

# The Higgs and vector resonances in bosonic technicolor

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Thanks to my collaborators [Seung J. Lee](#), [Adam Martin](#), [Patipan Uttayarat](#), [Jure Zupan](#), especially Patipan for preparing most of the plots

# Plan

- Introduction
- Higgs phenomenology
- $S$  and  $T$  away from the chiral limit
- vector phenomenology

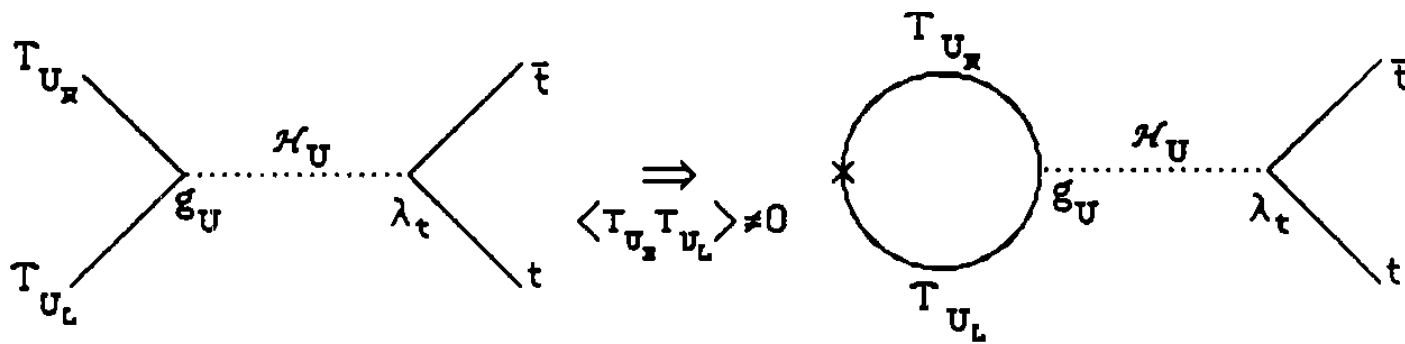
# Introduction

- BTC combines technicolor and supersymmetry Dine, A.K., Samuel, 1990; non-susy version: Simmons, 1989
- technicolor condensates trigger electroweak symmetry breaking
- fundamental Higgs fields  $H_u, H_d$  give masses to quarks, leptons
- supersymmetry stabilizes the Higgs scalar masses
- Higgs VEV's via Yukawa couplings to technifermion condensates

$$\lambda_U \bar{U}_R T_L H_u + \lambda_D \bar{D}_R T_L H_d \Rightarrow \langle H_u \rangle \sim \lambda_U \frac{\langle \bar{U}_R U_L \rangle}{m_{H_u}^2}, \quad \langle H_d \rangle \sim \lambda_D \frac{\langle \bar{D}_R D_L \rangle}{m_{H_d}^2}$$

- positive Higgs mass parameters,  $m_{H_u}^2, m_{H_d}^2 > 0 \Rightarrow$  no electroweak symmetry breaking in absence of TC
- $W, Z$  receive masses both from technicolor condensates, Higgs VEV's

$$v_W^2 = (246 \text{ GeV})^2 \approx f_{\text{TC}}^2 + f_u^2 + f_d^2, \quad \langle H_{u,d} \rangle \equiv f_{u,d}/\sqrt{2}$$



- Fermion mass generation in BTC via “Higgs scalar exchange”, integrated out in heavy limit
- for light Higgs, use chiral Lagrangian approach [Carone, Simmons](#); [Carone, Georgi](#)

- Minimal BTC = MSSM +  $SU(N)_{TC}$ , with technifermion superfields

$$\hat{T}_L(2_{TC}, 1_C, 2_L, 0), \quad \hat{U}_R(2_{TC}, 1_C, 1_L, -1/2), \quad \hat{D}_R(2_{TC}, 1_C, 1_L, +1/2),$$

and Yukawa superpotential

$$W_Y = \lambda_U \hat{U}_R \hat{T}_L \hat{H}_u + \lambda_D \hat{D}_R \hat{T}_L \hat{H}_d$$

- $N_{TC} = 2$  is minimal choice
- $N_{TC} = 3$  disfavored: stable fractionally charged technibaryons;  $SU(2)_L$  anomaly
- $N_{TC} = 4$  disfavored by  $S$  parameter

- superpartner technigluino, technisquarks acquire masses  $> \Lambda_{TC}$ , yielding a [QCD-like](#) technicolor theory at lower scales

# Original Motivation - 90's

- large  $m_h$  easily obtained: unlike MSSM, where  $m_h \sim m_Z$ , in BTC  $m_h$  not tied to quartic coupling - little change if set  $D^2$  terms to zero
- at the time,  $m_t \gtrsim 100$  GeV
- for  $\lambda_U \sim 1$  and top Yukawa  $y_t \sim 1$ , was possible to obtain  $m_t \sim 100$  GeV for  $m_h \sim 1/2$  TeV
  - $\Rightarrow$  multi-TeV squark, slepton masses (5-10 TeV) natural
- motivation was to combine SUSY and TC, to ease FCNC problems in each
  - heavy superpartners  $\Rightarrow$  SUSY FCNC problem alleviated - relaxed degeneracy
  - Extended TC fermion mass generation plagued by FCNC problems, unlike Higgs Yukawa couplings

## As it turned out

- top significantly heavier, Higgs significantly lighter (preferred by precision electroweak for some time)
- combined with preference for perturbative  $O(1)$  top and TC Yukawa couplings, to allow  $m_{H_u}^2, m_{H_d}^2 > 0$  without fine-tuning

$$\Rightarrow v_W^2 \approx f_u^2 + f_d^2 \gg f_{TC}^2, \quad \text{e.g. } f_{TC} \lesssim 100 \text{ GeV}$$

- bulk of  $W, Z$  masses come from Higgs VEV's, but **EWK symmetry breaking triggered by TC:  $f_{TC} \neq 0$**       AK, KITP '08; Azatov, Galloway, Luty '11
- $f^2 \ll v_W^2$ , light Higgs also considered in non-susy BTC  
Carone, Simmons; Carone, Georgi; Antola et al.

- light Higgs  $\Rightarrow$  relaxing SUSY FCNC no longer a motivation
- However, from low energy perspective,  $m_h \approx 125$  GeV is easy: no fine-tuned cancelations in scalar potential, no need for heavy stops with large left-right mixing,...
- as in MSSM, Higgs mass parameters log sensitive to large SUSY breaking mediation scales
  - perhaps  $U(1)_R$  symmetric BTC with Dirac  $SU(3)_C$  and TC gauginos, i.e. with supersoft properties, can improve the situation (under investigation)
  - add TC adjoint and  $SU(3)_c$  adjoint matter superfields  $a_{TC}, a_C$  to minimal BTC set-up  $\Rightarrow m_{\tilde{g}_{TC}} \tilde{g}_{TC} a_{TC}, m_{\tilde{g}} \tilde{g} a_C$
  - advantage over R-symmetric MSSM (and MSSM in general)
  - $\mu$  problem may be solved via partial compositeness: higgsinos, electroweak gauginos gain mass via mixing with technifermion-techniscalar bound states,

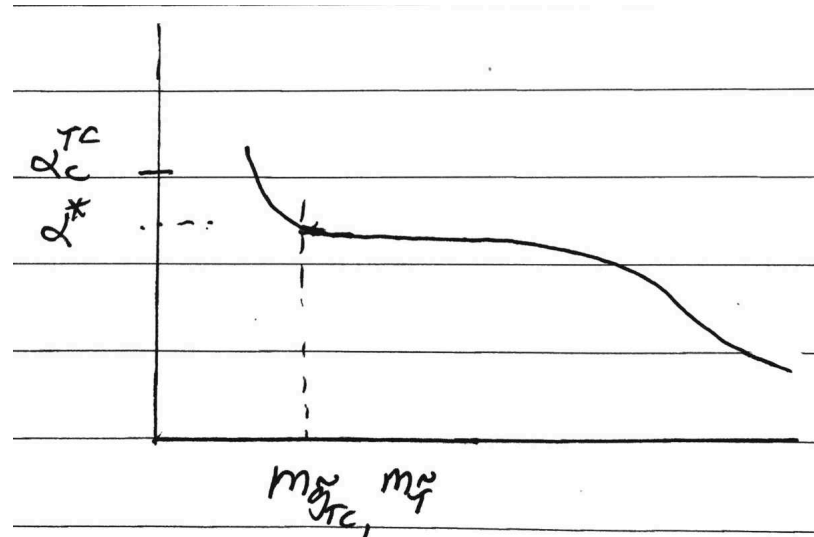
$$\text{e.g. } \lambda_U \tilde{h} T_L \tilde{U}_R \rightarrow m \tilde{h} \psi_1, \quad g_2 \tilde{w} T_L \tilde{T}_L \rightarrow m' \tilde{w} \psi_2$$

