

Status of the New Muonium HFS Experiment at J-PARC/MUSE

P. Strasser (KEK)

on behalf of the MuSEUM Collaboration

A photograph of a museum gallery. The walls are covered with numerous framed paintings of various sizes. A large, ornate chandelier hangs from the ceiling. In the foreground, a man and a woman are looking at a painting. The lighting is warm and focused on the art.

New Collaboration Name

MUSEUM

**Muon Spectroscopy Experiment
Using Microwave**

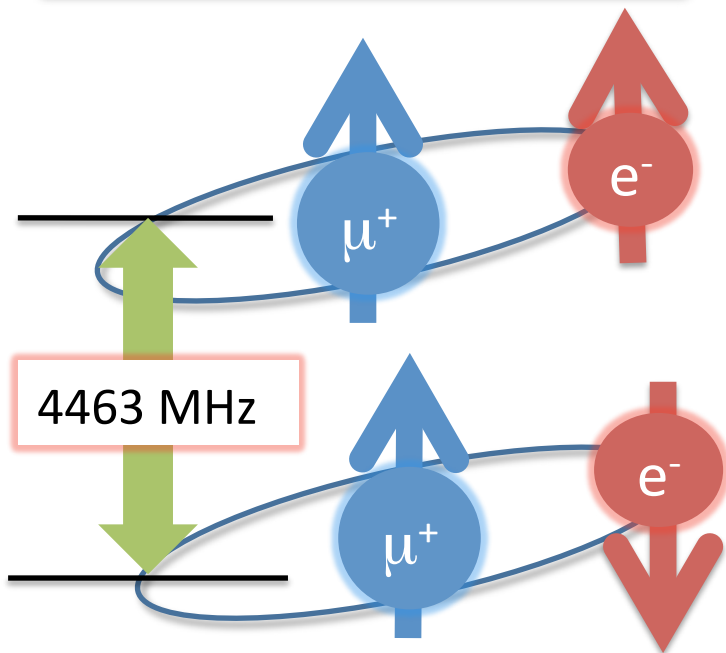
Muonium ground state

$$\mathcal{H} = h\Delta\nu \mathbf{I}_\mu \cdot \mathbf{J} - \mu_B^\mu g'_\mu \mathbf{I}_\mu \cdot \mathbf{H} + \mu_B^e g_J \mathbf{J} \cdot \mathbf{H}$$

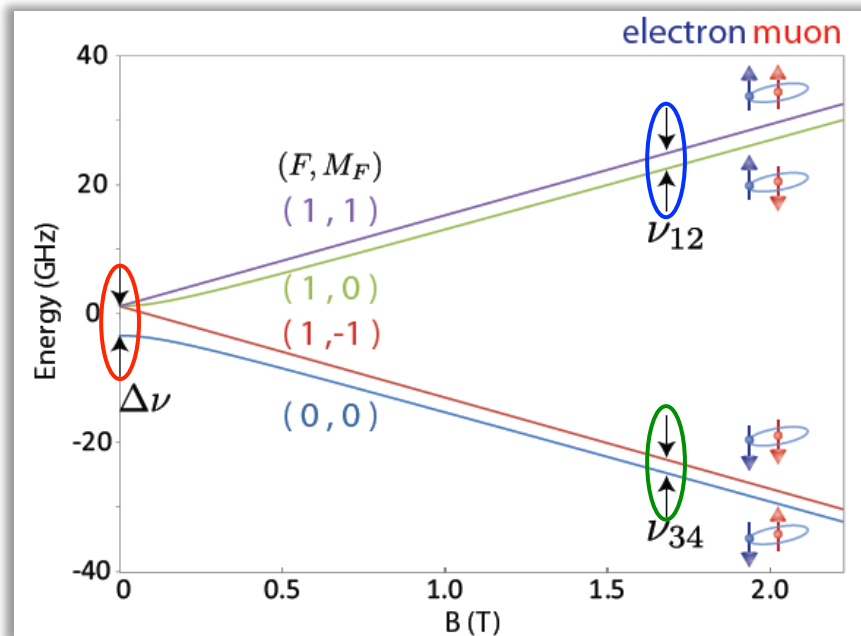
$\Delta\nu_{\text{HFS}}$: Mu Hyperfine Structure

Zeeman Splitting

Breit-Rabi diagram



Pure lepton
= point particle



$$\nu_{12} + \nu_{34} = \Delta\nu_{\text{HFS}}$$

$$\nu_{12} - \nu_{34} \propto \mu_\mu / \mu_p \propto m_\mu / m_p$$

Purpose of MuSEUM

- Measure two RF resonances (ν_{12} and ν_{34}) in 1.7 T magnetic field.
- Muonium ground state HFS
 - Precise test of bound-state QED
 - Current uncertainty: 12 ppb
 - Test of CPT and Lorentz Invariance
- Muon magnetic moment relative to that of proton
 - Basic property of muon
 - Current uncertainty: 120 ppb
 - Basic input parameter for muon g-2 experiment

We aim to improve the uncertainties of both quantities by a factor of 10, taking advantage of the high intensity beam at J-PARC/MUSE.

Recent Summary of experimental and theoretical data (by D. Nomura)

D. Nomura, Nucl. Phys. B 867 (2013) 236-243

Exp. $\nu_{\text{HFS}}(\text{exp.})$ 4463.302 765 (53) MHz [12 ppb]

The. $\nu_{\text{HFS}}(\text{theory})$ 4463.302 891 (272) MHz [63 ppb]

$\nu_{\text{HFS}}(\text{QED})$ 4463.302 720 (253)(98)(3)
(m_{μ}/m_e)(QED)(α)

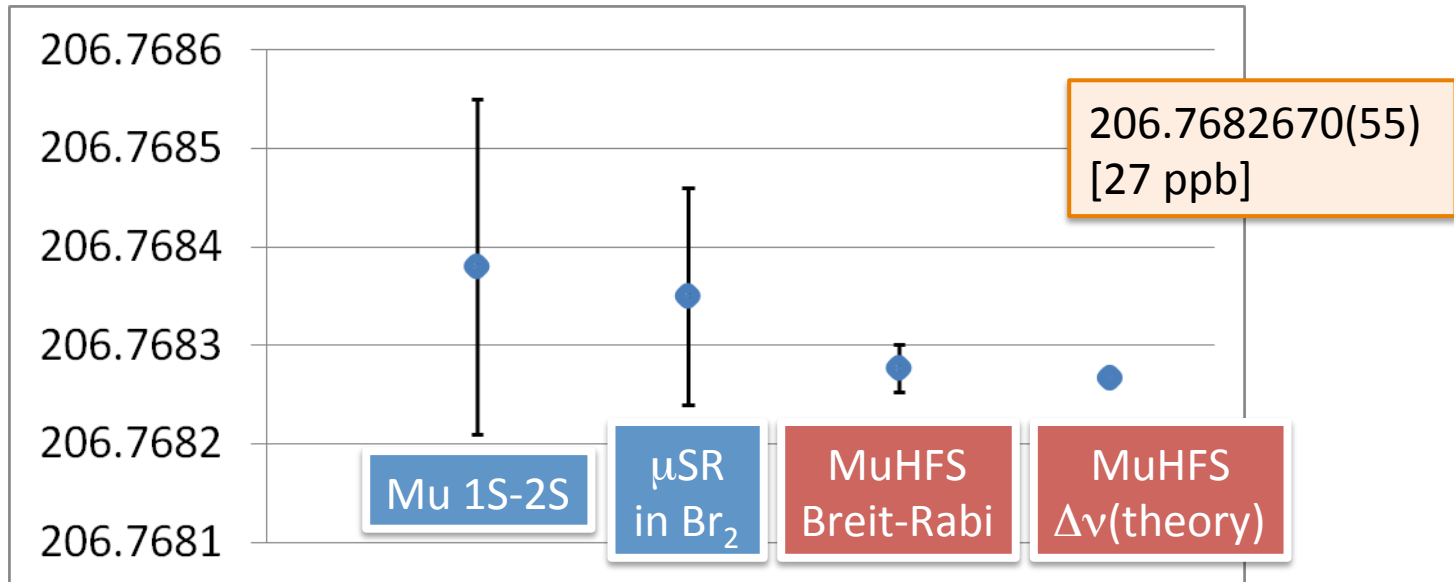
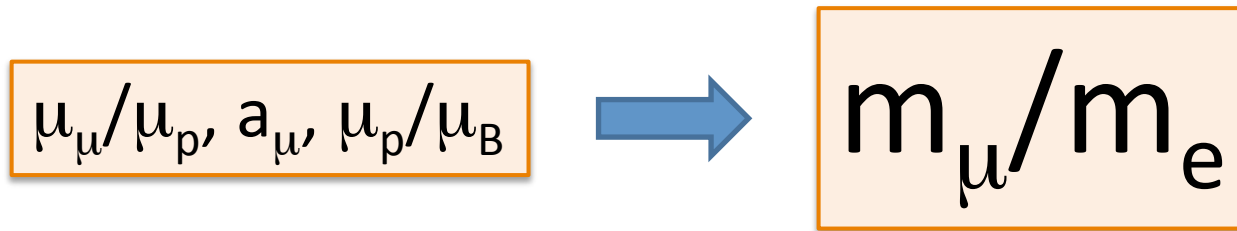
$\nu_{\text{HFS}}(\text{weak})$ -65

$\nu_{\text{HFS}}(\text{had. v.p.})$ 232(1)

$\nu_{\text{HFS}}(\text{had. h.o.})$ 5

QED calculation \rightarrow 10 Hz accuracy within a few years (by Eides)

Determination of the Muon Mass

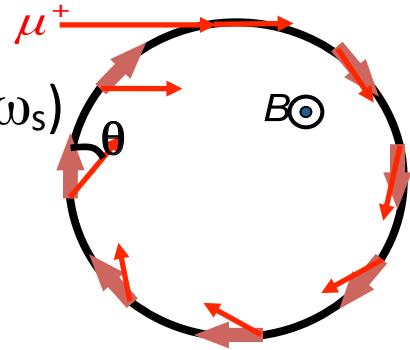


Muon mass (CODATA2010) determined by MuHFS (LAMPF 1999)

Why Mu HFS measurement is so important ?

$g-2$ E821(BNL) 0.5ppm 3σ deviation

- Measurement of the deviation of muon spin direction (ω_s) and muon momentum direction (ω_c) $\omega_a \propto (g-2)/2 = a_\mu$



$$\Rightarrow \vec{\omega}_a = \frac{e}{mc} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \beta \times \vec{E} \right]$$

a_μ an independent precise muon mass measurement is required!

- The ratio to the proton NMR frequency is important!

$$\Rightarrow a_\mu = \frac{R}{\lambda - R}$$

From $g-2$ storage ring

$$R \equiv \frac{\omega_a}{\omega_p} \quad \lambda \equiv \frac{\mu_\mu}{\mu_p}$$

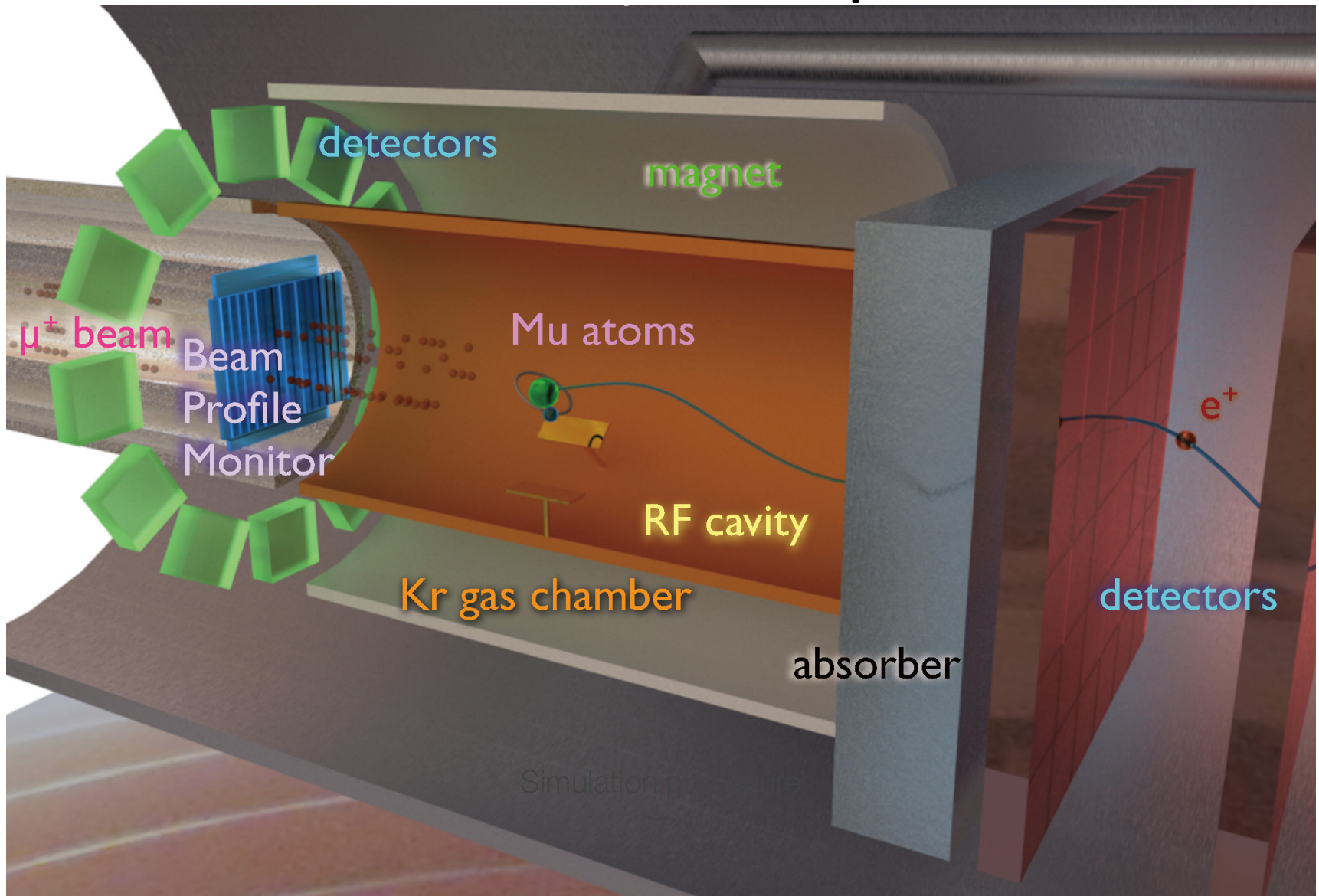
From Muonium HFS

$$\begin{aligned} \frac{\omega_a}{\omega_L(\mu)} &= \frac{a_\mu \left(\frac{eB}{mc} \right)}{g_\mu \left(\frac{eB}{2mc} \right)} = \frac{a_\mu}{\left(\frac{g_\mu}{2} \right)} = \frac{a_\mu}{1 + a_\mu} \\ &= \frac{\omega_a}{\omega_L(p)} \frac{\omega_L(p)}{\omega_L(\mu)} = \frac{\omega_a}{\omega_p} \frac{\mu_p}{\mu_\mu} = \frac{R}{\lambda} \end{aligned}$$

μ_μ/μ_p accuracy from direct measurement of 120 ppb.

