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# Higgsstrahlung at forward rapidities

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Based upon [ArXiv:1403.2014](#)

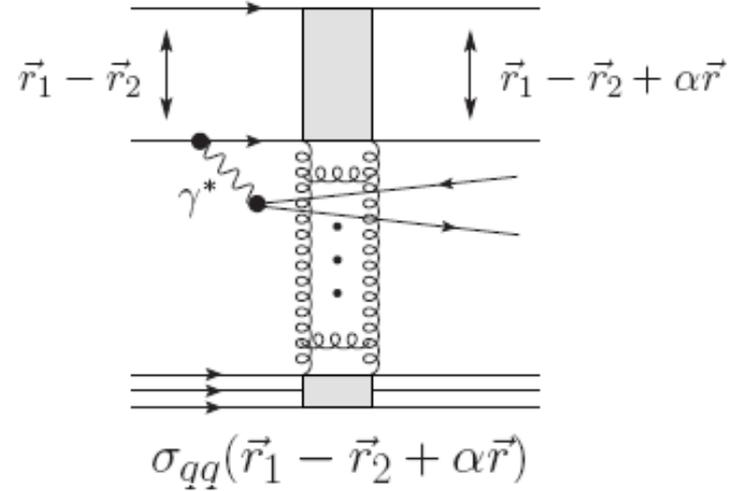
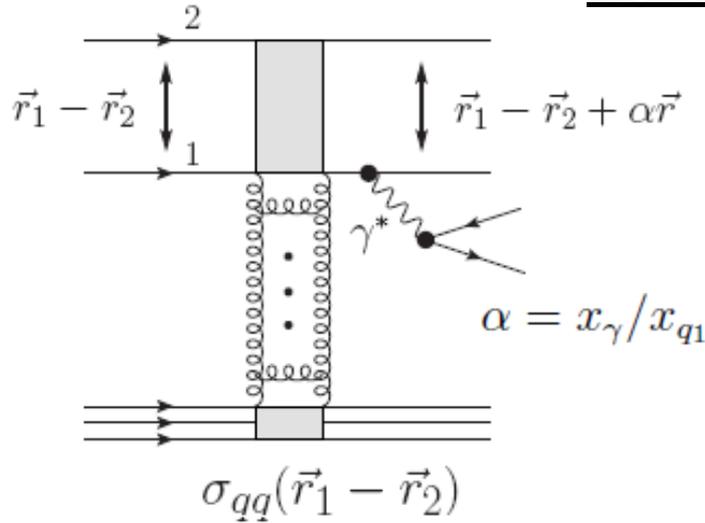
Trento, April 16<sup>th</sup>, 2014

# Contents

- Color Dipole Picture of diffraction – DDY example
- Abelian vs non-Abelian diffractive production
- Diffractive factorisation breaking
- Forward diffractive heavy quarks production
- Diffractive Higgsstrahlung off heavy quarks
- Single diffractive Higgs production
- Inclusive vs diffractive Higgsstrahlung
- Conclusions

# DY example: Abelian Bremsstrahlung off a dipole

...due to transverse motion of partons



$$2i \operatorname{Im} f_{el}(\vec{b}, \vec{r}_p) = \frac{i}{N_c} \sum_X \sum_{c_f c_i} |V_q(\vec{b}) - V_q(\vec{b} + \vec{r}_p)|^2$$

$$\sigma_{\bar{q}q}(r_p) = \int d^2b 2 \operatorname{Im} f_{el}(\vec{b}, \vec{r}_p)$$

**dipoles with different sizes interact differently!**



**The fundamental reason for diffraction!**

**DDY in the dipole-target scattering**

$$M_{q\bar{q}}^{(1)}(\vec{b}, \vec{r}_p, \vec{r}, \alpha) = -2ip_i^0 \sqrt{4\pi} \frac{\sqrt{1-\alpha}}{\alpha^2} \Psi_{\gamma^*q}^\mu(\alpha, \vec{r}) \left[ 2\operatorname{Im} f_{el}(\vec{b}, \vec{r}_p) - 2\operatorname{Im} f_{el}(\vec{b}, \vec{r}_p + \alpha \vec{r}) \right]$$

**destructive interference**



**one of the reasons for diffractive factorisation breaking!**

# Elastic amplitude and gap survival

Complete dipole elastic amplitude has **eikonal form**:

$$\text{Im } f_{el}(\vec{b}, \vec{r}_1 - \vec{r}_2) = 1 - \exp[i\chi(\vec{r}_1) - i\chi(\vec{r}_2)],$$

$$\chi(b) = - \int_{-\infty}^{\infty} dz V(\vec{b}, z), \quad \textit{nearly imaginary at high energies!}$$

**Diffractive amplitude** is proportional to

$$\text{Im } f_{el}(\vec{b}, \vec{r}_1 - \vec{r}_2 + \alpha\vec{r}) - \text{Im } f_{el}(\vec{b}, \vec{r}_1 - \vec{r}_2) = \underbrace{\exp[i\chi(\vec{r}_1) - i\chi(\vec{r}_2)]}_{\text{Exactly the soft survival probability amplitude}} \exp[i\alpha\vec{r} \cdot \vec{\nabla}\chi(\vec{r}_1)]$$

*another source of QCD factorisation breaking*

**Exactly the soft survival probability amplitude**

*controlled by soft spectator partons*

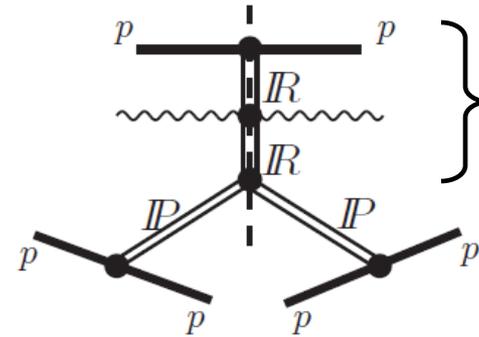
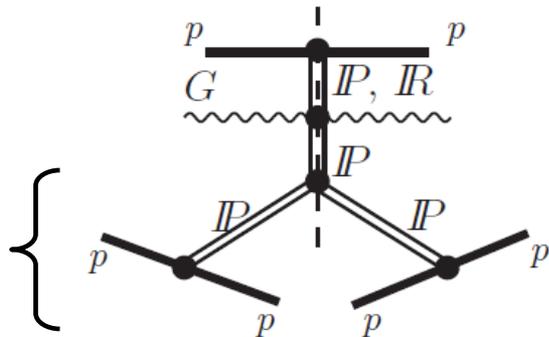
*vanishes in the black disc limit!*

*Absorption effect should be included into elastic amplitude parameterization (at the amplitude level)*

# DY example: Regge picture of diffractive excitations

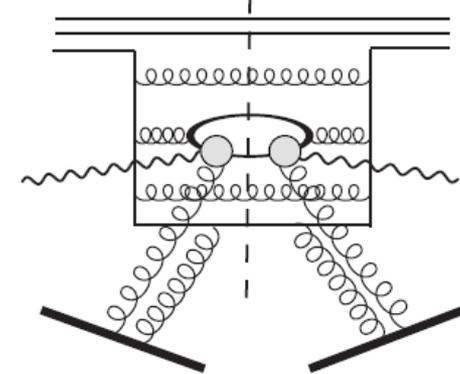
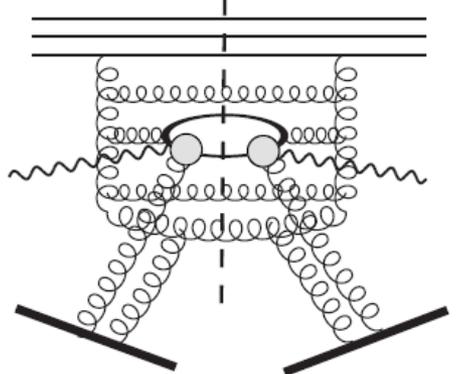
$$\xi = 1 - x_F = \frac{M_X^2}{s} \ll 1$$

