

# Recent MINERvA results and implications for neutrino energy reconstruction

NuFACT 2014

25-30 August 2014

University of Glasgow, Glasgow, Scotland



Jeremy Wolcott

University of Rochester

(on behalf of the MINERvA collaboration)

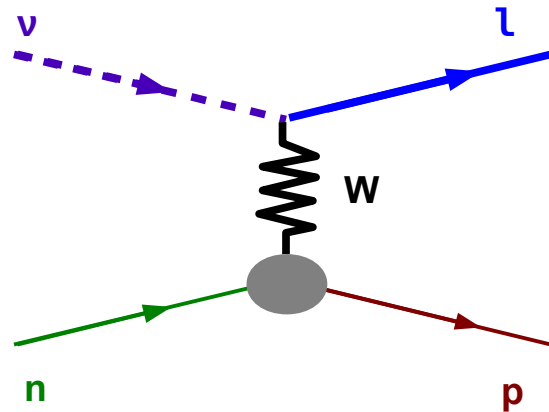


# Outline

- Introduction: your  $E_\nu$  distribution's dependence on models
- How MINERvA data reins models in:
  - CCQE scattering
  - Resonant charged pion production
  - Coherent pion production
- Summary and outlook

# Ingredients for measuring $\{E_\nu\}$

1. Estimator = f(observables)



$$E_\nu^{QE} = \frac{m_n^2 - (m_p - E_b)^2 - m_\mu^2 + 2(m_p - E_b)E_\mu}{2(m_p - E_b - E_\mu + p_\mu \cos \theta_\mu)}$$

Fan favorite (and simplest case!): CC quasi-elastic  
(let's consider as test case)

# Ingredients for measuring $\{E_\nu\}$

## 2. Signal model

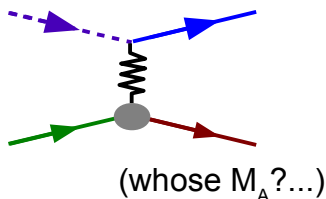
CCQE formula only applies to CCQE events.  
What should CCQE look like in my detector,  
with my neutrino flux?



Generator predictions

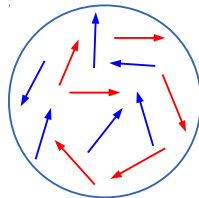
e.g.:

Free nucleon  
cross-section  
[Llewellyn Smith, 1972]



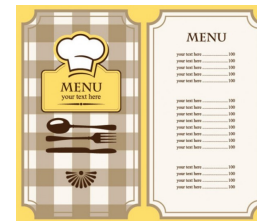
+

Relativistic Fermi Gas  
(RFG) of nucleons  
[Smith & Moniz, 1972]



+

Choose your  
favorite nucleon  
correlation model(s)



# Ingredients for measuring $\{E_\nu\}$

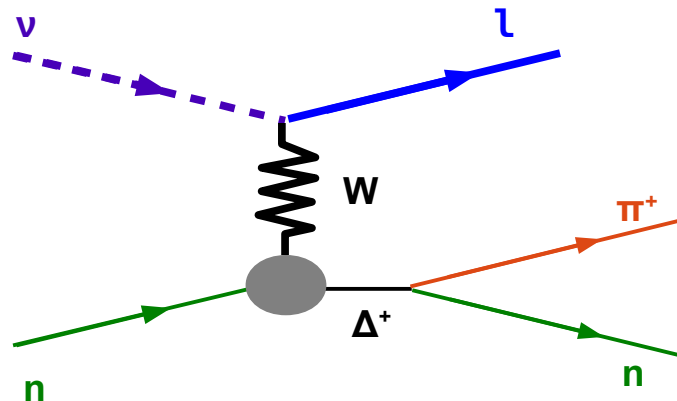
## 3. Background model

CCQE formula only applies to CCQE events.  
What other kinds of events might I need to subtract off?



Generator predictions

e.g.:

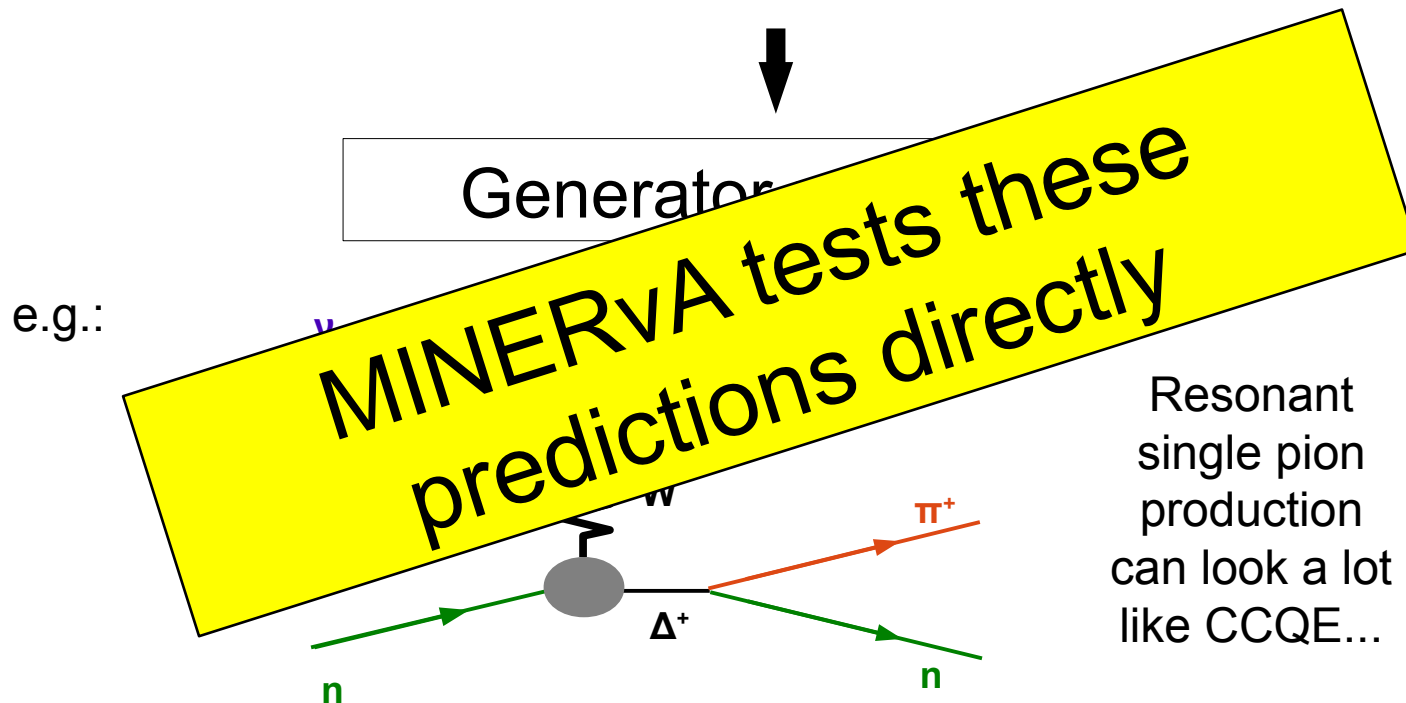


Resonant  
single pion  
production  
can look a lot  
like CCQE...

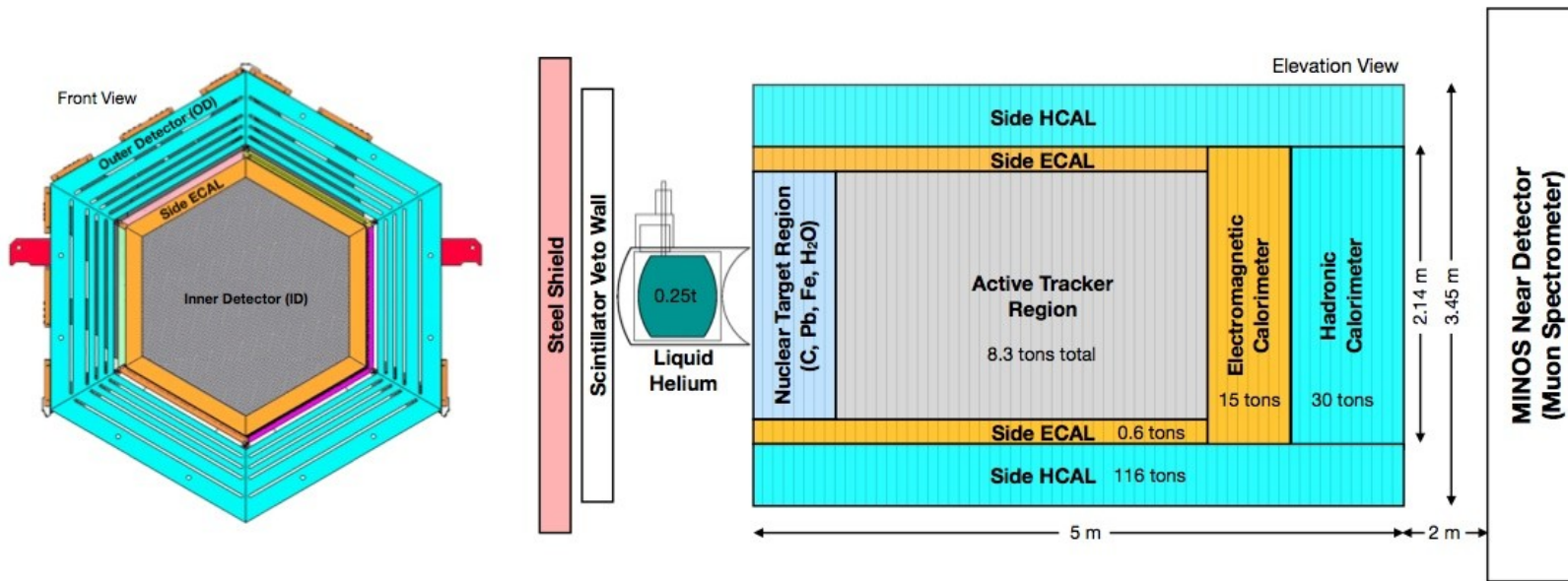
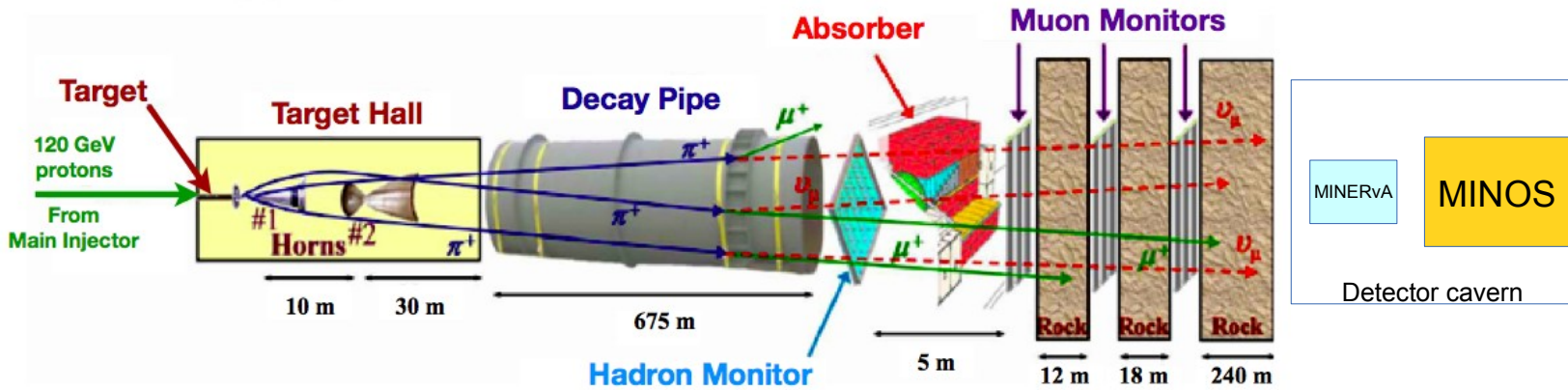
# Ingredients for measuring $\{E_\nu\}$

## 3. Background model

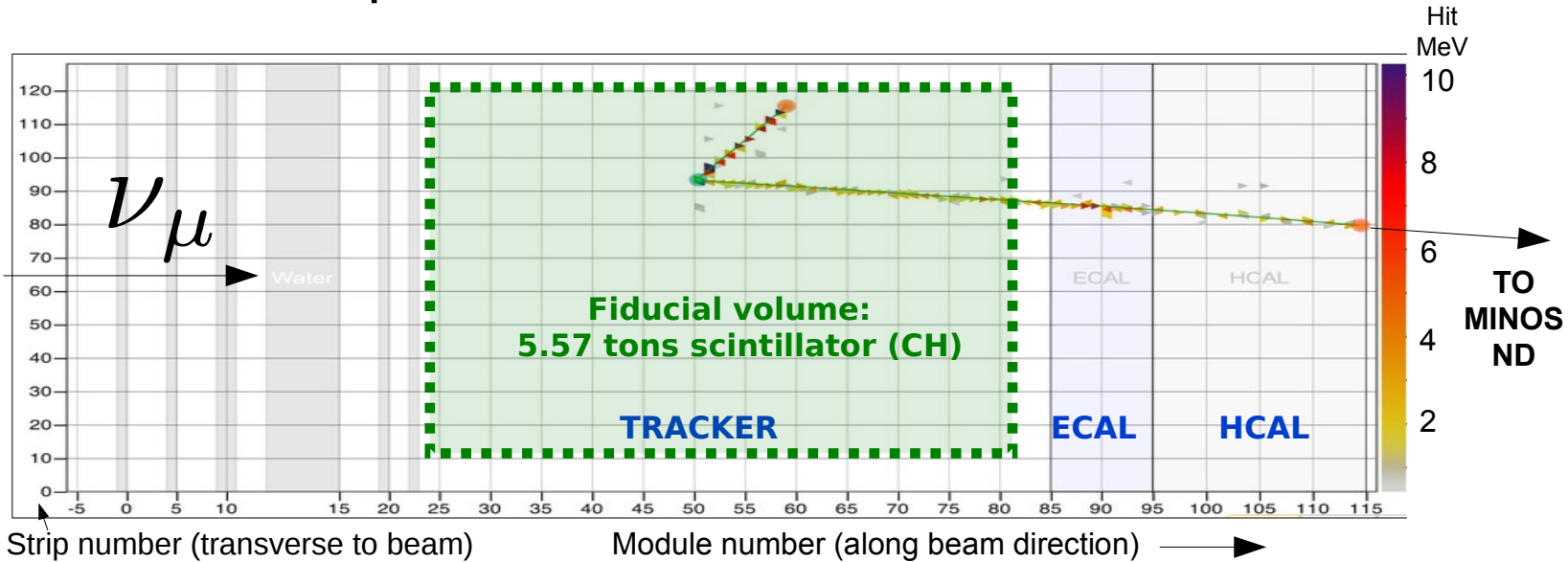
CCQE formula only applies to CCQE events.  
What other kinds of events might I need to subtract off?



