

Muon Acceleration: NuMAX and Beyond

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NuFact 2014
Glasgow, Scotland

August 25-30, 2014



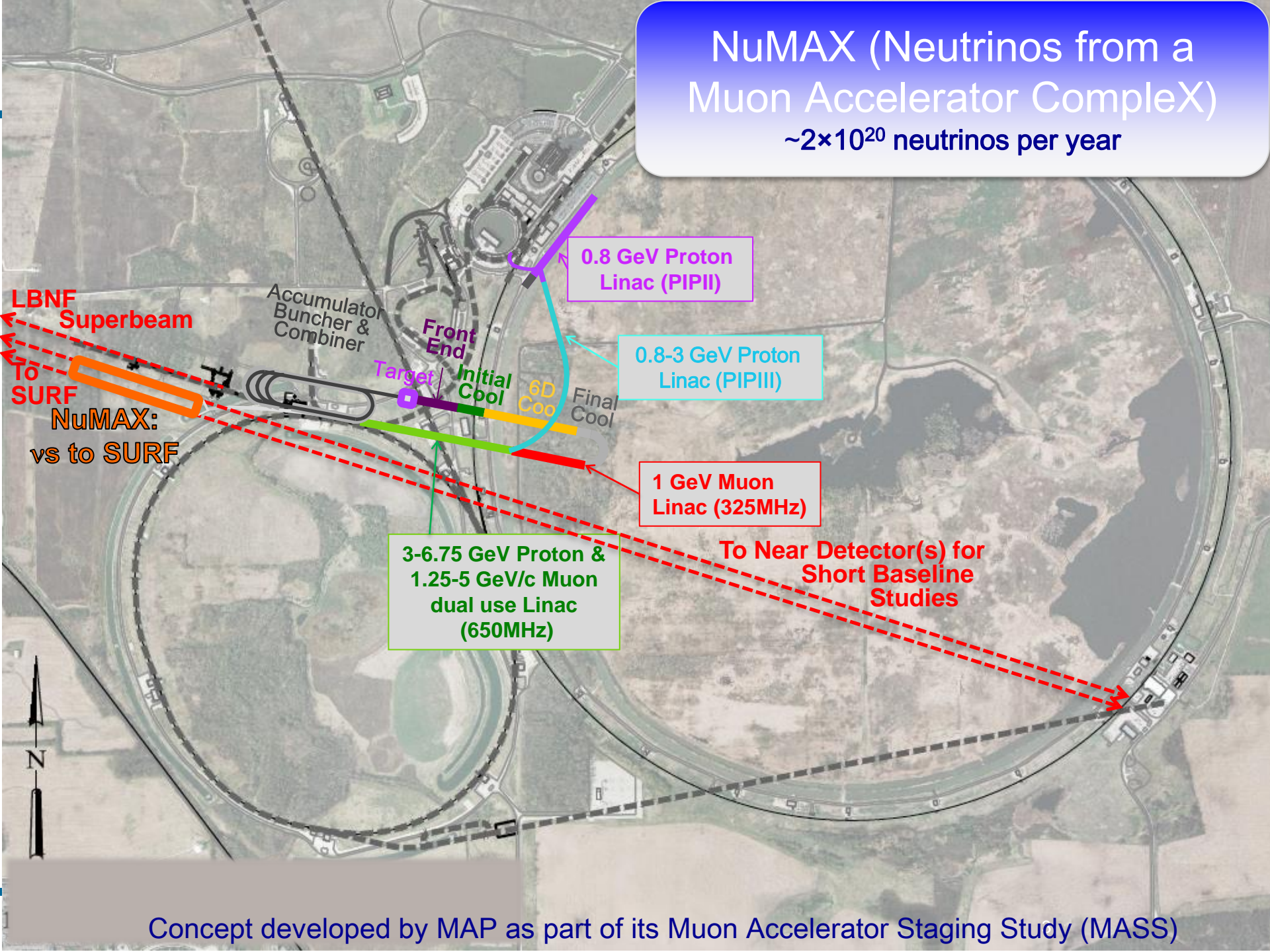
University
of Glasgow

Overview

- Develop cost effective concepts for acceleration of muon beams for a post-LBNF Neutrino Factory and beyond...
 - Exploration of dual-use (H^- and muon) linac concepts and other efficient acceleration options for muons alone.
 - Reducing the cost while maintaining performance through proper balance between the cooling systems (4D/6D) and the acceptance of the acceleration complex (transverse/longitudinal).
 - Exploring efficient acceleration beyond 5 GeV via RLAs (Higgs Factory).
- The main thrust is to explore the means to make the muon complex at Fermilab affordable in the future.
- Significant groundwork was already laid by the IDS-NF efforts and by MAP.

NuMAX (Neutrinos from a Muon Accelerator CompleX)

$\sim 2 \times 10^{20}$ neutrinos per year



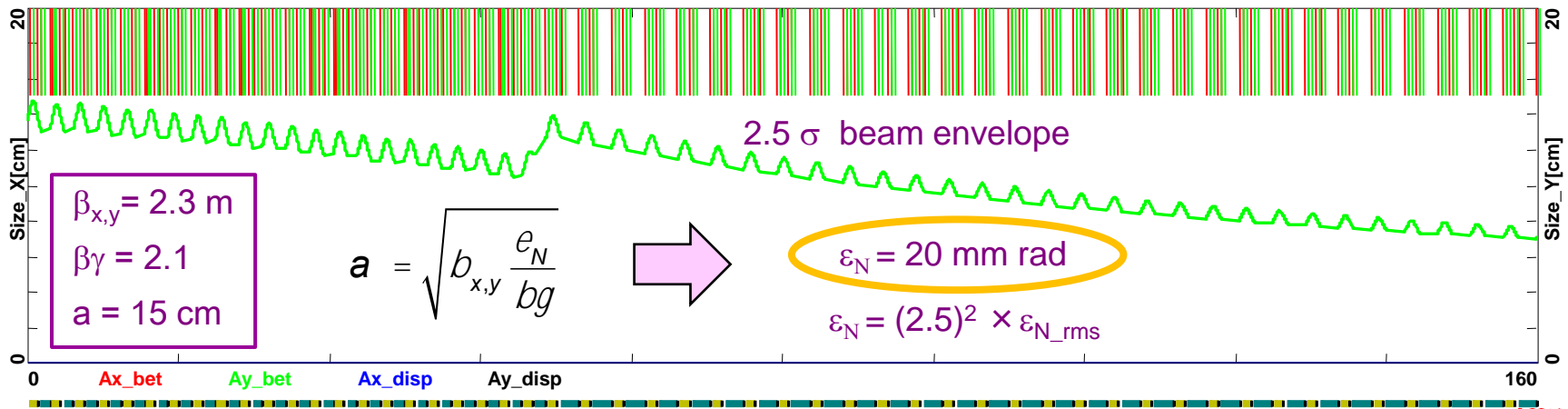
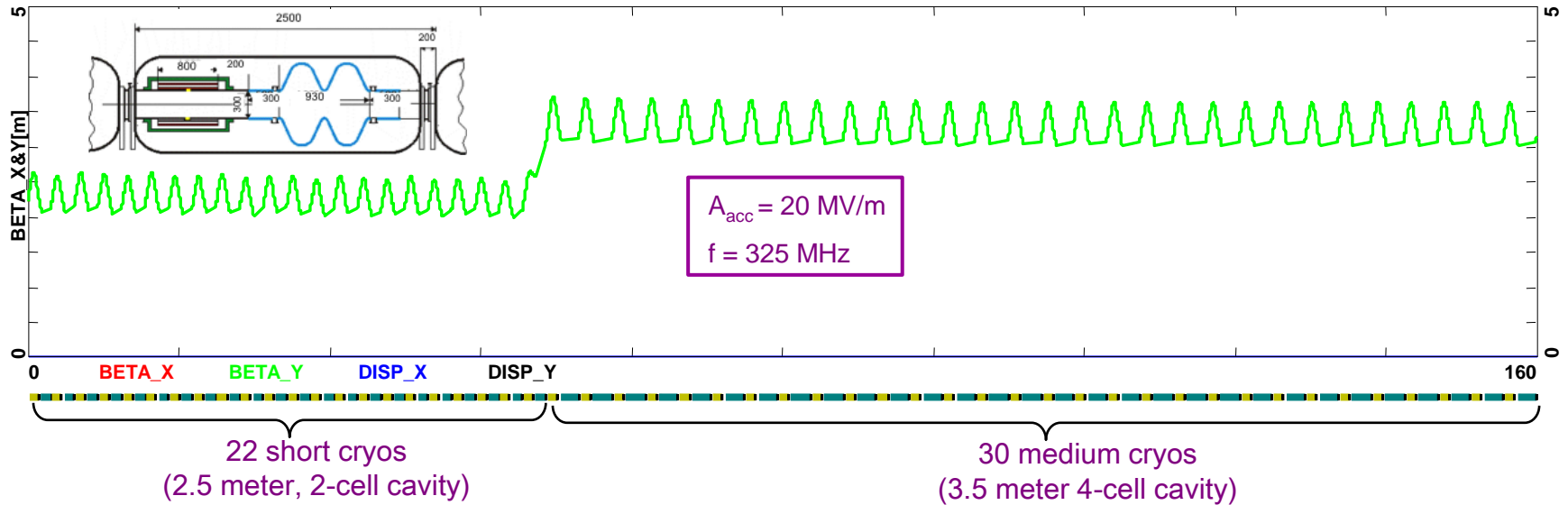
Concept developed by MAP as part of its Muon Accelerator Staging Study (MASS)

Initial 325 MHz Linac – Transverse Acceptance

$p = 255 \text{ MeV}/c$

beta functions

1250 MeV

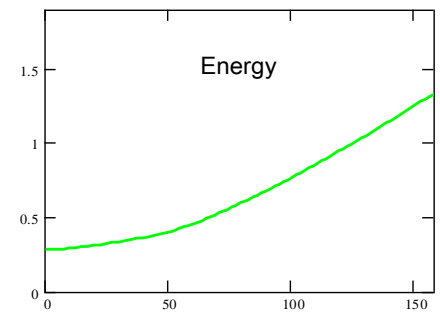
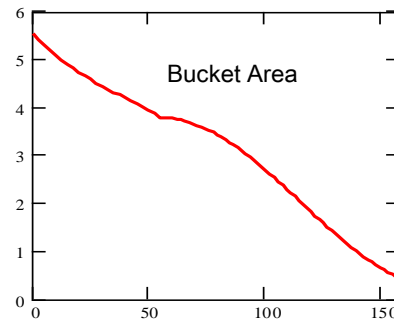
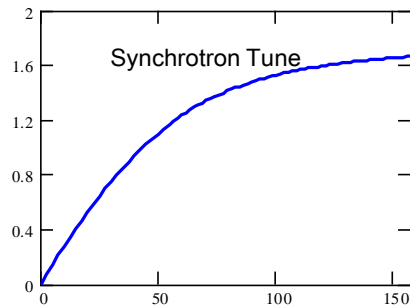
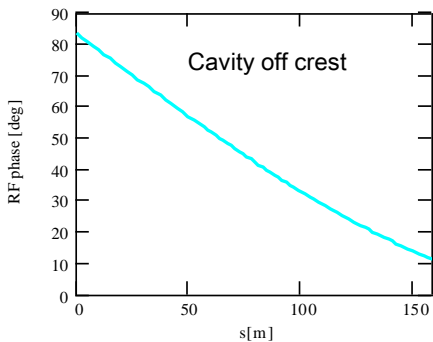
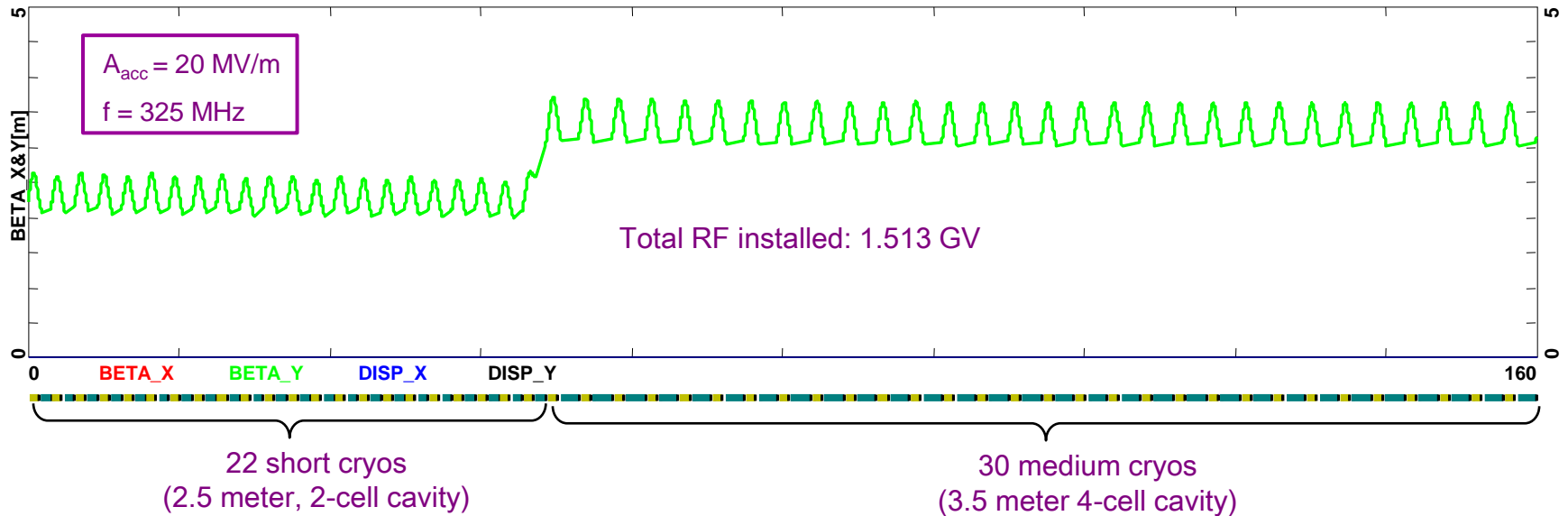