LRG

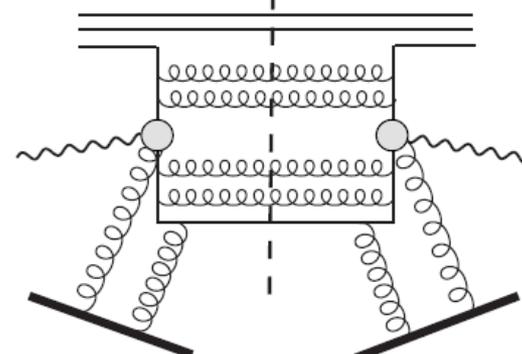
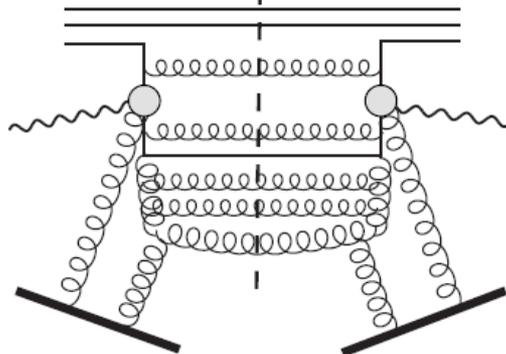


projectile  
fragmentation  
region  
(diffractive mass)

diffractive  
sea quark  
excitation



diffractive  
valence quark  
excitation

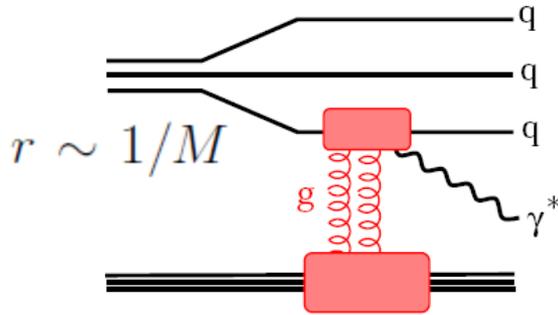


# DY example: Probing large distances in the proton...

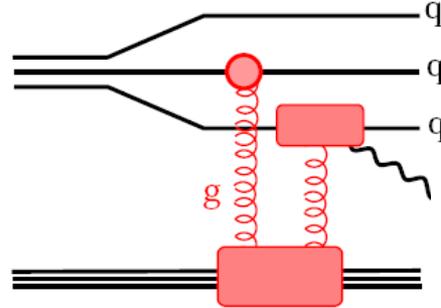
R. Pasechnik, B. Kopeliovich, I. Potashnikova, *Phys. Rev. D*86, 114039, 2012

R. Pasechnik, B. Kopeliovich, *Eur. Phys. J. C*71: 1827, 2011

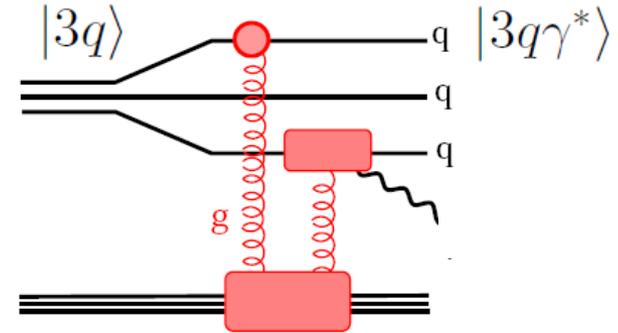
B. Kopeliovich, I. Potashnikova, I. Schmidt and A. Tarasov, *Phys. Rev. D*74: 114024, 2006



**GBW dipole (ex.)**



$$\sigma(r) = \sigma_0 \left(1 - e^{-r^2/R_0^2}\right)$$



Interplay between hard and soft scales

**Amplitude**  $\propto \sigma(\vec{R}) - \sigma(\vec{R} - \alpha\vec{r}) = \frac{2\alpha\sigma_0}{R_0^2(x_2)} e^{-R^2/R_0^2(x_2)} (\vec{r} \cdot \vec{R}) + O(r^2)$

**Diffractive DIS**  $\propto r^4$

**diffractive factorization holds!**

**Higher twist effect!**

Diffraction is dominated by soft fluctuations!

