontsch, Zanderighi (2011)]
- ❖ EW  $W^+W^+jj$  production [Zanderighi, B.J. (2011)]
- ❖ EW  $W^+W^-jj$  production [Zanderighi, B.J. (2013)]
- ❖ EW  $ZZjj$  production [Karlberg, Zanderighi, B.J. (2013)]

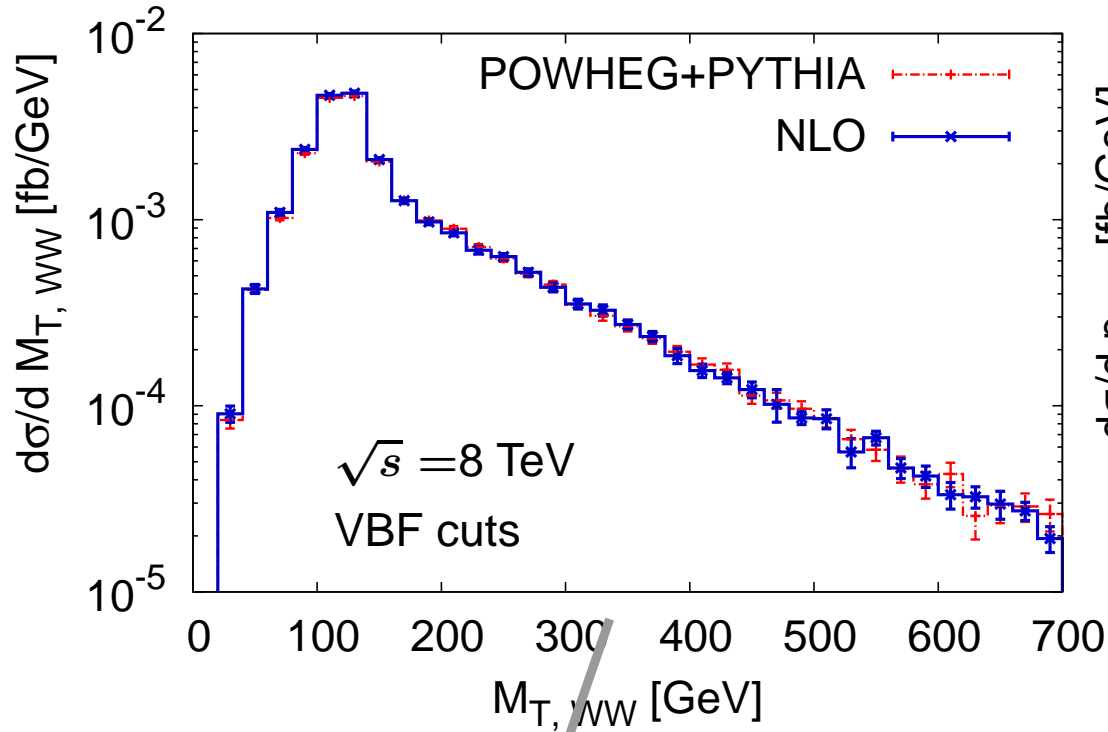
# $W^+W^-jj$ via VBF: resonance and continuum



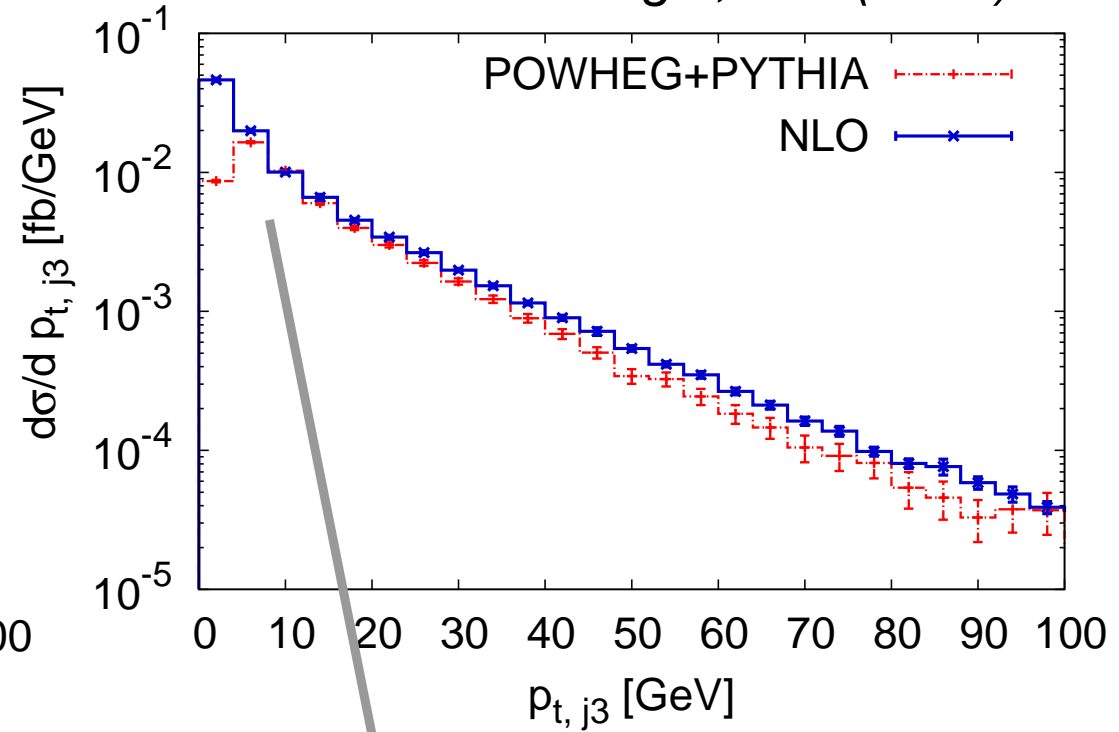
G. Zanderighi, B.J. (2013)

