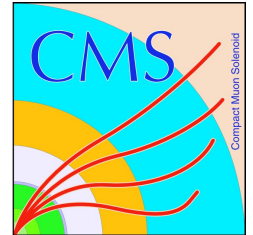


Status of and prospects for W mass and Z mass measurements



Stefano Camarda

On behalf of the
CMS and ATLAS
Collaborations

Physics at LHC and beyond
Qui-Nhon, Vietnam
10-17 August 2014

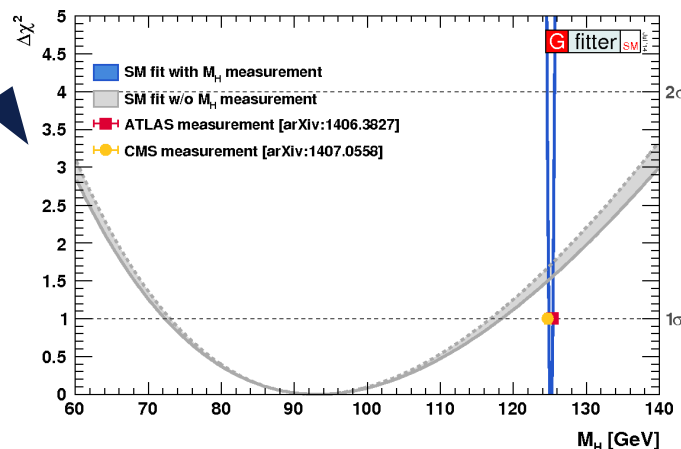


Motivation

The EW sector of the SM, relates M_W to α , G_F , and $\sin^2\theta_w$

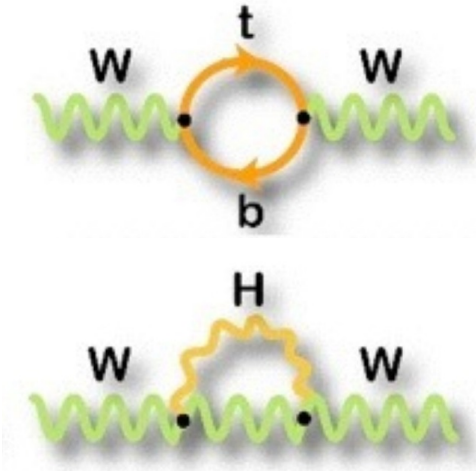
$$M_W^2 = \frac{\pi \alpha_{EM}}{\sqrt{2} G_F (1 - M_W^2/M_Z^2) (1 - \Delta r)}$$

- The relation between M_{top} , M_H and M_W provides a stringent test of the SM
- The comparison between the measured M_H and the predicted M_H is sensitive to new physics

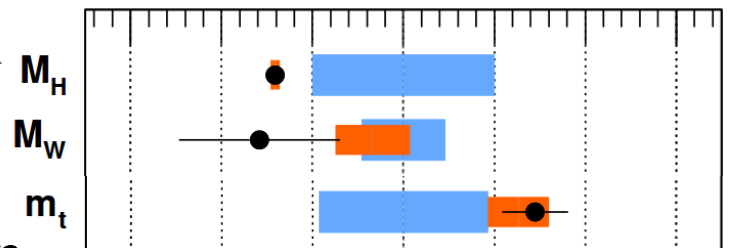


Indirect determination of M_W (± 8 MeV) is more precise than the experimental measurement

Radiative corrections Δr are dominated by Top and Higgs loops



Global EW fit
Indirect determination
Measurement [arXiv:1407.3792](https://arxiv.org/abs/1407.3792)



Call for $\delta M_W^{\text{exp}} < 10$ MeV

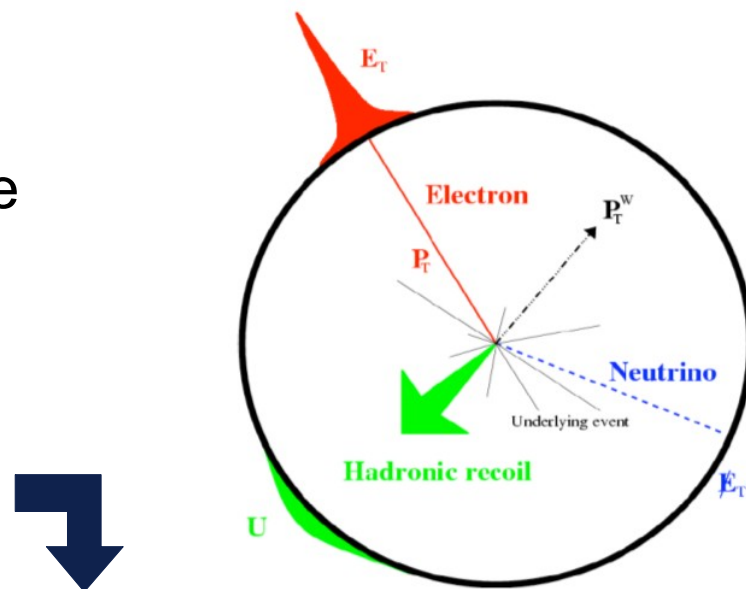
Status and prospects for W mass measurement

- Methodology for the M_W extraction
- The Tevatron experience on M_W
- Measurements of M_W and M_Z at the LHC
- Theoretical uncertainties for M_W at the LHC
- ATLAS and CMS measurements to constrain uncertainties on M_W
- Prospect for M_W and M_Z measurements at future colliders

Methodology for the W mass extraction

- Event selection: W leptonic decay
 $W \rightarrow l \nu$, $l = e, \mu$
- The full kinematic of the W decay cannot be reconstructed, since the longitudinal momentum of the neutrino is unknown

Traditional analyses are based on a template fit extraction from observables sensitive to M_W



Lepton transverse momentum

$$p_T^l$$

W transverse mass

$$M_T = \sqrt{2 \cdot p_T^l p_T^\nu \cdot (1 - \cos \Delta\phi(l, \nu))}$$

Neutrino transverse momentum
(from hadronic recoil)

$$p_T^\nu$$

More sophisticated analysis techniques suggest simultaneous measurements of W and Z observables

TS2008-022

Eur.Phys.J. C69 (2010) 379-397



In the same spirit, a common strategy of template fits analyses is to use $Z \rightarrow ll$ events to constraint both experimental and theory systematics