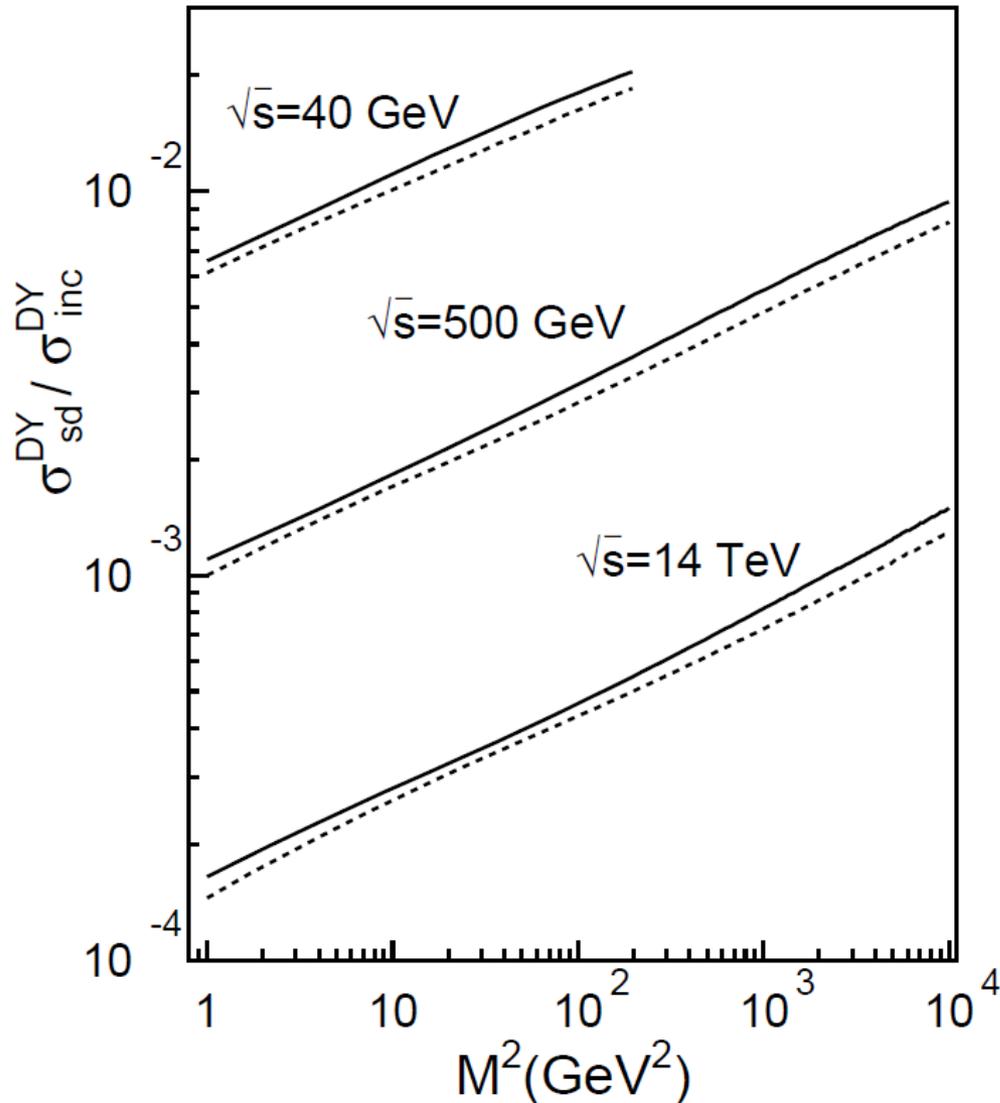
**Diffractive DY**  $\propto r^2$

**diffractive factorization is broken!**

**Leading twist effect!**

Diffraction is dominated by semisoft-semihard fluctuations!

# DY example: signatures for QCD factorisation breaking



**saturated shape of the dipole CS**

**+**

**unitarity corrections**



**Fraction of diffractive events**

- **steeply falls with energy**
- **grows with the hard scale**



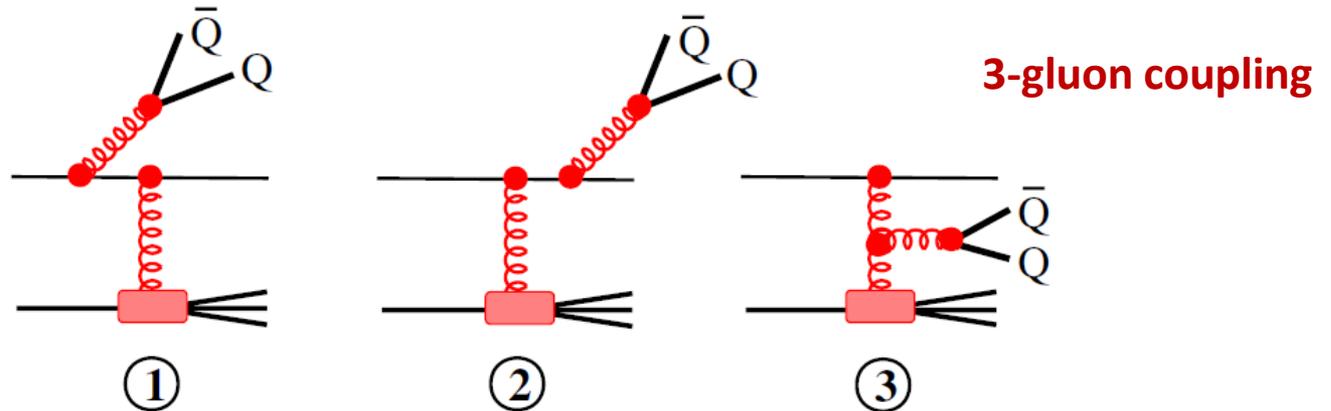
**Opposite to factorization-based results (like Ingelman-Schlein)**

c.f. G. Kubasiak, A. Szczurek,  
Phys.Rev.D84:014005,2011

# Non-Abelian diffraction

- Larger single diffractive cross sections than heavy QQ CEP/Abelian mechanisms (dominates the diffractive heavy flavor production)
- One more promising test of QCD diffraction mechanisms and, in particular, diffractive factorisation breaking effects
- An important background for intrinsic heavy flavor studies via diffraction
- An important playground for forward Higgsstrahlung studies off heavy flavor/gauge bosons (Brodsky et al '06, '07)
- One of the ways of direct Higgs-bottom/Higgs-top Yukawa couplings studies via diffraction

# Non-Abelian Bremsstrahlung off a quark and gg-fusion

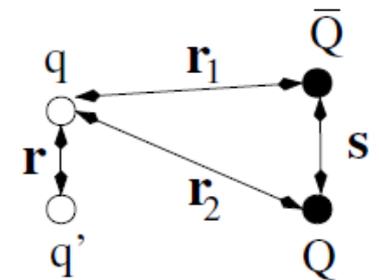
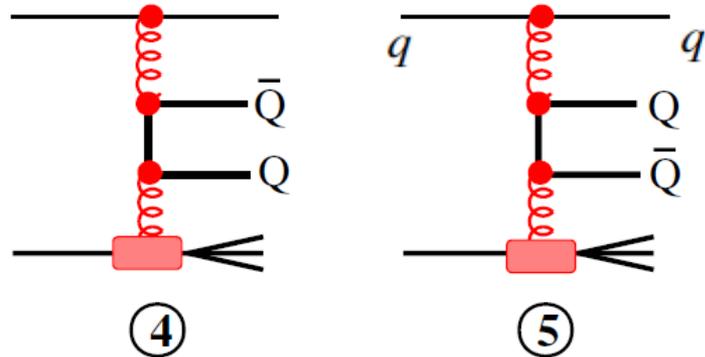


Bremsstrahlung  
component

Extra QQ production terms

Impact  
parameters

$$M_{\text{Br}}^T = M_1^T + M_2^T + \frac{Q^2}{M^2 + Q^2} M_3^T$$



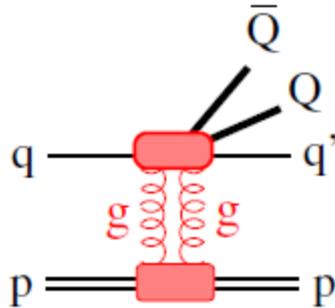
Production  
component

$$M_{\text{Pr}}^T = \frac{M^2}{M^2 + Q^2} M_3^T + M_4^T + M_5^T$$

q'-(QQ) distance:  $\vec{\rho} = \vec{r} - \beta \vec{r}_1 - (1 - \beta) \vec{r}_2$

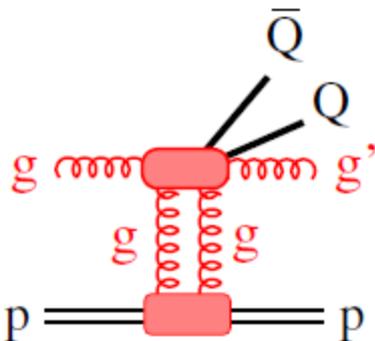
# QQ production: diffractive parton-proton scattering

Quark-proton scattering  
(diffractive quark excitation)



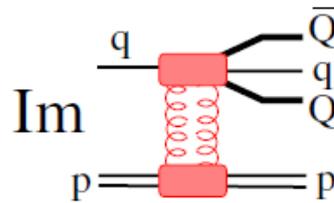
...dominant at forward rapidities

Gluon-proton scattering  
(diffractive gluon excitation)