# $pp \rightarrow W^+W^-jj$ via VBF with leptonic decays

G. Zanderighi, B.J. (2013)

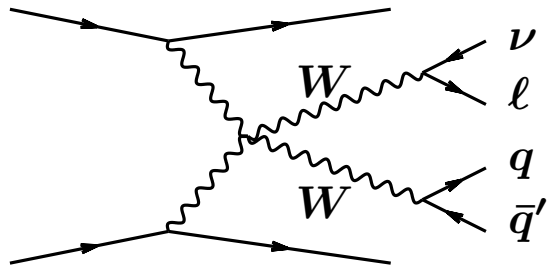


leptonic observables  
not very sensitive to  
parton shower



growth of jet distribution  
tamed by Sudakov factor

# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays



“semi-leptonic” final state:

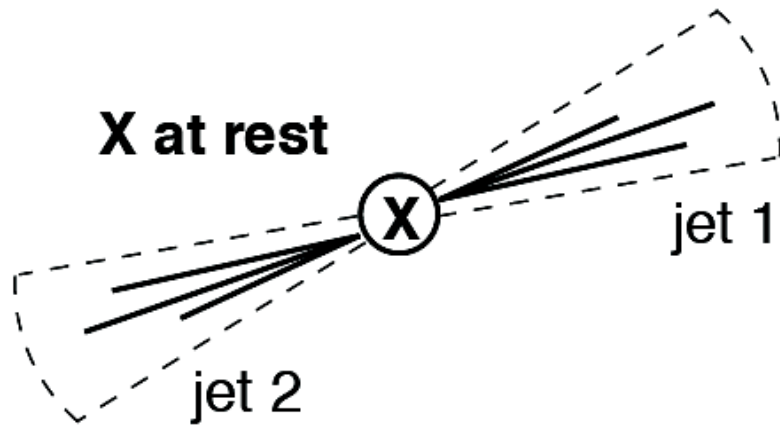
$$W^+W^- \rightarrow \ell\nu + q\bar{q}'$$

different from fully leptonic modes:

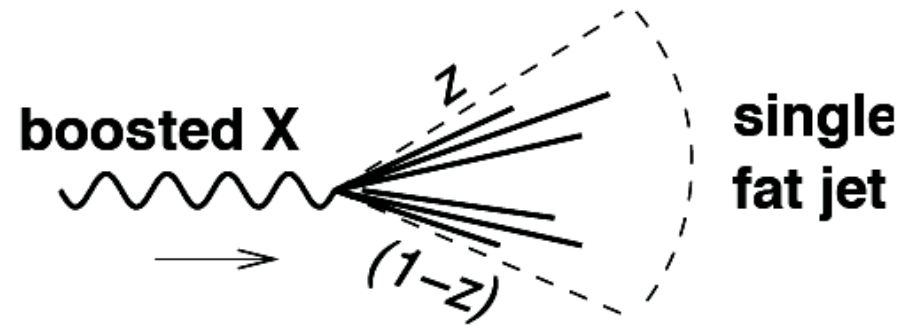
- ✓ branching ratio  $\text{BR}_{W \rightarrow q\bar{q}'} \approx 3 \times \text{BR}_{W \rightarrow \ell\nu} \rightarrow$  larger x-sec
- ✓ only one neutrino  $\rightarrow$  on-shell:  $M_{WW}$  reconstruction possible
- ✗ sophisticated analysis techniques needed to isolate signal

# boosted jet techniques

Normal analyses: two quarks from  $X \rightarrow q\bar{q}$  reconstructed as two jets