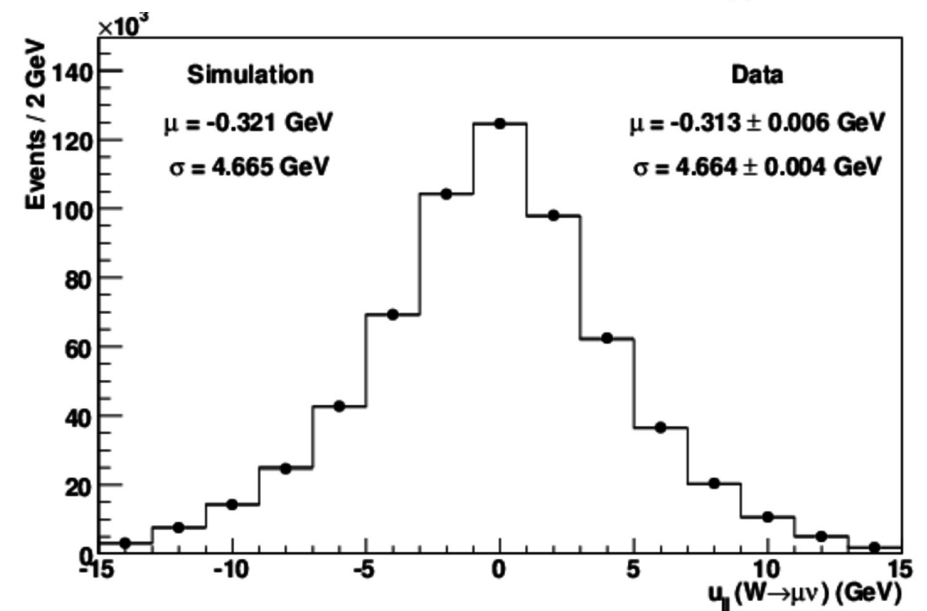
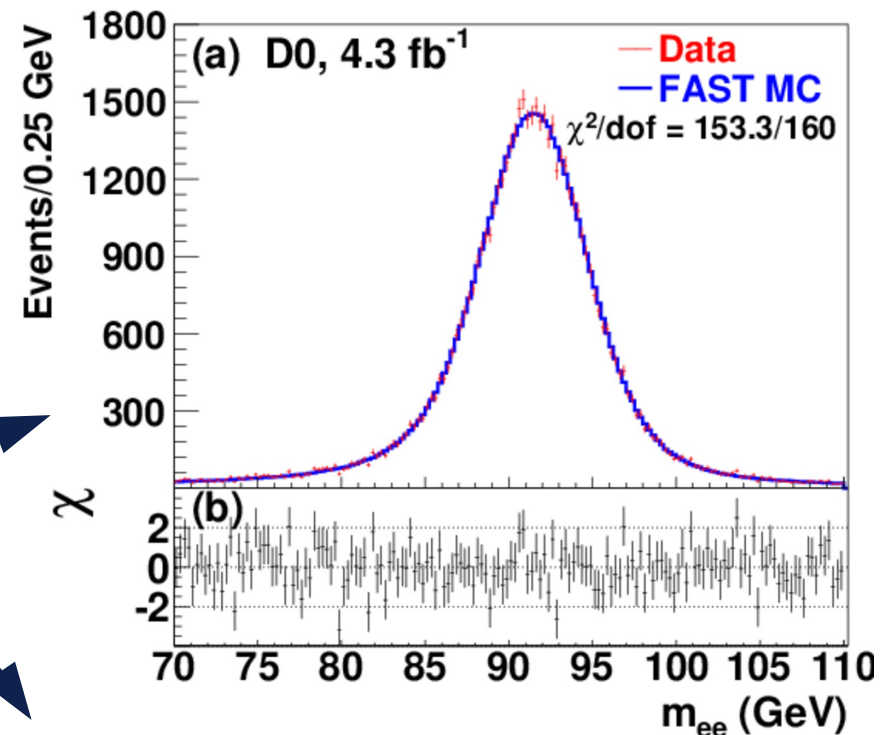
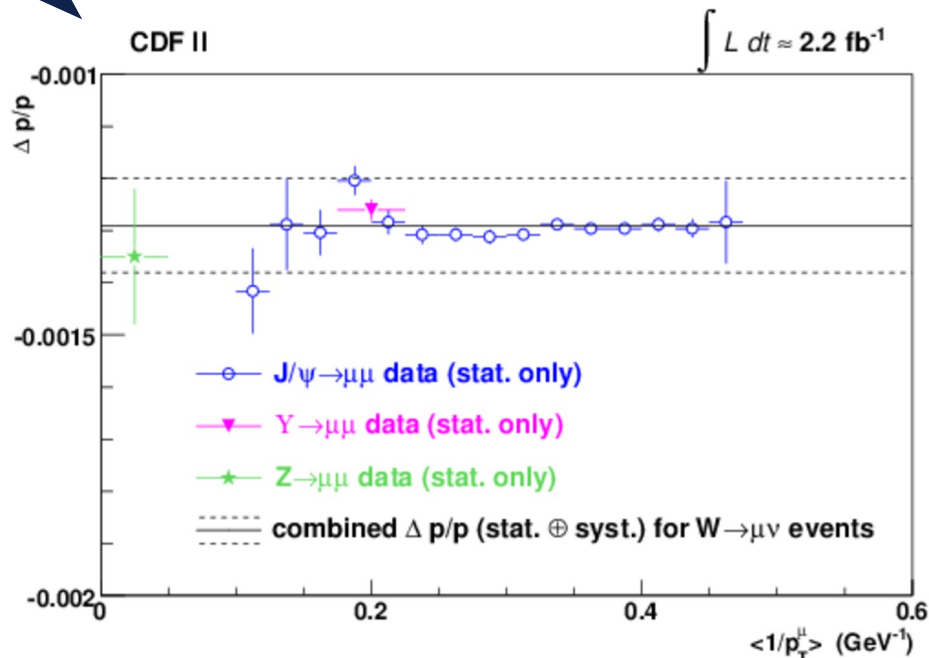
Tevatron measurements of M_W - Methodology

Phys. Rev. D 89, 072003 (2014)

Phys. Rev. D 89, 012005 (2014)

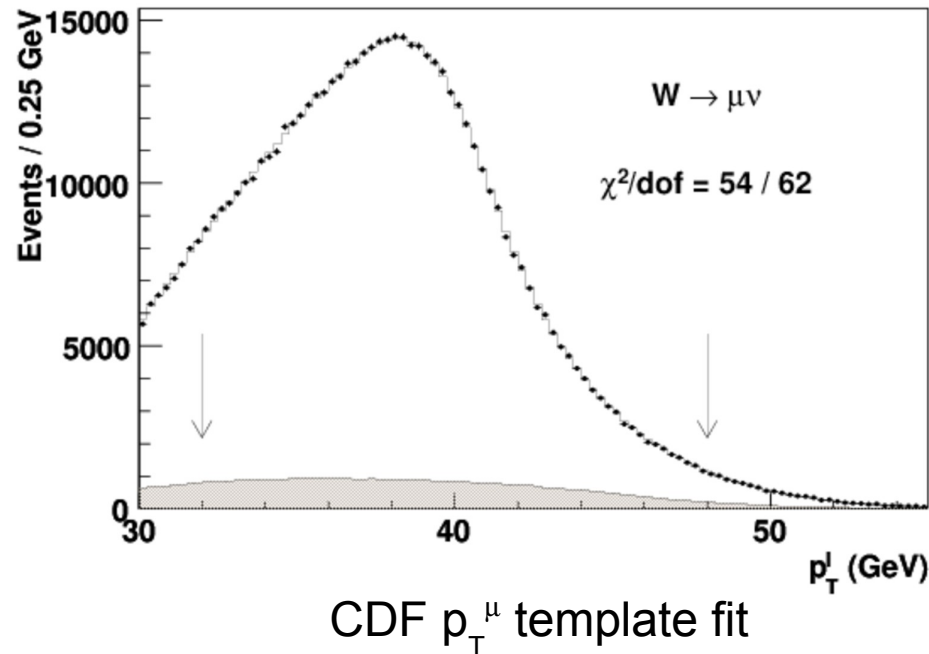
Detector calibrations:

- Muon momentum scale
→ Calibration of the track curvature in the drift chamber
- Electron energy scale
→ Calorimeter calibration
- Neutrino transverse momentum
→ Hadronic recoil calibration