W. Liu et al., Phys. Rev. Lett. 82 (1999) 711

Schematic of the Experiment



Improvement of statistics

LAMPF Experiment

$\delta(\Delta v)$

$\delta(\mu_u/\mu_p)$

Statistics

10.9 ppb

Statistics

107 ppb

Kr Density/Pressure

4.4 ppb

Magnetic field

56 ppb

Muon stopping

1.0 ppb

Muon stopping

13 ppb

RF power

0.96 ppb

Kr Density/Pressure

11 ppb

RF power

9.6 ppb

LAMPF: DC $10^7/s$
total 10^{13}

x200

J-PARC/MUSE: **Pulsed $1 \times 10^8/s$**
H-Line
total 2×10^{15}

Systematic error

LAMPF $\delta(\mu_\mu/\mu_p)$

Statistics

107 ppb

DC $10^7/s$, total 10^{13}

x200

J-PARC MUSE

Intense pulsed muon beam

Pulsed $10^8/s$, total 2×10^{15}

Magnetic field

56 ppb

More Uniform Field + Stability

Muon stopping

13 ppb
accuracy 5 mm

**Beam profile monitor
(accuracy ~ 1 mm)**

Kr Density/Pressure

11 ppb
cavity length: 159.73mm

**Low gas density : Long RF cavity
(~ 300 mm)**

RF power

9.6 ppb

RF Input : Coaxial cable

Key Components

- Intense Muon Beamline
Kawamura, Toyoda
- MuHFS S.C. Magnet
Sasaki, Mizutani, Ueno, Higashi
- RF Cavity
Tanaka, Matsuda
- Kr Chamber
Tanaka, Torii, Strasser
- Positron Detector
Kanda, Fukao, Mibe
- Beam Profile Monitor
Tajima, Toyoda, Ito
- Systematic Error Study
Tanaka, Kanda, Ishida

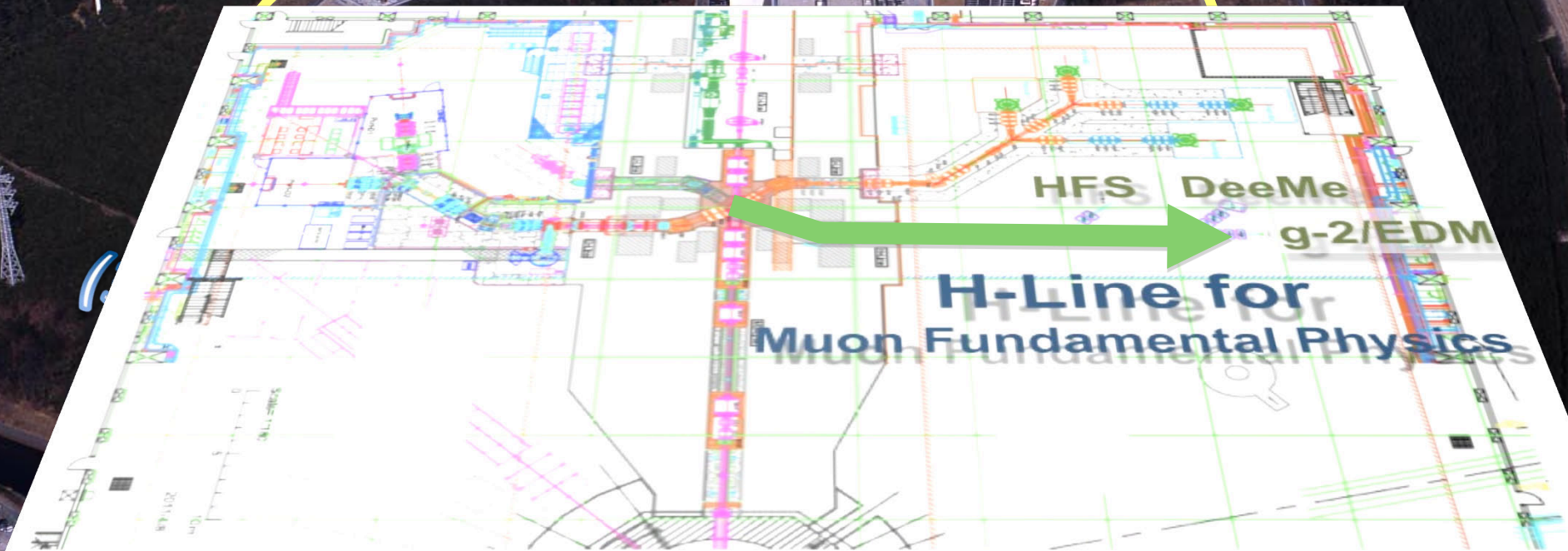
**J-PARC Facility
(KEK/JAEA)**

Kawamura, Toyoda

LINAC

**3 GeV
Synchrotron**

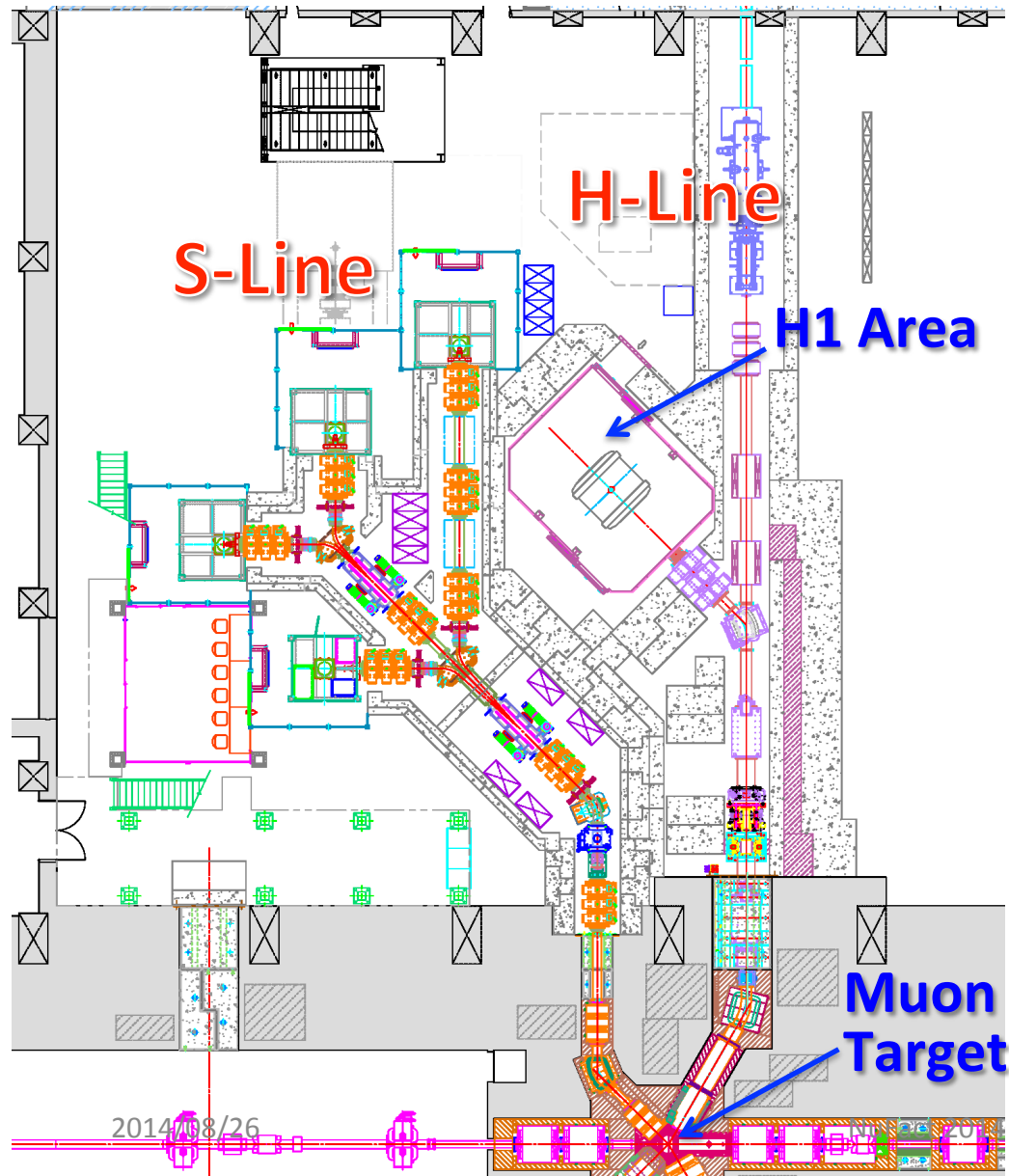
**Neutrino Beam
To Kamioka**



**HFS DeeMe
g-2/EDM**

**H-Line for
Muon Fundamental Physics**

MLF Experimental Hall No.1

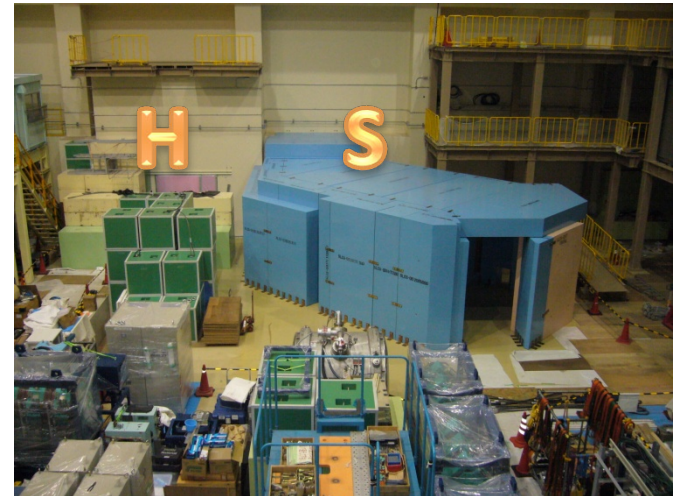


S-Line: surface muon

Surface muons are provided to four experimental areas simultaneously.

H-Line: large scale experiments

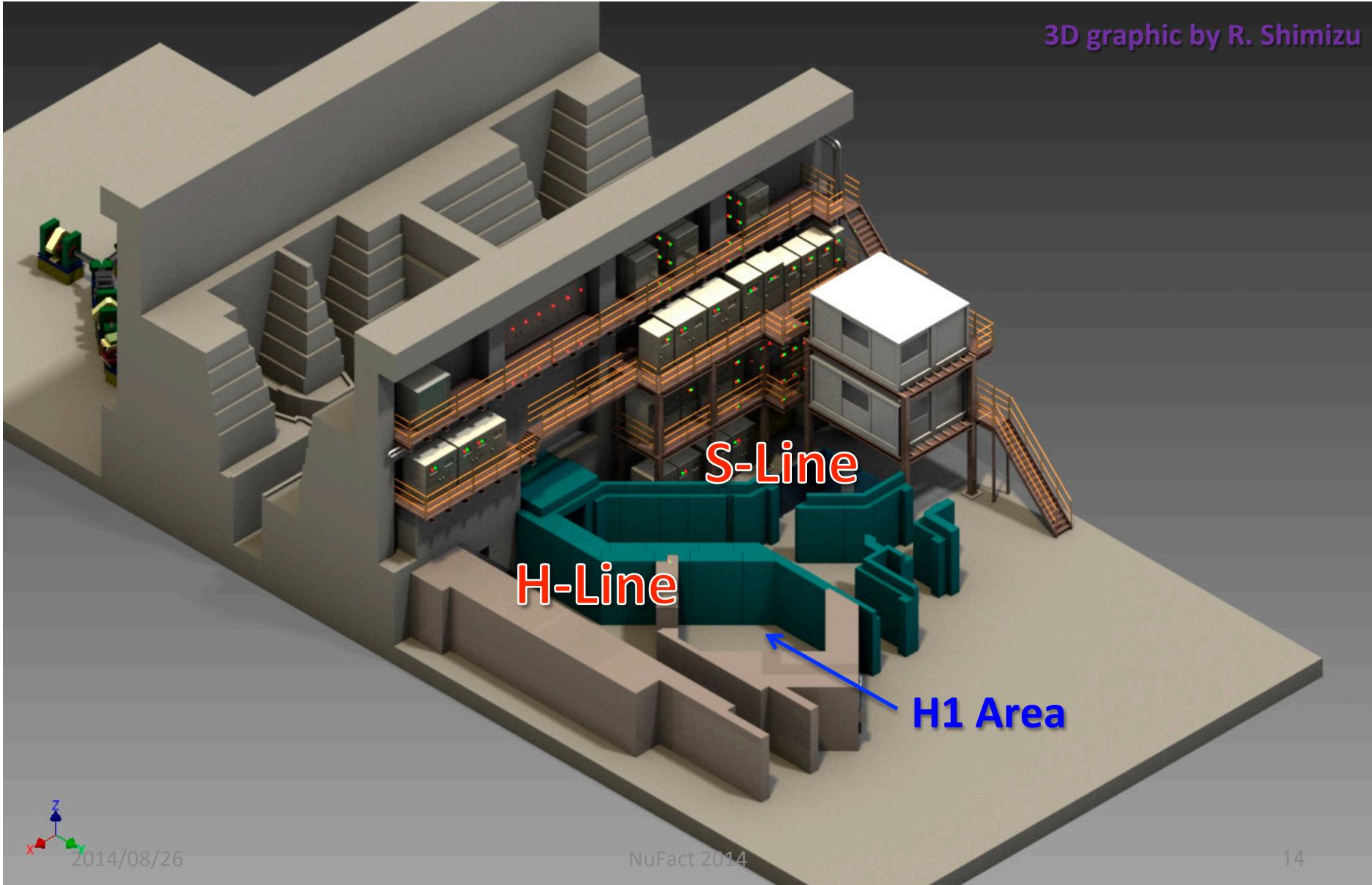
Higher intensity tunable ($<120\text{MeV}/c$) μ^+ and μ^- beams are provided. (g-2, MuSEUM, Deeme, ...)



Experimental Hall No. 1 (Dec. 20, 2013)

MLF Experimental Hall No.1

3D graphic by R. Shimizu



2014/08/26

S.C. Magnet (MRI magnet)

Sasaki, Mizutani, Ueno

- ▶ Stability: 0.03 ppm/h
- ▶ Uniformity (30cm DSV) < 1 ppm
- ▶ Effective bore radius: 680 mm
- ▶ Multi NMR probe for precise field measurement.
- ▶ With shim coils (in the magnet), and Fe shimming plates.
- ▶ Twice 500L LHe refilling a year is needed.