**High- $p_t$  regime: EW object X is boosted, decay is collimated,  $q\bar{q}$  both in same jet**



- ❖ pioneering work on  $WW$  scattering at the LHC

*Butterworth, Cox, Forshaw (2002)*

- ❖ break-through in  $pp \rightarrow VH$

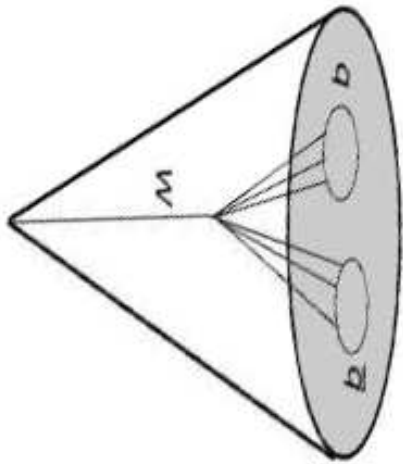
*Butterworth, Davison, Rubin, Salam (2008)*

- ❖ today: established field in its own

# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays

$$pp \rightarrow W^+(q\bar{q}')W^-(\ell\nu)jj:$$

require a **highly boosted fat jet**  
with invariant mass close to  $M_W$



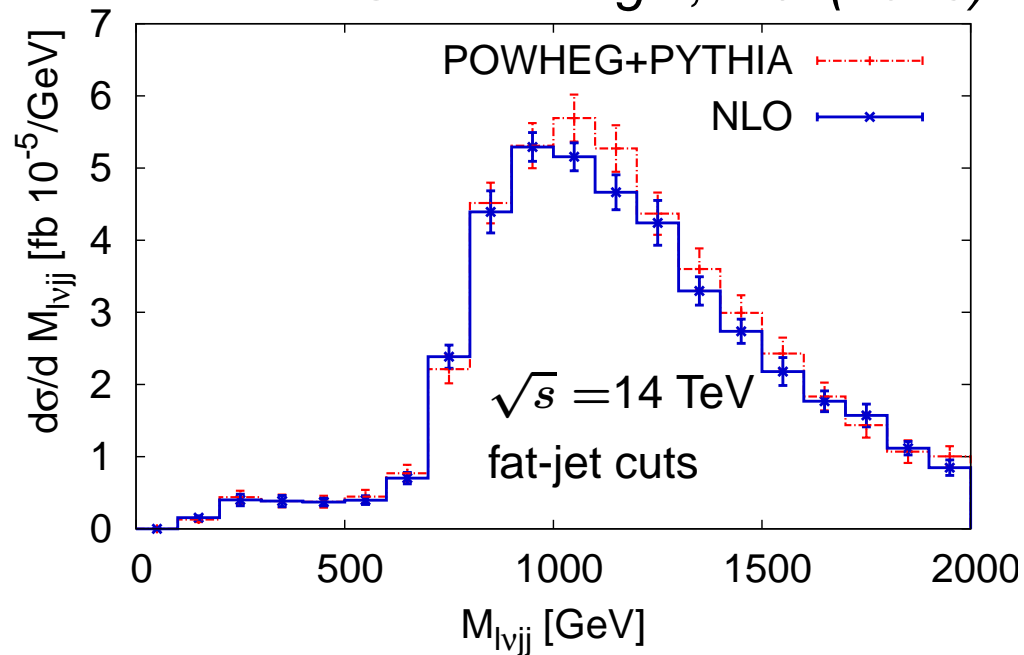
make use of jet properties / composition:

→ distinguish hadronically decaying  
heavy bosons  
from ordinary QCD jets

(stable against parton-shower effects)

# $pp \rightarrow W^+W^-jj$ via VBF with semi-leptonic decays

G. Zanderighi, B.J. (2013)



results stable against  
parton-shower effects

selection cuts  
specific for fat-jet analysis:

$$p_{T,J}^{\text{boosted}} > 300 \text{ GeV},$$
$$M_J \in (M_W \pm 10 \text{ GeV}),$$
$$p_{T,\ell} > 300 \text{ GeV}$$

cuts enforce highly energetic  
 $WW$  system  
(above light Higgs resonance)

# BSM effects: effective operator approach

parameterize deviations from Standard Model via  
**effective field theory** expansion  
(valid up to scale  $\Lambda$ ):

$$\mathcal{L}_{\text{eff}} = \sum \frac{c_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)} = \mathcal{L}_{\text{SM}} + \sum \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$$

[ cf. Degrande et al. (2012) ]