## Linking $\Lambda_{\text{TC}}$ and $m_{\text{susy}}$

- BTC introduces two scales at low energies: (i)  $m_{\text{susy}}$ , the scale of superpartner masses; (ii)  $\Lambda_{\text{TC}}$ , the scale of TC chiral symmetry breaking
- potential coincidence problem since, e.g.  $m_{\text{susy}}/\Lambda_{\text{TC}} = O(\text{few})$
- when techni-superpartners acquire masses and “decouple”, technicolor beta function becomes more negative.
  - more rapid increase in  $\alpha_{\text{TC}}$  below  $m_{\text{susy}}$  could link the two scales  
AK, Samuel '91



- most attractive scenario [Azatov, Galloway, Luty '11](#):  
 above  $m_{\text{susy}}$ ,  $\alpha_{\text{TC}}$  sits near a superconformal strong IR fixed point. Provides direct link between  $m_{\text{susy}}$  and  $\Lambda_{\text{TC}}$
- appealing realization: susy  $SU(2)$  with  $n_f = 2$  and one adjoint matter superfield is known to have a strongly interacting IR fixed point  
[Elitzur, Forge, Giveon, Rabinovici '95](#)
- $R$  symmetric BTC has precisely this TC field content. Can yield the following running of  $\alpha_{\text{TC}}$ :



# Higgs Phenomenology

- in chiral limit  $\lambda_{u,d} \rightarrow 0$ ,  $M_{R,L} \rightarrow 0$ : TC sector has global  $SU(4)$  symmetry
- Yukawa couplings ensure desired vacuum alignment  
 $\langle \bar{U}_R T_L \rangle, \langle \bar{D}_R T_L \rangle \neq 0 \Rightarrow SU(4) \rightarrow Sp(4) \Rightarrow 5$  pseudo-NGB's
- $\pi^a$  : the usual  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$  triplet
- $\pi_{UD}, \pi_{\bar{U}\bar{D}}$ : "baryonic" states which could lead to TC dark matter candidate  
Ryttov, Sanino; Frandsen, Sanino

for Higgs phenomenology suffices to consider  $SU(2)_L \times SU(2)_R$  subgroup of  $SU(4)$ :

- taking into account MSSM scalar fields, after electroweak symmetry breaking have 8 physical linear combinations of MSSM scalars and TC pions,  $\sigma$ 
  - one light higgs  $h$ , two heavy Higgs  $H$
  - two charged pions  $\pi_1^\pm, \pi_2^\pm$
  - two neutral pions  $\pi_1^0, \pi_2^0$
- recently, have included a heavy scalar  $\sigma[\bar{T}T]$  bound state with  $\langle\sigma\rangle = f$ 
  - in QCD the  $\sigma$  has  $O(1)$  width, due to  $\sigma \rightarrow \pi\pi$
  - over the years this has led to a bias against consideration of a  $\sigma$  in TC
  - but BTC is far from the chiral limit. The  $\pi$  are heavy  $\Rightarrow \sigma \rightarrow \pi\pi$  channel is closed, or suppressed, leading to a relatively narrow  $\sigma$

$$\Gamma_\sigma/m_\sigma \leq O(10\%), \text{ due to } \sigma \rightarrow (W, Z)\pi, WW, ZZ$$

# TC Chiral Lagrangian

Employ two flavor  $SU(2)_L \times SU(2)_R$  non-linear sigma model chiral Lagrangian  $\mathcal{L}_\chi$  + MSSM Higgs scalar potential

$$\text{Yukawa couplings : } -\bar{T}_L \Phi_\Lambda T_R + h.c., \quad T_{R(L)} = \begin{pmatrix} U_{R(L)} \\ D_{R(L)} \end{pmatrix}$$

$$\Lambda_u = \begin{pmatrix} \lambda_u & 0 \\ 0 & 0 \end{pmatrix} \quad \Lambda_d = \begin{pmatrix} 0 & 0 \\ 0 & \lambda_d \end{pmatrix},$$

$$\text{ext. source for } \mathcal{L}_\chi : \quad \Phi_\Lambda = \Phi_u \Lambda_u + \Phi_d \Lambda_d, \quad \Phi_\Lambda \rightarrow L \Phi_\Lambda R^\dagger$$

$$\text{MSSM Higgs fields : } \quad \Phi_q = \frac{1}{\sqrt{2}} (\sigma_q + f_q + 2i\pi_q^a T^a), \quad q = u, d.$$

$$\pi^a, \sigma : \quad \Sigma_\sigma = \frac{\sigma + f}{\sqrt{2}} \text{Exp} \left[ \frac{i2\pi^a T^a}{f} \right], \quad \Sigma \rightarrow L \Sigma R^\dagger$$

$$f = f_{\text{TC}} \text{ in chiral limit, } \quad m_U = m_D = 0$$

● Chiral Lagrangian for QCD-like TC:

$$\mathcal{L}_\chi = \frac{Z_1}{2} \text{Tr} \left( D_\mu \Sigma_\sigma^\dagger D_\mu \Sigma_\sigma \right) + \frac{Z_3}{2\sqrt{2}\pi} \left[ \text{Tr} \left( D_\mu \Sigma_\sigma^\dagger D_\mu \Phi_{\Lambda_1} \right) + \text{h.c.} \right] + \frac{1}{2} \sum_{q=u,d} \text{Tr} \left( D_\mu \phi_q^\dagger D_\mu \phi_q \right) \\ + Z_2 4\sqrt{2}\pi f^2 \left[ \text{Tr} \left( \Phi_{\Lambda_1} \Sigma_\sigma^\dagger \right) + \text{h.c.} \right] + 2Z_4 \left[ \text{Tr} \left( \Phi_{\Lambda_1} \Sigma_\sigma^\dagger \right) + \text{h.c.} \right]^2,$$

- $Z_i[\hat{m}]$  are dimensionless functions of  $\hat{m} \equiv (m_U + m_D)/2$  and the low energy chiral Lagrangian constants
- condensate at  $O(p^2)$  :  $\langle \bar{T}T \rangle_0 = -8\pi f^3 Z_2[\hat{m} = 0]$
- TC pion mass at  $O(p^2)$  :  $m_{\pi\pi}^2 = 16\pi^2 Z_2[\hat{m} = 0] f \hat{m}$  (GMOR relation)
- the chiral symmetry breaking scale  $\Lambda_\chi \sim 4\pi f$  in NDA

- scaling to TC from QCD:
  - use low energy  $O(p^4)$  constants from  $n_f = 2$  lattice QCD [ETM 0911.5061](#)
  - include  $1/N$  scalings to account for  $N_{\text{TC}} = 2$  vs  $N_c = 3$
  - for massive quantities scale up by powers of  $f/f_\pi^{\text{QCD}}$
  - for  $\hat{m}/f > 1$  use linear extrapolation of chiral logs (analog of  $\hat{m} \gtrsim m_s$  in QCD)
  - included multiplicative fudge factors for the  $Z_i$ ,  $\in [0.5, 1.5]$ 
    - to account for uncertainties from  $1/N$  scaling, higher orders in  $p^2$ ,  $\hat{m}/f > 1$ , back reaction of Yukawa couplings on TC condensate,...
    - true theory uncertainties probably require larger ranges for the fudge factors

- The  $Z_3$  term  $\Rightarrow$  kinetic mixing between the TC and fundamental pions, and between the TC and fundamental neutral scalars at  $\geq O(p^4)$ 
  - transform to canonical bases
- The  $Z_2, Z_4$  terms  $\Rightarrow$  TC pion mass; mass mixing between the TC and fundamental pions; mass mixing between the TC and fundamental scalars at  $\geq O(p^2)$ 
  - diagonalization of the scalar mass matrix yields the (light) Higgs and an intermediate mass Higgs: primarily fundamental  $\sigma_u, \sigma_d$ ,
  - a heavy Higgs: primarily composite  $\sigma$
- for the pure TC  $\sigma$  mass term, we scale up NJL-type  $\sigma_{\text{QCD}}$  mass  
e.g. Klevansky '92; Hatsuda, Kunihiro '94

$$m_\sigma^2 = (2M_c)^2 \frac{f^2}{f_\pi^2} \frac{3}{N_{\text{TC}}} + c m_\pi^2, \quad c = O(1)$$

- took QCD “constituent” quark mass  $M_c \in [0.25, 0.40]$  GeV,  $c \in [0.35, 1.0]$
- yields  $m_\sigma \lesssim m_\rho$  (come to  $\rho$  mass later)

# calculability of loop effects?

- pion loop effects are calculable if the chiral expansion parameter

$$\frac{M^2}{\Lambda_\chi^2} \approx \frac{\hat{m}}{2\pi f} \ll 1$$

- relevant for  $\Delta S, \Delta T$

- $\rho, a_1$  loops are not calculable because  $m_{\rho, a_1}/\Lambda_\chi \sim 1$

- $h \rightarrow \gamma\gamma$  not calculable (a drawback, but significant range about SM in principle possible)