Tevatron measurements of M_W - Results

CDF

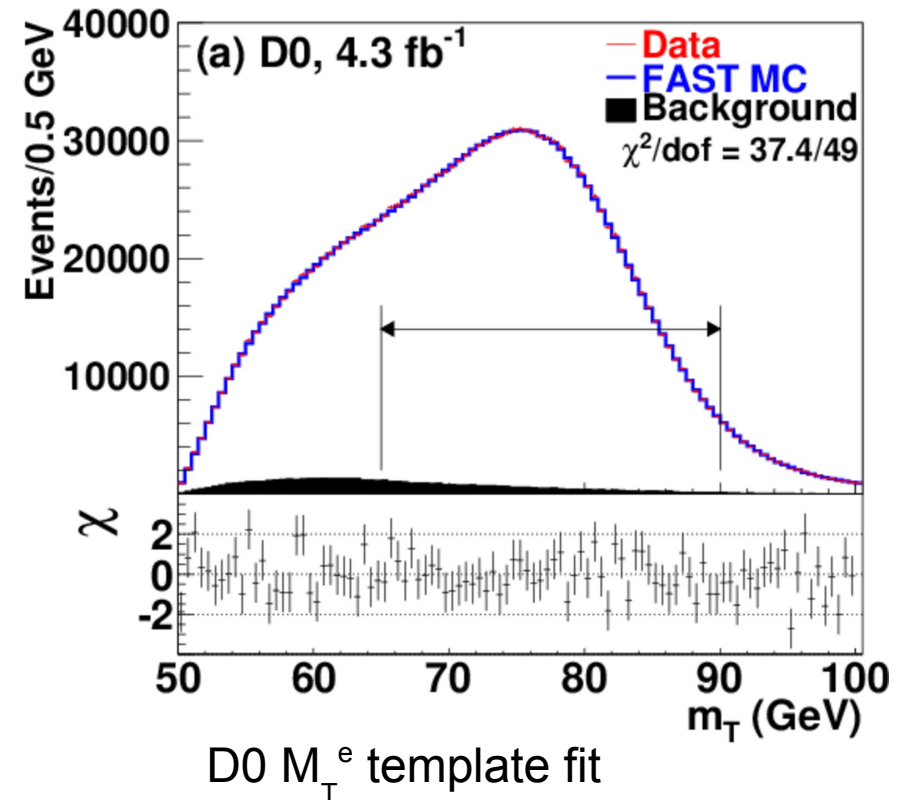


M_W extracted from p_T^l , M_T , p_T^ν
in electron and muon channels
 $L = 2.2 \text{ fb}^{-1}$

$$M_W = 80.387 \pm 19 \text{ MeV}$$

Phys. Rev. D 89, 072003 (2014)

D0



M_W extracted from p_T^l , M_T
in electron channel
 $L = 4.3 (+1) \text{ fb}^{-1}$

$$M_W = 80.375 \pm 23 \text{ MeV}$$

Phys. Rev. D 89, 012005 (2014)

W mass measurement at the LHC

- The M_W measurement at the LHC follows a strategy similar to the Tevatron
- Important differences:
 - Higher pile-up environment → affect hadronic recoil calibration
 - Potentially larger theoretical uncertainties due to pp instead of $p\bar{p}$ collisions
 - W^+ and W^- production is not symmetric → Require a charge dependent analysis

Most precise observables for the M_W extraction

p_T^l	M_T
Observable does not depend on hadronic recoil, smaller experimental uncertainty	Depends on hadronic recoil measurement, expected larger experimental uncertainties
Larger theory uncertainty due to higher order QCD, p_T^W modelling, PDF, W polarisation, charm mass	M_T is quite stable wrt perturbative QCD corrections, smaller PDF uncertainties, smaller non-perturbative QCD uncertainties



M_W extraction is likely to be limited by **theoretical uncertainties**



Final balance between theory and exp uncertainties will depend on pile-up mitigation algorithms

Z mass measurement at the LHC

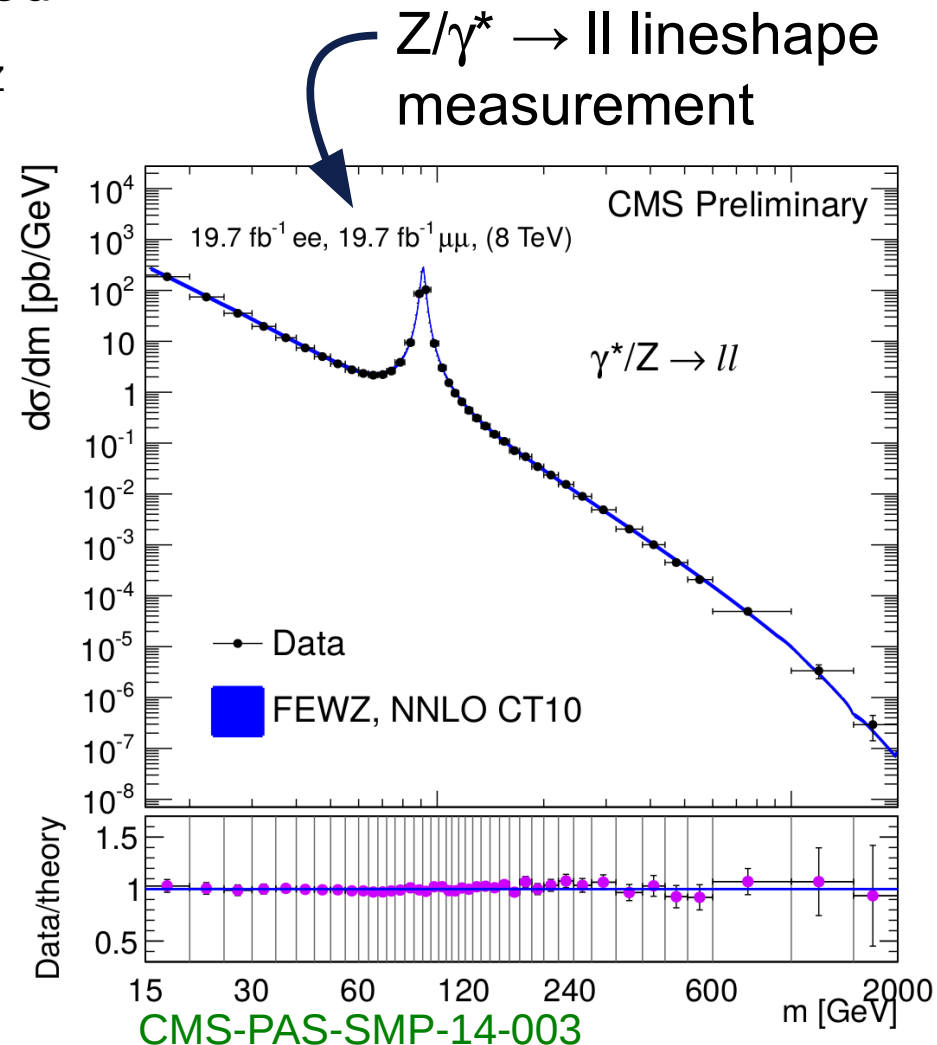
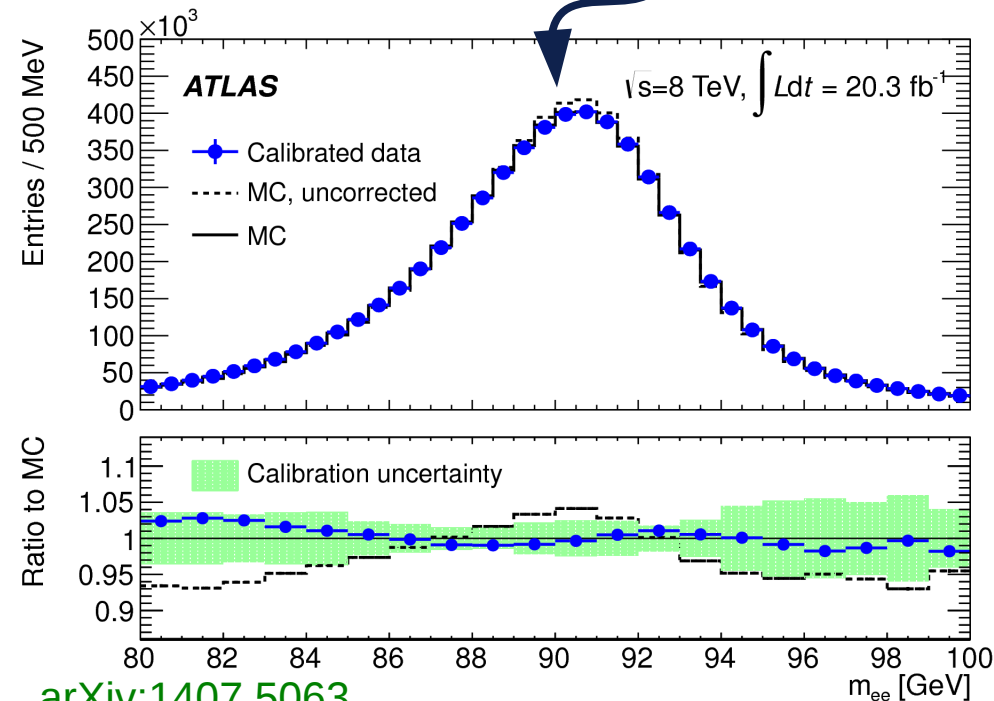
A first step towards the measurement of M_W at the LHC is the measurement of M_Z



