



Status of and prospects for top quark mass measurements

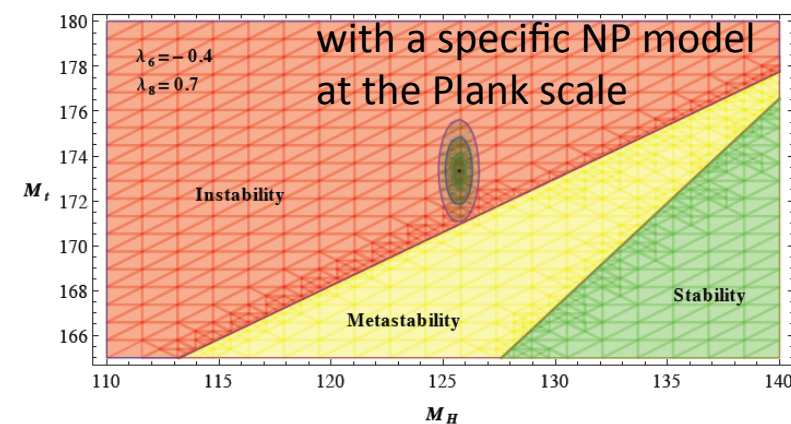
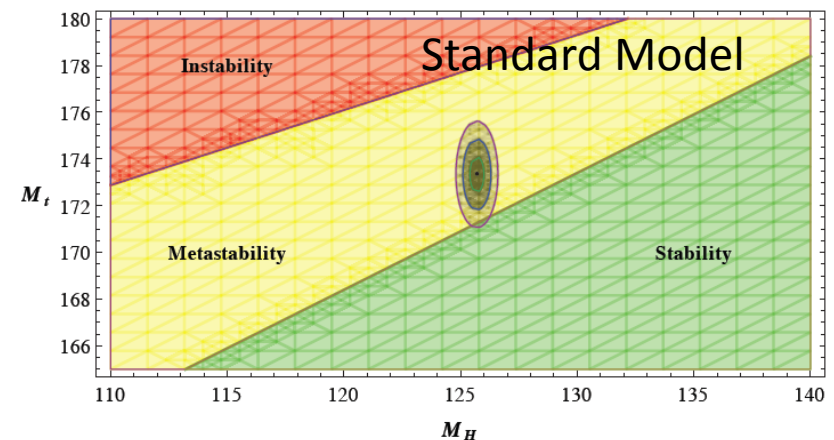
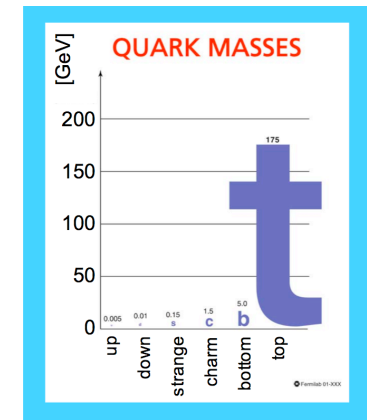
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Disclaimer: this is NOT a review talk, the aim is to discuss experimental methods and perspectives. A complete accounting of most recent top mass results is given at <http://indico.ific.uv.es/indico/sessionDisplay.py?sessionId=30&confId=2025#20140703>

Its highness, the top quark

- Because of the non-decoupling properties of electroweak interactions (Veltman, 1977) **the top quark** gives large contributions to pure EWK radiative corrections ($\approx G_F m_t^2$) hence it is **“the quark” for EWK precision physics**
- The fate of our universe, i.e. the stability of the EWK vacuum (Degrassi et al., arXiv:1205.6497), might not depend (only) on its mass, nevertheless the top mass value opens a window to new physics up to the Planck scale (Branchina et al., arXiv:1407.4112)



Quick reminder of top properties

- Very high mass \rightarrow very short lifetime:
bound states are not formed, almost a
free quark $\tau_{top} \approx 0.4 \times 10^{-24} s$

- Hierarchy of CKM elements \rightarrow only
decays to a b quark and a W boson are
relevant for this discussion, the decay
mode is $t \rightarrow Wb$

- Dominant production mode at
colliders in top pairs, events usually
classified and selected according to
their W-pair decays

- Top pair decay channels** have different
rates, different backgrounds, different
amount of missing energy (ν)
providing useful consistency tests

Top Pair Decay Channels

$\bar{c}s$	electron+jets	muon+jets	tau+jets	all-hadronic	
$\bar{u}d$					
τ^-	$e\tau$	$\mu\tau$	$\tau\tau$	tau+jets	
μ^-	$e\mu$	$\mu\mu$	$\mu\tau$	muon+jets	
e^-	ee	$e\mu$	$e\tau$	electron+jets	
W decay	e^+	μ^+	τ^+	$u\bar{d}$	$c\bar{s}$

Methods for top mass measurement (1)

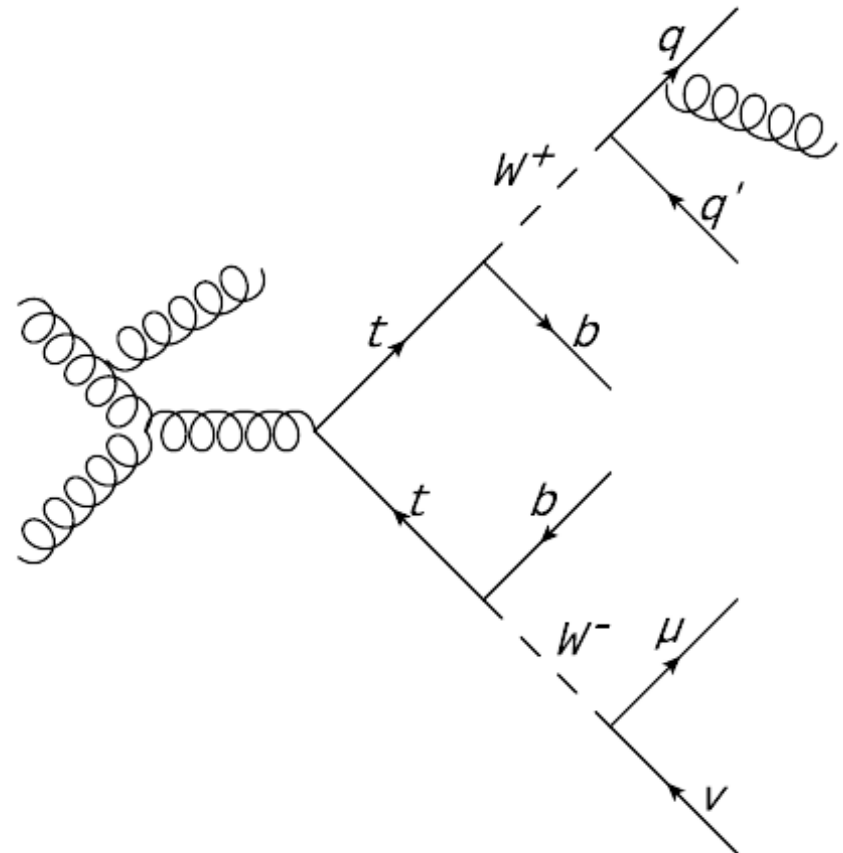
- *Standard methods* at hadron colliders: measure the top mass from the decay products in a specific **top pair decay channel**
 - from the simplest versions: **measure invariant mass of, e.g. three jets in lepton+jets events**
 - to the more sophisticated versions: **use of the full event information to gain sensitivity, e.g. Matrix Element method**
- The *standard methods* are the most precise with the current statistics
 - they are used in current LHC, Tevatron, World combinations
 - the top mass in EWK fits comes from these methods
- Crucial points for the *standard methods*
 - accurate calibration of physics objects, in particular Jet Energy Scale: use of kinematic fits for JES calibration in situ, e.g. **use the W mass to constraint light quarks jet energy scale (JES) from two-jet invariant mass**
 - associate measured objects (jets, leptons, missing E_T) to top candidate: **e.g. use b-tagging to choose the right b-jet for the 3-jet combination**