- parametrize TC induced  $h\gamma\gamma$  coupling using NDA

$$\frac{\alpha}{2\pi} \frac{1}{\Lambda} \kappa \frac{\lambda_u c_u + \lambda_d c_d}{\sqrt{2}} h A^{\mu\nu} A_{\mu\nu}$$

where  $h = c_u \sigma_u + c_d \sigma_d + c_\sigma \sigma$  and  $\kappa = O(1)$ . Took

$$\Lambda = 4\pi f, \quad \kappa \in \pm[0.5, 3]$$



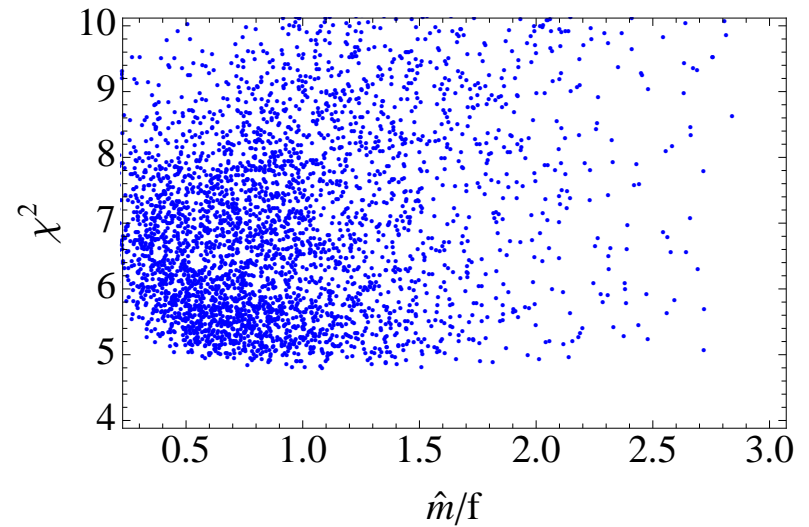
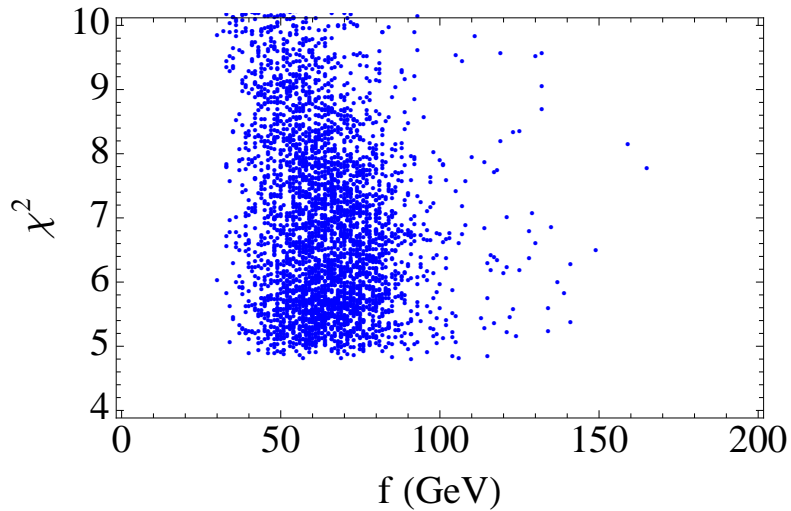
## Fit to the Higgs data

Channel	$(\mu_V, \mu_F)$	$(\Delta\mu_V, \Delta\mu_F)$	$\rho$
ATLAS $\gamma\gamma$	(1.75, 1.62)	(1.25, 0.63)	-0.17
CMS $\gamma\gamma$	(1.48, 0.52)	(1.33, 0.60)	-0.48
ATLAS ZZ	(1.2, 1.8)	(3.9, 1.0)	-0.3
CMS ZZ	(1.7, 0.8)	(3.3, 0.6)	-0.7
ATLAS WW	(1.57, 0.79)	(1.19, 0.55)	-0.18
CMS WW	(0.71, 0.72)	(0.96, 0.32)	-0.23
ATLAS $\tau\bar{\tau}$	(1.67, 0.97)	(1.14, 1.86)	-0.49
CMS $\tau\bar{\tau}$	(1.28, 0.46)	(0.66, 0.81)	-0.42
Combined $Vh, h \rightarrow b\bar{b}$	(0.9, -)	(0.3, -)	-
Combined $t\bar{t}h, h \rightarrow b\bar{b}$	(-, -0.1)	(-, 1.8)	-

Current signal strengths with their uncertainties and correlations for the 126 GeV resonance used in the fit. 18 measurements

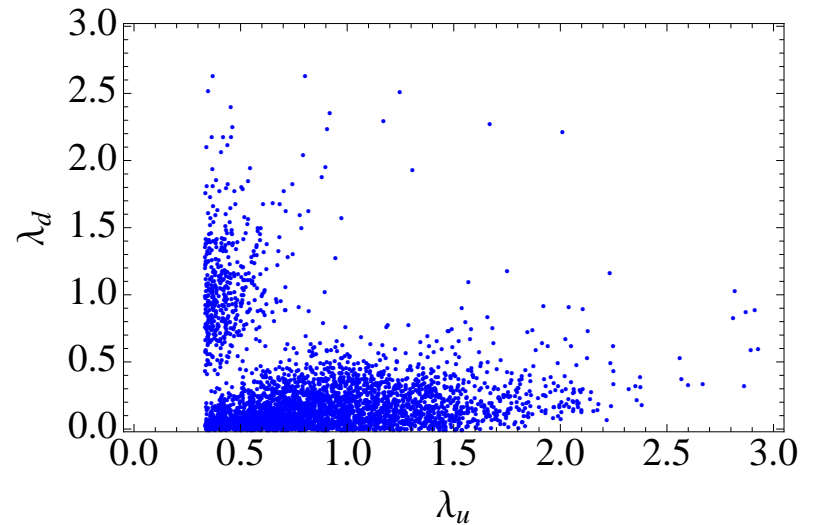
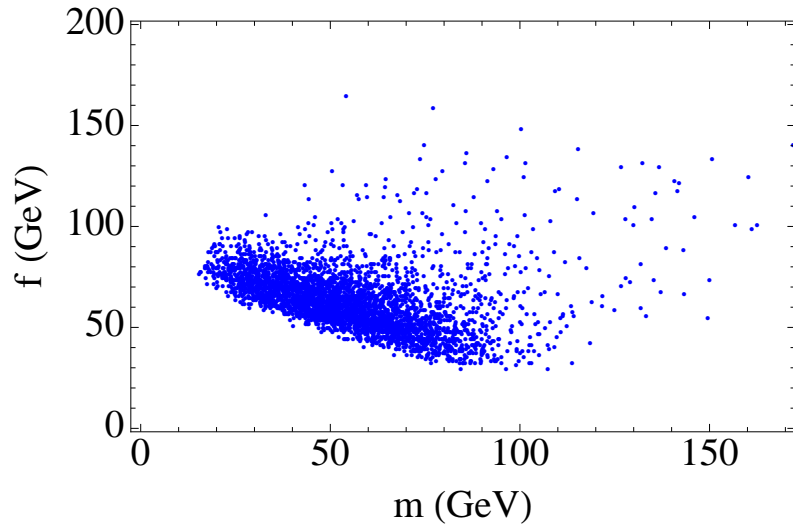
# Preliminary

- 18 measurements, 6 parameters ( $m_{H_u}^2, m_{H_d}^2, B\mu, \lambda_u, \lambda_d, f$ ),  
2 constraints ( $v_W, m_h$ )  $\Rightarrow$  14 d.o.f. + 4 fudge factors for  $Z_i$ , 2 fudge factors for  $m_\sigma$
- restricted  $\tan\beta \in [1/3, 3]$ , and  $m_U, m_D > 0$  with  $|m_U - m_D| < 100$  GeV
- SM  $\chi^2 \approx 5.8$
- the scan has  $\chi_{\min}^2 \approx 4.8$