...vanishes at forward rapidities

Imaginary amplitude

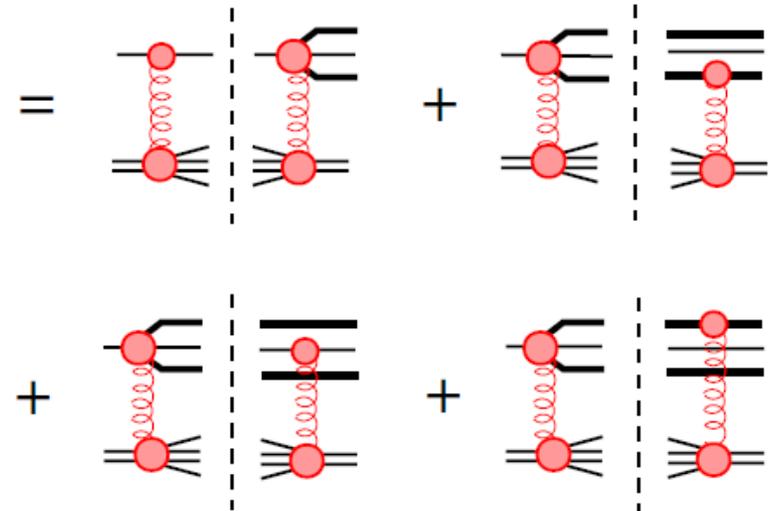


Cutting rules

$$\langle \rho^2 \rangle \sim \langle s^2 \rangle \sim \frac{1}{m_Q^2}$$

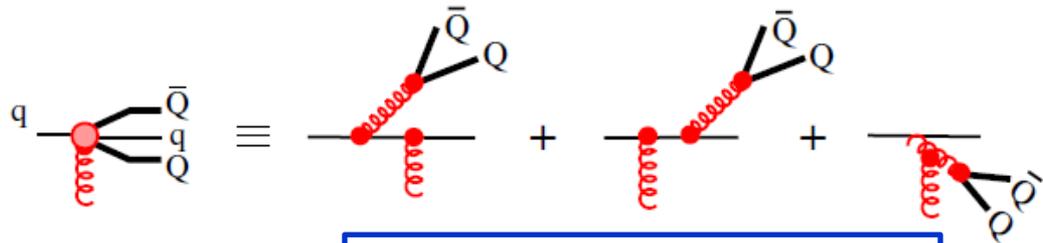
$$\langle s^2 \rangle \sim 1/m_Q^2$$

$$\langle \rho^2 \rangle \sim 1/m_q^2$$



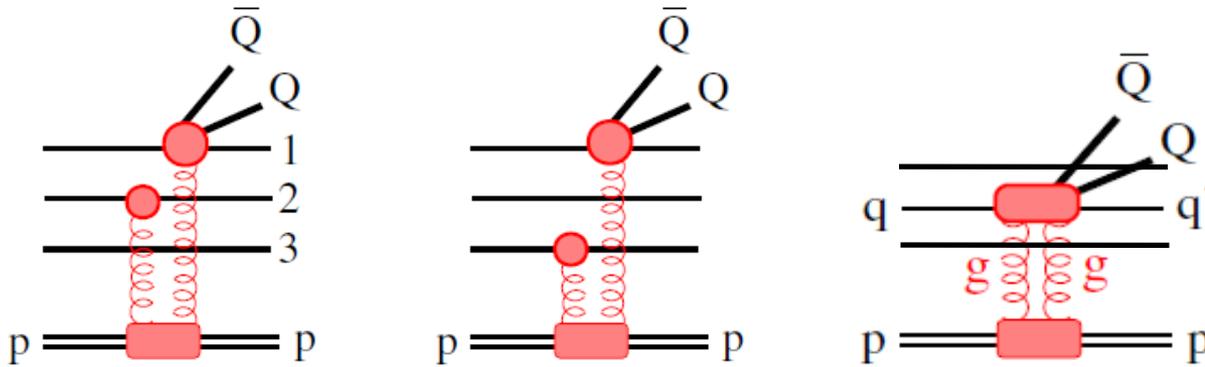
"Bremsstrahlung" contribution

"Production" contribution



Does not vanish  
in the forward scattering!

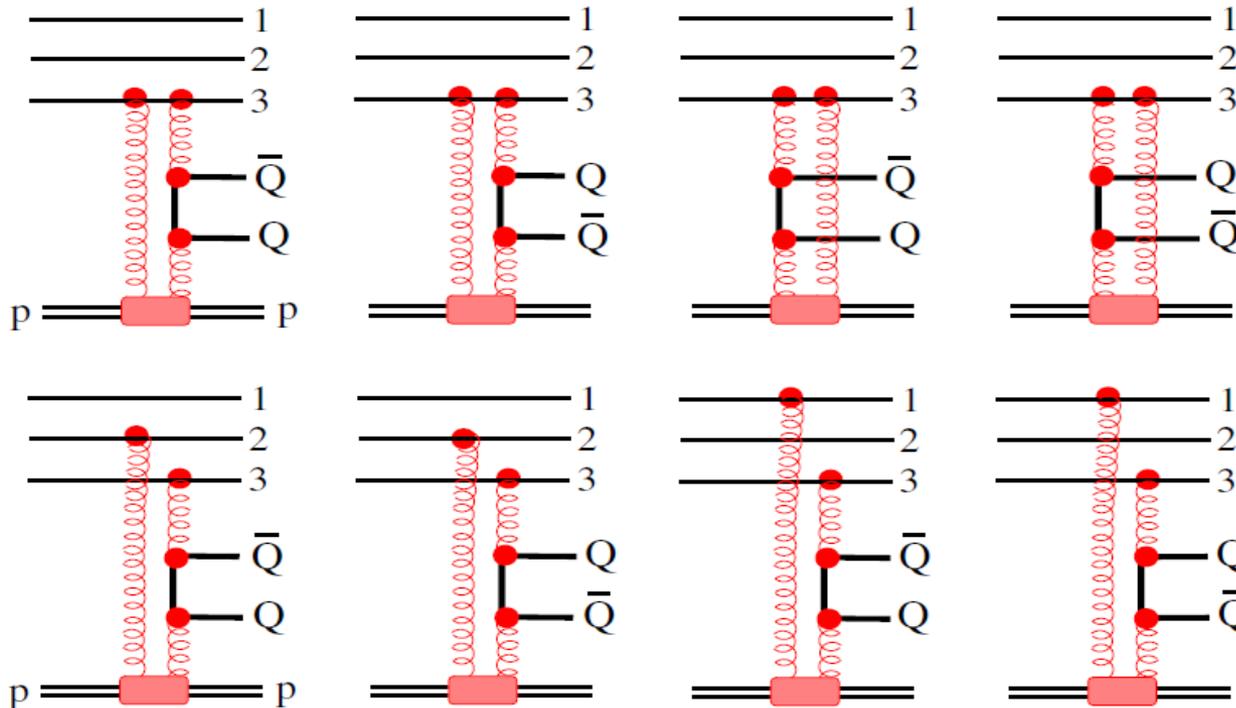
# QQ production: diffractive proton-proton scattering



and sea gluons/quarks must be included!

$$|\Psi_{in}(\vec{r}_i, x_i)|^2 \Rightarrow \frac{1}{3} \left[ \sum_q q(x) + \bar{q}(x) + \frac{81}{16} g(x) \right]$$