A couple of examples from the lepton+jets channel

Event selection: lepton+jets final state

[example from CMS, TOP-14-001 / JHEP 12 (2012) 105]

- Trigger for isolated muon or electron + jets ($p_T > 33$ GeV)
 - Exactly 1 isolated lepton with $p_T > 30$ GeV, $|\eta| < 2.1$ (veto additional isolated e, μ)
 - ≥ 4 “particle flow” jets (anti-kt, $R = 0.5$) with $p_T > 30$ GeV, $|\eta| < 2.4$
 - 2 jets b-tagged among the 4 leading jets
 - Composition:
 - 94% $\bar{t}t$, 2% W+jets, 3% single-top, 1% other
- 108000 events in 19.5 fb^{-1} at 8 TeV selected

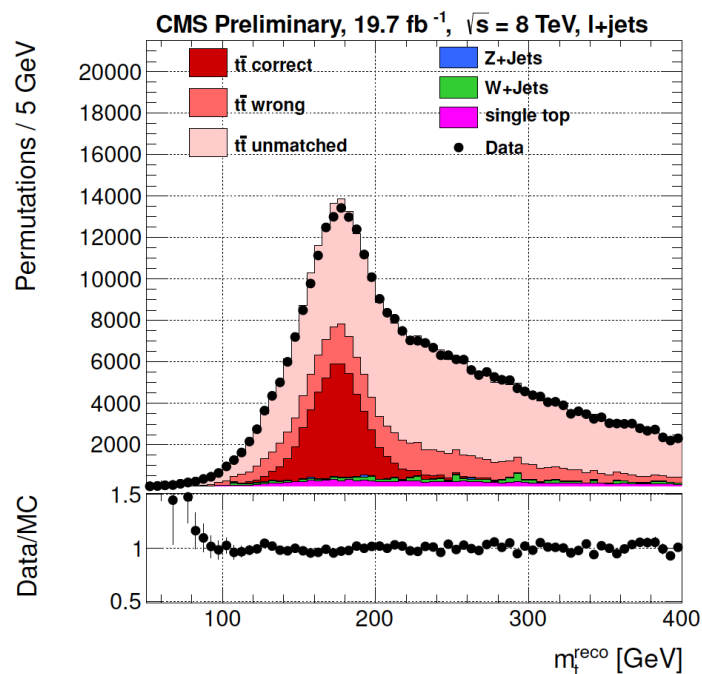


Compare with selections at Tevatron
with full statistics: about 2500 events

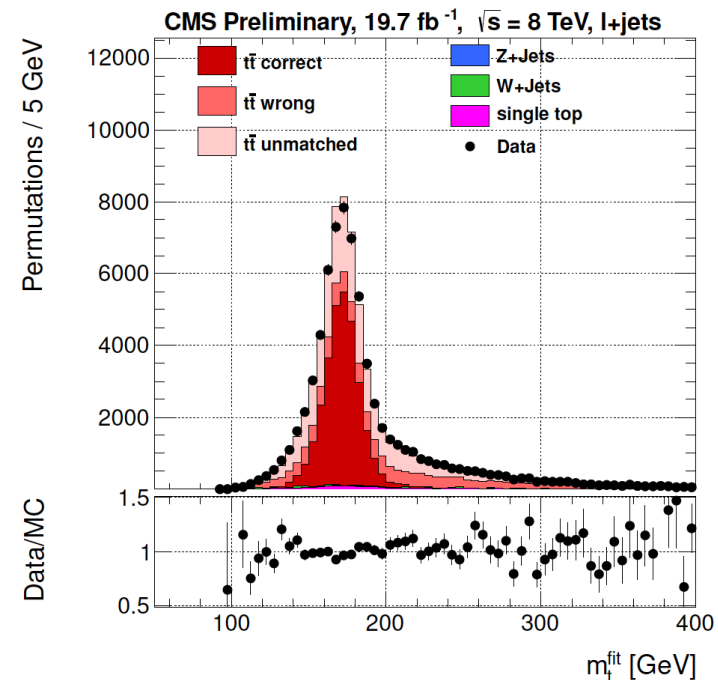
Event reconstruction

[example from CMS, TOP-14-001 / JHEP 12 (2012) 105]

- Assign 4 leading jets to partons from $t\bar{t}$ decay (obey b-tag)
 - Kinematic fit with constraints: $m_W = 80.4$ GeV, $m_t = m_{t\text{bar}}$
 - Weight each permutation by $P_{\text{gof}} = \exp(-1/2\chi^2)$, select $P_{\text{gof}} > 0.2$
- 28750 events in 19.7 fb^{-1} 2012 data (94% $t\bar{t}$, 44% correct perm.)



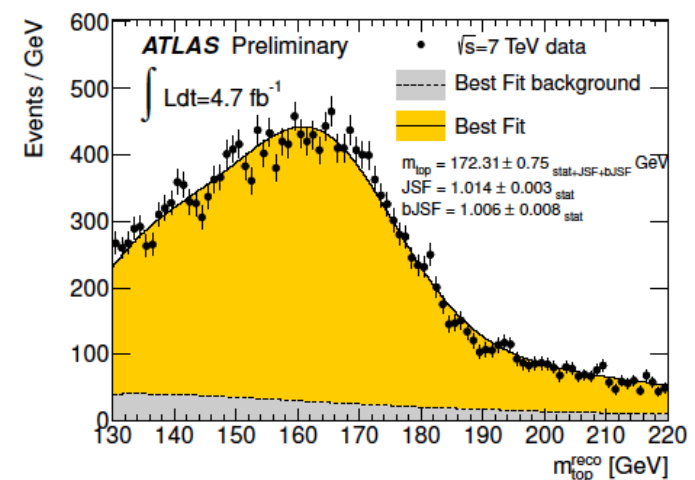
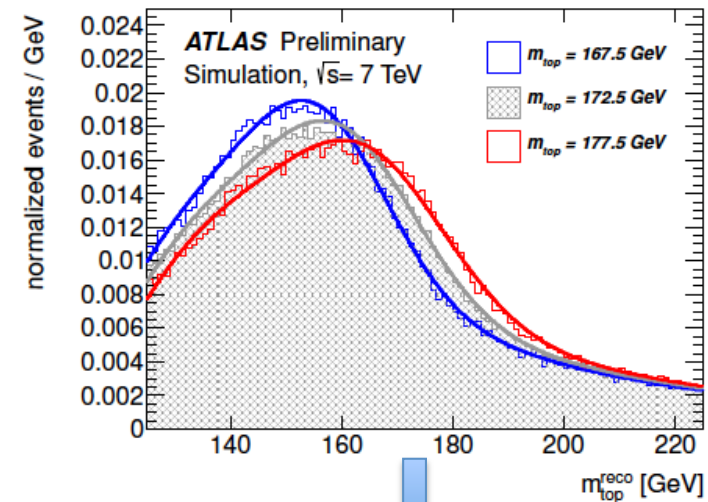
$P_{\text{gof}} > 0.2$