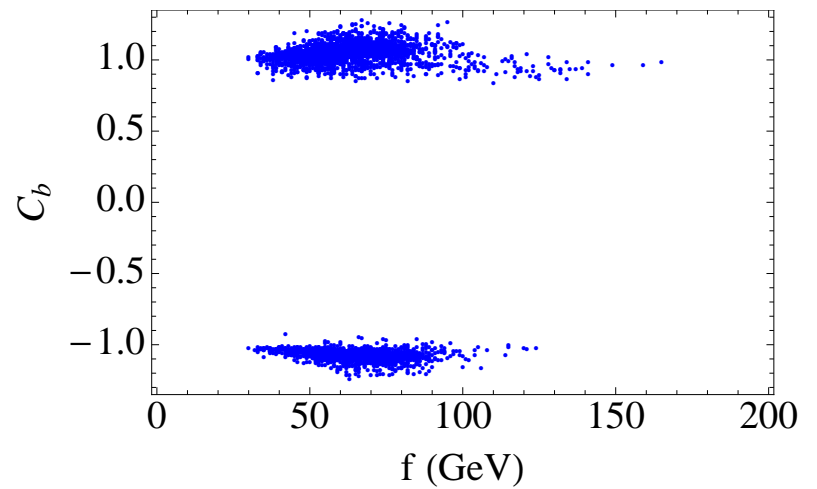
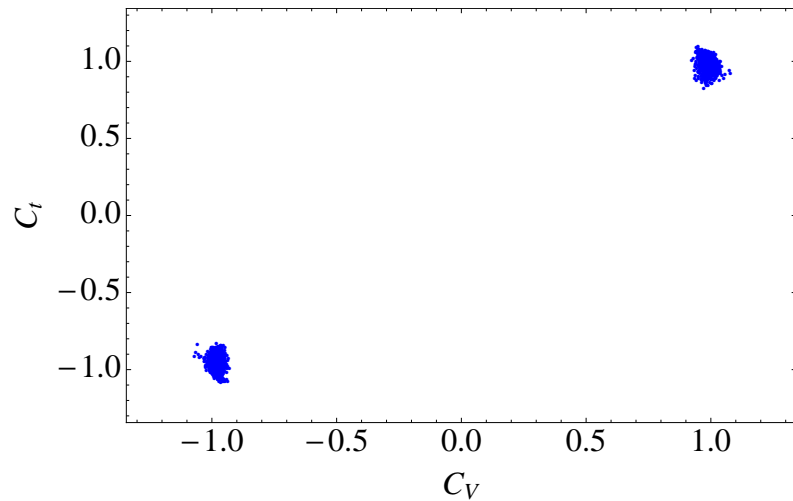


throughout,  $\chi^2$  plots are for points within  $1\sigma$  of  $\chi_{\min}^2$

●  $f$  vs.  $\hat{m}$ , and the technifermion Yukawa couplings  $\lambda_u$  vs.  $\lambda_d$ :

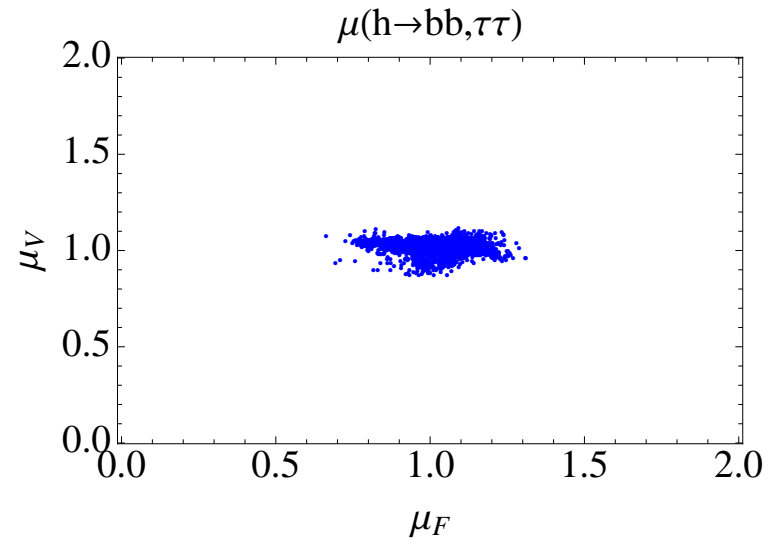
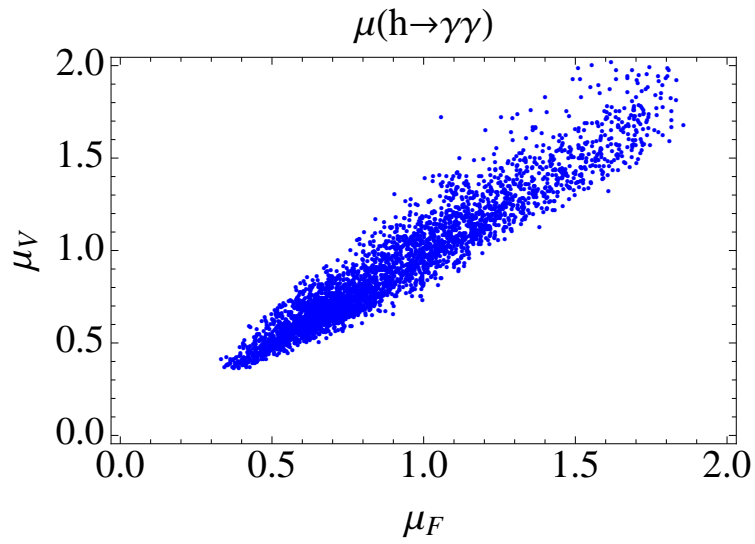


●  $c_V$  and  $c_t$  are ratios of  $hVV$  and  $htt$  couplings to their SM values

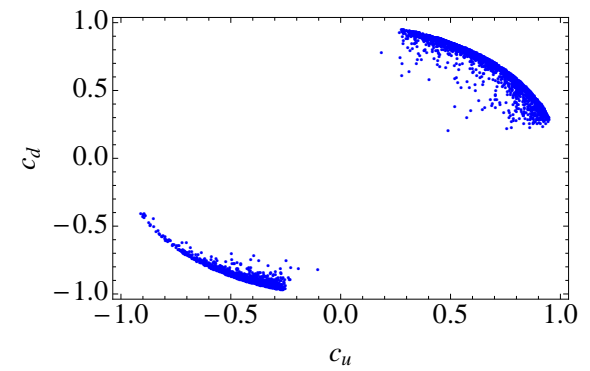
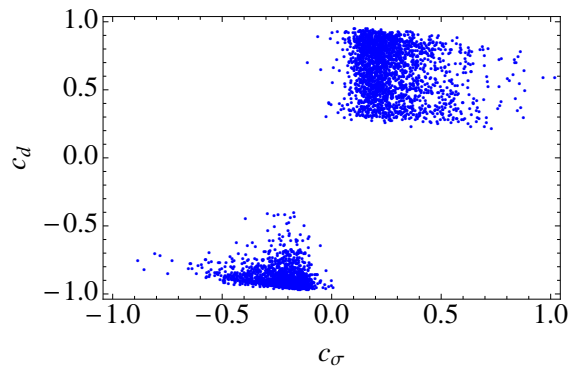
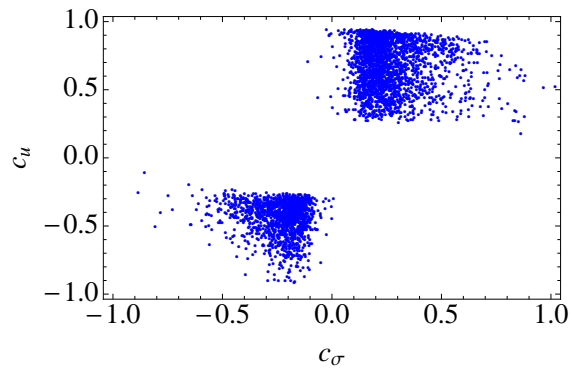


●  $hVV$  and  $htt$  couplings are SM-like;  $h\bar{b}b$ ,  $h\bar{\tau}\tau$  ( $c_b = c_\tau$ ) exhibit mild variation, consistent with  $\tan\beta = O(1)$

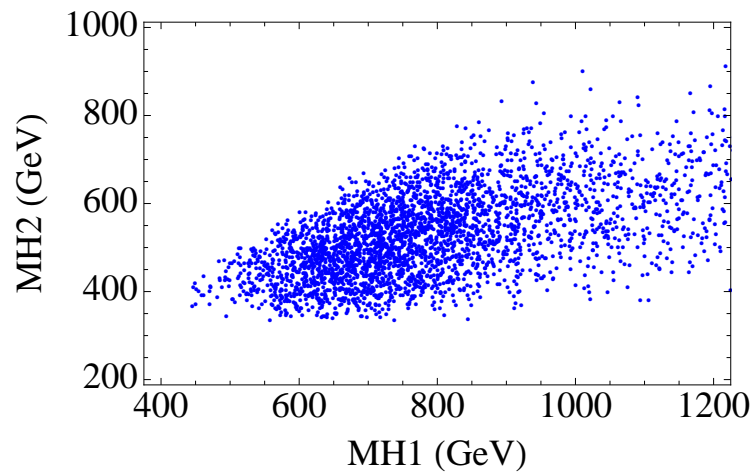
●  $h \rightarrow \gamma\gamma$  signal strengths (left);  $h \rightarrow bb, \tau\tau$  signal strengths (right),  
for vector boson fusion ( $\mu_V$ ) vs. gg ( $\mu_F$ )



● Higgs admixtures with  $\sigma_u, \sigma_d, \sigma$ :  $h = c_u \sigma_u + c_d \sigma_d + c_\sigma \sigma$



