

# *Global fits from Neutrino Oscillation Experiments*

*NuFact 2014, 25-30 August 2014, Glasgow, UK*

Thomas Schwetz



Stockholms  
universitet



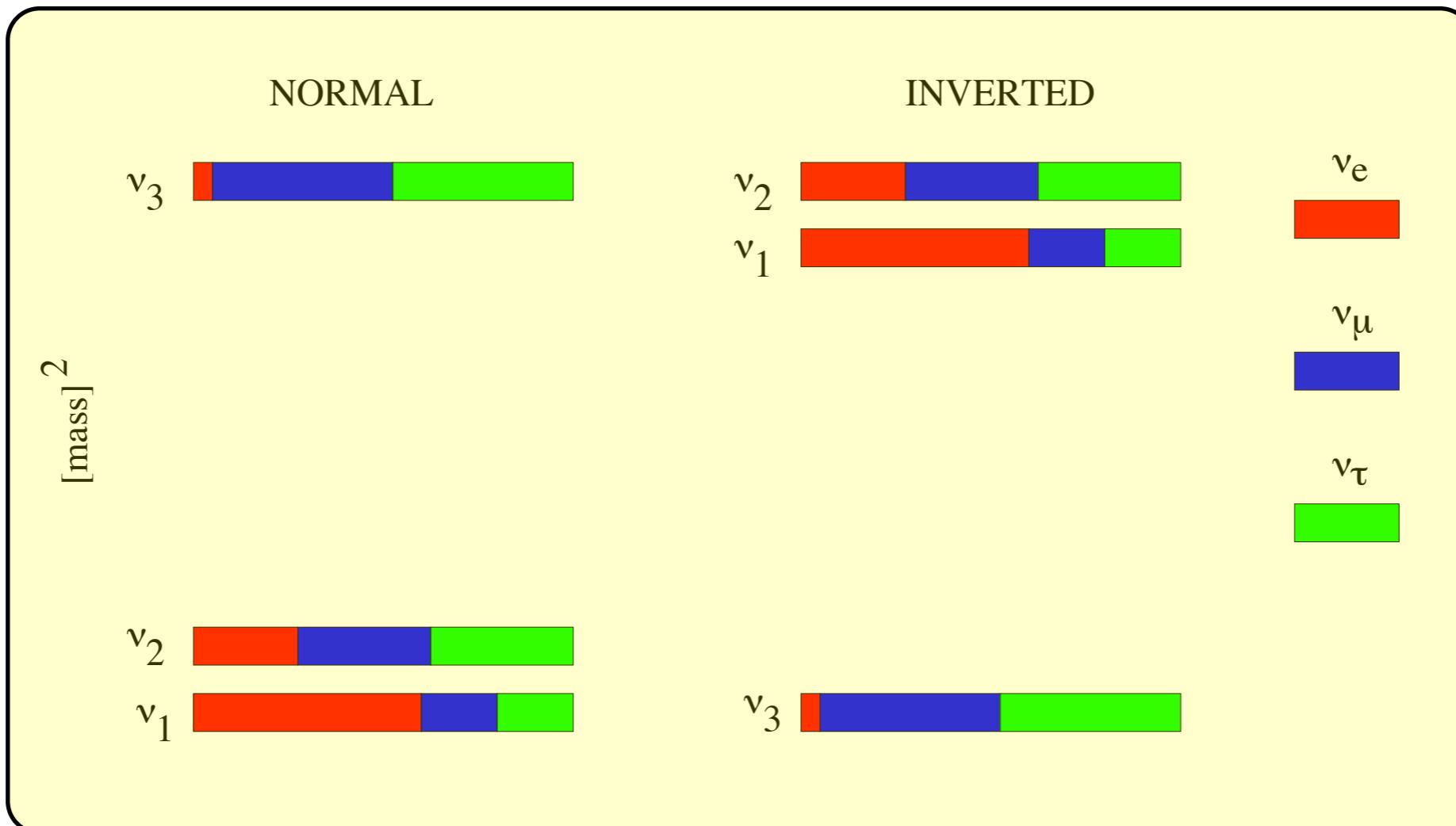
Oscar Klein  
centre



# *Content*

- *Global 3-flavour fit*
  - ▶ *Neutrino mass ordering*
  - ▶ *CP phase*
  - ▶ *Octant of  $\theta_{23}$*
- *Sterile neutrinos*

# 3-flavour oscillations



# 3-flavour global fit to oscillation data



with C. Gonzalez-Garcia, M. Maltoni

website with up-to-date results from global fit  
 current version 1.3 (after Neutrino2014)  
 version 2.0 (plus publication) in preparation

	Normal Ordering ( $\Delta\chi^2 = 0.97$ )		Inverted Ordering (best fit)		Any Ordering
	bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range	$3\sigma$ range
$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.270 \rightarrow 0.344$	$0.304^{+0.012}_{-0.012}$	$0.270 \rightarrow 0.344$	$0.270 \rightarrow 0.344$
$\theta_{12}/^\circ$	$33.48^{+0.77}_{-0.74}$	$31.30 \rightarrow 35.90$	$33.48^{+0.77}_{-0.74}$	$31.30 \rightarrow 35.90$	$31.30 \rightarrow 35.90$
$\sin^2 \theta_{23}$	$0.451^{+0.051}_{-0.026}$	$0.382 \rightarrow 0.643$	$0.577^{+0.027}_{-0.035}$	$0.389 \rightarrow 0.644$	$0.385 \rightarrow 0.644$
$\theta_{23}/^\circ$	$42.2^{+2.9}_{-1.5}$	$38.2 \rightarrow 53.3$	$49.4^{+1.6}_{-2.0}$	$38.6 \rightarrow 53.3$	$38.4 \rightarrow 53.3$
$\sin^2 \theta_{13}$	$0.0218^{+0.0010}_{-0.0010}$	$0.0186 \rightarrow 0.0250$	$0.0219^{+0.0010}_{-0.0011}$	$0.0188 \rightarrow 0.0251$	$0.0188 \rightarrow 0.0251$
$\theta_{13}/^\circ$	$8.50^{+0.20}_{-0.21}$	$7.85 \rightarrow 9.10$	$8.52^{+0.20}_{-0.21}$	$7.87 \rightarrow 9.11$	$7.87 \rightarrow 9.11$
$\delta_{CP}/^\circ$	$305^{+39}_{-51}$	$0 \rightarrow 360$	$251^{+66}_{-59}$	$0 \rightarrow 360$	$0 \rightarrow 360$
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.50^{+0.19}_{-0.17}$	$7.03 \rightarrow 8.09$	$7.50^{+0.19}_{-0.17}$	$7.03 \rightarrow 8.09$	$7.03 \rightarrow 8.09$
$\frac{\Delta m_{3i}^2}{10^{-3} \text{ eV}^2}$	$+2.458^{+0.046}_{-0.047}$	$+2.317 \rightarrow +2.607$	$-2.448^{+0.047}_{-0.047}$	$-2.590 \rightarrow -2.307$	$\begin{bmatrix} +2.325 \rightarrow +2.599 \\ -2.590 \rightarrow -2.307 \end{bmatrix}$

# 3-flavour global fit to oscillation data



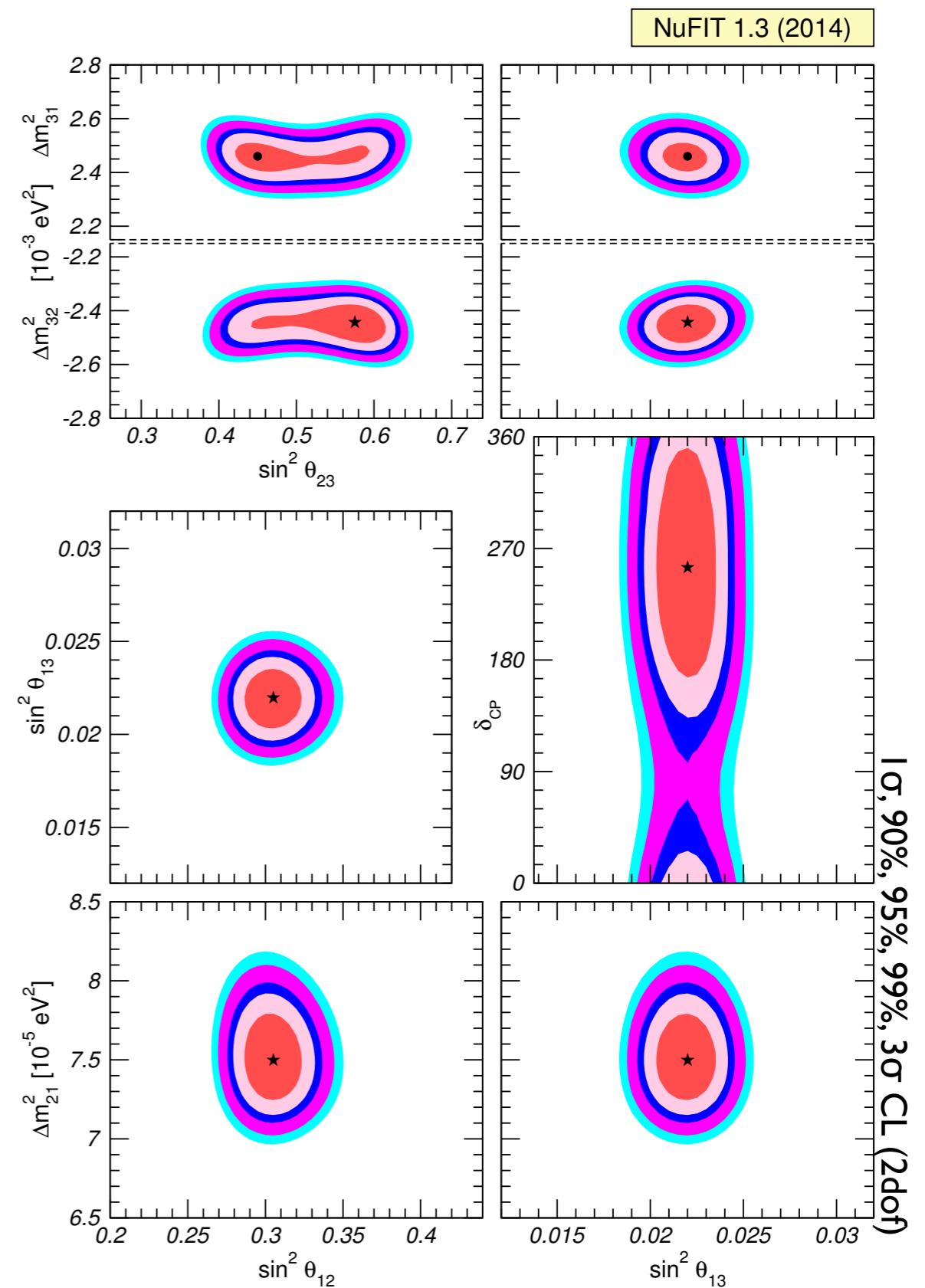
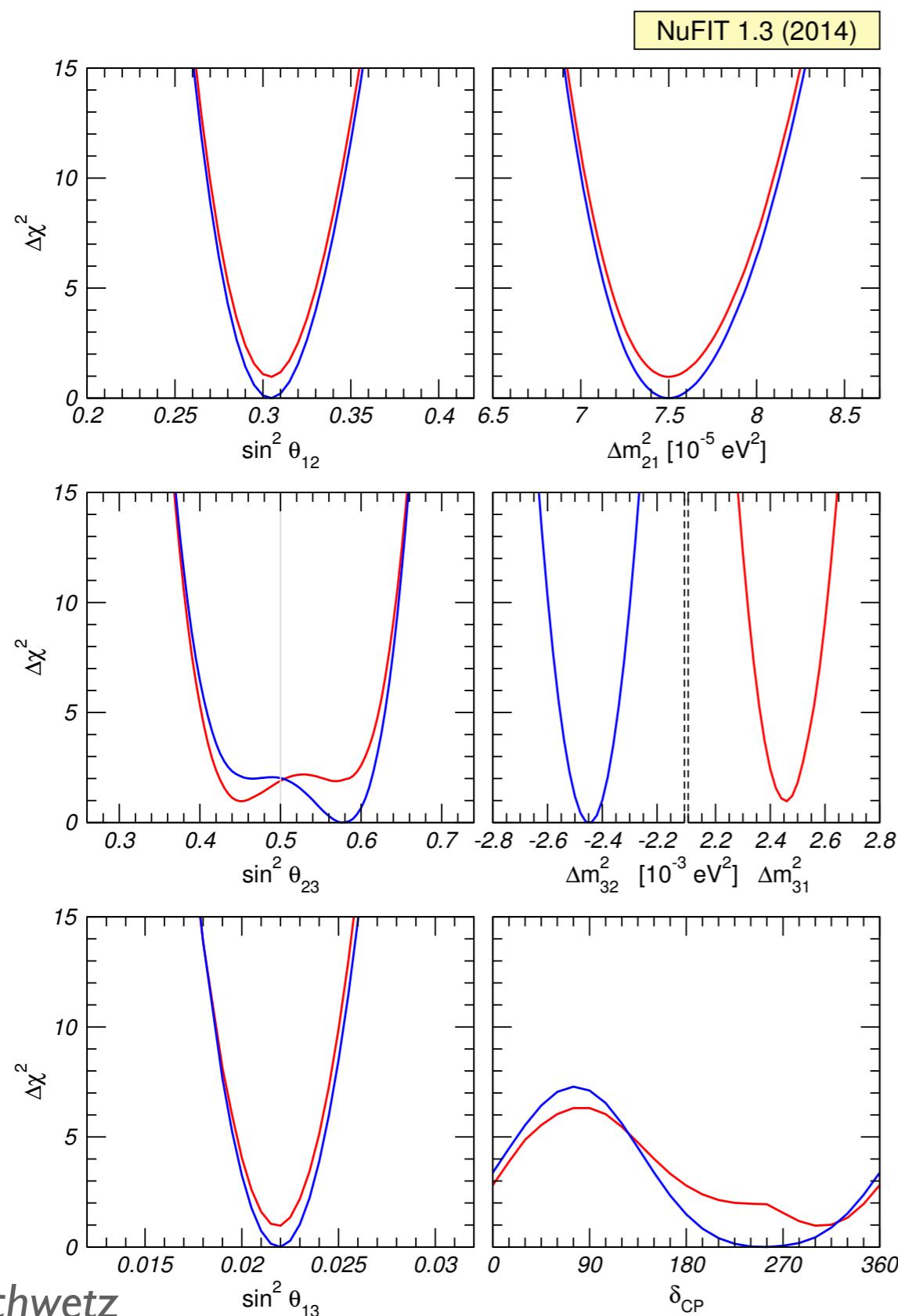
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website with up-to-date results from global fit  
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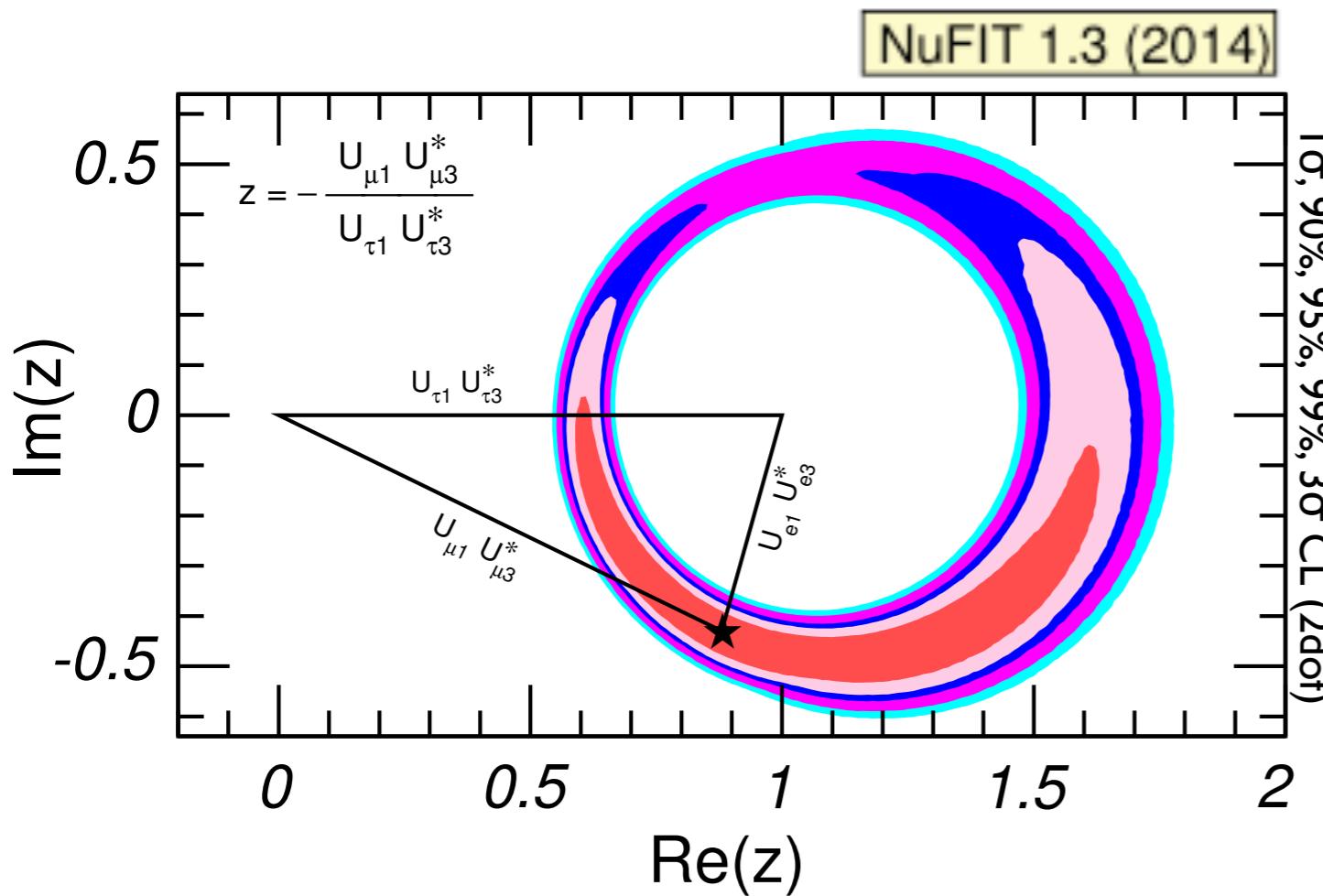
precision  
@  $3\sigma$

	Normal Ordering ( $\Delta\chi^2 = 0.97$ )		Inverted Ordering (best fit)		Any Ordering	
	bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range	$3\sigma$ range	
$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.270 \rightarrow 0.344$	$0.304^{+0.012}_{-0.012}$	$0.270 \rightarrow 0.344$	$0.270 \rightarrow 0.344$	<b>4.6° (14%)</b>
$\theta_{12}/^\circ$	$33.48^{+0.77}_{-0.74}$	$31.30 \rightarrow 35.90$	$33.48^{+0.77}_{-0.74}$	$31.30 \rightarrow 35.90$	$31.30 \rightarrow 35.90$	
$\sin^2 \theta_{23}$	$0.451^{+0.051}_{-0.026}$	$0.382 \rightarrow 0.643$	$0.577^{+0.027}_{-0.035}$	$0.389 \rightarrow 0.644$	$0.385 \rightarrow 0.644$	<b>15° (32%)</b>
$\theta_{23}/^\circ$	$42.2^{+2.9}_{-1.5}$	$38.2 \rightarrow 53.3$	$49.4^{+1.6}_{-2.0}$	$38.6 \rightarrow 53.3$	$38.4 \rightarrow 53.3$	
$\sin^2 \theta_{13}$	$0.0218^{+0.0010}_{-0.0010}$	$0.0186 \rightarrow 0.0250$	$0.0219^{+0.0010}_{-0.0011}$	$0.0188 \rightarrow 0.0251$	$0.0188 \rightarrow 0.0251$	<b>1.2° (15%)</b>
$\theta_{13}/^\circ$	$8.50^{+0.20}_{-0.21}$	$7.85 \rightarrow 9.10$	$8.52^{+0.20}_{-0.21}$	$7.87 \rightarrow 9.11$	$7.87 \rightarrow 9.11$	
$\delta_{CP}/^\circ$	$305^{+39}_{-51}$	$0 \rightarrow 360$	$251^{+66}_{-59}$	$0 \rightarrow 360$	$0 \rightarrow 360$	<b><math>\infty</math></b>
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.50^{+0.19}_{-0.17}$	$7.03 \rightarrow 8.09$	$7.50^{+0.19}_{-0.17}$	$7.03 \rightarrow 8.09$	$7.03 \rightarrow 8.09$	<b>14%</b>
$\frac{\Delta m_{3i}^2}{10^{-3} \text{ eV}^2}$	$+2.458^{+0.046}_{-0.047}$	$+2.317 \rightarrow +2.607$	$-2.448^{+0.047}_{-0.047}$	$-2.590 \rightarrow -2.307$	$\begin{bmatrix} +2.325 \rightarrow +2.599 \\ -2.590 \rightarrow -2.307 \end{bmatrix}$	<b>11%</b>