# Enter: MINERvA



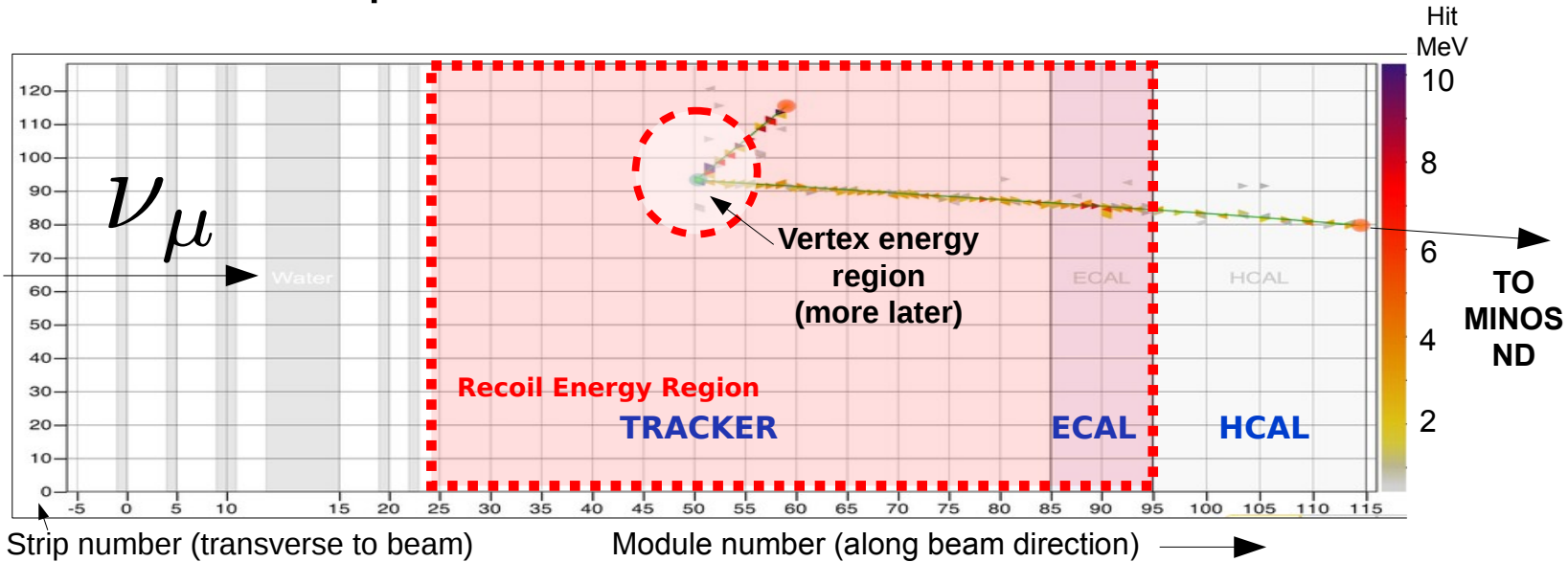
# $\nu_\mu$ CCQE in MINERvA



Find a MINOS-matched track...

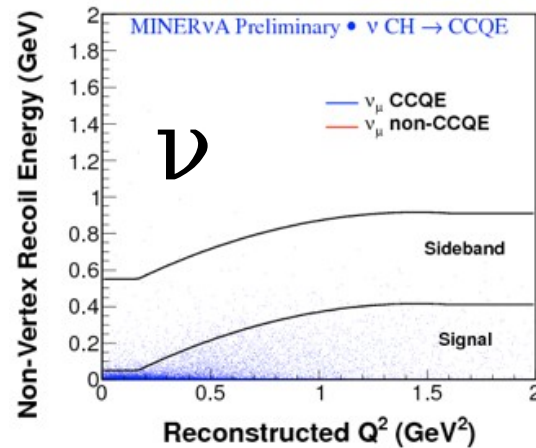


# $\nu_\mu$ CCQE in MINERvA

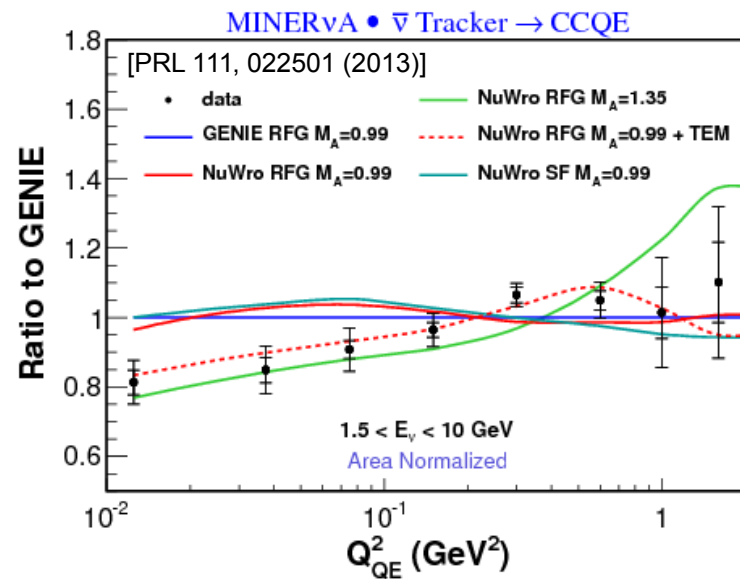
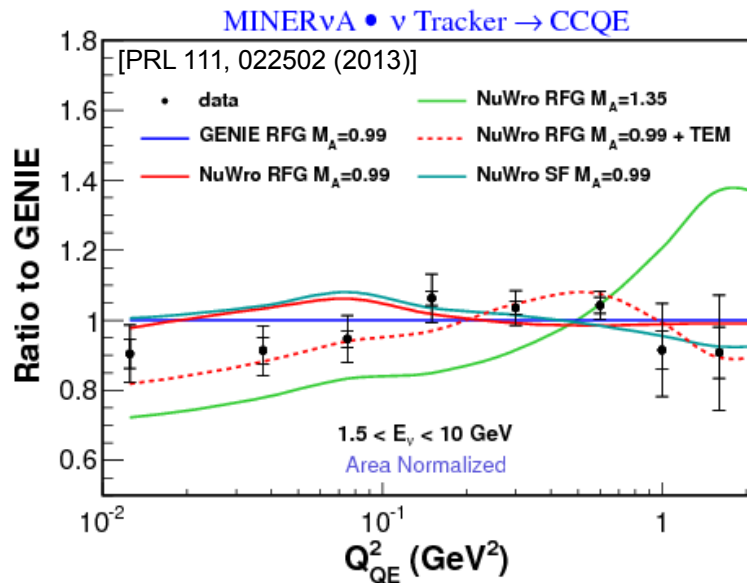


... in an event with little (non-vertex) recoil energy.

[We furthermore cut events with more than 2 (1) isolated shower(s) in (anti-)neutrino mode.]



# $\nu_\mu$ CCQE: model comparisons

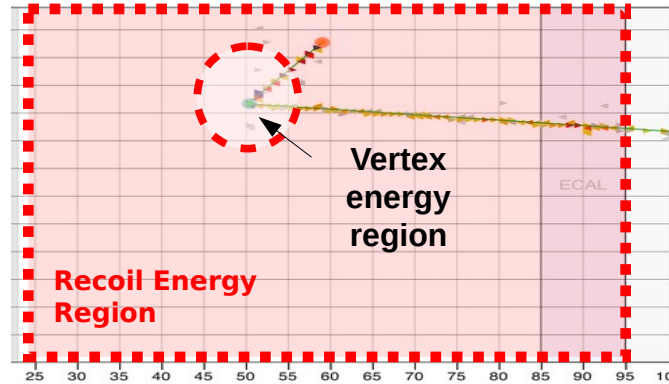


NuWro model	RFG $M_A = 0.99$	RFG + TEM $M_A = 0.99$	RFG $M_A = 1.35$	SF $M_A = 0.99$
$\nu$ shape $\chi^2/\text{d.o.f.}$	4.1	1.7	2.1	3.8
$\bar{\nu}$ shape $\chi^2/\text{d.o.f.}$	2.9	0.7	1.7	3.0

Model most preferred is “vanilla” RFG  
 + empirical corrections for correlations (motivated by electron scattering)  
 (10-20% deviations from GENIE in some regions of phase space)

# Corroboration: vertex activity

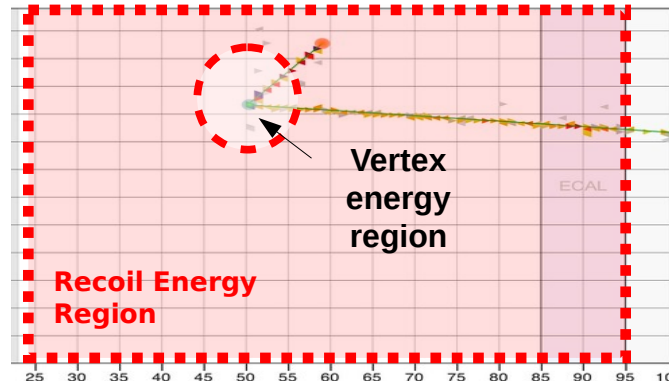
Remember the “blind spot” we left  
in the recoil region?  
Nuclear activity from extra  
correlated nucleon should show  
up there...



# Corroboration: vertex activity

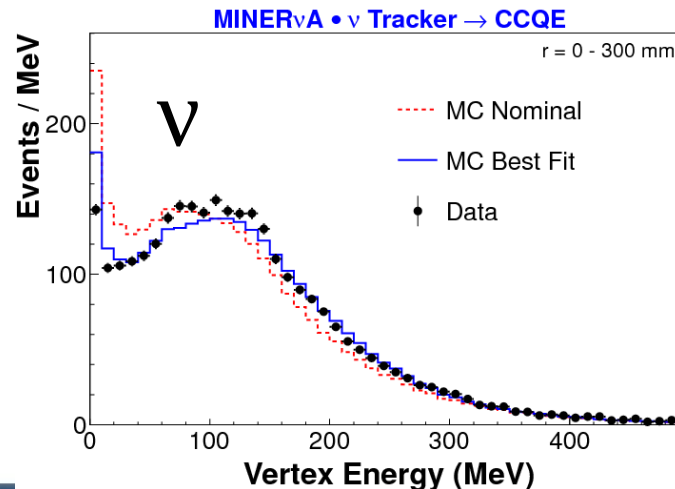
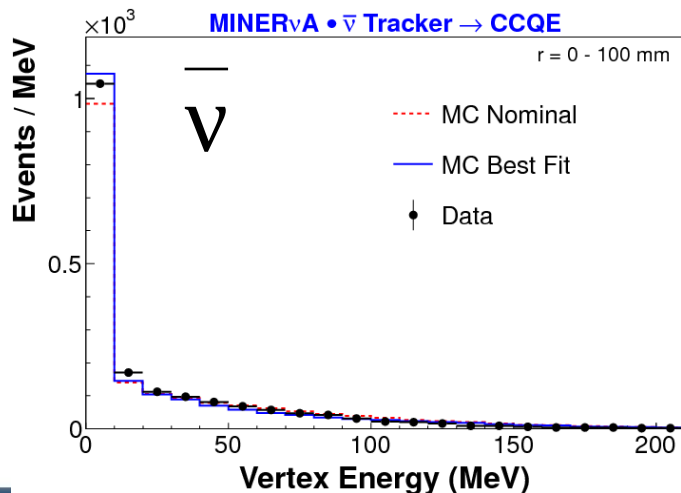
Remember the “blind spot” we left in the recoil region?

We fitted the distribution of energy in this region by adding a simulated proton to some events.



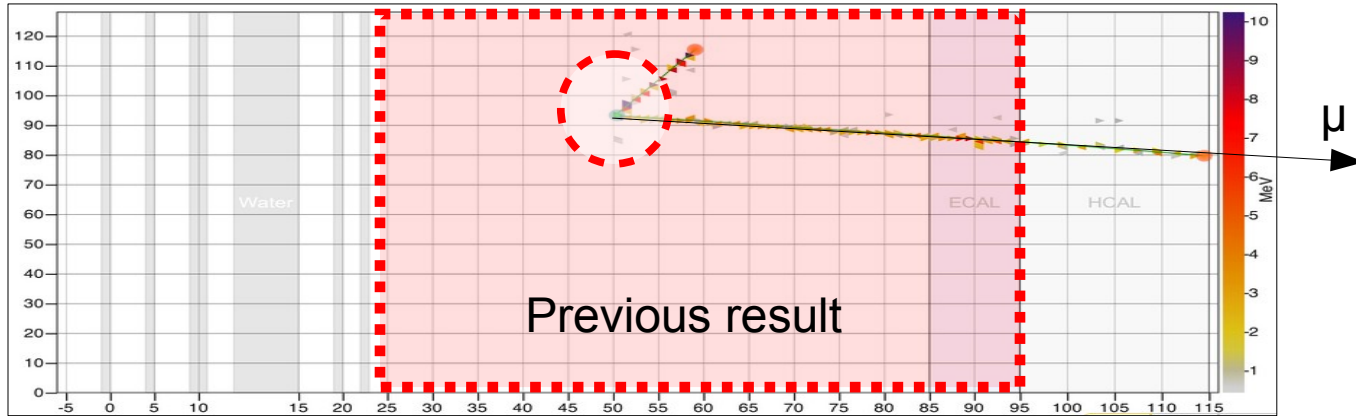
~(25±10)% of events in neutrino mode needed another proton to make the vertex energy distribution fit; contrast (-10±7)% in antineutrino mode

Since CCQE takes  $n \rightarrow p$  for  $\nu$  and  $p \rightarrow n$  for  $\bar{\nu}$   
*this suggests (unmodeled) initial-state np correlations*

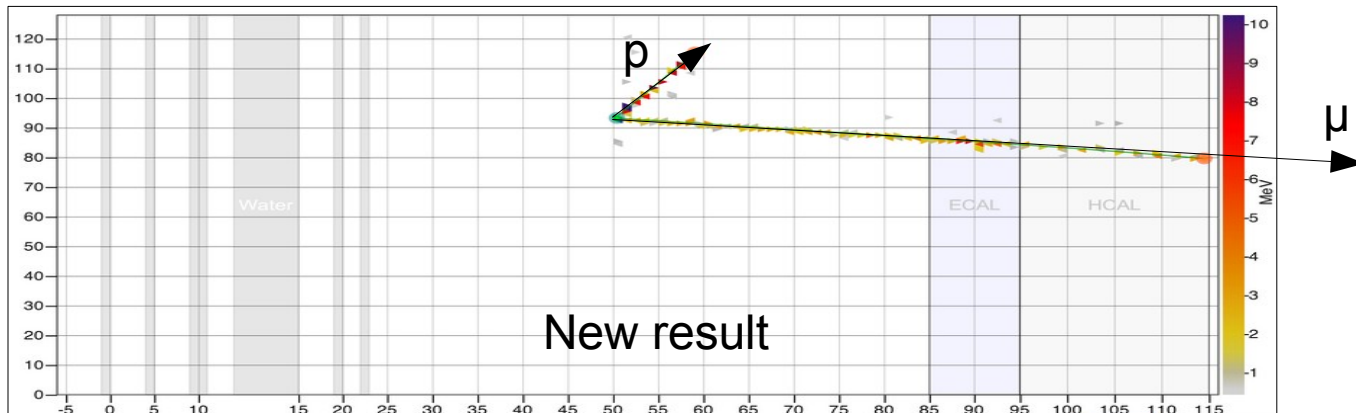


# A different approach: CCQE with proton kinematics

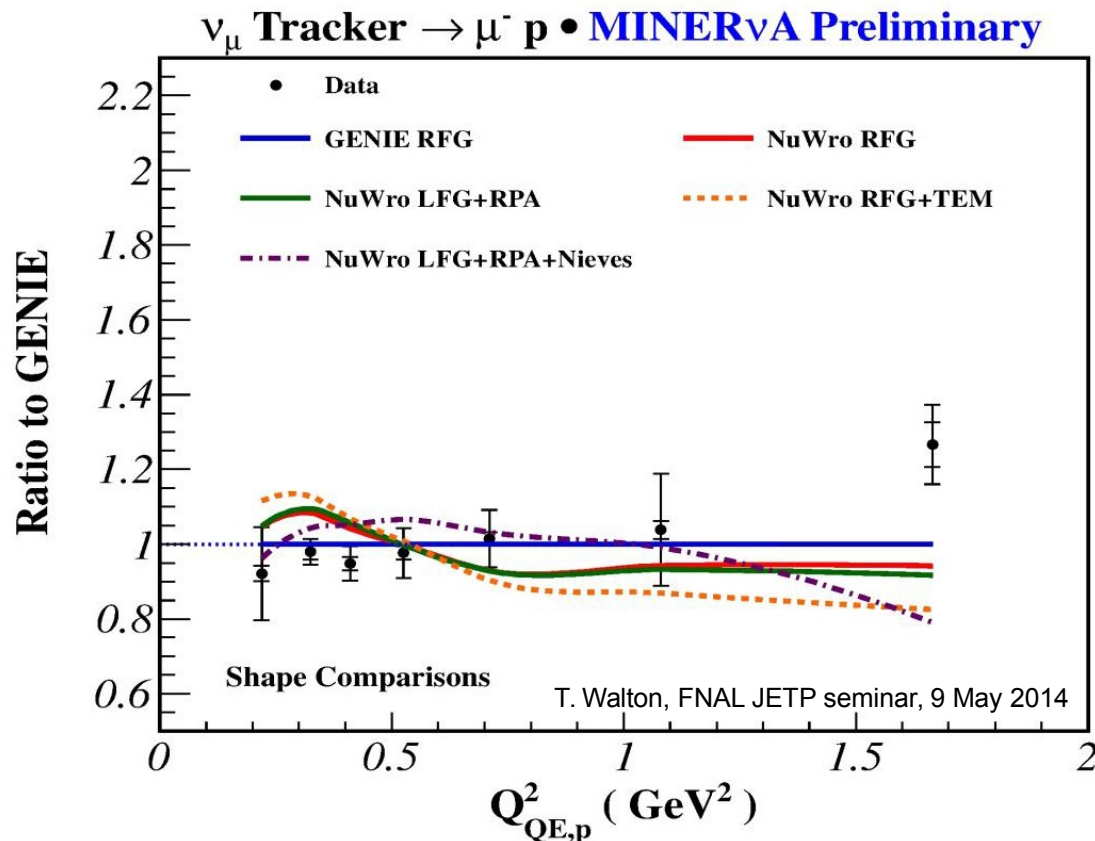
Use  $\mu$  track,  
recoil for  
selection;  
use  $\mu$  track  
for  
kinematics



Use  $\mu$  and p  
tracks and  
recoil for  
selection;  
use p track  
for  
kinematics



# A different approach: CCQE with proton kinematics



The results agree with the “vanilla” GENIE model reasonably well (!)