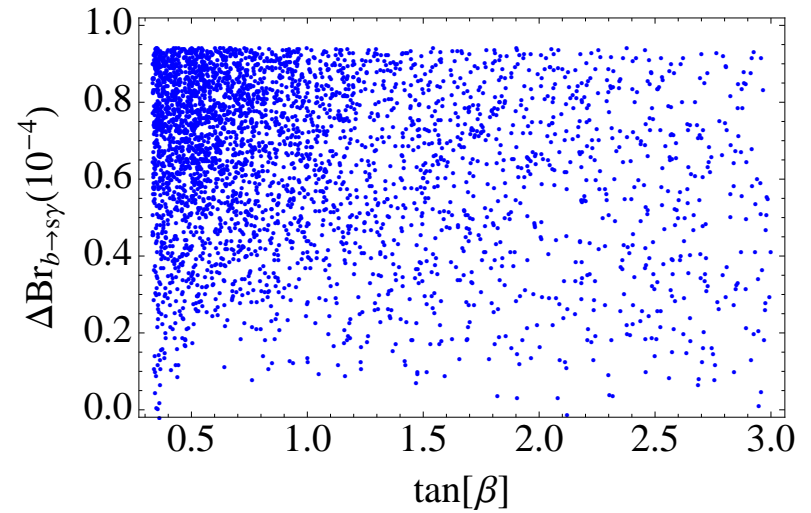
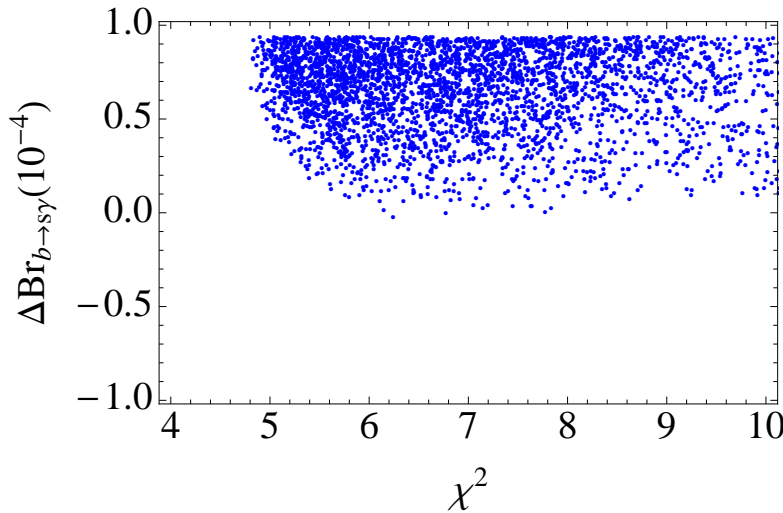
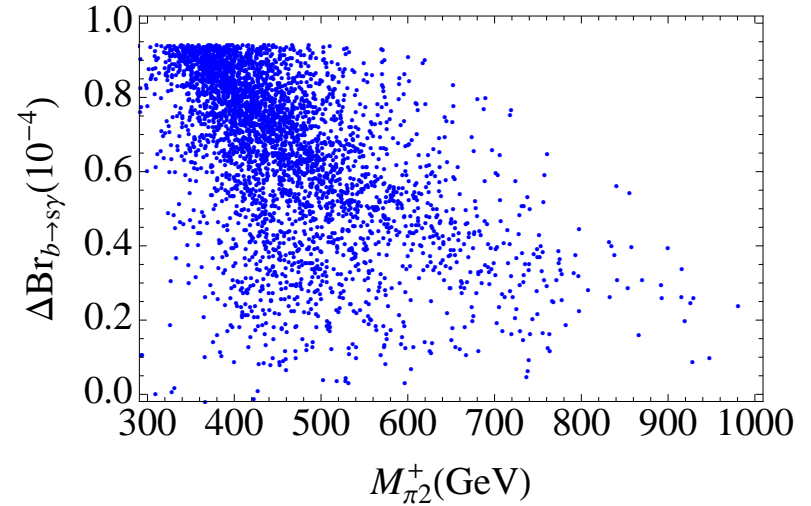
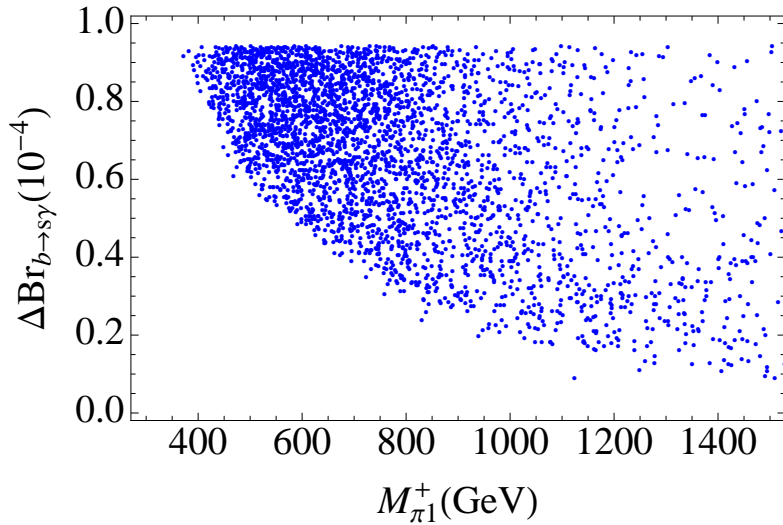
● Heavy Higgs eigenvalues



# $b \rightarrow s \gamma$

presence of charged pions means we should check  $\text{Br}(B \rightarrow X_s \gamma)$ . Define

$$\Delta\text{Br} \equiv \text{Br}_{\text{BTC}} - \text{Br}_{\text{SM}}, \quad \text{compare to } \text{Br}_{\text{exp}} - \text{Br}_{\text{SM}} = (0.28 \pm 0.32) \times 10^{-4}$$