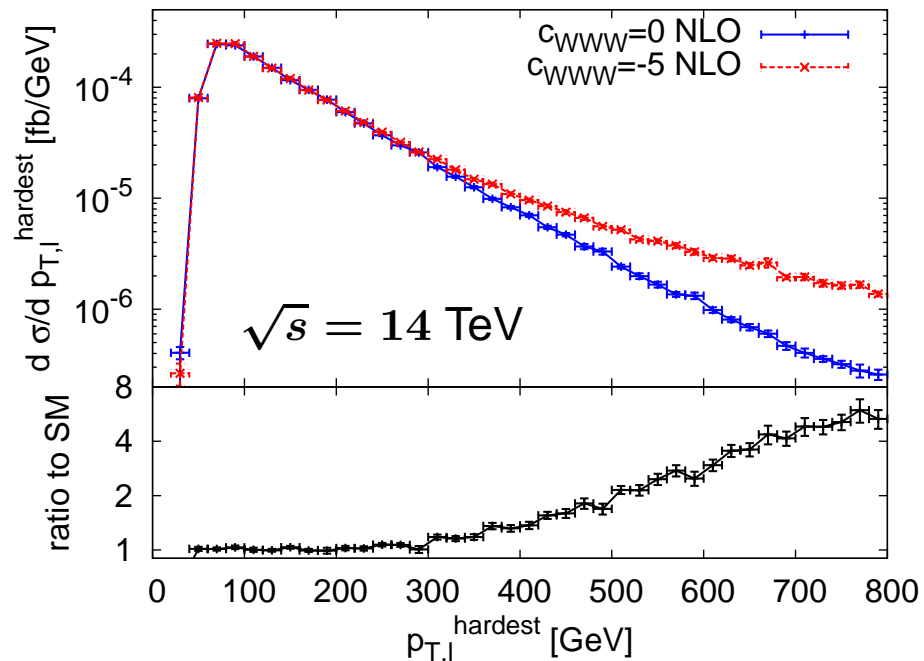
modifications of triple and  
quartic gauge couplings

note: higher dim. operator coefficients severely constrained by data from LEP, Tevatron, LHC



# new interactions in electroweak $ZZjj$ production

Karlberg, Zanderighi, B.J. (2013)



allow for non-zero dimension-six operator coefficients

(compatible with exp. limits)

→ tails of transverse momentum distributions enhanced

but:

very demanding at LHC14 because of small signal rates

(much better limits possible with 33 or 100 TeV)

# limitations of EFT

effective field theory **valid up to scale  $\Lambda$**  by construction

higher-dim operators suppressed by extra powers of  $1/\Lambda$

→ no problems with unitarity

contributions from regime beyond validity:

→ violations of unitarity (unphysical)

need to **avoid regions where EFT breaks down** by:

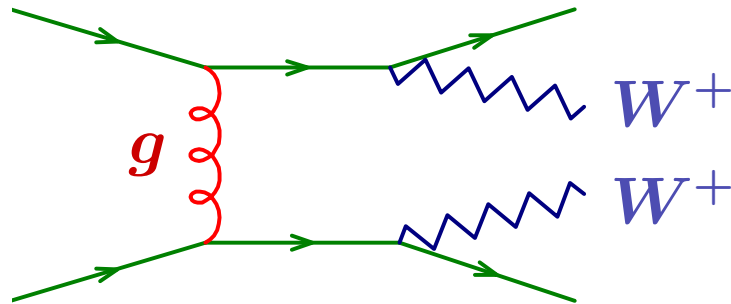
- kinematic cuts
- form factors (damp contributions  $> \Lambda$ )
- unitarization prescriptions,  
e.g. K-matrix unitarization (WHIZARD)

# $pp \rightarrow W^+W^+jj$ in the POWHEG-BOX

## QCD-induced production

*Melia, Melnikov, Rontsch, Zanderighi (2010);*

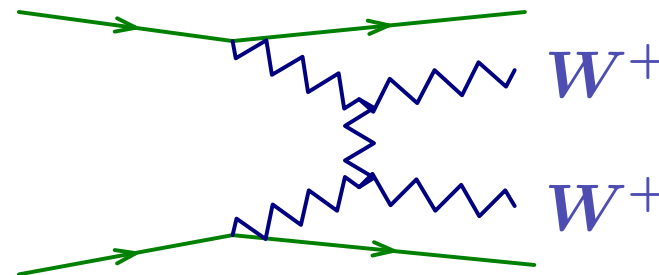
*Melia, Nason, Rontsch, Zanderighi (2011)*