Top mass fitting techniques

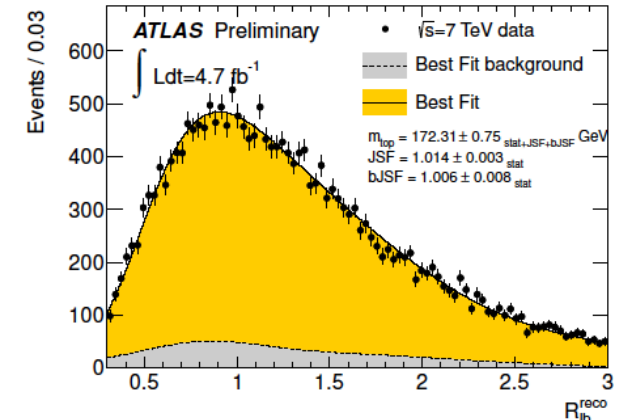
[example from ATLAS, CONF-2013-046]

- Invariant mass distributions are distorted by
 - phase space constraints
 - detector resolution
 - wrong particle assignments to jets
 - backgrounds, pileup
 - selection cuts
- Need a MC simulation, tuned to data, to construct templates or probability densities
 - **important:** at this stage the top mass definition in MC is not too relevant.



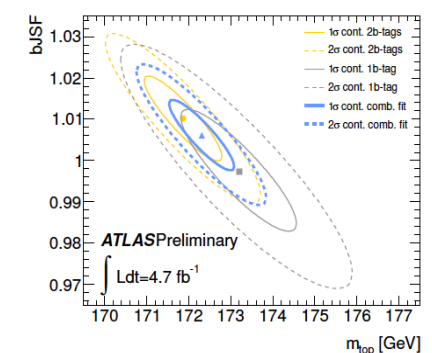
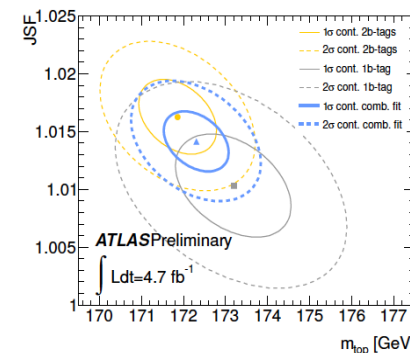
Top mass fitting techniques and JES

- The Jet Energy Scale is the most important source of experimental uncertainties, the W mass constraint is a powerful tool for light quark JES
- Can also find a variable sensitive to b-jet JES and constraint it in situ [ATLAS, CONF-2013-046] in this case b-tagging is used not only for jet classification, but also for JES determination
- Otherwise the simulation is used for b-jet JES, the impact of modeling assumption depends on the jet reconstruction technique



$$R_{lb}^{reco,2b} = \frac{p_T^{b_{had}} + p_T^{b_{lep}}}{p_T^{W_{jet1}} + p_T^{W_{jet2}}},$$

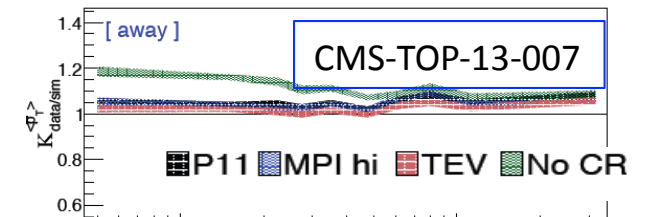
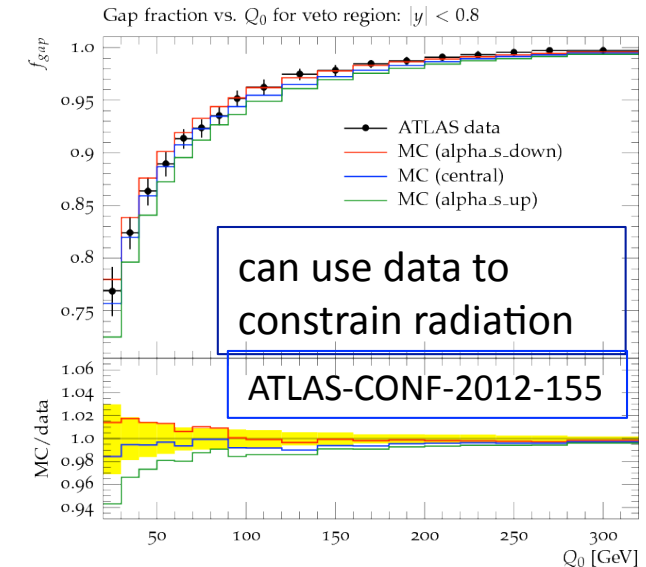
$$R_{lb}^{reco,1b} = \frac{p_T^{b_{tag}}}{(p_T^{W_{jet1}} + p_T^{W_{jet2}})/2}$$