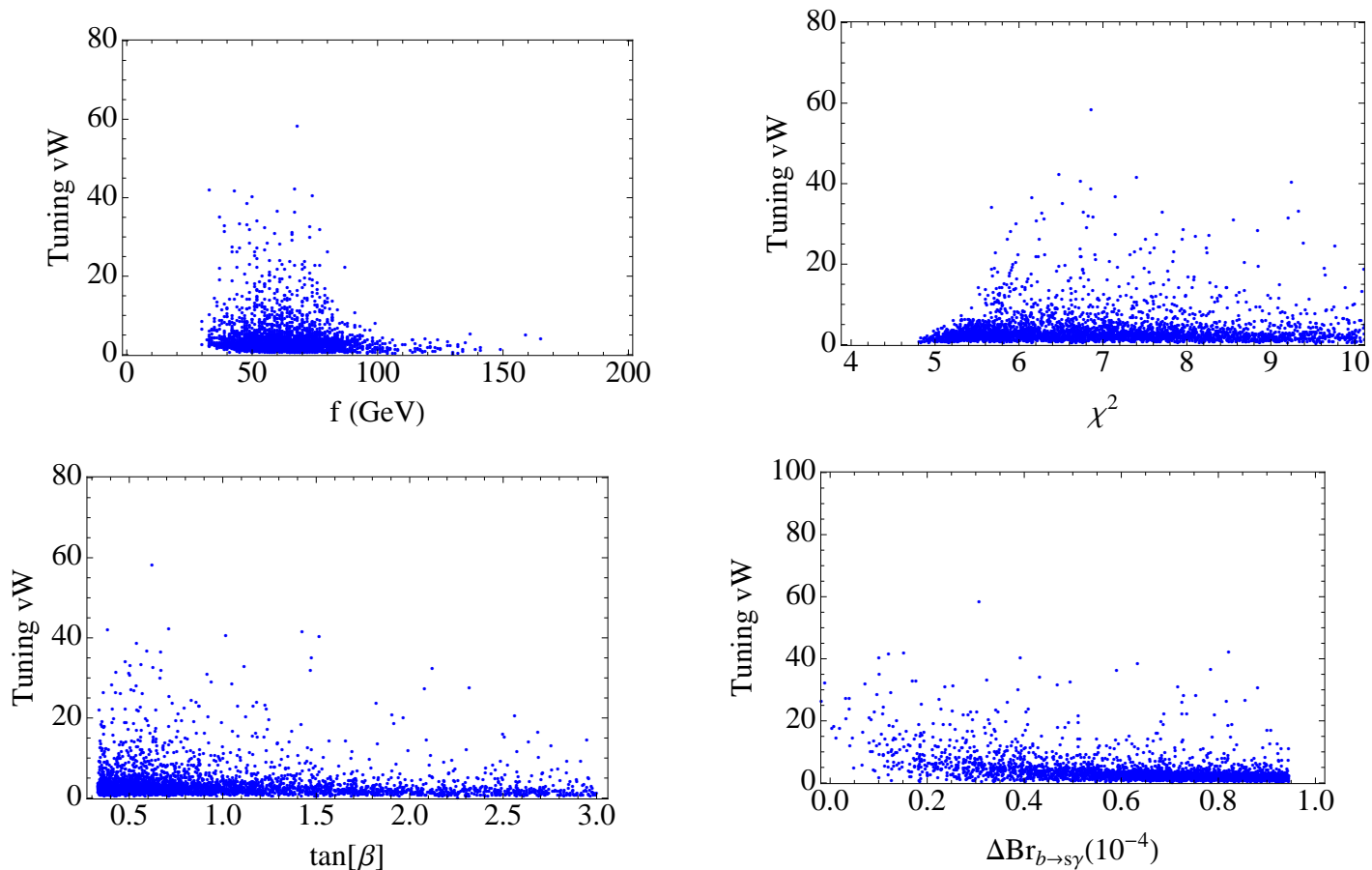


next scan:  $\tan \beta > 1$

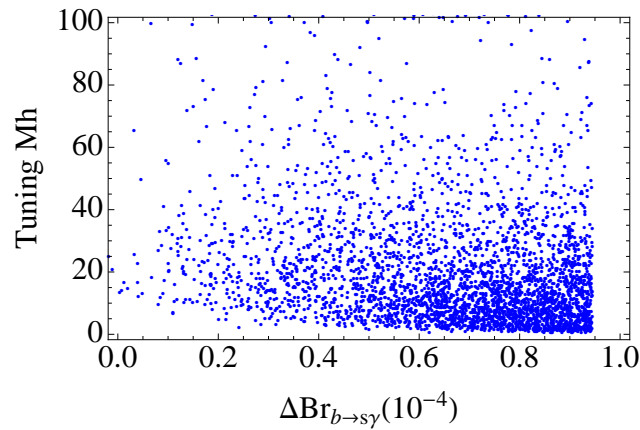
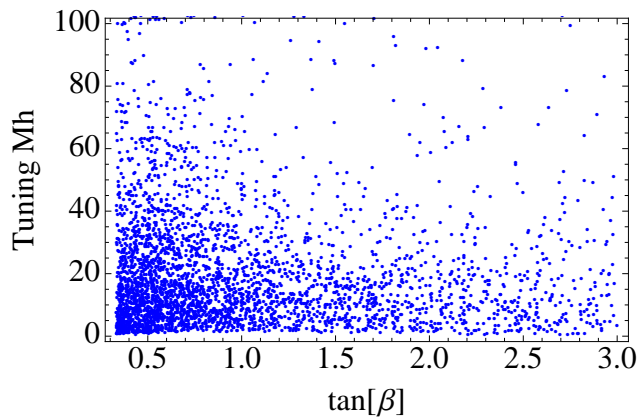
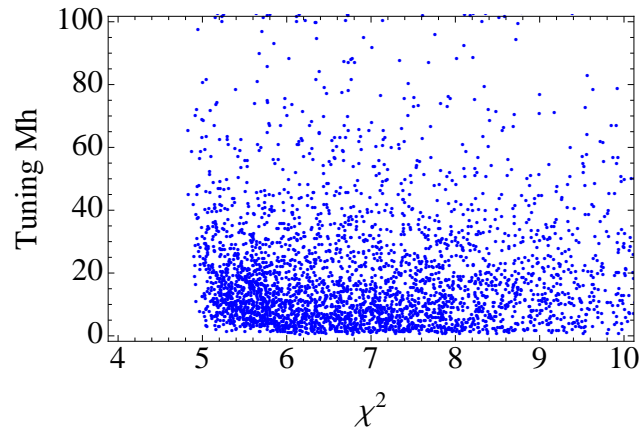
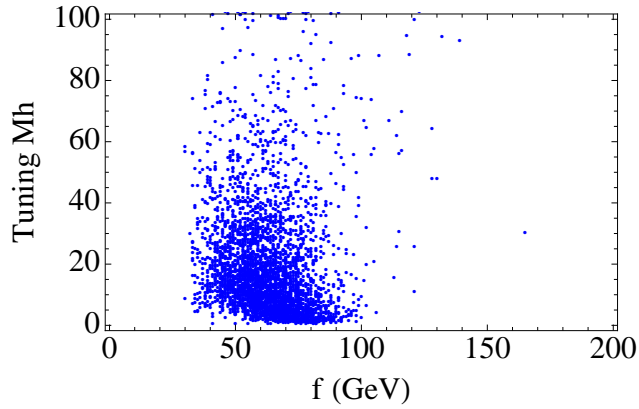
# Tuning from the low energy scale perspective

- consider Barbieri-Giudice type measure for a given solution

$$\text{tuning}_{v_W(m_h)} = \text{Max} \left[ \frac{\partial \log v_W(m_h)}{\partial \log p_i} \right]; \quad p_i = f, \lambda_u, \lambda_d, m_{H_u}^2, m_{H_d}^2, B\mu, \text{ fudge factors}$$



- confirm that  $v_W$  generically does not require significant tuning



- generically, more tuning required for  $m_h = 126$  GeV than for  $v_W$ , but plenty of solutions can be found with moderate  $< 10$  tuning, e.g.  $O(\text{few})$  that are consistent with  $\text{Br}(b \rightarrow s\gamma)$  (particularly for  $\tan \beta > 1$ )



# $\Delta S$ and $\Delta T$ away from the chiral limit

- $\Delta S_{\text{tree}}$  in the narrow width approximation, due the lowest lying  $\rho$ ,  $a_1$  resonances

$$\Delta S_{\text{tree}} = 4\pi \left( \frac{f_\rho^2}{m_\rho^2} - \frac{f_{a_1}^2}{m_{a_1}^2} \right)$$

- $f_\rho$  is well known in QCD,  $f_{a_1}$  is not so well known
- take  $f_{a_1} = 160$  MeV: average of 152 MeV from  $\text{Br}(\tau^+ \rightarrow \nu_\tau \pi^+ \pi^+ \pi^-)$  (Isgur et al. '89 + updated Br measurement) and 168 MeV from QCD sum rules (K.C. Yang '07)

$$\Rightarrow \Delta S_{\text{tree}} \approx \left( .25 \frac{N_{\text{TC}}}{3} \right)$$

agrees with  $\Delta S_{\text{tree}}$  using Weinberg's sum rules in narrow resonance approximation [Peskin, Takeuchi](#)

- but the  $\Delta S_{\text{tree}}$  estimates have essentially been obtained [in the chiral limit](#)  
 $m_{u,d} \ll f$

- what happens far from the chiral limit, as in BTC?
  - based on QCD, lattice, we know that  $m_\rho$  must increase more rapidly than  $f_\rho$  with increasing  $\hat{m}$
  - $m_{a_1}$  is  $\approx 50\%$  larger than  $m_\rho$  (due to  $P$ -wave quark energy)
    - $\Rightarrow$  slower relative increase in  $m_{a_1}$  than  $m_\rho$ , with increasing  $\hat{m}$
- Therefore,  $S_{\text{tree}}$  could **decrease significantly** with increasing  $\hat{m}$ !

- get an idea of the effect from lowest lying  $[s\bar{s}]$  vector  $V_s$  and axial vector  $A_s$  resonance masses and decay constants. Ideally, would evaluate

$$\Delta S'_{\text{tree}} = 4\pi \left( \frac{f_{V_s}^2}{m_{V_s}^2} - \frac{f_{A_s}^2}{m_{A_s}^2} \right)$$

- $f_{V_s} = f_\phi$ ,  $m_{V_s} = m_\phi$  to very good approximation
- $A_s$  is  $O(10\%)$  admixture of  $f_1(1285)$  and  $f_1(1420)$ ; heavier  $f_1(1420)$  is dominantly  $[\bar{s}s]$   $\Rightarrow m_{A_s} < m_{f_1(1420)}$
- but  $f_{A_s} > f_{a_1}$

$$\Rightarrow \Delta S'_{\text{tree}} < 4\pi \left( \frac{f_\phi^2}{m_\phi^2} - \frac{f_{a_1}^2}{m_{f_1(1420)}^2} \right) \approx 0.14 \quad (N_c = 3)$$

compared to chiral limit  $\Delta S_{\text{tree}} \approx 0.25 \quad (N_c = 3)$

- lattice data for  $f_{\eta_h}$ , for variation of  $M_{\eta_h}$  between  $M_{\eta_c}$  and  $M_{\eta_b}$  gives an excellent approximation for the variation of the quarkonium decay constant between the  $J/\psi$  and  $\Upsilon$  [HPQCD, 1207.0994](#)
- combining with known  $f_\rho, f_\omega, f_\phi$  in QCD get an approximate extrapolation for quarkonium decay constants over a wide range of  $\hat{m}$ . Rescale to BTC via scale factor  $f/f_\pi \Rightarrow$

$$f_\rho[\hat{m}] = f_\rho^{\text{QCD}} \frac{f}{f_\pi} \mathcal{F} \left[ \frac{m_\rho[\hat{m}]}{m_\rho[0]} \right]$$

- the dependence of the BTC  $\rho$  and  $a_1$  masses on  $\hat{m}$  approximated by scaling from a naive quark model estimate of the QCD light vector mass dependence on  $\hat{m}$ :

$$m_{\rho(a_1)}^2[\hat{m}] \approx m_{\rho(a_1)}^2 \text{QCD} \left( \frac{f}{f_\pi} \right)^2 \frac{3}{N_{TC}} + 2\mu_{V(A)} \frac{f}{f_\pi} \sqrt{\frac{3}{N_{TC}}} \hat{m}$$

with  $\mu_V, \mu_A \approx 2.2$  GeV from naive quark model QCD fit.