Initial Linac – Longitudinal Profile

$p = 255 \text{ MeV}/c$

1250 MeV

beta functions

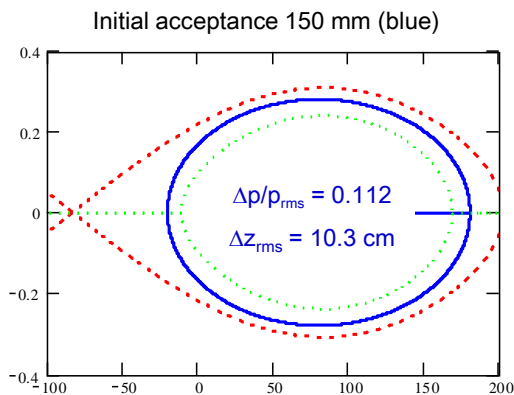
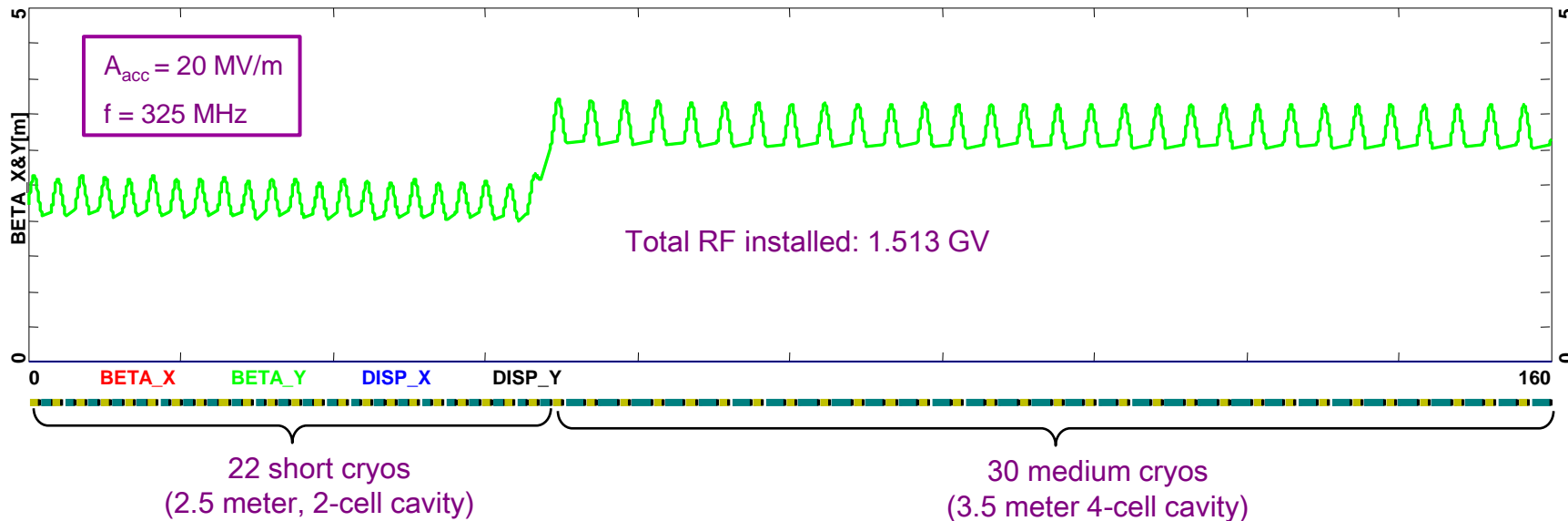


Initial Linac – Longitudinal Acceptance

$p = 255 \text{ MeV}/c$

beta functions

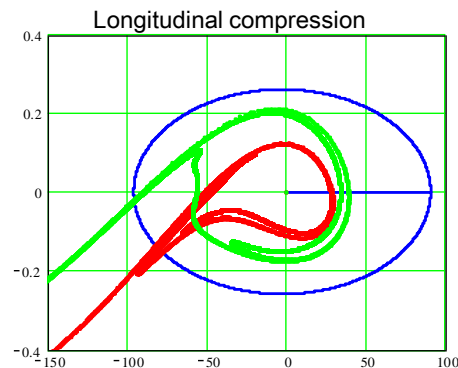
1250 MeV



Longitudinal acceptance

$$\epsilon_{\text{Long}} = 150 \text{ mm}$$

$$\epsilon_{\text{Long}} = (2.5)^2 \times \epsilon_{\text{Long_rms}}$$

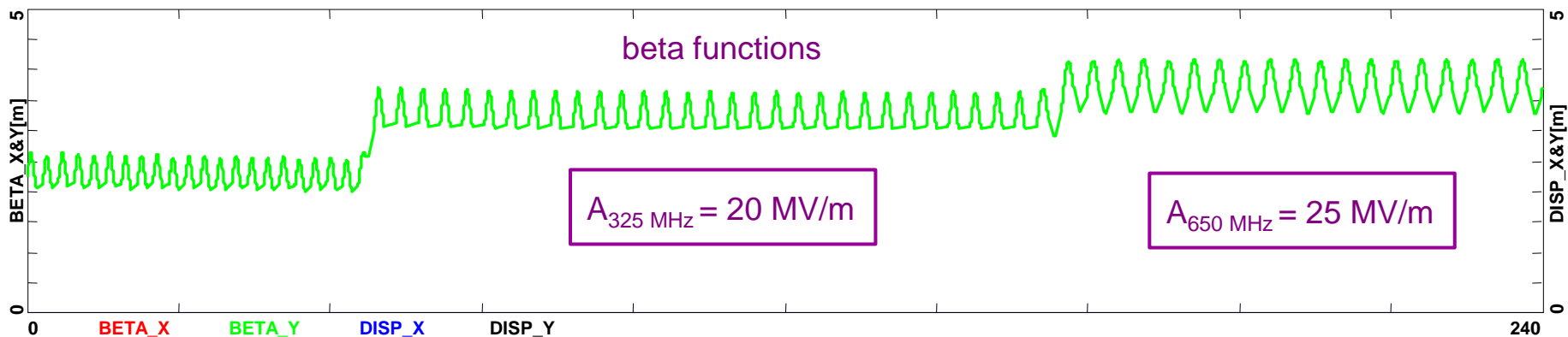


325 MHz – 650 MHz Linac

p = 255 MeV/c

1.25 GeV

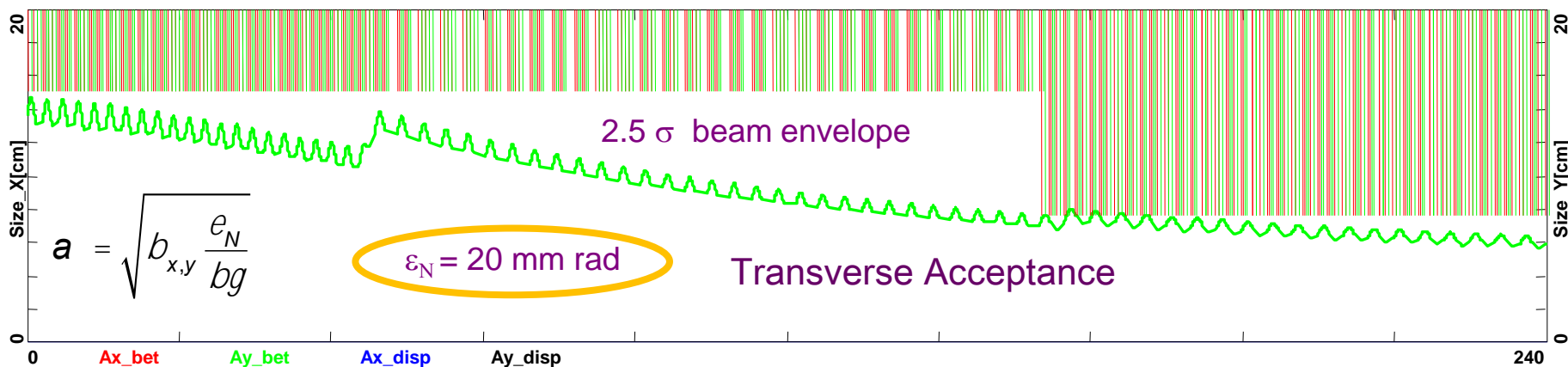
2.25 GeV



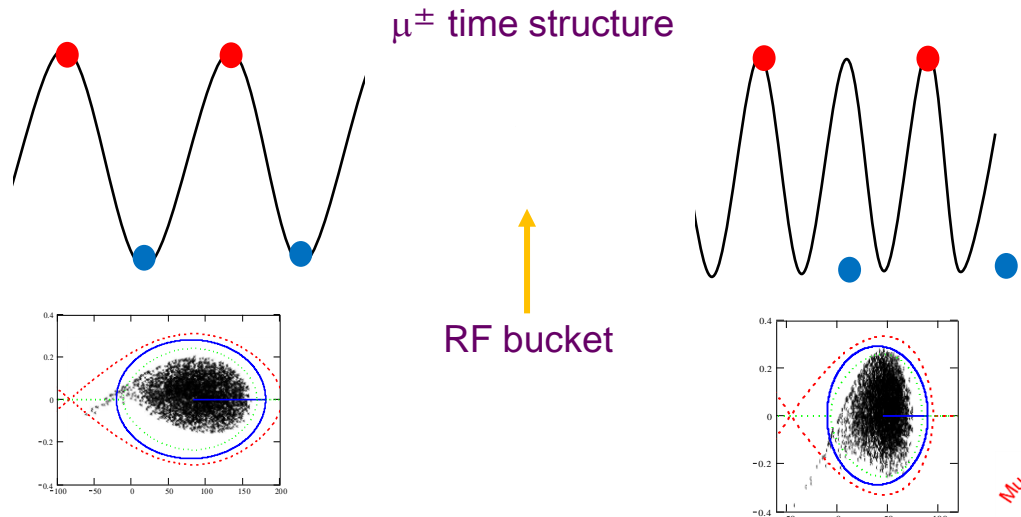
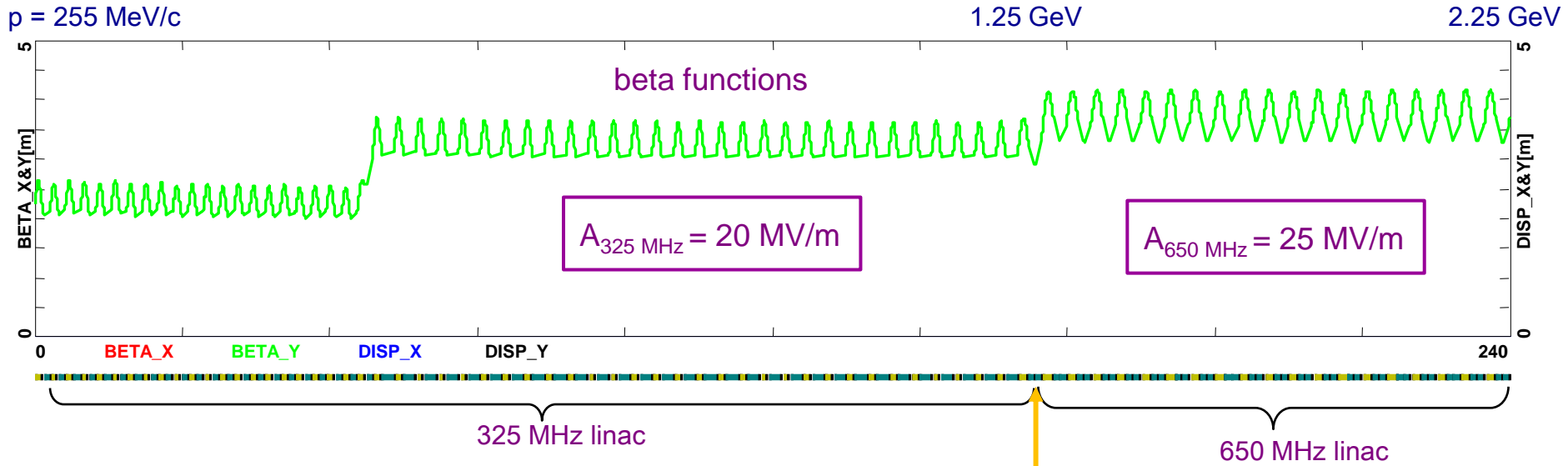
22 short cryos (2.5 meter)
325 MHz, 2-cell cavity