Main sources of systematic uncertainties

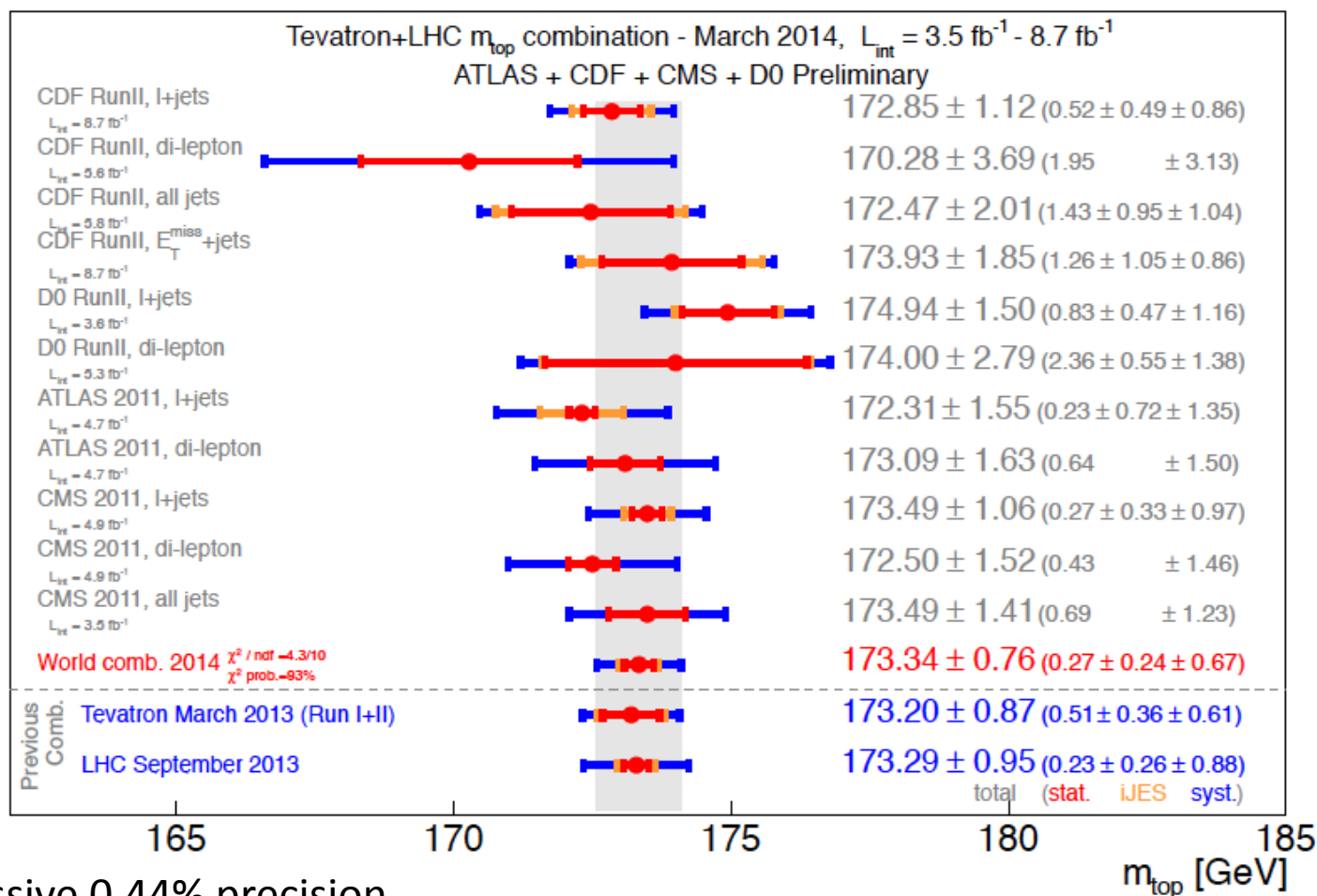
- Jet Energy Scale (depends on technique and jet reco, in situ statistical not included)
 - light jets, detector response [0.2-0.7 GeV]
 - b jets [0.1-0.6 GeV]
- Modeling of gluon radiation [0.3 – 0.45 GeV]
- Modeling of underlying event [0.1 – 0.2 GeV]
- Modeling of Colour Reconnection [0.2 – 0.5 GeV]
- Proton PDF [0.1 – 0.2 GeV]
- Hadronization, b-fragmentation (included also in JES) [0.3 -0.6 GeV]
- b-tagging [0.1 – 0.8 GeV]
- pileup modeling (included also in JES) (0.1-0.3 GeV)

[The numbers are ranges for illustration only, more details in specific analysis and LHC combination notes]



can use data to constrain generator modeling

World combination of m_{top}

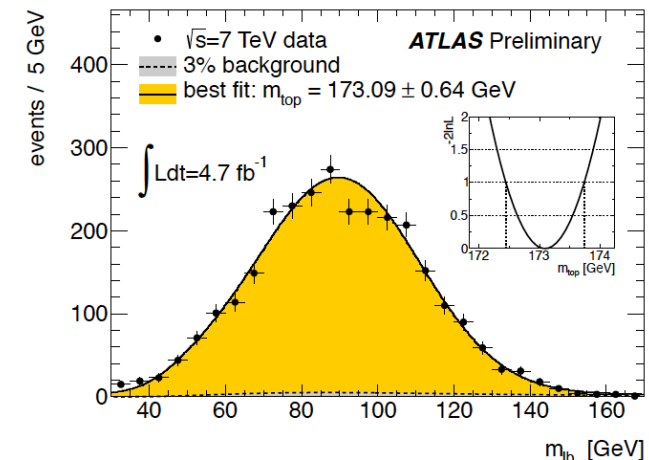


- An impressive 0.44% precision
- Some of the most precise measurements non included yet, e.g.
 - D0 full statistics, matrix element method, arXiv:1405.1756, $m_t = 174.98 \pm 0.76$
 - CMS l+jets at 8 TeV, $L = 19.6 \text{ fb}^{-1}$ CMS-TOP-2014-001, $m_t = 172.04 \pm 0.77$

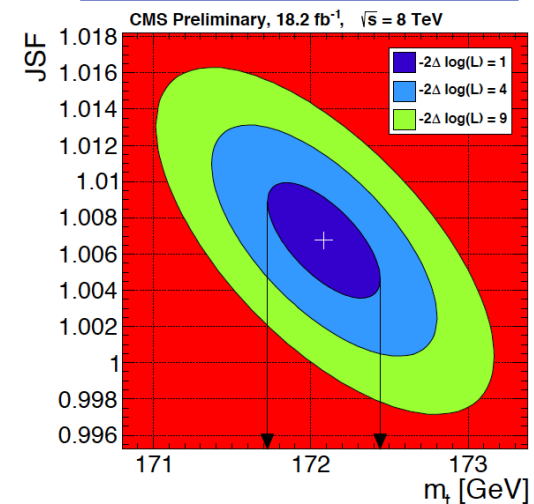
A note on the other channels at LHC

ATLAS-CONF-2013-077

- The dilepton and all-hadronic decay channels provide an important cross check, given the **difference in colour structure of the final state** (next slide).
- The **dilepton channel** is kinematically underconstrained (2 ν 's), but with low background
- The **all-hadronic channel** can profit from an accurate in-situ fit of the JES, already providing a result factor 2 better than Tevatron