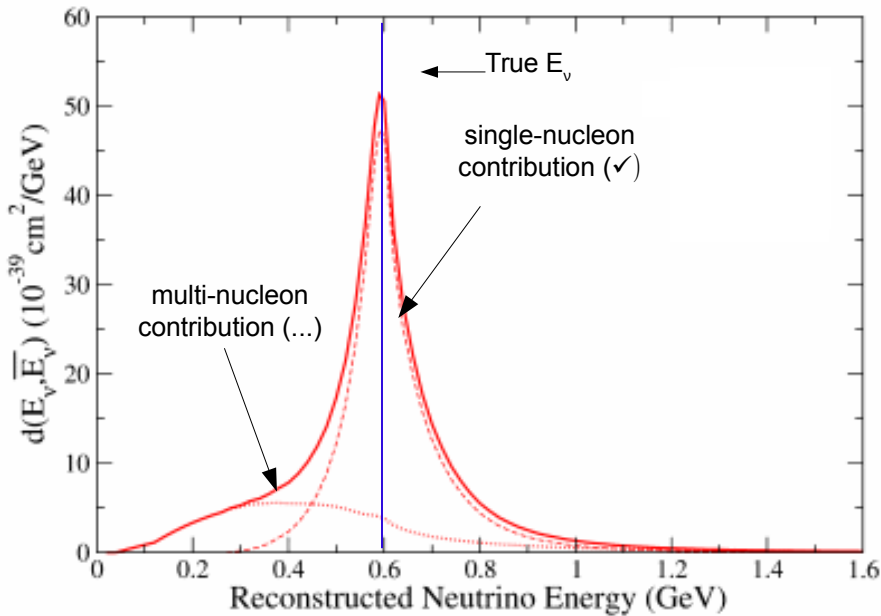
# The (CCQE) lesson

How well you know the final-state particle content influences how well you can reconstruct the kinematics of an event

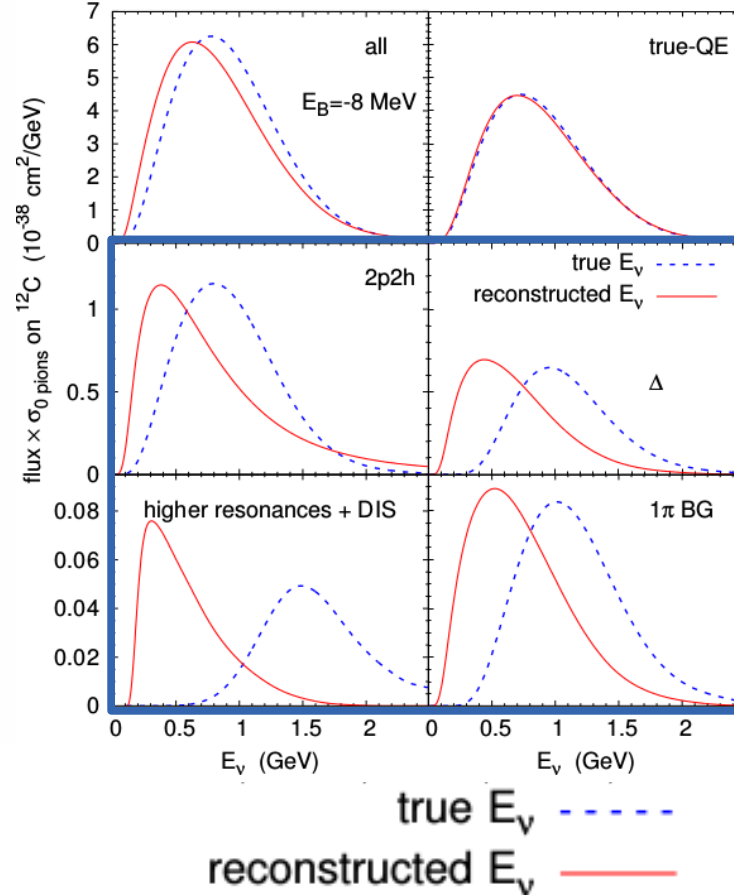
- RFG model struggles to get muon kinematics right for less restrictive “ $\mu$ +little recoil”
- RFG model does ok at predicting proton kinematics in known “ $\mu$ +p” events

# Getting the kinematics wrong

[Adapted from Martini *et al.*, arXiv:1211.1523 by P. Rodrigues]



[Lalakulich *et al.*, arXiv:1208.3678]



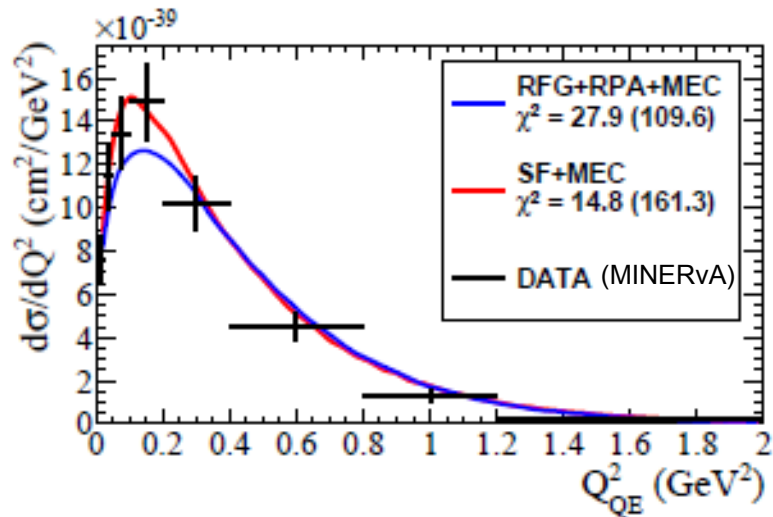
Not  
CCQE  
from  
quasi-free  
nucleon!

Worry that not accounting for the correlations could have significant consequences for  $E_\nu$  reconstruction...

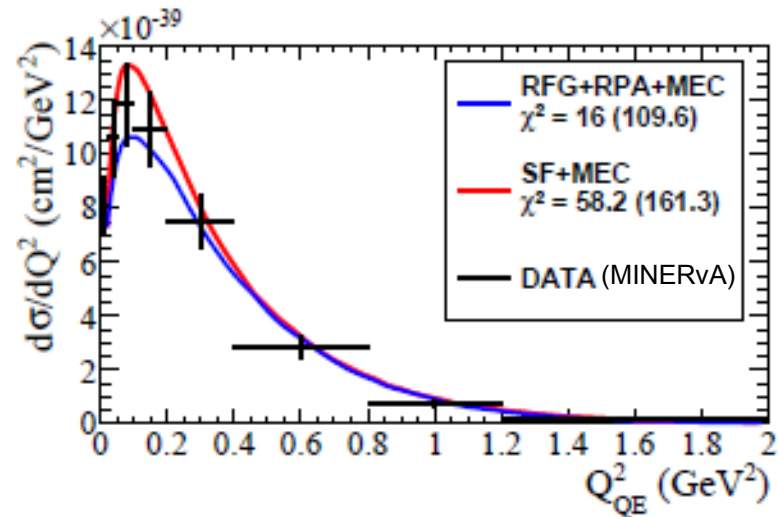


# Not just a cautionary tale any more!

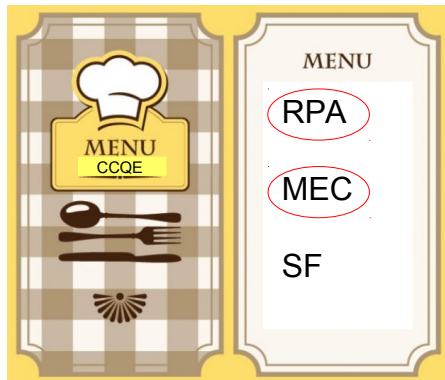
[C. Wilkinson, NuFACT 2014]



Neutrino



Antineutrino



There is work underway right now to use MINERvA data to constrain the models used in T2K's oscillation fits!

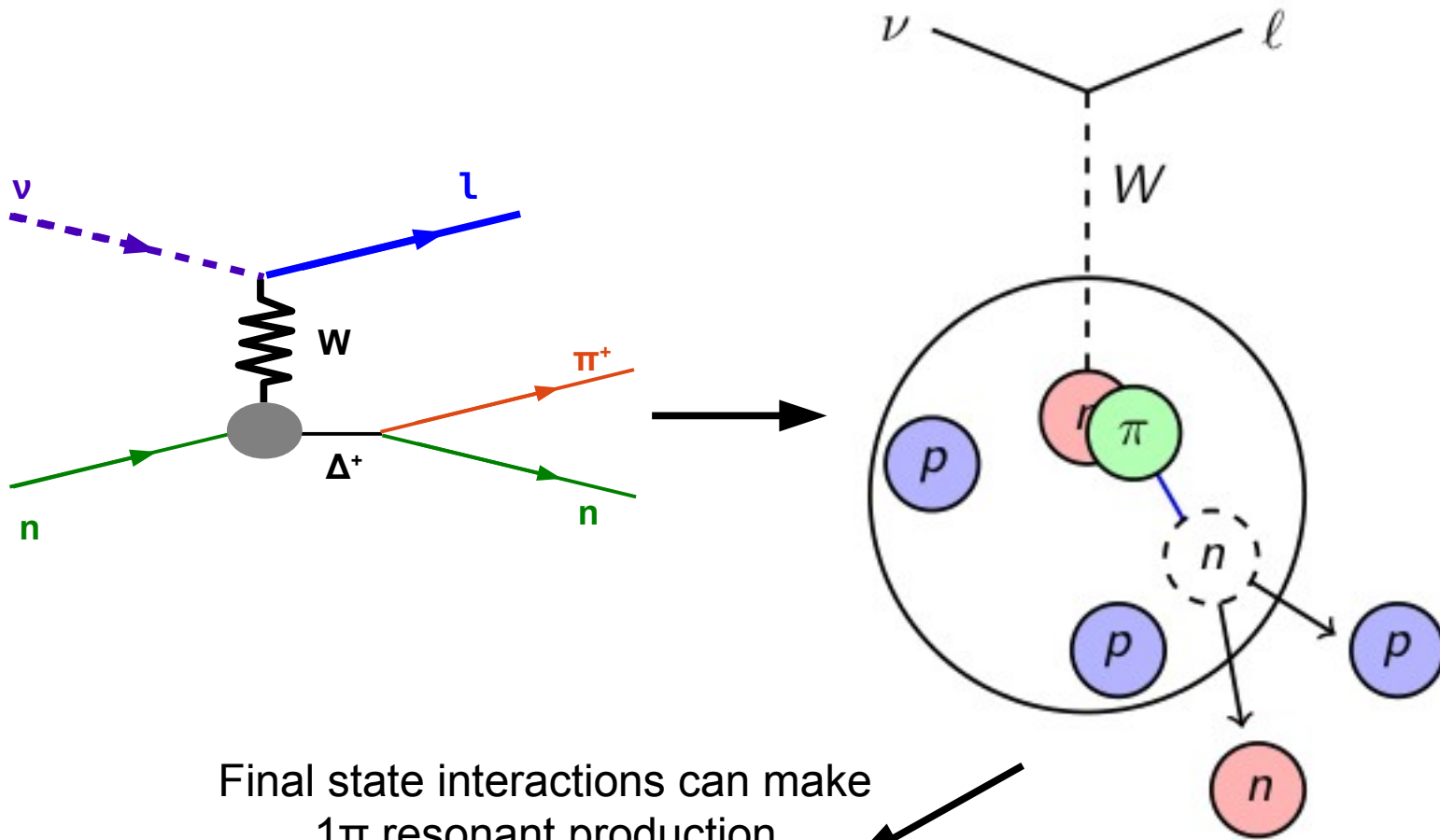
(See C. Wilkinson's talk in WG1 from Tuesday)

# CCQE: what's still coming

Other MINERvA CCQE results coming soon will further exercise the models...

- Doubly differential XS in muon variables ( $d^2\sigma/dp_z dp_t$ ) with Michel electron veto & exclusion of proton tracks from recoil (improves S/B)
- Electron neutrino CCQE (first ever!): see talk tomorrow by J.W.

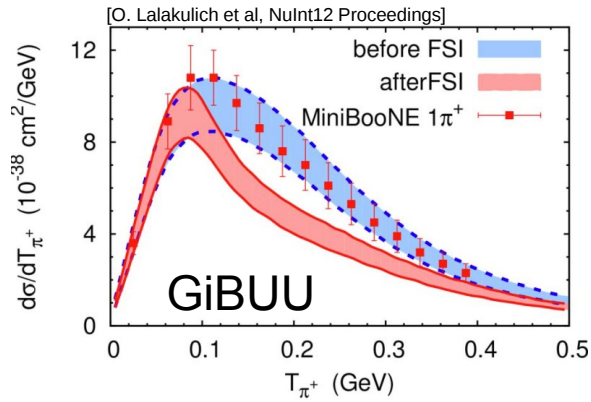
# Another energy estimator problem: FSI



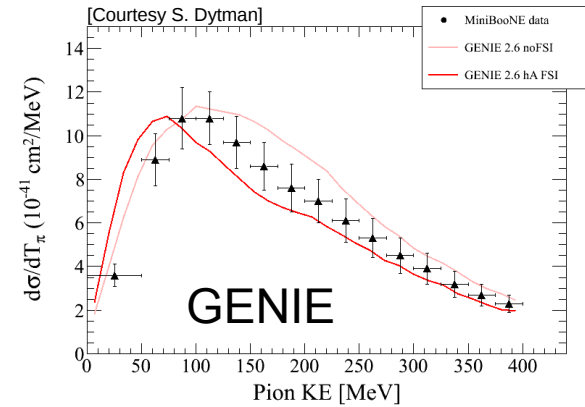
Final state interactions can make  
 $1\pi$  resonant production  
indistinguishable from CCQE...  
*but CCQE formula doesn't apply*

# Charged pion production

$$\nu_{\mu} \text{ CH} \rightarrow \mu^{-} \pi^{\pm} X$$

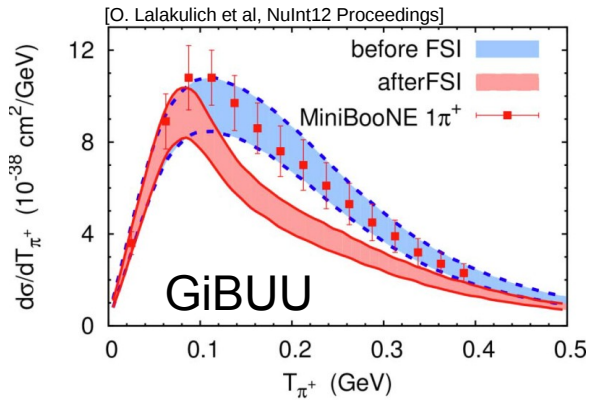


Choice of FSI model impacts shape and normalization of cross-section (data from MiniBooNE exp't)