30 medium cryos (3.5 meter)
325 MHz, 4-cell cavity

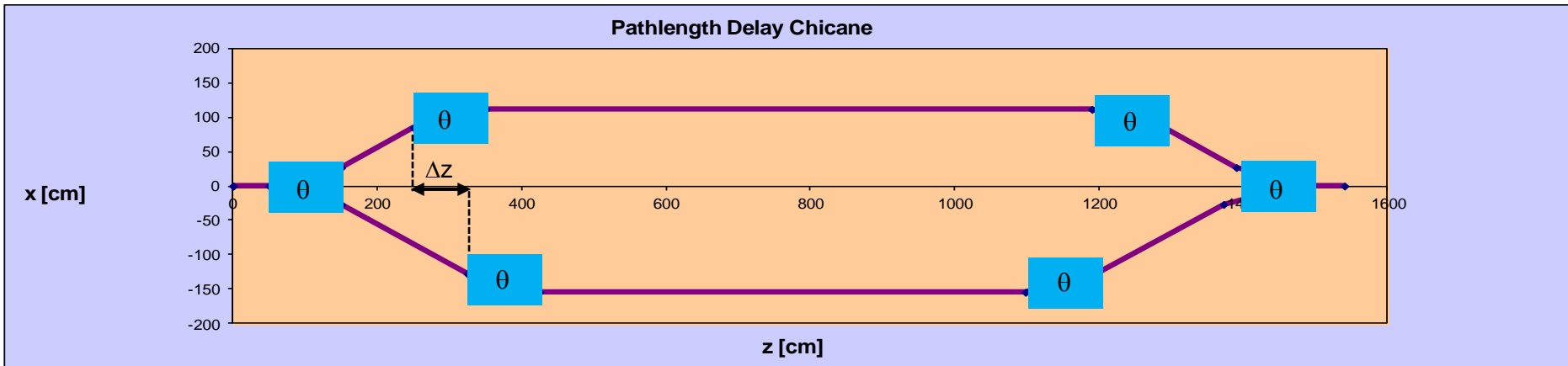
20 long cryos (4 meter)
650 MHz, 2 × 4-cell cavity



325 MHz – 650 MHz Transition



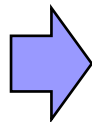
Path-length Delay Chicane



$$\Delta S = 2 \times \Delta z \frac{1 - \cos \theta}{\cos \theta}$$

$$\Delta S = \frac{\lambda}{2}$$

$$\Delta z = \frac{\lambda}{4} \times \frac{\cos \theta}{1 - \cos \theta}$$



$$\lambda = 46.122 \text{ cm}$$

$$\theta = 30^\circ$$

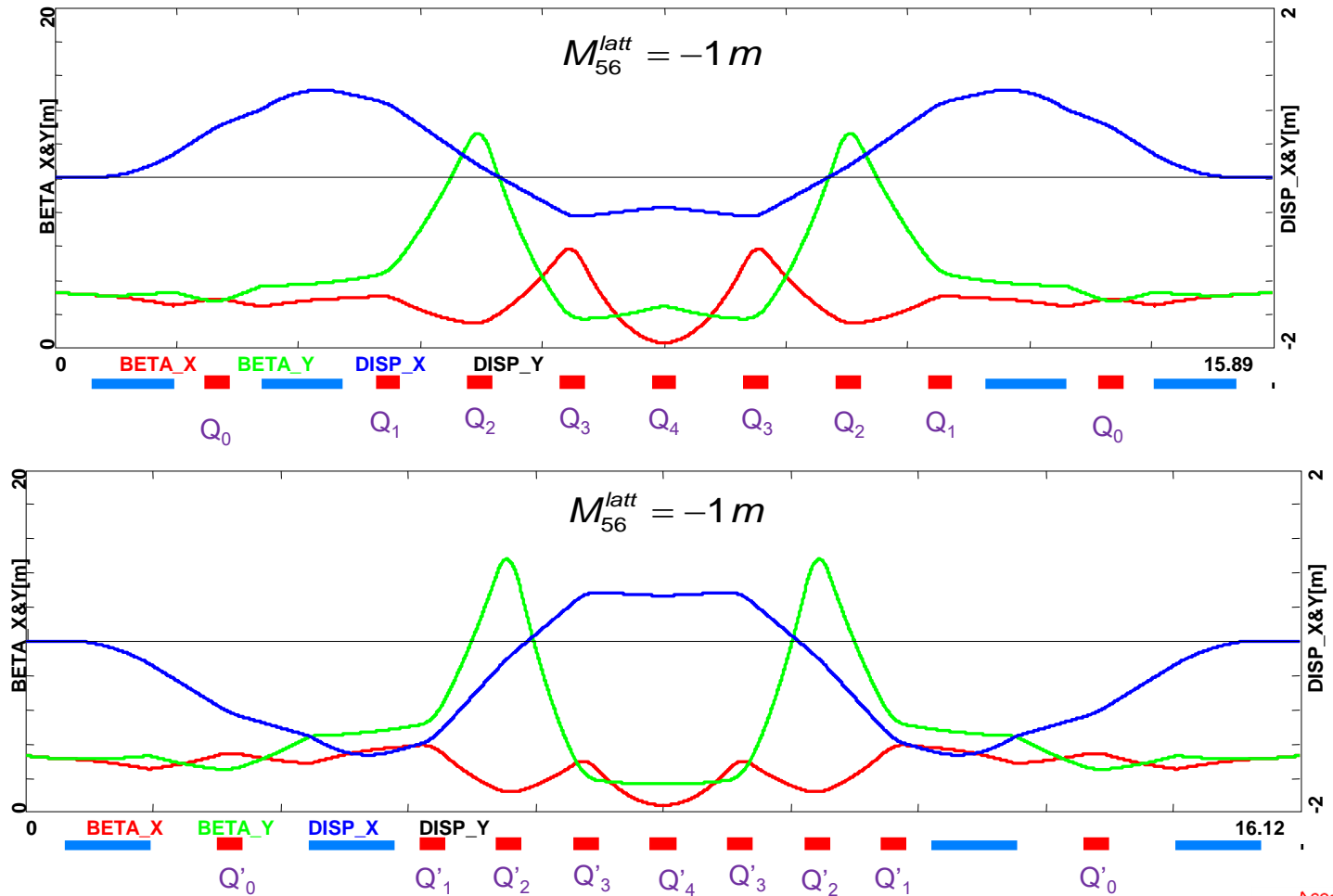
$$\Delta z = 74.534 \text{ cm}$$

$$\frac{\cos \theta}{1 - \cos \theta} = \frac{1}{2} \left(\cotan^2 \frac{\theta}{2} - 1 \right)$$

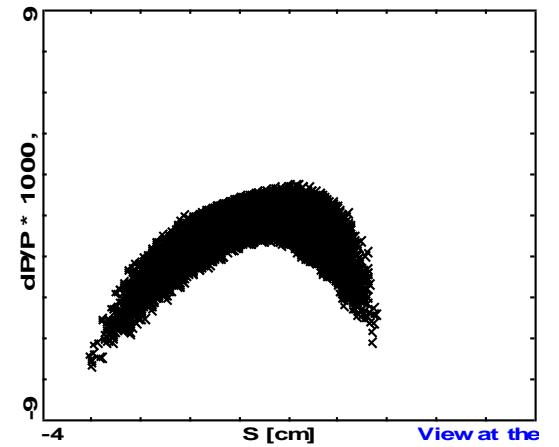
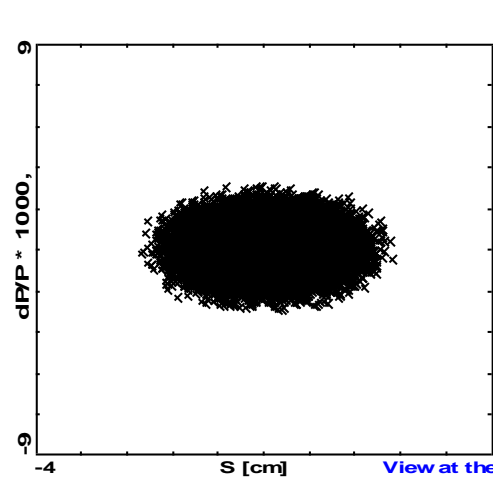
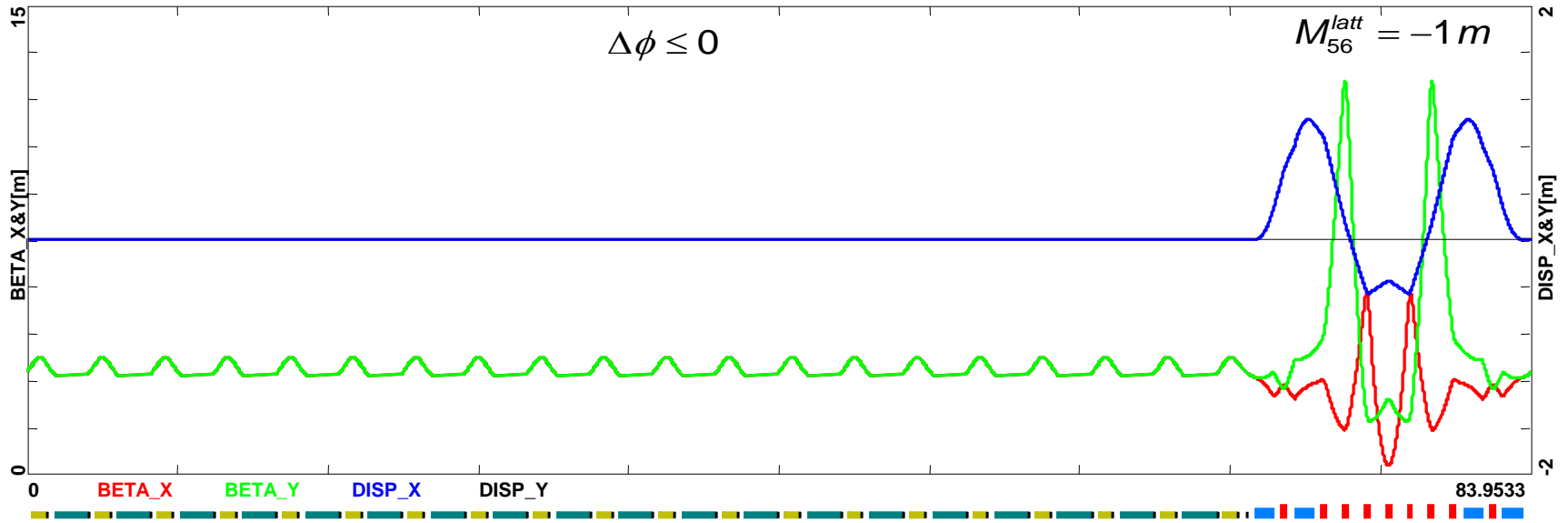
Delay/Compression Chicane – Optics

5 free parameters needed to match: 2 betas + 2 alphas + disp.