Length	2014 mm
Outside diameter	2152 mm
Minimum roof height	2688 mm
Weight	10.5 tons
Bore diameter	925 mm
Central magnetic field strength	2.9 T
B field leakage (5 Gauss)	Z6 m
	R3.5 m
Uniformity	2.0 ppm @ 40 cm DSV
	1.0 ppm @ R30 cm, Z20 cm



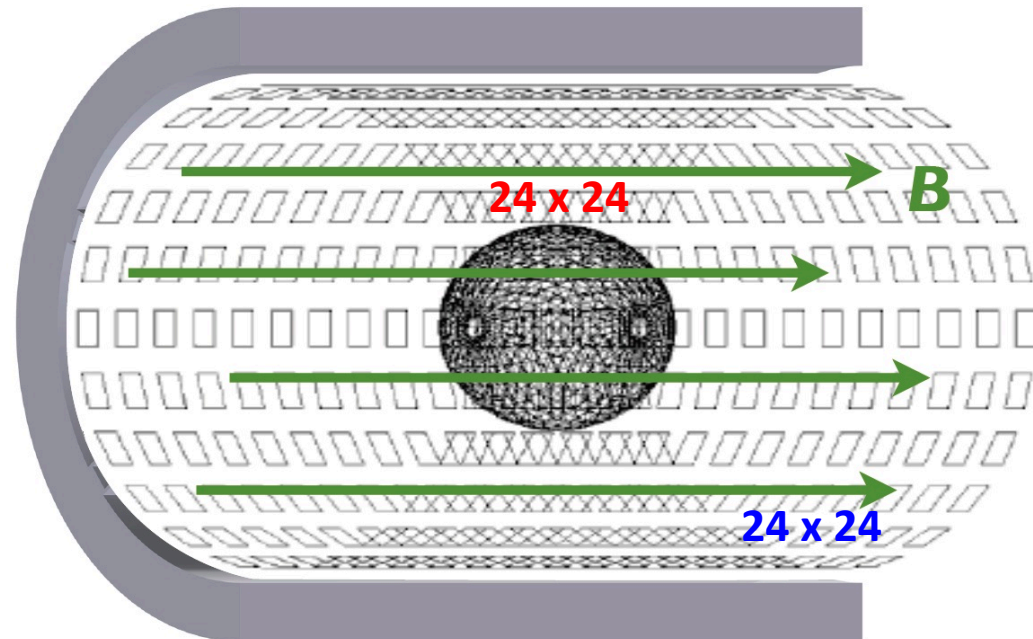
Superconducting Magnet

1.7 T high-precision superconducting magnet

Bore diameter = $\varnothing 925$ mm

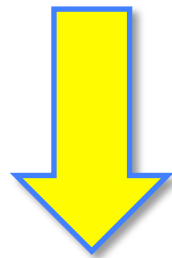
Requirements: **O(0.1 ppm)** homogeneity + **absolute** calibration
in 300 mm x $\varnothing 200$ mm spheroidal region

- Field strength to be measured by water **NMR probes**.
 - 24 probes x 24 positions
- Field correction by shim coils and insertion of Fe shim plates.
- **Shim plate positioning** to be calculated by Singular Value Decomposition Method.
- Iterative process of field adjustment.



B Field Monitoring System

- The homogeneity of the B field in our magnet should be better than 0.1 ppm.



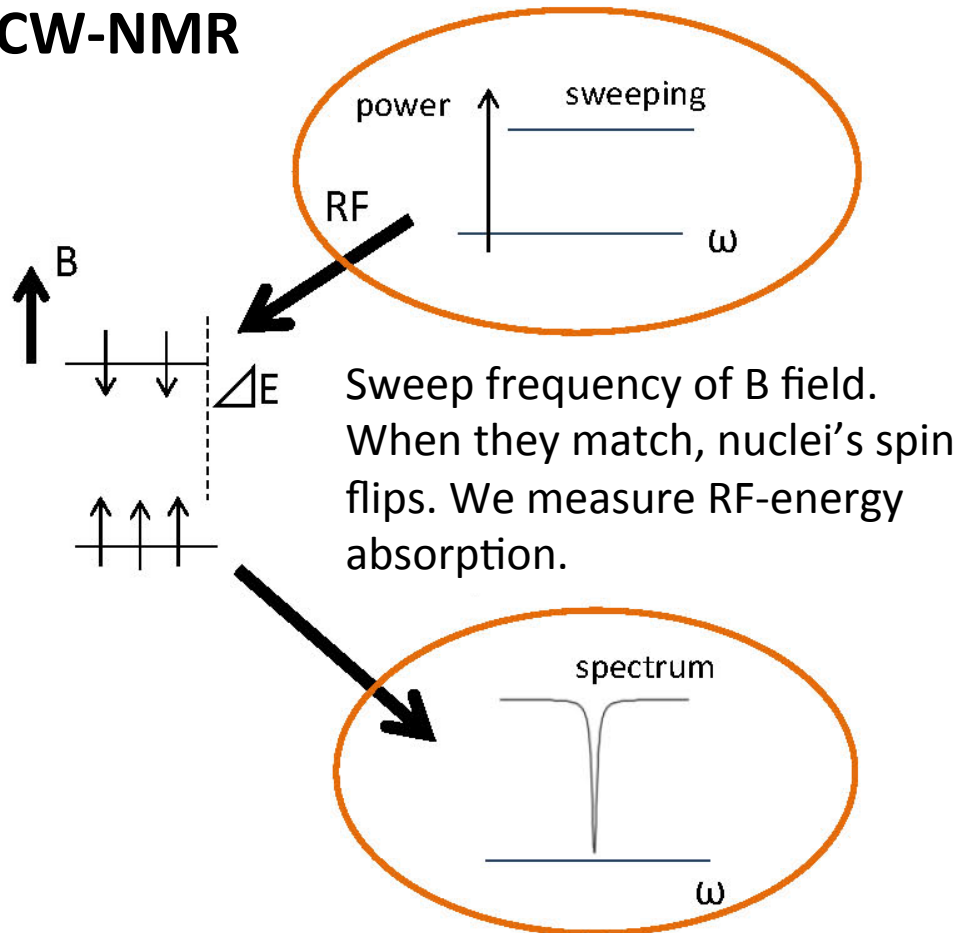
- So, we need to measure the B field with high accuracy, or 0.05 ppm.
- Measuring time should be short (a few hours).

B Field Monitoring System

By Mizutani

NMR Unit

CW-NMR



Echo-denshi

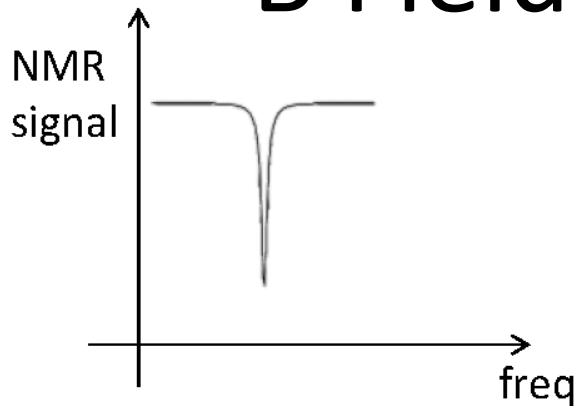


We use commercial NMR unit.

Some improvements are required.

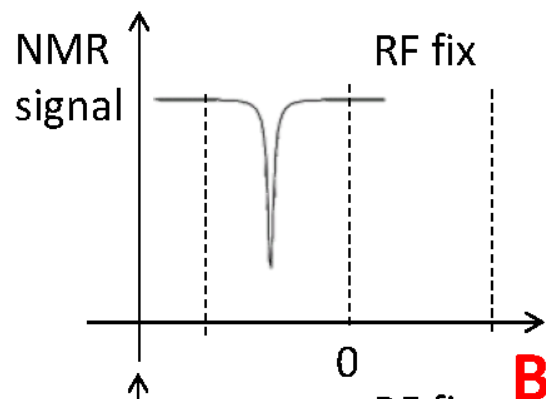
B Field Monitoring System

By Mizutani

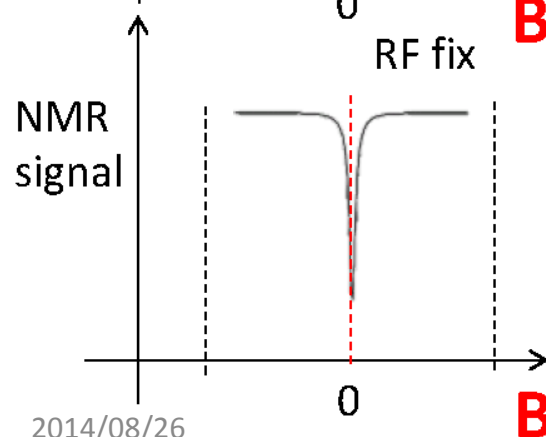


Sweeping RF frequency linearly is difficult. → We **fix the RF frequency**.

We **sweep B field around a cell with another coil**.



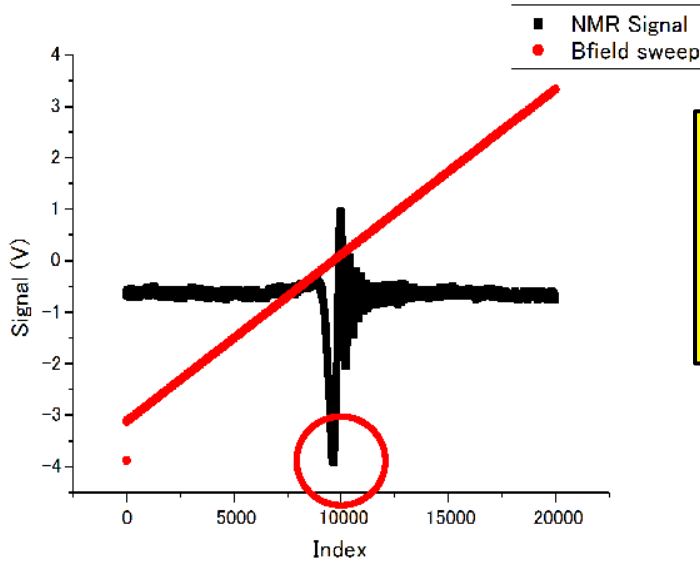
1. Get NMR resonance signal.
2. Change RF frequency (resonance moves).
3. When the **resonance peak comes to the zero-crossing point**, we get the resonant frequency = B field.



By this way, we can get rid of the uncertainty of the B field modulation coil.

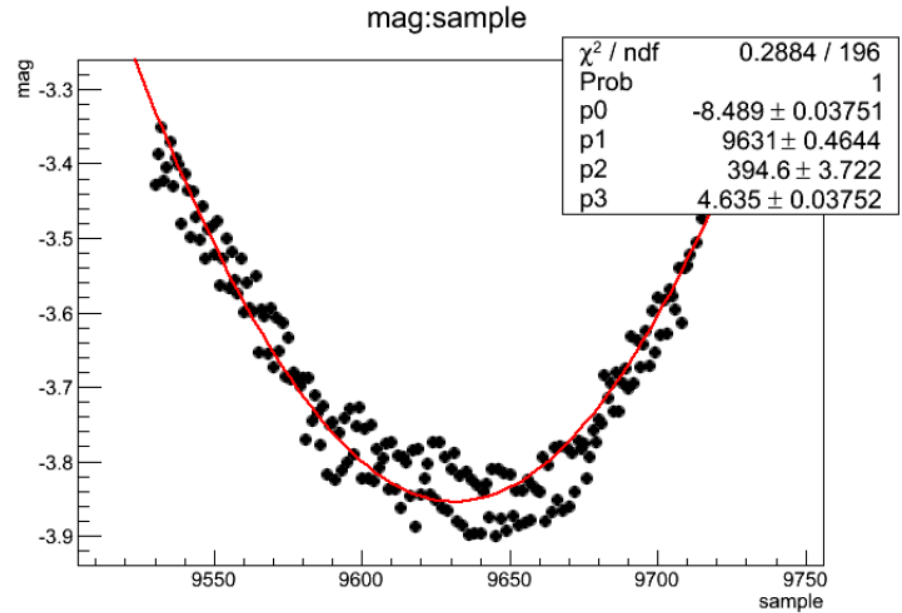
Fixed Point Measurement Test

By Mizutani



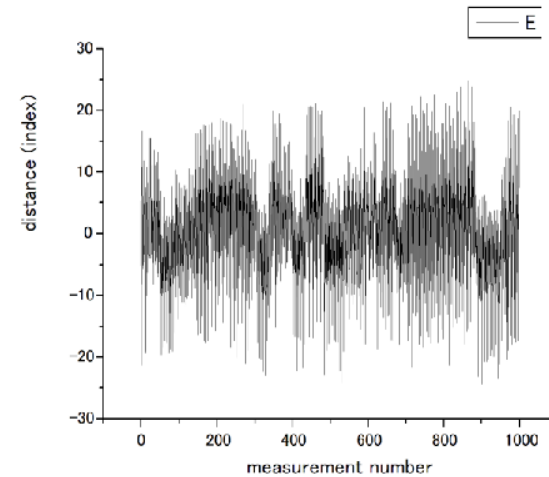
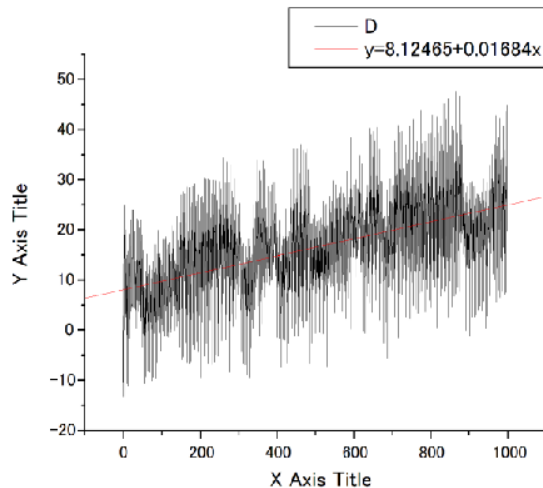
Z = 10 mm
Sampling rate 100 kHz
 $\pm 50 \mu\text{T} / 0.2 \text{ sec.}$
So this graph consists of 20,000 points.

We get 1000 sets of data.
(so we can draw 1000 similar graphs)
And so we can make a histogram of peak points. \Rightarrow
experimental uncertainty
We can also fit or smooth the wave shapes.