# 3-flavour global fit to oscillation data



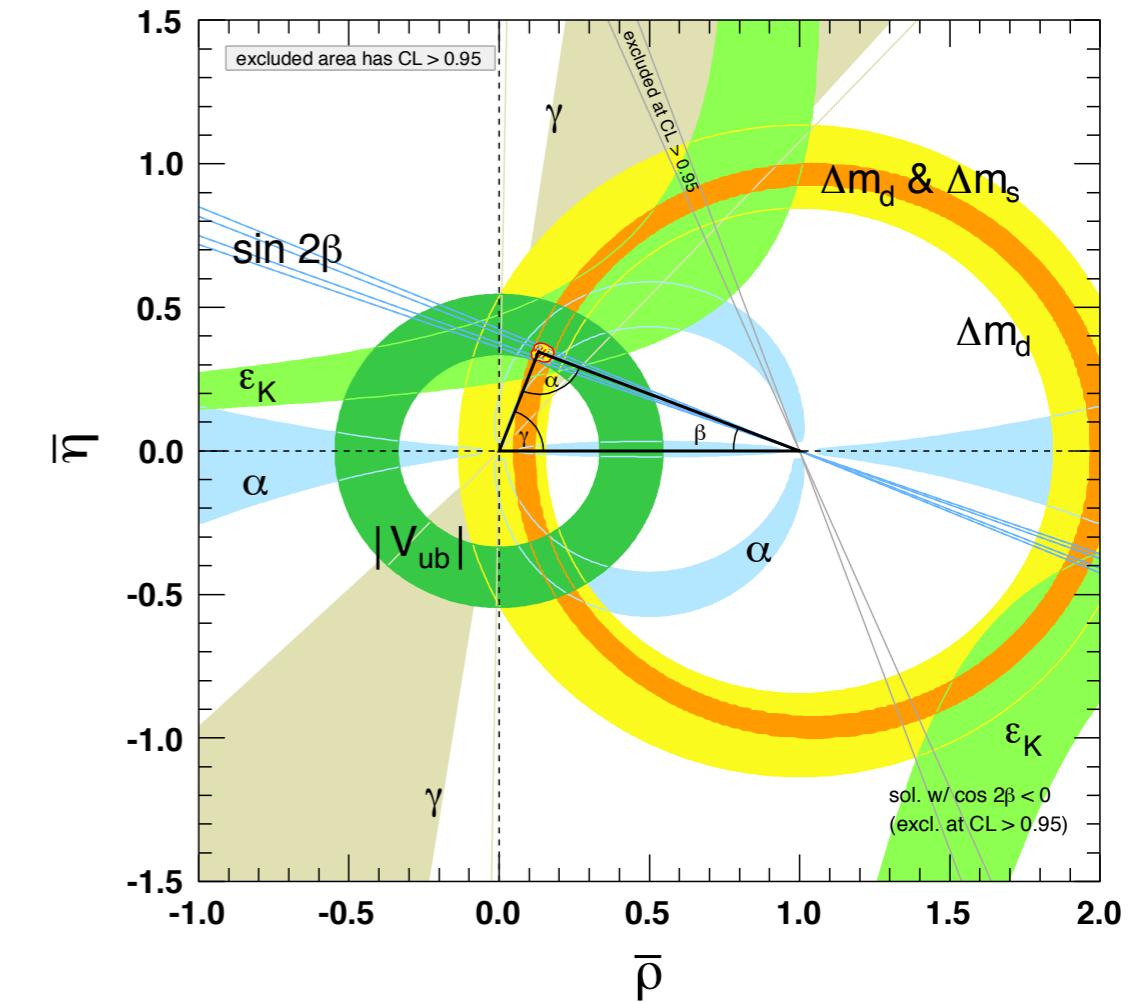
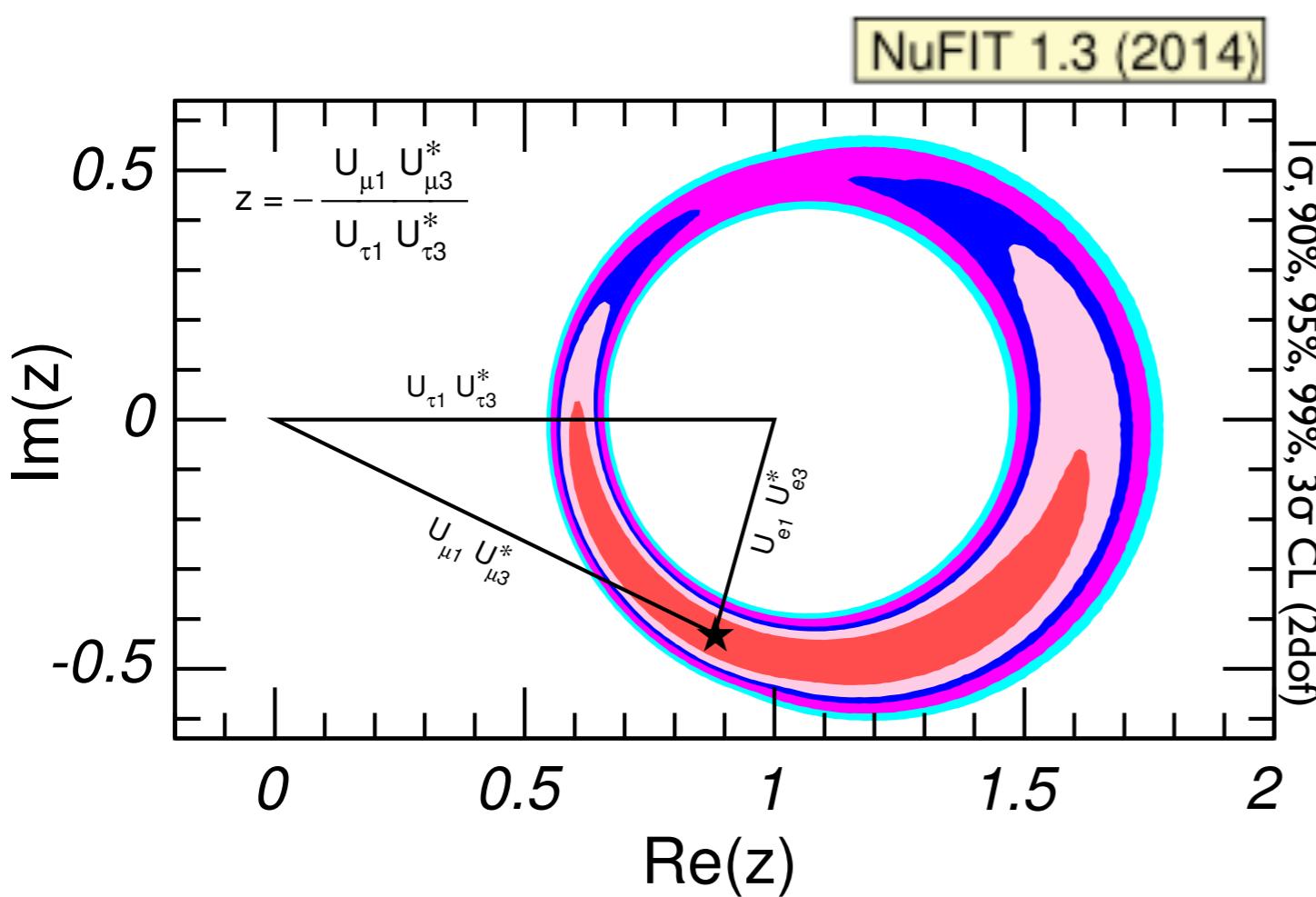
# Leptonic unitarity triangle



Farzan, Smirnov, hep-ph/0201105  
Smirnov, 0810.2668

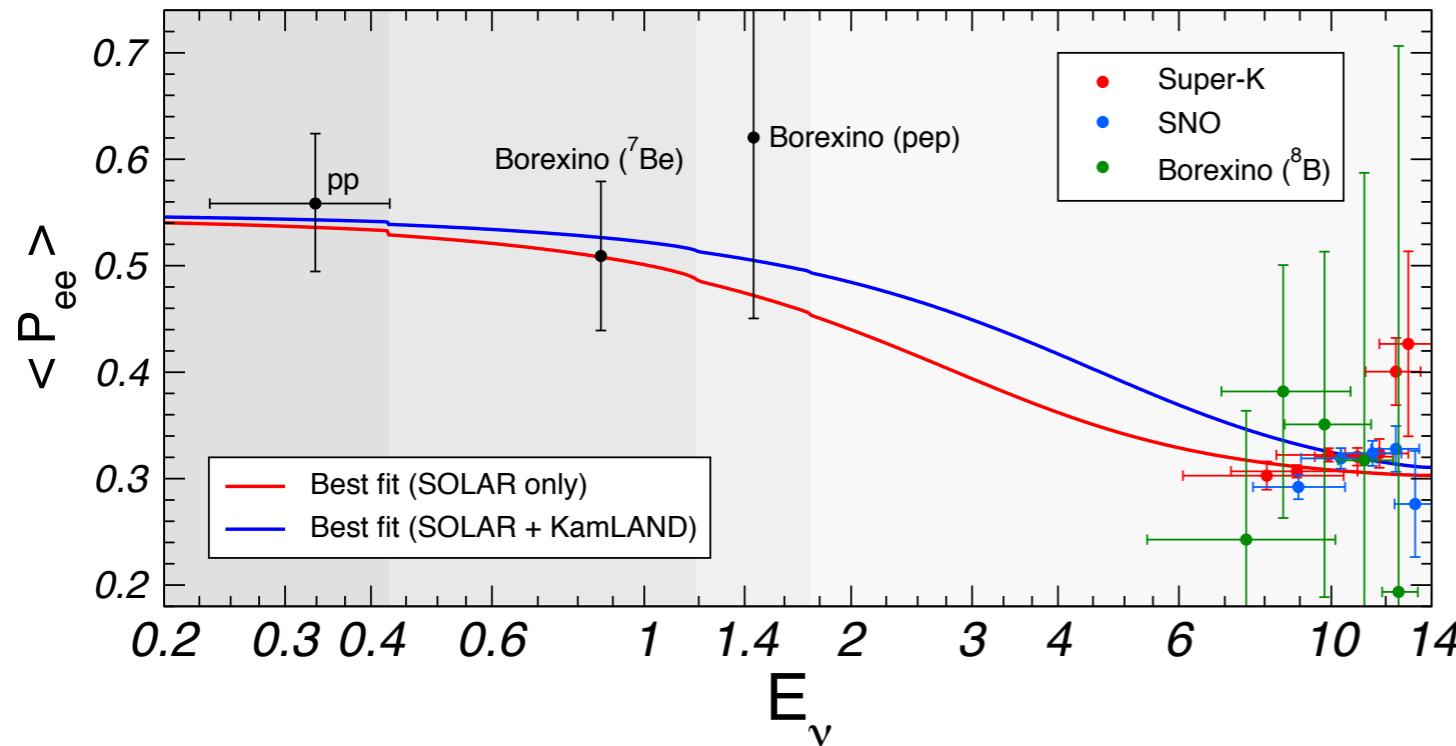
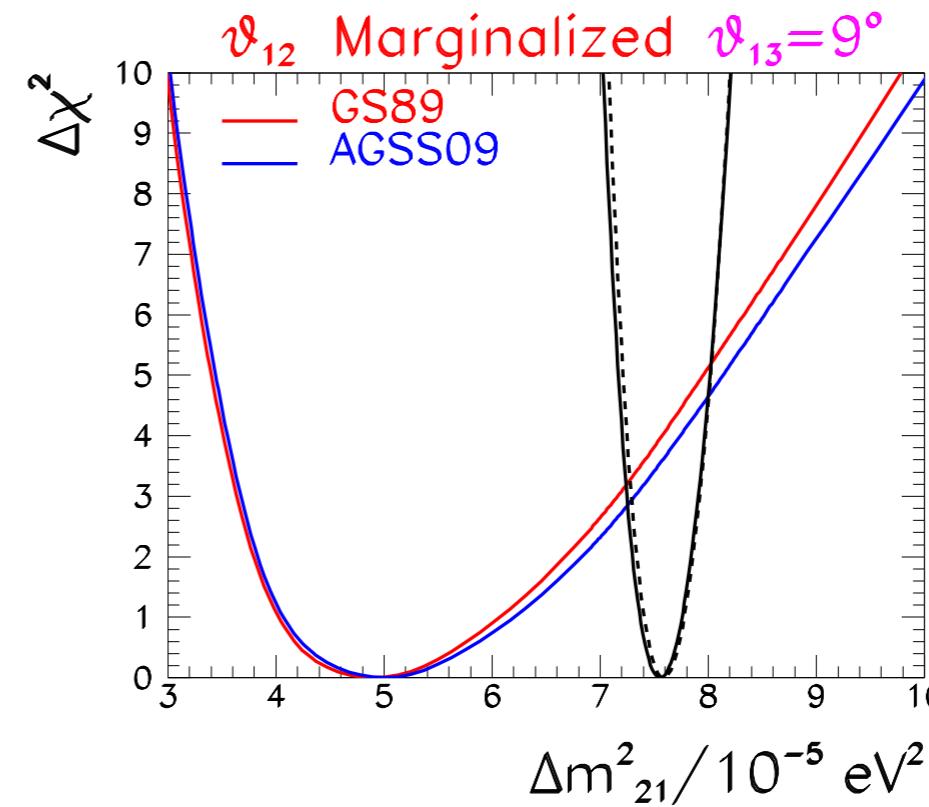
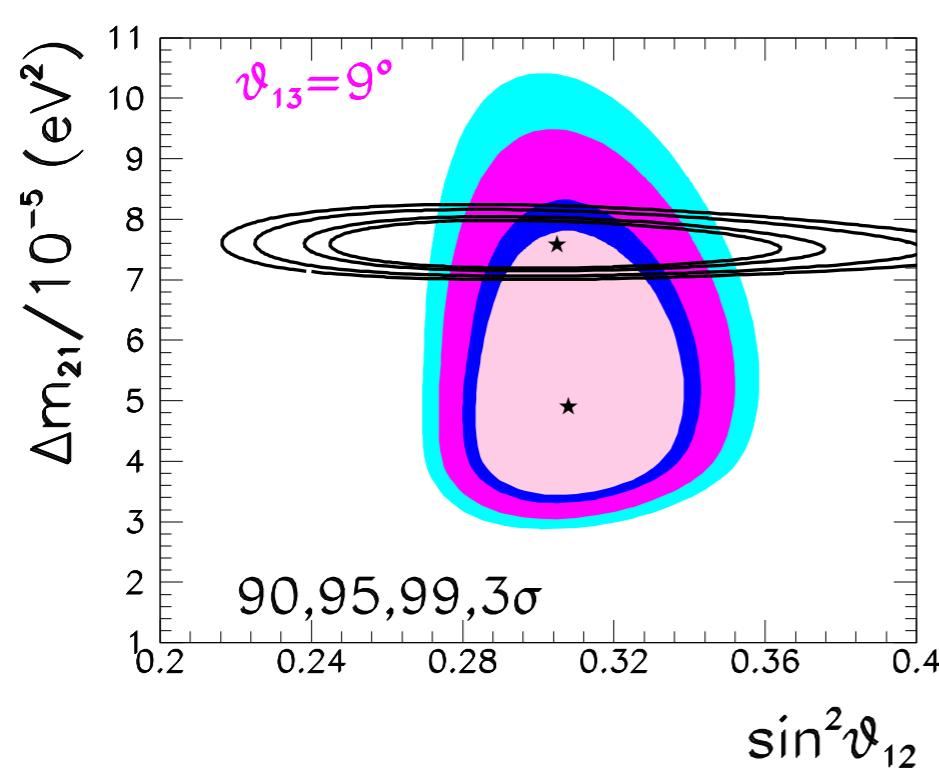
- *unitarity is always assumed (no test of unitarity!)*

# Leptonic unitarity triangle



- still far from knowledge we have on UT in quark sector

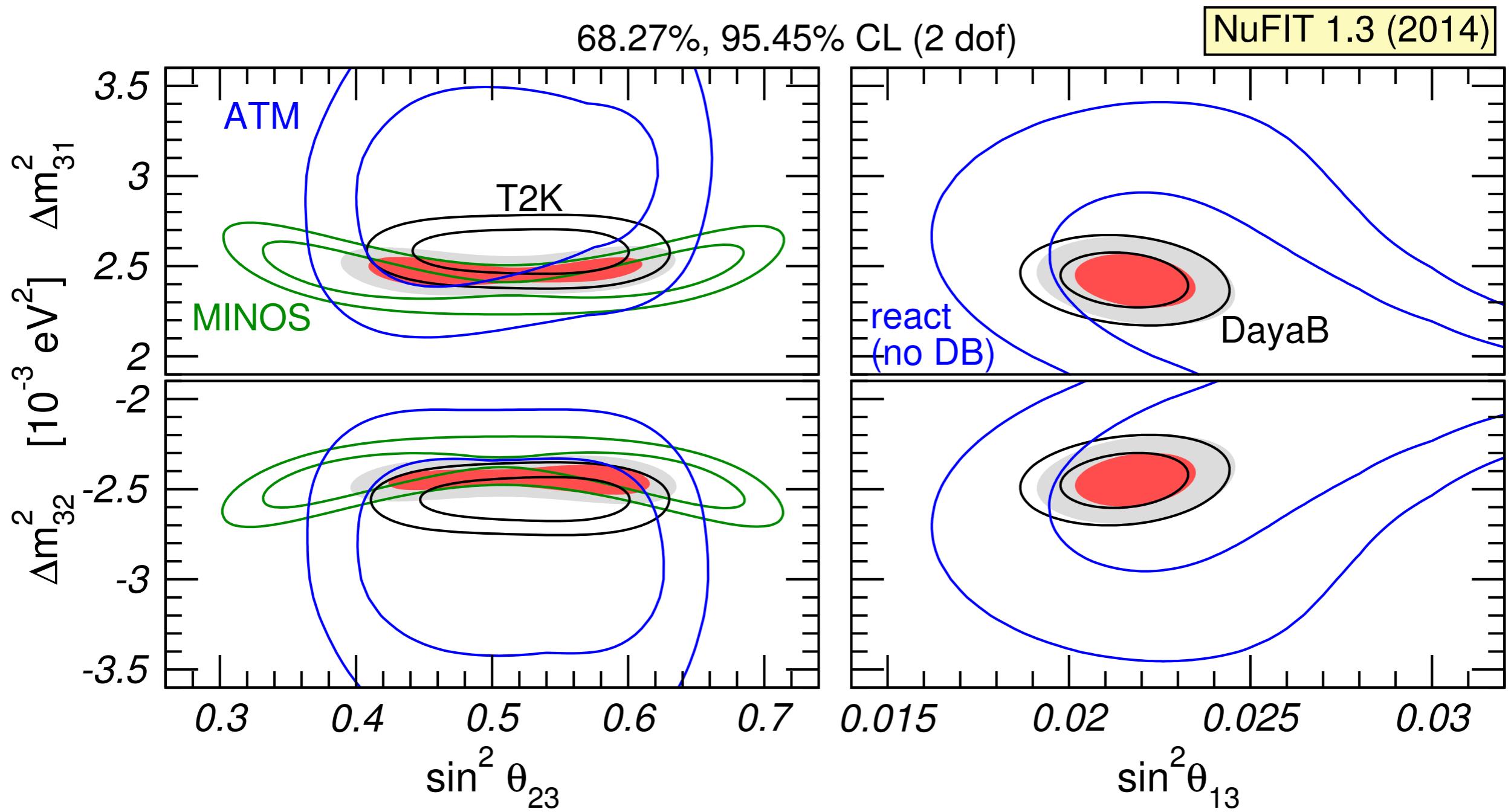
# 1-2 sector



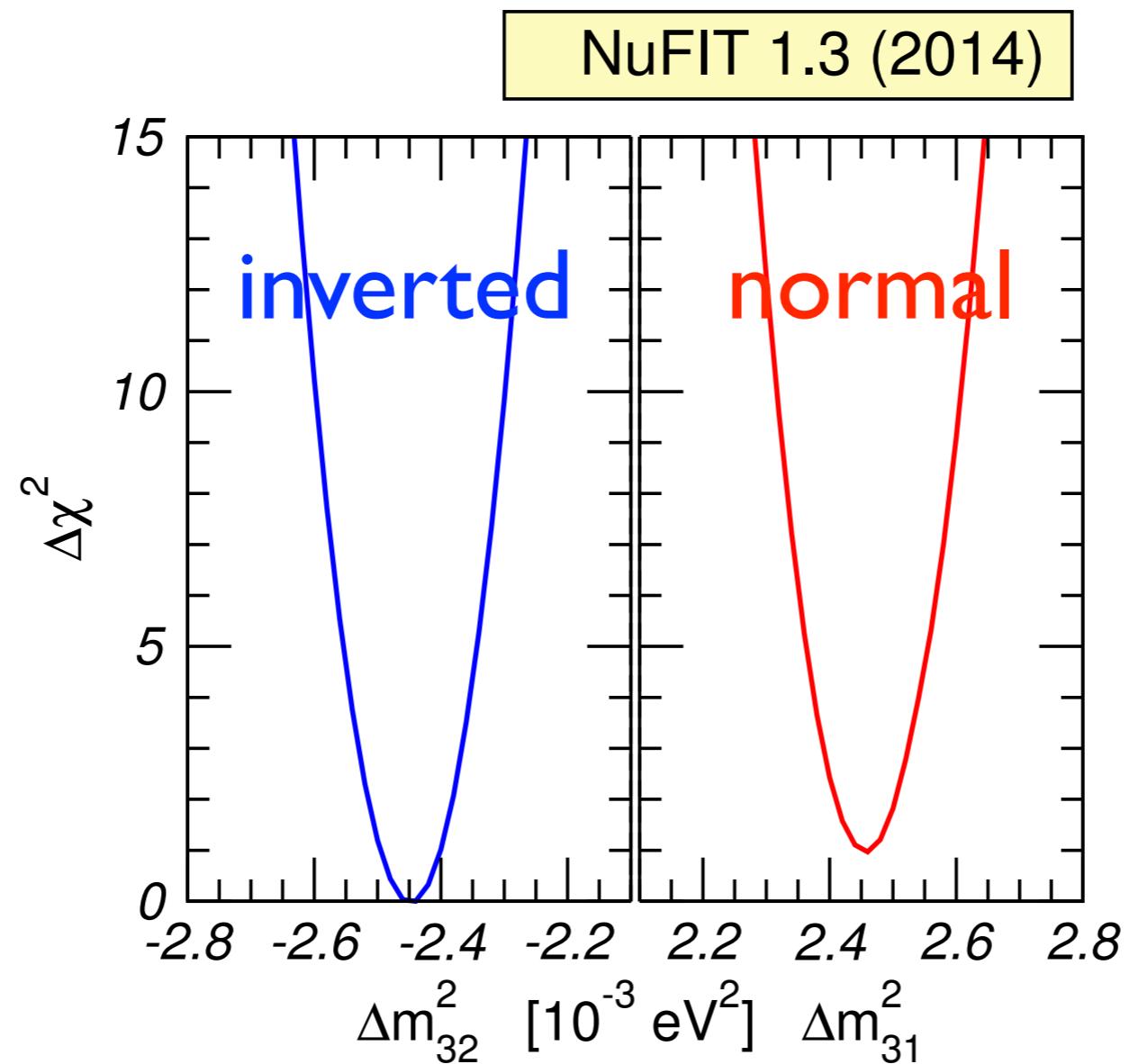
“tension” between solar and  
Kamland at  $2\sigma$  level ( $\Delta\chi^2 = 4$ )  
missing up-turn of solar neutrino  
spectrum in SNO and SK