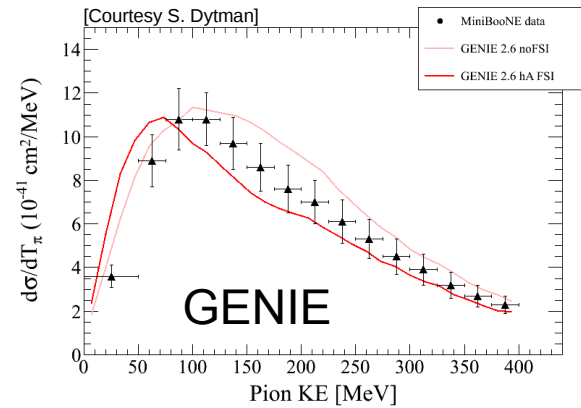


# Charged pion production

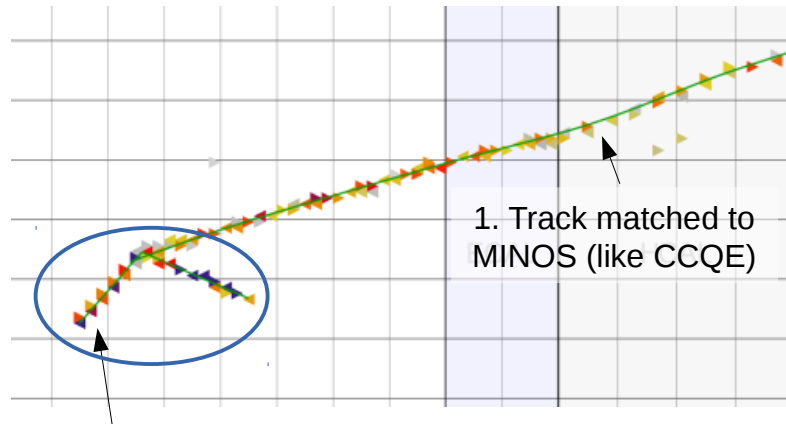
$$\nu_{\mu} \text{ CH} \rightarrow \mu^{-} \pi^{\pm} X$$



Choice of FSI model impacts shape and normalization of cross-section (data from MiniBooNE exp't)

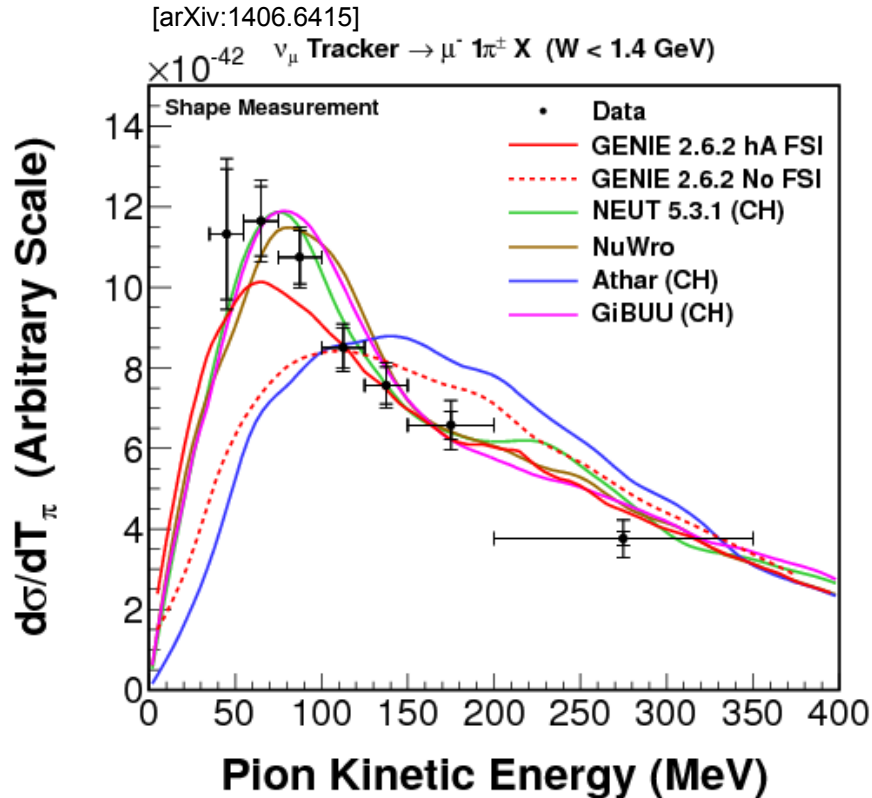


in MINERvA:



2. One or two hadron track candidates, at least one of which is consistent with a pion by  $dE/dx$  and Michel  $e^-$

# Charged pion production in MINERvA



**GENIE hA** (generator): isospin symmetry +  $A^{2/3}$  scaling extrapolation from  $\pi + \text{Fe}$  cross-section data

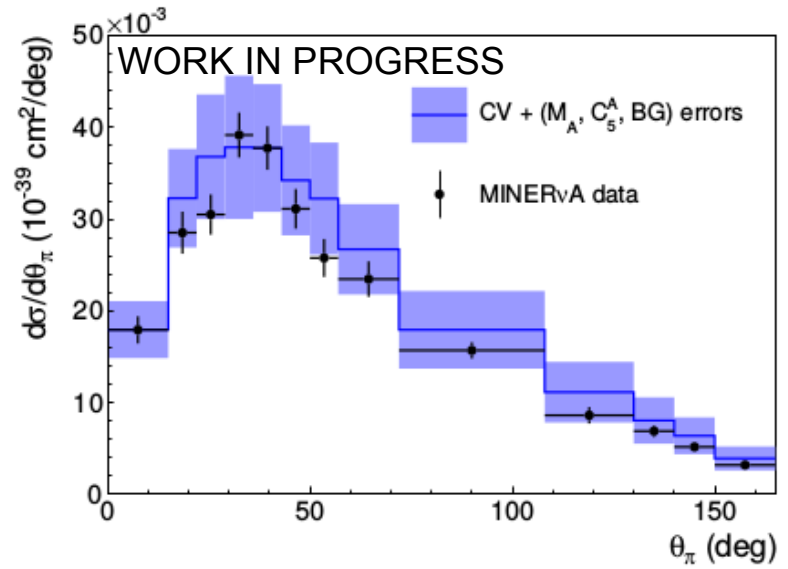
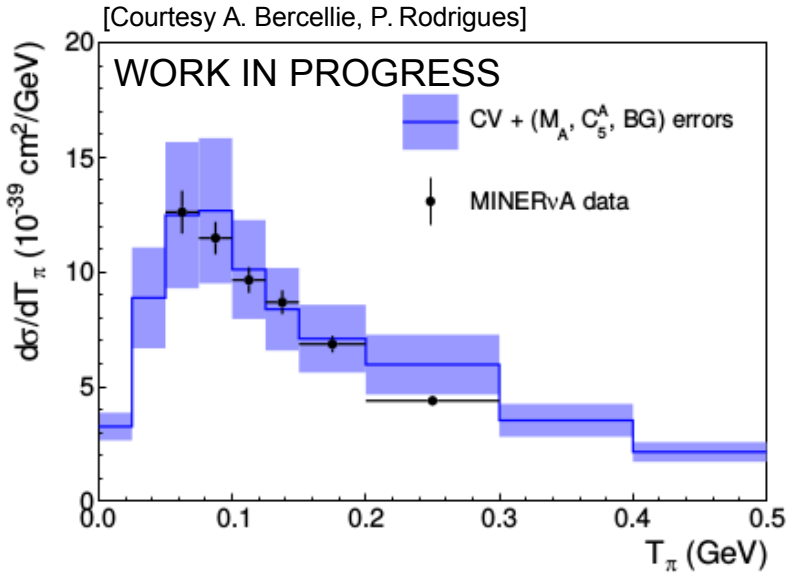
**Neut** (generator): stepping (semi-classical) cascade model tuned to  $\pi + \text{C}$  cross-section data

**NuWro** (generator): tuned similarly to Neut

**Athar** (theoretical calculation): theoretical model with *partial* FSI model (no pion re-scattering)

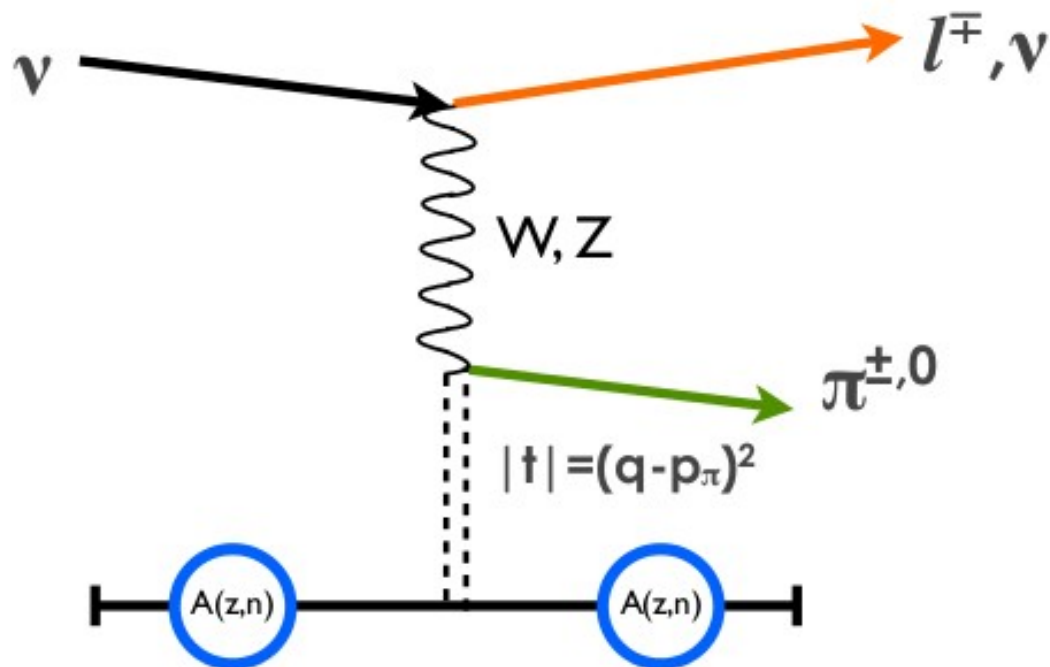
**Models with full FSI treatment are preferred by shape of MINERvA data**

# Using the result



T2K collaborators have been applying MINERvA's data to tune the parameters used in NEUT's single pion production model

# One last example: coherent $\pi$

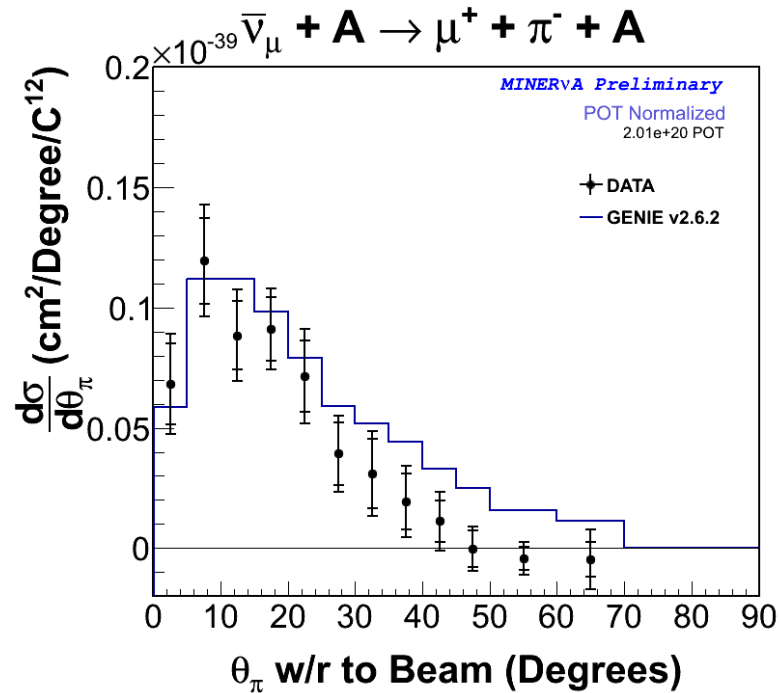
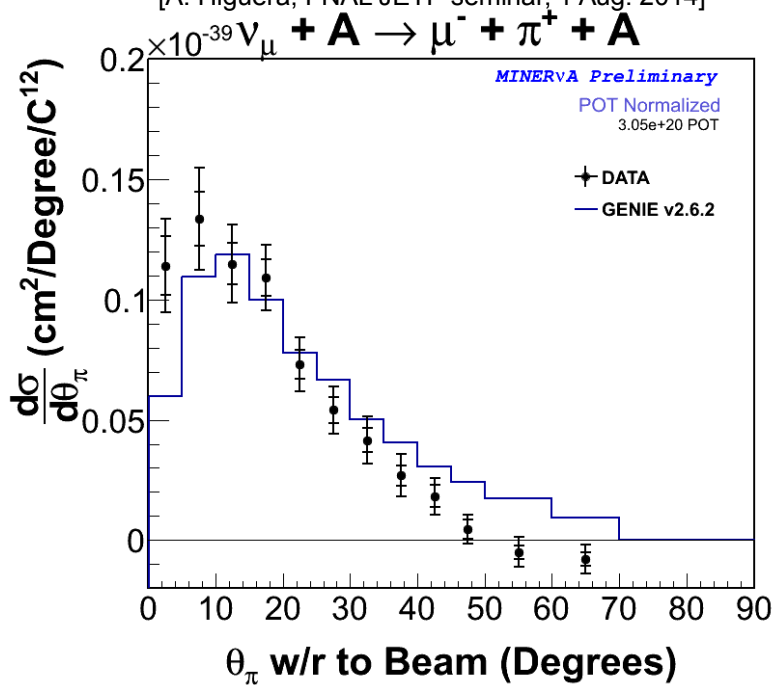


Shares problem with resonant production  
(can look like CCQE—particularly for NC coherent  $\pi^0$ , which can  
fake  $\nu_e$  CCQE—but CCQE energy formula doesn't apply)



# Coherent $\pi$

[A. Higuera, FNAL JETP seminar, 1 Aug. 2014]



MINERvA data indicates serious flaws in commonly-used model for coherent pion production (Rein-Sehgal).

See J. Morfín's talk tomorrow for many more details.

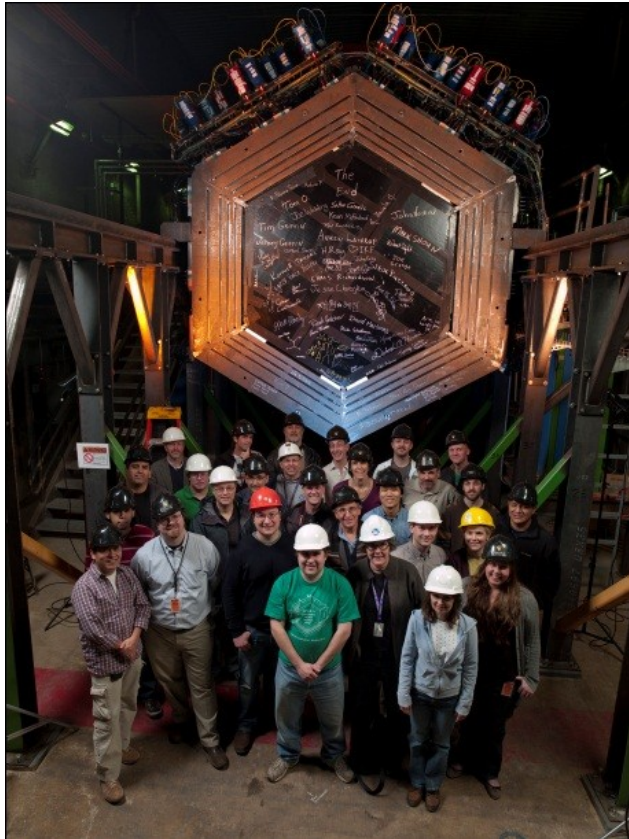
# Summary

- MINERvA's cross-section measurements are already being put to work improving models needed for  $E_\nu$  reconstruction
  - Comparison to CCQE models underscores the importance of understanding the role the initial state plays
  - Comparison to pion production models suggests that current generators' FSI model is reasonable and necessary to match the data
- Recent and forthcoming results promise to continue this tradition
  - Other CCQE:  $d^2\sigma/dp_z dp_t$  for  $\nu_\mu$ ;  $d\sigma/dQ^2$ ,  $d\sigma/d\theta$ ,  $d\sigma/dE_e$  for  $\nu_e$
  - Coherent  $\pi^\pm$

University of California at Irvine  
Centro Brasileiro de Pesquisas Físicas  
University of Chicago  
Fermilab  
University of Florida  
Université de Genève  
Universidad de Guanajuato  
Hampton University  
Inst. Nucl. Reas. Moscow  
Massachusetts College of Liberal Arts  
University of Minnesota at Duluth



Universidad Nacional de Ingeniería  
Northwestern University  
Otterbein University  
Pontificia Universidad Católica del Perú  
University of Pittsburgh  
University of Rochester  
Rutgers, The State University of New Jersey  
Universidad Técnica Federico Santa María  
Tufts University  
William and Mary

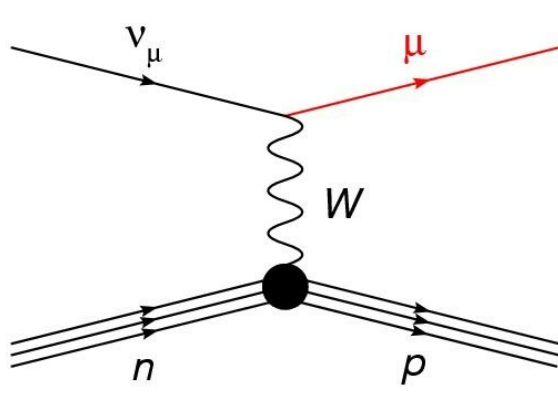


Thank you  
from MINERvA!