Test the methodology of the M_W extraction:
→ Neglect one of the two leptons, extract M_Z from p_T and hadronic recoil

The lepton energy scale is calibrated by comparing the reconstructed M_Z to the LEP measurement of M_Z

Electron calibration from $Z \rightarrow ee$ invariant mass



Theory systematics for M_W at the LHC



Why theory systematic uncertainties are crucial for the W mass measurement at the LHC?

W production at the LHC is relatively cheap
 $7(8) \text{ TeV}, 5(20) \text{ fb}^{-1} \rightarrow \sim 15(75) \times 10^6$
in $W \rightarrow l\nu$ ($l = e, \mu$)



- Statistics is not an issue
→ expected $\sim 6(2) \text{ MeV}$
statistical uncertainty on M_W

- Main experimental systematic uncertainties
 - Lepton energy scale, resolution, efficiency
 - hadronic recoil scale and resolution

Estimates depend on the analysis strategy:
between 5-15 MeV

Theory uncertainties at the
Tevatron: 10-15 MeV
Expected similar or higher
uncertainties at the LHC

Eur.Phys.J.C57:627-651,2008 TS2008-022

Constrain M_W theory uncertainties at the LHC

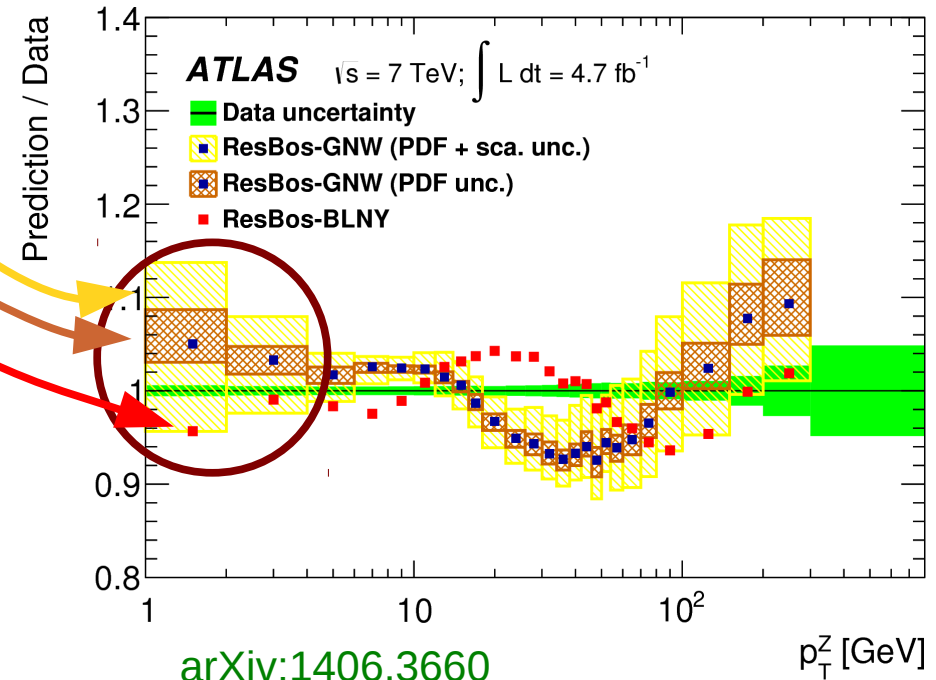
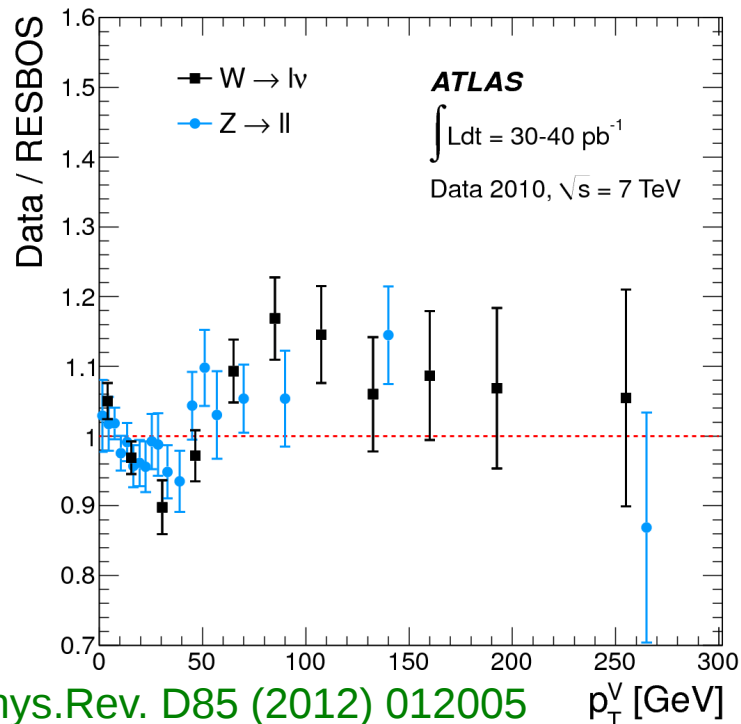
ATLAS and CMS are performing measurements of alternative W, Z observables to control the theoretical models and reduce the uncertainties on the measurement of M_W

Theory uncertainties	Measurements which can provide constraints to the theoretical models
p_T^W modelling	p_T^W, p_T^Z
PDF	W asymmetry, Z rapidity, W + charm
W polarization	Angular coefficients in W, Z production

p_T^W and p_T^Z modelling

Theory uncertainties at low W, Z p_T

- Factorization, renormalization, resummation or PS scales
- PDF, low x gluon PDF
- Non perturbative QCD parameters
- Strong-interaction coupling $\alpha_s(M_Z)$
- Heavy flavour masses, HF thresholds in the PDF



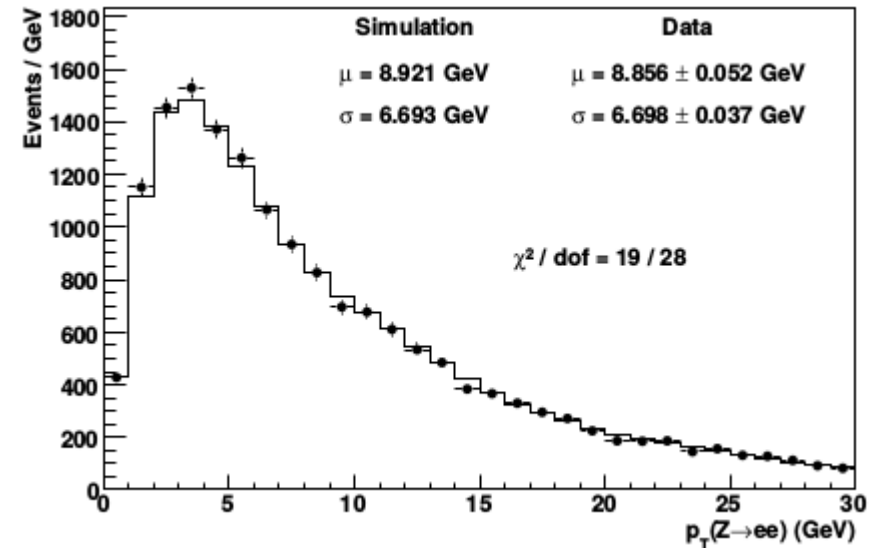
- Measurement of p_T^W is less precise in the low p_T region
- However it provides an important cross check