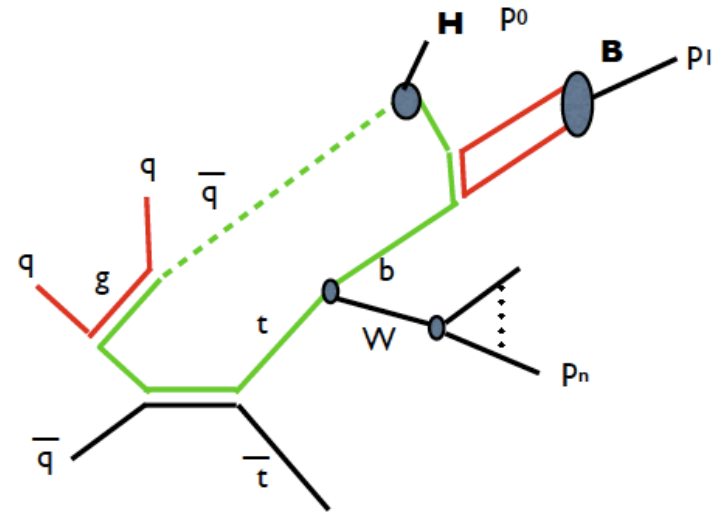
CMS-TOP-2014-002



About measuring the top mass from its decay products

- **Top is a coloured fermion**, it decays before hadronizing, but the b quark from its decay must hadronize
 - **there is no way to assign final state particles only to the original top**, the concept is ill-defined as it is the use of a pole mass for a coloured particle
 - the effect is expected to be of the order of $\Lambda_{\text{QCD}} \approx 0.2 \text{ GeV}$ but the actual impact depends on the experimental method
1. **important to test variables sensitive to the final state definition**
 2. **important to measure the mass with alternative techniques**

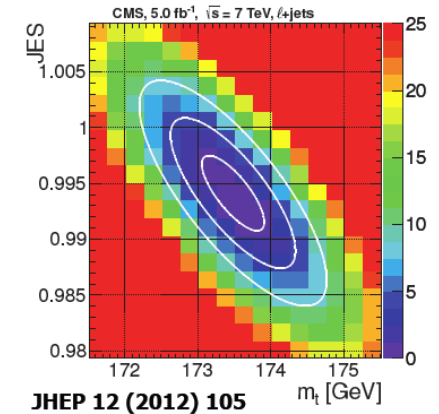
In prospect **1** and **2** will take advantage of the large LHC statistics



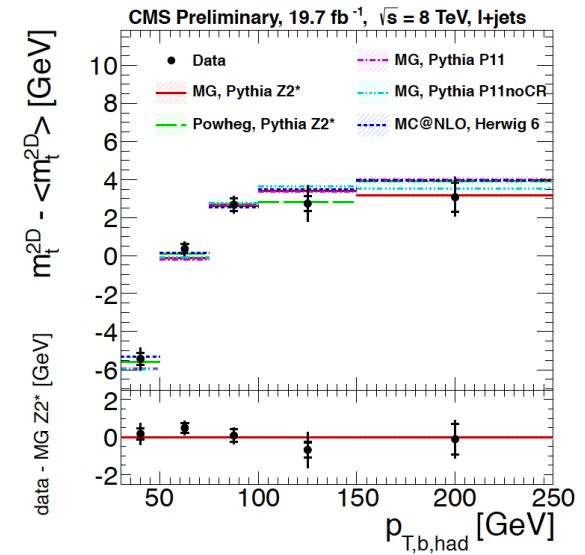
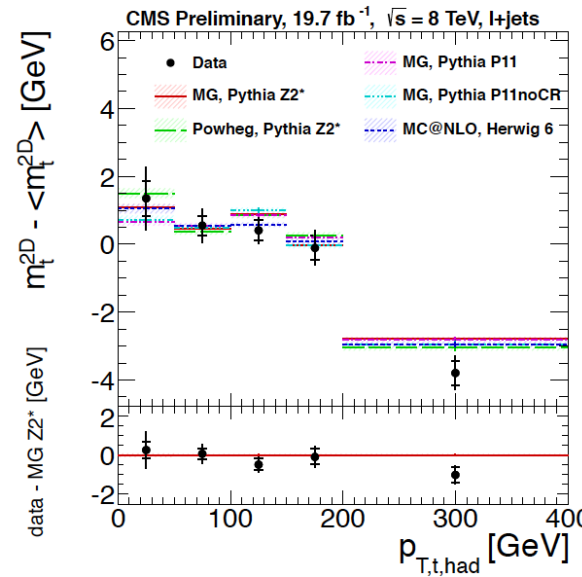
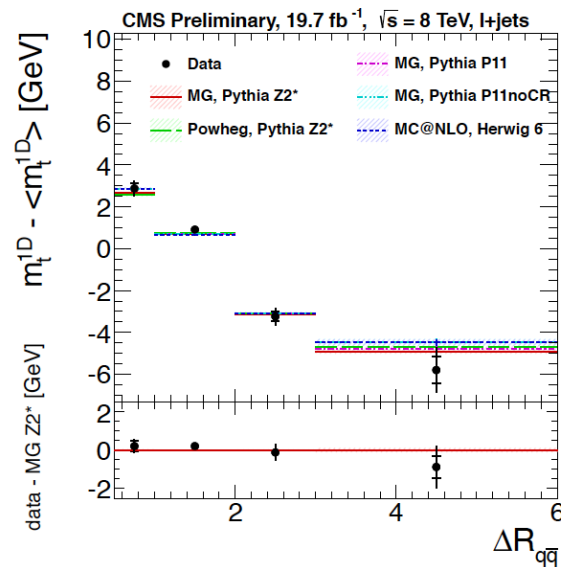
plot courtesy of Michelangelo Mangano

Dependence of Top Mass observable on event kinematics

- test variables sensitive to the final state definition
 - kinematic dependence on final state properly modeled by MC? \rightarrow 12 kinematic variables checked, related to Color Reconnection, ISR/FRS, b-jet kinematics
 - Good data/MC agreement rules out dramatic effects \rightarrow need to pursue the study with Run 2 high statistics !!



CMS-TOP-12-029
CMS-TOP-14-001



Methods for top mass measurement (2)