Backup slides follow



# Models for $\nu_\mu$ CCQE



CCQE = “standard candle?”  
(simplest CC process)

Basic formalism for *free nucleon*  
cross-section well known...

(Llewellyn Smith, 1972)

$$\frac{d\sigma}{dQ^2} = \frac{M^2 G_F^2 \cos^2 \theta_C}{8\pi E_\nu^2} \times \left[ A(Q^2) \mp \frac{(s-u)B(Q^2)}{M^2} + \frac{C(Q^2)(s-u)^2}{M^2} \right]$$

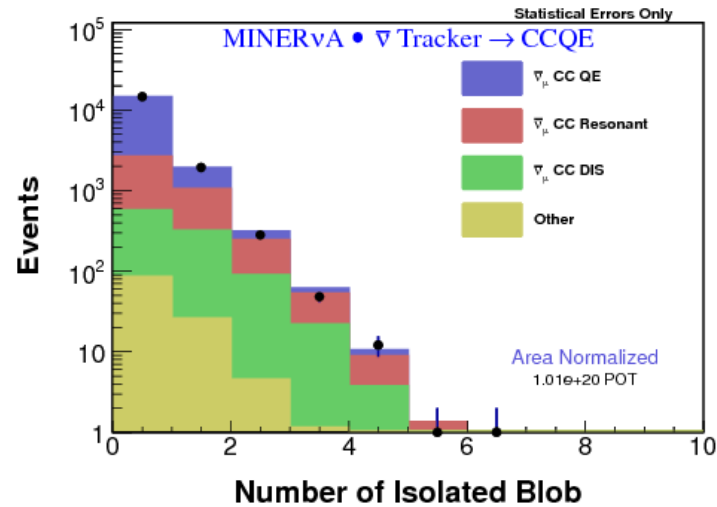
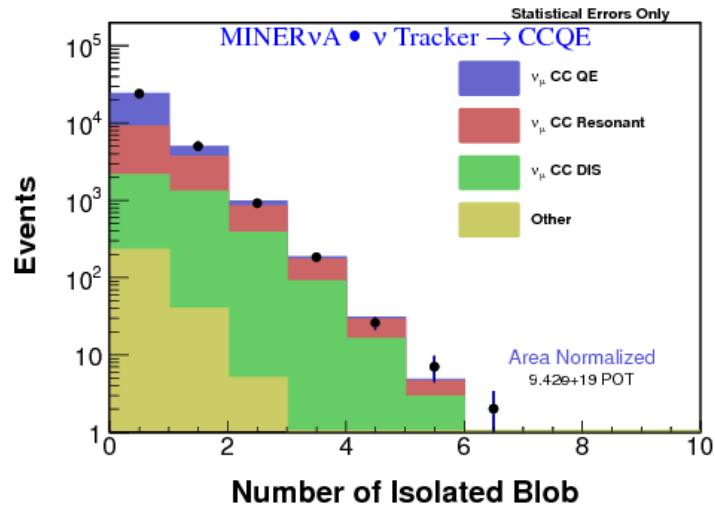
- Parameterized in terms of *nuclear form factors*
- One free parameter not constrained by electron scattering data: “axial mass”  $m_A$ 
  - Fits to  $\nu$ -D<sub>2</sub> and  $\nu$ -C scattering data:  $m_A = 0.99$  (ANL, BNL, NOMAD)
  - MiniBooNE fit to  $\nu$ -CH<sub>2</sub> scattering data:  $m_A = 1.35$

... but that *nucleus* ...

- Relativistic Fermi Gas (RFG): “vanilla” quasi-free nucleon model
- Spectral Function (SF): nucleon momentum spectrum including NN correlation effect (but  $\nu$  still interacts with single nucleon) [Nucl. Phys. A579, 493 (1994)]
- Random Phase Approximation (RPA): models long-range correlations between nucleons (nuclear polarization) by altering electroweak coupling [Phys. Rev. C 70, 055503 (2004)]
- Meson Exchange Currents (MEC): models multi-nucleon ejection [Phys. Rev. C 49, 2650 (1994)]
- Transverse Enhancement Model (TEM): empirical model based on modification of cross-section observed in e+A scattering [Eur. Phys. J. C 71, 1726 (2011)]

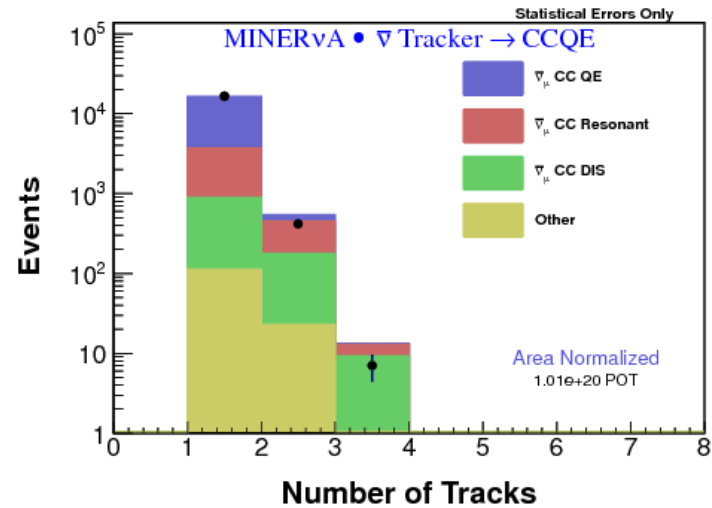
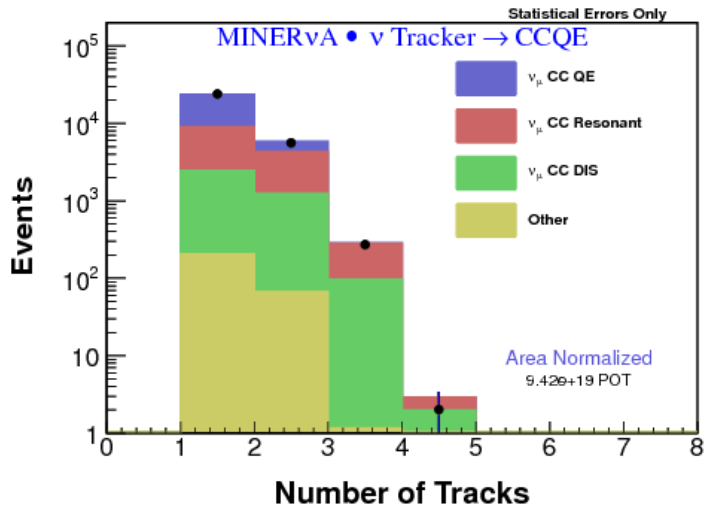
Lots of  
models to  
mix and  
match!  
(Where do they  
overlap?...)

# CCQE: isolated showers cut



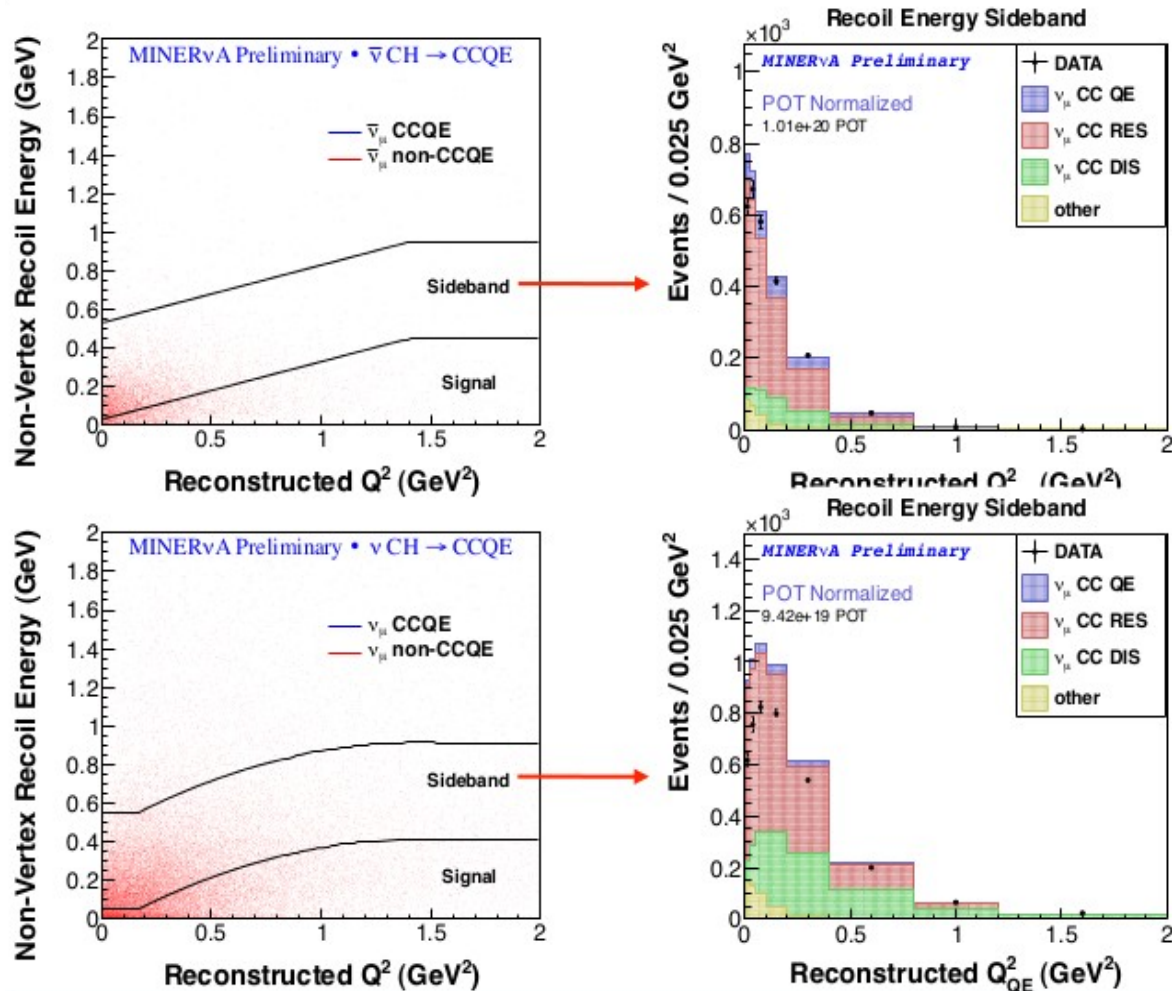
- $\leq 2$  for neutrino,  $\leq 1$  for nubar