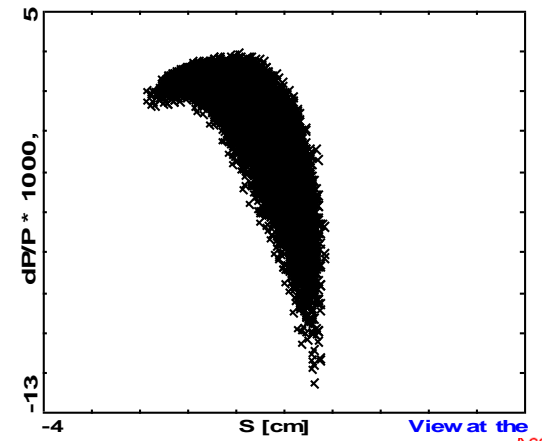
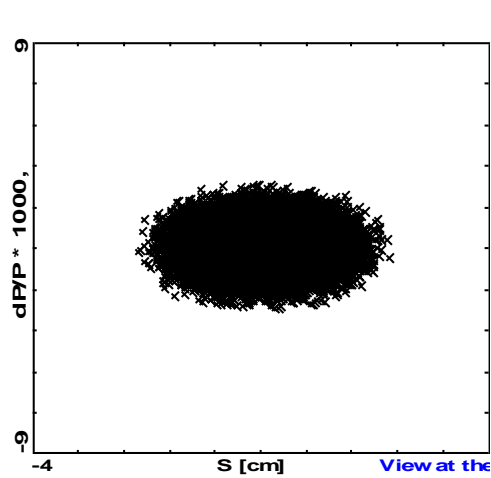
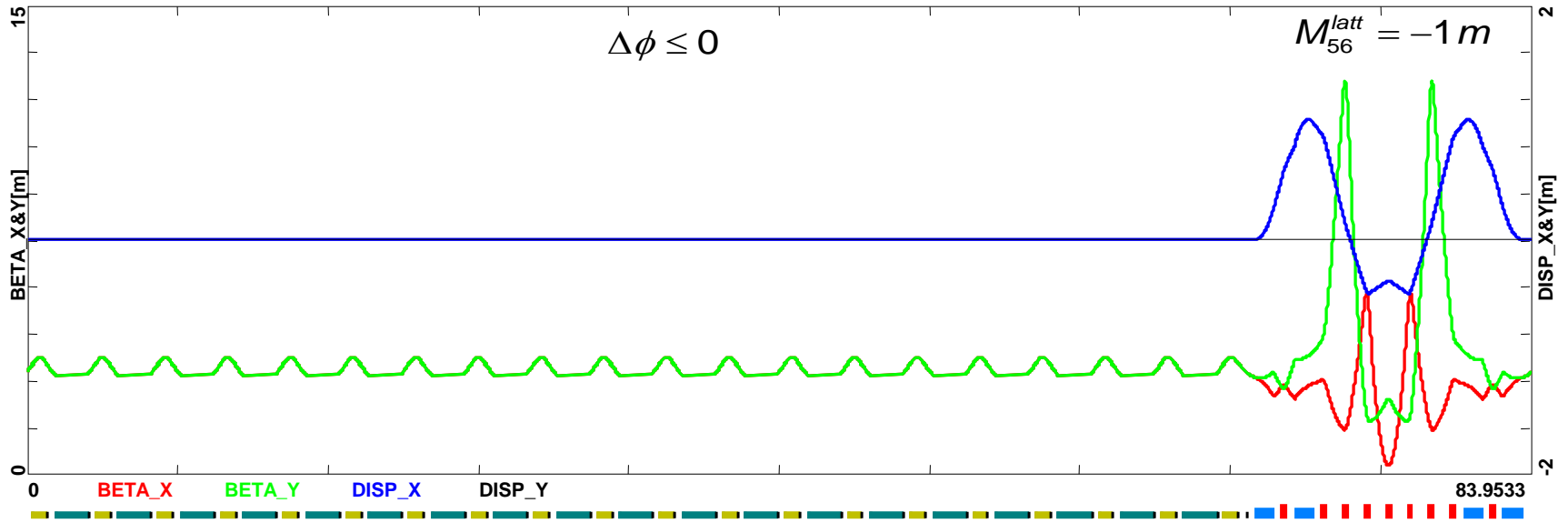
$$M_{56} = \int \left(\frac{1}{\gamma^2} - \frac{D}{\rho} \right) ds$$



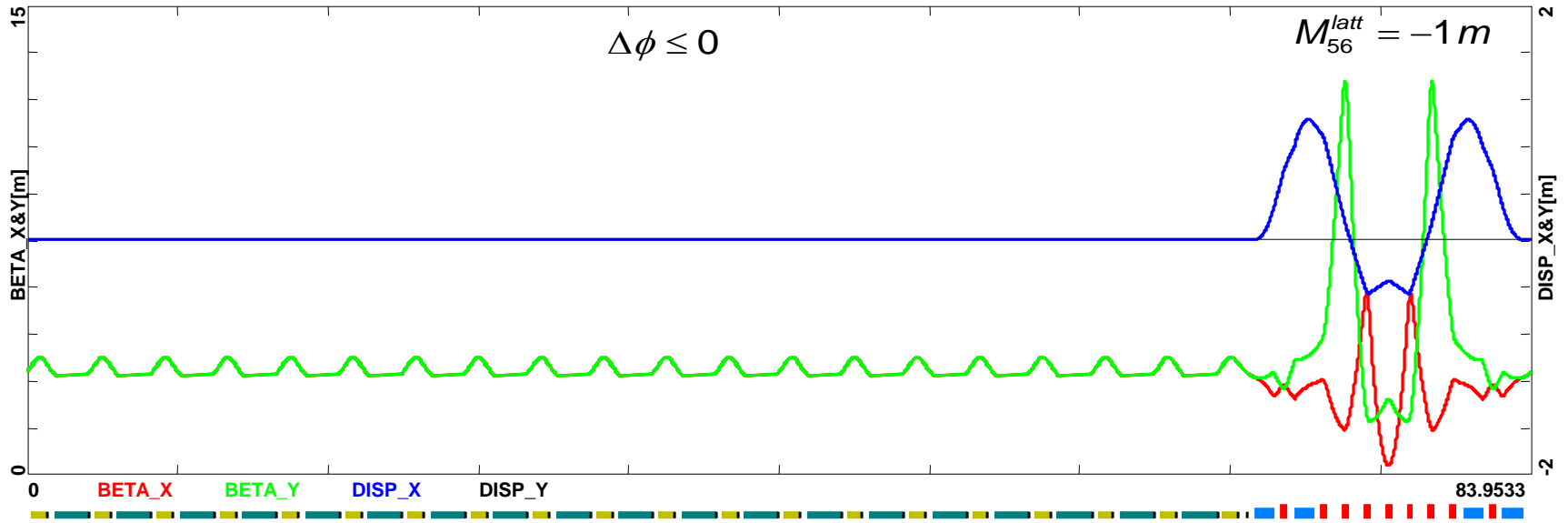
Longitudinal Compression with M_{56}



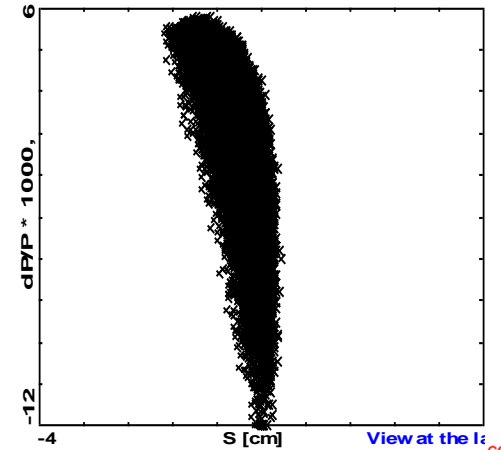
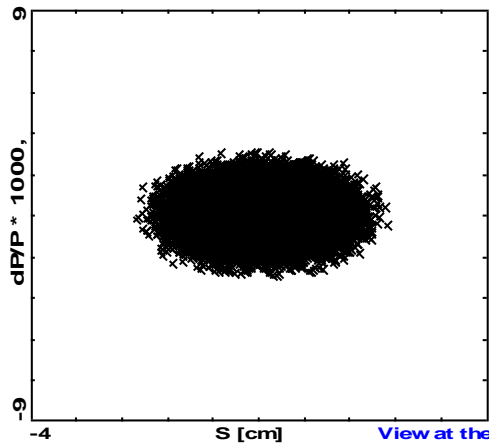
Longitudinal Compression with M_{56}



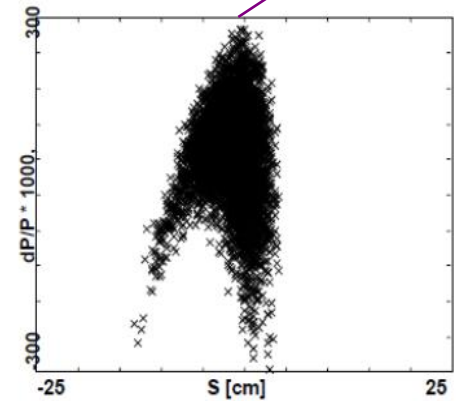
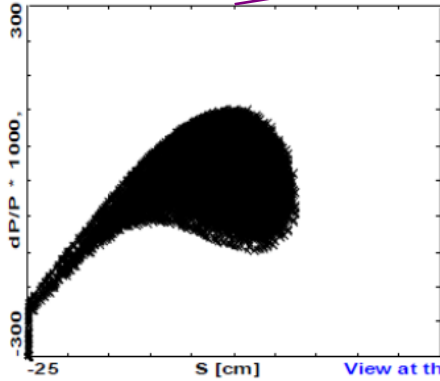
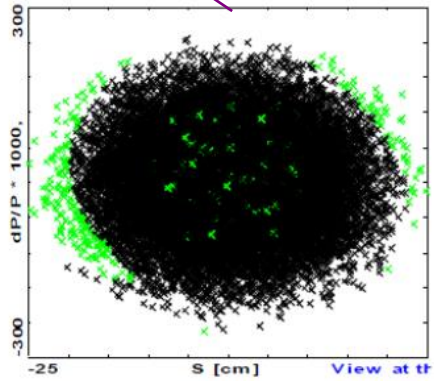
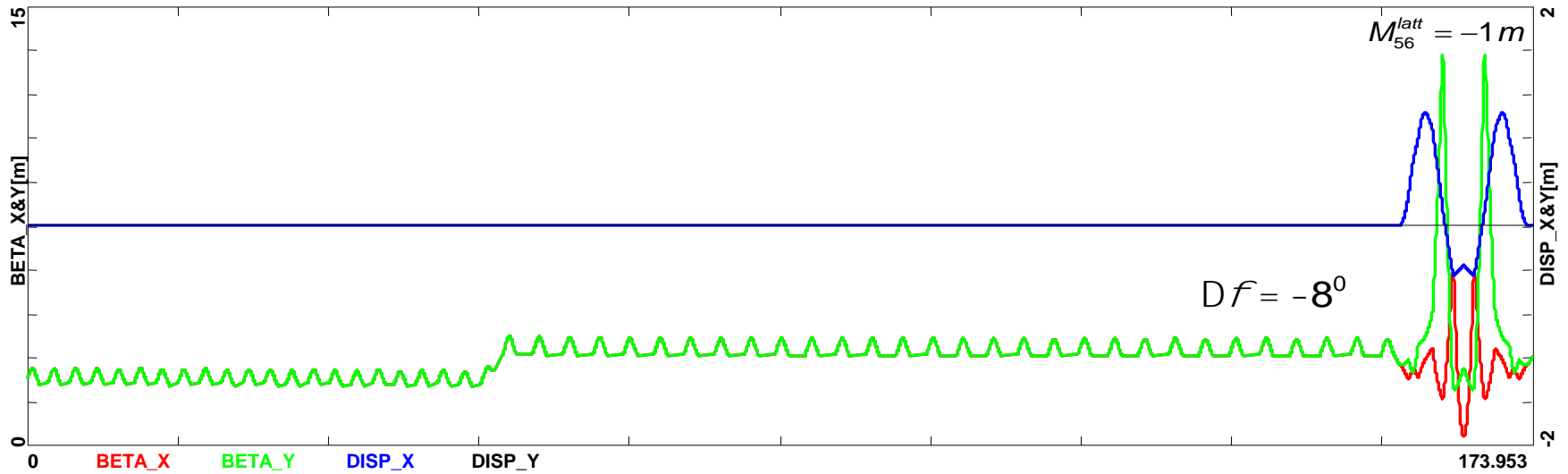
Longitudinal Compression with M_{56}