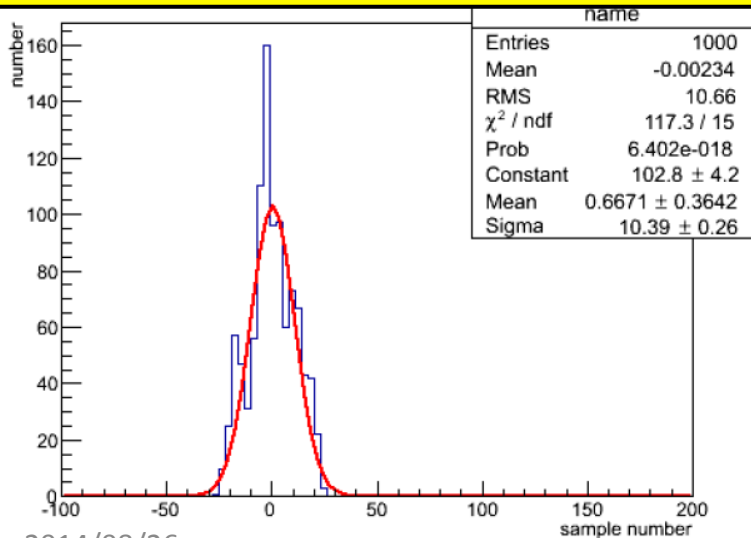


Fixed Point Measurement Test

By Mizutani



Index number × (sweeping rate)[T/sec] × 42.576396 [MHz/T] ÷ 100 [kHz]



2.246 Hz / 67.98 MHz = 33 ppb

Simulation study of NMR probe

By Sasaki

- For precise magnetic field measurement using NMR, some effects should be carefully considered.
- In the previous g-2 experiment at BNL, following contributions were evaluated.

$$\delta_t = \sigma(\text{H}_2\text{O}) + \delta_b + \delta_p + \delta_s. \quad (3)$$

- ▶ $\sigma(\text{H}_2\text{O})$: Internal diamagnetic shielding in the water molecule
- ▶ δ_b : Bulk diamagnetism of the water sample (shape effect)
- ▶ δ_p : Paramagnetic impurities in the water sample
- ▶ δ_s : Paramagnetic and diamagnetic materials in the probe structure

Simulation study of NMR probe

By Sasaki

- ▶ $\sigma(\text{H}_2\text{O})$: Internal diamagnetic shielding in the water molecule
 - ▶ Dominant contribution to the correction factor

$$\sigma(\text{H}_2\text{O}, 34.7^\circ\text{C}) = 25.790(14) \times 10^{-6}. \quad (5)$$

- Derived from the comparison with the oscillation frequency of a hydrogen maser in the same magnetic field

Ref: “Nuclear magnetic shielding constants of liquid water: Insights from hybrid quantum mechanics/molecular mechanics models,” J. Chem. Phys. 126(2007)

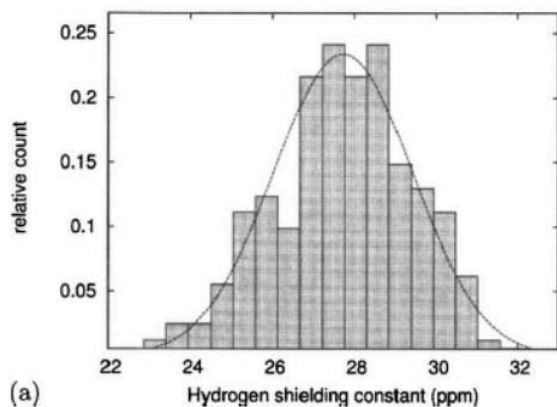


TABLE II. The hydrogen shielding, σ^{H} , and the shift related to vacuum, $\Delta\sigma^{\text{H}} = \sigma_{\text{liq}}^{\text{H}} - \sigma_{\text{vac}}^{\text{H}}$, calculated using different potentials and number of water molecules in the part of the system treated using DFT [DFT ($x = 1, 5, 10$)]. The results have been obtained by averaging over 1500 configurations except for the DFT(10)/MM results which are based on 300 configurations. The error in the mean values is calculated according to σ/\sqrt{N} . The results are in ppm.

	Potential	DET(1)/MM	DFT(5)/MM	DFT(10)/MM	Expt. ^{a,b}
σ^{H}	TIP3P	29.84±0.02	28.63±0.04	28.36±0.08	25.79
σ^{H}	SPCpol	29.39±0.03	28.14±0.05	27.7±0.1	25.79
$\Delta\sigma^{\text{H}}$	TIP3P	-1.05±0.02	-2.26±0.04	-2.53±0.08	-4.26
$\Delta\sigma^{\text{H}}$	SPCpol	-1.50±0.03	-2.75±0.05	-3.3±0.1	-4.26

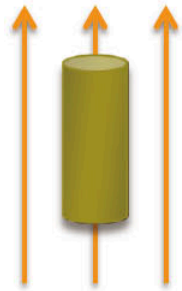
Study of shape effect by FEM simulation

By Sasaki

► Model

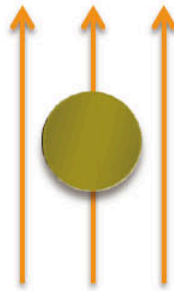
- Water relative permeability : 0.999992

(a) Cylinder
(parallel)



R: 2.5 mm
L: 20 mm

(b) Bulb



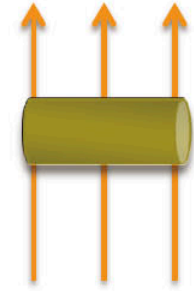
R: 2.5 mm

(c) Bulb+Cylinder



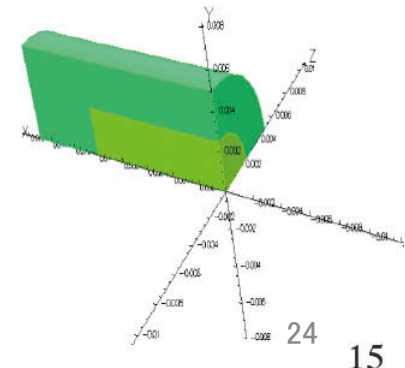
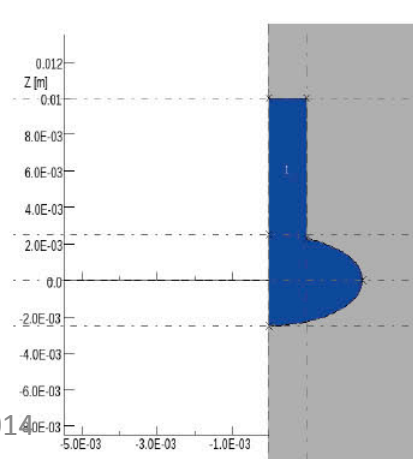
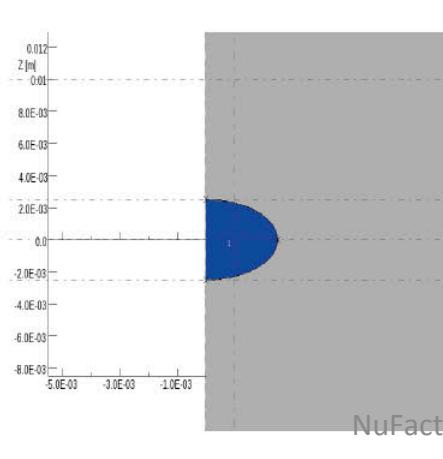
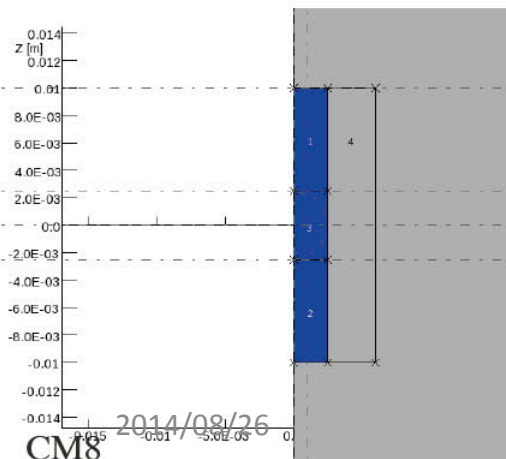
Bulb R: 2.5 mm
Tube R: 1.0 mm
Tube L: 7.5 mm

(d) Cylinder
(perpendicular)