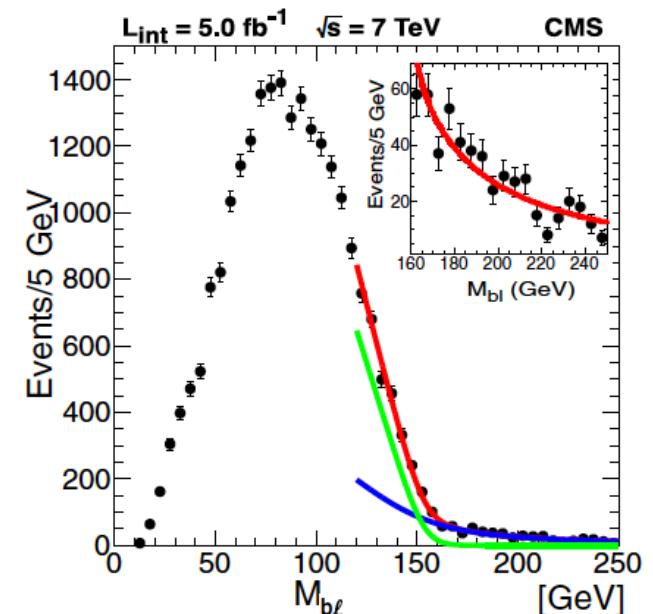
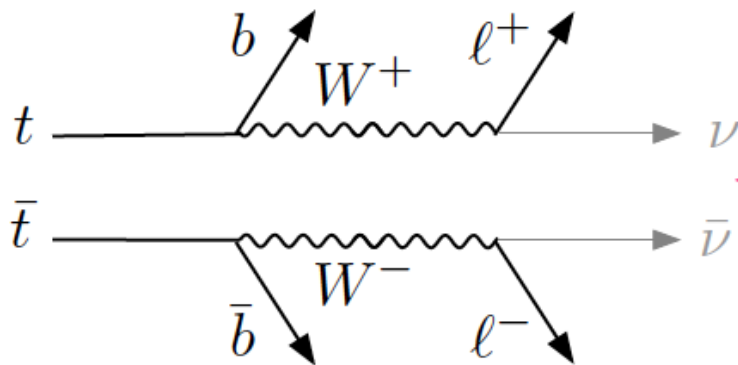
- Given the potential bias in measuring the top mass from its decay products, important to explore **alternative techniques**, e.g.
 - Measure the **decay length** (the boost) of B hadrons produced in top decays, the boost is related to the original top mass
 - Select **specific channels**, for example top with $W \rightarrow l \nu$ and $B \rightarrow J/\psi + X$ decays and measure the three-lepton invariant mass
 - Measure the **endpoint** of the lepton **spectrum** or other quantities in top decays
 - Measure the mass from single top events (great potential !)
- Alternative methods have typically larger statistical uncertainties, however at LHC we have large $t\bar{t}$ samples
 - Systematic uncertainties can be controlled with data, again large samples help.
- Another alternative: **move away from properties of the decay products**
 - **extract the top mass from the top cross section**

TOP mass from alternative techniques

- Example of a technique already yielding interesting precision:
Endpoint method
- The shape of the signal can be computed analytically,
background data-driven
- Use of MC limited to study underlying assumption:
independent decay of two tops (color connections and
reconnections violate this assumption)

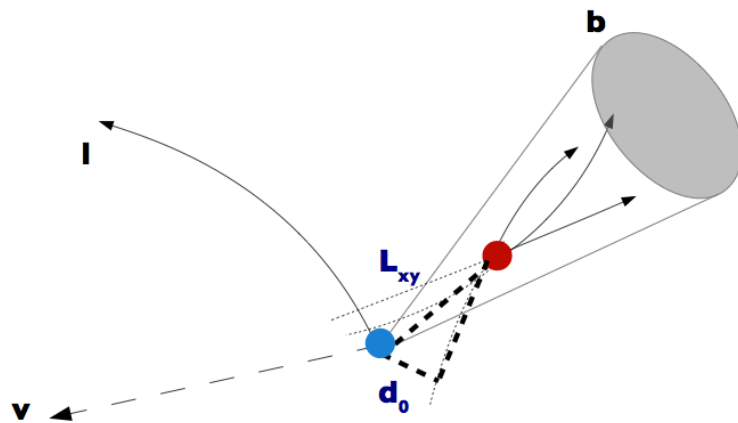
arXiv:1304.7498

$$M_t = 173.9 \pm 0.9 (\text{stat.})_{-2.0}^{+1.6} (\text{syst.}) \text{ GeV}$$

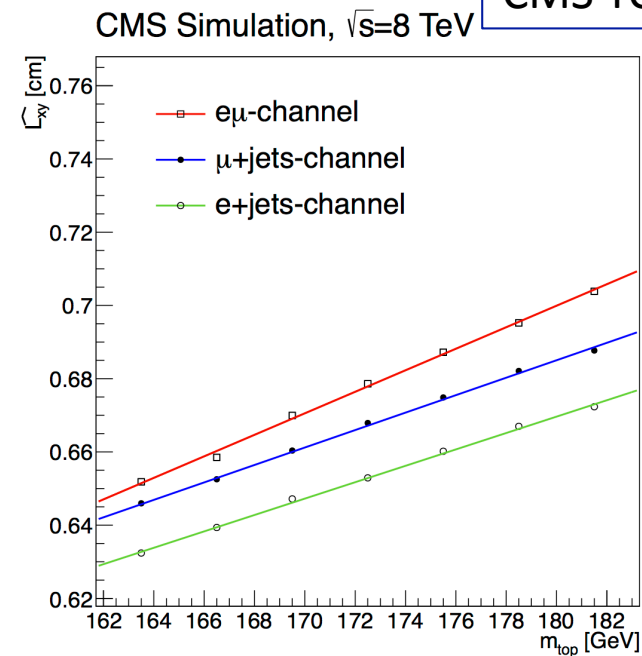


Another example: top mass from the b decay length

- The decay length of b hadrons from top decays is correlated to their boost, i.e. to the top mass



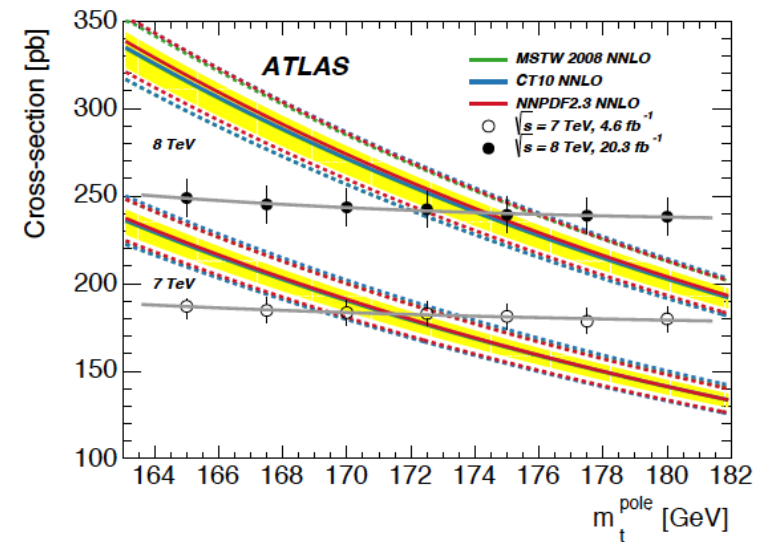
$$m_t = 173.5 \pm 1.5_{\text{stat}} \pm 1.3_{\text{syst}} \pm 2.6_{p_t(\text{top})} \text{ GeV}$$



$t\bar{t}$ cross section: mass interpretation

[example from ATLAS, arXiv:1406.5375]