- For illustration, will assume TC  $f_{a_1}$  has same extrapolation as TC  $f_\rho$ , i.e.

$$f_{a_1}[\hat{m}] = f_{a_1}^{\text{QCD}} \frac{f}{f_\pi} \mathcal{F} \left[ \frac{m_{a_1}[\hat{m}]}{m_{a_1}[0]} \right]$$

●  $\Delta T_{\text{tree}}$  from

$$\mathcal{L} \sim \left( \text{Tr} \left[ \Phi_{\Lambda} D^{\mu} \Sigma^{\dagger} \right] \right)^2 \Rightarrow \Delta T_{\text{tree}} \sim \frac{1}{16\pi^2 \alpha} \frac{(m_U - m_D)^2}{v_W^2}$$

- e.g.  $\Delta T_{\text{tree}} < 0.10$  corresponds to  $|m_U - m_D| \lesssim 90 \text{ GeV}$
- imposed  $|m_U - m_D| < 100 \text{ GeV}$  on the scan

## $\Delta S_{\text{loop}}, \Delta T_{\text{loop}}$ from loops with (pseudo) scalars, $Z, W$

- including the TC  $\sigma$ , we can directly carry over the results for  $S$  and  $T$  at one loop in multi-Higgs doublet models [Grimus, Lavoura OGREID, OSLAND '08](#)  
-with [three](#) doublets in BTC
- including the SM subtraction yields scale independent results
- for simplicity we have not included loops containing the  $\rho, a_1$ . However, with the SM scale dependent contribution already subtracted in  $\Delta S_{\text{loop}}$ , we can consistently approximate the TC resonance contributions at tree-level
  - the scale dependence is removed because the  $\sigma$  is included
  - contributions of loops with vectors to  $\Delta S$  can be neglected [Orgogozo, Rychkov](#)

●  $\Delta T_{\text{loop}}$  from to  $\pi^+ - \pi^-$  mass splitting

- previous authors considered  $\pi^+ - \pi^-$  mass splitting via the operator

$$f^2 \text{Tr} \left( \left[ \Phi_\Lambda \Sigma^\dagger \right] - \text{h.c.} \right)^2$$

- 1-loop diagrams with  $\pi$ 's, Higgs then yield a scale dependent (log-divergent) contribution to  $\Delta T$  - interpreted as logarithmic enhancement by setting the cutoff scale to  $\Lambda_\chi \sim 4\pi f$ .
- therefore thought to dominate over  $\Delta T_{\text{tree}}$

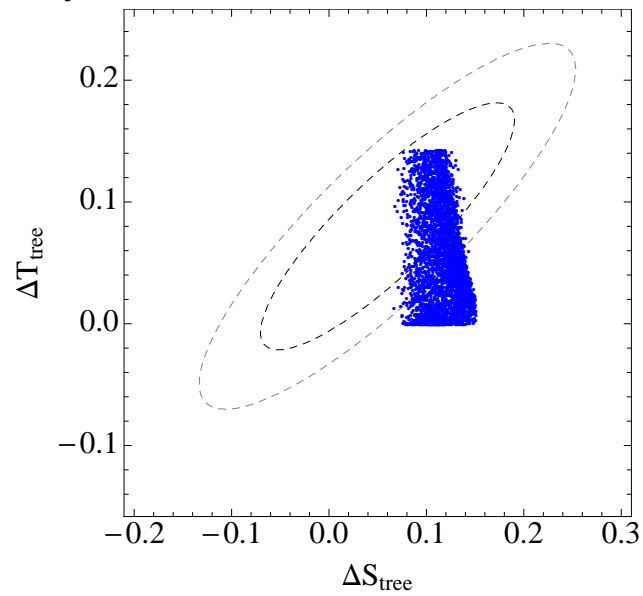
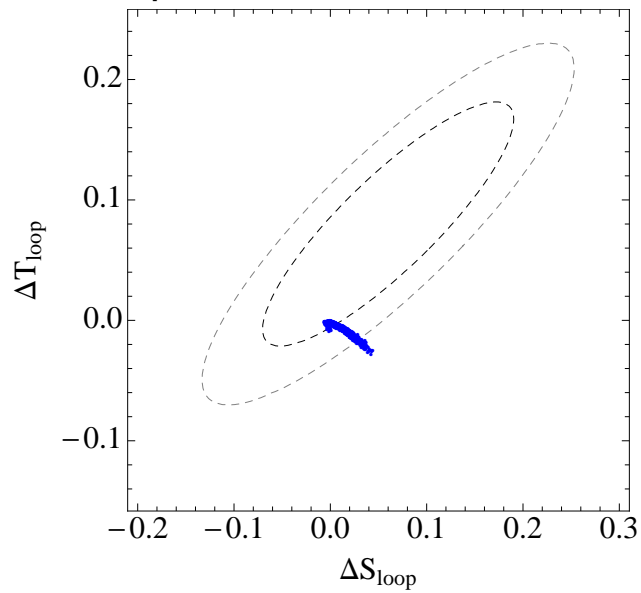
● instead the  $\pi^+ - \pi^0$  mass splitting should be attributed to  $\pi - \eta'$  mixing - this should be the dominant source.

- adapting the QCD  $\pi - \eta - \eta'$  mixing formalism in [Kroll '08](#) to  $\pi - \eta'$  mixing in BTC (scaling from QCD), and also including the  $\eta'$  in  $\Delta T_{\text{loop}}$  yields finite, negligible corrections to  $\Delta T < 0.001$
- therefore can ignore the effect of the  $\eta'$  or  $\pi^+ - \pi^0$  mass splitting

# Results for $\Delta S$ , $\Delta T$ in BTC



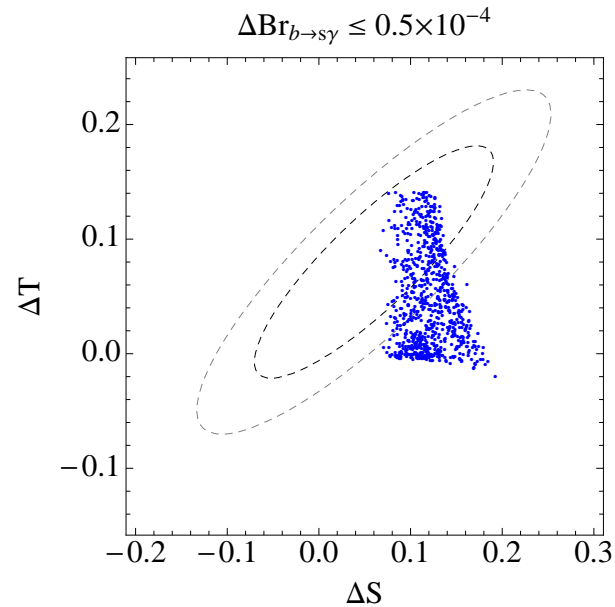
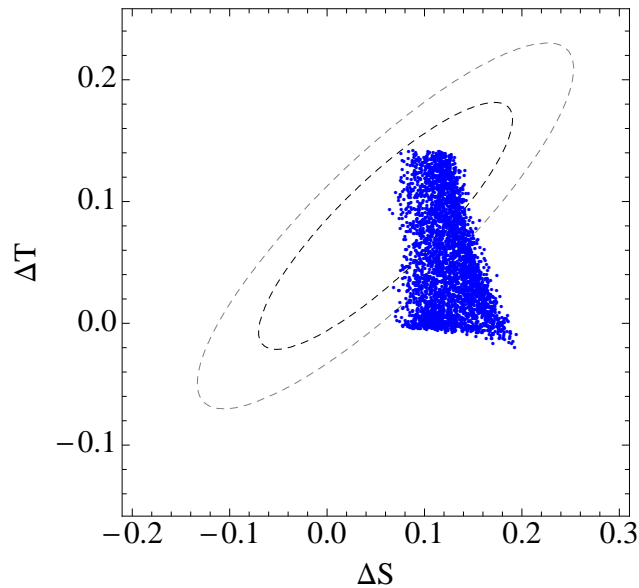
the loop and tree contributions separately:



$1\sigma$  and  $2\sigma$  ellipses from [Ciuchini et al](#)



