

You need to measure elastic scattering angular distribution ${}^7\text{Li}+{}^{12}\text{C}$ at $E_{\text{lab}}=100$ MeV.

Define the experimental condition for this measurement :

- 1) Verify if a target thickness of $200 \mu\text{gr}/\text{cm}^2$ is ok for discriminating elastic from inelastic scattering measurement up to 150° .
- 2) Si-Detector thicknesses (verify if a $15 \mu\text{m}$ ΔE detector is ok for your purposes)
- 3) Angular resolution (target angular straggling, beam emittance)

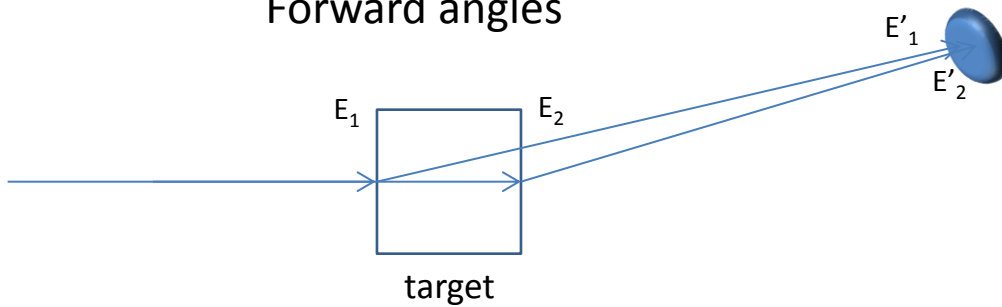
Knowing that:

- 1) You need to separate elastic scattering from the inelastic excitation of ${}^7\text{Li}$ ($E_x=0.48$ MeV)
- 2) You need to identify ${}^7\text{Li}$ using a ΔE -E technique (choose ΔE thickness). Detection threshold 0.5 MeV.
- 3) Your beam transverse emittance is $\Delta\phi\Delta\theta=1/\beta \pi\text{mm.mrad}$ ($\gamma=1$) and the beam spot size is 3mm .
- 4) You have to design a collimation system to limit your angular resolution at forward angles to 0.2° knowing that the distance between the collimators is 1 m.
- 5) You want to measure at very large angles $\theta \approx 150^\circ$.

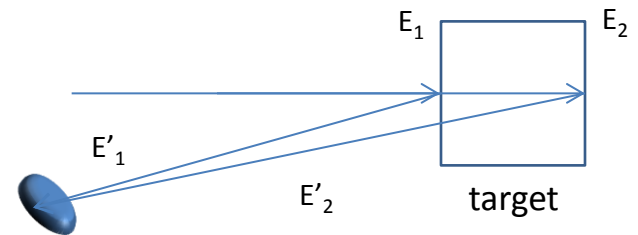
Use LISE++

Remember that:

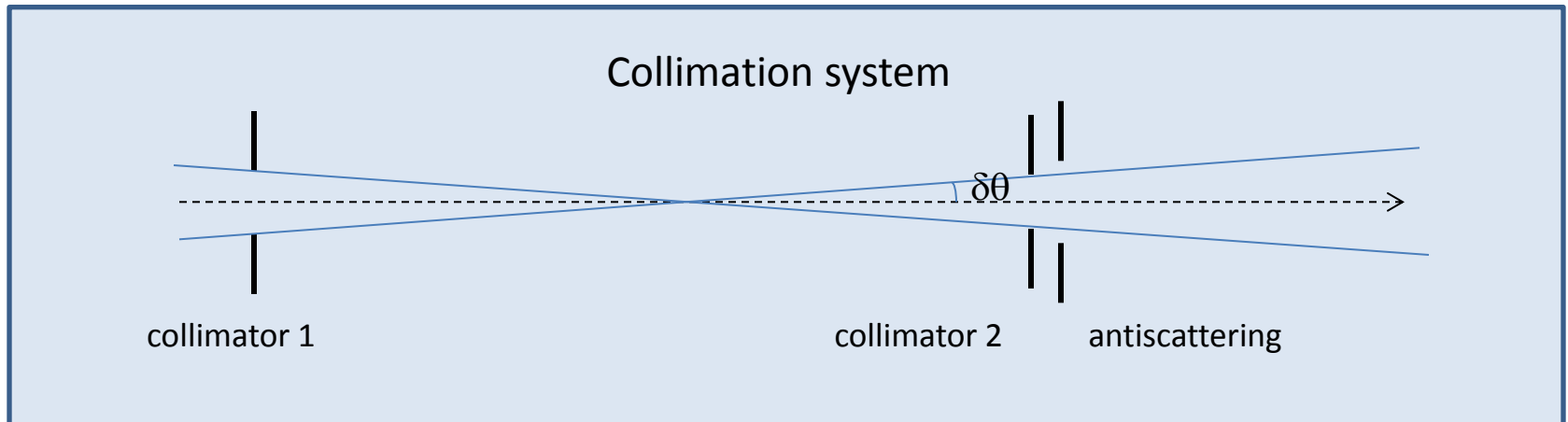
Forward angles



Backward angles



Normalised beam emittance $\Delta\phi\Delta\theta = \varepsilon/\beta\gamma = 1 \pi \text{ mm.mrad}$



At forward angles the ${}^7\text{Li}$ beam energy is around 100 MeV \rightarrow need to choose a ΔE detector thickness where the energy deposited by the ${}^7\text{Li}$ is sufficiently above the detection threshold.