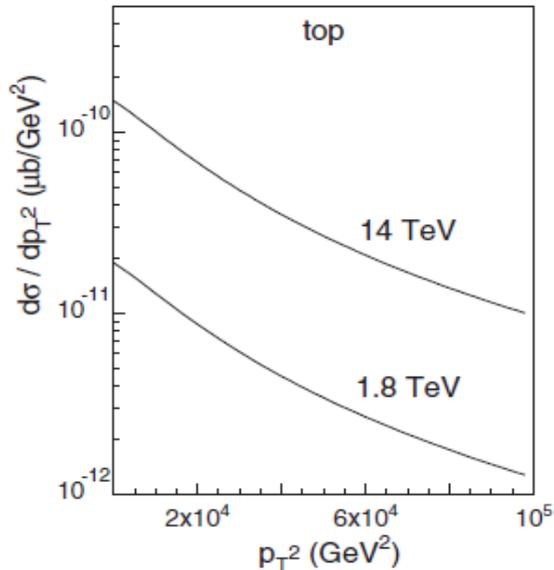
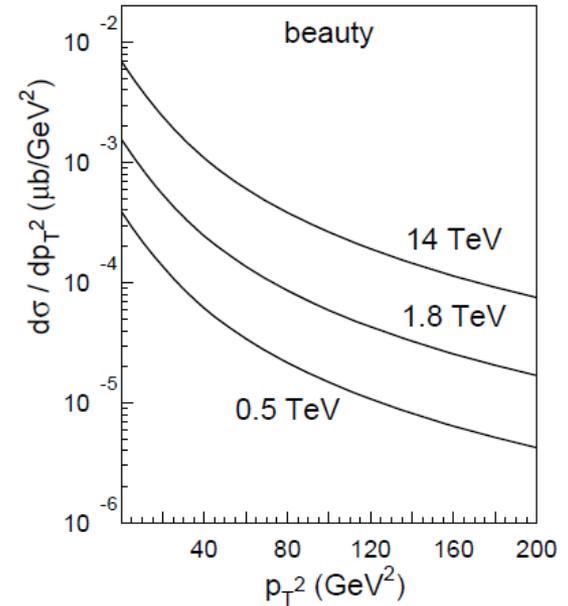
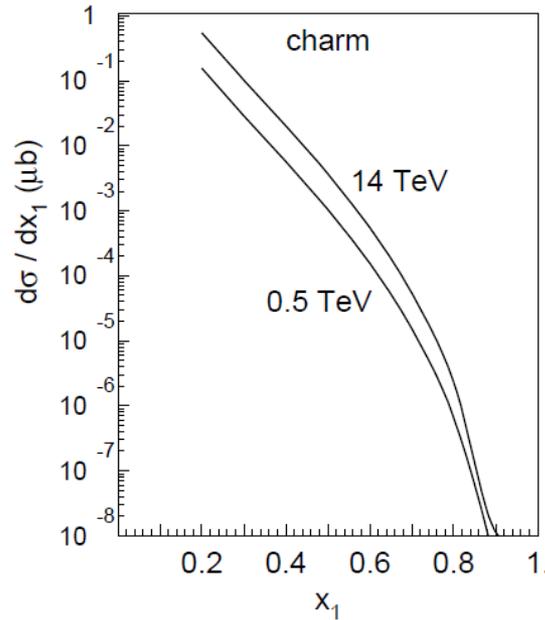
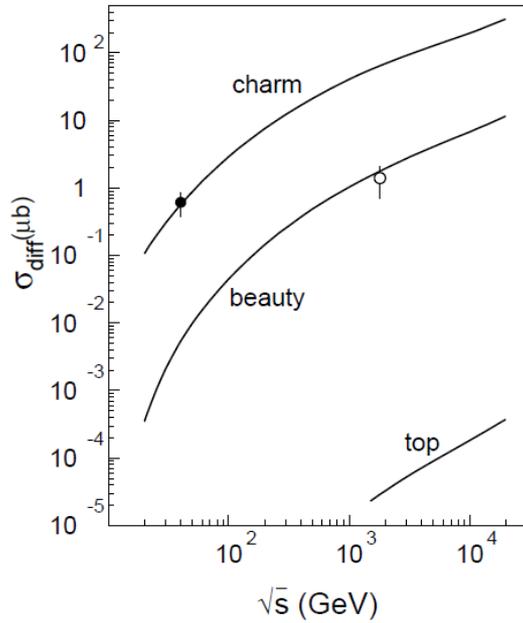
Production component strongly dominates the diffractive cross section!



the largest leading-twist contribution

$$\sim 1/m_Q^2$$

# Forward diffractive heavy flavor: cross sections



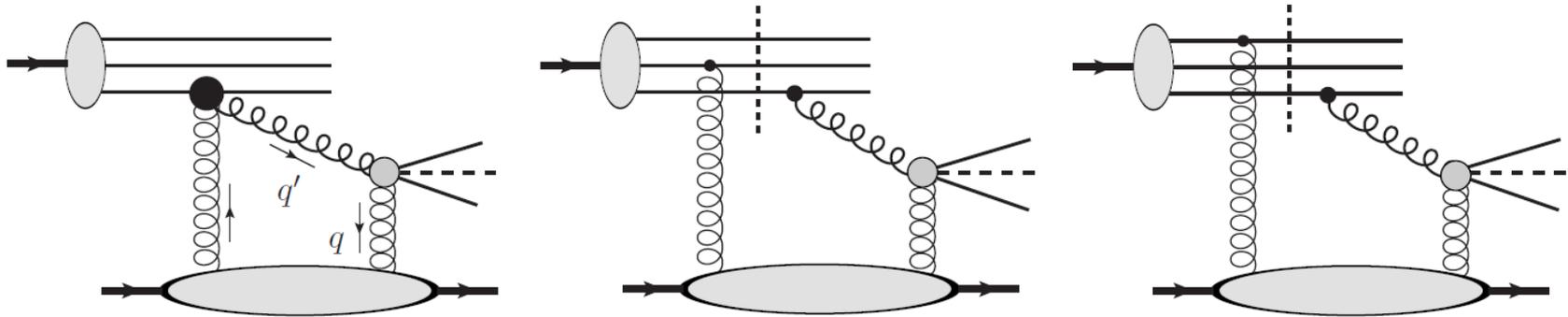
**B. Kopeliovich et al, Phys.Rev.D76, 034019 (2007)**