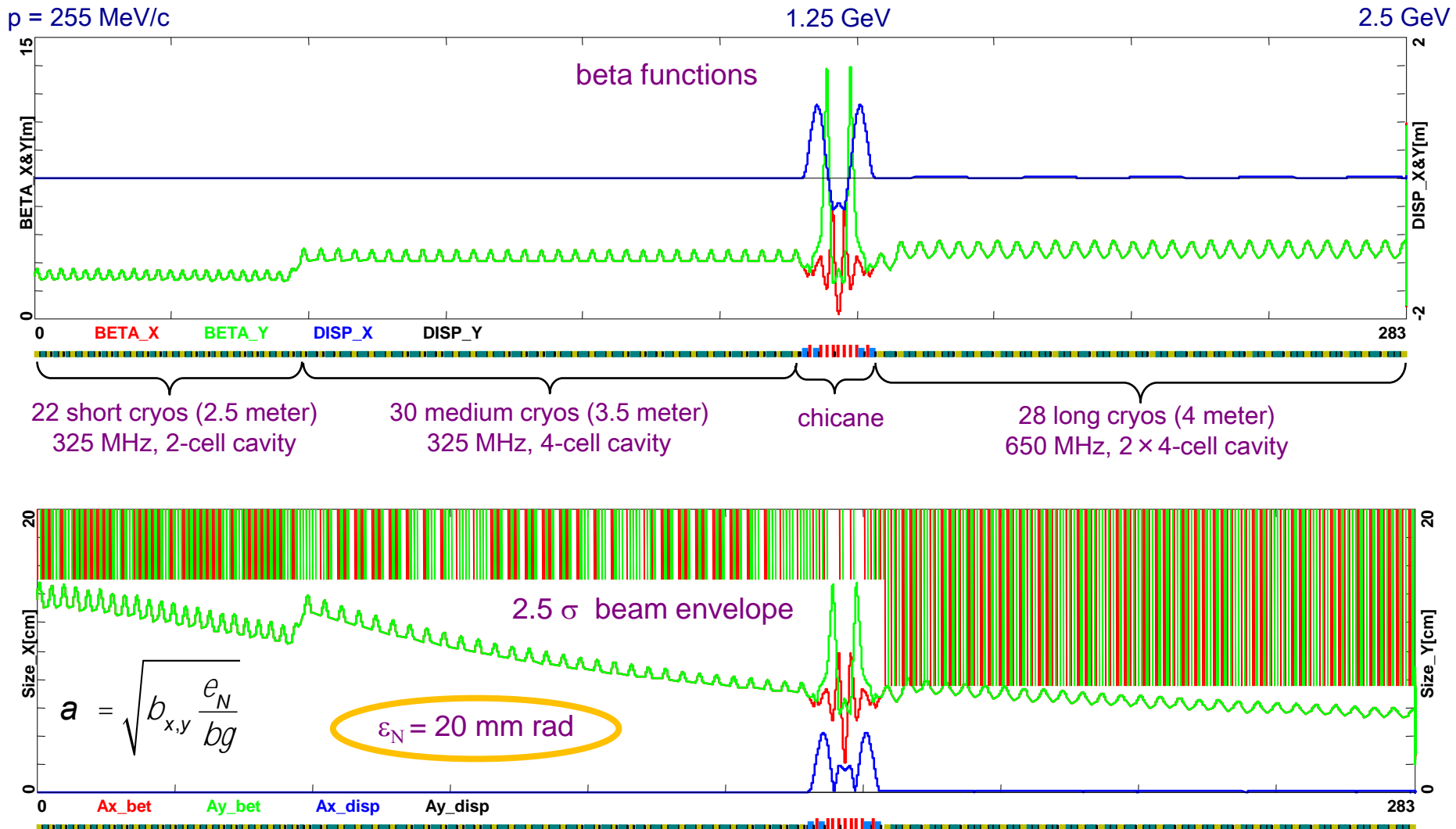
$\Delta\phi = -8^\circ$



Longitudinal Compression with $M_{56}^{latt} = -1 m$



325 MHz – 650 MHz Linac

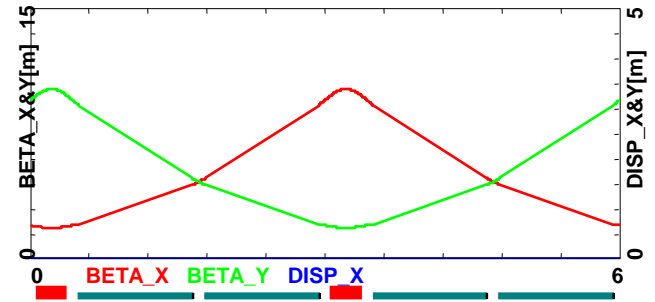
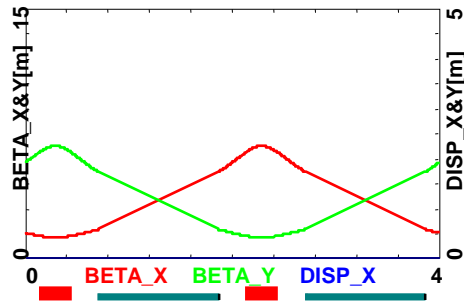
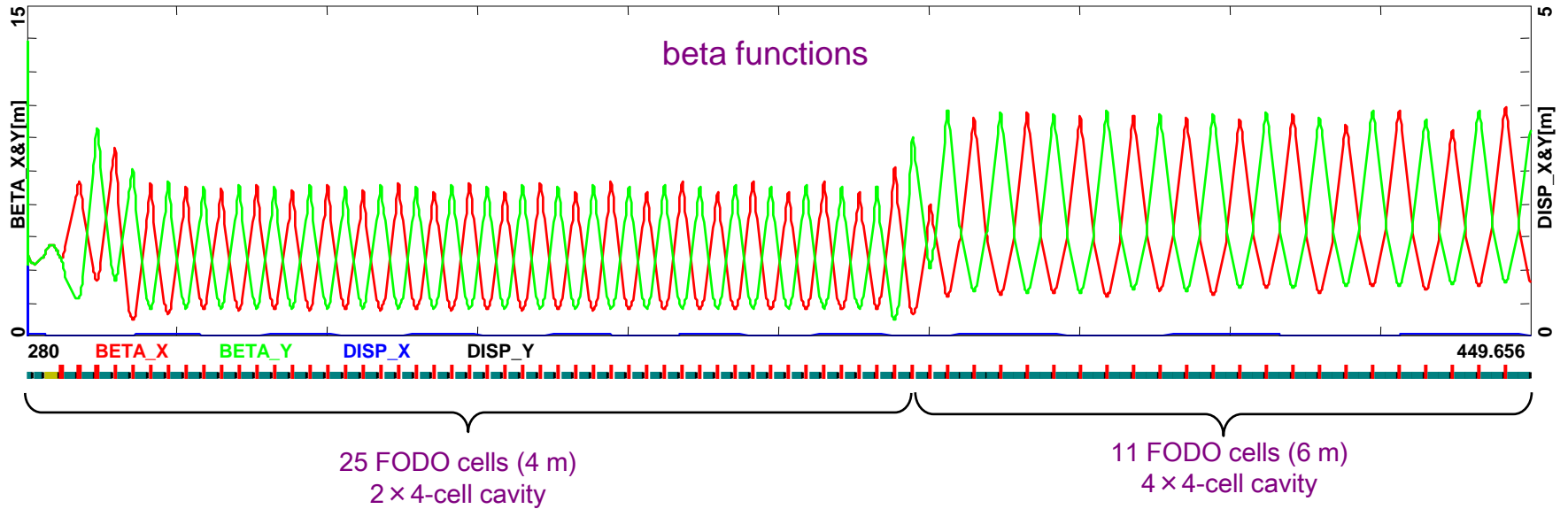


650 MHz FODO Linac

2.5 GeV

3.8 GeV

5 GeV

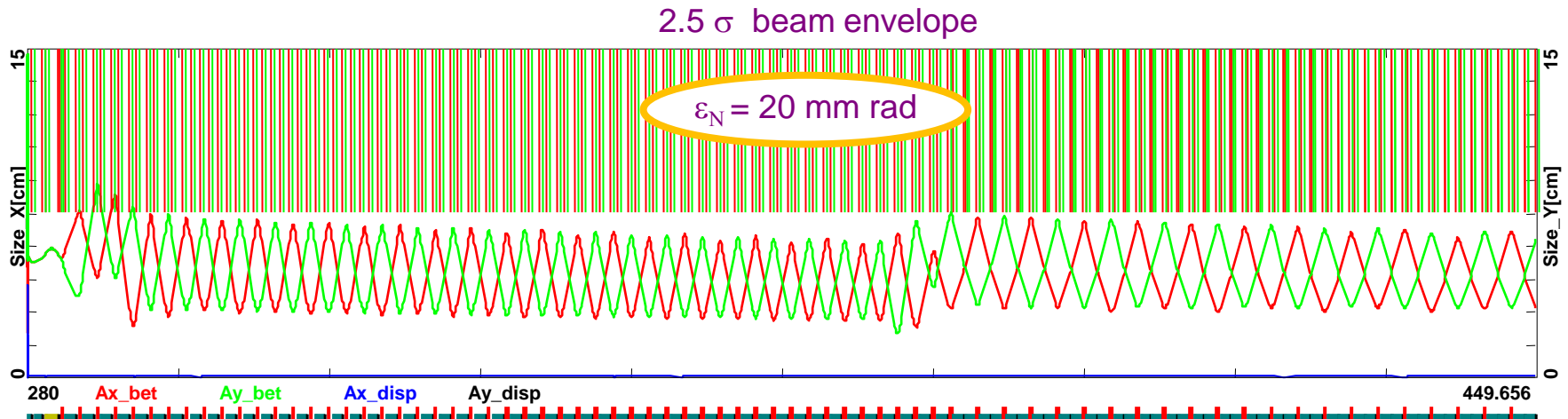
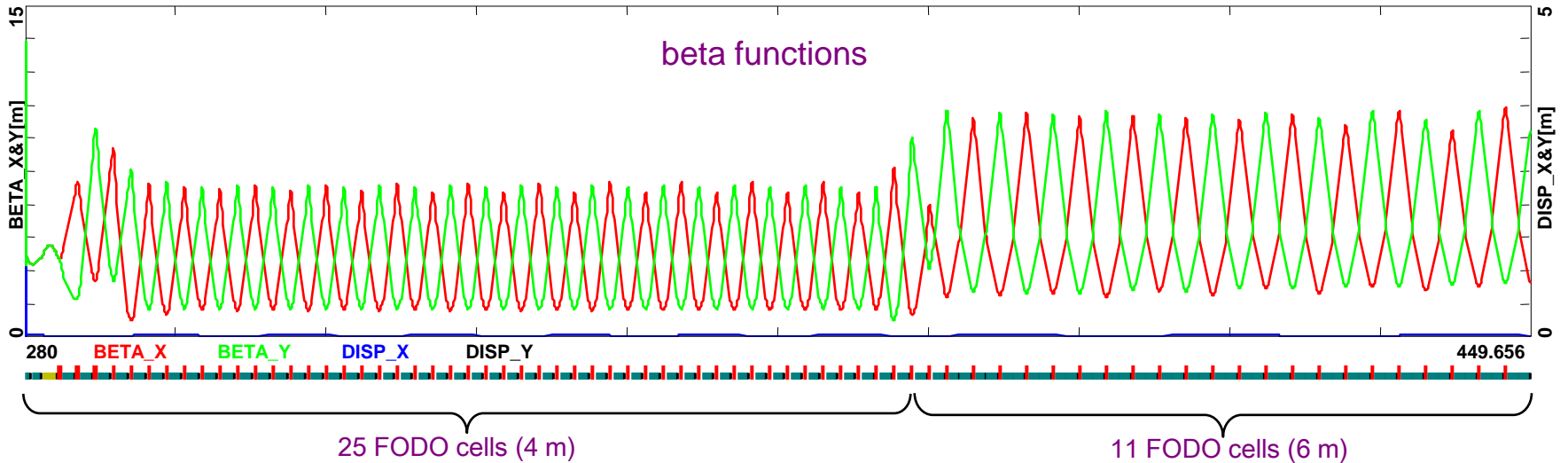