# CCQE: number of tracks cut



- No more than 1 for nubar, no cut for neutrino

# CCQE: sidebands

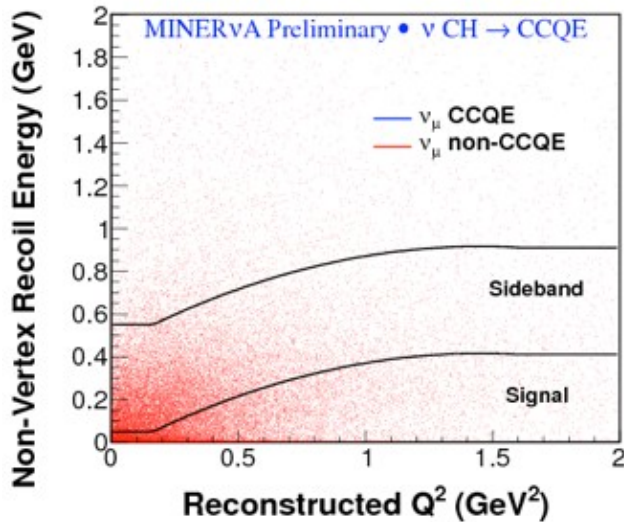


$\bar{\nu}_\mu$

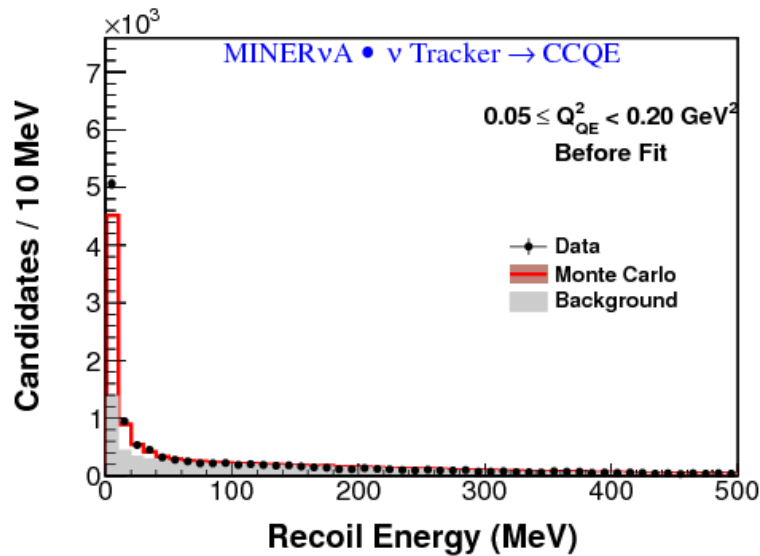
$\nu_\mu$



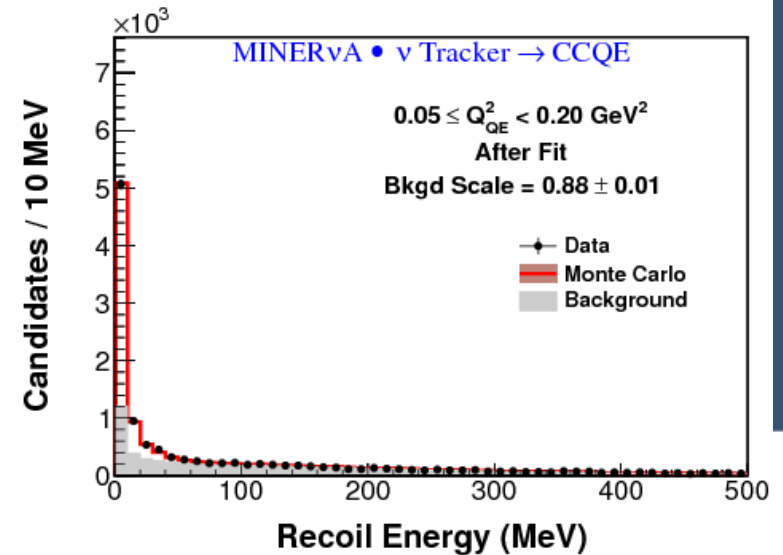
# $\nu_{\mu}$ CCQE: sideband constraint



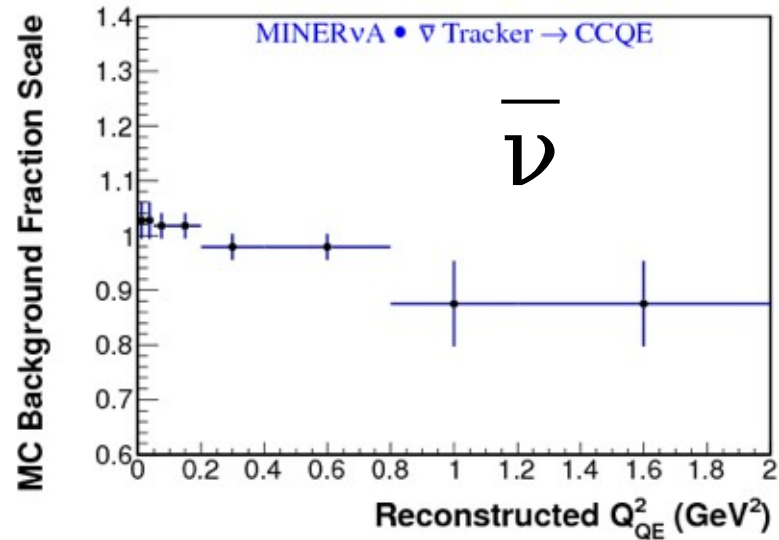
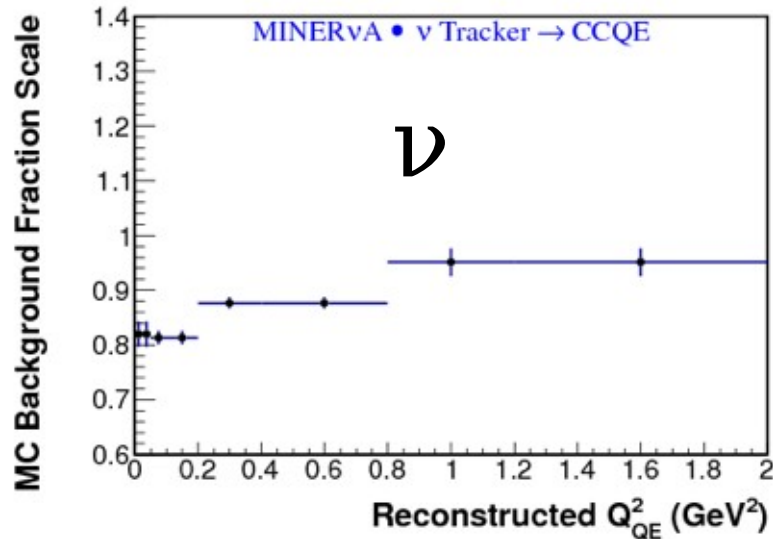
We use a sideband in the non-vertex recoil energy to constrain the background prediction in bins of  $Q^2$ .



Sideband  
fit



# $\nu_\mu$ CCQE: background scales

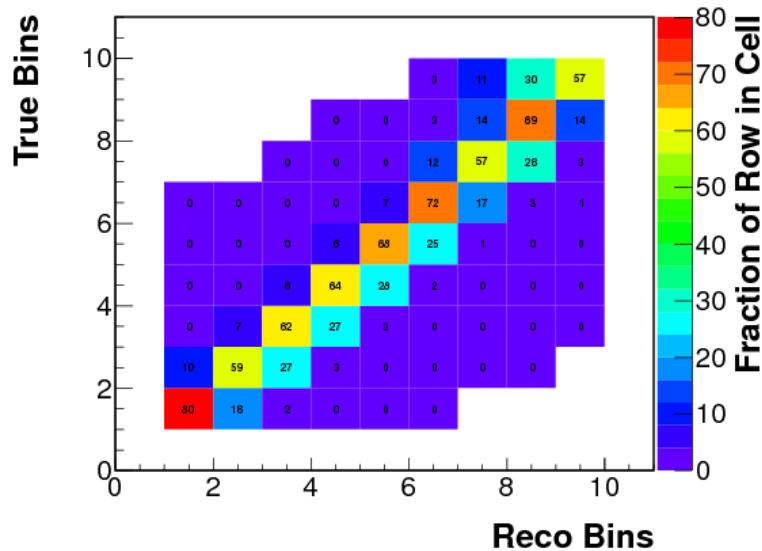


The corrections to background model  
are not insignificant...

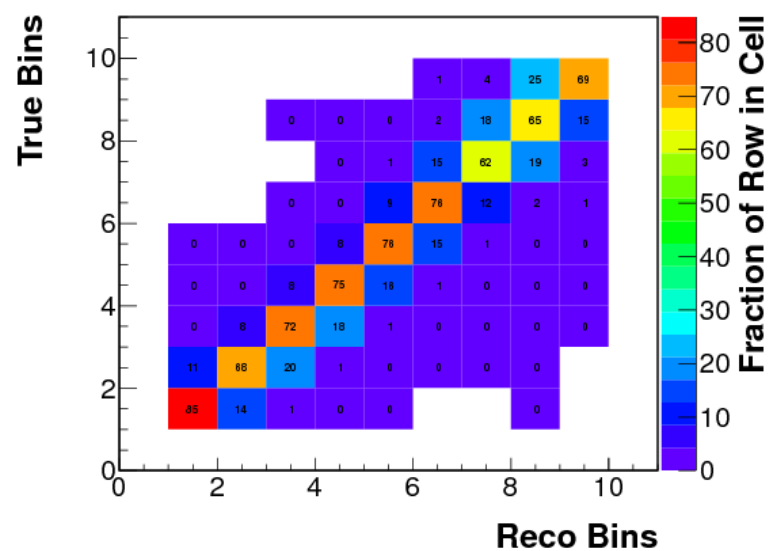
We then subtract the backgrounds, unfold to muon kinematic  
variables, efficiency correct, and then...

# CCQE unfolding matrices

neutrino

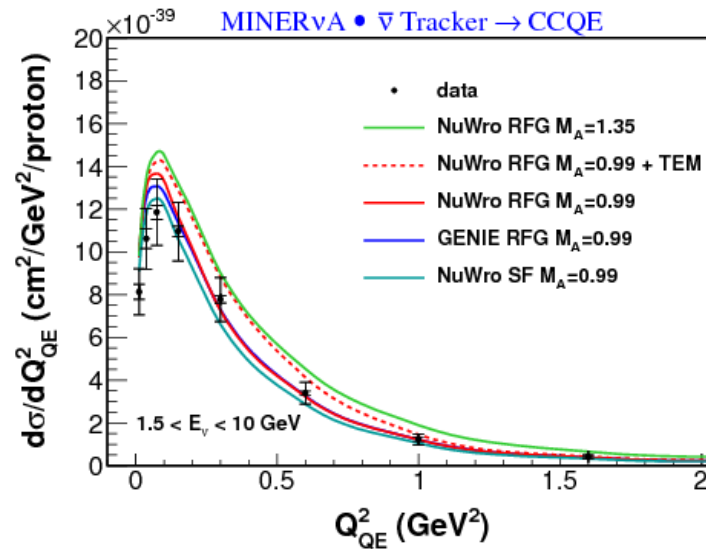
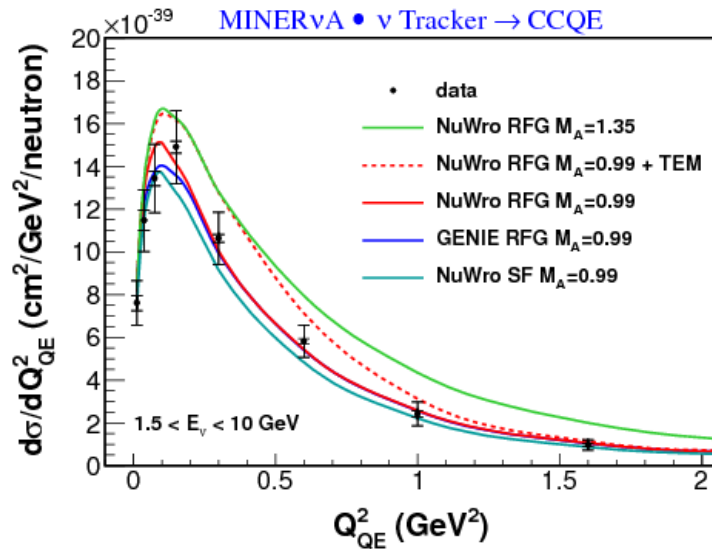


antineutrino



- Bins of  $Q^2_{QE}$
- Unfolded using Bayesian method with 4 iterations

# CCQE: absolute cross section



$M_A = 1.35$  —

TEM - - -

GENIE —

SF —

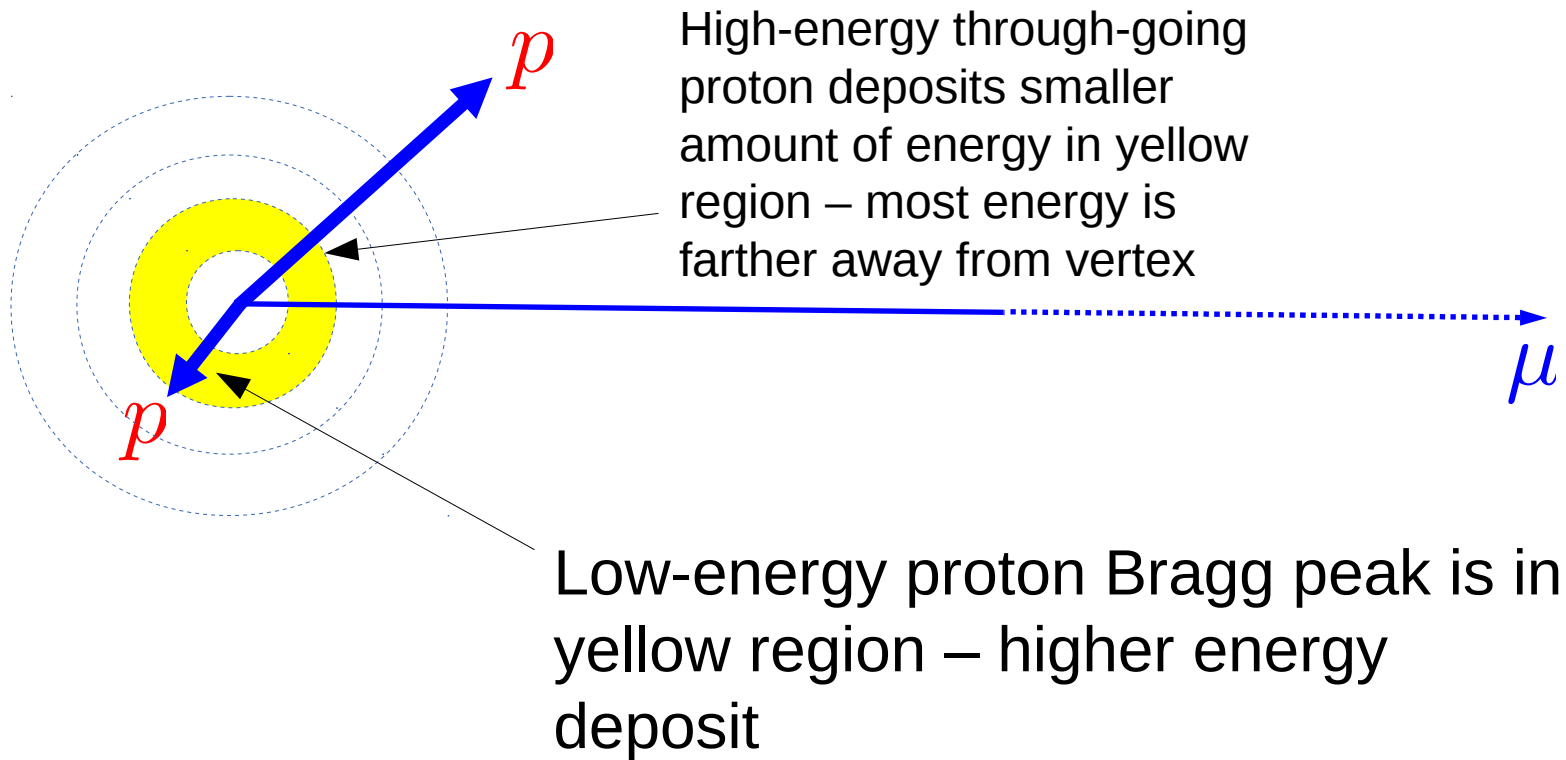
best fit to MiniBooNE data

empirical model based on electron scattering data

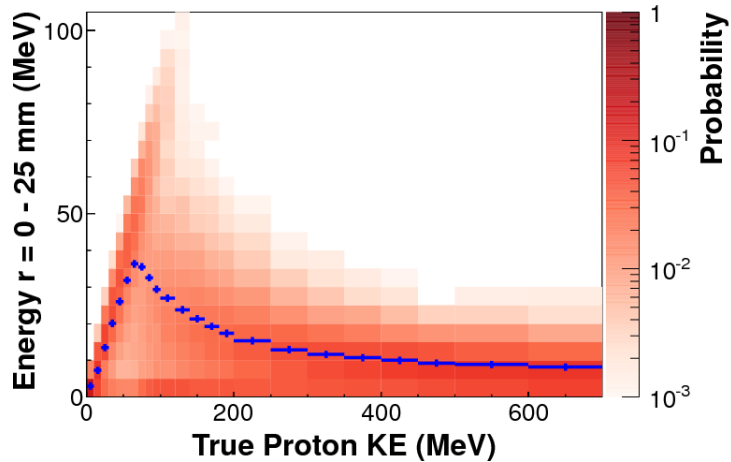
independent nucleons in mean field

more realistic nucleon momentum-energy relation

# Vertex energy “annuli”

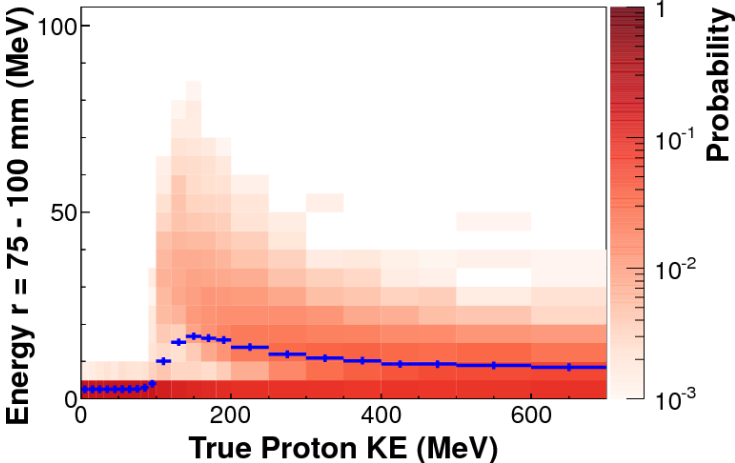


# Vertex energy due to 1 proton



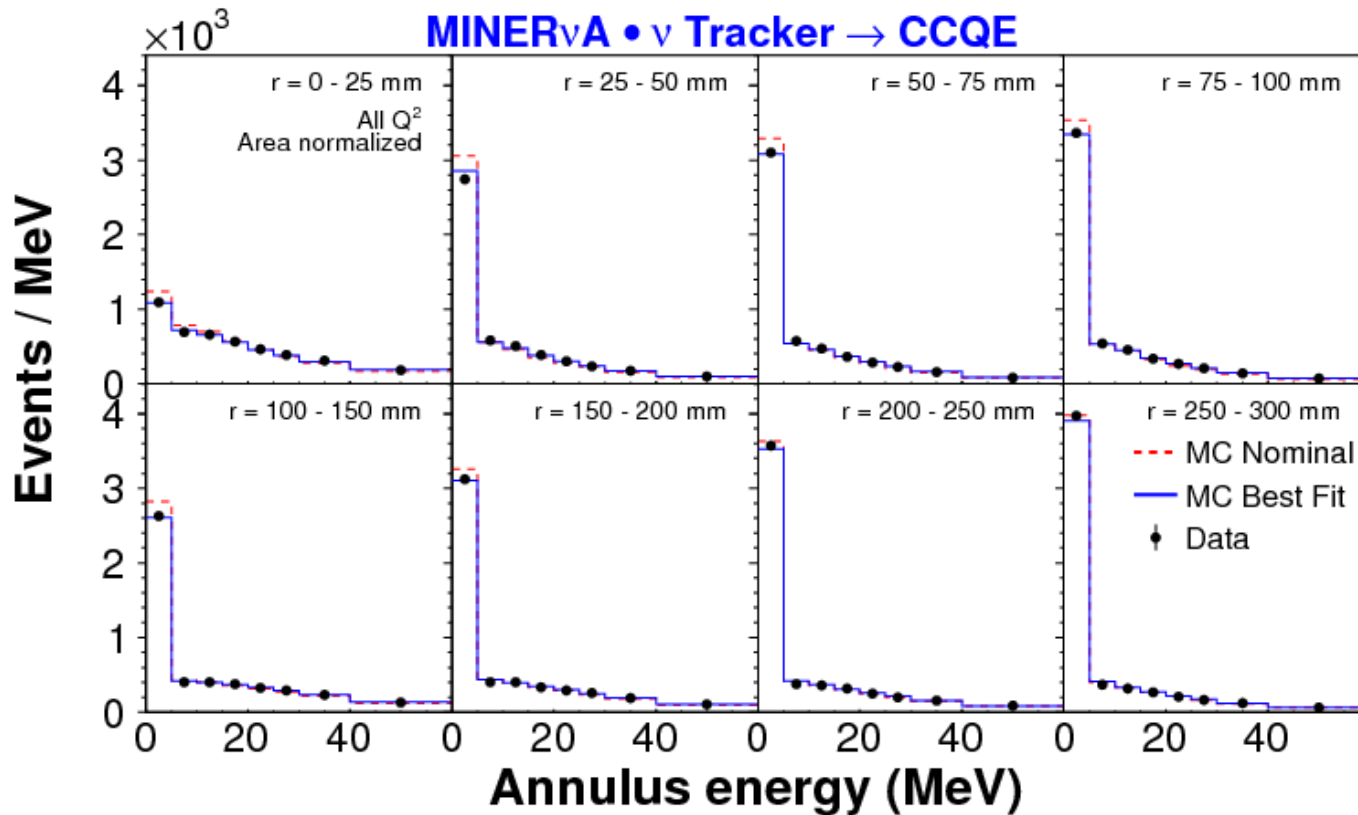
Simulated CC events with exactly 1 proton, no  $\pi/\gamma$