# 1-3 sector

consistent determination of  $|\Delta m^2_{31}|$  from LBL, ATM, and Daya Bay



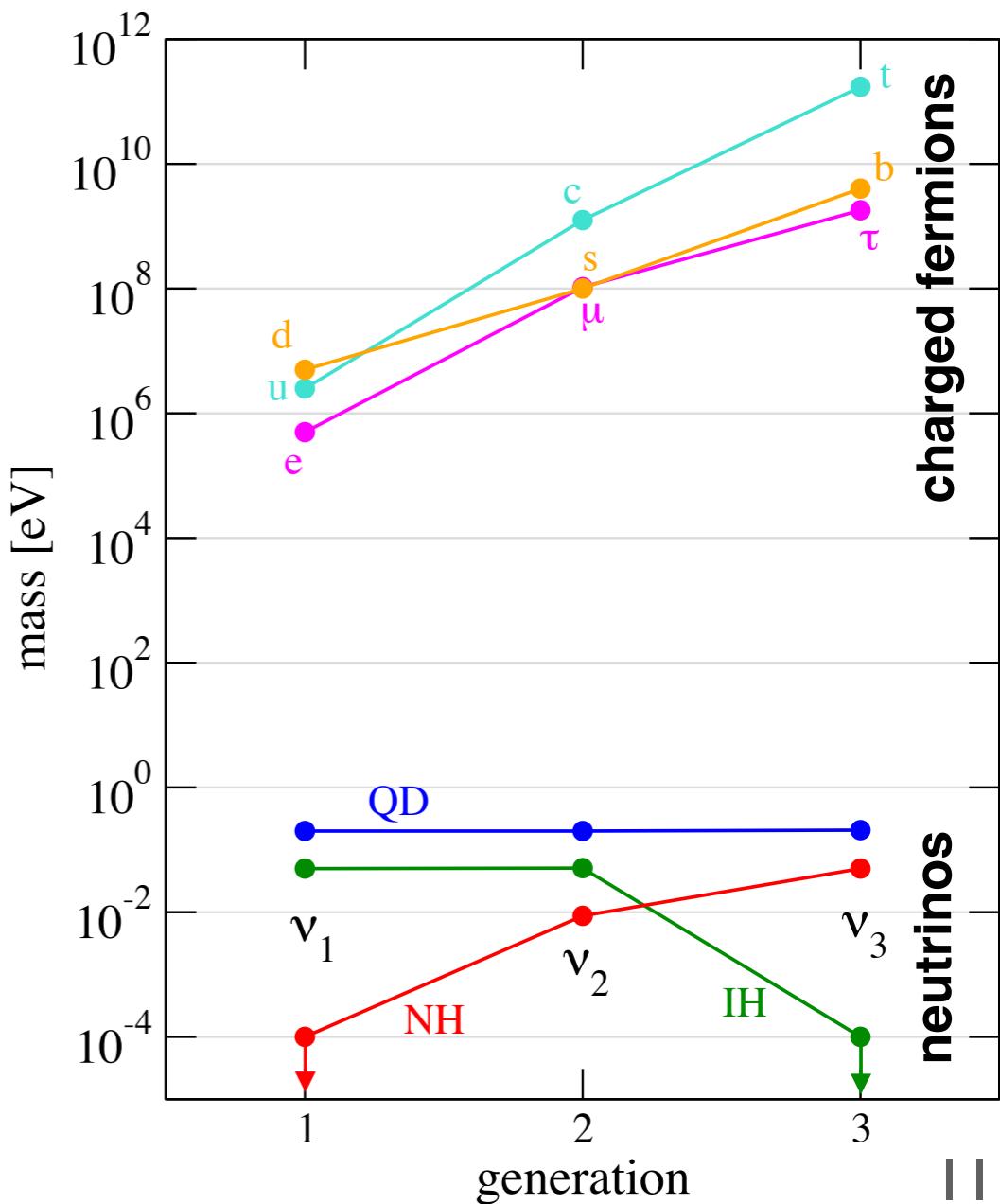
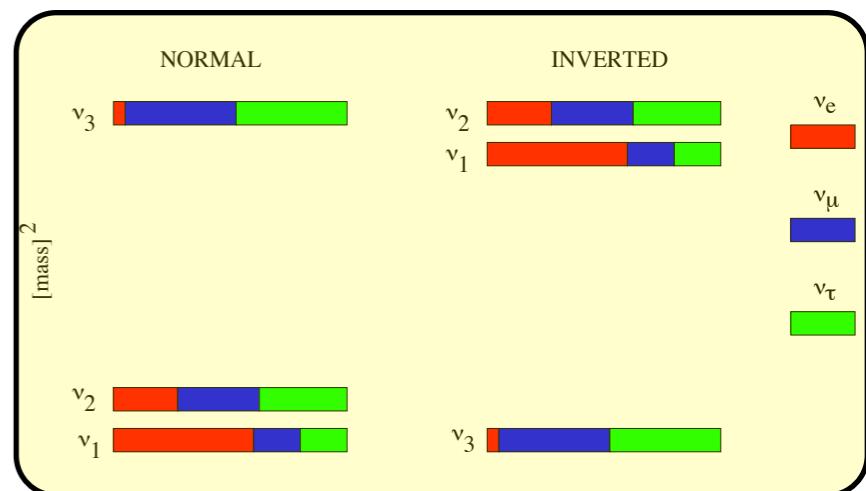
# *Neutrino mass ordering*



almost complete degeneracy in present data

# *normal versus abnormal*

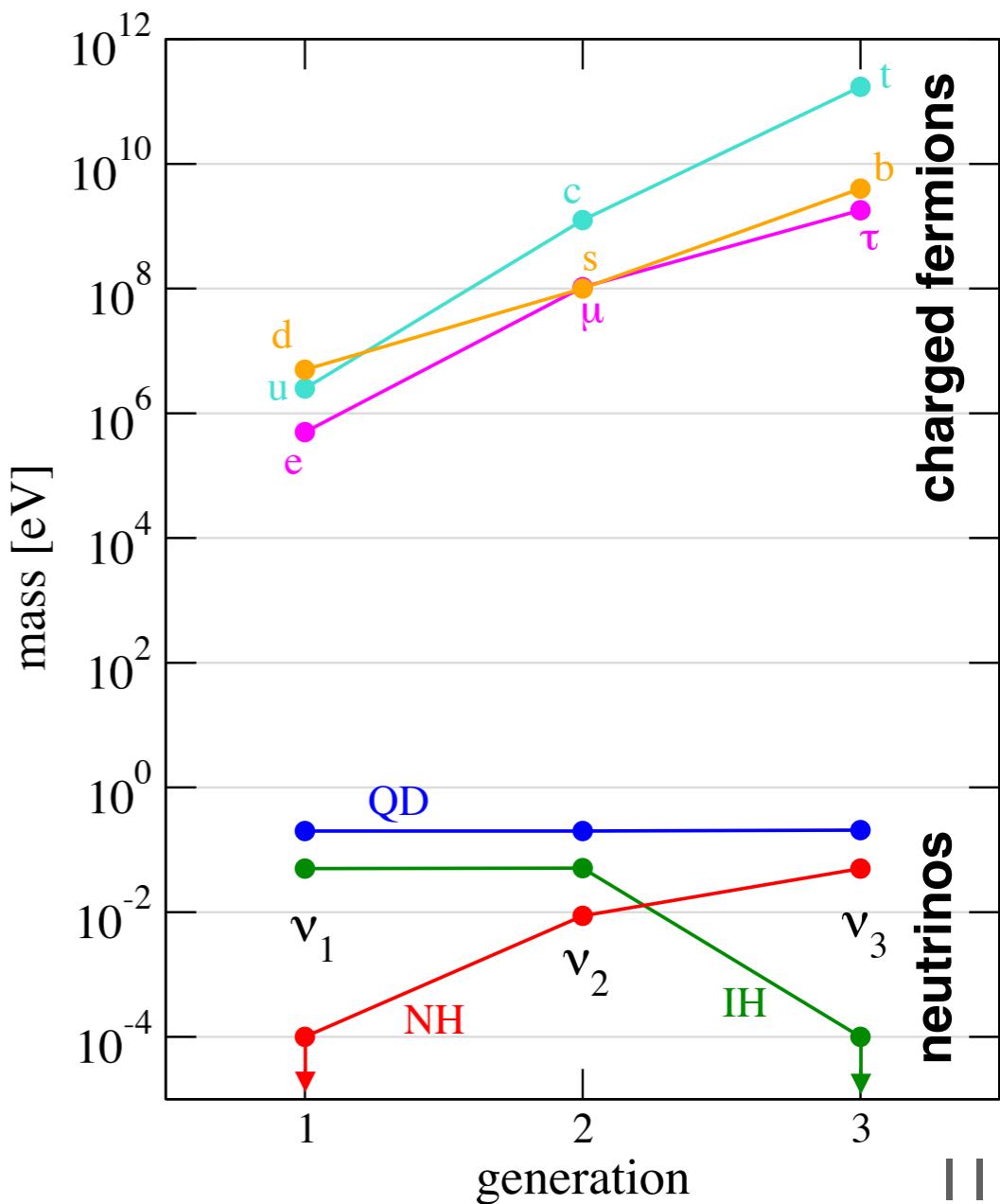
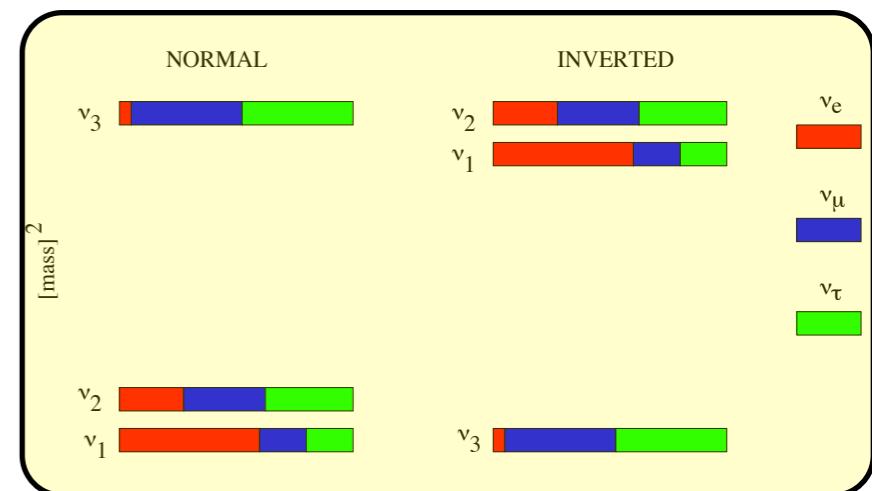
for inverted ordering lepton mixing  
is very different from quarks:



# *normal versus abnormal*

for inverted ordering lepton mixing  
is very different from quarks:

- *the neutrino mass state mostly related to the 1st generation is not the lightest*



# normal versus abnormal

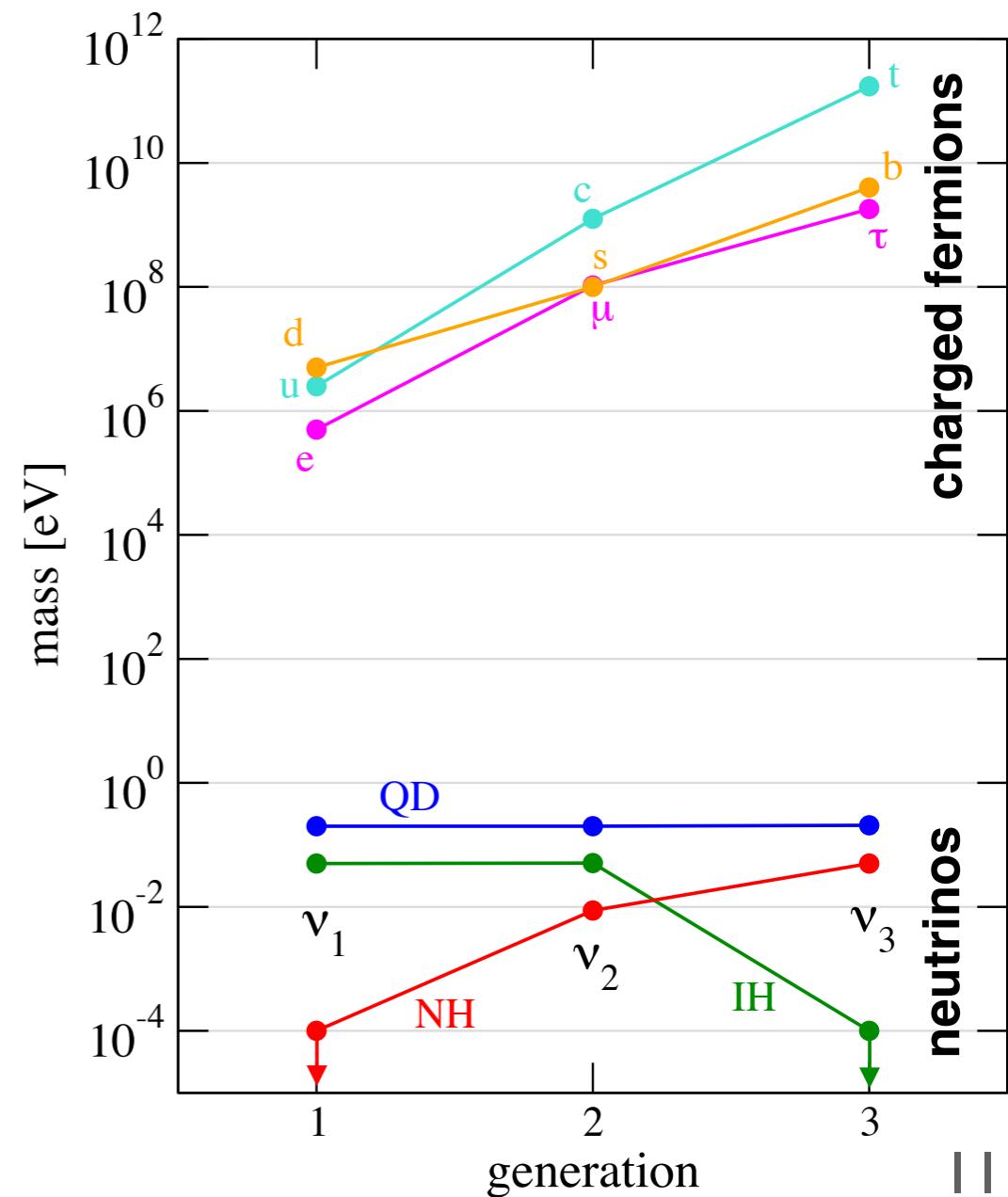
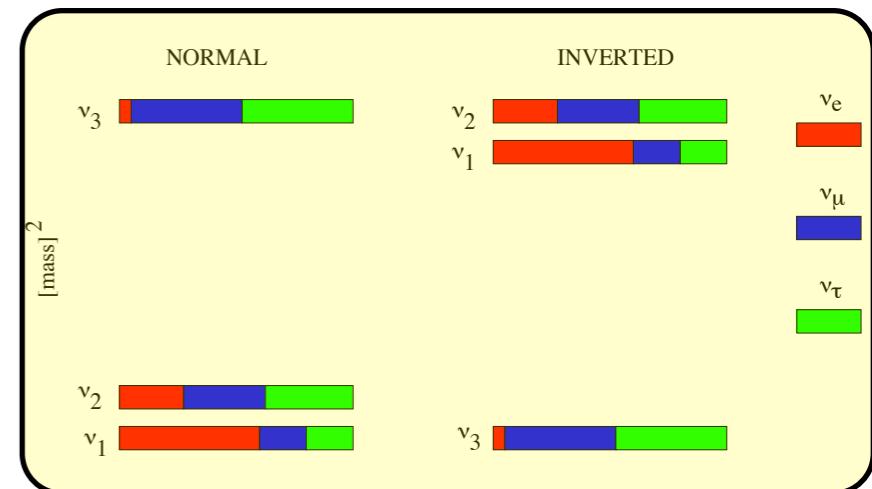
for inverted ordering lepton mixing  
is very different from quarks:

- the neutrino mass state mostly related to the 1st generation is not the lightest
- there is strong degeneracy between at least two mass states

$$deg \equiv \frac{m_2 - m_1}{\bar{m}} = 2 \frac{\Delta m_{21}^2}{(m_1 + m_2)^2}$$

$$\approx \frac{1}{2} \frac{\Delta m_{21}^2}{|\Delta m_{31}^2| + m_3^2} \leq \frac{1}{2} \frac{\Delta m_{21}^2}{|\Delta m_{31}^2|}$$

$$1.3 \times 10^{-3} \left( \frac{\sum m_i}{0.5 \text{ eV}} \right)^{-2} \leq deg \leq 1.8 \times 10^{-2}$$



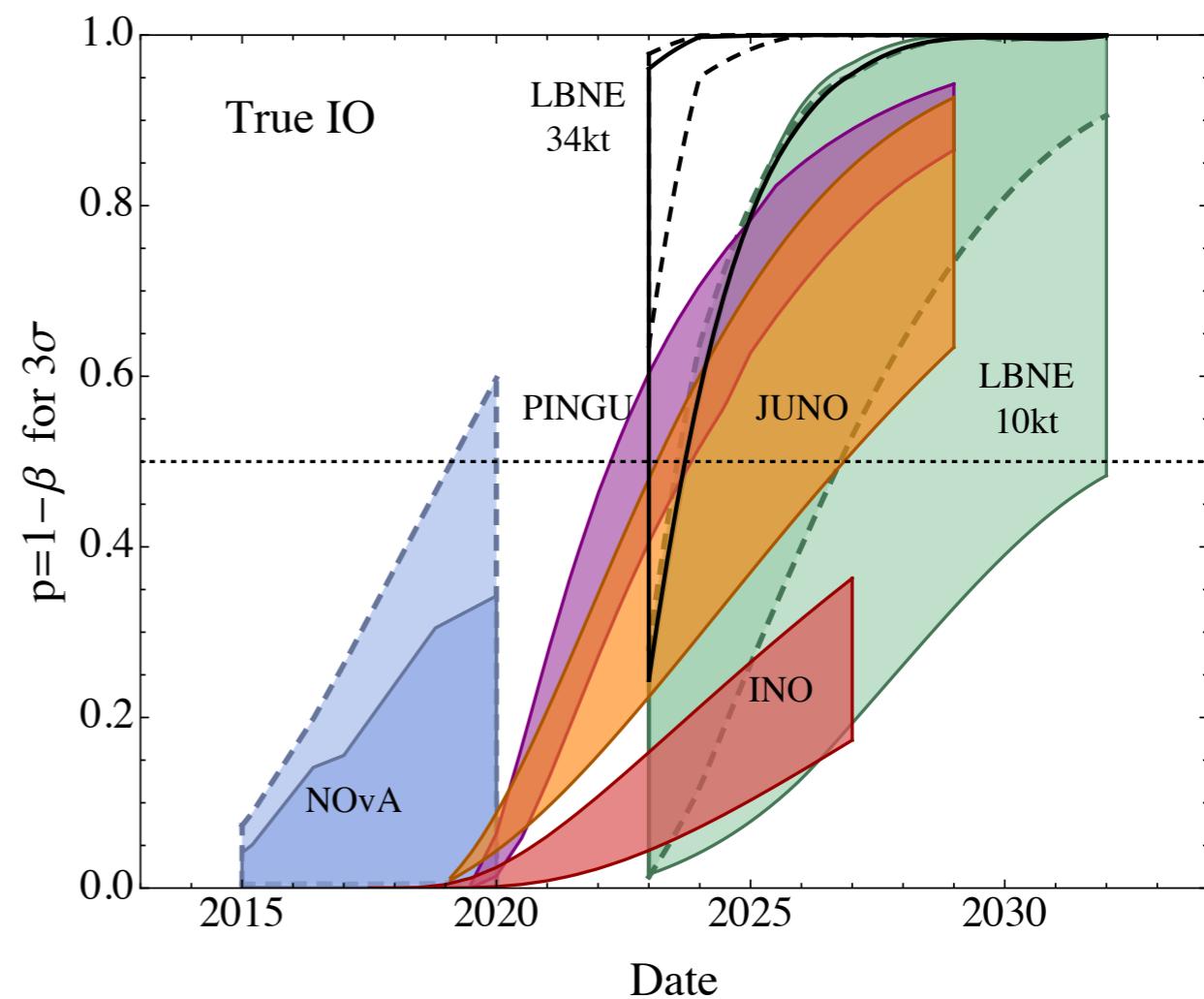
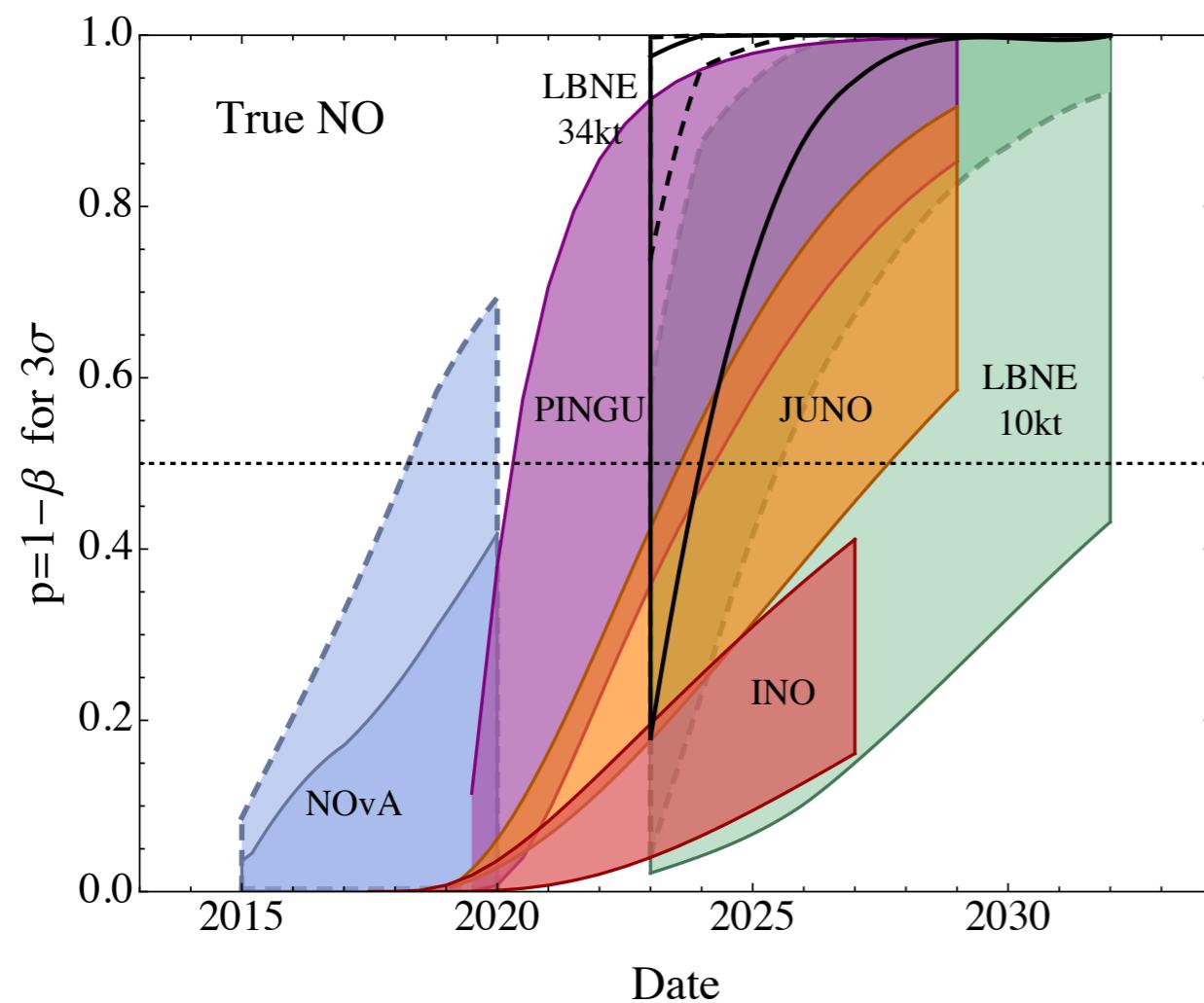
# *How to determine the mass ordering?*

- Matter effect in the 1-3 sector
  - ▶ long-baseline accelerator experiments  
*NOvA, LBNE, LBNO, ESS-SB, NuFact*
  - ▶ atmospheric neutrinos *INO, PINGU, ORCA, HyperK*
- Interference of oscillations with  $\Delta m^2_{21}$  and  $\Delta m^2_{31}$ 
  - ▶ Reactor experiment at  $\sim 60$  km *JUNO, RENO50*
- other methods: cosmology, supernova,...