650 MHz FODO Linac

2.5 GeV

3.8 GeV

5 GeV



325 MHz – 650 MHz Linac

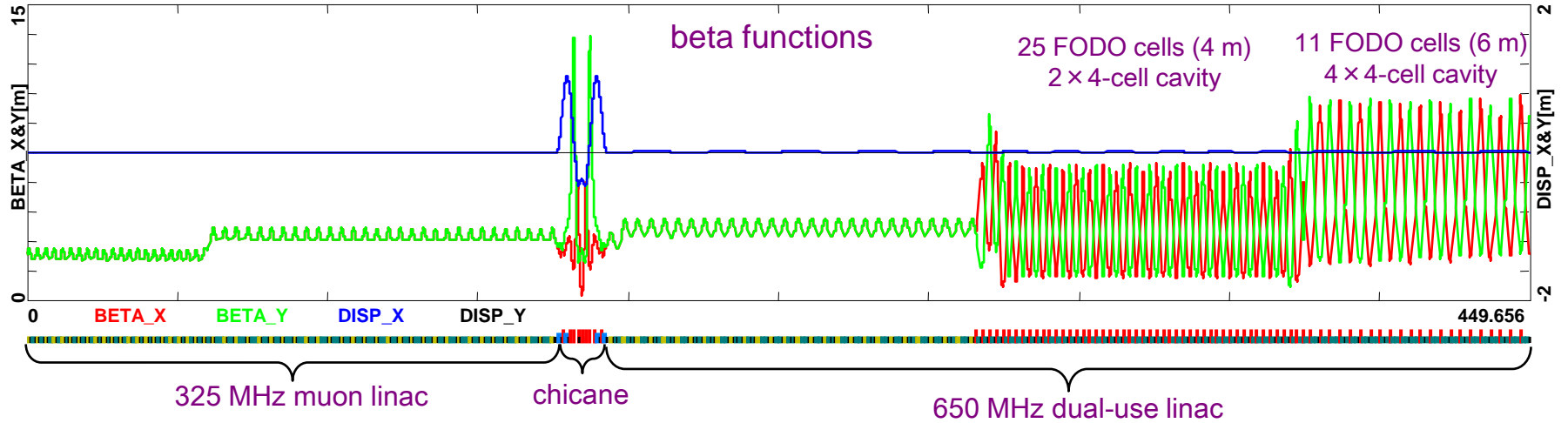
$p = 255 \text{ MeV}/c$

1.25 GeV

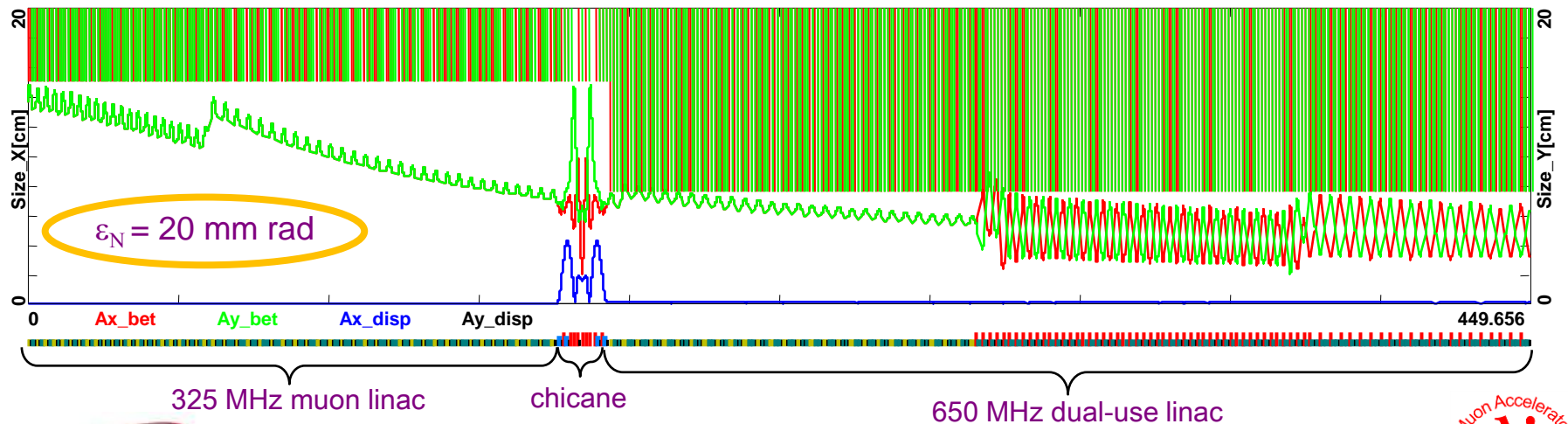
2.5 GeV

3.8 GeV

5 GeV



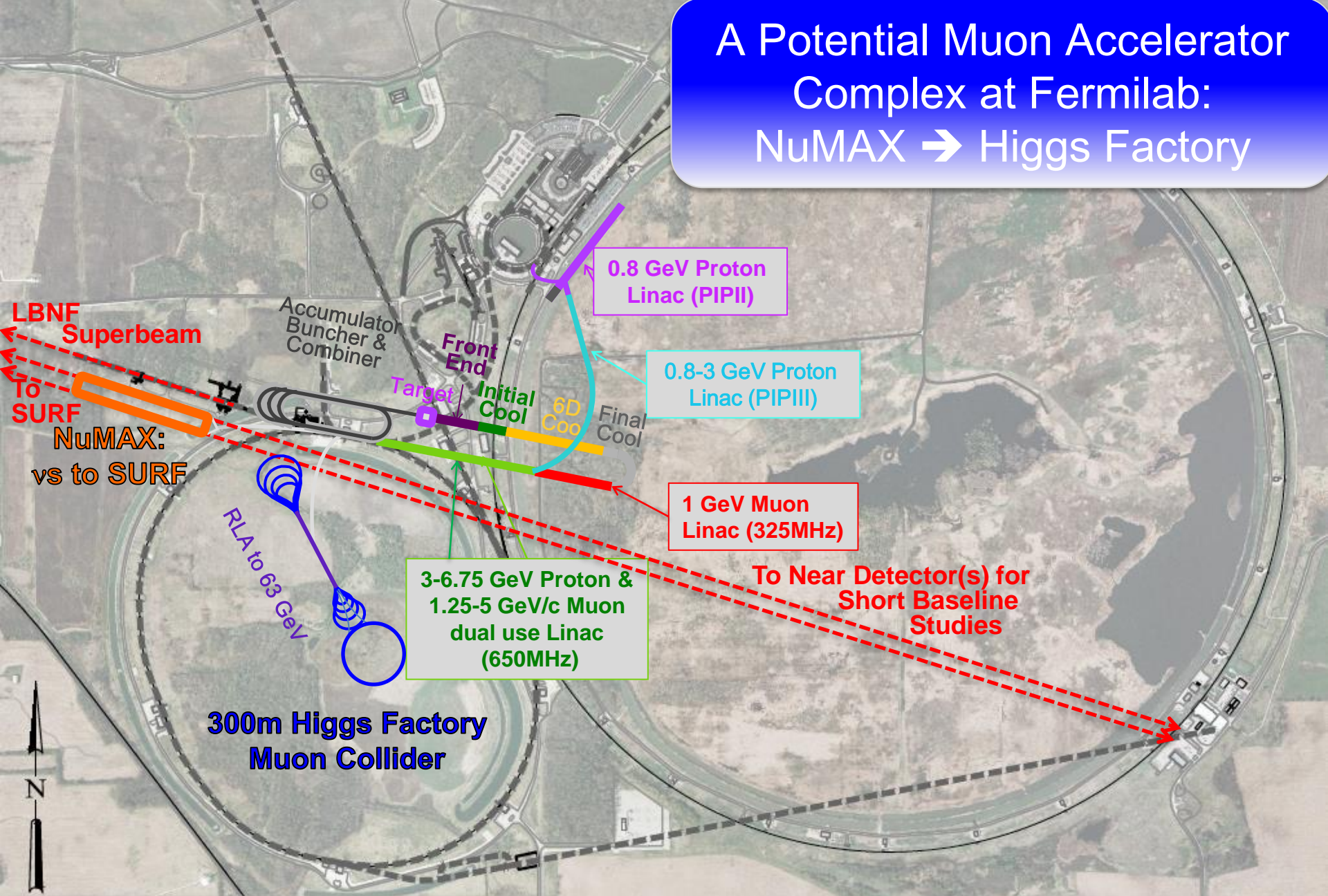
2.5 σ beam envelope



Compatibility with H⁻ Acceleration

- So far, the presented linac design was optimized for muon acceleration only.
 - We have developed a diverse modular linac structure composed of various style solenoid focusing FOFO cells and quadrupole based FODO cells.
- Further studies will follow to address compatibility with H⁻ acceleration. They will focus on:
 - H⁻ injection into the linac (effect of a chicane bend on ion stripping)
 - H⁻ betatron matching into the linac
 - H⁻ dynamics in a strongly focusing solenoid based FOFO channel
 - Different phase requirements for muon and H⁻ acceleration ⇒ cavity-by-cavity phase adjustment needs to be made to switch between species
- Depending on the results of the above H⁻ compatibility study, one will optimize the dual-use linac with appropriate combination of the developed lattice modules.

A Potential Muon Accelerator Complex at Fermilab: NuMAX → Higgs Factory



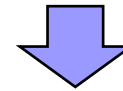
Beam Loading

J.S. Berg
J.-P. Delahaye

stored energy in a cavity: $\frac{V^2}{\omega(R/Q)}$

fractional reduction in the cavity voltage : $\frac{\Delta V}{V} = \frac{enN\omega(R/Q)\cos\phi}{V}$

RF gradient G defined as: $V = n_C G \pi c / \omega$



$$\frac{\Delta V}{V} = \frac{enN\omega^2[(R/Q)/n_C]\cos\phi}{\pi Gc}$$

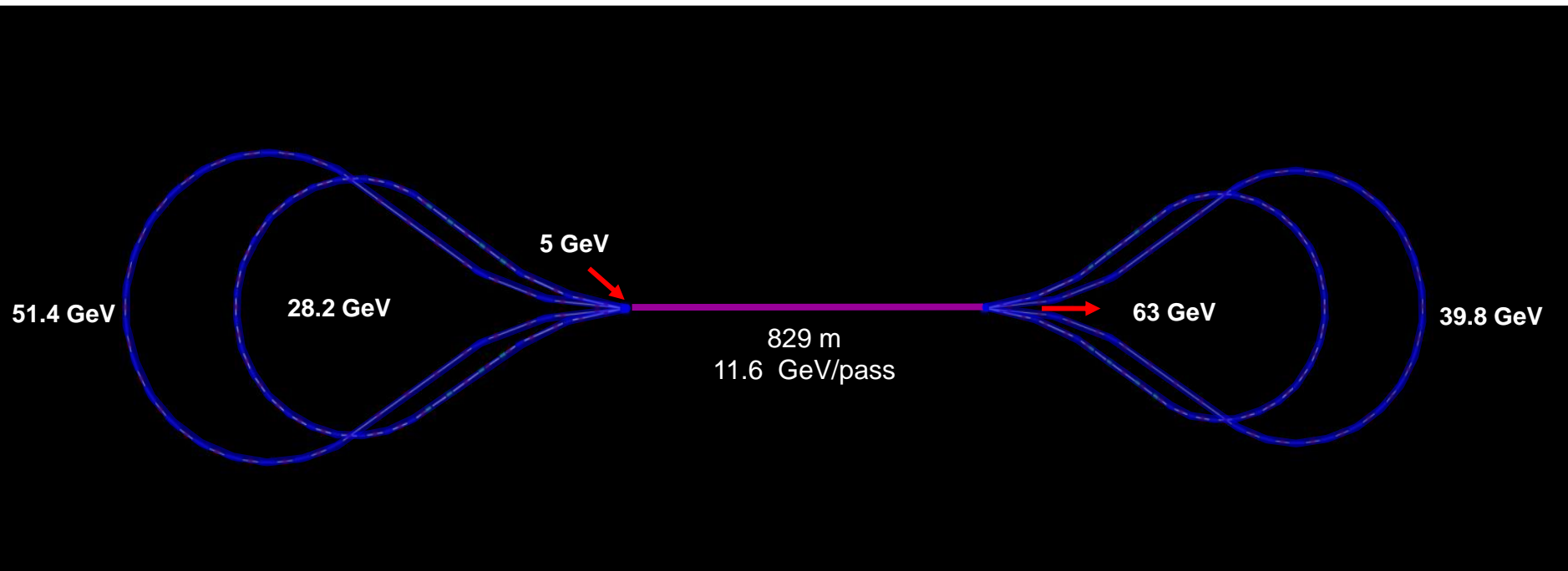
fractional voltage reduction:

$$(R/Q)/n_C = 114 \Omega$$

$$\phi = 0$$

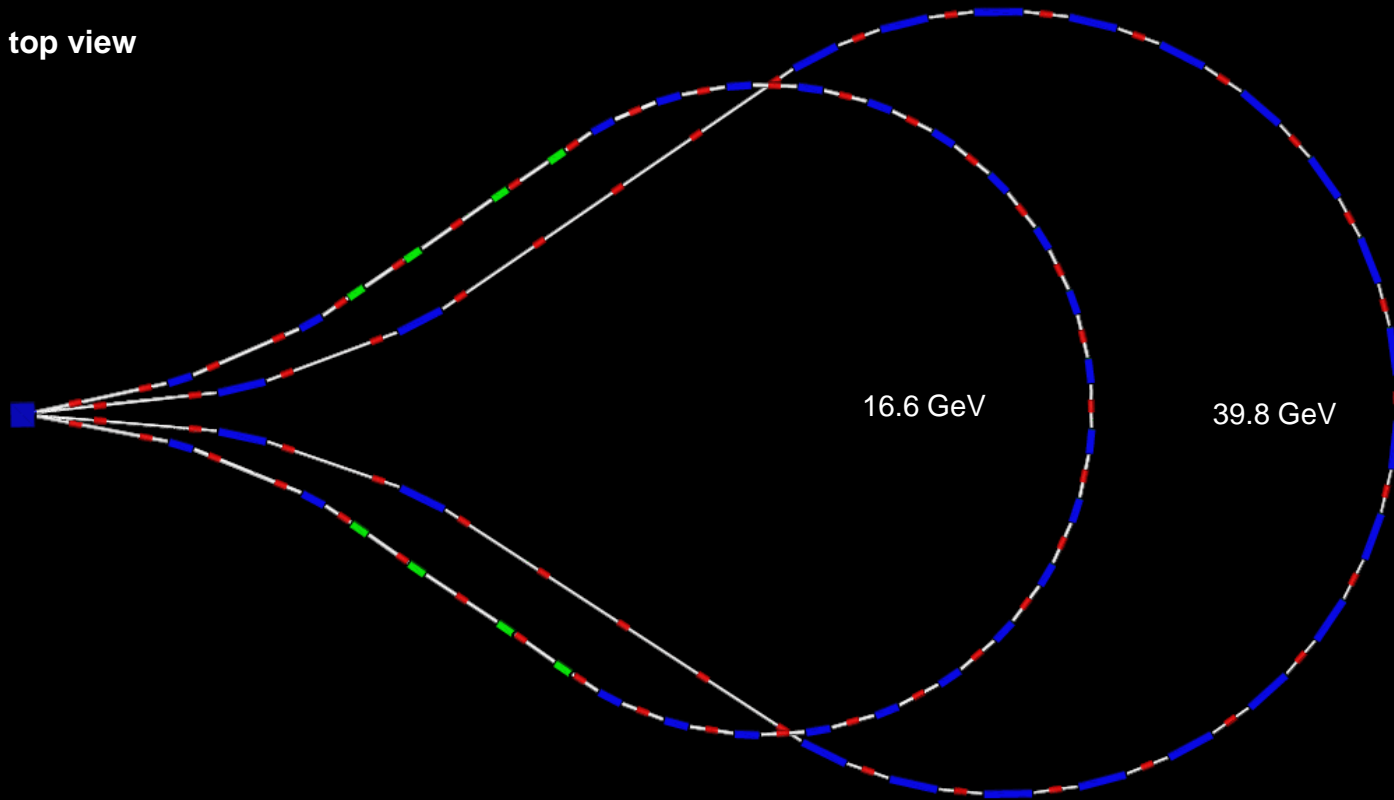
Particles	2×10^{12}	4×10^{12}	2×10^{12}	4×10^{12}
Frequency	325 MHz	325 MHz	650 MHz	650 MHz
Passes	Relative reduction (%)			
3	2	5	8	16
5	4	8	13	26
7	6	11	18	36
9	7	15	23	47

5-pass RLA 5–63 GeV

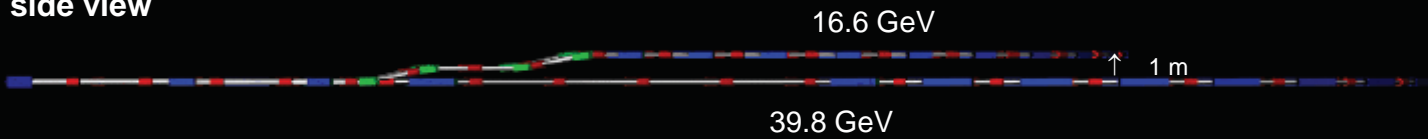


Arc 1 and Arc 3

top view

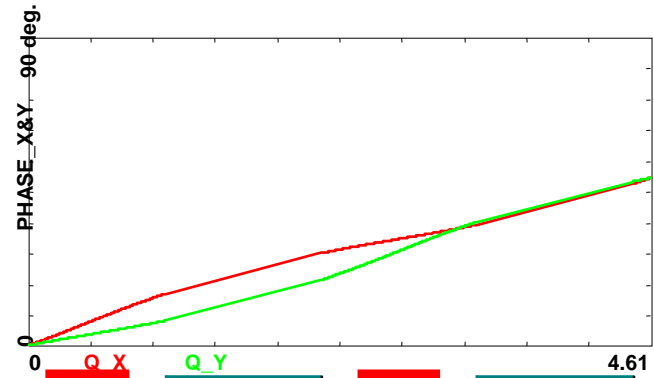
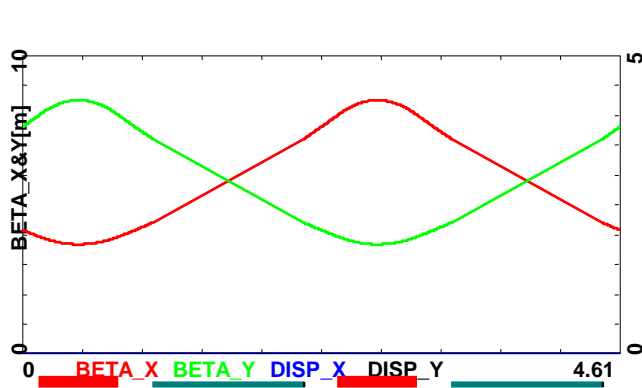
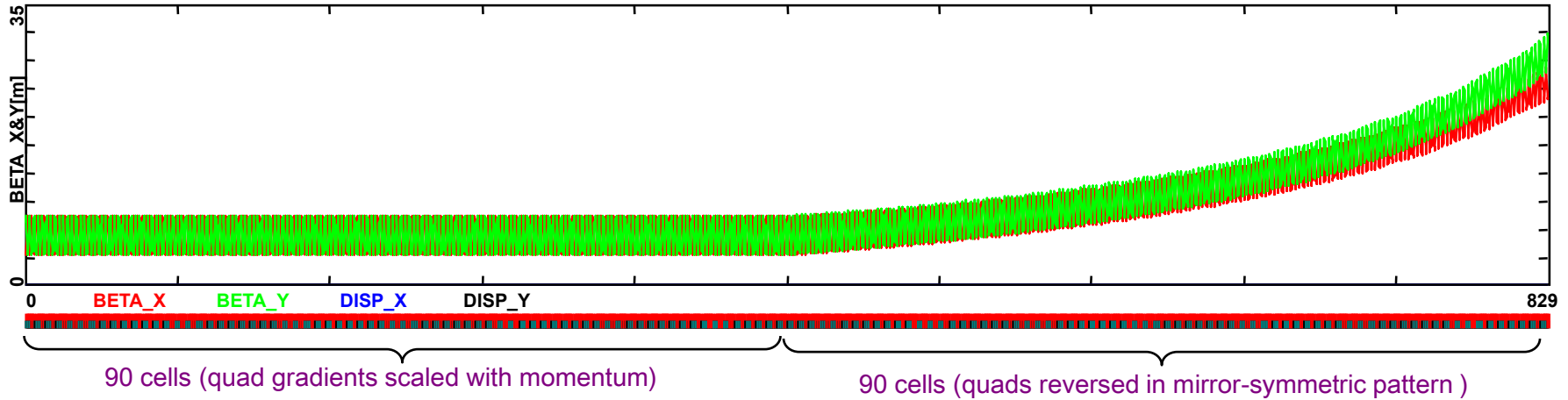