Constraining p_T^W and p_T^Z theory uncertainties

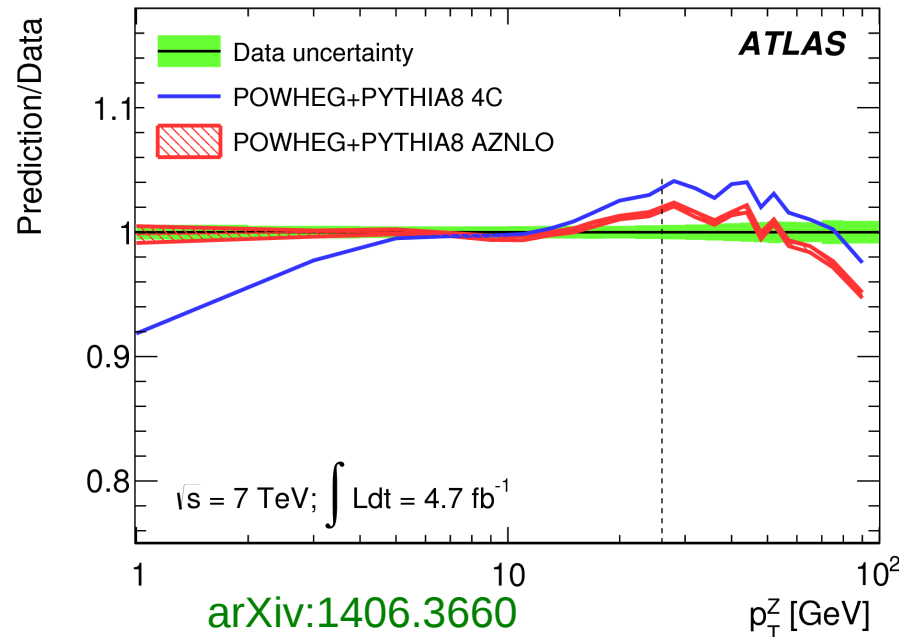
CDF W mass measurement

- RESBOS used to model $p_T^{W,Z}$
- Fit non-pQCD parameter g_2 and α_s to p_T^Z data
- Uncertainties propagated to M_W
3, 9, 4, MeV for M_T , p_T^l , p_T^{ν}

$$S = \left[g_1 - g_2 \log \left(\frac{\sqrt{\hat{s}}}{2Q_0} \right) - g_1 g_3 \log(100x_j x_k) \right] b^2$$



Phys. Rev. D 89, 072003 (2014)

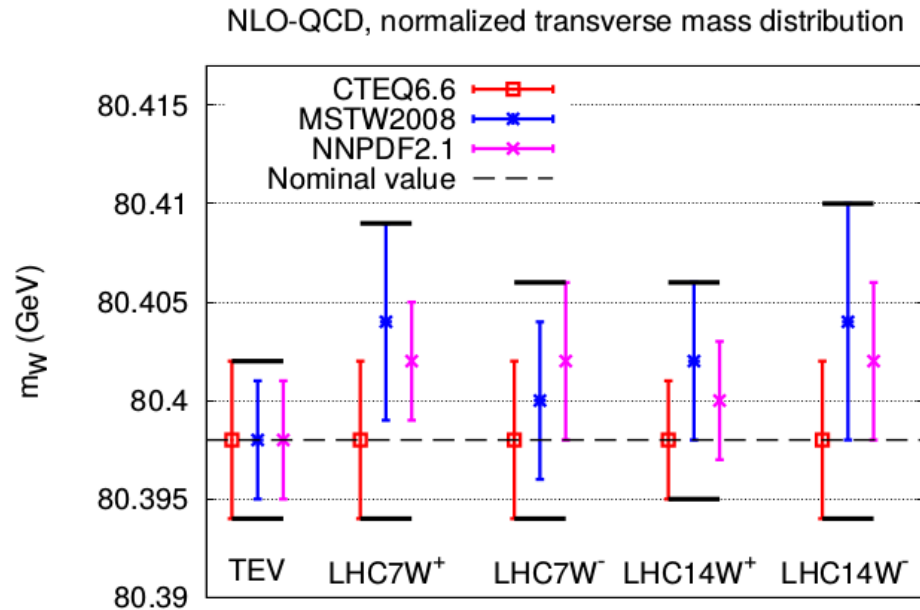


ATLAS

- POWHEG+PYTHIA8 model
- Fit non-pQCD parameters primordial k_T and ISR cut-off to p_T^Z data

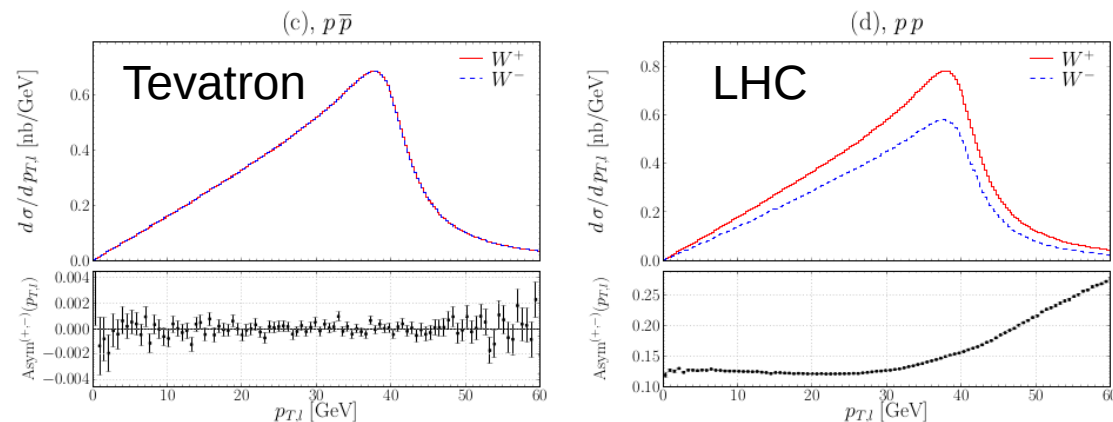
PDF uncertainties

PDF uncertainties on M_W extraction from M_T (DYNNLO) [Phys.Rev.D83:113008,2011](#)
[arXiv:1309.1311](#)



- Normalised distribution are essential to reduce PDF uncertainties
- PDF uncertainties are expected to be larger at the LHC than at the Tevatron, and different between W^+ and W^-
- Estimated small α_s and m_c uncertainties