# Sensitivity comparison

Blennow, Coloma, Huber, TS, I3/I.I.1822  
talk by M. Blennow, and many more

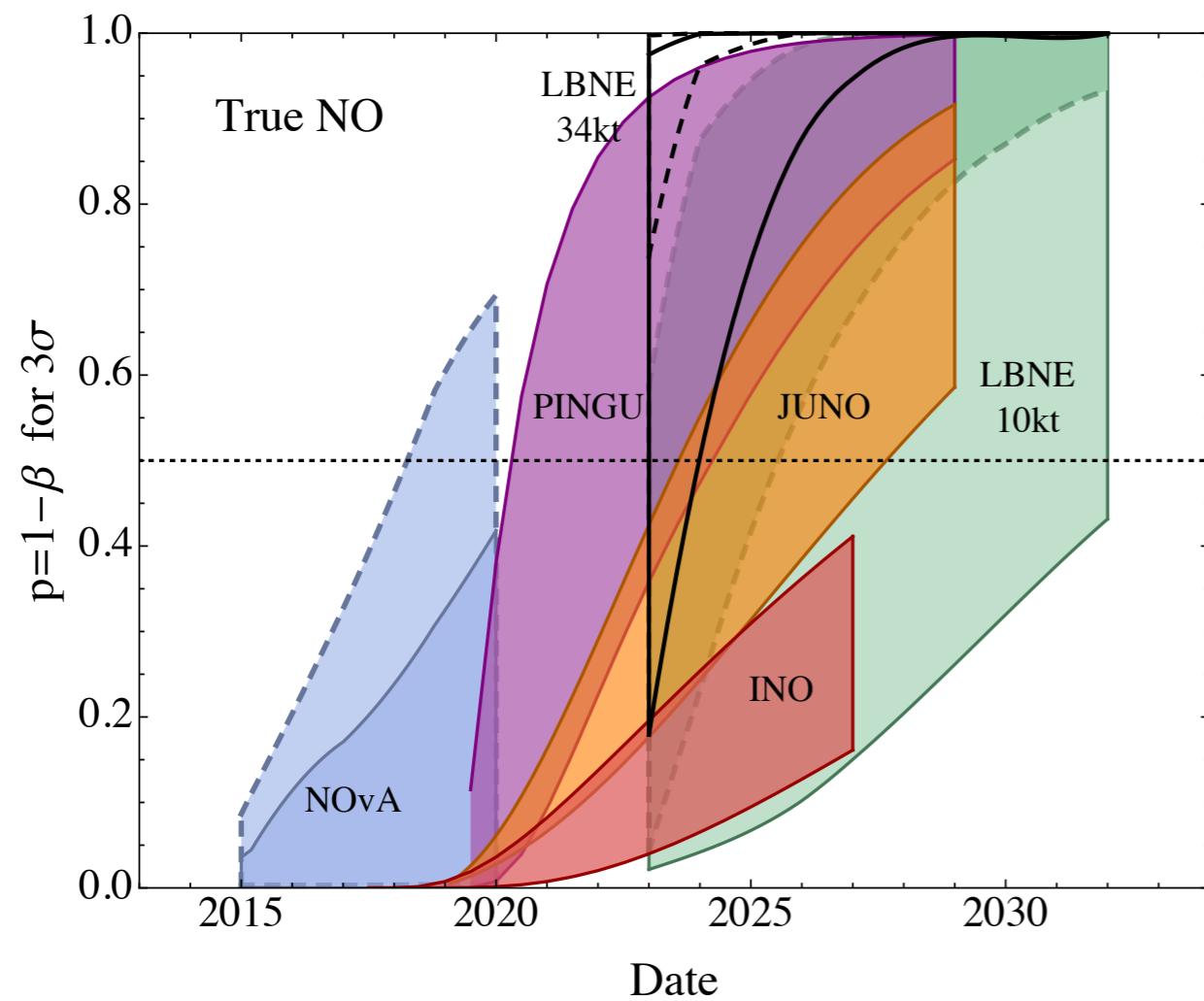
probability to exclude wrong ordering at  $3\sigma$   
("representative" selection of experiments)



# Sensitivity comparison

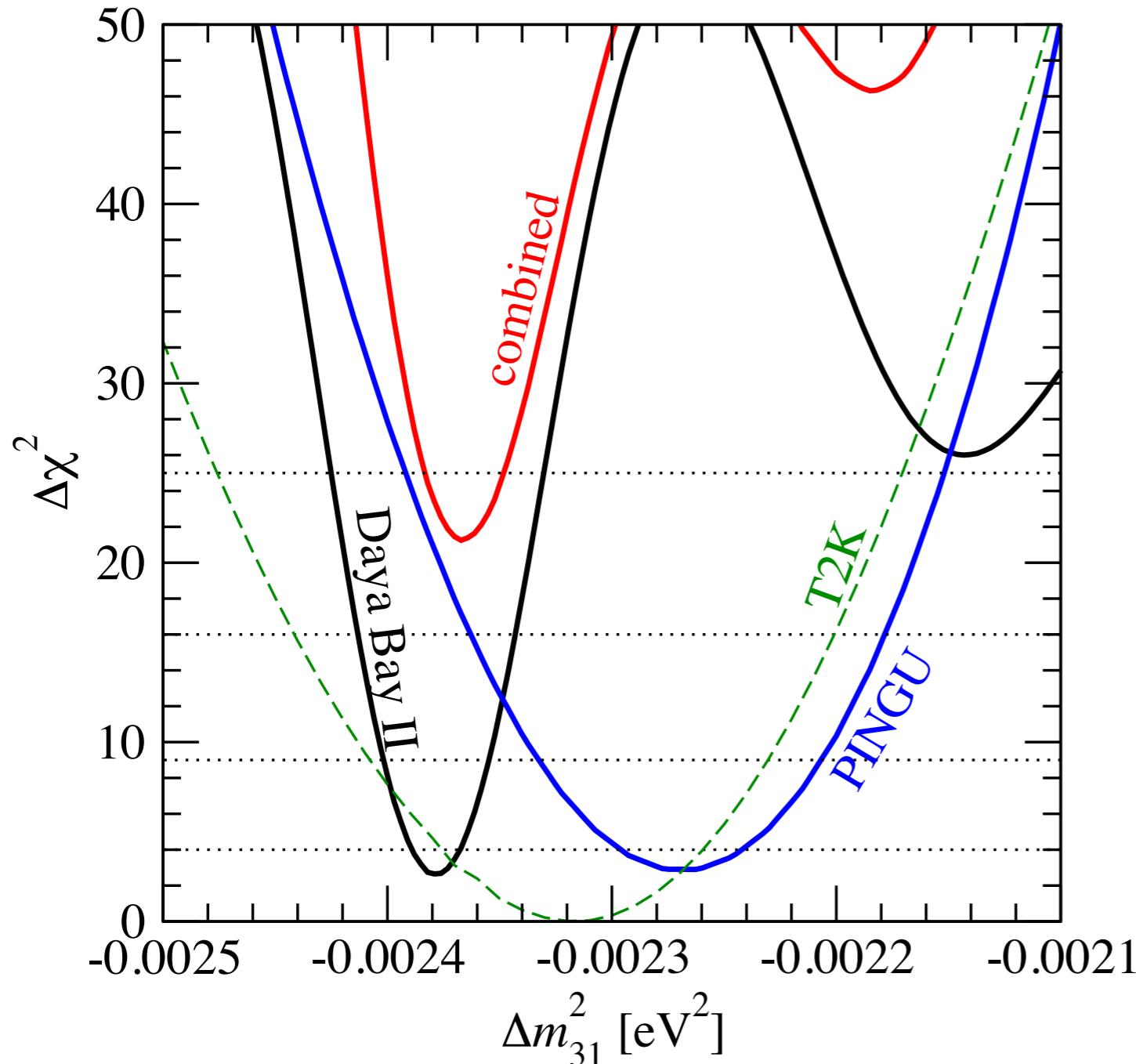
Blennow, Coloma, Huber, TS, I3/I.I.1822  
talk by M. Blennow, and many more

probability to exclude wrong ordering at  $3\sigma$   
("representative" selection of experiments)



- experimental parameters (event reconstruction abilities / energy scale) crucial (esp for PINGU, JUNO,...)
- LBL experiments: sens. depends on true values of  $\theta_{23}$  and  $\delta_{CP}$
- atmospheric neutrino expts.: true value of  $\theta_{23}$

# *Explore synergy between different experiments*

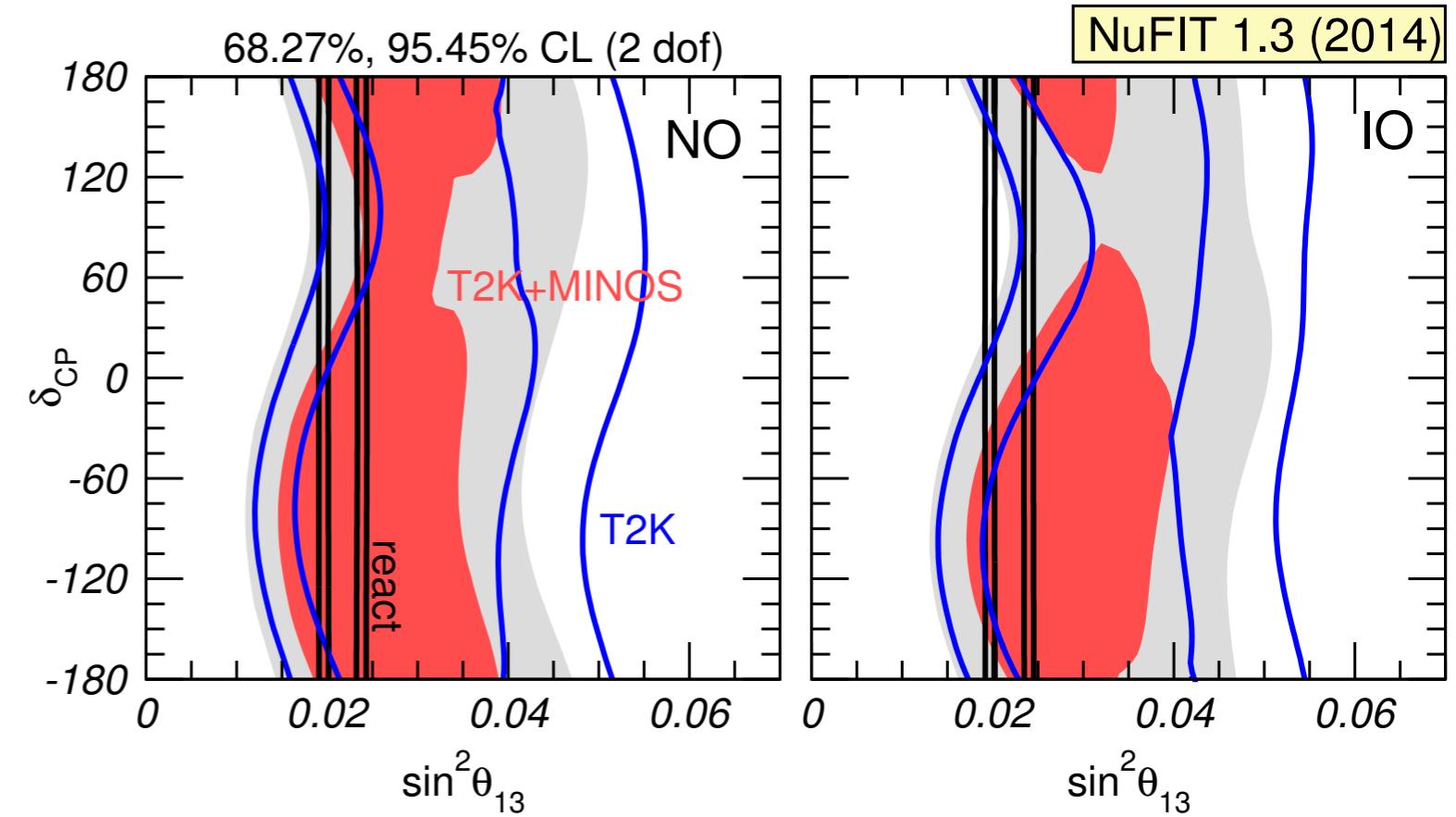
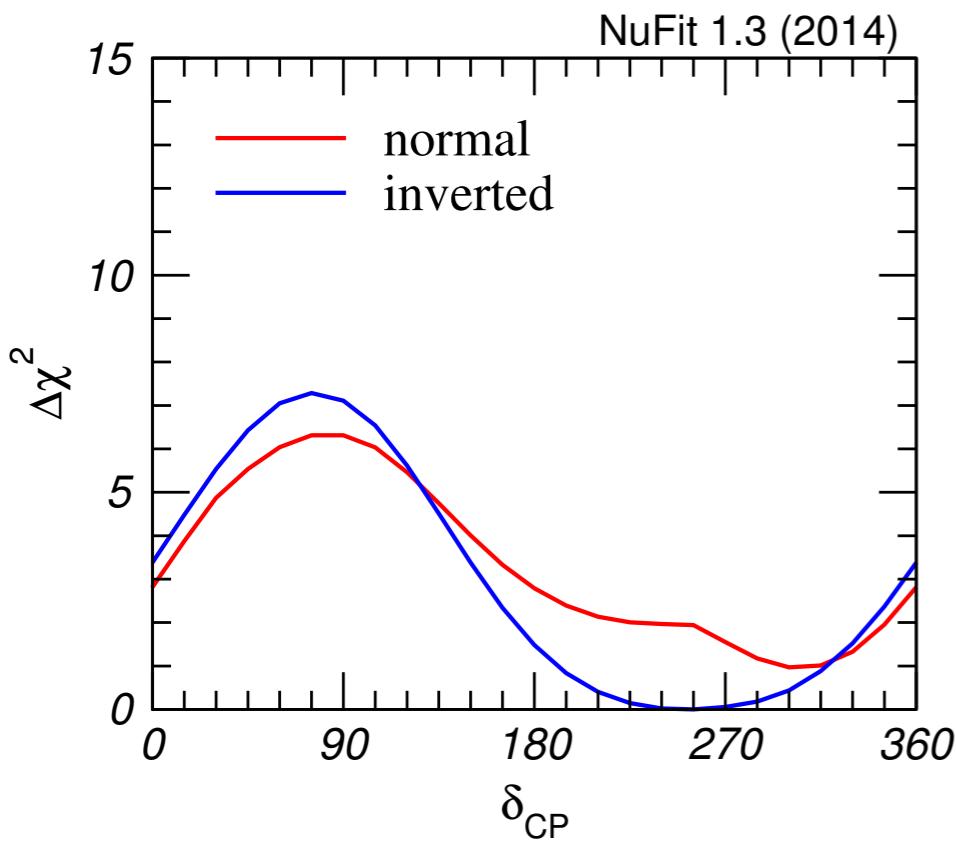


combine measurements  
of  $|\Delta m_{31}^2|$  from PINGU  
and JUNO

Blennow, Schwetz, arXiv:1306.3988

requires more careful  
investigations wrt to energy  
scale uncertainties - both for  
JUNO and PINGU!

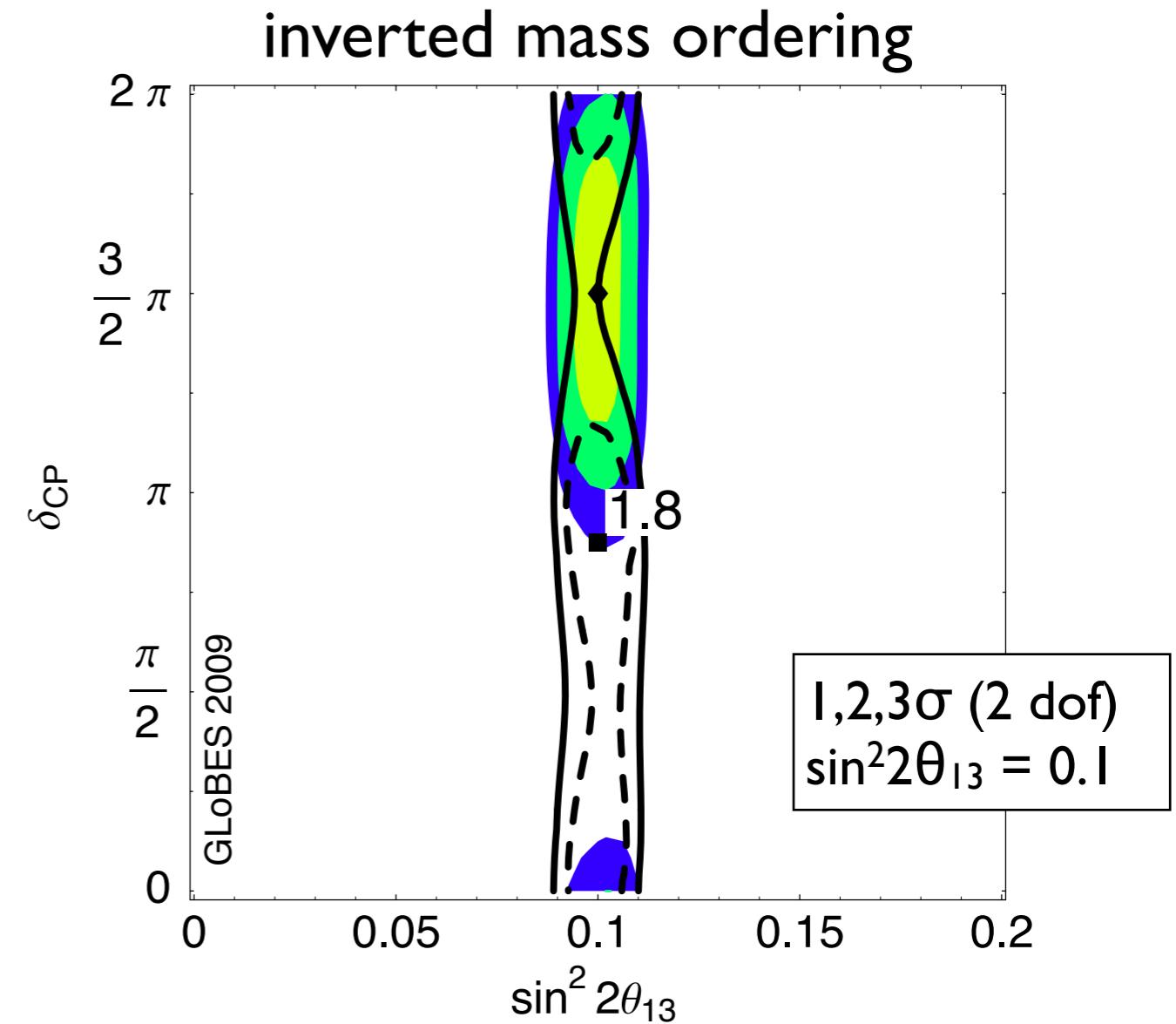
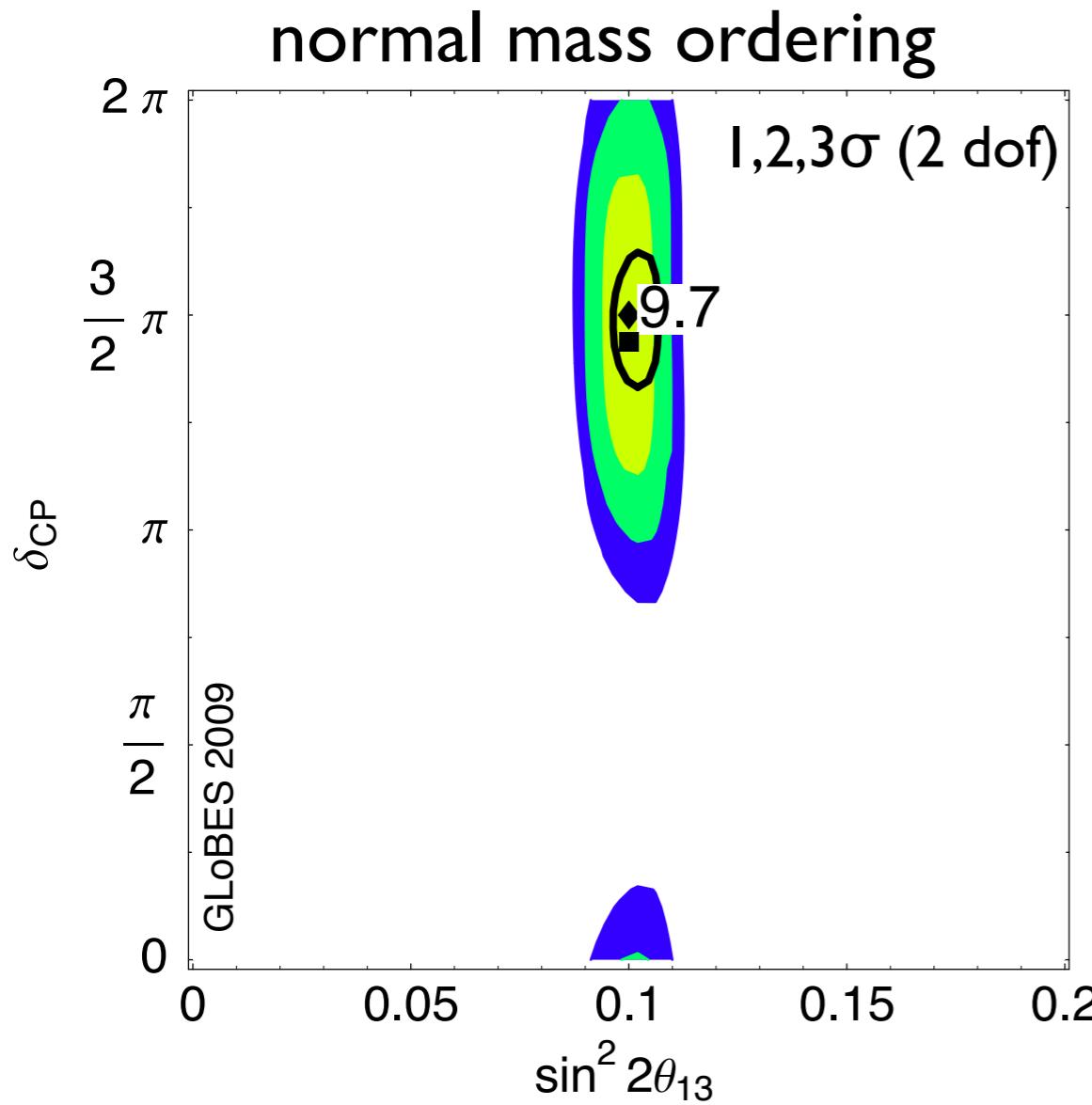
# *CP phase*