side view



Linac – Bisected Optics

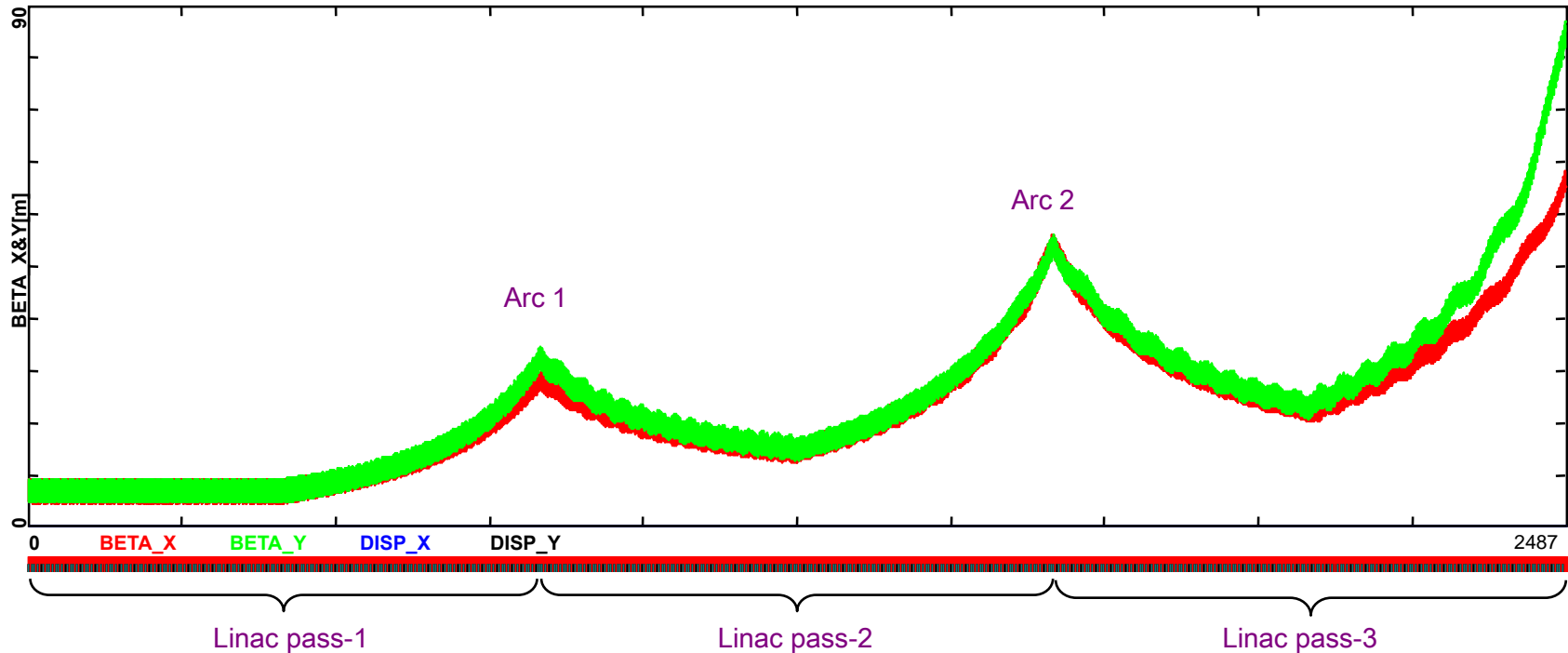
E = 5–16.6 GeV



RF	f [MHz]	cells/cavity	Grad [MV/m]	phase [deg]
	650	5	25	22

Multi-pass Linac – Bisected Optics

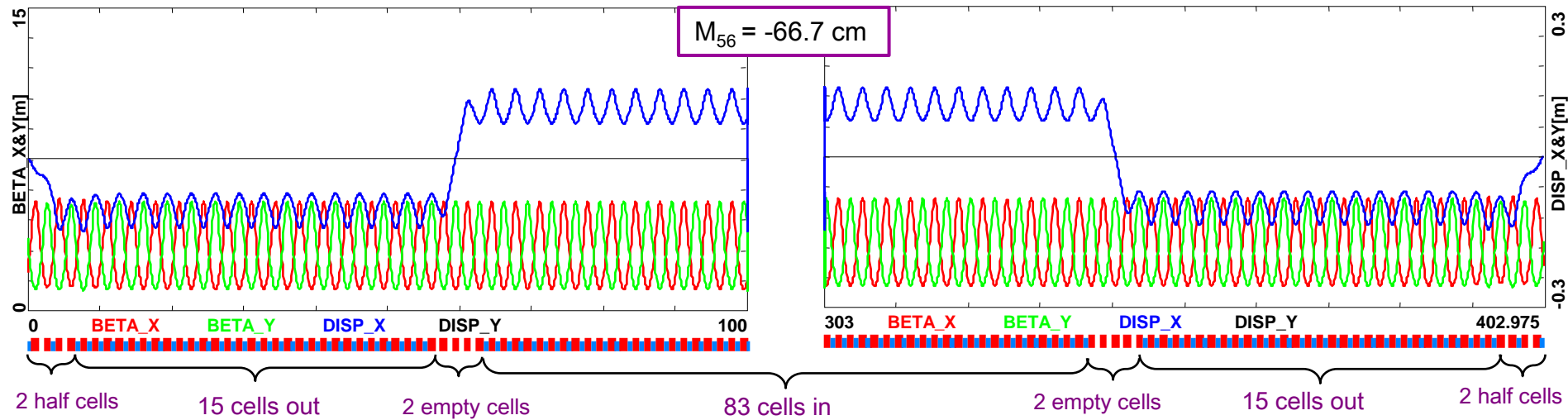
E = 5–63 GeV



RF	f[MHz]	cells/cavity	Grad [MV/m]	phase [deg]
	650	5	25	22

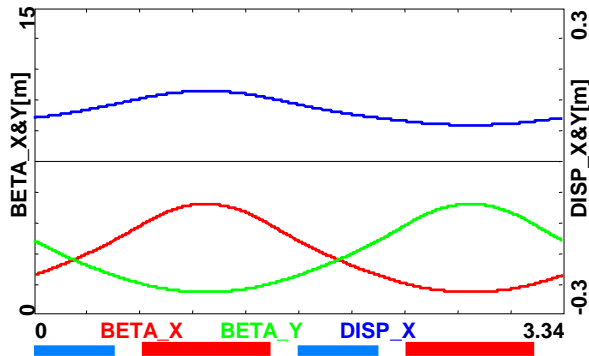
Arc Optics – Longitudinal Distortion

E = 24 GeV



90° FODO

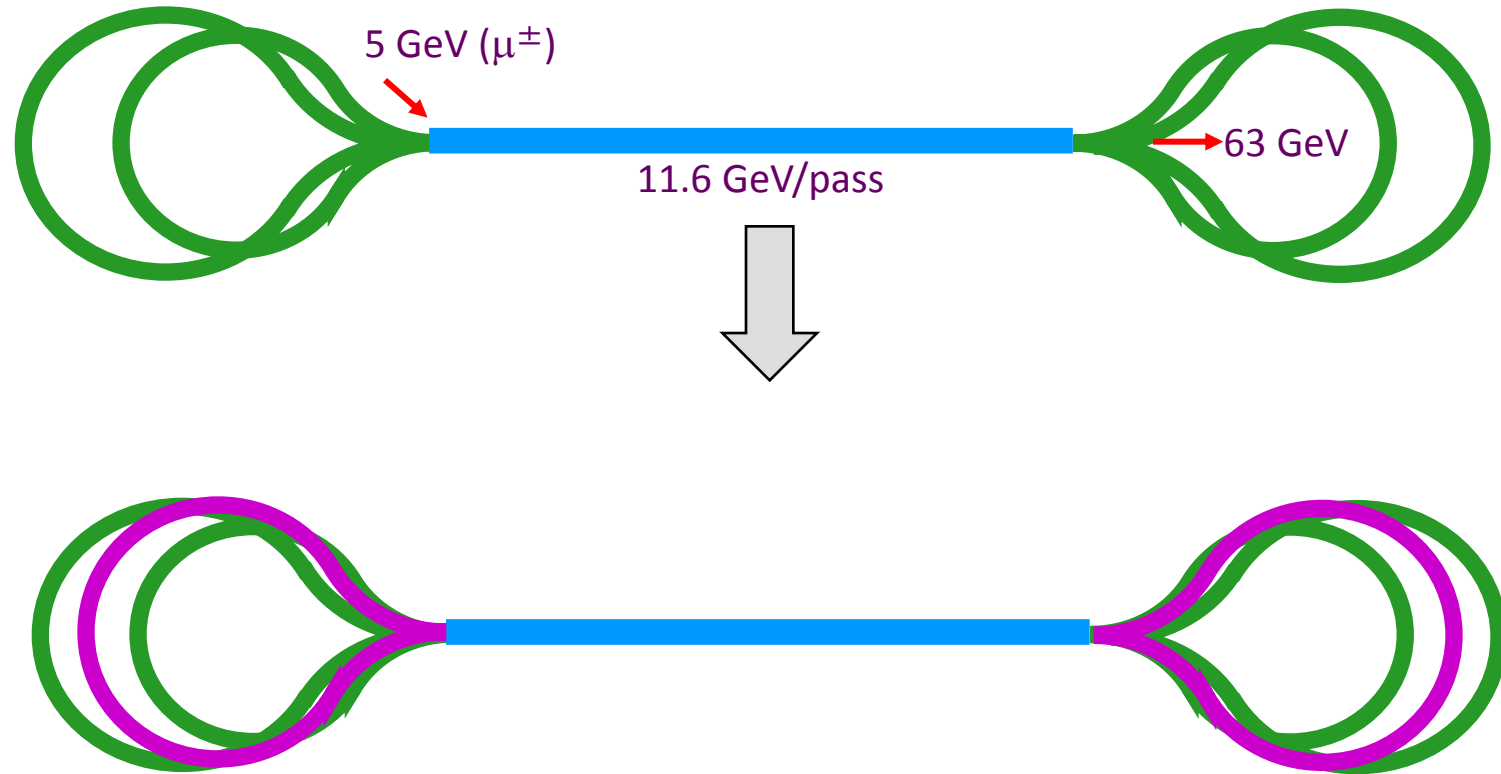
$$n_i = 5n_o + 8$$



Quads	L[cm]	G[kG/cm]
qF	80	10.2924
qD	80	-10.2788

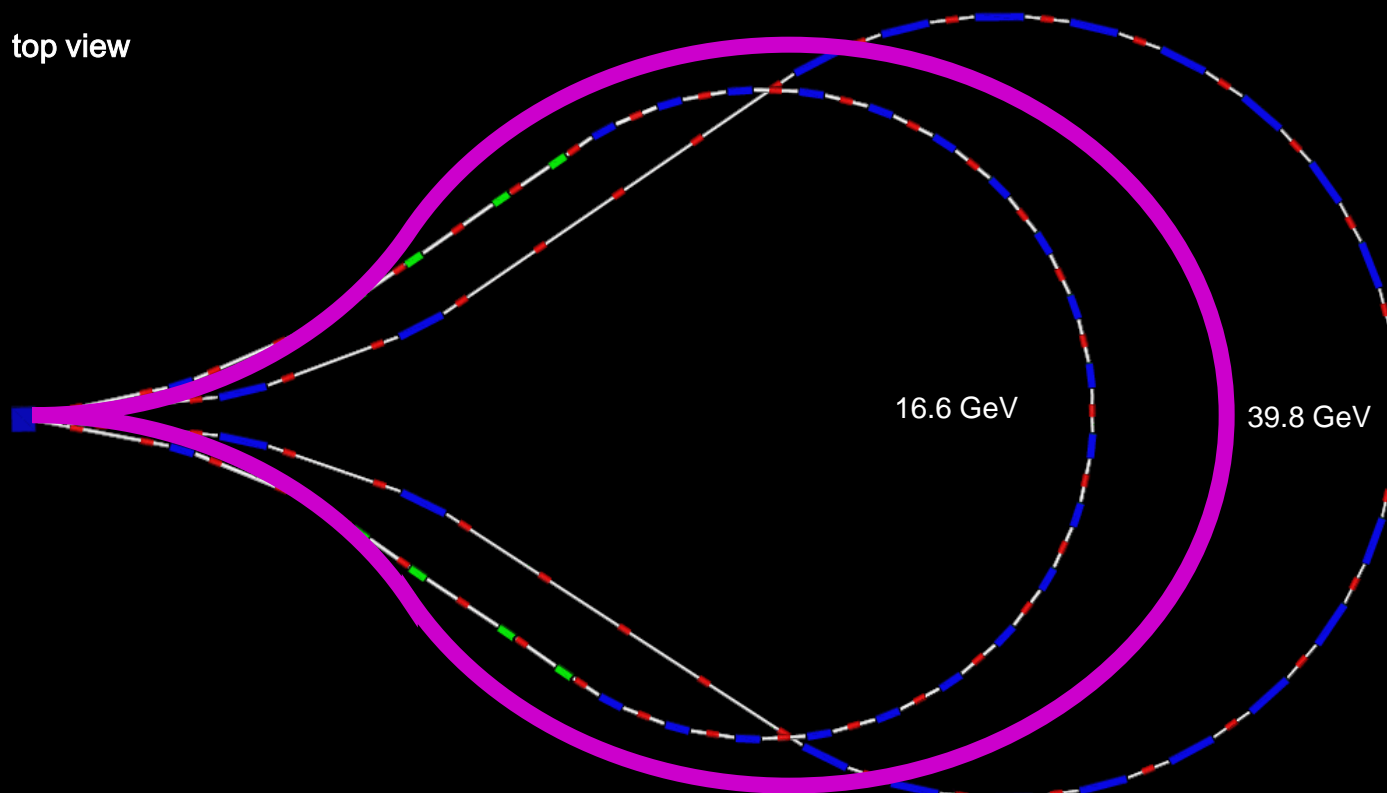
Dipoles	L[cm]	B[kG]	bend angle [deg]
	50.00	49.3116	1.7647

Multi-pass Arc Muon RLA



Single- vs Multi- pass Droplet Arcs

top view



JEMMRLA □ Jlab Electron Model of Muon RLA

side view



Summary

- The main thrust is to develop concepts for acceleration of muon beams for a cost effective, stageable Neutrino Factory and then Higgs Factory.
- We propose expansion of D&S efforts on muon acceleration for NuMAX and beyond:
 - Utilizing building blocks (schemes and lattices) developed by the IDS-NF and taking advantage of the opportunities identified by MASS for staging.
 - Reducing the cost while maintaining performance exploiting interplay between the cooling systems and the acceptance of the accelerator.
 - Fully explore dual-use linac concept through muon/H⁻ compatibility study, which will lead to a cost optimized acceleration complex.
 - Optimize RLA scheme for Higgs Factory:
 - Number of passes (beam loading)
 - RLA with multi-pass arcs