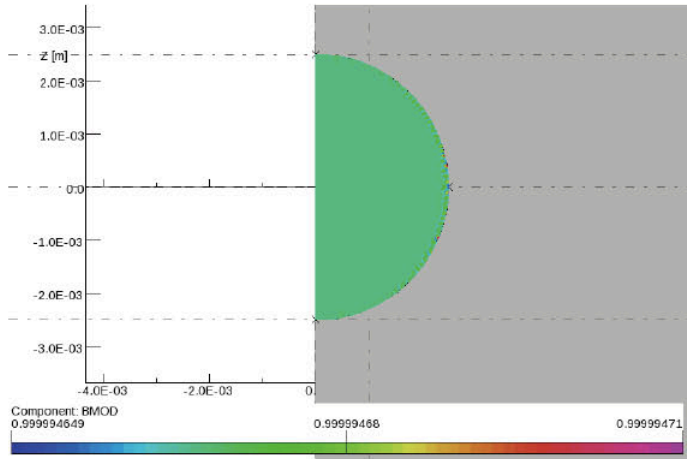
R: 2.5 mm
L: 20 mm

1 T

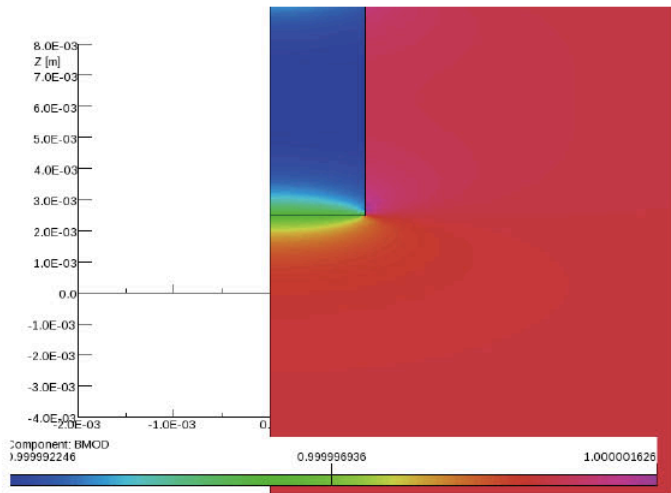


Results ~ bulb + tube

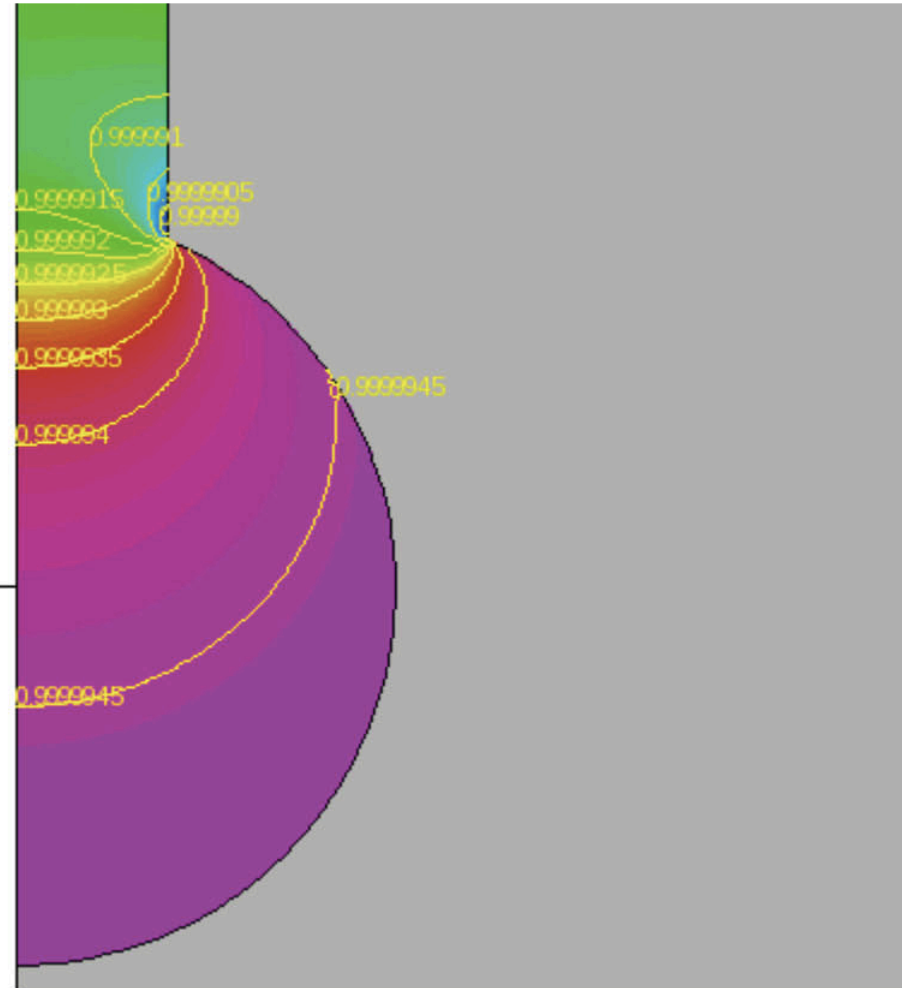
By Sasaki



+

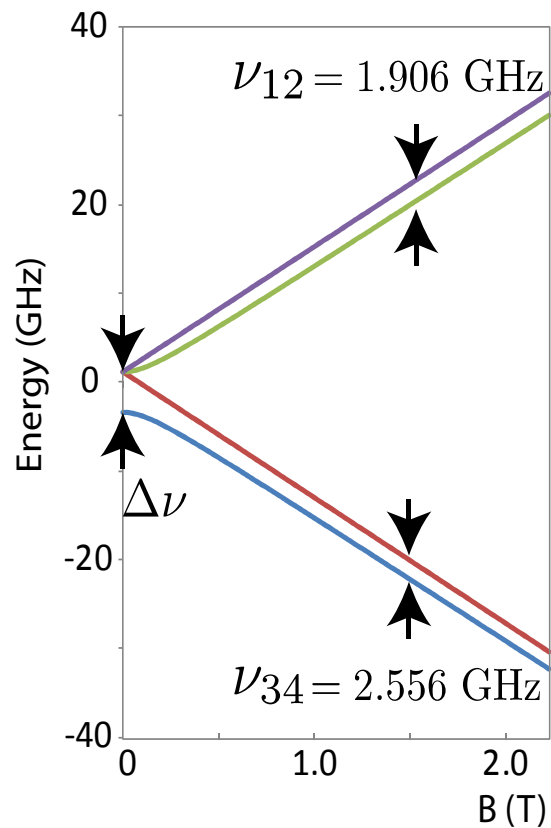


► Contour : 0.5 ppm

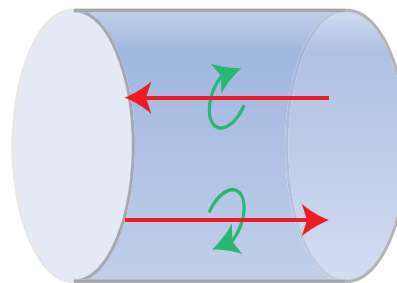


RF Cavity

Tanaka, Matsuda, Torii

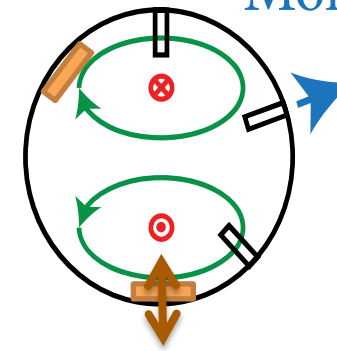


TM110



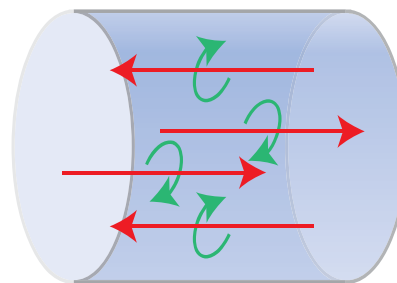
Input

Monitor



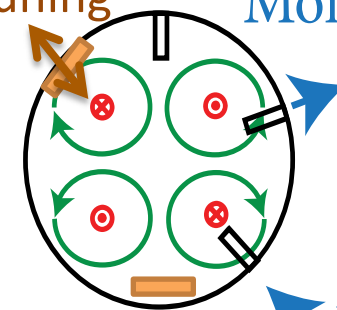
Tuning

TM210



Tuning

Monitor



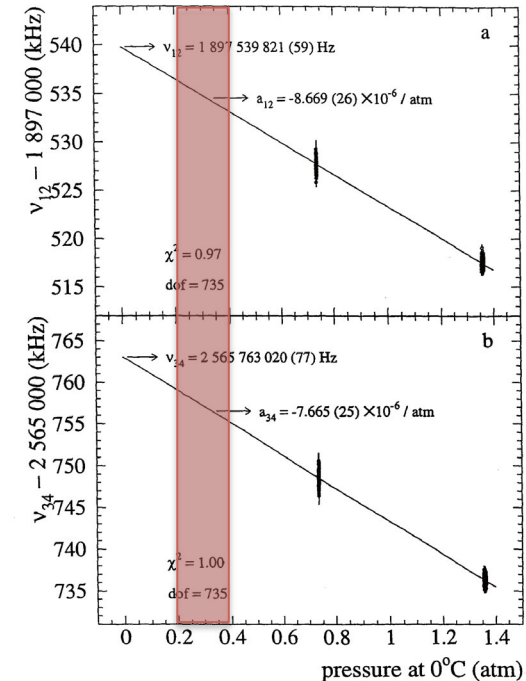
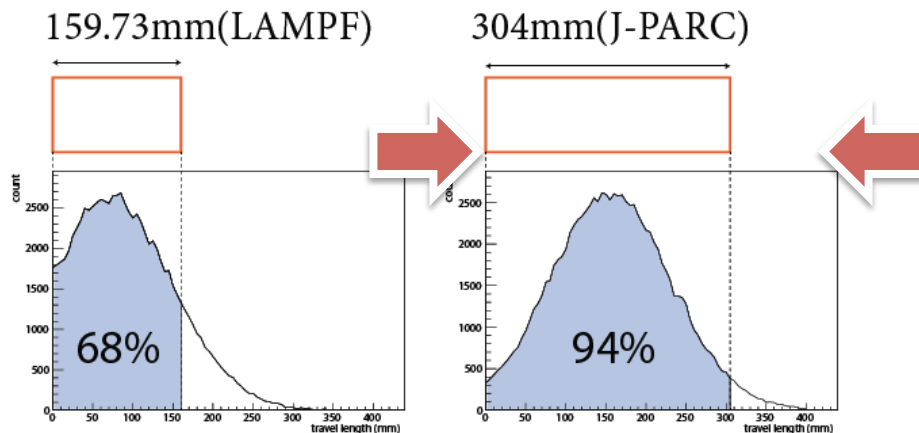
Input

Improvement from LAMPF

Tanaka, Matsuda, Torii

Cavity Length

Muonium distribution at 0.3 atm Kr gas



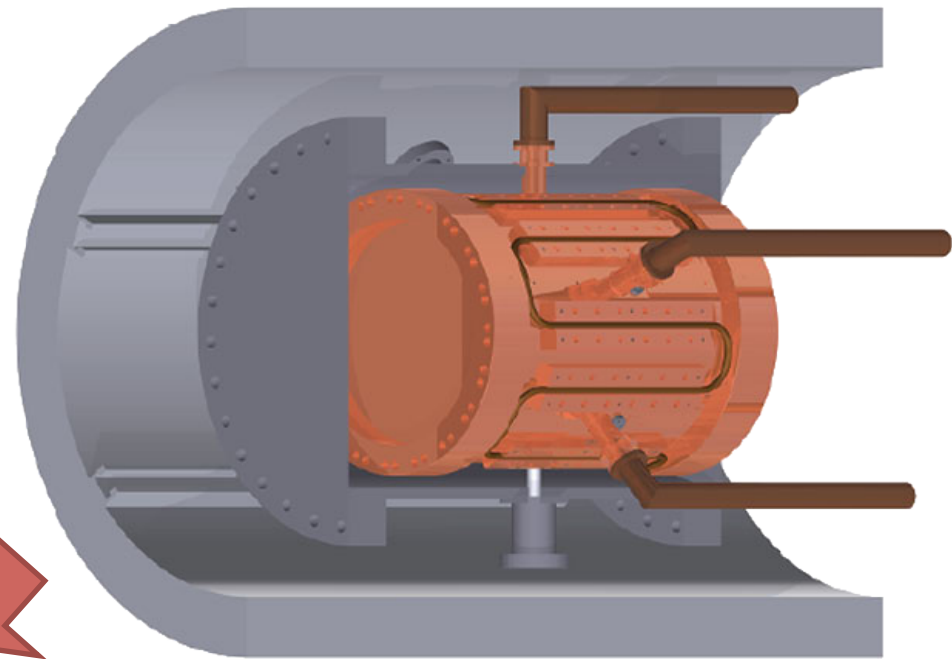
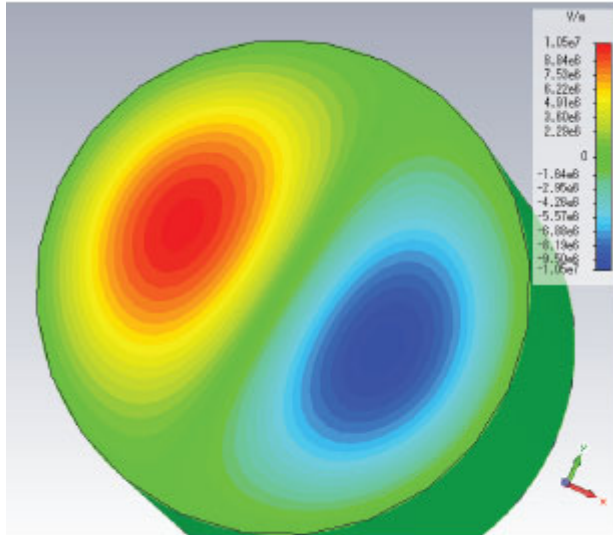
The transition frequency of muonium in gas vary with the gas pressure due to atomic collision between Mu and Kr.

- ⇒ Fitting 0.8 and 1.5 atm data, old quadratic dependence parameter was used (Los Alamos).
- ⇒ We need data at lower pressure for improved fitting.

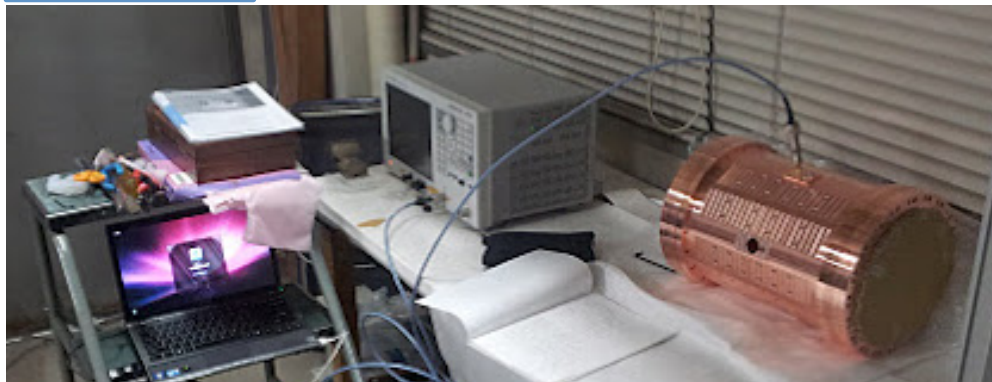
RF Cavity

Tanaka, Matsuda, Torii

MWS simulation

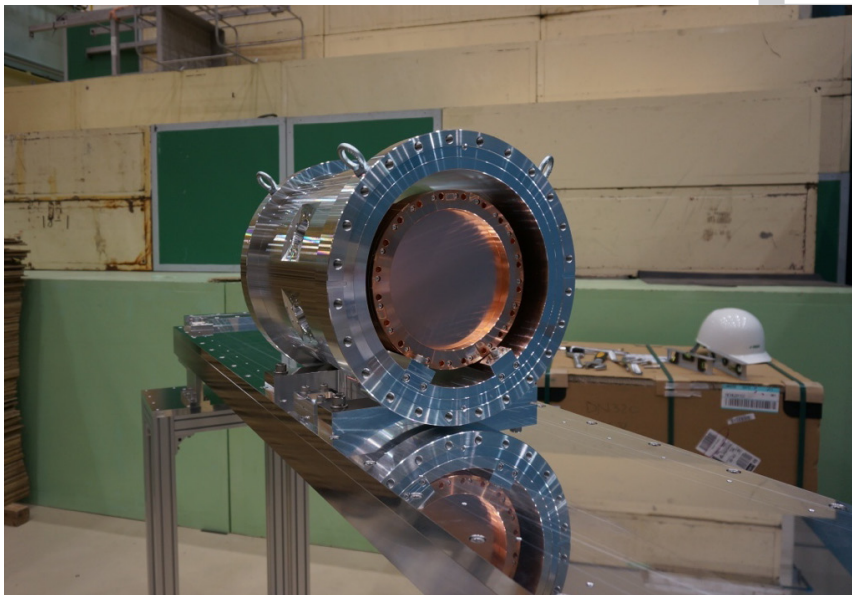
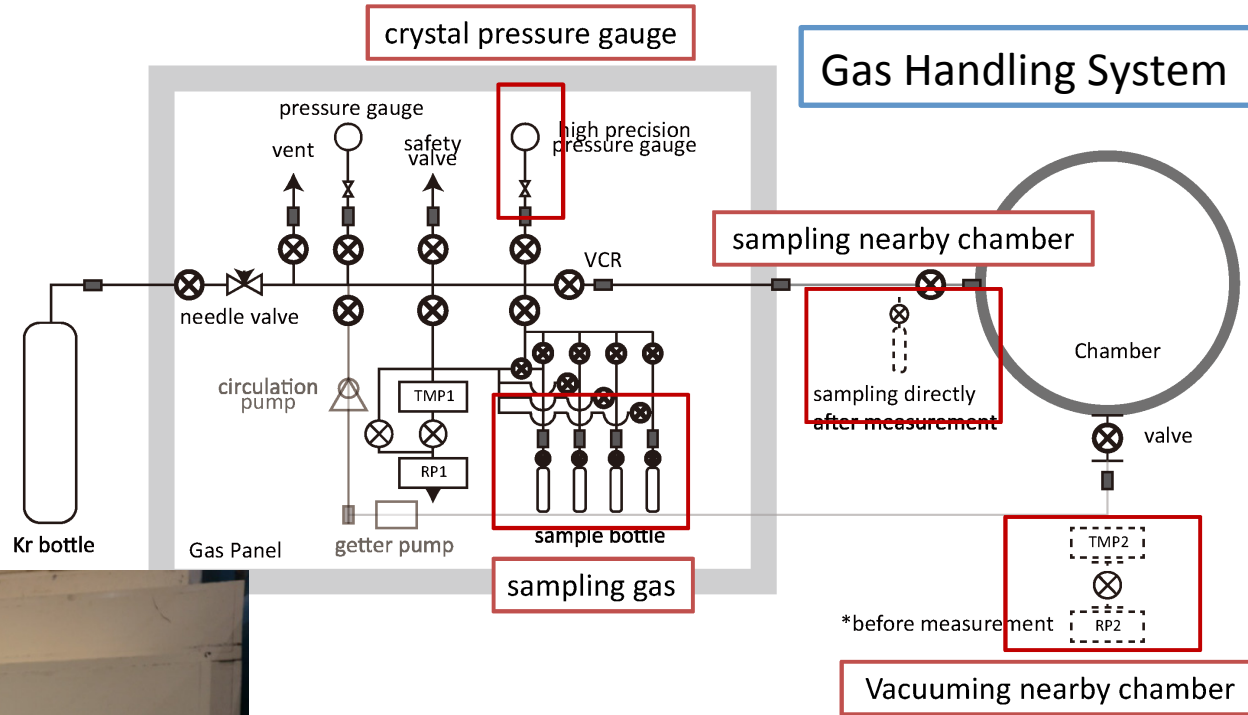


Test Cavity



3D CAD

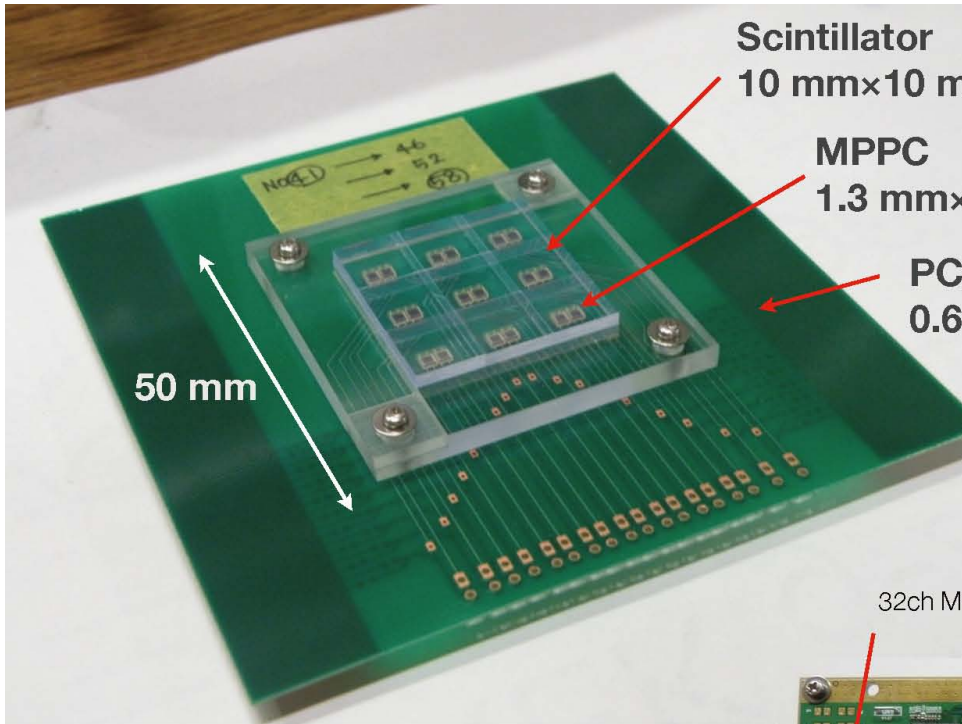
RF Cavity & Gas Chamber



- Pressure: 0.5 – 1.5 atm
- Readout precision: several ppm (crystal gauge: 0.008% of full range)
- Contamination: below 1ppm.
- gas sampling before, during and after the experiment (several weeks).