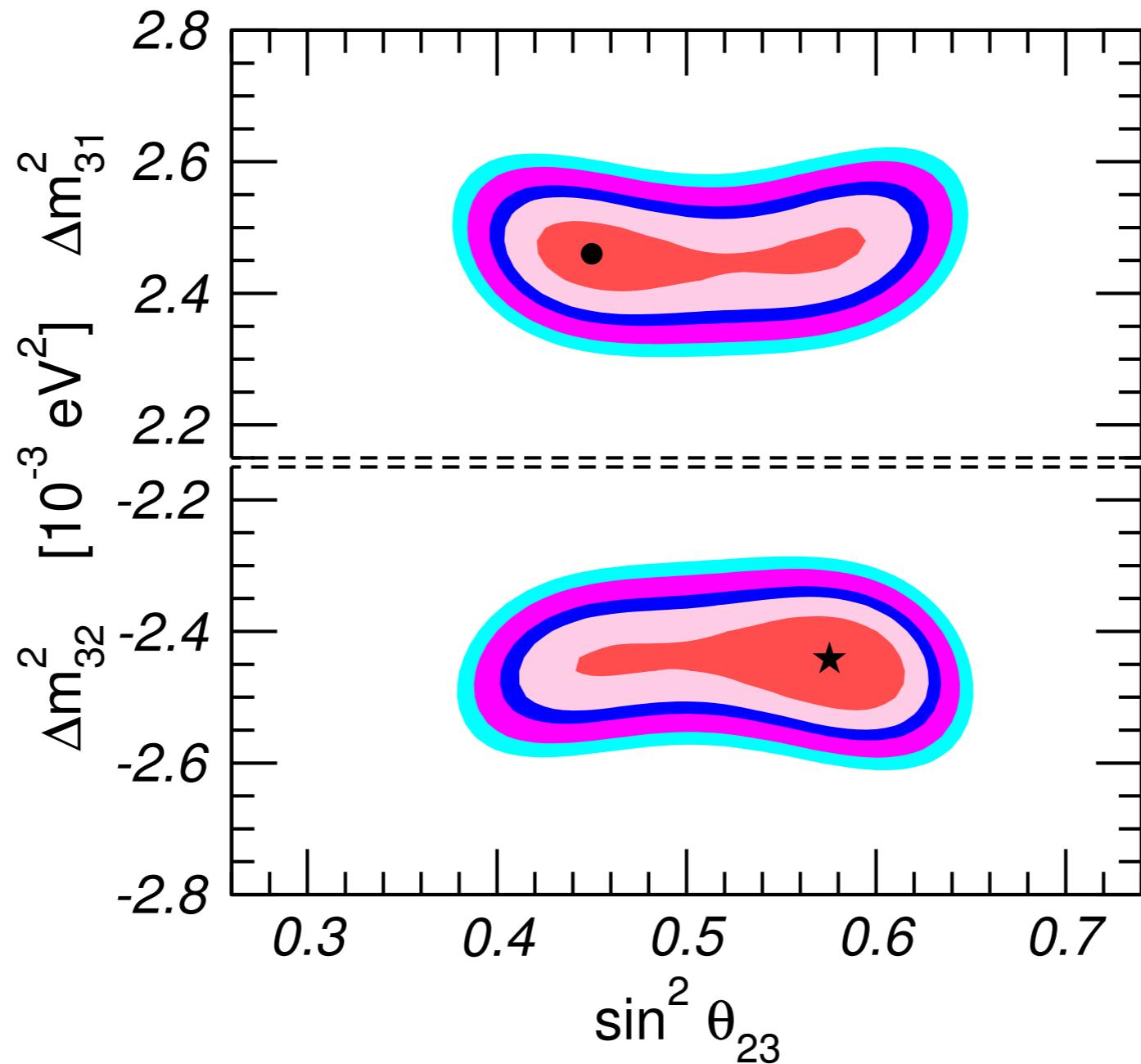
values of  $\delta_{CP} \sim 90^\circ$  disfavoured with  $\Delta\chi^2 \sim 7$   
emerges from interplay of T2K and reactor data

*Let's suppose that  $\delta_{CP} = 270^\circ$*

global fit ~2020:T2K, NOvA, DayaBay



# Octant of $\theta_{23}$



# *Interplay of Reactor + LBL appearance data*

$$\begin{aligned} P_{\mu e} \simeq & \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2(1-A)\Delta}{(1-A)^2} \\ & + \sin 2\theta_{13} \hat{\alpha} \sin 2\theta_{23} \frac{\sin(1-A)\Delta}{1-A} \frac{\sin A\Delta}{A} \cos(\Delta + \delta_{CP}) \\ & + \hat{\alpha}^2 \cos^2 \theta_{23} \frac{\sin^2 A\Delta}{A^2} \end{aligned}$$

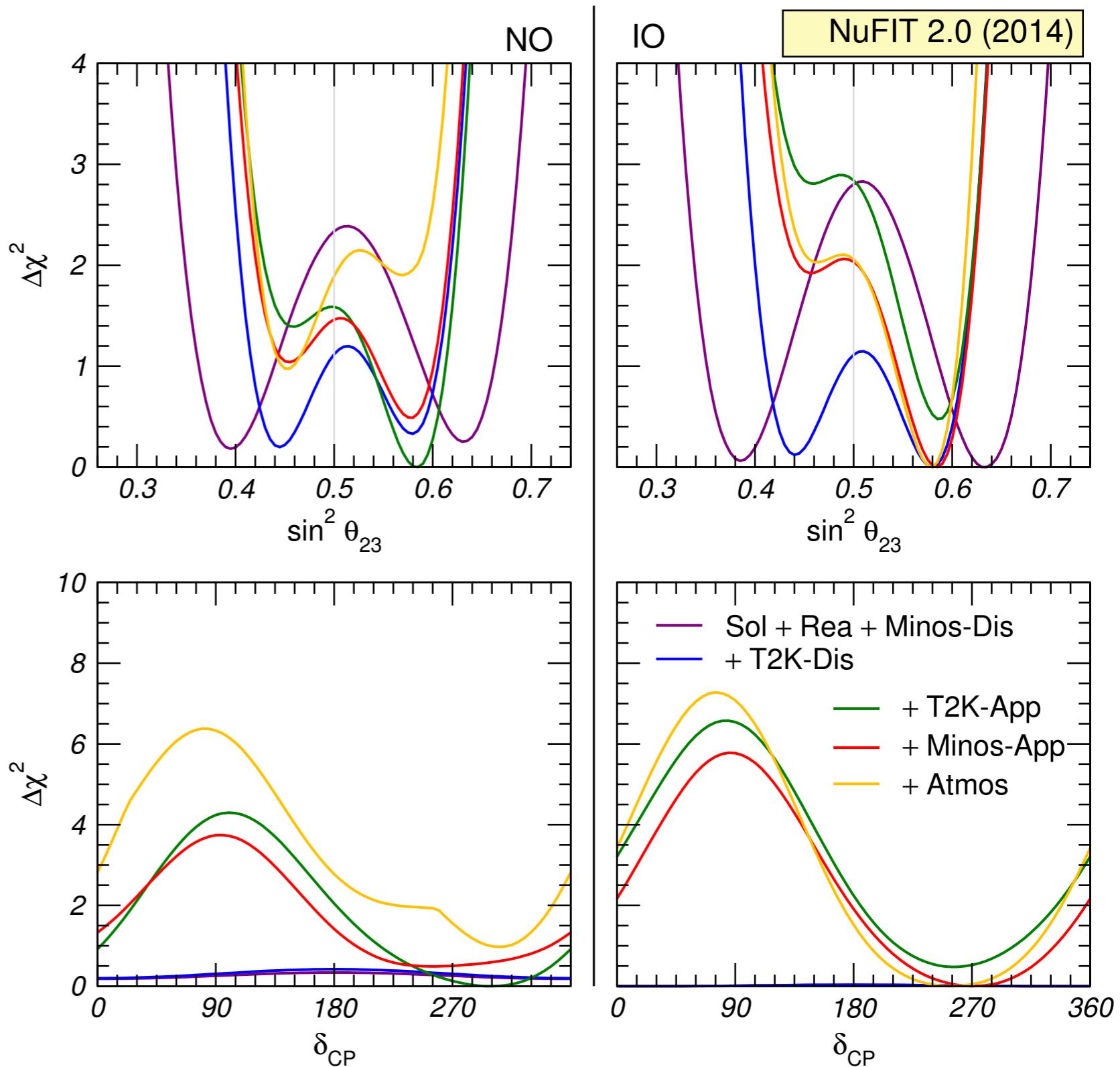
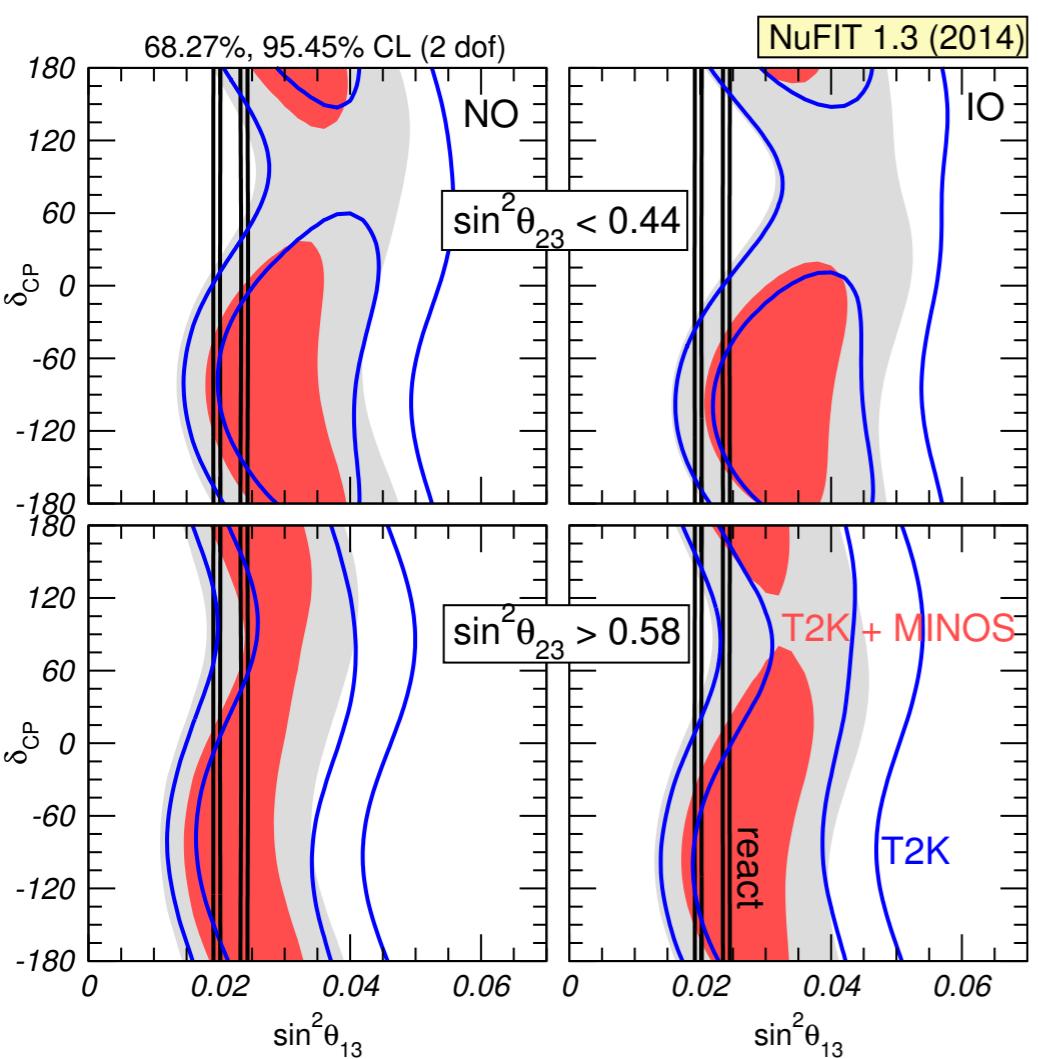
with

$$\Delta \equiv \frac{\Delta m_{31}^2 L}{4E_\nu}, \quad \hat{\alpha} \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \sin 2\theta_{12}, \quad A \equiv \frac{2E_\nu V}{\Delta m_{31}^2}$$

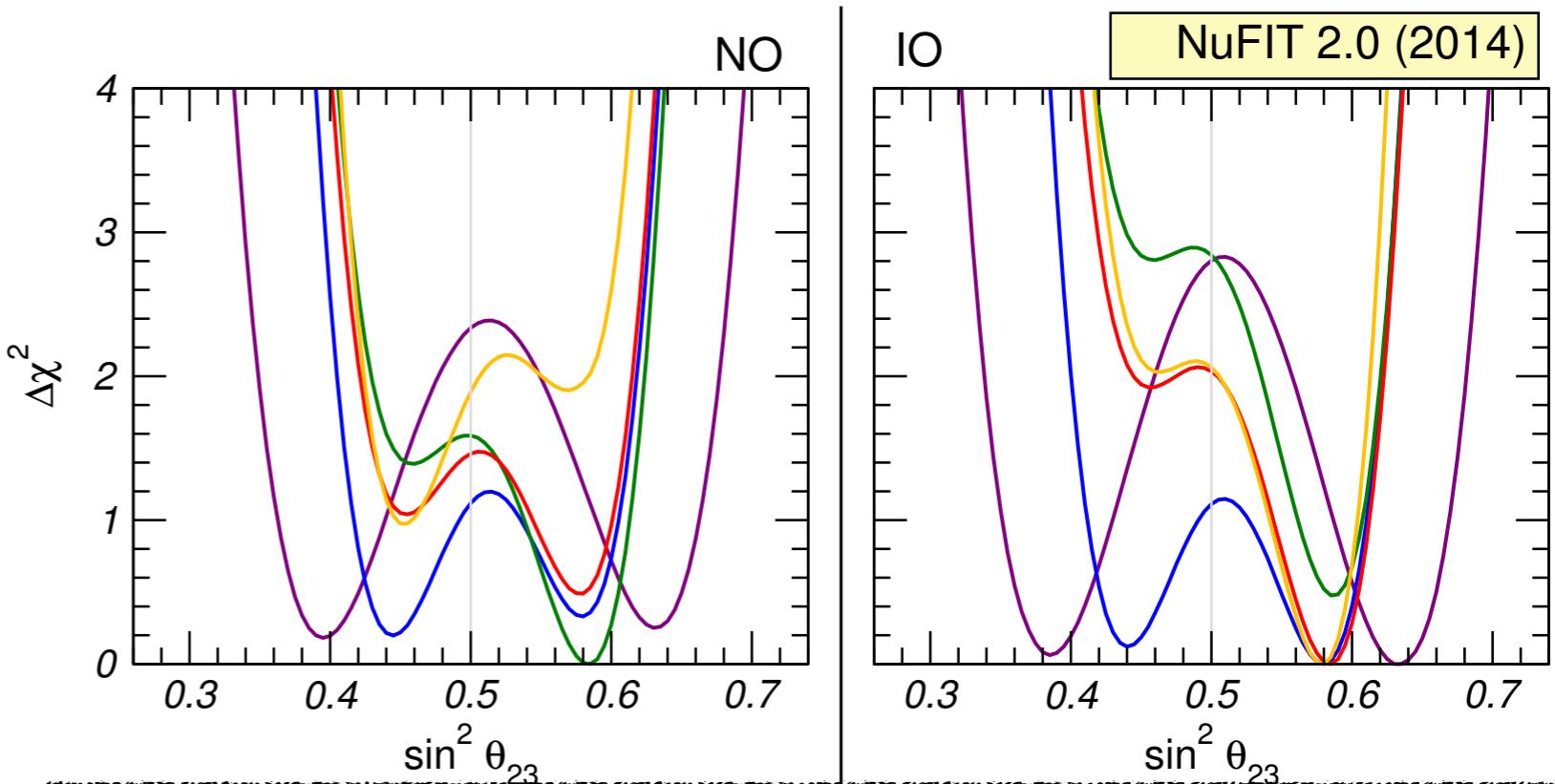
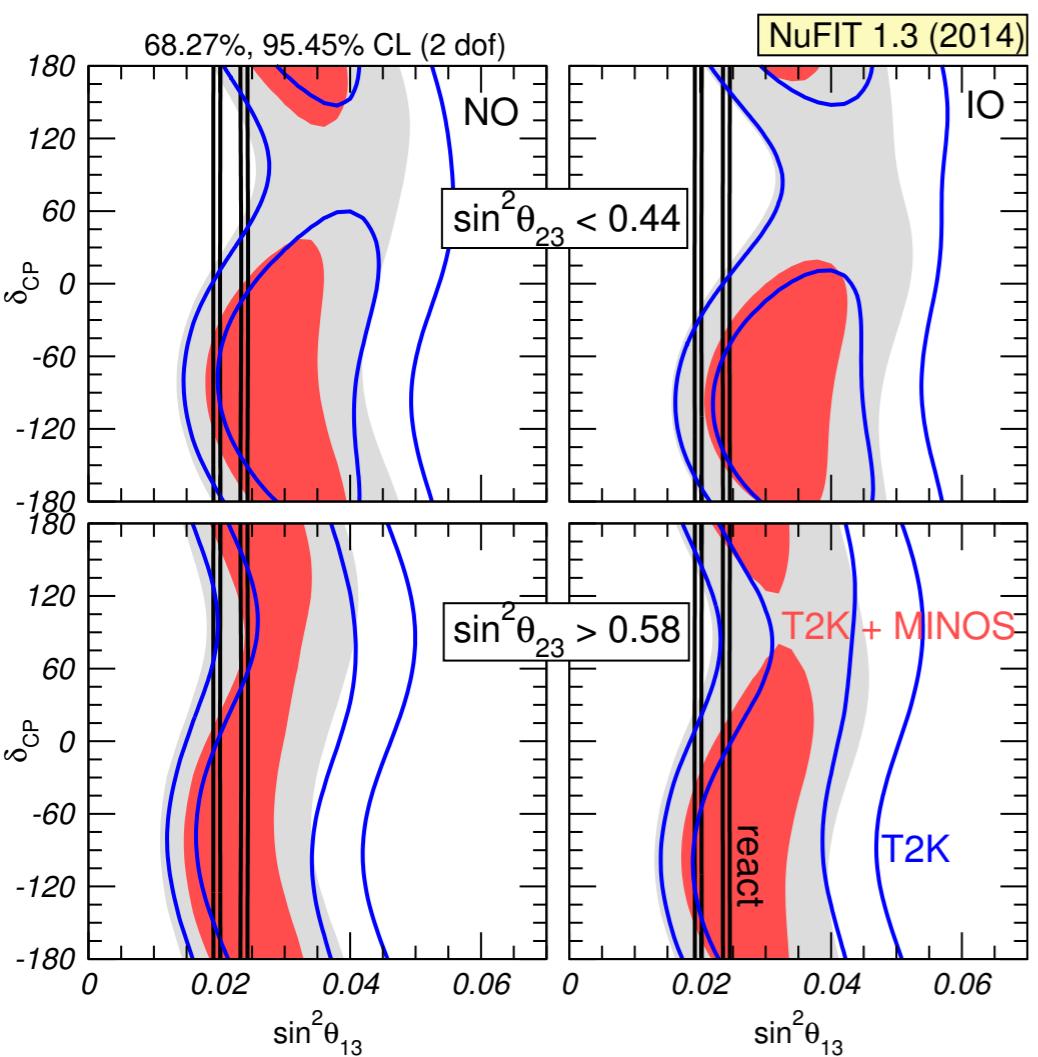
- for large  $\theta_{13}$  the leading term depends on octant
- beam+reactor combination may be sensitive to octant

Minakata et al. hep-ph/0211111; McConnel, Shaevitz, hep-ex/0409028

# *CP phase vs octant of $\theta_{23}$*



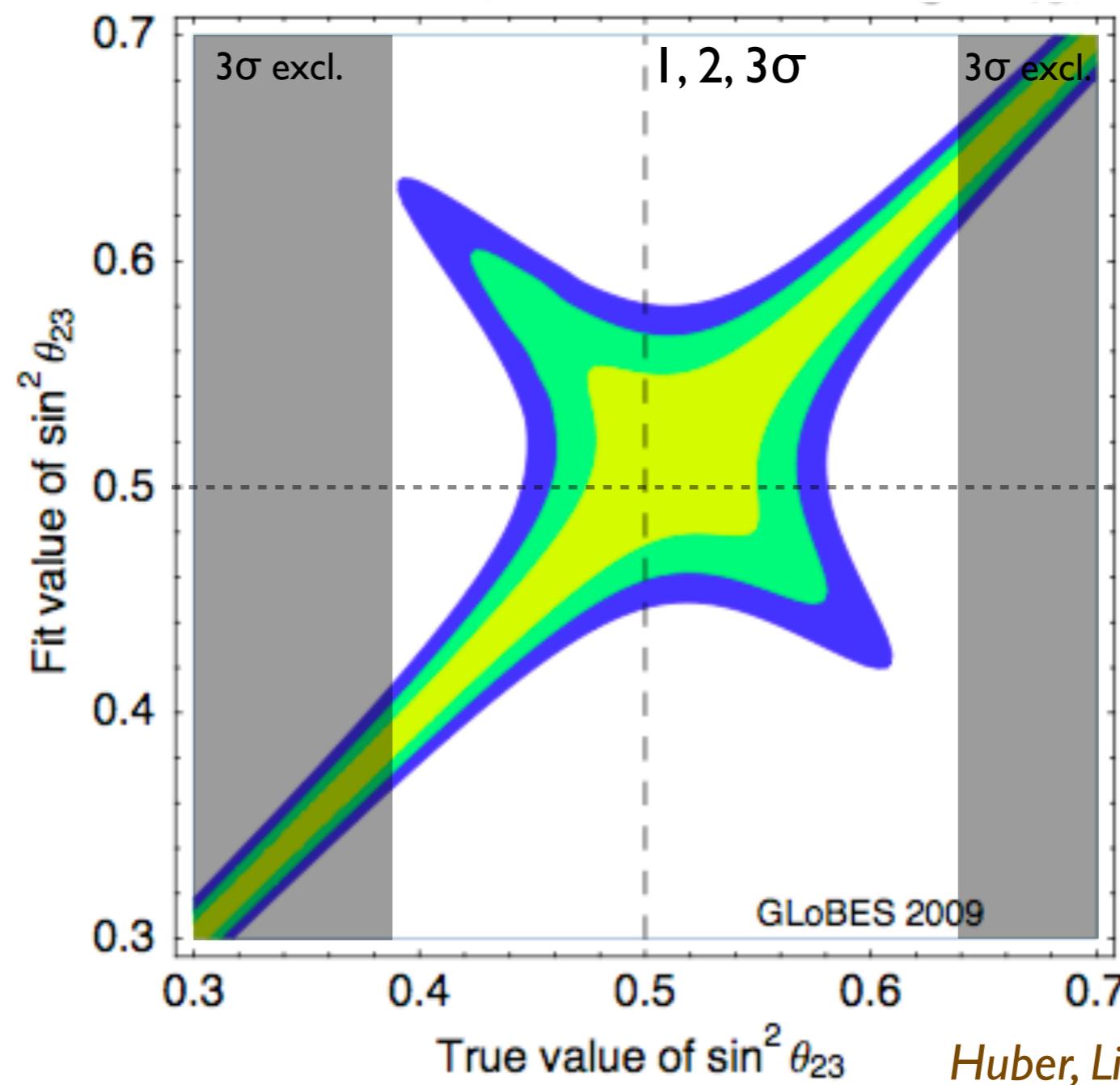
# *CP phase vs octant of $\theta_{23}$*



- some “tendencies” appear at low significance ( $\Delta\chi^2 \sim 3$ )
- Reactor + LBL appearance prefer second octant
- for NO atmospheric data pushes best fit point to first octant