For proton of given KE, column represents probability distribution for energy deposit in given region

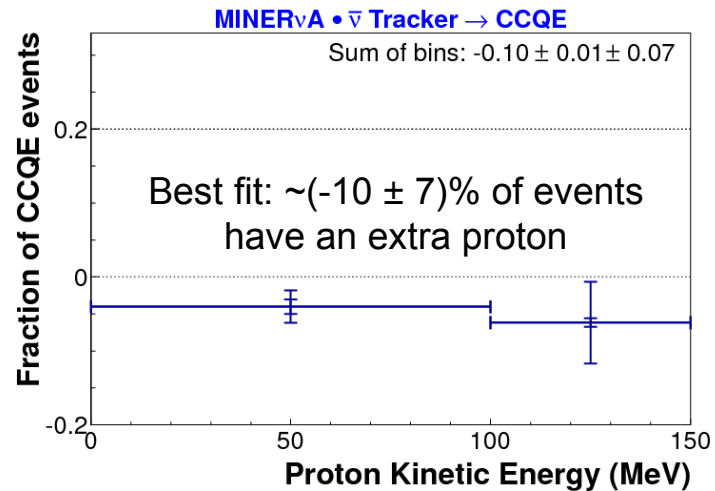
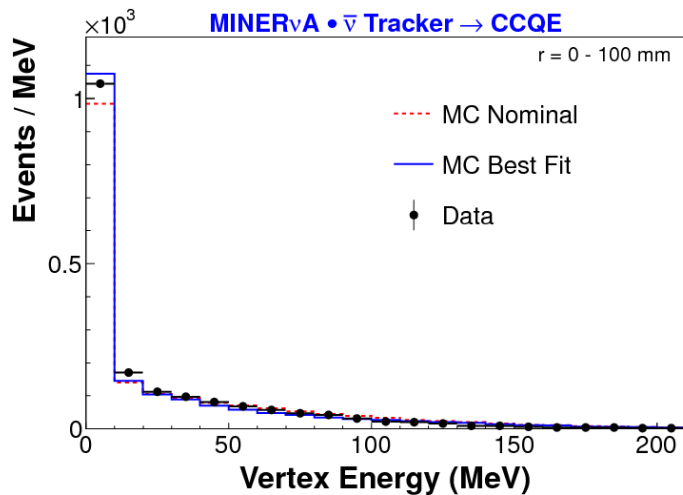


Fit by adding energy to some fraction of events based on these distributions

# Vertex energy annulus fits



# Vertex activity ( $\bar{\nu}$ incident)



Fit suggests  $\bar{\nu}$  events do not require any extra protons:  
**consistent with (n,p) correlated pair model  
(CCQE converts  $np \rightarrow nn$ )**

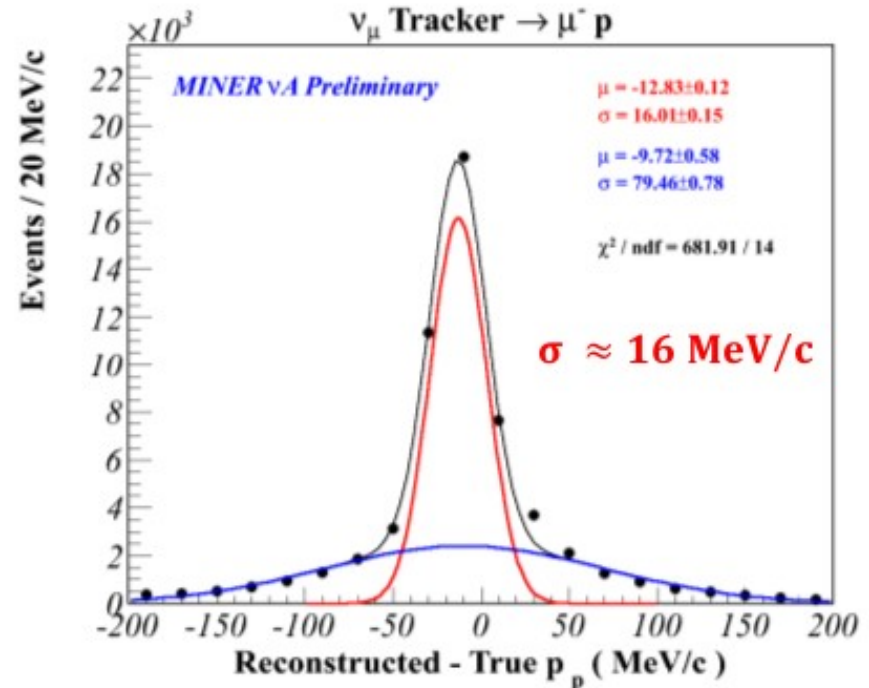


# Q<sup>2</sup> from proton kinematics

- Reconstruct Q<sup>2</sup> using kinetic energy of the leading proton.
- Use the QE hypothesis.
- Assume scattering from a free nucleon at rest.

$$Q_{QE,p}^2 = (M')^2 - M_p^2 + 2M'(T_p + M_p - M'),$$

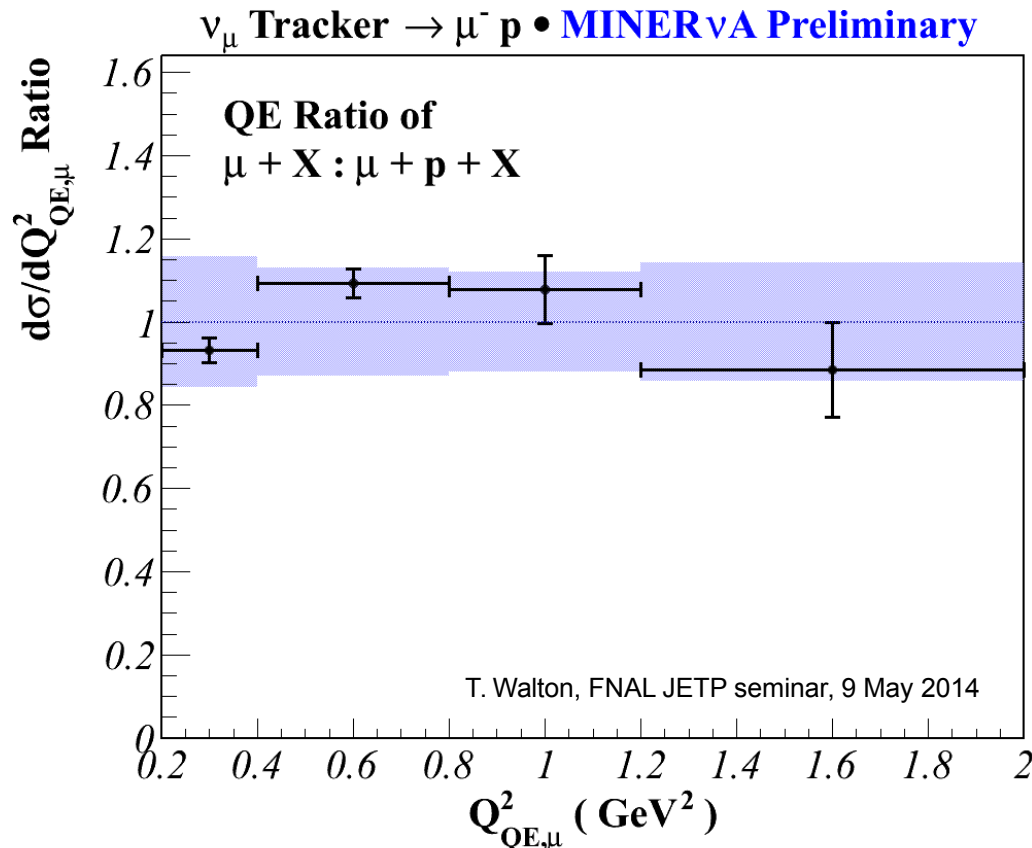
- $M' = M_n - E_{bind}$
- $E_{bind}$  is the binding energy
- $T_p$  is the proton kinetic energy
- $M_n$  is the mass of the neutron
- $M_p$  is the mass of the proton



Compare Q<sup>2</sup> from muon kinematics:

$$Q_{QE}^2 = 2E_\nu^{QE} (E_\mu - p_\mu \cos \theta_\mu) - m_\mu^2$$

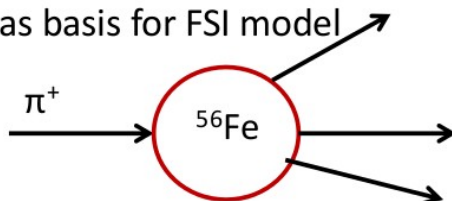
# CCQE methods comparison



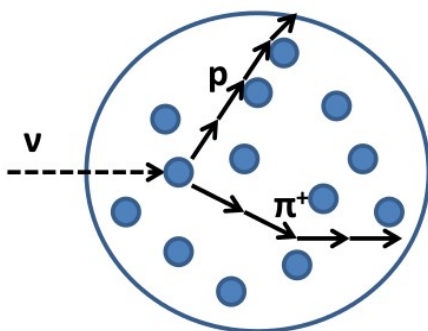
Results of “ $\mu$ +little recoil” and “ $\mu$ +p” techniques, when examined vs. muon variables, are consistent within systematics of “ $\mu$ +p” (blue band)

# Pion models & FSI

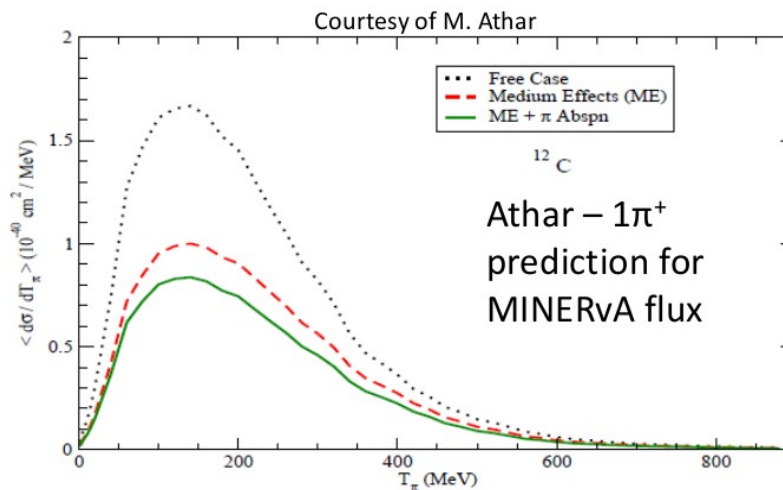
GENIE: Use  $p, \pi$  scattering on Fe data as basis for FSI model



NuWro, Neut: Step interaction products through nucleus and use nucleon cross sections



Athar: Use an Eikonal approximation. Reduces observed pions, but does not significantly change  $T_\pi$  shape

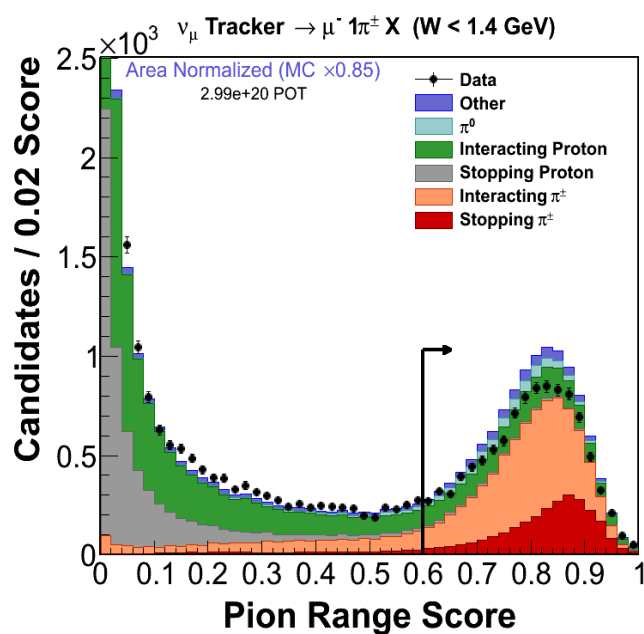
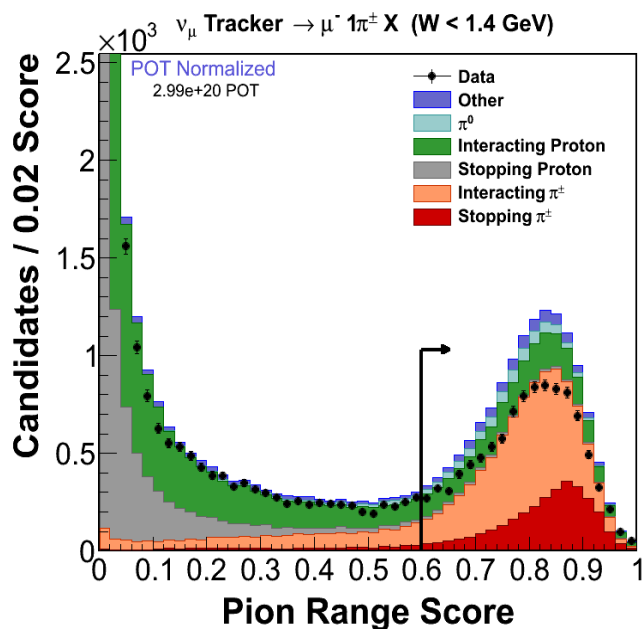


# Pion ID

## Select a pion (Particle ID):

- Use energy loss ( $dE/dx$ ) profile of each hadron track to separate protons and pions

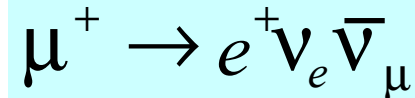
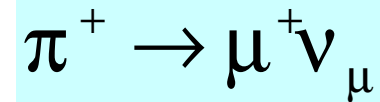
- Find the best fit momentum for a pion hypothesis: this is the ***reconstructed momentum***