Positron Detector

Kanda, Mibeuda, Kojima

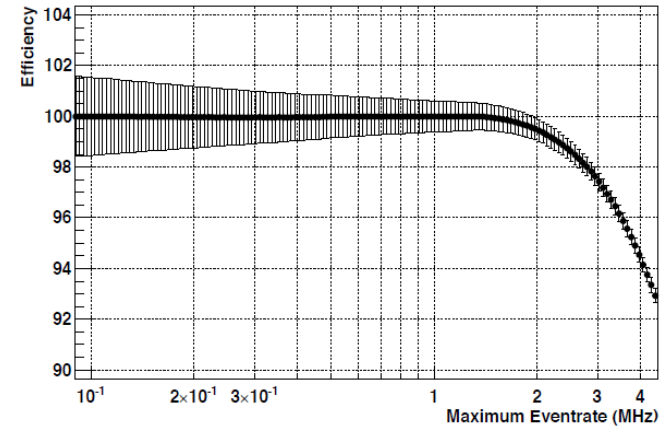


Scintillator
10 mm×10 mm×3 mm t

MPPC
1.3 mm×1.3 mm

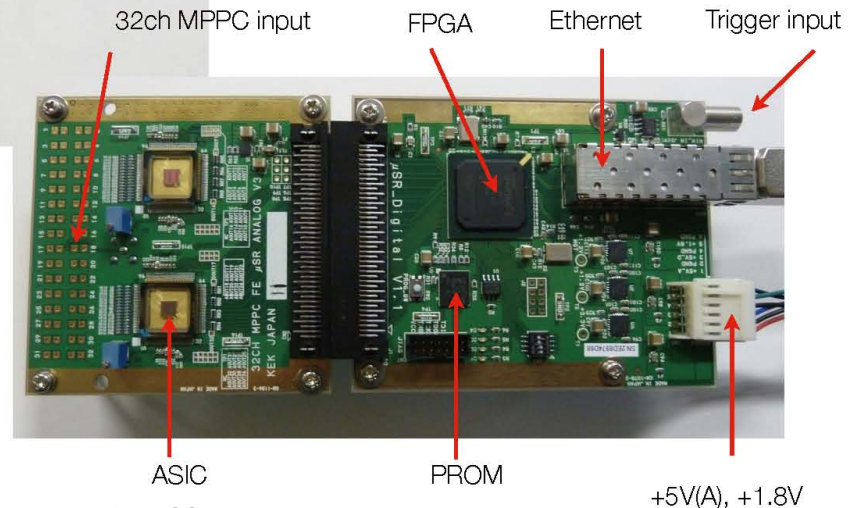
PCB
0.6 mm t

50 mm



Pileup loss at 3MHz/ch ~ 2%

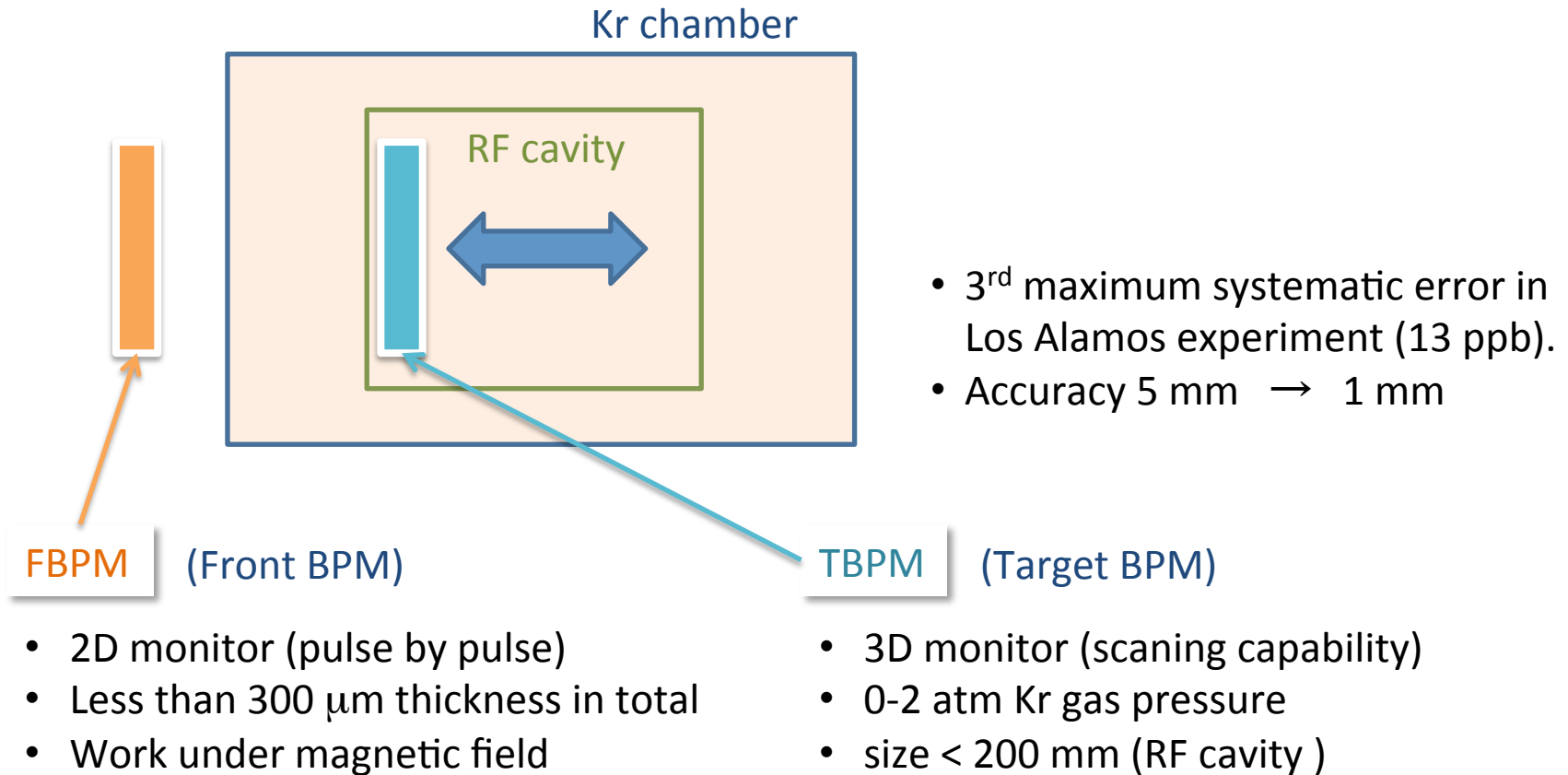
**Plastic scintillator + MPPC
+ Kalliope readout circuit.**
18 channels of 9 scintillator segments.



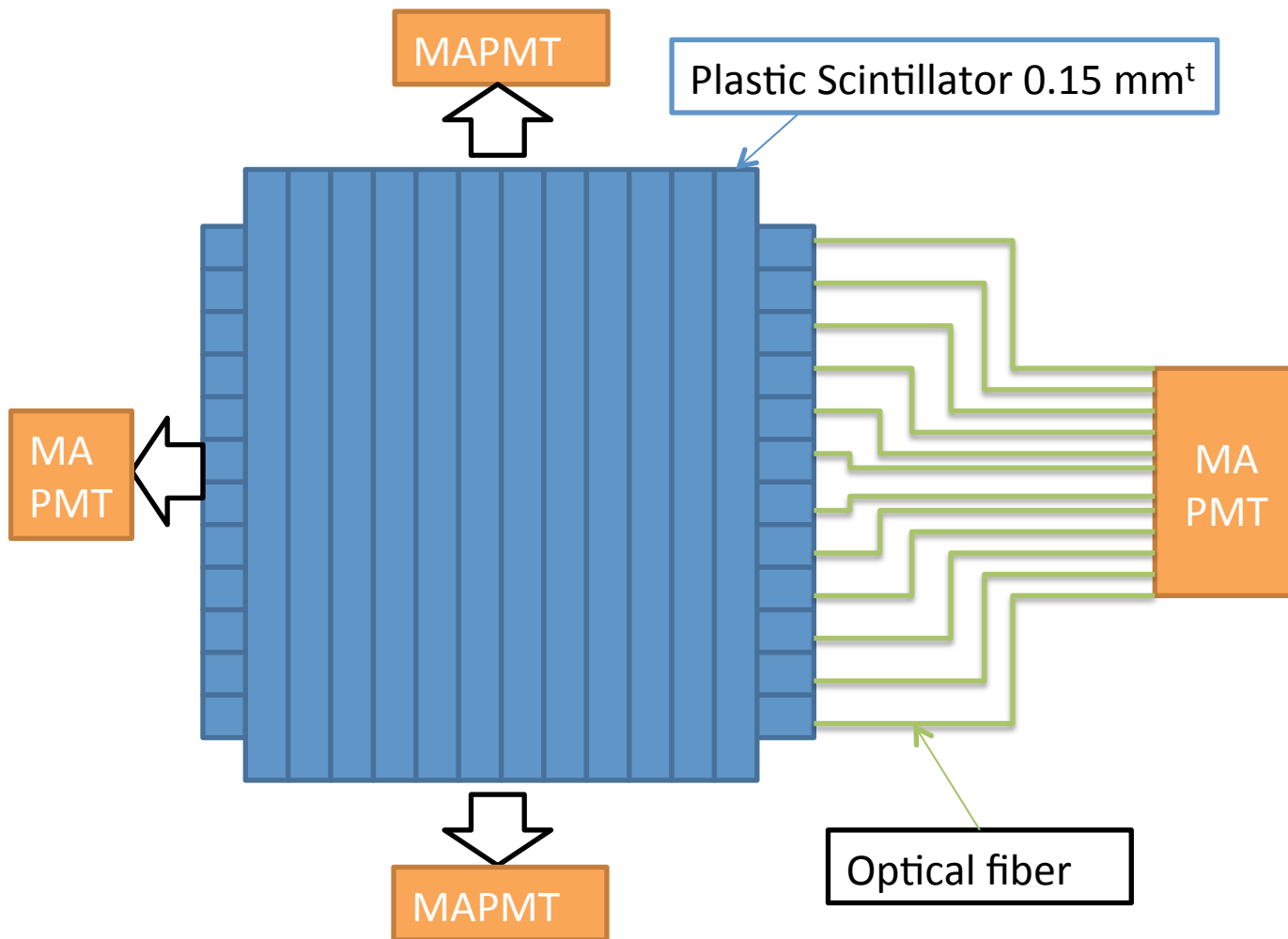
NuFact 2014

Beam Profile Monitor

Tajima, Toyoda, Ito (JAEA)



FBPM



Challenge 1

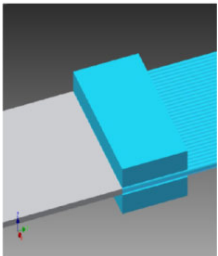
- Uniform muon beam range
- uniform thickness

Challenge 2

- Enough light transmission
- light guide or fiber

FBPM (Prototype)

Fiber
light guide



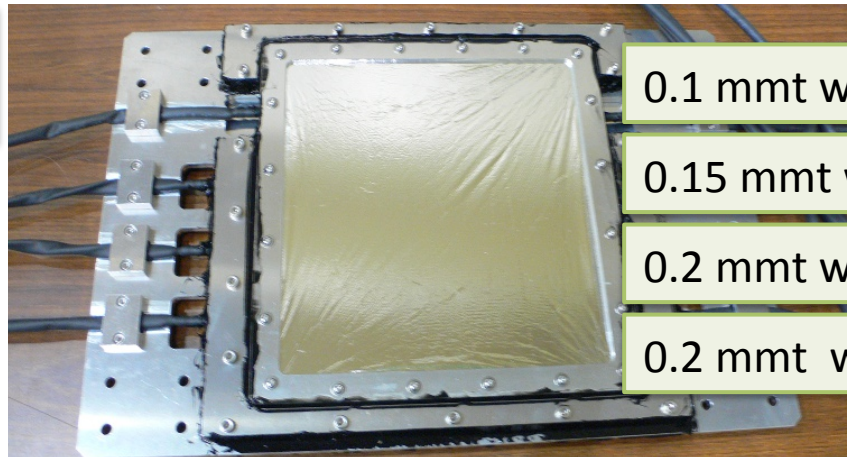
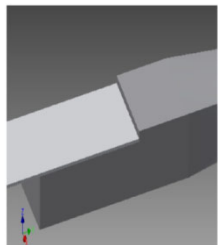
0.15 mmt w/ Al

0.15 mmt w/o Al

0.15 mmt w/ Al

Plastic scintillator sheet
6 mm in width
180 mm in length
5m Fiber
Multianode PMT

Acryl
light guide



0.1 mmt w/o Al

0.15 mmt w/ Al

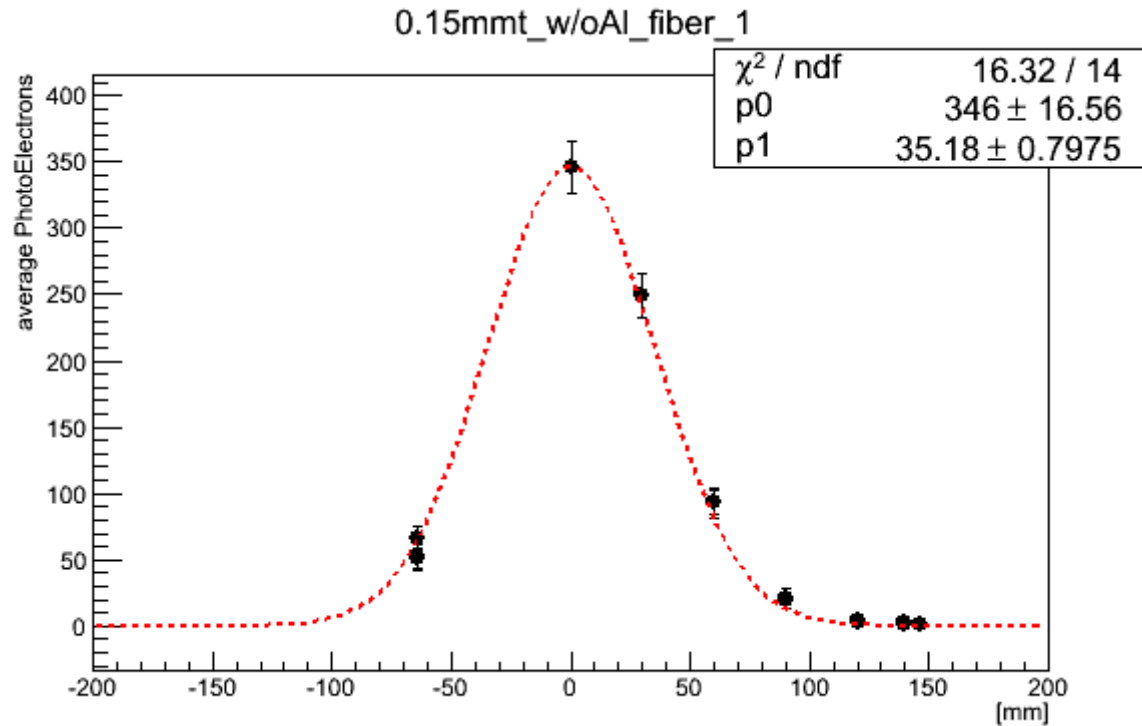
0.2 mmt w/o Al

0.2 mmt w/ Al

Check List

- Effect of Al coating
- Thickness dependence
- Light guide selection
- Position dependence