## EW production

*Oleari, Zeppenfeld, B.J. (2009);*

*Zanderighi, B.J. (2011)*



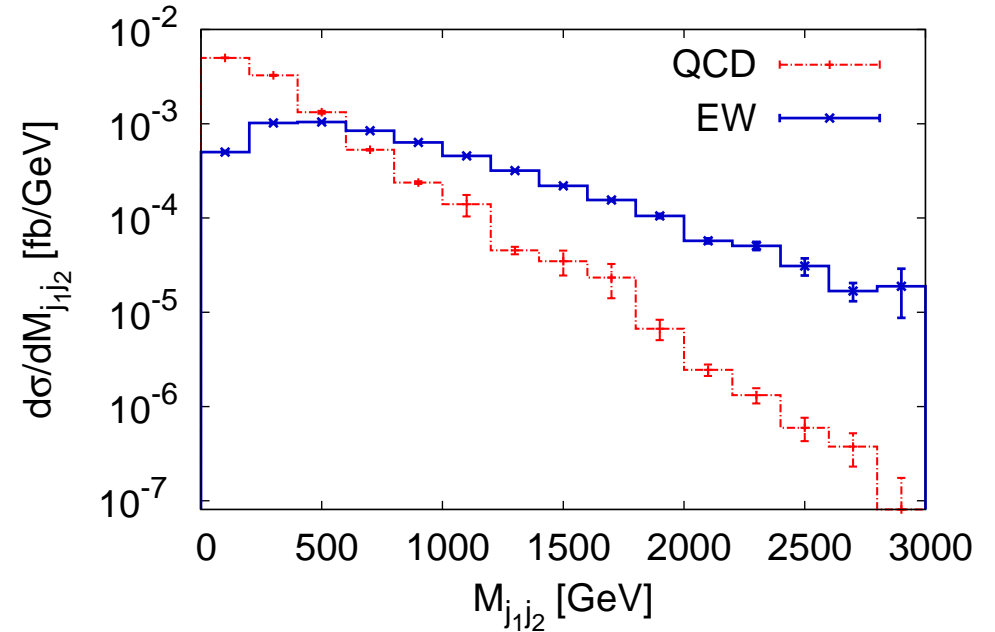
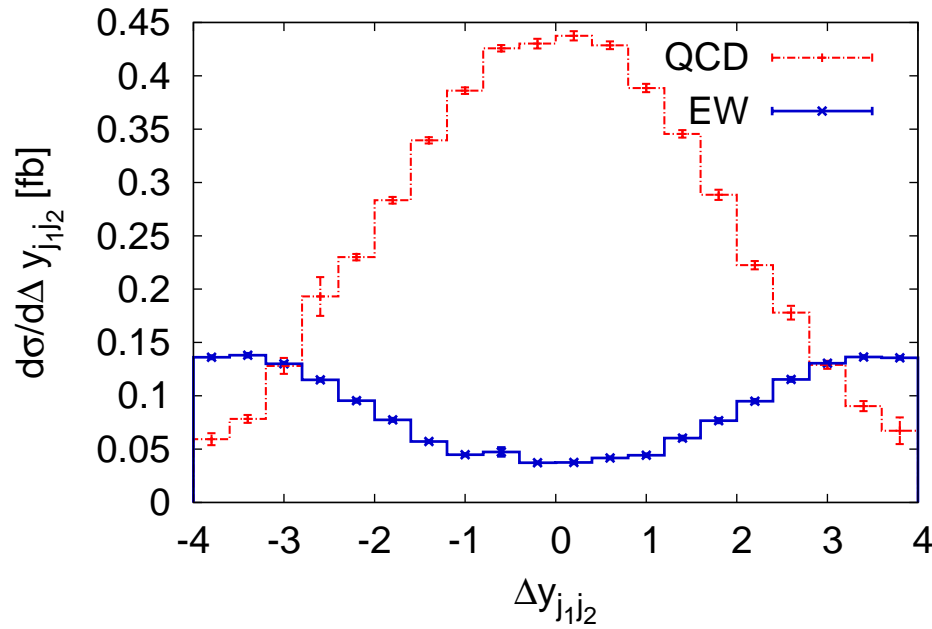
NLO-QCD results for  $\sqrt{s} = 7$  TeV with basic jet cuts only ( $p_T^{\text{tag}} > 20$  GeV):

$$\sigma_{\text{QCD}}^{\text{inc}} = 2.12 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{inc}} = 1.097 \text{ fb}$$