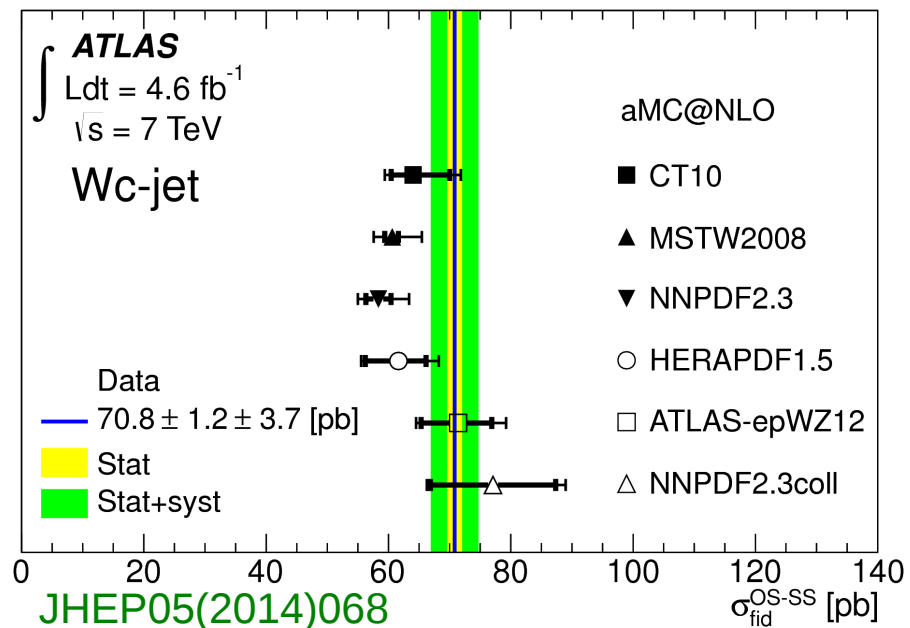
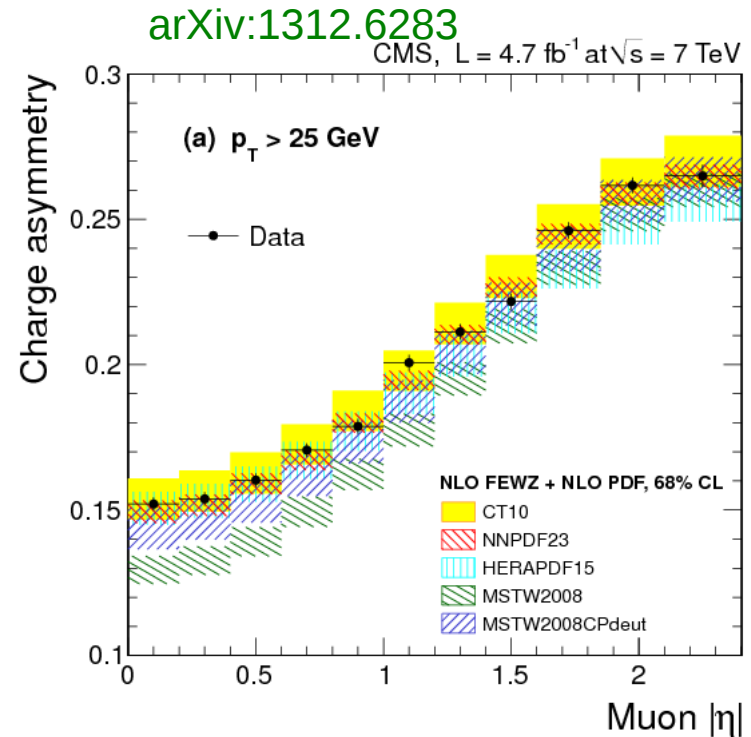
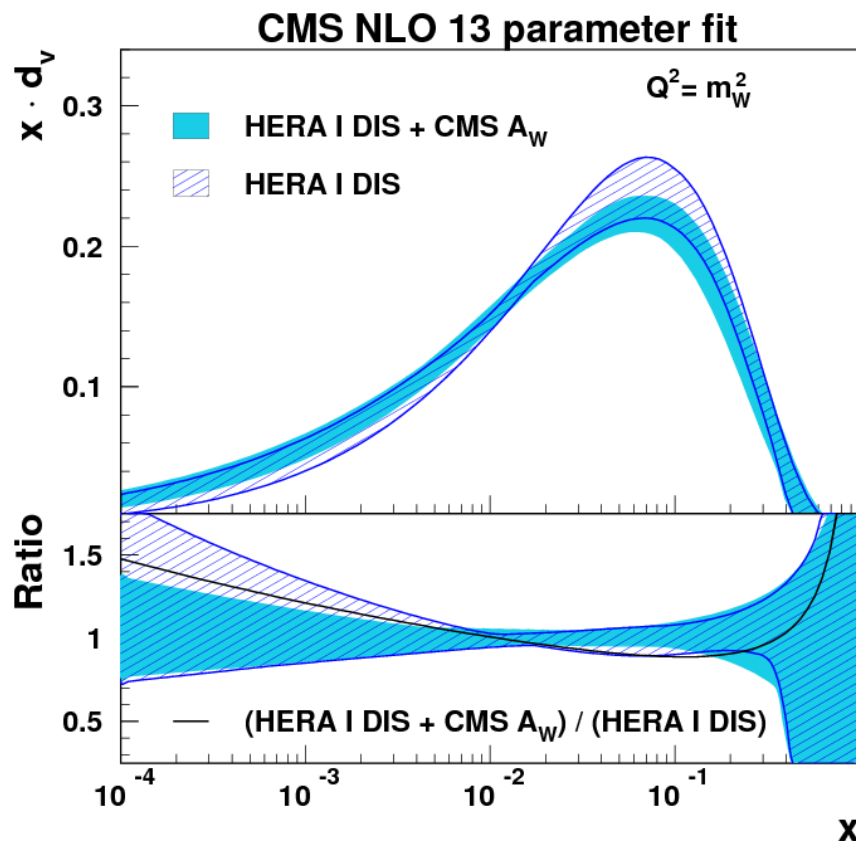
- pp collision \rightarrow no symmetry between W^+ and W^- lepton p_T due to $u_v \neq d_v$ and W polarization \rightarrow Larger PDF uncertainties at LHC than Tevatron
- At the LHC, a charge-dependent separate analysis of W^+ and W^- helps to reduce PDF uncertainties



[Eur.Phys.J. C69 \(2010\) 379-397](#)

PDF uncertainties

- Crucial to reduce the valence PDF uncertainty
- The strange PDF uncertainty could be large for the M_W extraction from p_T^l
- ATLAS and CMS have provided several measurements of W, Z inclusive and W+charm, which can constrain PDF uncertainties



W, Z polarization

- Set of 8 observables: angular coefficients
 $A_i \rightarrow$ ratio of helicity cross sections
- A_i are functions of the leptons kinematic $A_i(p_T^\parallel, y^\parallel, M^\parallel)$
- A_i coefficients can be calculated from MC sample with moments method

$$\langle m \rangle = \frac{\int d\sigma(p_T, y, \theta, \phi) m d\cos\theta d\phi}{\int d\sigma(p_T, y, \theta, \phi) d\cos\theta d\phi}$$

- A_i can be measured precisely for Z, the W measurement is more challenging

- Related to boson polarization, V-A coupling
- Provide insight into QCD and EW dynamics
- Stringent test of predictions and MC generators