**Leading-twist diffractive excitations  
are proven to be dominated!**

cf. factorisation-based approach by

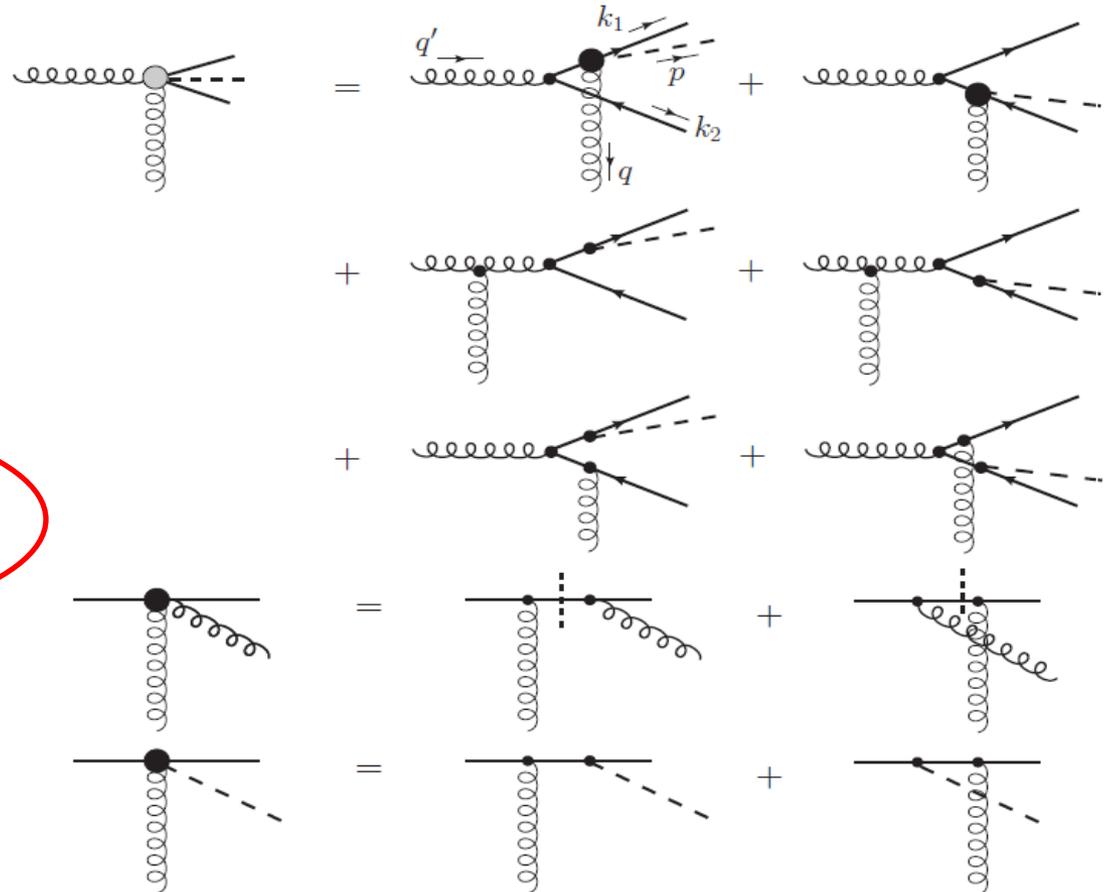
**M. Luszczak, W. Schafer and A.Szczurek,  
arXiv:1305.4727 [hep-ph]**

# Diffractive Higgsstrahlung off heavy flavor



$$p + p \rightarrow \bar{Q}Qh + X + p$$

**Gluon-Gluon fusion strongly dominates over gluon Bremsstrahlung!**



# Single diffractive cross section: Higgsstrahlung

The general result:

$$\begin{aligned}
 & \frac{d\sigma^{L,T}(pp \rightarrow p(Q\bar{Q}h)X)}{d^2\vec{\kappa} d^2\vec{r} d\ln\alpha d\ln\beta d\ln\xi d^2\delta_{\perp}} \Big|_{\delta_{\perp} \rightarrow 0} = \frac{1}{(2\pi)^4} \frac{9}{256\pi^2} \\
 & \times \sum_{l=q,g} \sum_{q=val, sea} \int d^2\vec{r}_1 d^2\vec{r}_2 d^2\vec{r}_3 d^2\vec{\omega} d^2\vec{\rho}_1 d^2\vec{\rho}_2 d^2\vec{\sigma}_1 d^2\vec{\sigma}_2 dx_q \prod_{j \neq 1} dx_q^j \prod_k dx_g^k e^{i\vec{\kappa} \cdot (\vec{\rho}_1 - \vec{\rho}_2)} \\
 & \times e^{i\vec{r} \cdot (\vec{\sigma}_1 - \vec{\sigma}_2)} \Sigma_l^{L,T}(\vec{r}_1, \vec{r}_2, \vec{r}_3; \alpha, \vec{\omega}; \beta, \vec{\rho}_1; \xi, \vec{\sigma}_1) \Sigma_l^{L,T*}(\vec{r}_1, \vec{r}_2, \vec{r}_3; \alpha, \vec{\omega}; \beta, \vec{\rho}_2; \xi, \vec{\sigma}_2) \\
 & \times |\Psi_i(\vec{r}_1, \vec{r}_2, \vec{r}_3; x_q, \{x_q^{2,3,\dots}\}, \{x_g^{1,2,\dots}\})|^2,
 \end{aligned}$$



diffractive amplitude of QQh  
production in parton-proton scattering

Incoming proton wave function

$$\begin{aligned}
 |\Psi_i(\vec{r}_1, \vec{r}_2, \vec{r}_3; x_q, x_{q_2}, x_{q_3})|^2 &= \frac{3a^2}{\pi^2} e^{-a(r_1^2 + r_2^2 + r_3^2)} \rho(x_q, x_{q_2}, x_{q_3}) \quad a = \langle r_{ch}^2 \rangle^{-1} \\
 &\times \delta(\vec{r}_1 + \vec{r}_2 + \vec{r}_3) \delta(1 - x_q - x_{q_2} - x_{q_3})
 \end{aligned}$$

...in terms of **valence/sea (anti)quark** distribution

an immediate access  
to the quark PDFs at large x!

Diff. Higgsstrahlung is of the higher twist

$$\sigma(pp \rightarrow Q\bar{Q}h + X) \propto r_{\text{hard}}^4$$

# Single diffractive amplitude: Higgsstrahlung

Effective wave function



$$\Sigma_{q(1)}^{L,T}(\vec{r}_1, \vec{r}_2, \vec{r}_3; \alpha, \vec{\omega}; \beta, \vec{\rho}; \xi, \vec{\sigma}) = \frac{1}{2} (\tau_b^{q1} \tau_a^{q1}) (\tau_a^Q \tau_b^Q) \left\{ \tilde{\Phi}_q^{T,L}(\alpha, \vec{\omega}; \beta, \vec{\rho}; \xi, \vec{\sigma}) \right. \\ \times \int d^2b \left\{ \left[ 2\text{Im} f_{el}(\vec{b}, (1-\alpha)\vec{\omega} - \xi\vec{\sigma}) - 2\text{Im} f_{el}(\vec{b}, (1-\alpha)\vec{\omega}) \right] \right. \\ \left. \left. - \left[ 2\text{Im} f_{el}(\vec{b}, (1-\alpha)\vec{\omega} - \beta\vec{\rho} - \xi\vec{\sigma}) - 2\text{Im} f_{el}(\vec{b}, (1-\alpha)\vec{\omega} - \beta\vec{\rho}) \right] \right\} \right\} + a \text{ lot more...}$$

Effective dipole cross section

Soft scale:  $\langle \omega^2 \rangle \sim 1/m_q^2 \sim \langle R \rangle^2$

Hard scales:

$$\left\{ \begin{array}{l} \langle \rho^2 \rangle \sim 1/m_Q^2 \\ \langle \sigma^2 \rangle \sim 1/M_h^2 \end{array} \right.$$

The source of the higher-twist Higgsstrahlung:

$$\left[ \text{Im} f_{el}(\vec{b}, \vec{R} + A\vec{\rho} + B\vec{\sigma}) - \text{Im} f_{el}(\vec{b}, \vec{R} + A\vec{\rho}) \right] - \left[ \text{Im} f_{el}(\vec{b}, \vec{R} + B\vec{\sigma}) - \text{Im} f_{el}(\vec{b}, \vec{R}) \right]$$