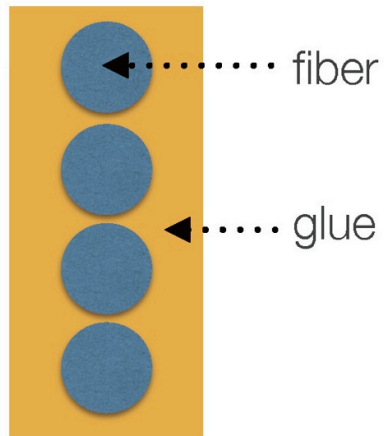
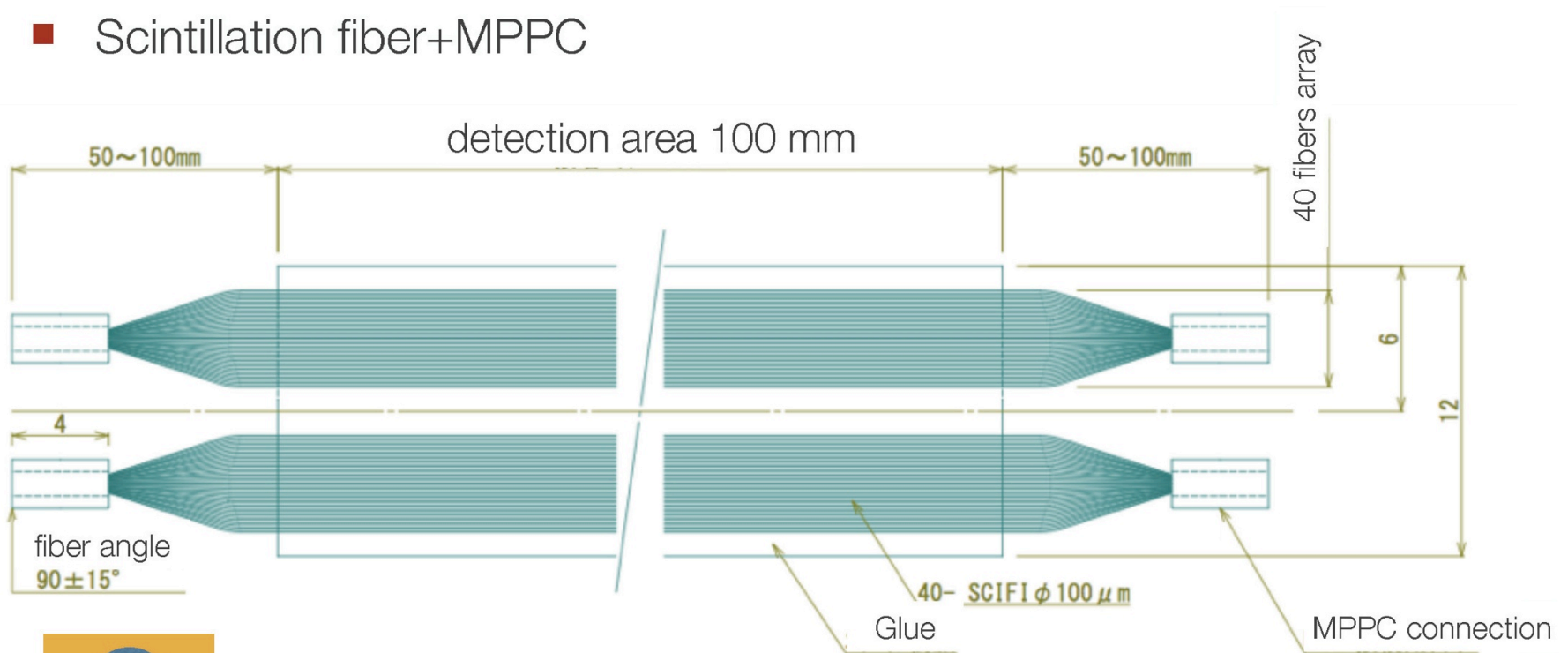
Beam Profile Measurement at D-Line



1mm accuracy is achieved.

FBPM (New Design)

- Scintillation fiber+MPPC

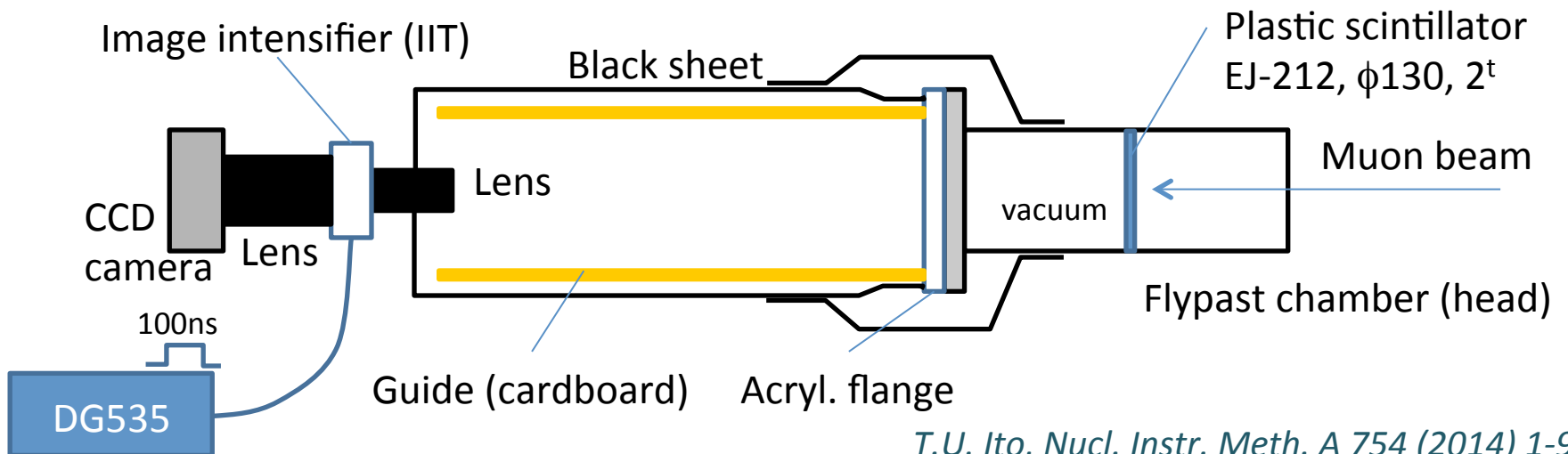
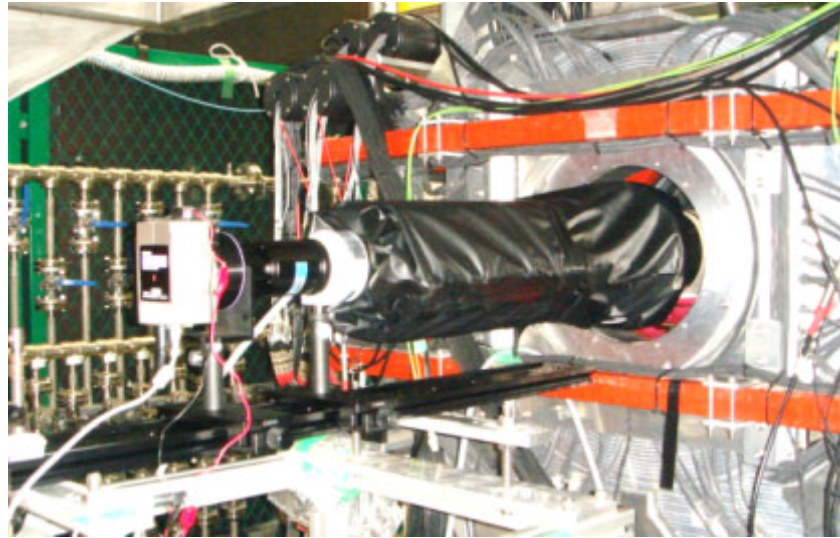


Use a bundle of fine scintillation fibers ($\phi 0.10 \text{ mm}$).

- Better optical coupling to MPPC
- Less position dependence along the fiber
- Better control of (effective) thickness ??

TBPM (IIT muon beam profile monitor)

Tajima, Toyoda, Ito (JAEA)



T.U. Ito, Nucl. Instr. Meth. A 754 (2014) 1-9

TBPM

Tajima, Toyoda, Ito (JAEA)

Setup

Scintillator plate

Scintillation light

Lens

ITT

Lens

CCD

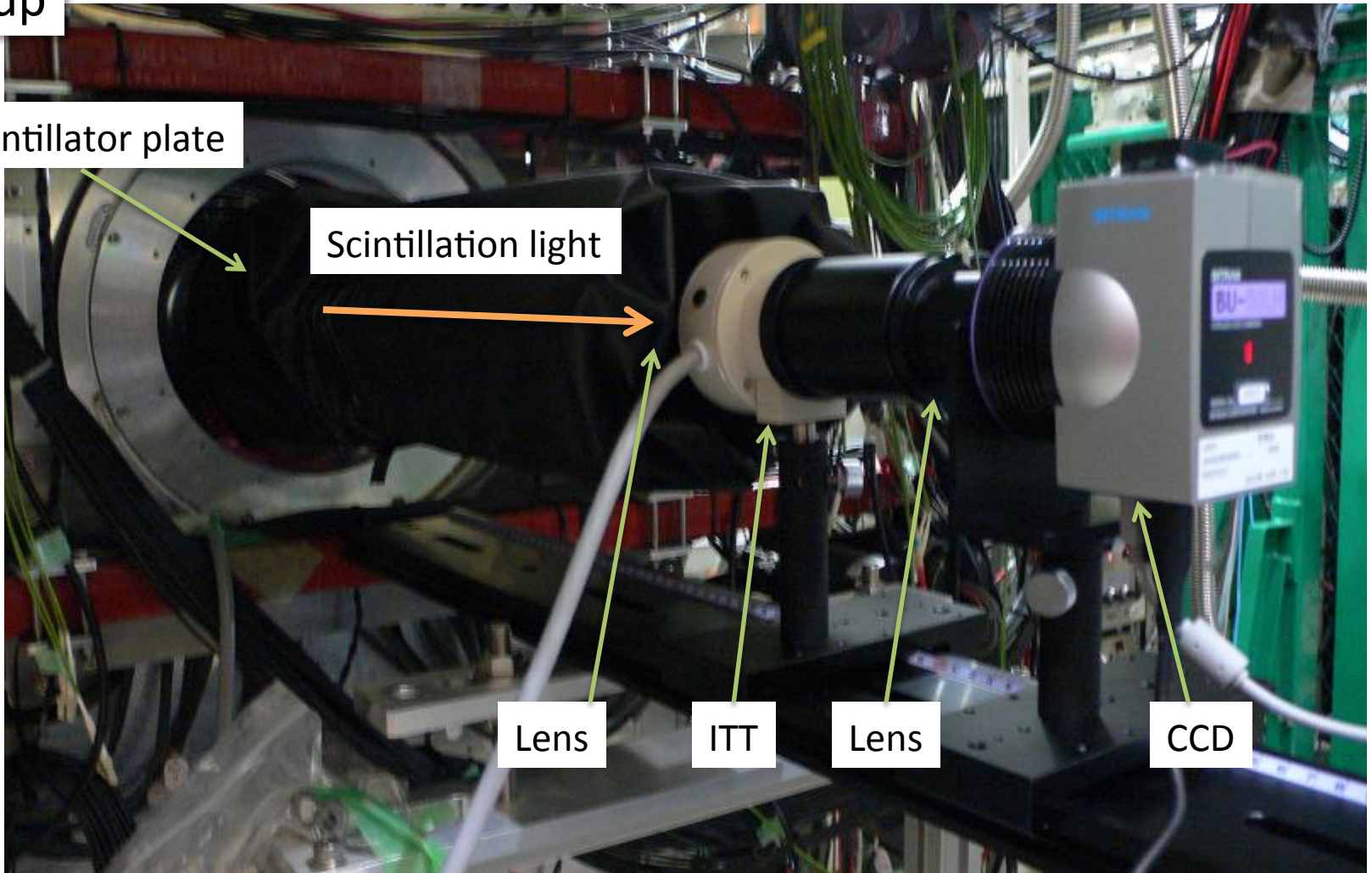
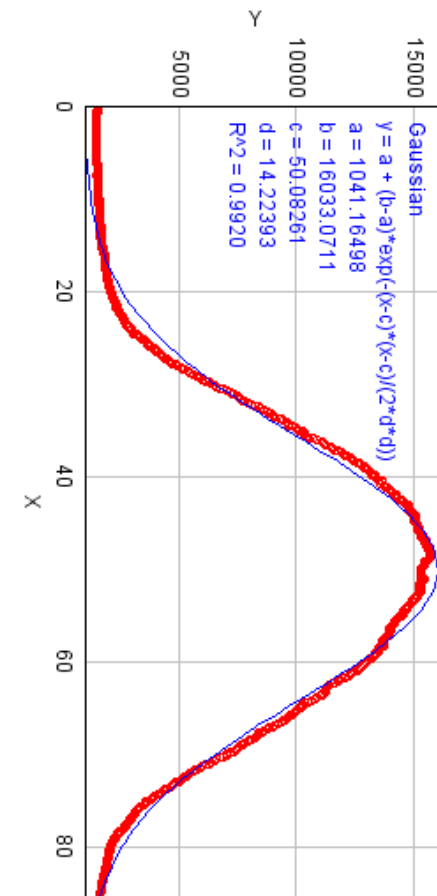
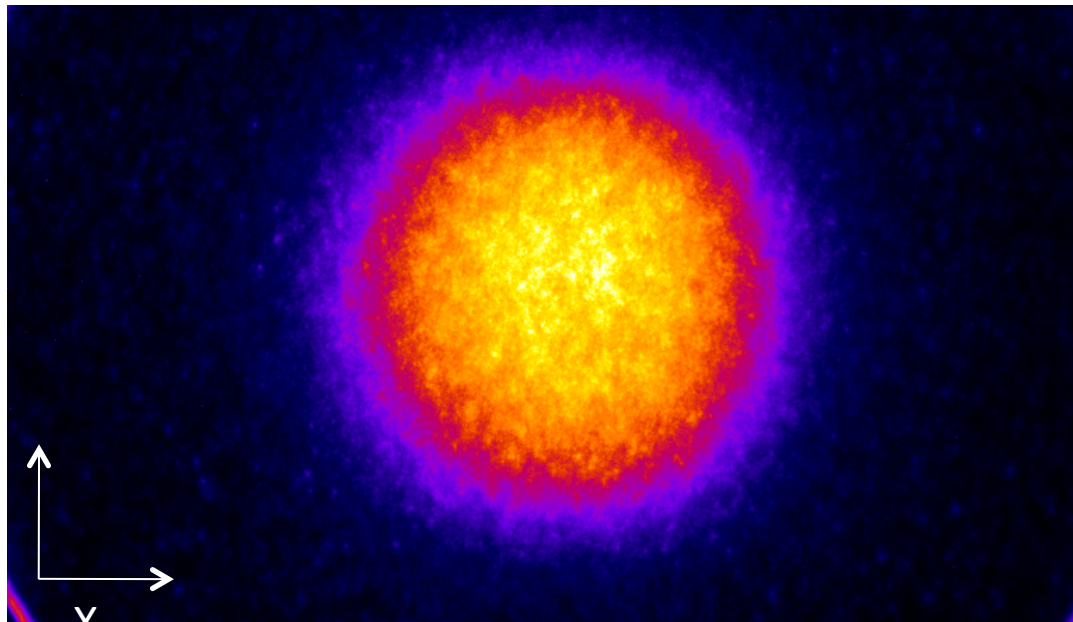
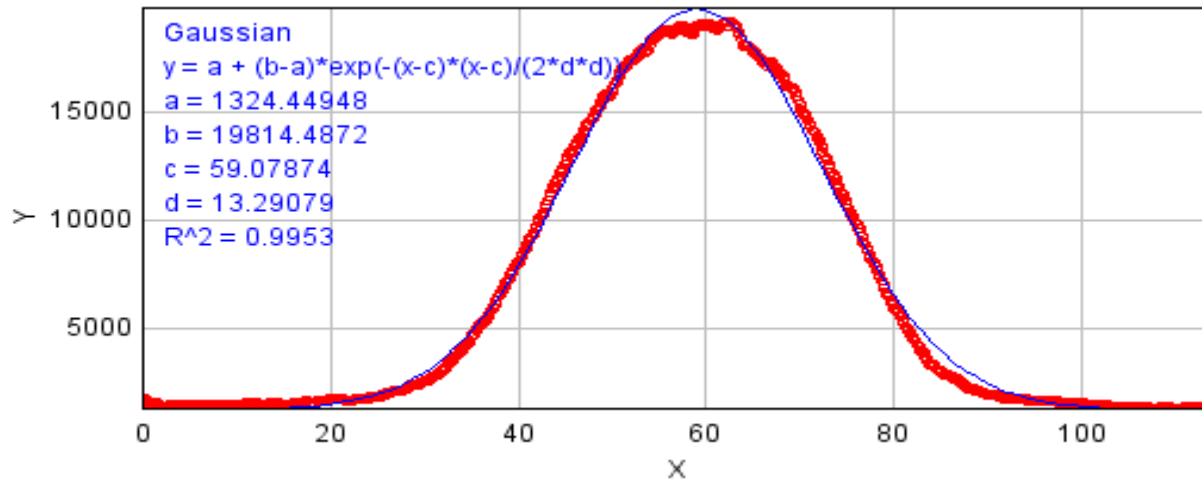