# $pp \rightarrow W^+W^+jj$ : QCD versus EW production

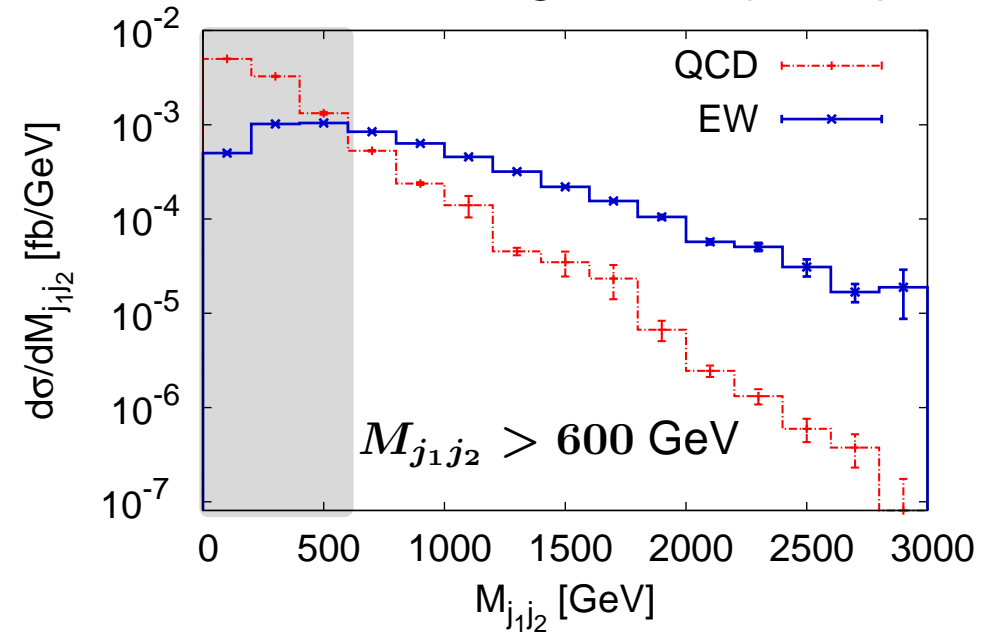
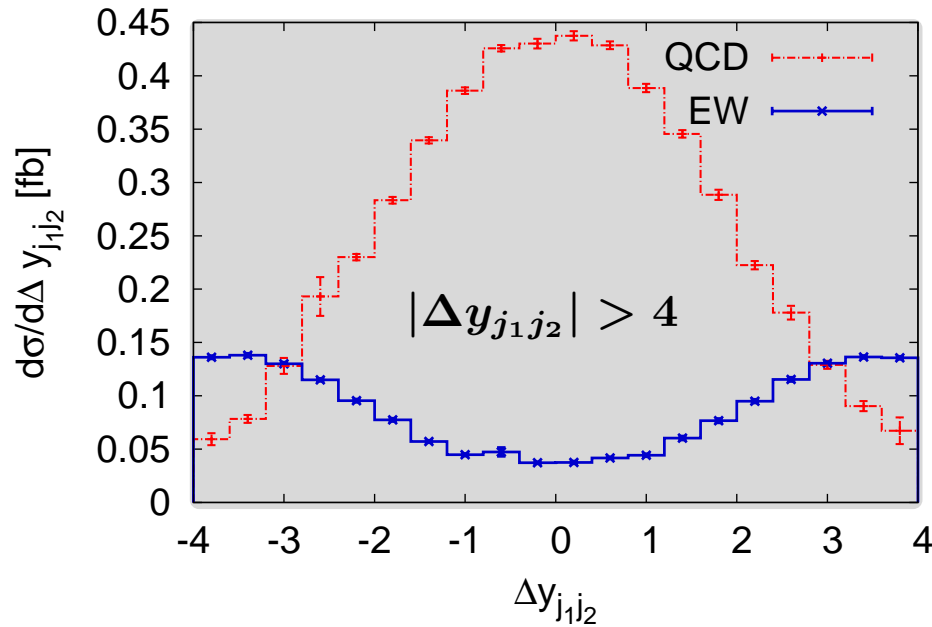
Zanderighi, B.J. (2011)



- $\sqrt{s} = 7$  TeV
- basic jet cuts only
- NLO-QCD accuracy

# $pp \rightarrow W^+W^+jj$ : QCD versus EW production

Zanderighi, B.J. (2011)