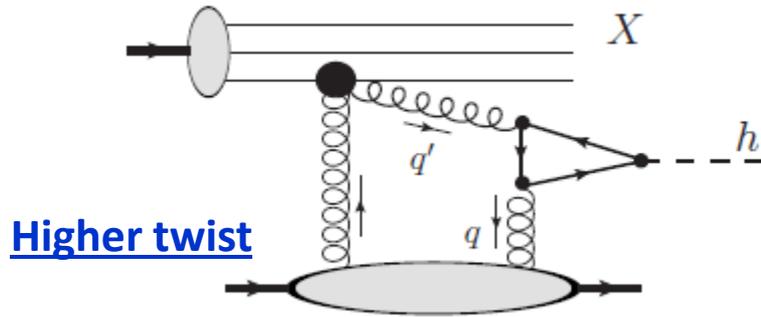
$$\simeq AB \frac{\partial^2 \text{Im} f_{el}(\vec{b}, \vec{x})}{\partial x_i \partial x_j} \Big|_{\vec{x}=\vec{R}} \rho_i \sigma_j,$$

the principal source of diffractive factorisation breaking

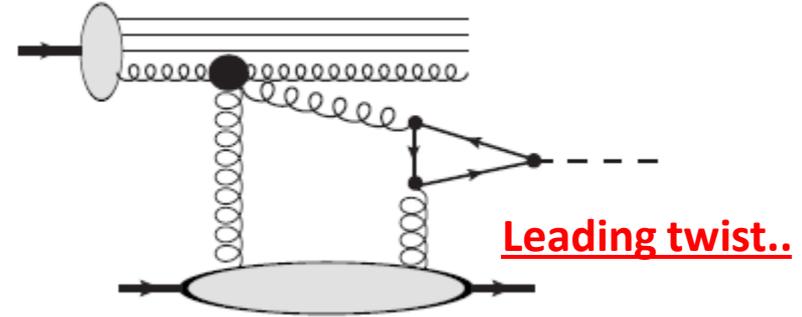
$$\int d^2b \frac{\partial^2 \text{Im} f_{el}(\vec{b}, \vec{x})}{\partial x_i \partial x_j} \Big|_{\vec{x}=\vec{R}} \equiv C_{ij}(\vec{R}), \quad C_{ij}(\vec{R}) = \frac{\sigma_0(s)}{R_0^2(s)} e^{-R^2/R_0^2(s)} \left[ \delta_{ij} - \frac{2R_i R_j}{R_0^2(s)} \right]$$

# Loop-induced single diffractive Higgs: the dipole picture

Diffractive quark excitation:



Diffractive gluon excitation:



**Gluon-gluon fusion via a heavy top loop**

**BUT! ..suppressed in the forward region of large x!**

$$T_{\mu\nu}^f(q, q') \simeq i \frac{\sqrt{\alpha_s}}{2\pi} \frac{1}{v} [(qq')g_{\mu\nu} - q_\mu q'_\nu] G_1^f \left( \frac{M_h^2 + i\epsilon}{4m_f^2} \right) \quad G_1^f \rightarrow 2/3$$

**The cross section**

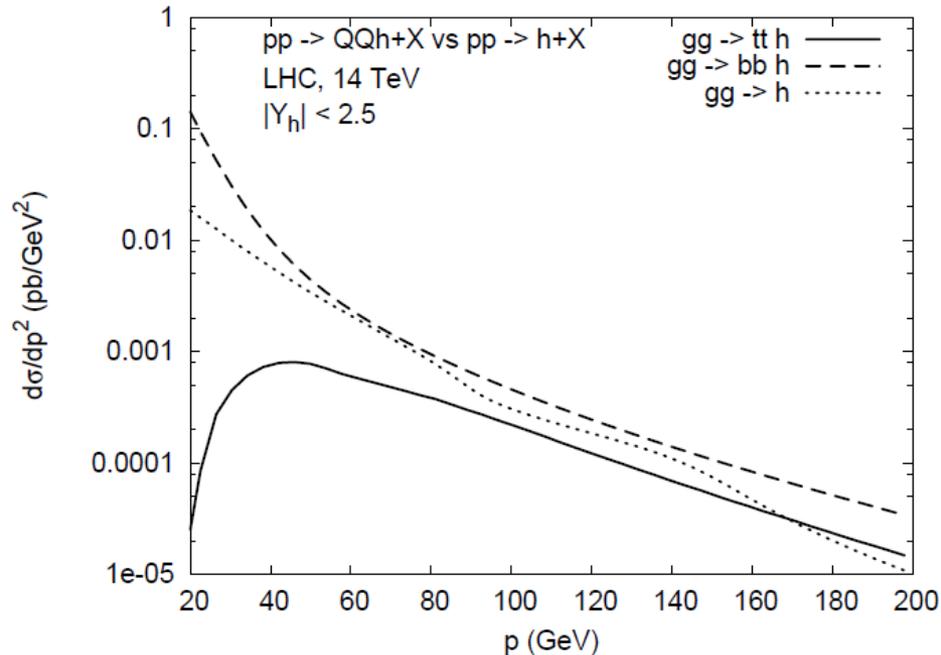
$$\frac{d\sigma_q(pp \rightarrow phX)}{d^2\vec{p} d \ln \alpha d^2\vec{\delta}_\perp} \Big|_{\delta_\perp \rightarrow 0} = \frac{1}{(2\pi)^2} \frac{1}{64\pi^2} \sum_q \int d^2\vec{\omega} d^2\vec{\omega}' dx_q \left[ \rho_q(x_q) + \rho_{\bar{q}}(x_q) \right] \\ \times \Phi_\Delta^q(\alpha, \vec{\omega}) \Phi_\Delta^{q*}(\alpha, \vec{\omega}') \Sigma_\Delta(\alpha, \vec{\omega}) \Sigma_\Delta(\alpha, \vec{\omega}') e^{i\vec{p} \cdot (\vec{\omega} - \vec{\omega}')},$$

**The hard scale**

$$\Sigma_\Delta = \frac{3}{2} \left[ \sigma(\vec{\omega}) - \sigma((1-\alpha)\vec{\omega}) \right] \simeq \frac{3\sigma_0}{2R_0^2} \alpha(2-\alpha)\omega^2 \quad \omega \ll r_{ij} \sim R.$$

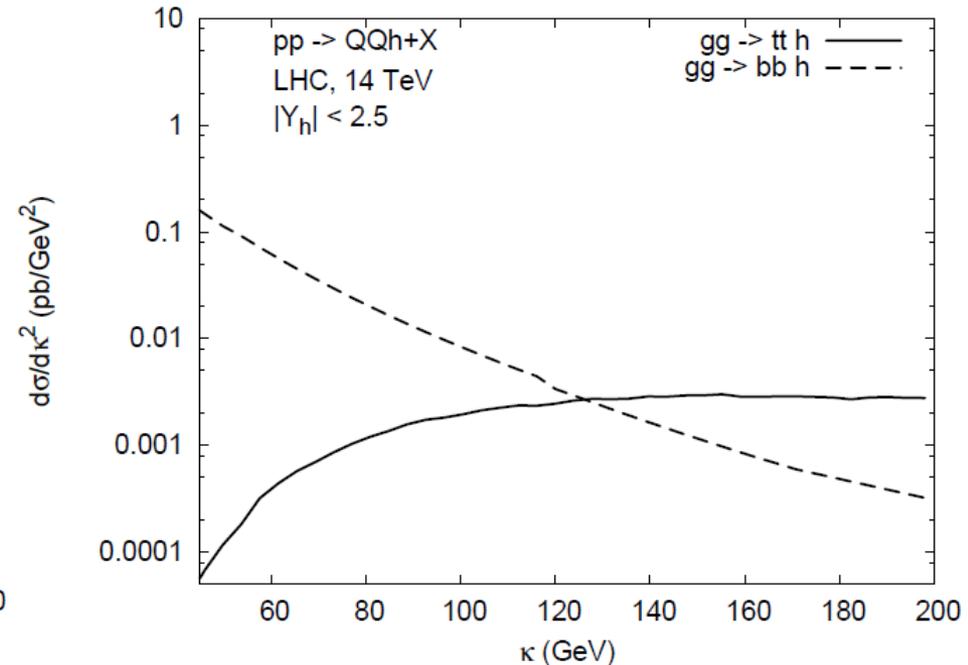
# Inclusive Higgsstrahlung vs loop-induced contribution