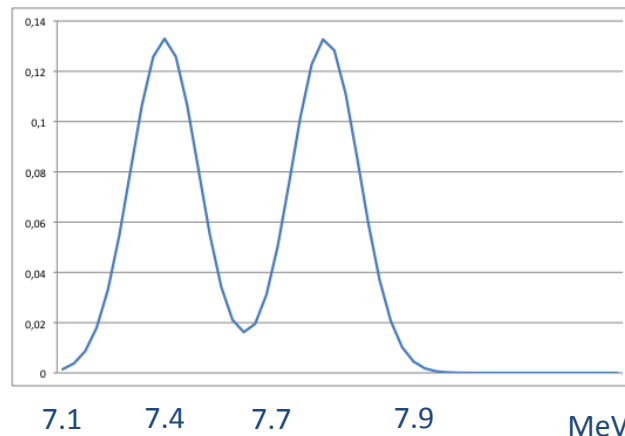
For $\Delta E=15 \mu\text{m}$ $E_{\text{loss}}({}^7\text{Li } 100\text{MeV}) \approx 900 \text{ keV}$

$E_{\text{loss}}({}^7\text{Li } 8 \text{ MeV from kinematics}) \approx 5.7 \text{ MeV}$ $E_{\text{residual}}=2.3 \text{ MeV}$

Target thickness $200 \mu\text{gr}/\text{cm}^2$ E_{loss} in target at 150° to be evaluated if you energy resolution is an issue.

Condition 1: no beam energy loss E given by kinematics $\rightarrow E_{7\text{Li}}=7.91 \text{ MeV}$

Condition 2: E_{loss} of the beam in the whole target \rightarrow kinematics $\rightarrow E_{\text{loss}}$ of particle in the target thickness $t/\cos(\pi-\theta)= 0.250 \text{ MeV}$



Beam emittance:

$$\varepsilon = 1/\beta\gamma \pi \text{ mm.mrad} \quad \beta = \sqrt{\frac{2E}{m}} = \sqrt{\frac{2 \times 100 \text{ MeV}}{7 \times 931 \text{ MeV}}} = 0.175$$

$$\varepsilon = \frac{1}{0.175} = 5.71\pi \text{ mm.mrad}$$

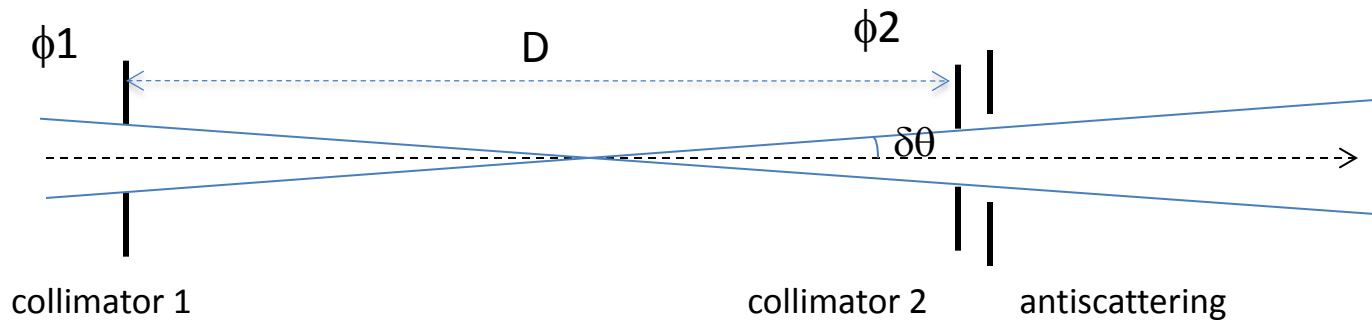
$$\Delta\phi\Delta\theta = 5.71\pi \text{ mm.mrad}$$

$$\Delta\theta = \frac{5.71\pi}{3} \text{ mrad} = 5.97 \text{ mrad} = 0.34^\circ$$

$$\delta\theta = \sqrt{\delta\theta_{beam}^2 + \delta\theta_{straggling}^2}$$

Target angular straggling at forward angles $\delta\theta \approx 0.05^\circ$ FWHM

Target angular straggling at $\theta = 150^\circ$ $\delta\theta \approx 0.6^\circ$ FWHM



ϕ_1 = diameter of collimator 1

ϕ_2 = diameter of collimator 2

D = distance between the two collimators = 1000 mm

$\delta\theta = 0.2^\circ$

$$\frac{1}{2}(\phi_1 + \phi_2) = D \sin \delta\theta = 3.5 \text{ mm} \quad \text{If you want a beam spot of 3 mm} \rightarrow \phi_2 = 3, \phi_1 = 4$$