# *Global fit ~2020 - $\theta_{23}$ octant*

T2K, NOvA, DayaBay

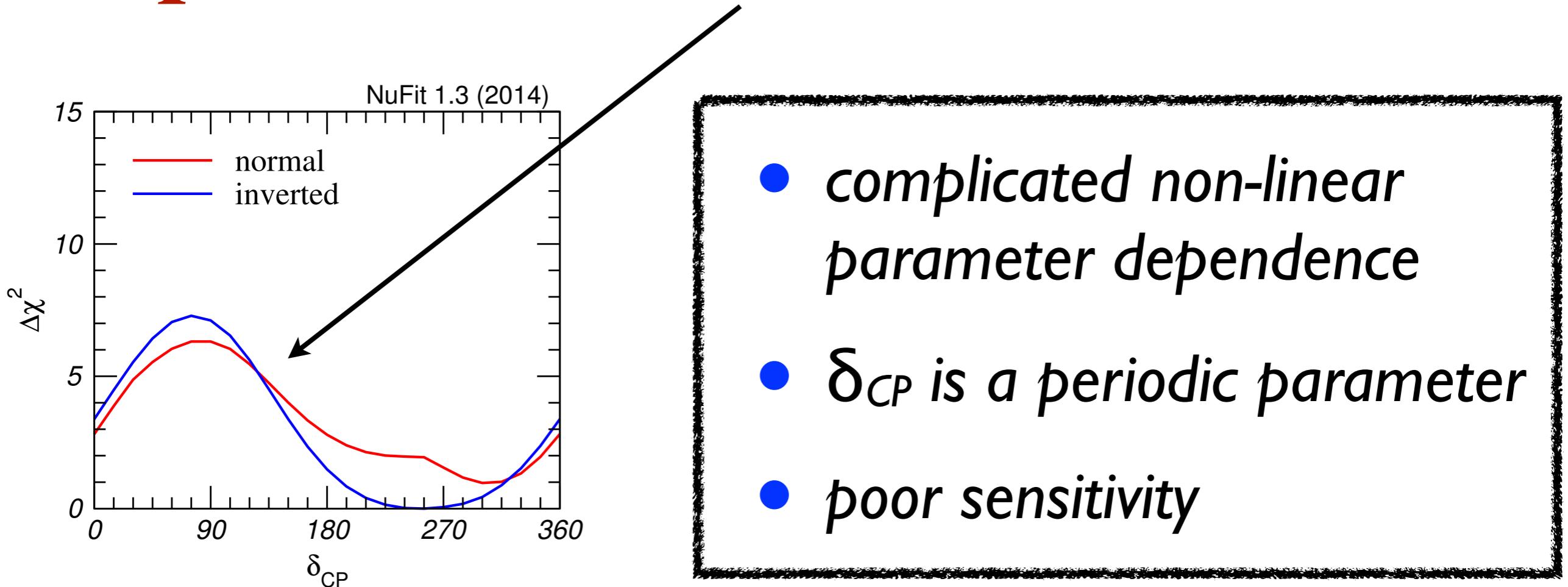


$$\sin^2 2\theta_{13} = 0.1$$

$\delta_{CP} = 0$   
(may change for  
other values)

*Huber, Lindner, TS, Winter, 0907.1896*

# *CP phase - what is the CL?*



usual  $\Delta\chi^2$  approximations may not be valid

Schwetz, hep-ph/0612223

Blennow, Coloma, Fernandez-Martinez, 1407.3274

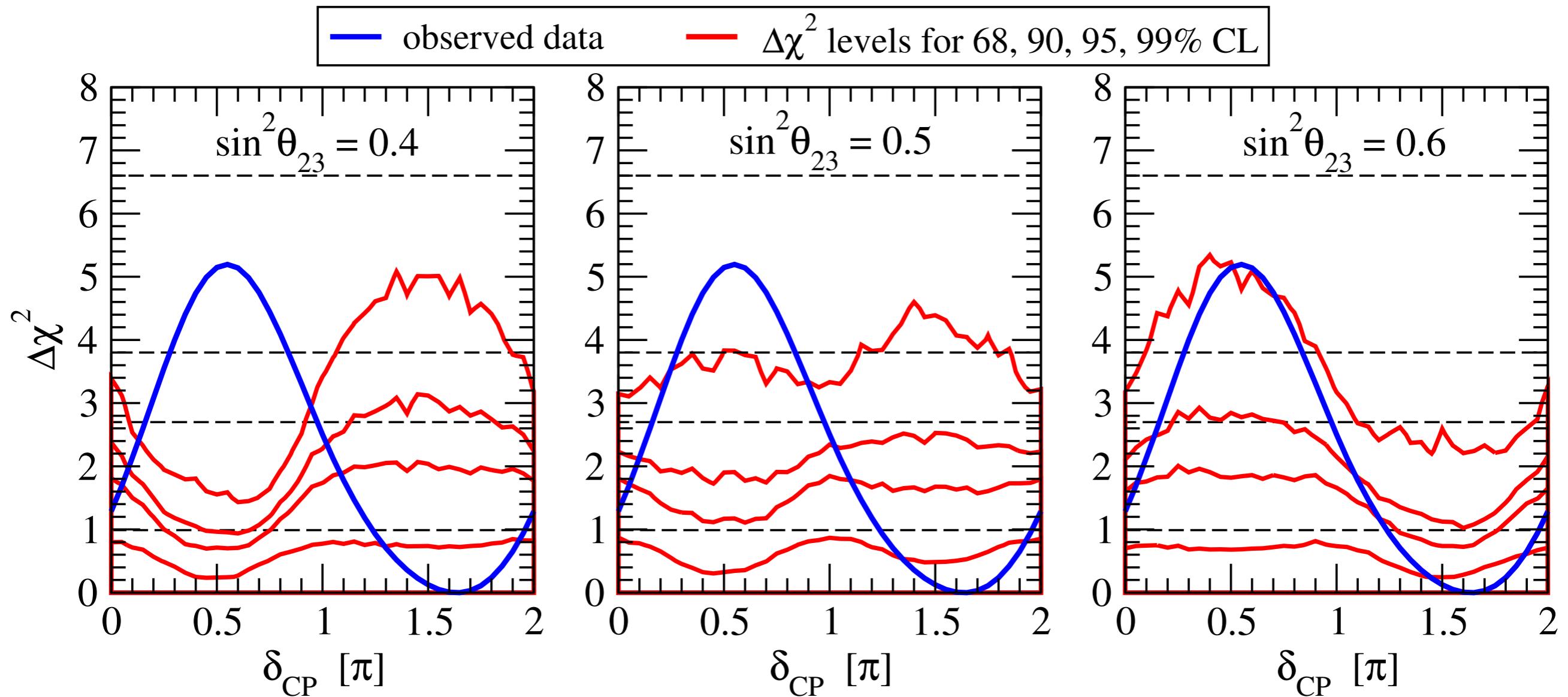
talk by M. Blennow

# *CP phase - what is the CL?*

generate pseudo data for T2K (appear + disappear)

check distribution of  $\Delta\chi^2$

consider  $\delta_{\text{CP}}$  and  $\theta_{23}$  as free parameters (all others fixed, incl NO)

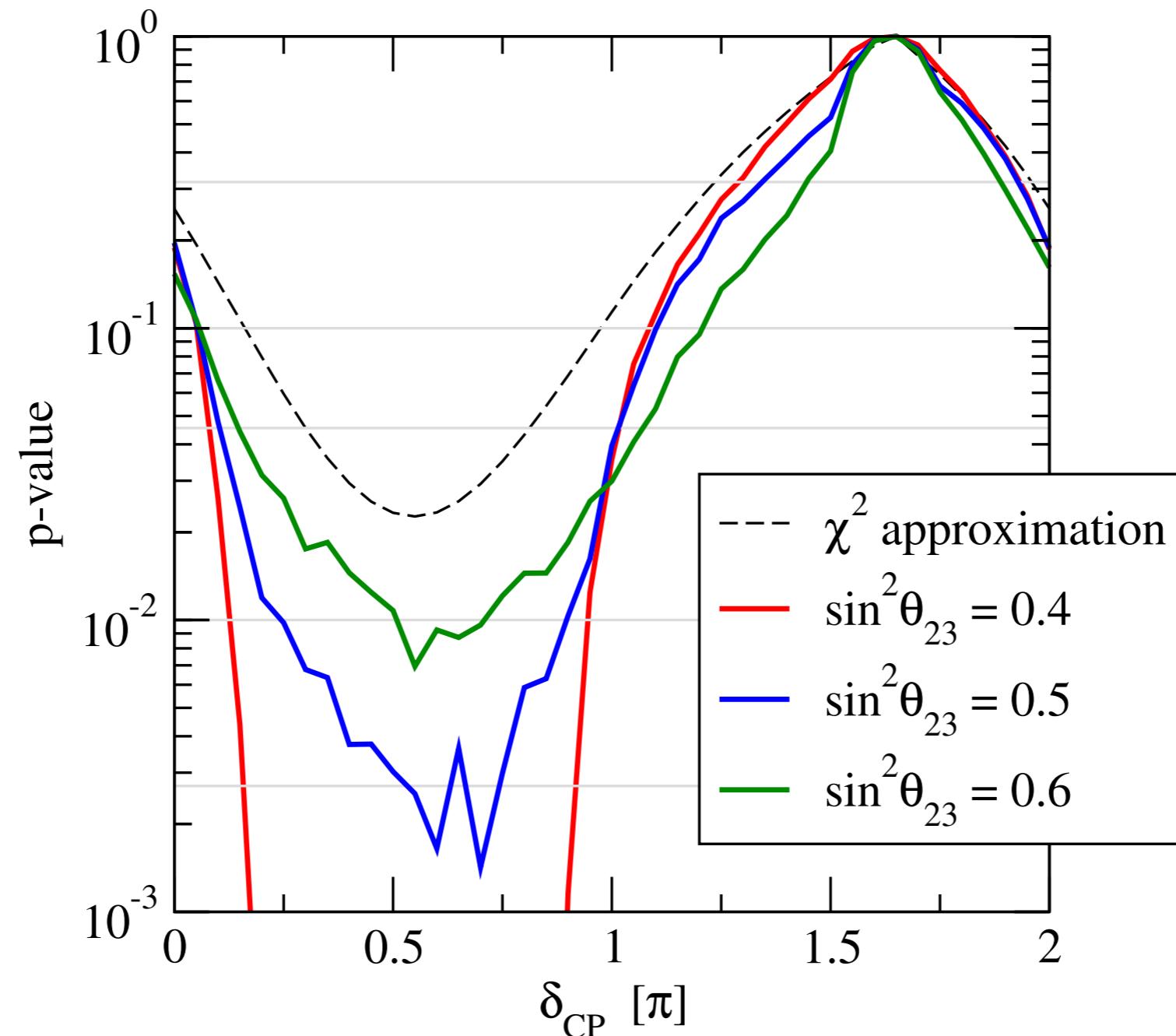


# *CP phase - what is the CL?*

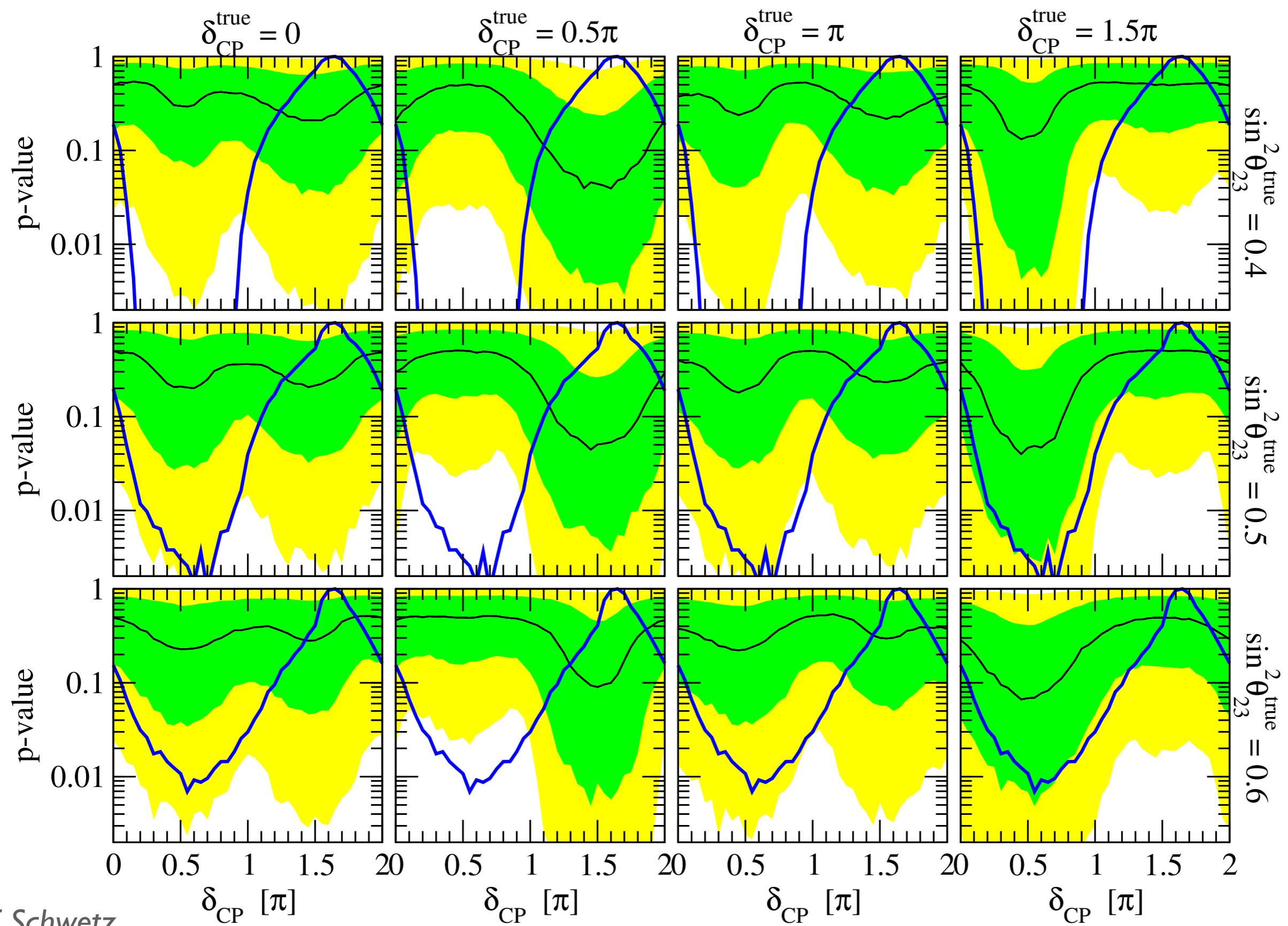
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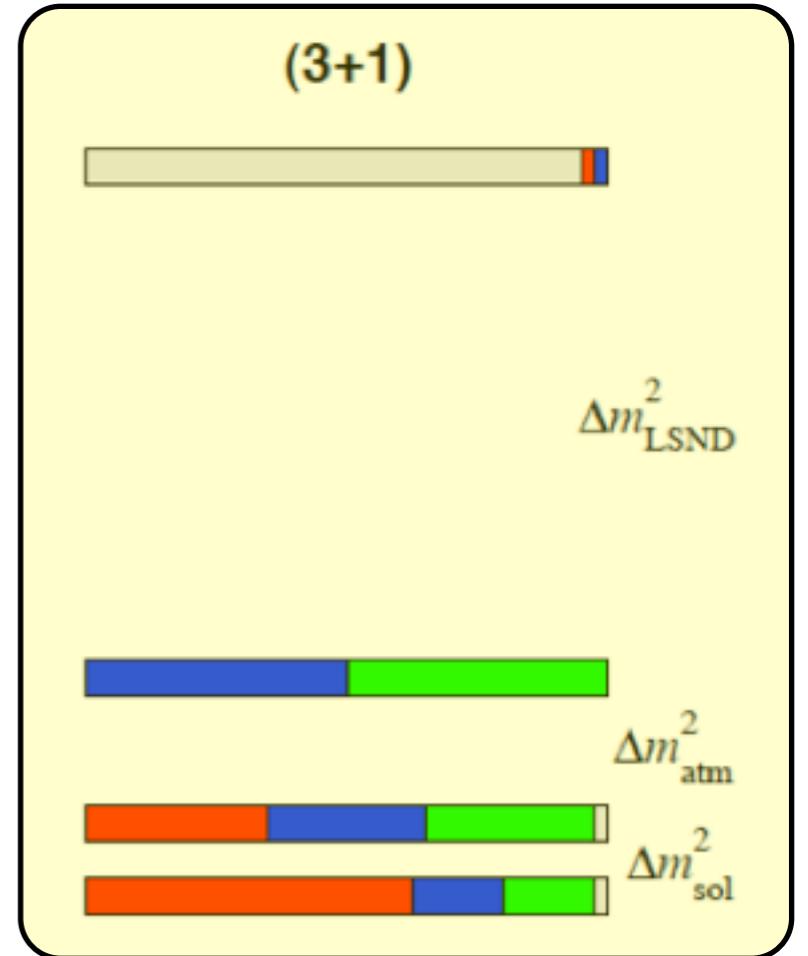
# Expected sensitivity



# Anomalies at the $E/L \sim eV^2$ scale

- Reactor anomaly ( $\bar{\nu}_e$  disappearance)
- Gallium anomaly ( $\nu_e$  disappearance)
- LSND ( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  appearance)
- MiniBooNE ( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ,  $\nu_\mu \rightarrow \nu_e$  appearance)

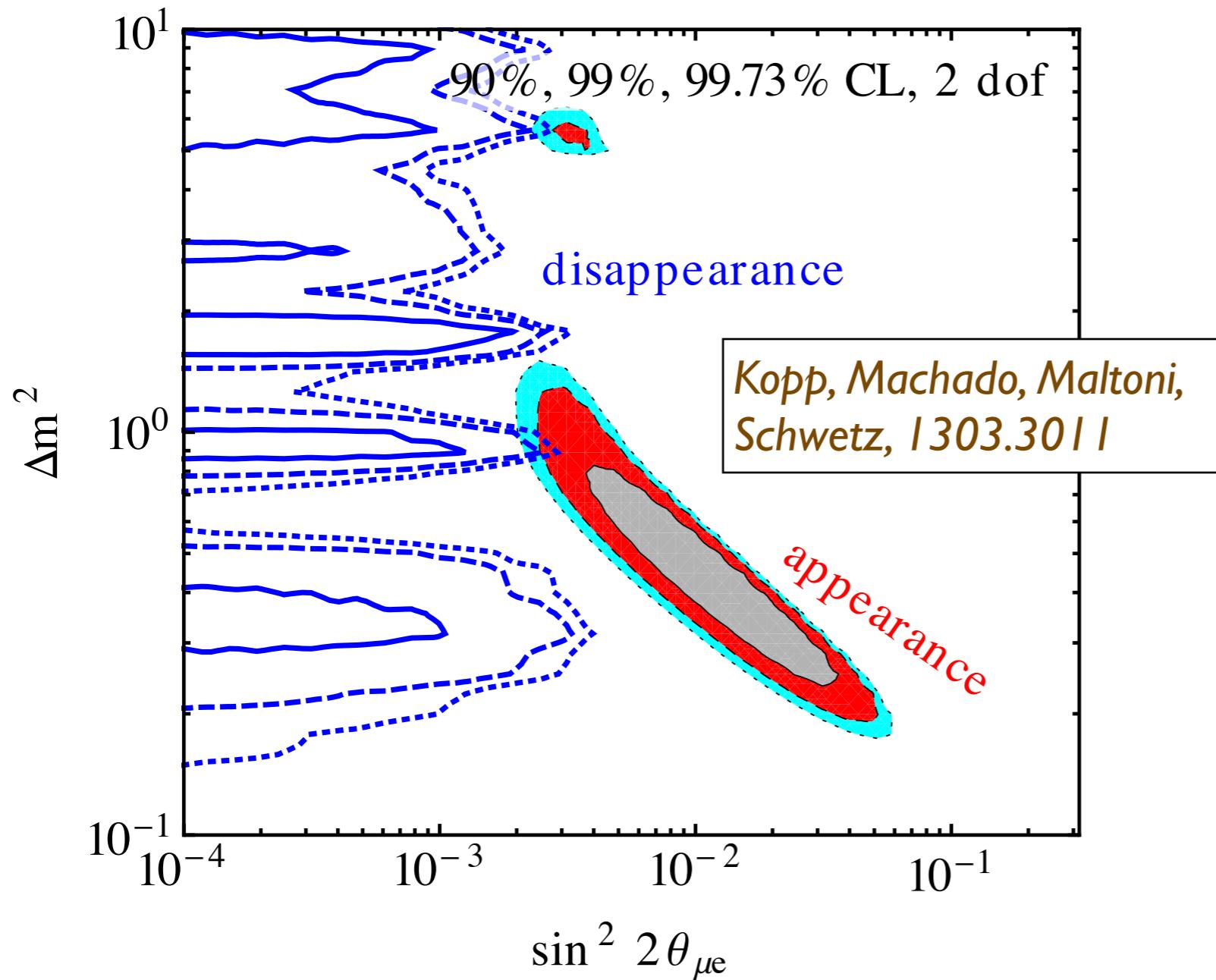
$$\sin^2 2\theta_{\mu e} \approx \frac{1}{4} \sin^2 2\theta_{ee} \sin^2 2\theta_{\mu\mu}$$



- no hint for  $\nu_\mu$  disappearance  
limits from SK, CDHS, MiniBooNE, MINOS

# *Strong tension in global data*

- consistency of appearance and disappearance data with  $p$ -value  $10^{-4}$



expect somewhat increased tension due to recent data from MINOS, SK-atm, ICARUS, OPERA

