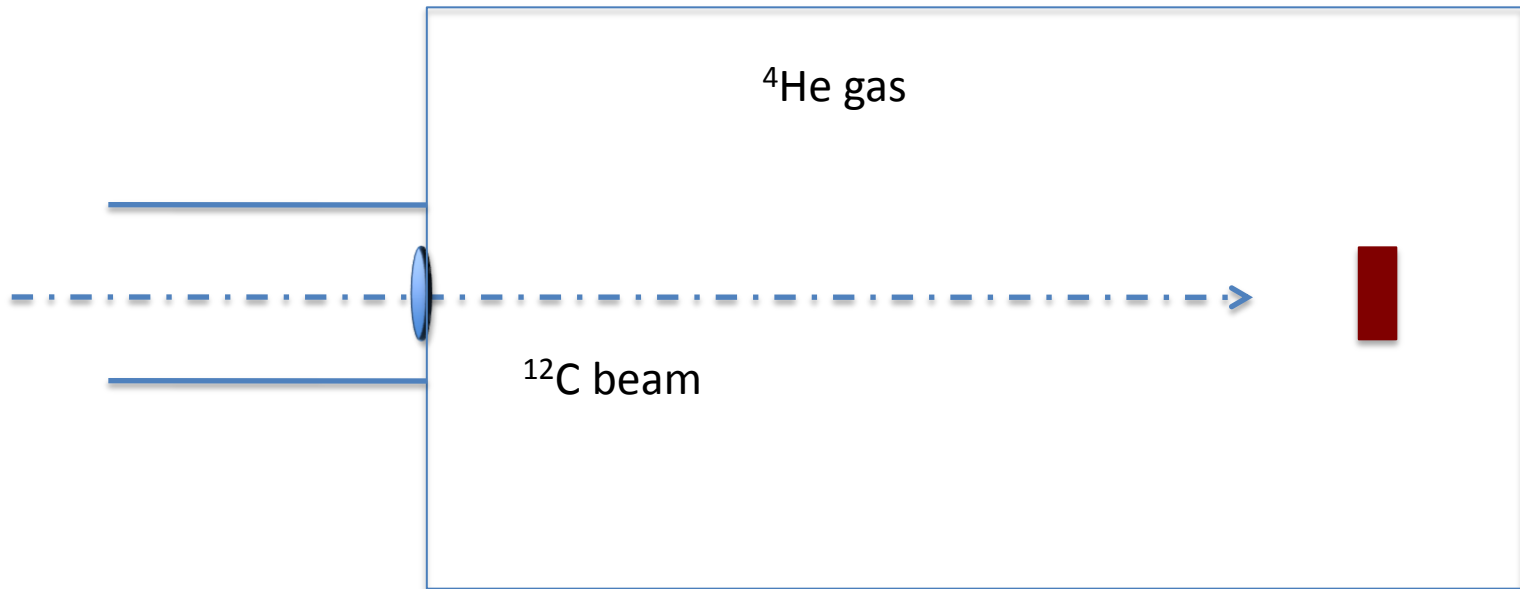


Measurement of cluster states of ^{16}O using the resonant elastic scattering $^{12}\text{C}+^4\text{He}$



Sketch of the set-up. Detector at 0° with respect to the entrance window.

- 1) Define the beam energy in order to study the ^{16}O excitation energy range $8\text{MeV} < E^* < 17\text{MeV}$ knowing that the entrance window that separates the beam line under vacuum from the gas target is made of Havar $2\ \mu\text{m}$ thick.
- 2) Define the gas pressure needed to stop the beam at 500 mm and 1000 mm from the entrance window.
- 3) Knowing that the detector at 0° is placed 100 mm away from where the beam is stopped, estimate if, due to energy and angular straggling, one configuration ($d=500\ \text{mm}$) gives a better resolution than the other ($d=1000\ \text{mm}$).
- 4) Estimate the energy resolution at the maximum measured excitation energy and at the minimum measured excitation energy (the beam energy resolution is negligible with respect to the other effects).

1)

$$Q_{\text{val}} = 2.425 + 4.737 = 7.2 \text{ MeV}$$

$$E^* = E_{\text{c.m.}} + Q$$

For $E^* = 17 \text{ MeV}$ the energy of the beam roughly 40 MeV but to be exact I have to evaluate E_{loss} in the window. I vary the beam energy slightly to have E_{beam} after window to be 40 MeV.

$$E_{\text{loss in Havar}} = 3.3 \text{ MeV}$$

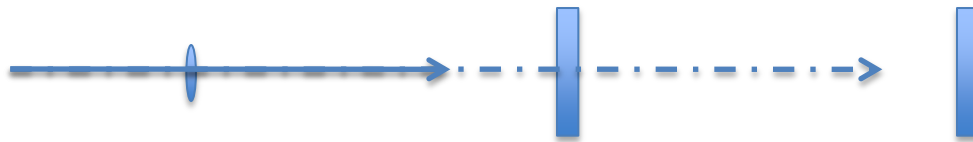
$$\text{Residual energy of } ^{12}\text{C after Havar} = 39.8 \text{ MeV}$$

Due to energy loss of recoiling α s in the gas before reaching the detector the minimum $E_{\text{c.m.}}$ that one can measure corresponds to $E_{\text{lab}} = 2.7 \text{ MeV}$ (energy of recoil α s in the lab = 2 MeV).

Excitation energy explored $8 \text{ MeV} < E^* < 17 \text{ MeV}$

2) Gas pressure to stop 40 MeV ^{12}C in 1000 mm is 320 torr and in 500 mm is 640 torr

3) There is no difference between the two configurations because the number of target nuclei in the two conditions of pressure are the same so there are the same stragglings and energy losses.



4) Energy straggling in the Havar window = $\delta E_{\text{Havar}} = 0.085 \text{ MeV FWHM}$

Angular straggling in the Havar window = 1.2° FWHM

After the gas the energy and angular stragglings are:

$$\delta E = \sqrt{\delta E_{\text{beam}}^2 + \delta E_{\text{Havar}}^2 + \delta E_{\text{gas}}^2} = 0.3 \text{ MeV}$$

$$\delta \theta = \sqrt{\delta \theta_{\text{beam}}^2 + \delta \theta_{\text{Havar}}^2 + \delta \theta_{\text{gas}}^2} = 1.62^\circ$$

Beam energy and angular straggling negligible.

Energy resolution in the c.m. at the minimum energy explored

$$\varepsilon = \frac{\Delta E}{4} \frac{z^2}{Z^2} \frac{m_2}{M} = \frac{\delta E}{4} \frac{4}{36} \frac{4}{16} = \frac{300keV}{144} = 2keV$$

Energy resolution in the c.m. at the maximum energy explored

$$\varepsilon = \frac{\Delta E}{4} \frac{z^2}{Z^2} \frac{m_2}{M} = \frac{\delta E}{4} \frac{4}{36} \frac{4}{16} = \frac{85keV}{144} = 0.59keV$$

We neglect the energy straggling of the α s in the gas