## in Higgs transverse momentum



**Higgsstrahlung is important  
at all Higgs  $p_T$ 's!**

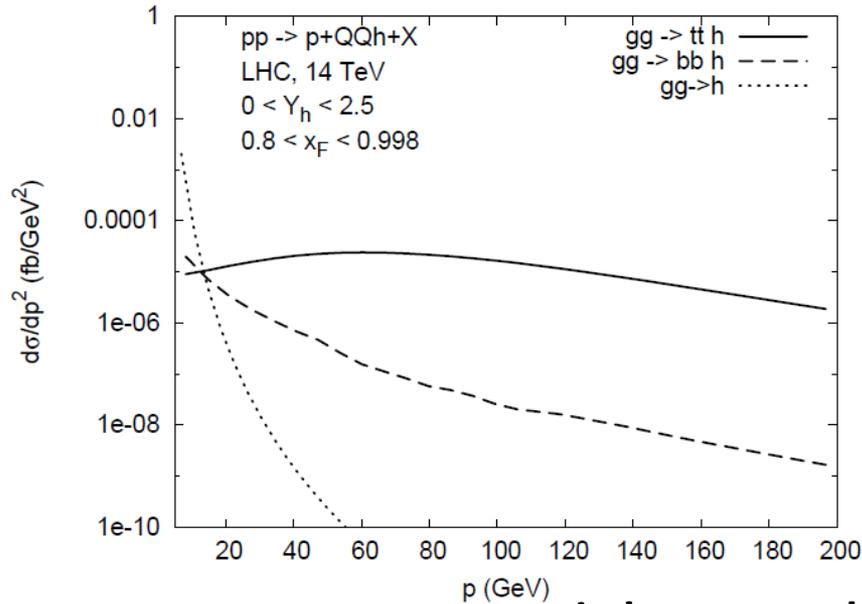
## in heavy quark transverse momentum



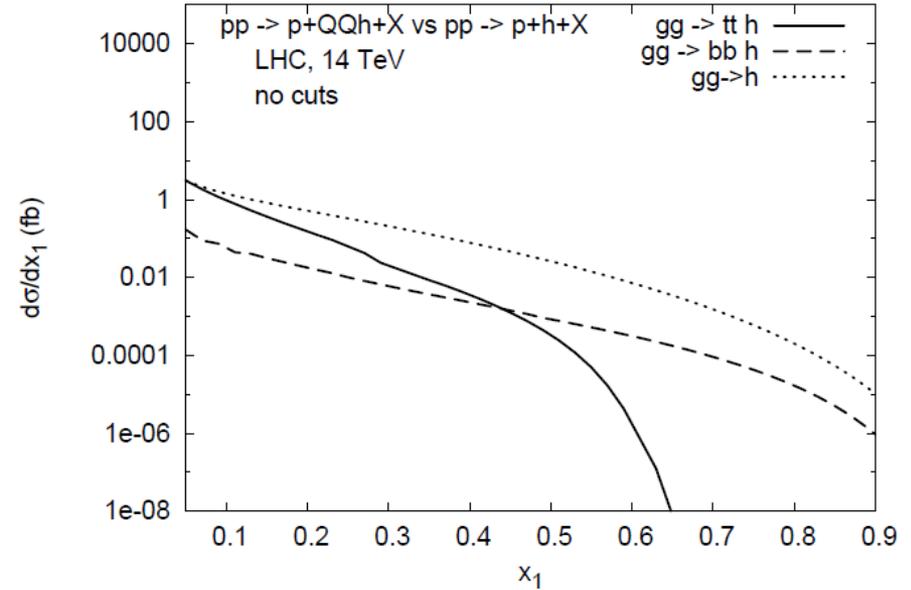
**Higgsstrahlung off top quarks  
dominates at large quark  $p_T$ 's!**

# Single diffractive Higgsstrahlung vs loop-induced contribution

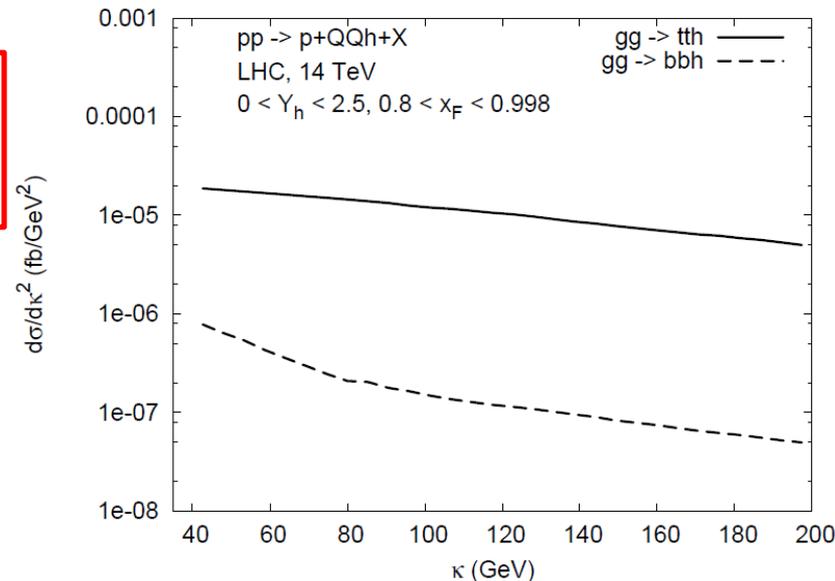
## in Higgs transverse momentum



## in QQh momentum fraction



## in heavy quark transverse momentum



**Diffractive Higgsstrahlung  
off tops dominates  
at Higgs  $p_T > 20$  GeV**

**Loop mechanism dominates  
at large  $x_1$**

# Conclusion

- The diffractive factorisation is **broken by the presence of transverse motion of spectator quarks at large separations**. The same effect is responsible for the absorption.
- Hard/soft interactions and interplay leads to **dominance of leading-twists mechanisms** in the diffractive heavy flavor (DHF) production
- The observation of DHF production **provides a good tool for studies of intrinsic heavy flavors**
- The **diffractive Higgsstrahlung** off heavy quarks is enhanced at large Higgs  $p_T$ 's w.r.t. the loop-induced single diffractive Higgs boson production
- The **major background** for the diffractive Higgsstrahlung comes from  $(t\bar{t})+(b\bar{b})$  final states at large  $Y$ 's is expected to come **multiparton interactions** and needs to be analyzed at the next step