- A_0 - A_4 coefficients measured at CDF
- Precise measurements at the LHC of A_0 - A_7 can discriminate between different predictions

$$\frac{dN}{d\Omega} \propto \boxed{(1 + \cos^2 \vartheta)} +$$

$$A_0 \frac{1}{2} (1 - 3 \cos^2 \vartheta) +$$

$$A_1 \sin 2\vartheta \cos \varphi +$$

$$A_2 \frac{1}{2} \sin^2 \vartheta \cos 2\varphi +$$

$$A_3 \sin \vartheta \cos \varphi +$$

$$A_4 \boxed{\cos \vartheta} +$$

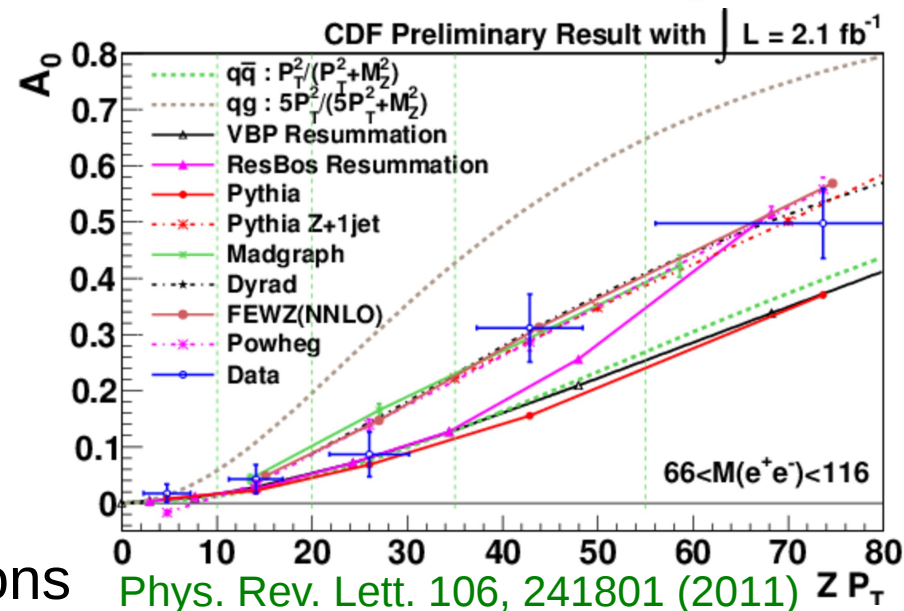
$$A_5 \sin^2 \vartheta \sin 2\varphi +$$

$$A_6 \sin 2\vartheta \sin \varphi +$$

$$A_7 \sin \vartheta \sin \varphi .$$

LO terms

Phys.Rev. D50 (1994) 5692
 Nucl.Phys. 387 (1992) 3



Prospects for M_W at ILC and TLEP

M_W can be measured at e^+e^- colliders through an energy scan of the WW production threshold

Near threshold, the WW cross section is proportional to the non-relativistic W velocity

$$\sigma(WW) \propto \beta_W$$

arXiv:1306.6352

ILC Giga-Z program

- Energy scan 160 to 170 GeV
- $\delta M_W = 6-7$ MeV

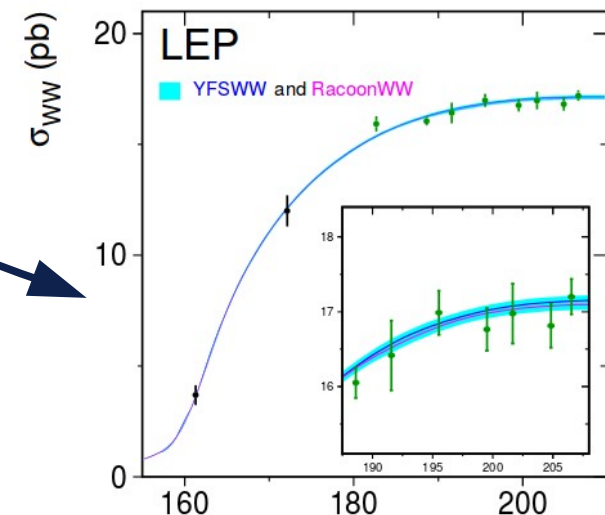
JHEP 1401 (2014) 164

TLEP OkuW program

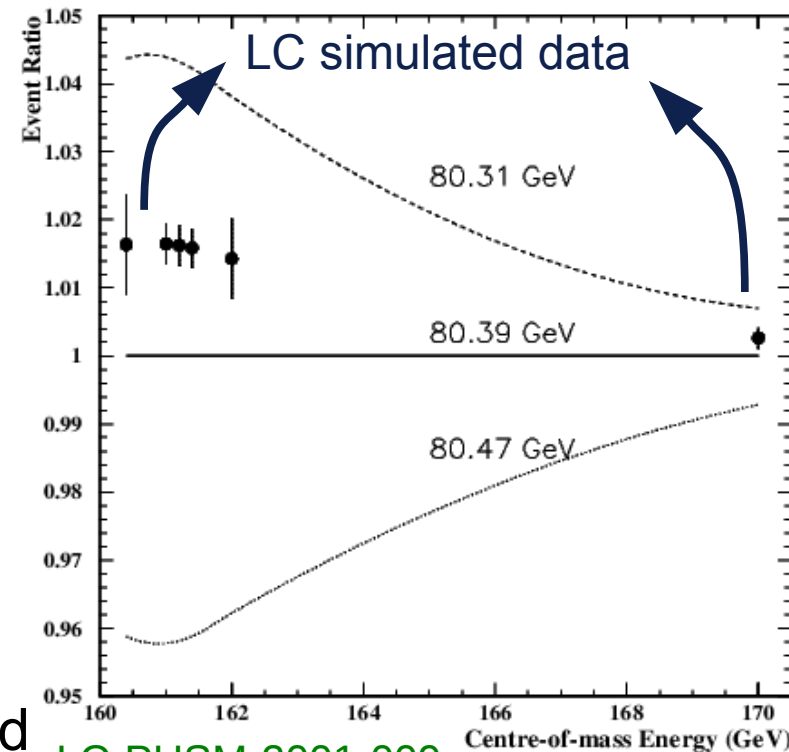
- $\delta M_W = 0.5$ MeV
- dominated by statistical uncertainty

Dominant theory uncertainties

- Initial state QED corrections
- Parametrization of cross section near threshold



Phys.Rept. 532 (2013) 119-244



LC-PHSM-2001-009

Prospects for M_Z at TLEP

- TeraZ program: 7×10^{11} visible Z in one year of data taking at 91 GeV

M_Z extracted from Z lineshape

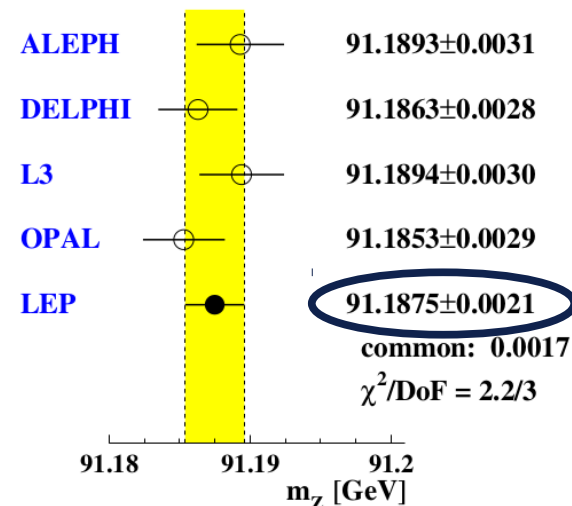
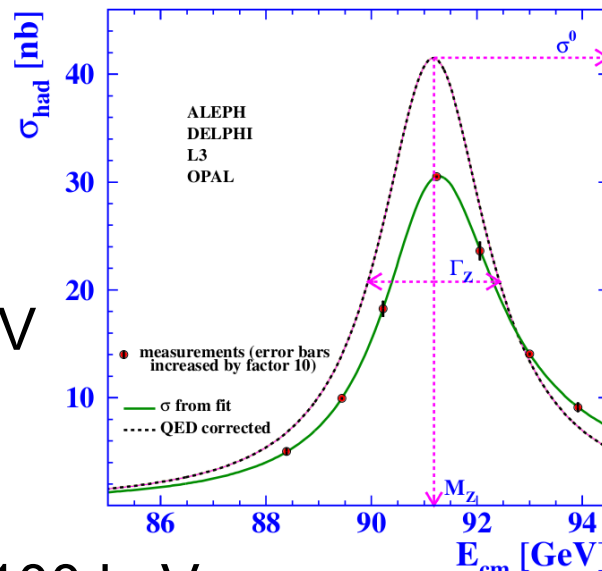
- Statistical uncertainty: 5 keV
- Systematic uncertainty: 100 keV
→ dominated by beam energy calibration