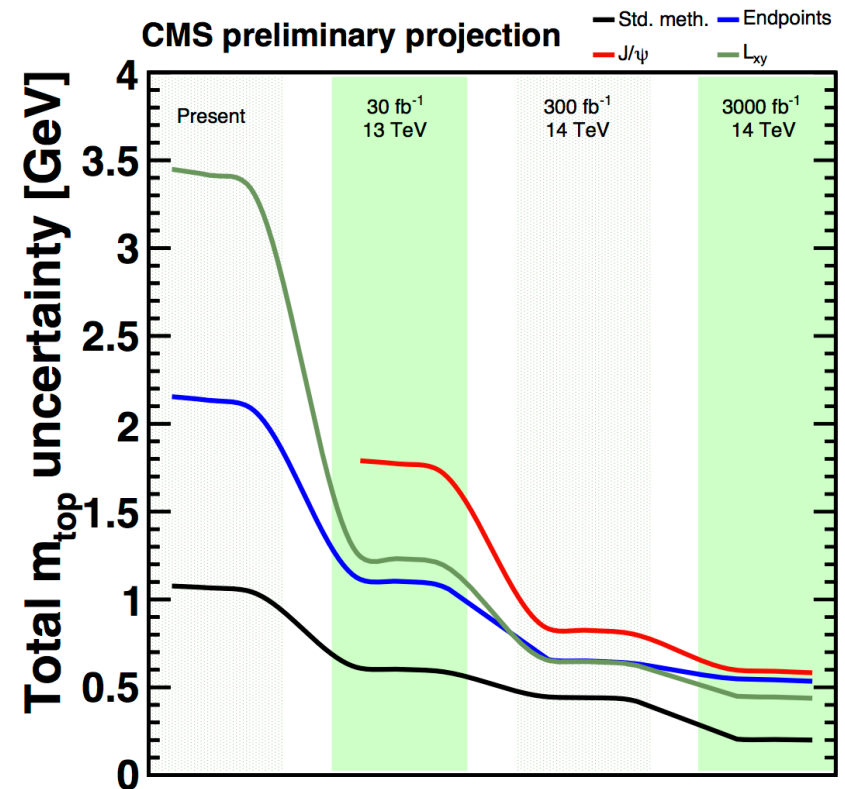
- Measure cross section in the most precise channel: dilepton $e\mu$
- Use b-tagging and double tag method to avoid dependence on b-tag efficiency
 - interesting by-product: acceptance dependence on m_t is flat because of calibration of the jet acceptance in situ and cancelation with Wt background
- Use recent NNLO calculation of top pair cross section to extract m_t
- The method takes advantage of the excellent luminosity knowledge at LHC ($\sim 2\%$), which is also the long-term experimental limitation, together with the knowledge of the LHC beam energy



$$m_t = 172.9^{+2.5}_{-2.6} \text{ GeV}$$

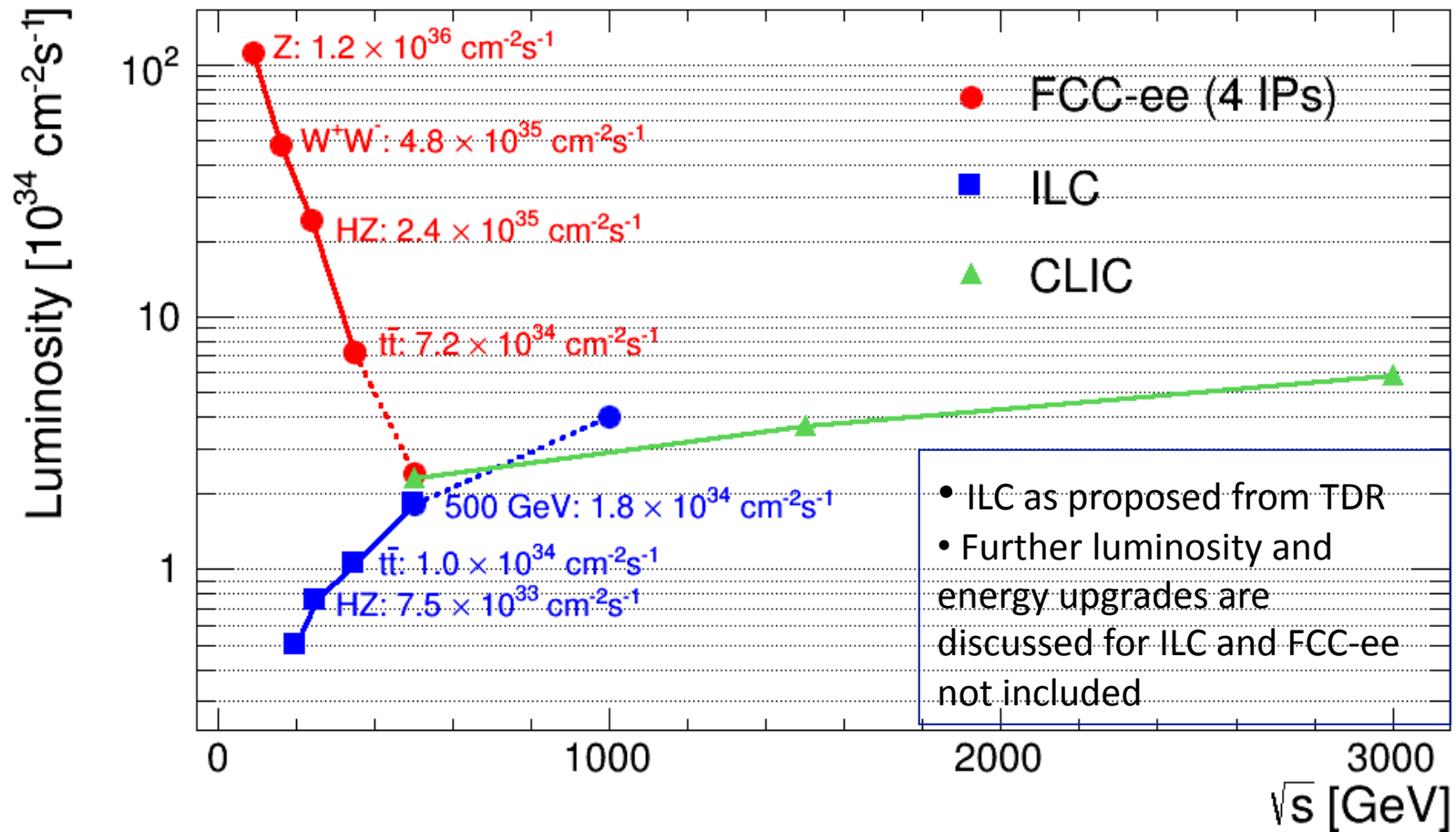
Prospects for top mass at the LHC

- There is potential to improve standard methods, taking advantage of the high statistics for, e.g., in-situ JES calibration, constraining models from differential studies, etc.
- There is even greater potential for alternative methods, most of the current systematic uncertainties can be reduced with higher statistics, e.g. top pt modeling, in-situ JES again
- Improvements on the cross section method are linked to improvements in the luminosity and beam energy uncertainties at LHC
- A optimistic view (maybe realistic give past experience at colliders !) of the evolution in precision is given in the picture