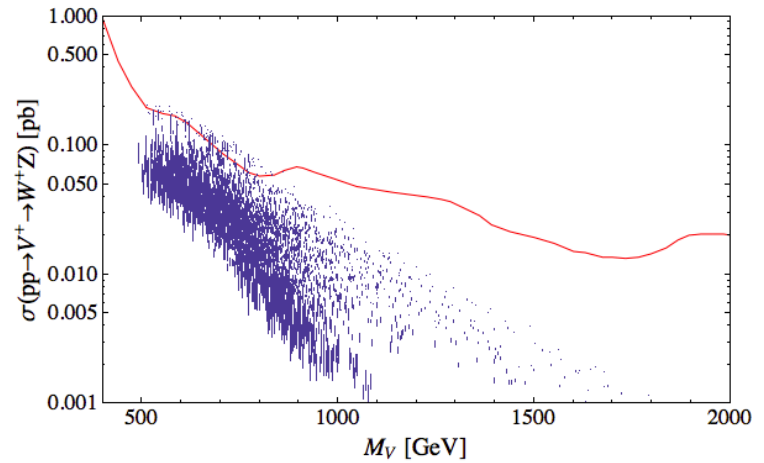
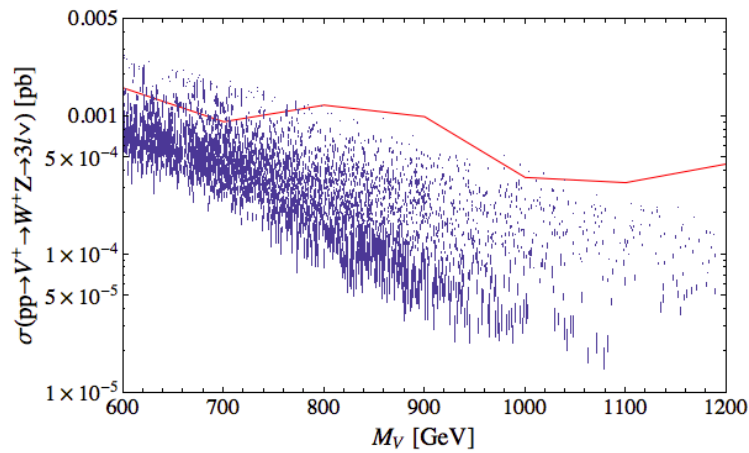
- totals of loop and tree:



- BTC is a technicolor example which can satisfy the constraints on  $S$  and  $T$  **at 1 $\sigma$**  via QCD-like dynamics,
  - no need to invoke unproven conjectures about exotic strong interactions, e.g. conformal or walking dynamics
  - this is because BTC is realized away from the chiral limit

# Vector phenomenology

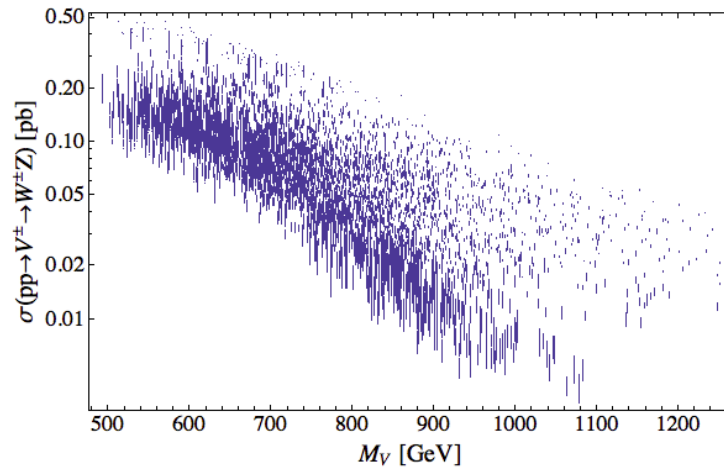
- employ chiral Lagrangian formalism for vectors [Ecker et al. '89](#)
- for now consider LHC bounds on Drell-Yan production  $\sigma(pp \rightarrow \rho^\pm \rightarrow W^\pm Z)$
- use CMS  $19.6 \text{ fb}^{-1}$   $W' \rightarrow WZ$  trilepton search at 8 TeV [CMS PAS EXO-12-025](#);  
ATLAS  $20 \text{ fb}^{-1}$   $W' \rightarrow WZ \ell\ell q\bar{q}$  search at 8 TeV [1409.6190](#)
  - CMS and ATLAS present bounds for narrow  $W'$
  - we compare to  $pp \rightarrow \rho \rightarrow WZ$  cross section in  $\rho$  narrow width approximation
  - the  $\rho$  width is typically  $\lesssim 5\%$ , so reasonable approximation.
  - Taking into account the  $\rho$  width only weakens the constraints

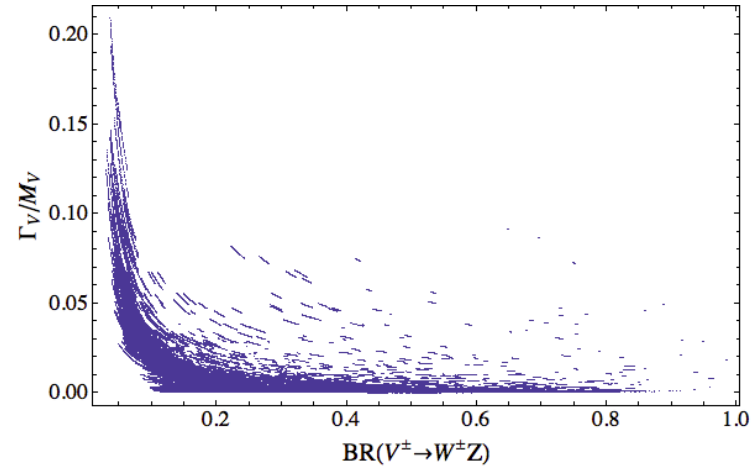
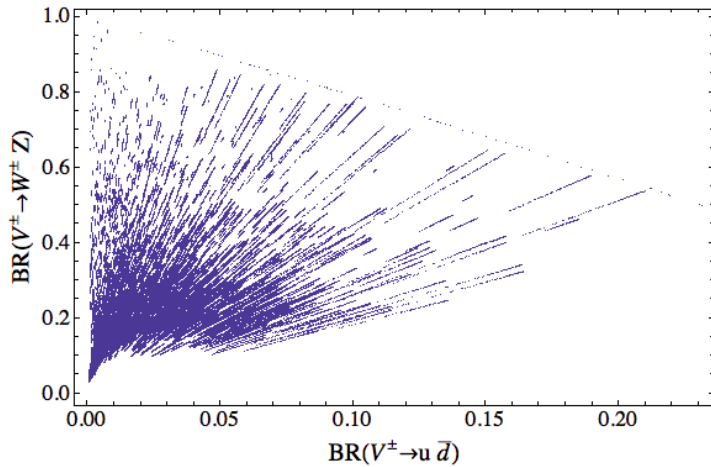


Comparison of  $\sigma(pp \rightarrow \rho \rightarrow WZ)$  to CMS bound (left), ATLAS bound (right)

$\Rightarrow$  predicted cross sections typically lie  $O(\text{few} - 10)$  below LHC bounds, except at lower  $m_\rho$ .

$\sigma(pp \rightarrow \rho \rightarrow WZ)$  at 14 TeV





● reason for weak bounds:  $\rho f f$  coupling  $\sim f_\rho/m_\rho$  and  $\rho W W$  coupling  $\sim m_\rho/f_\rho$ . therefore  $\text{Br}(\rho \rightarrow \bar{u}d)$  is small

● in narrow width approximation, partonic cross section

$$\sigma(u\bar{d} \rightarrow \rho \rightarrow WZ) \approx \frac{4\pi^2}{3} \frac{\Gamma_\rho}{m_\rho} \text{Br}(\rho \rightarrow u\bar{d}) \text{Br}(\rho \rightarrow WZ)$$

● Sensitivity to the  $\rho$  (and  $\sigma$ ) in  $WW$  scattering is probably more promising

# Summary

- The Higgs in BTC is dominantly fundamental
- Get very good fit to LHC Higgs phenomenology
  - unfortunately,  $h \rightarrow \gamma\gamma$  can only be estimated in NDA
- $\text{Br}(b \rightarrow s\gamma)$  provides an important constraint
- from the low energy perspective,  $v_W$  generically requires little or no tuning; for  $m_h$  moderate tuning of  $O(\text{few})$  can be obtained, while maintaining consistency with all constraints
- $S$  and  $T$  can easily lie within the  $1\sigma$  ellipse, primarily due to the effect of technifermion masses on the TC resonance contributions

- LHC bounds on Drell-Yan production of the vector resonances  $O(\text{few} - 10)$  above predicted cross sections
  - sensitivity to the  $\rho$  and  $\sigma$  in  $WW$  scattering is interesting to explore in Run-2
- important to study the LHC phenomenology of the heavier Higgs's and charged pions  
Chang, Evans, Luty; Chang, Galloway, Luty, Salvioni, to appear
- we are exploring potential benefits of  $R$ -symmetric BTC for
  - linkage of  $m_{\text{susy}}$  and  $\Lambda_{\text{TC}}$
  - solution of the  $\mu$  problem via partial compositeness
  - reduced sensitivity to the UV scale due to supersoft properties