C. Giunti et al find somewhat better fit: p-value  $10^{-3}$  1308.5288

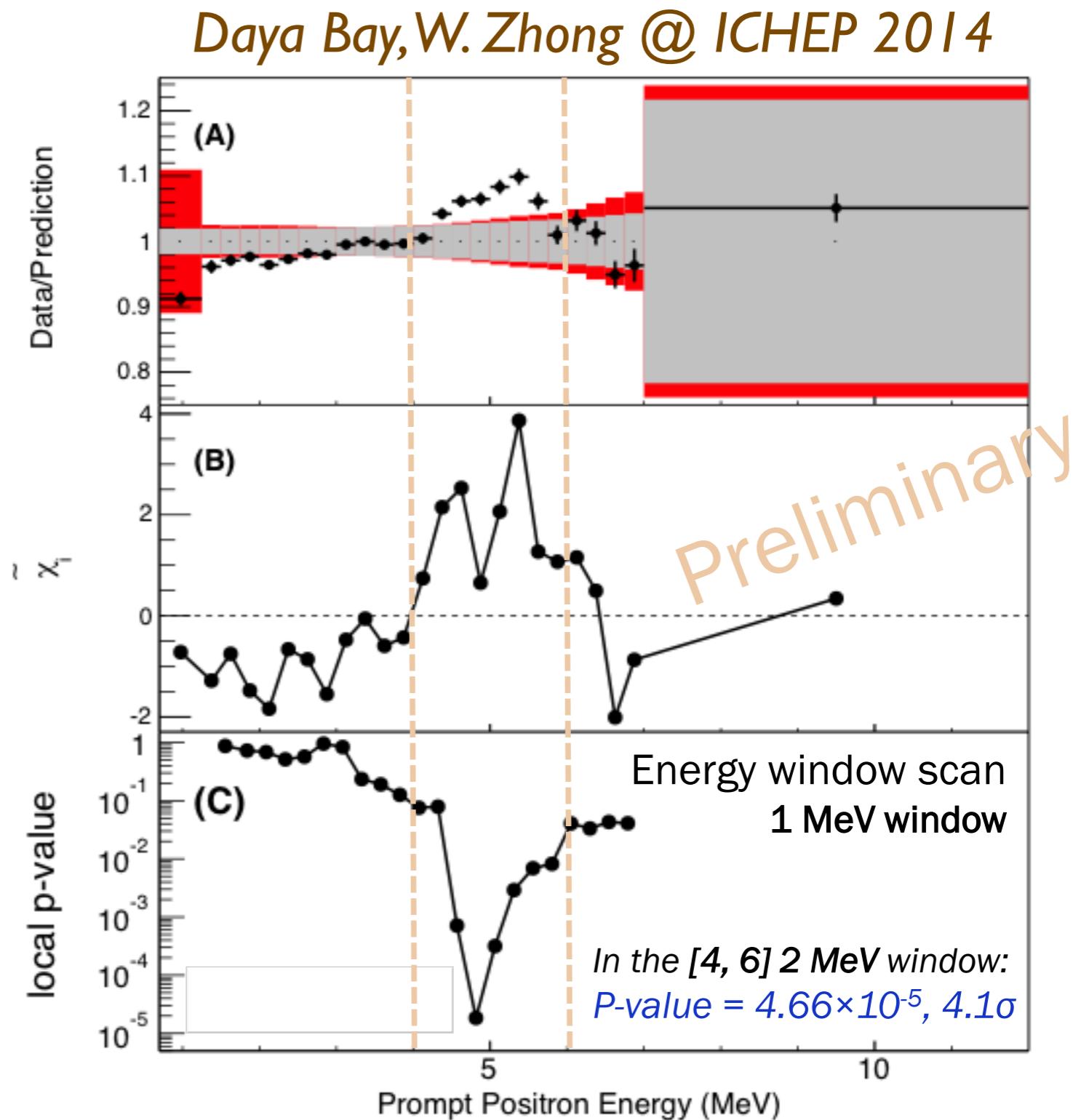
# *Remark on reactor anomaly*

“unexpected” bump in reactor neutrino spectrum

also seen in RENO,  
DoubleChooz, Chooz

bump seems to be present in ab-initio calculations of the anti-nu spectrum, but problems with beta-spectr?

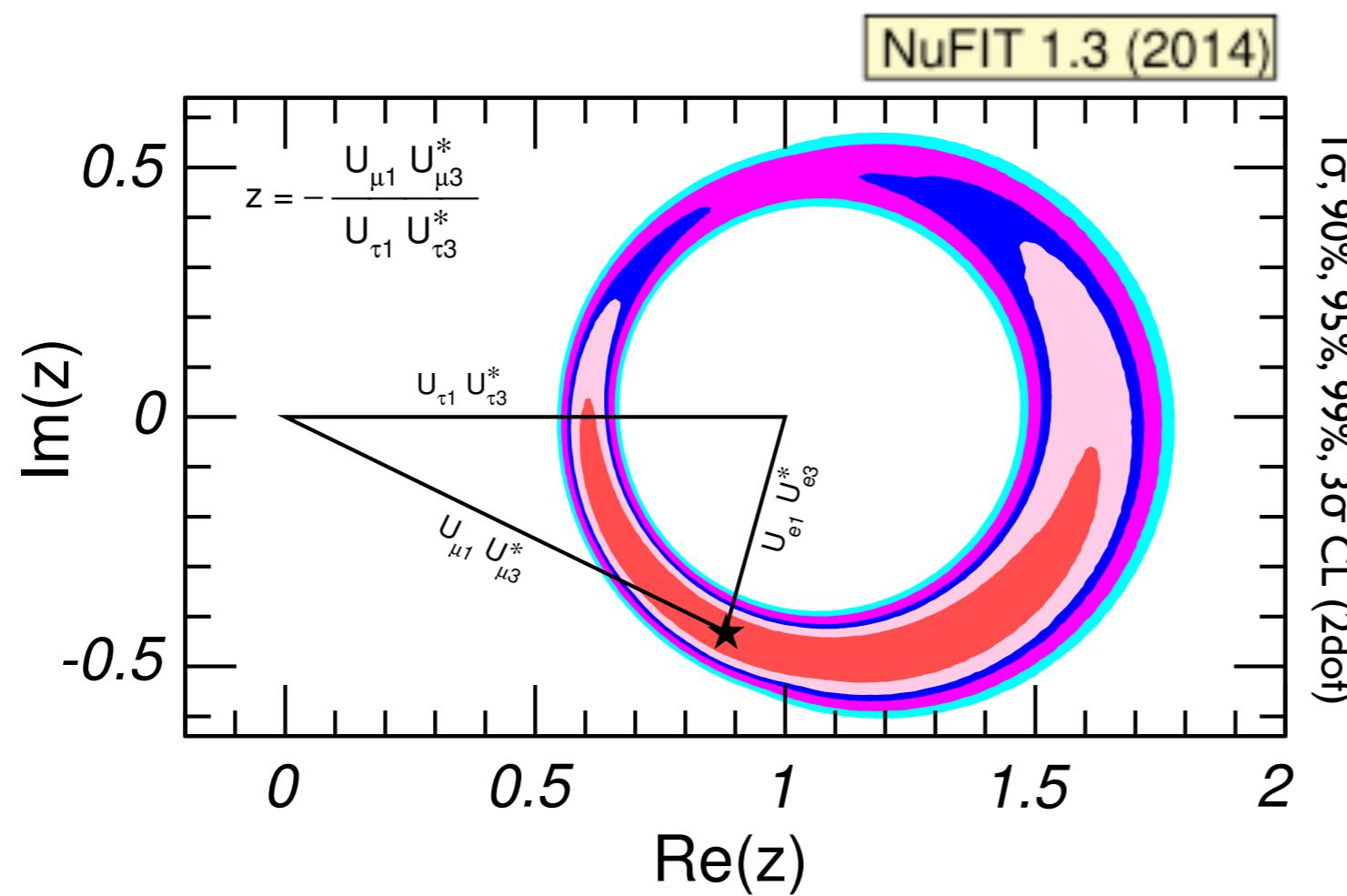
Dwyer, Langford, 1407.1281



# *Sterile neutrinos at the eV-scale?*

- *It is important to clarify “anomalies”*
- *hints for appearance experiments (LSND, MiniBooNE) are in strong tension with disappearance data*
- *reactor anomaly relies on complicated nuclear physics calculations and/or historical data - seem not under sufficient control to predict neutrino spectrum at %-level precision*