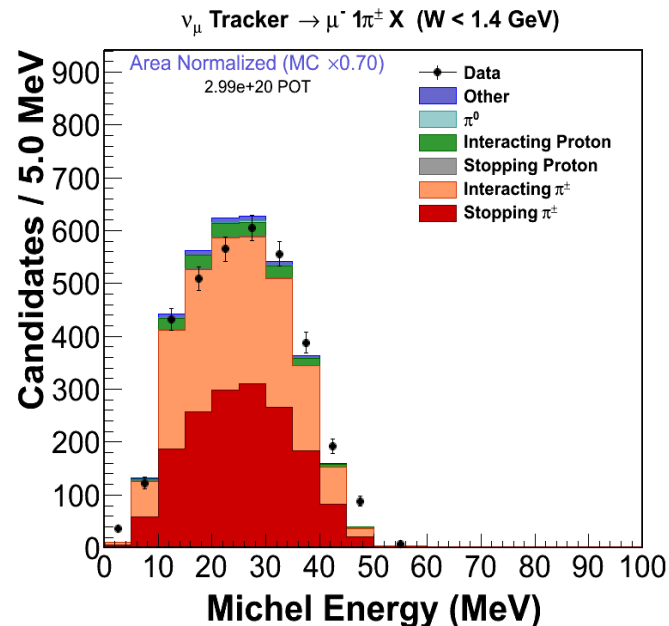
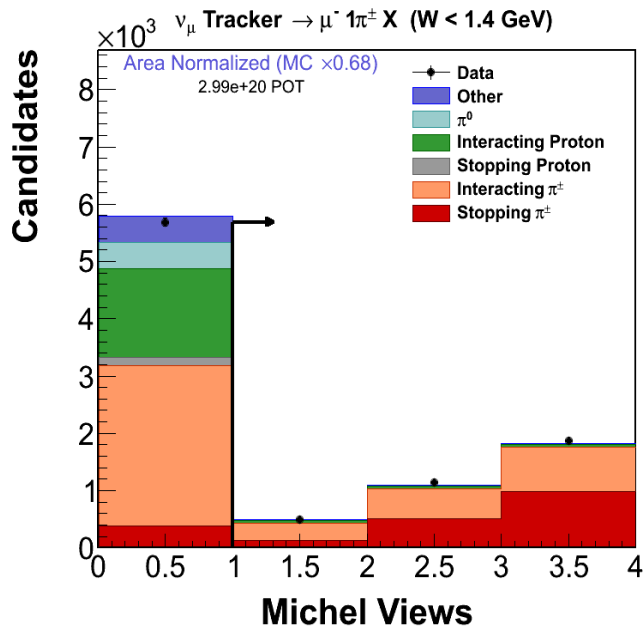
# Pion ID

**Select a pion (with good energy reconstruction):**

Select pions that stop and decay in the detector by looking for a Michel electron at the end of the track



## Shape Comparisons

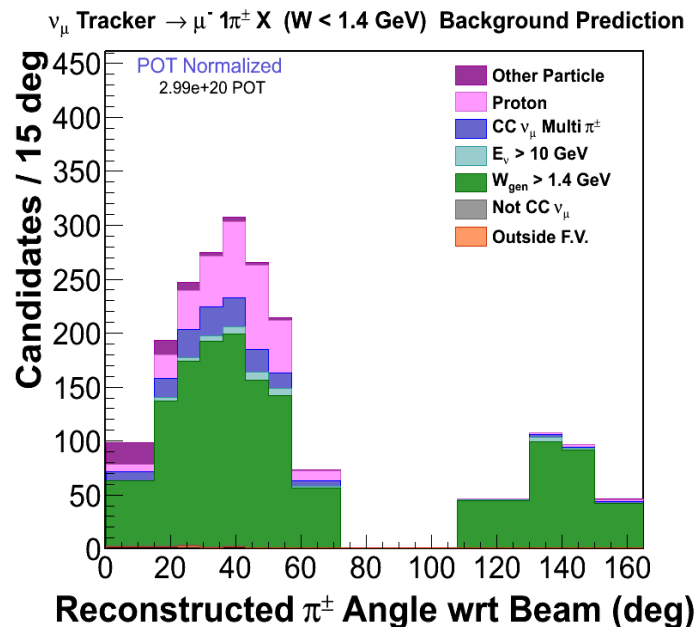
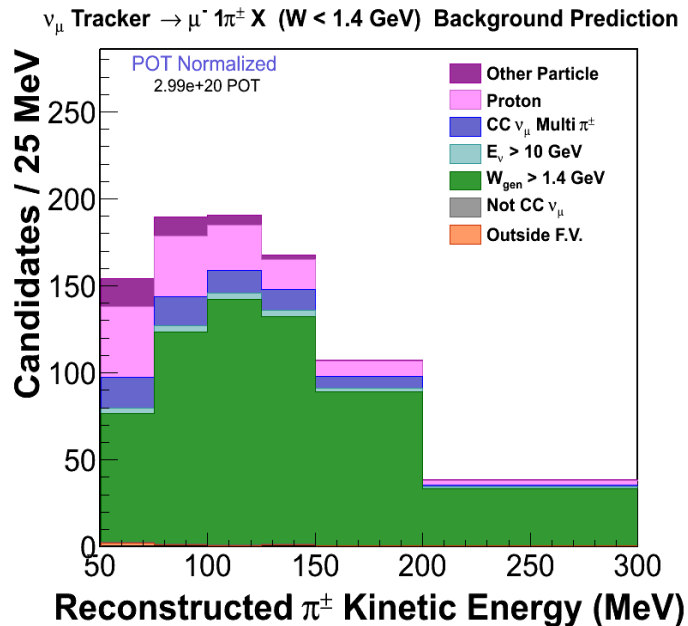


# Pion Background Summaries

**Largest background:**  $W > 1.4$  GeV ~17% of sample

**PID backgrounds:** Protons and other particles mis-ID as pion ~ 4% of sample

**All other backgrounds combined:** ~2% of sample

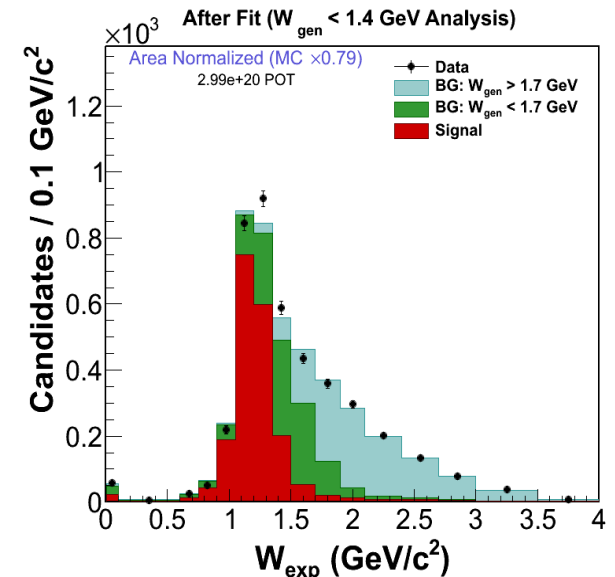
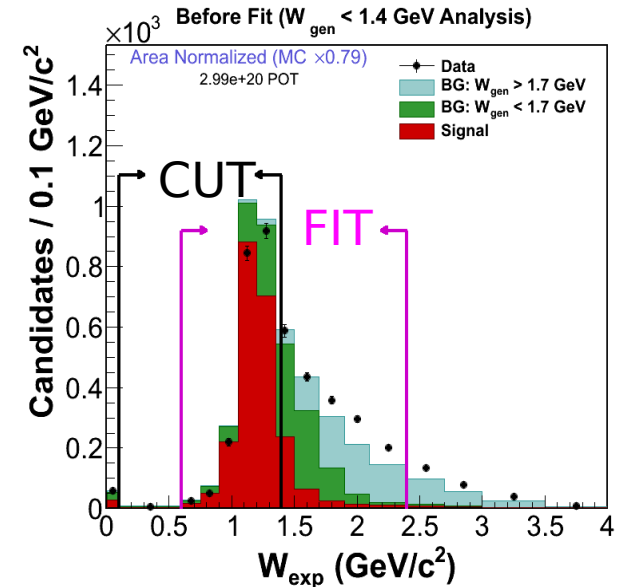


# Pion Background Subtraction

- Only significant background is feed down from large  $W$ . Concentrate on constraining this background with data

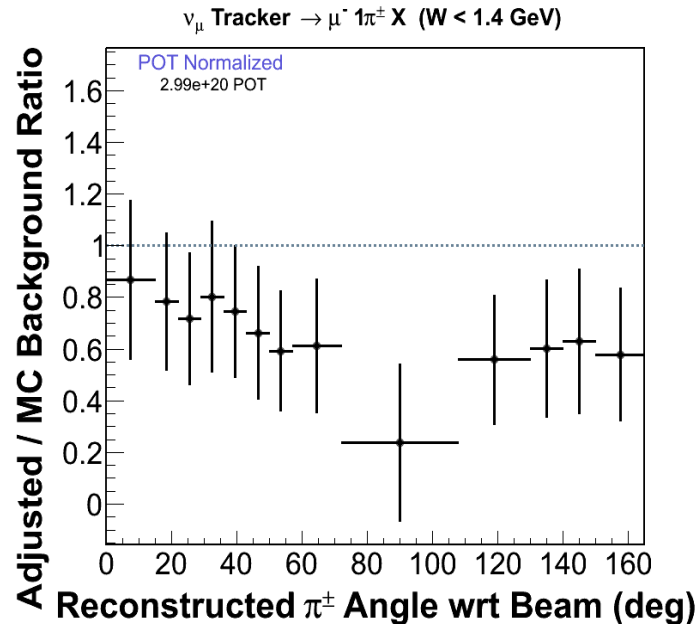
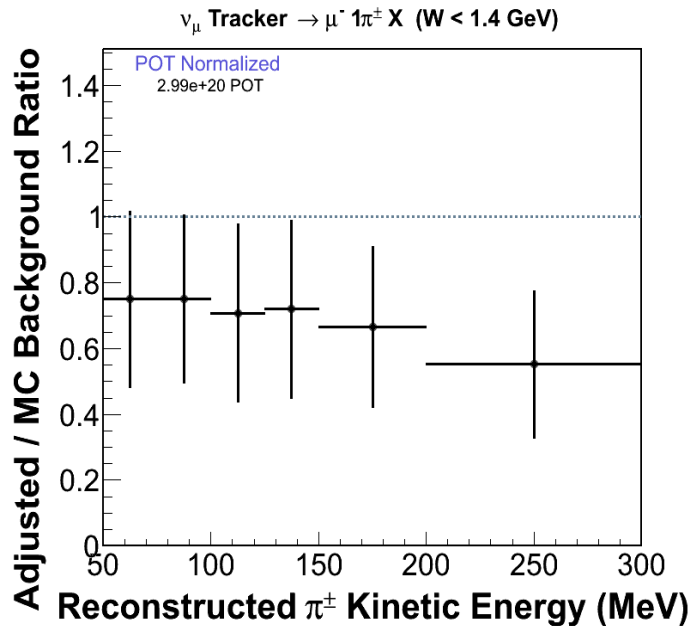
## Procedure:

- Construct the  $W_{\text{exp}}$  distribution, applying all cuts except the  $W$  cut
- Use the MC to create signal and background shape templates
- Fit the data for the relative normalizations of the templates



# Pion Background Scales

Ratio of adjusted to simulated background



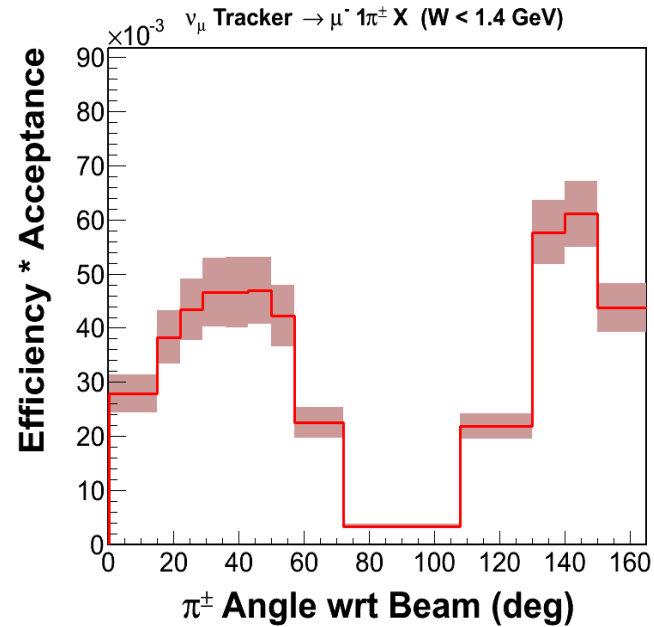
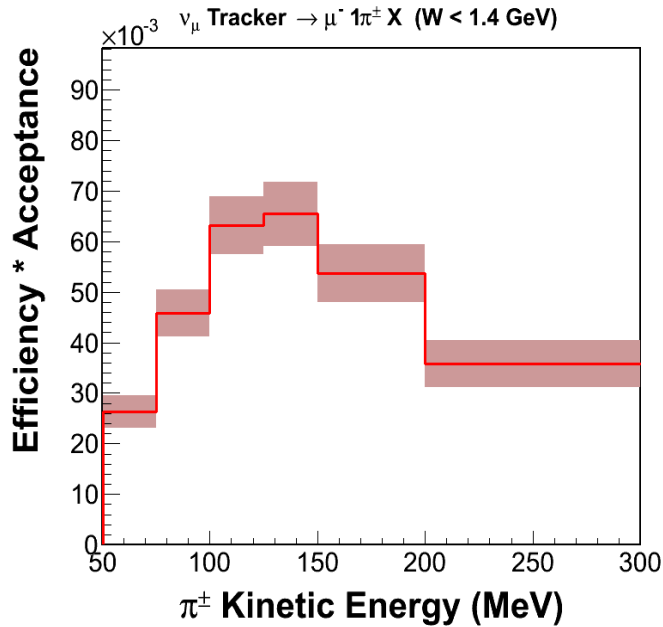
Dominant uncertainty on adjusted background is detector energy response





# Pion Efficiency Correction

Correct to the full range of muon energies and angles



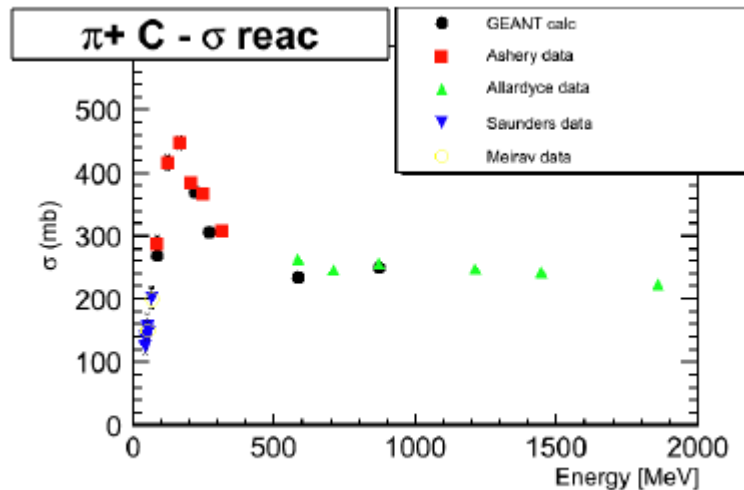
# Pion Systematic Errors (1)

- Analysis uses GENIE 2.6.2 to simulate neutrino interactions in nuclei
- Cross section model uncertainties enter the analysis through the efficiency correction
  - ~10%, but negligible shape errors
- FSI uncertainties enter through background subtraction (change W)
  - ~3-4%, and < 2% shape errors

FSI model parameter	uncertainty
pion/nucleon mean path	$\pm 20\%$
pion/nucleon charge exchange	$\pm 50\%$
pion absorption	$\pm 30\%$
pion/nucleon inelastic cross-section	$\pm 40\%$
elastic cross sections	$\pm 10-30\%$

# Pion Systematic Errors (2)

- Use Geant4 to simulate particle propagation in the detector
- Uncertainty on **inelastic pion** cross sections affects unfolding and efficiency correction. **Inelastic proton** cross section affects background estimate.
- Compare Geant4 predictions to external data to determine uncertainty on inelastic cross sections  $\sim 10\%$ 
  - Leads to up to 7% errors in analysis (greatest at large pion KE)



# Pion systematic errors (3)