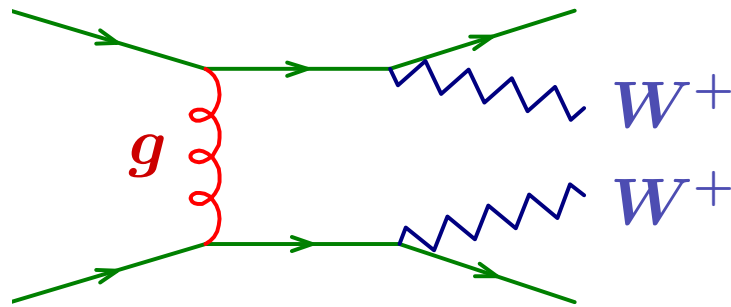


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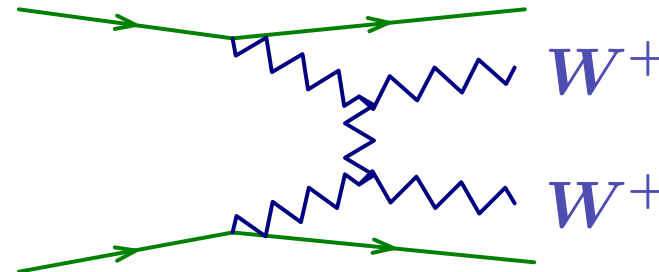
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*Melia, Melnikov, Rontsch, Zanderighi (2010);  
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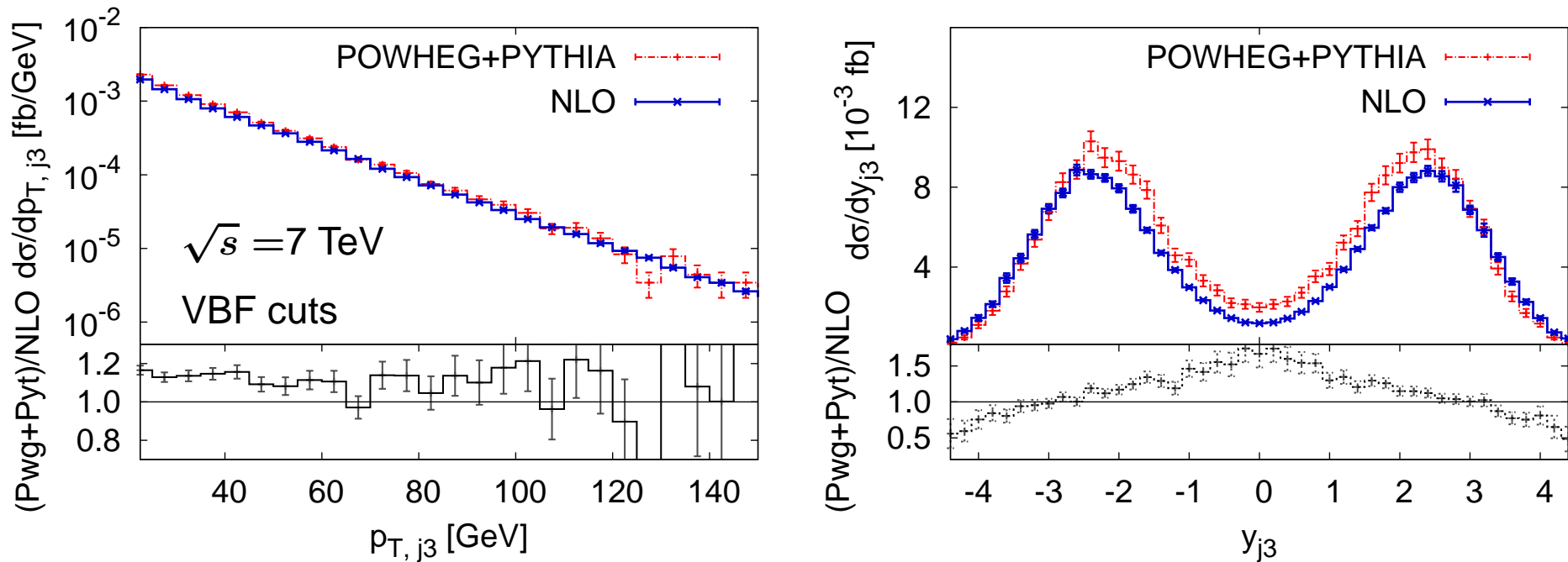
NLO results with VBF cuts:

$$\sigma_{\text{QCD}}^{\text{cuts}} = 0.0074 \text{ fb}$$

$$\sigma_{\text{EW}}^{\text{cuts}} = 0.201 \text{ fb}$$

# $pp \rightarrow W^+W^+jj$ via VBF in the POWHEG-BOX

Zanderighi, B.J. (2011)