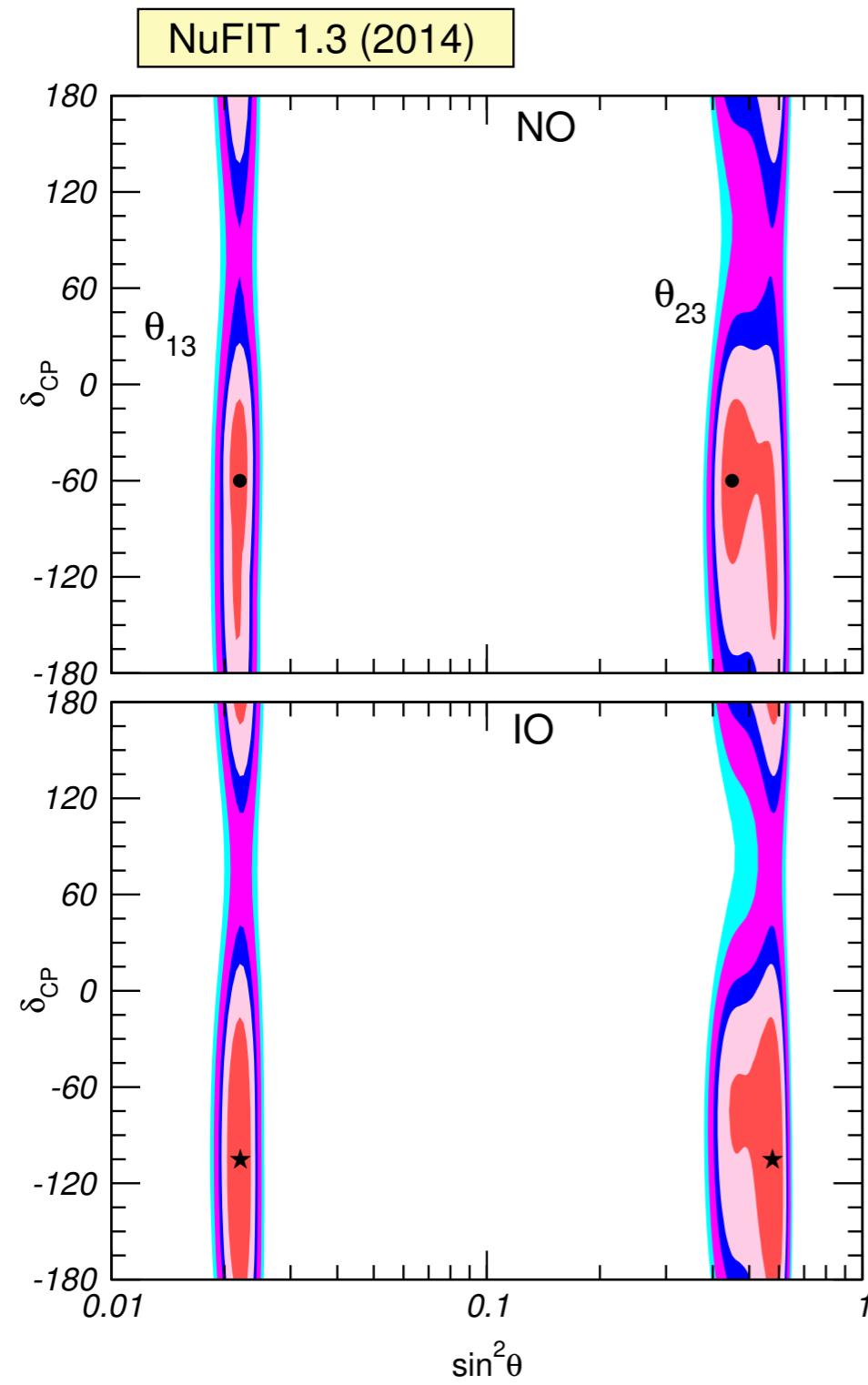
*Thank you for your attention!*



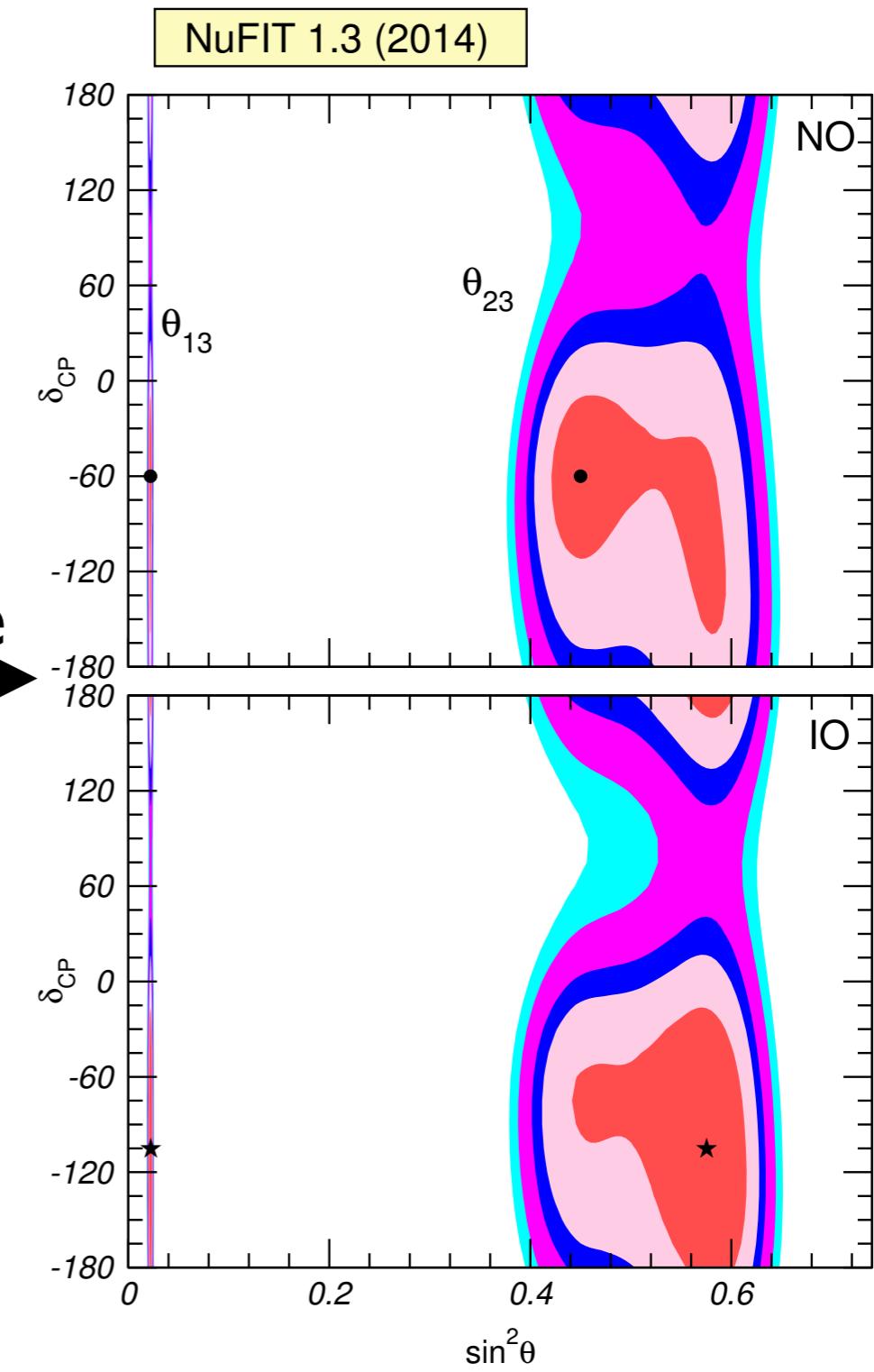
# *Additional slides*

# *CP phase vs $\theta_{23}$*

Minakata, Parke, I303.6178  
Coloma, Minakata, Parke, I406.2551

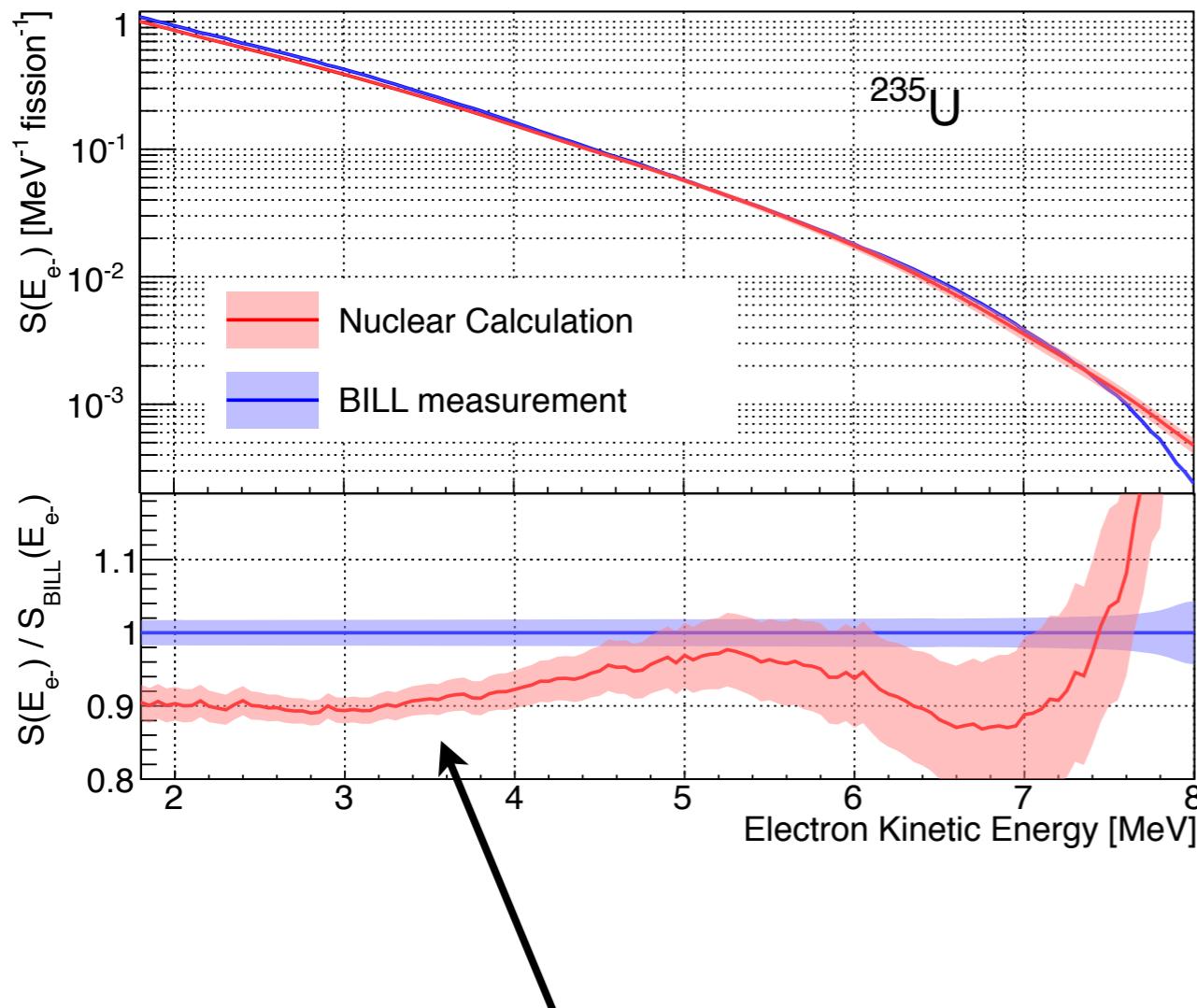


linear scale

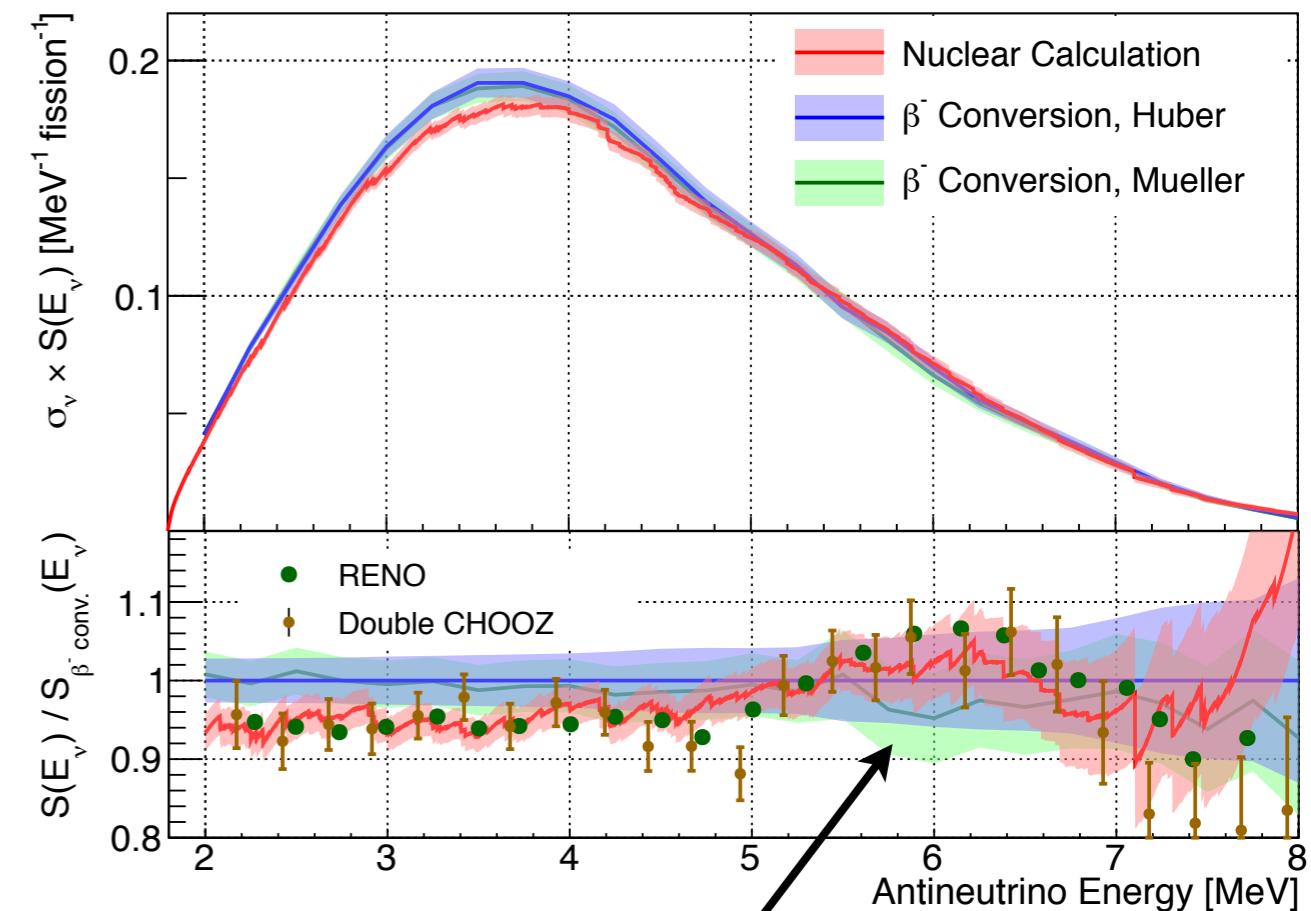


# *new ab-initio calculations*

Dwyer, Langford, I407.I28I



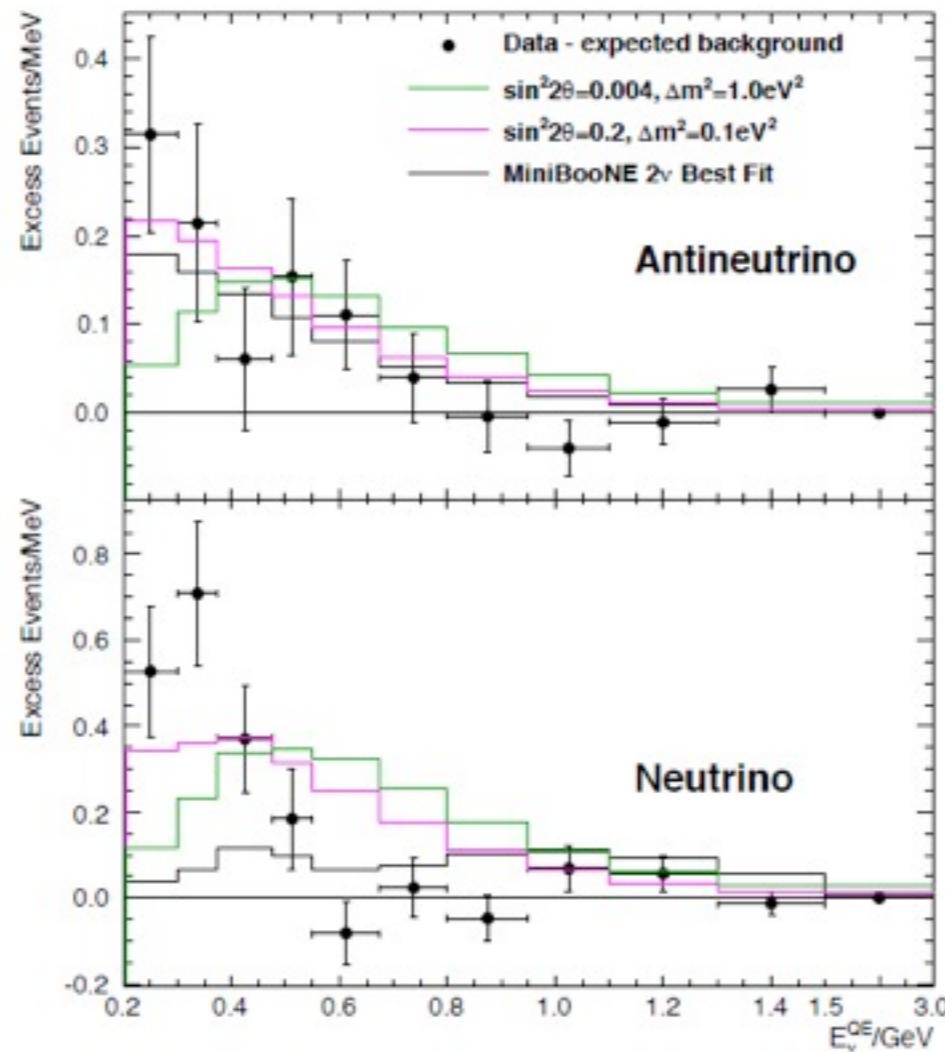
fails to predict beta spectr by ~10%



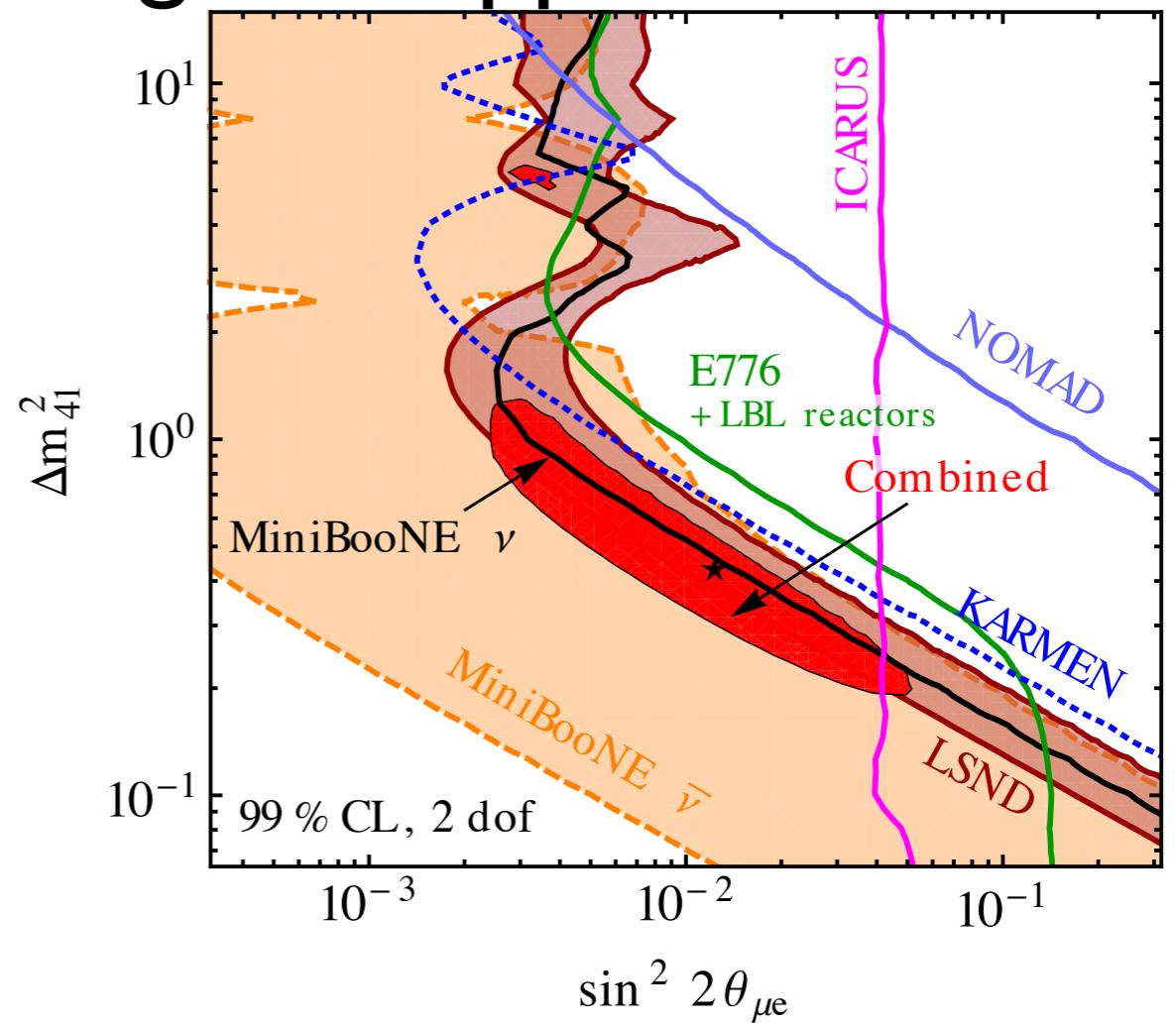
predicts bump around 6 MeV in  
agreement with data

# $\nu_\mu \rightarrow \nu_e$ hints from LSND & MiniBooNE

## MiniBooNE data



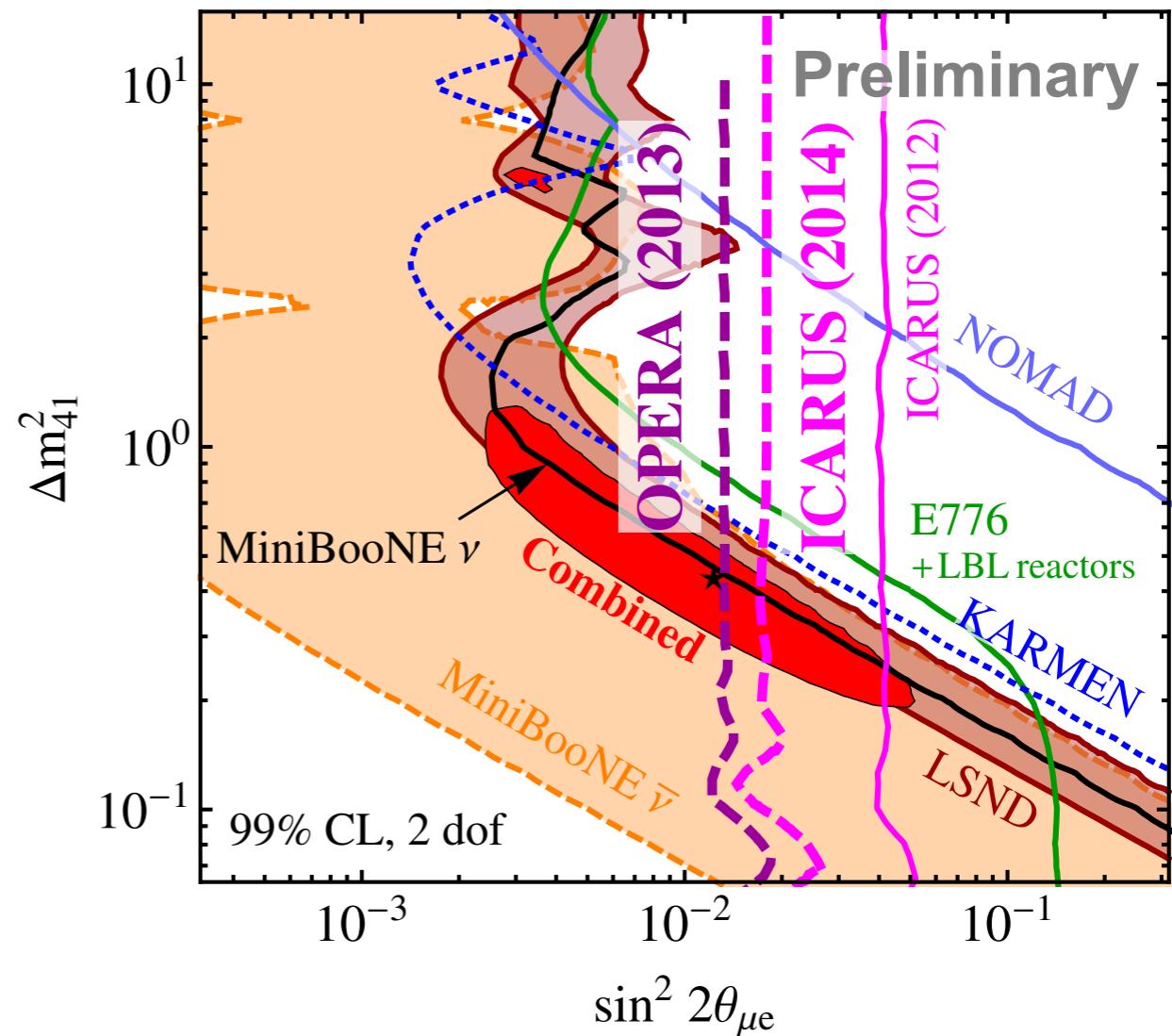
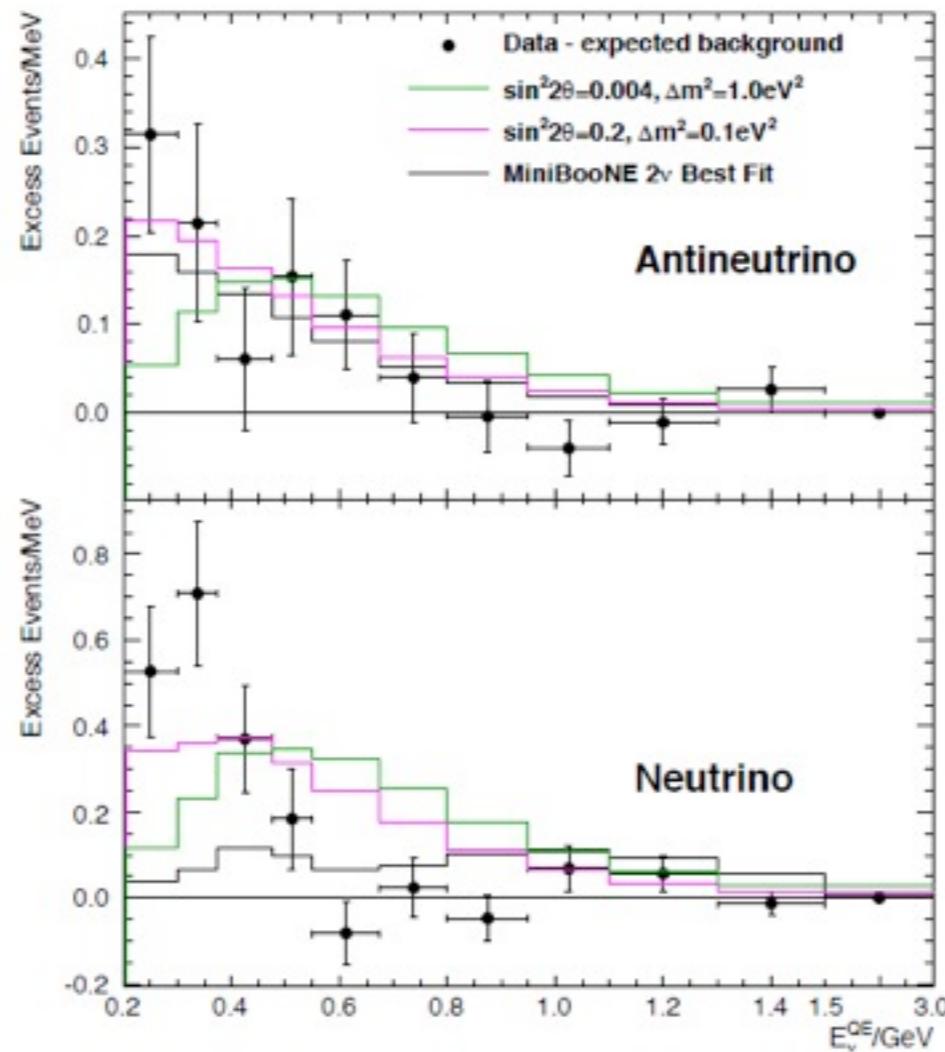
## global appearance data



- LSND signal at  $3.8\sigma$
- MB antineutrino excess ( $2.8\sigma$ ) consistent with oscillations
- MB neutrino excess ( $3.4\sigma$ ) marginally consistent with osc. ( $p$ -value 6.1%)

# $\nu_\mu \rightarrow \nu_e$ hints from LSND & MiniBooNE

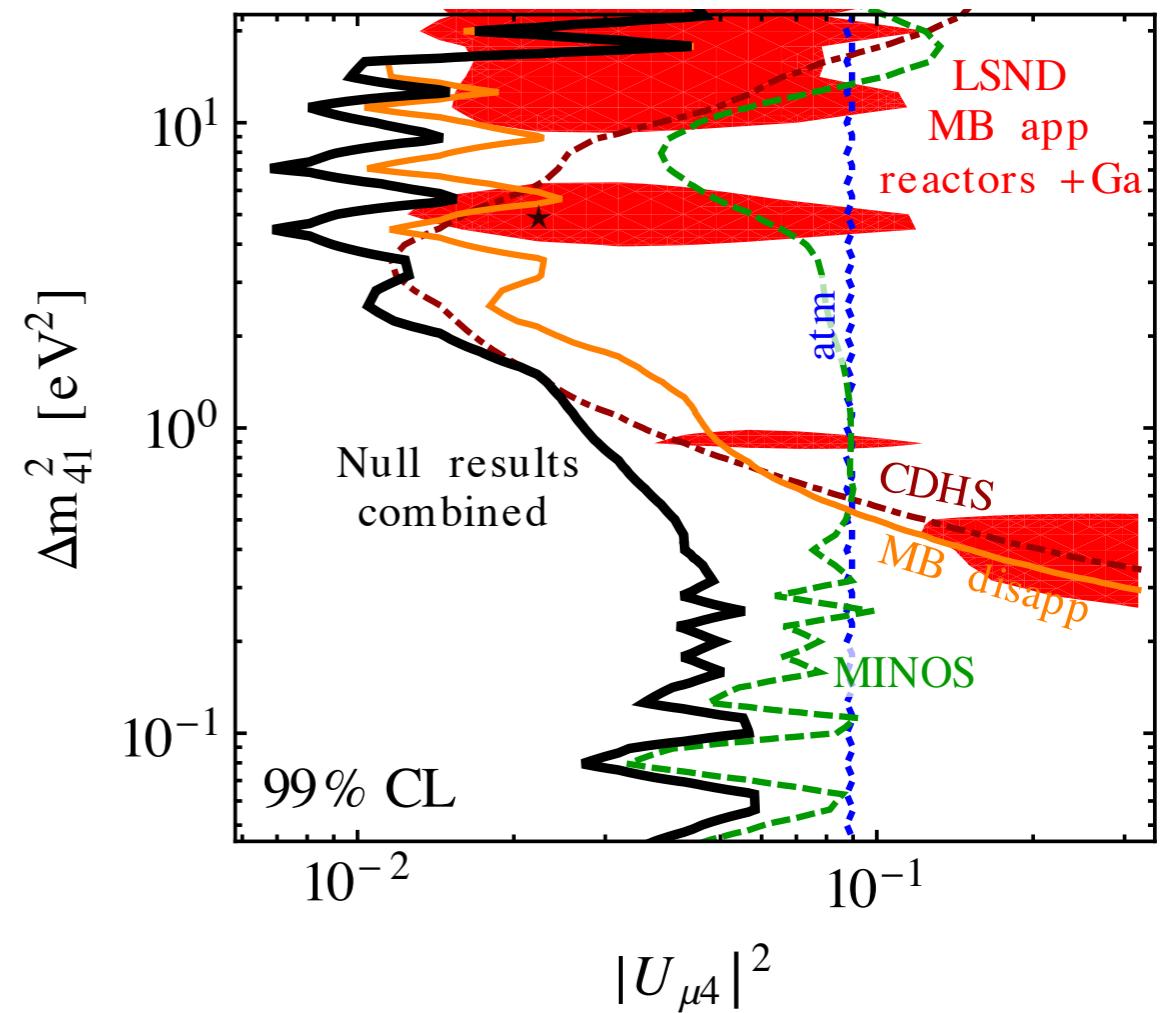
## MiniBooNE data



- LSND signal at  $3.8\sigma$
- MB antineutrino excess ( $2.8\sigma$ ) consistent with oscillations
- MB neutrino excess ( $3.4\sigma$ ) marginally consistent with osc. ( $p$ -value 6.1%)

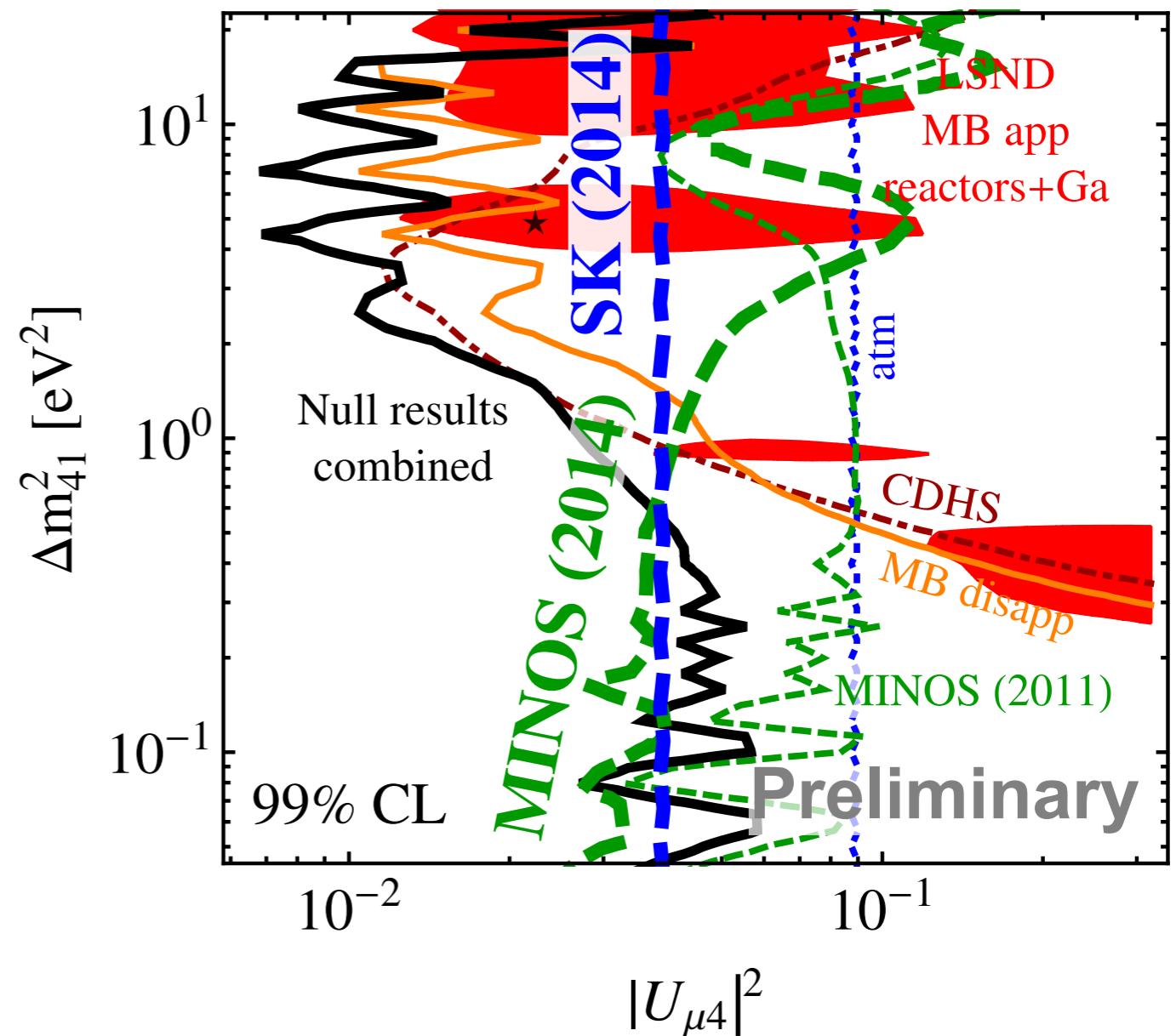
# Constraints on $\nu_\mu$ disappearance

- ▶ CDHS PLB 1984
- ▶ SuperK atmospheric  
Bilenky, Giunti, Grimus, TS 99;  
Maltoni, TS, Valle 01
- ▶ MINOS 1001.0336, 1104.3922  
(CC data most important)
- ▶ MiniBooNE  $\nu_\mu(\bar{\nu}_\mu)$   
disappearance 1106.5685



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expect somewhat increased tension