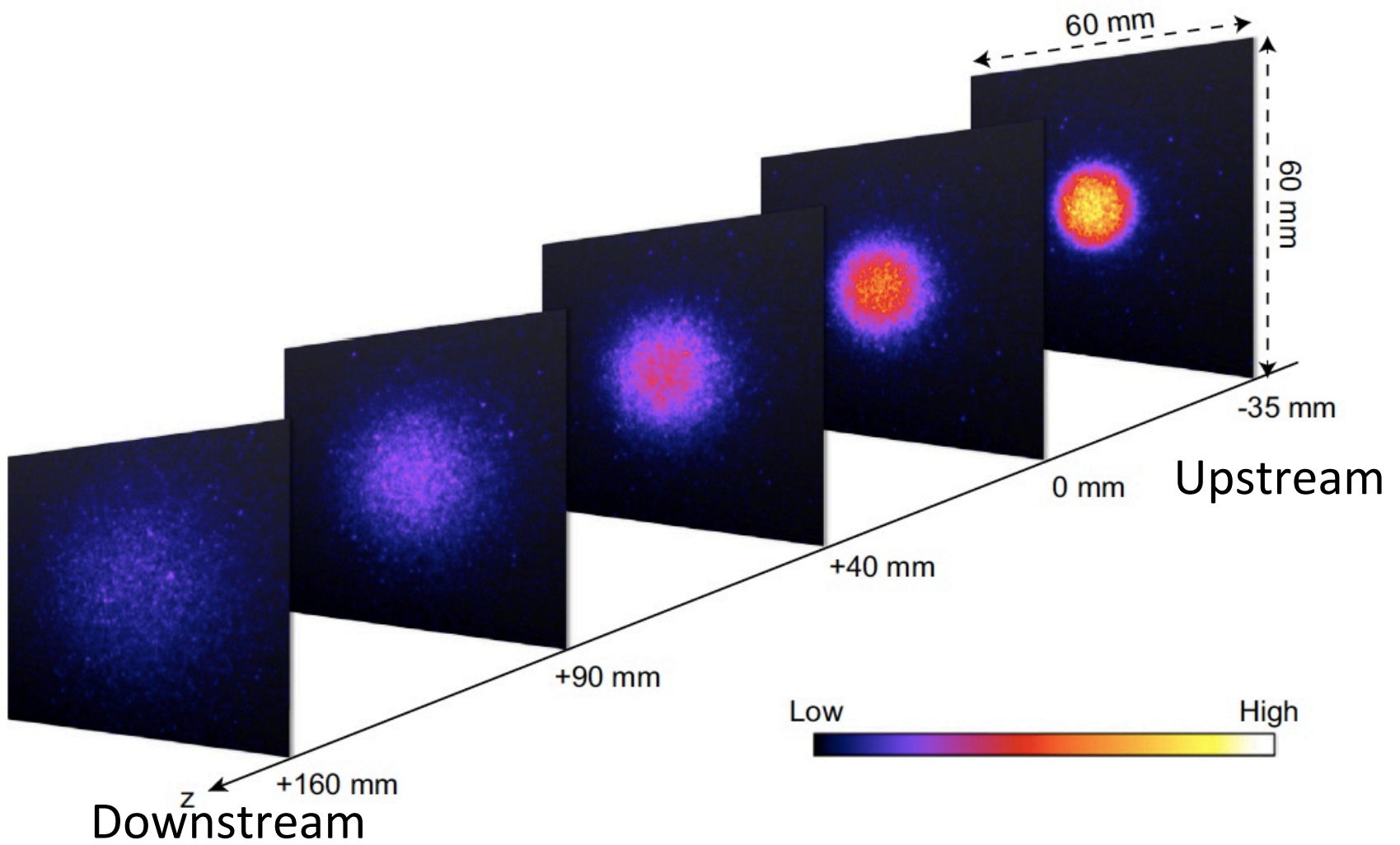
Image of Muon Beam at D-Line

Tajima, Toyoda, Ito (JAEA)



3D Image in Air

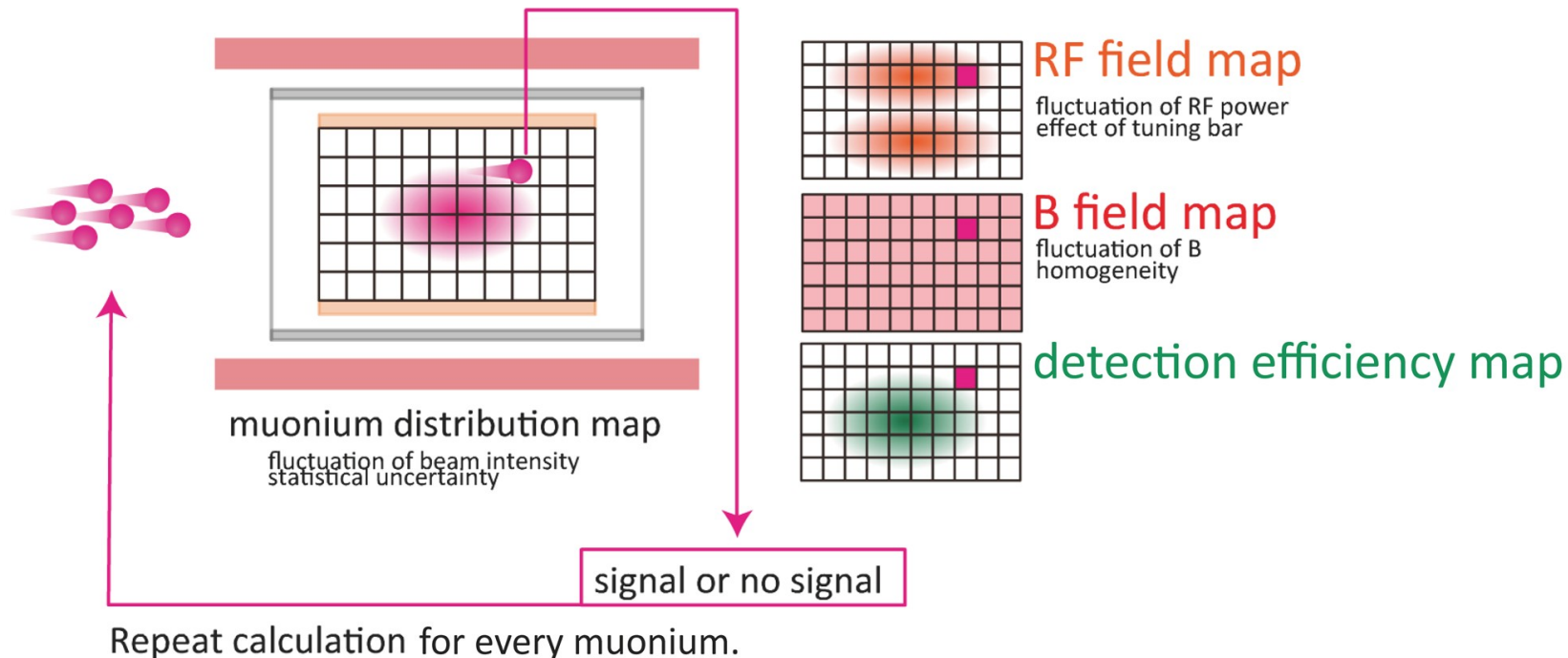
Tajima, Toyoda, Ito (JAEA)



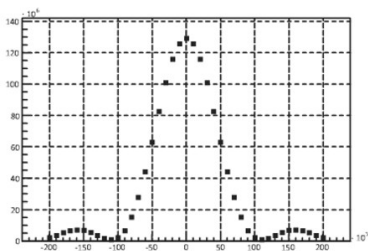
Systematic Error

Calculate transition probability.

Tanaka, Kanda, Ishida

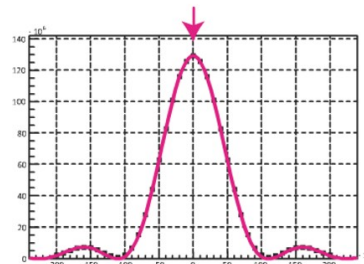


plotting



fitting

Center of the resonance line determined by fitting.



Systematic Error

Tanaka, Kanda, Ishida

	Accuracy	v_{12} and v_{34}	$\delta(\Delta v_{\text{HFS}})$	$\delta(\mu_u/\mu_p)$
Magnetic Field	30 ppb		0.0 ppb	15 ppb
RF power	0.10 %	10 Hz	2.0 ppb	20 ppb
Kr gas temperature	0.1 deg.	< 1 Hz	0.2 ppb	2 ppb
Kr gas pressure	0.01 hPa	1 Hz	0.2 ppb	0 ppb
H impurity	<50 ppm	1 Hz	0.5 ppb	0 ppb
Quadratic dependence		5 Hz	1.0 ppb	5 ppb
Muonium position (x,y)	1 mm	3 Hz	0.6 ppb	6 ppb
Muonium position (z)	1 mm	< 1 Hz	0.2 ppb	2 ppb
Beamline	10(e-4)	< 1 Hz	0.2 ppb	2 ppb
Detector pile-up		2.5 Hz 0.3 Hz	0.5 ppb < 0.1 ppb	3 ppb < 1 ppb

Summary and Next Step

- Present total systematic error roughly estimated as

HFS	2.4 ppb
Magnetic moment	27 ppb
- RF power, stability and homogeneity:
 - need more study!
- Stability and homogeneity of magnetic field:
 - need magnetic shield around the magnet.
 - demonstration using a magnet at KEK.
- Beam test (without magnetic field) at MUSE D2 Area.
 - Gas chamber, cavity, beam profile monitor, ...

MuSEUM Collaborators



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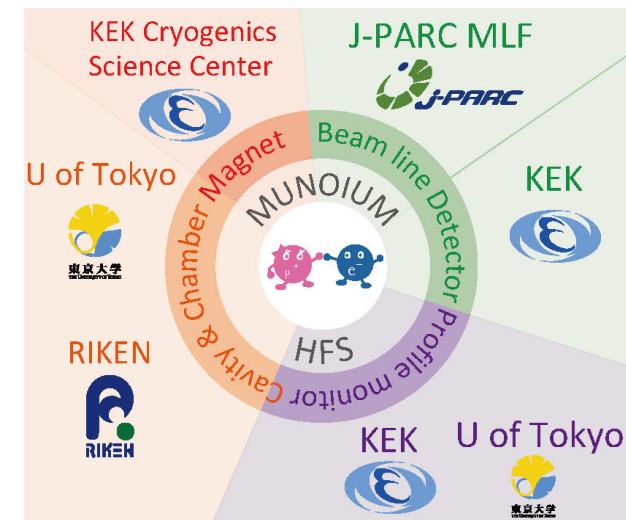
D. Kawall

Osaka University

M. Aoki

University of Yamanashi

E. Torikai



Extra Slides

Close relationship to $g_\mu - 2$

$$a_\mu = (g_\mu - 2)/2$$

Exp.

0.001 165 920 89 (68)
[580 ppb]



3.2 σ

The.

0.001 165 918 28 (49)
[420 ppb]

$$a_\mu = R/(\lambda - R)$$

$R_{\text{exp}}(g_\mu - 2)$: 500 ppb

$\lambda_{\text{exp}}(\text{MuHFS})$: 120 ppb

Test of CPT and Lorentz Invariance

CPT broken Theory \Rightarrow Lorentz symmetry is broken

O.W. Greenberg, Phys. Rev. Lett. 89 (2002) 231602

CPT violation search

Ex., Muon difference $g_{\mu^+} / g_{\mu^-} - 10^{-8}$

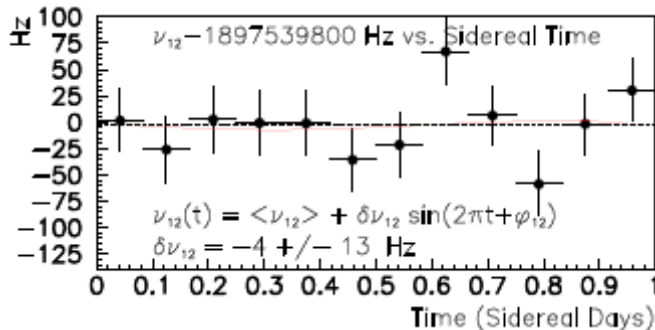
$g_{\mu^-} - 2/\text{MuHFS}$ precise measurement

Lorentz symmetry violating term in STE Lagrangian b

Corresponding MuHFS $\Delta\nu_{12/34}$

These value might change in sidereal time (23h56m)

$$\tilde{b}_3^\mu / \pi = -\delta\Delta\nu_{12} = \delta\Delta\nu_{34}$$



LAMPF Exp. Figure of Merit

$$2\sqrt{(b^{\mu^+}_X)^2 + (b^{\mu^+}_Y)^2} / m_\mu < 5 \times 10^{-22}$$

$$m_\mu / M_P \sim 10^{-20}$$

Planck scale sensitivity