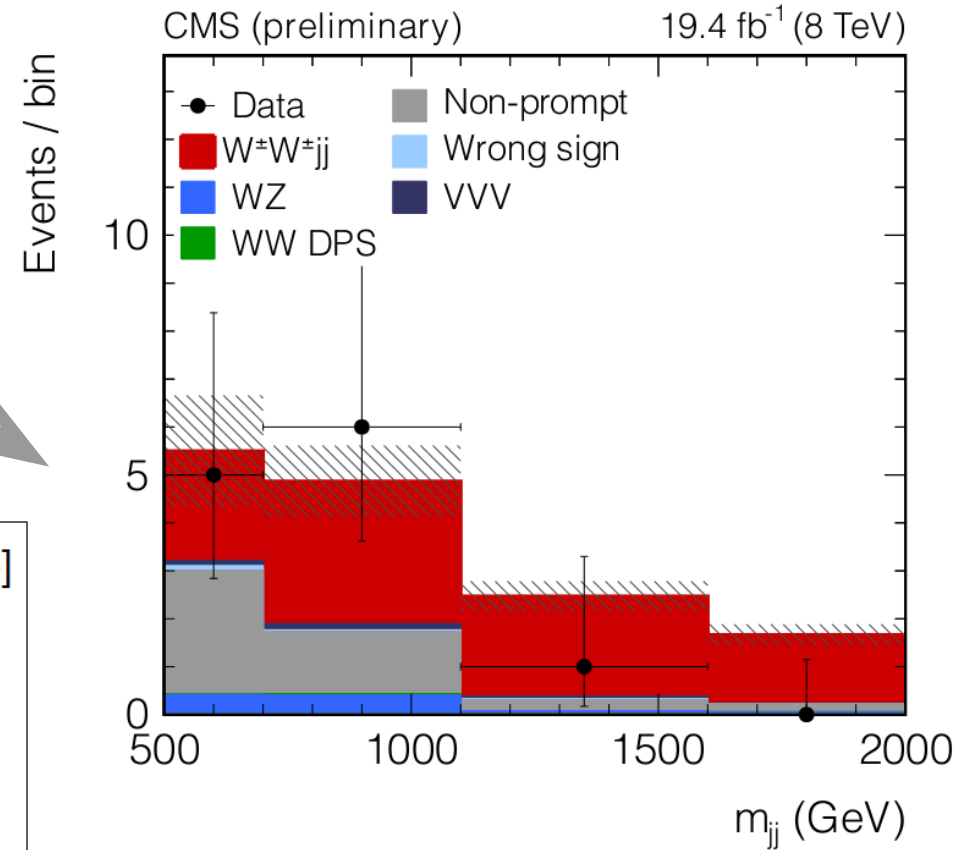
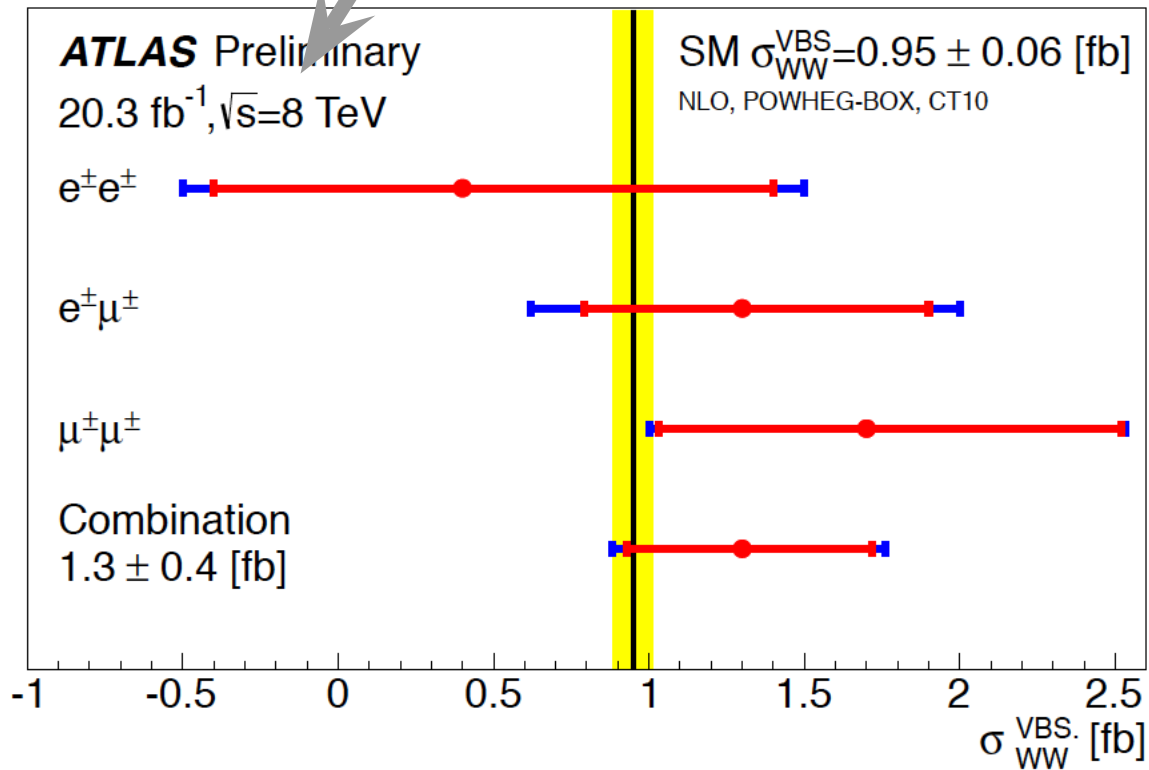


typical for VBF processes: little jet activity at central rapidities  
 $\rightarrow$  exploited by central-jet veto techniques

note: parton-shower effects slightly enhance central jet activity

# evidence for $W^\pm W^\pm jj$ from ATLAS and CMS

details in  
Nicolas Pierre  
Chanon's talk





# summary

VBF crucial for understanding mechanism of electroweak symmetry breaking:

- \*  $Hjj$ : very clean Higgs production channel
- \*  $VVjj$ : sensitive to signatures of new physics in the gauge boson sector

important pre-requisites:

- ✓ explicit calculations revealed that VBF reactions are **perturbatively well-behaved** (NLO-QCD corrections and parton-shower effects moderate)

# open issues

- \* all **QCD-induced  $VVjj$**  production processes matched to parton shower at NLO-QCD
- \* flexible Monte Carlo tools for all  $VVjj$  production modes in **BSM scenarios** including NLO-QCD corrections and parton-shower effects
- \* **electroweak corrections** to all  $VVjj$  production modes
- \* **mixing** between QCD- and EW-induced production modes

# summary

recent years have seen much progress on the theory side:

- ✓ precision calculations for  $VVjj$  processes
- ✓ tool development: public codes including
  - NLO-QCD corrections
  - parton-shower effects

... can develop their **full potential only**  
**if used by experimentalists ...**



...for your attention