Dominant theory uncertainties

- Initial state QED corrections ≤ 100 keV
- Additional lepton pairs ≤ 300 keV
- Lineshape parametrization ≤ 100 keV
→ Need to revisit theory predictions

JHEP 1401 (2014) 164

Phys.Rept.427:257-454,2006



Factor of 20 improvement
wrt LEP M_Z measurement

Quantity	Physics	Present precision	Measured from	Statistical uncertainty	Systematic uncertainty	Key	Challenge
m_Z (keV)	Input	91187500 ± 2100	Z Line shape scan	5 (6) keV	< 100 keV	E_{beam} calibration	QED corrections
Γ_Z (keV)	$\Delta\rho$ (not $\Delta\alpha_{\text{had}}$)	2495200 ± 2300	Z Line shape scan	8 (10) keV	< 100 keV	E_{beam} calibration	QED corrections
R_ℓ	α_s, δ_b	20.767 ± 0.025	Z Peak	0.00010 (12)	< 0.001	Statistics	QED corrections
N_ν	PMNS Unitarity, ...	2.984 ± 0.008	Z Peak	0.00008 (10)	< 0.004		Bhabha scat.
N_ν	... and sterile ν 's	2.92 ± 0.05	$Z_\gamma, 161$ GeV	0.0010 (12)	< 0.001	Statistics	
R_b	δ_b	0.21629 ± 0.00066	Z Peak	0.000003 (4)	< 0.000060	Statistics, small IP	Hemisphere correlations
A_{LR}	$\Delta\rho, \epsilon_3, \Delta\alpha_{\text{had}}$	0.1514 ± 0.0022	Z peak, polarized	0.000015 (18)	< 0.000015	4 bunch scheme, 2exp	Design experiment
m_W (MeV)	$\Delta\rho, \epsilon_3, \epsilon_2, \Delta\alpha_{\text{had}}$	80385 ± 15	WW threshold scan	0.3 (0.4) MeV	< 0.5 MeV	E_{beam} , Statistics	QED corrections
m_{top} (MeV)	Input	173200 ± 900	$t\bar{t}$ threshold scan	10 (12) MeV	< 10 MeV	Statistics	Theory interpretation

Summary

- The indirect determination of M_W from the global fit of the SM parameters calls for a target precision of 10 MeV on the measurement of M_W
- For the measurement of the W mass at the LHC it is necessary to control and reduce many sources of experimental and theoretical uncertainties
- A first step towards the measurement of M_W is the lepton calibration, and the validation of the analysis techniques through the measurement of M_Z
- ATLAS and CMS have an extensive program of W, Z measurements which can help constraining many of the theoretical uncertainties
- Prospects at future e^+e^- colliders ILC (TLEP) for approximately a factor of 2 (20) improvement on δM_W and δM_Z

BACKUP

W mass uncertainties at CDF

m_T fit uncertainties

Source	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Common
Lepton energy scale	7	10	5
Lepton energy resolution	1	4	0
Lepton efficiency	0	0	0
Lepton tower removal	2	3	2
Recoil scale	5	5	5
Recoil resolution	7	7	7
Backgrounds	3	4	0
PDFs	10	10	10
W boson p_T	3	3	3
Photon radiation	4	4	4
Statistical	16	19	0
Total	23	26	15

p_T^ν fit uncertainties

Source	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Correlation
Lepton energy scale	7	10	5
Lepton energy resolution	1	7	0
Lepton efficiency	2	3	0
Lepton tower removal	4	6	4
Recoil scale	2	2	2
Recoil resolution	11	11	11
Backgrounds	6	4	0
PDFs	11	11	11
W boson p_T	4	4	4
Photon radiation	4	4	4
Statistical	22	25	0
Total	30	33	18

p_T^ℓ fit uncertainties

Source	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Common
Lepton energy scale	7	10	5
Lepton energy resolution	1	4	0
Lepton efficiency	1	2	0
Lepton tower removal	0	0	0
Recoil scale	6	6	6
Recoil resolution	5	5	5
Backgrounds	5	3	0
PDFs	9	9	9
W boson p_T	9	9	9
Photon radiation	4	4	4
Statistical	18	21	0
Total	25	28	16

Phys. Rev. D 89, 072003 (2014)

Uncertainties are given in MeV

W mass uncertainties at D0

Phys. Rev. D 89, 012005 (2014)

Source	Section	m_T	p_T^e	\cancel{E}_T
Experimental				
Electron Energy Scale	VII C 4	16	17	16
Electron Energy Resolution	VII C 5	2	2	3
Electron Shower Model	V C	4	6	7
Electron Energy Loss	V D	4	4	4
Recoil Model	VII D 3	5	6	14
Electron Efficiencies	VII B 10	1	3	5
Backgrounds	VIII	2	2	2
$\sum(\text{Experimental})$		18	20	24
W Production and Decay Model				
PDF	VI C	11	11	14
QED	VI B	7	7	9
Boson p_T	VI A	2	5	2
$\sum(\text{Model})$		13	14	17
Systematic Uncertainty (Experimental and Model)		22	24	29
W Boson Statistics	IX	13	14	15
Total Uncertainty		26	28	33

Uncertainties are given in MeV

PDF uncertainties on M_T

	CTEQ6.6		MSTW2008		NNPDF2.1		$\delta_{\text{pdf}}^{\text{tot}}$
	$m_W \pm \delta_{\text{pdf}}$	$\langle \chi^2 \rangle$	$m_W \pm \delta_{\text{pdf}}$	$\langle \chi^2 \rangle$	$m_W \pm \delta_{\text{pdf}}$	$\langle \chi^2 \rangle$	
Tevatron, W^\pm	80.398 ± 0.004	1.42	80.398 ± 0.003	1.42	80.398 ± 0.003	1.30	4
LHC 7 TeV W^+	80.398 ± 0.004	1.22	80.404 ± 0.005	1.55	80.402 ± 0.003	1.35	8
LHC 7 TeV W^-	80.398 ± 0.004	1.22	80.400 ± 0.004	1.19	80.402 ± 0.004	1.78	6
LHC 14 TeV W^+	80.398 ± 0.003	1.34	80.402 ± 0.004	1.48	80.400 ± 0.003	1.41	6
LHC 14 TeV W^-	80.398 ± 0.004	1.44	80.404 ± 0.006	1.38	80.402 ± 0.004	1.57	8

Phys.Rev.D83:113008,2011

	Tevatron	LHC7W+	LHC7W-	LHC14W+	LHC14W-
$\alpha_s(m_Z) = 0.118$	80.398	80.400	80.398	80.402	80.400
$\alpha_s(m_Z) = 0.119$ (ref)	80.398	80.402	80.402	80.400	80.402
$\alpha_s(m_Z) = 0.120$	80.398	80.400	80.398	80.402	80.402

Table 7: Central value of the fit of m_W obtained with NNPDF2.1, using PDF sets that differ by the $\alpha_s(m_Z)$ value, for different colliders and energies. The fit has been done on normalized distributions and using normalized templates, and the distributions have been generated at NLO-QCD with DYNNLO.

m_W (GeV)	Tevatron	LHC7W+	LHC7W-	LHC14W+	LHC14W-
$m_c = 1.414$ (ref)	80.398	80.402	80.402	80.400	80.402
$m_c = 1.5$	80.398	80.400	80.398	80.398	80.399
$m_c = 1.6$	80.398	80.400	80.400	80.398	80.399
$m_c = 1.7$	80.396	80.400	80.400	80.396	80.398

Table 8: Central value of the fit of m_W obtained with NNPDF2.1 sets with different values of m_c for different colliders and energies. We include the default value in NNPDF2.1, $m_c^2 = 2 \text{ GeV}^2$ as well.