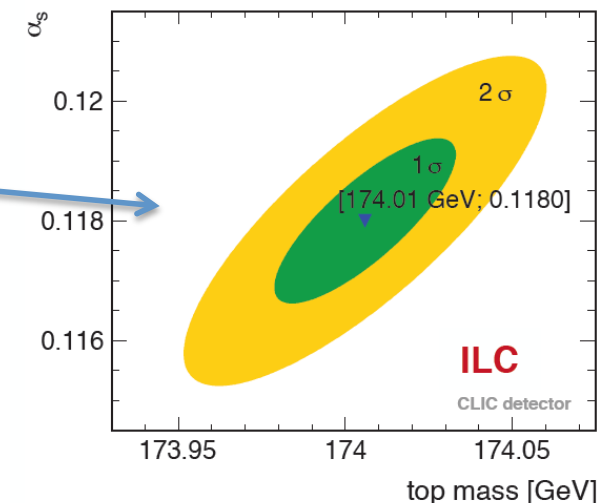
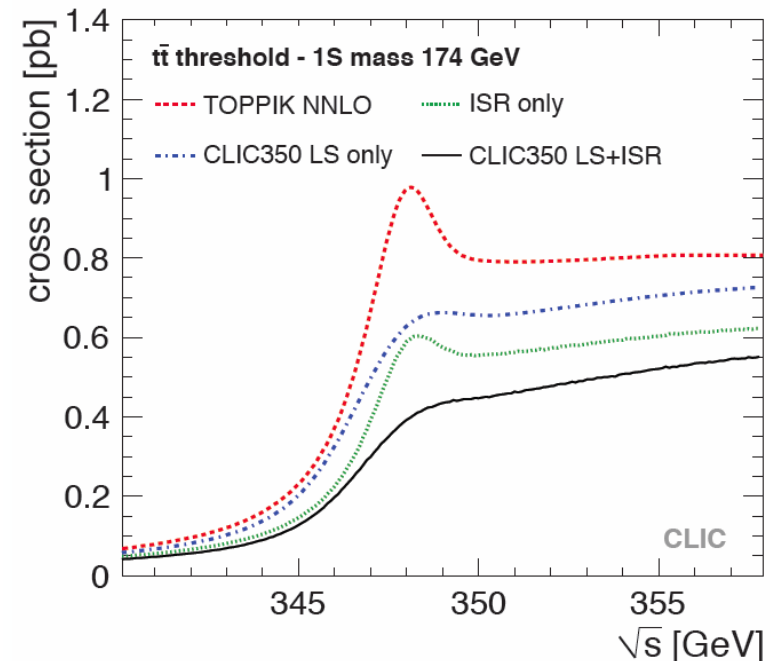
From CMS PAS FTR-13-017, prepared for the “European Strategy for particle physics” discussions

Prospects at future e^+e^- Colliders: Linear and Circular



top mass from threshold scan

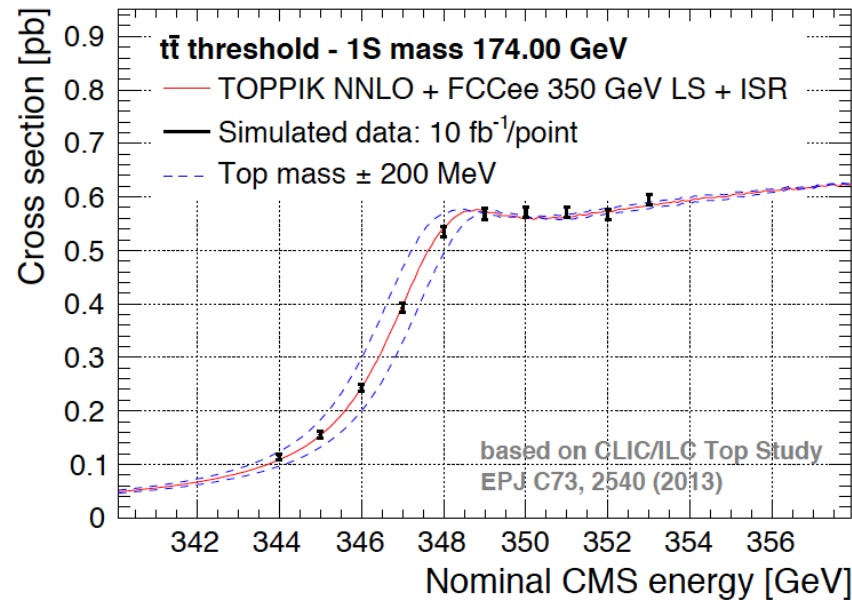
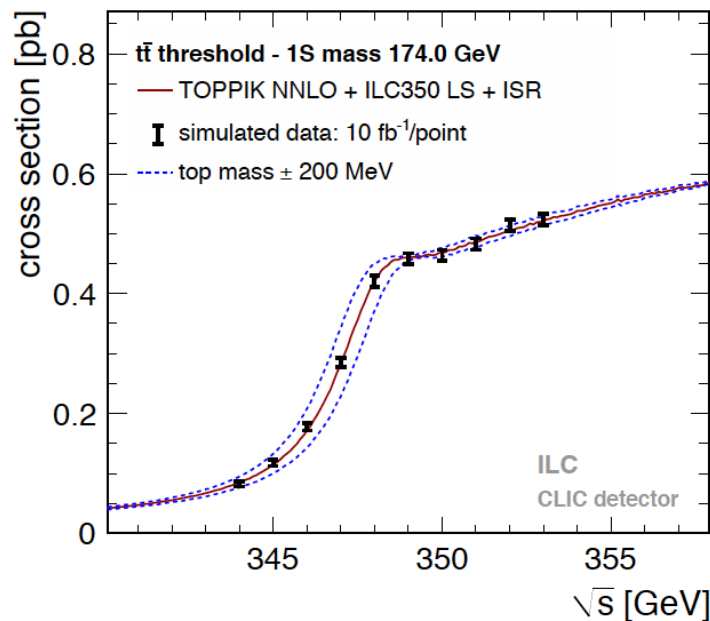
- Same conceptual advantage as cross section measurement at LHC, but experimentally dependent only on beam energy spectrum
- Other source of uncertainty is the lineshape related to α_s , top width and top-Higgs Yukawa coupling (with high statistics 2D / 3D fits possible)



Eur. Phys. J. C73 (2013) 2530

e^+e^- at 350 GeV: threshold scan

- At ILC statistical uncertainty of 30 MeV with 10 fb⁻¹ scan
- At FCC statistical uncertainty of 10 MeV expected - Advantage of a very low level of beamstrahlung at FCC
- Theoretical *current* uncertainty from higher order QCD contribution ~ 100 MeV
 - Comparing ILC and FCCee - assuming identical detector performance



Simulated data points -
same integrated luminosity

NB: Assuming unpolarized beams - LC
beams can be polarized, increasing cross-
sections / reducing backgrounds

From Frank Simon, presented at 7th TLEP-FCC-ee workshop, CERN, June 2014

Conclusions

- The 2014 top mass world average is 173.34 ± 0.76 GeV
- High statistics at LHC offers a unique opportunity of studying the robustness of top mass determination based on top decay products
 - data-based constraints on systematics
 - differential measurements
 - alternative techniques
- We need e⁺e⁻ colliders to reach precisions in the range 100 MeV \rightarrow 10 MeV