
The CTEQ Study of Nuclear Parton Distribution Function

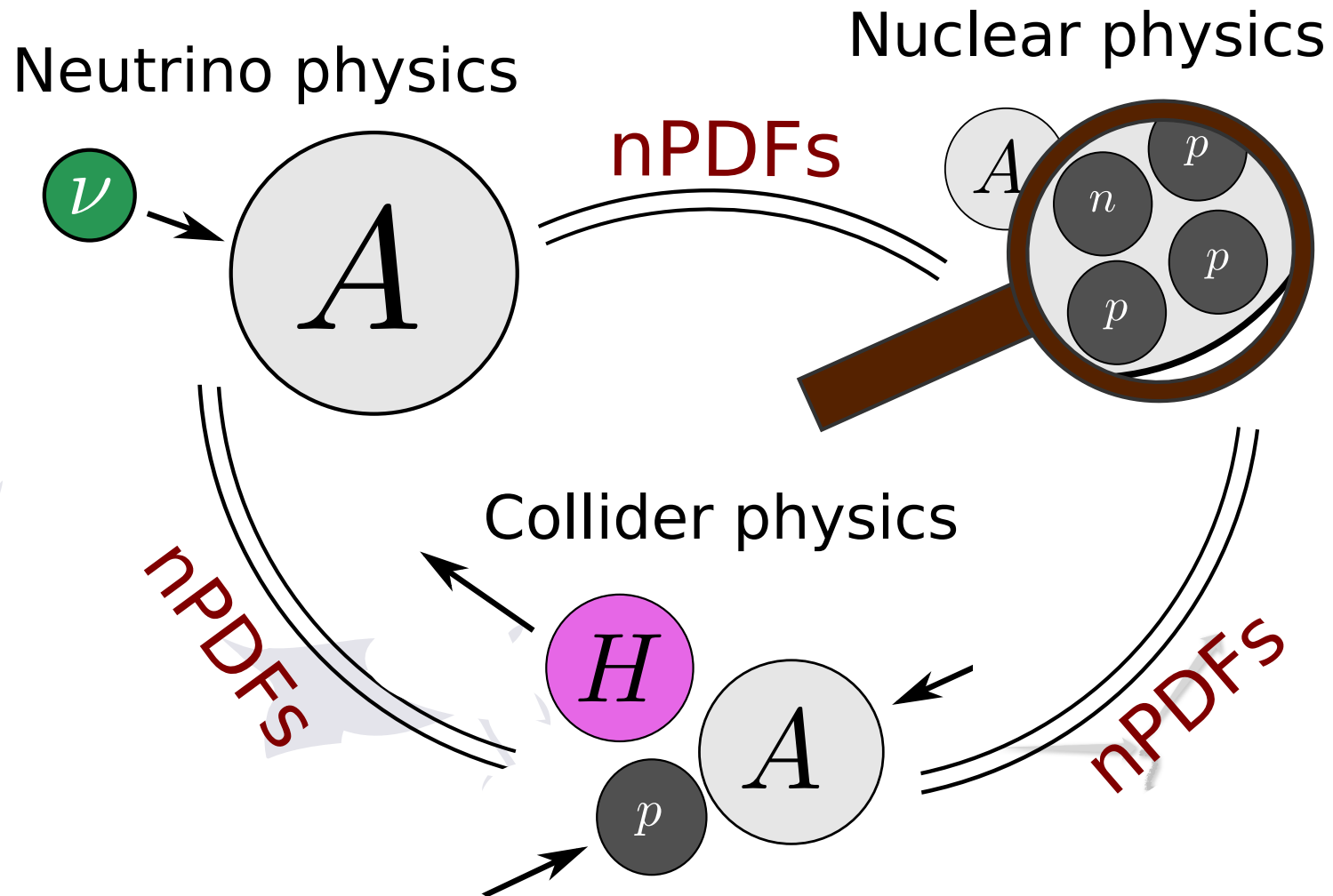
NuFact14 – Working Group 2
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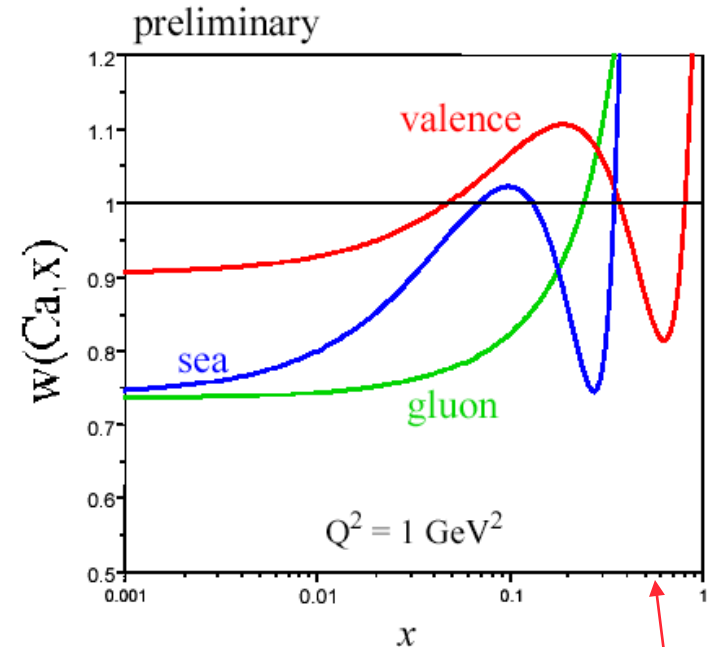
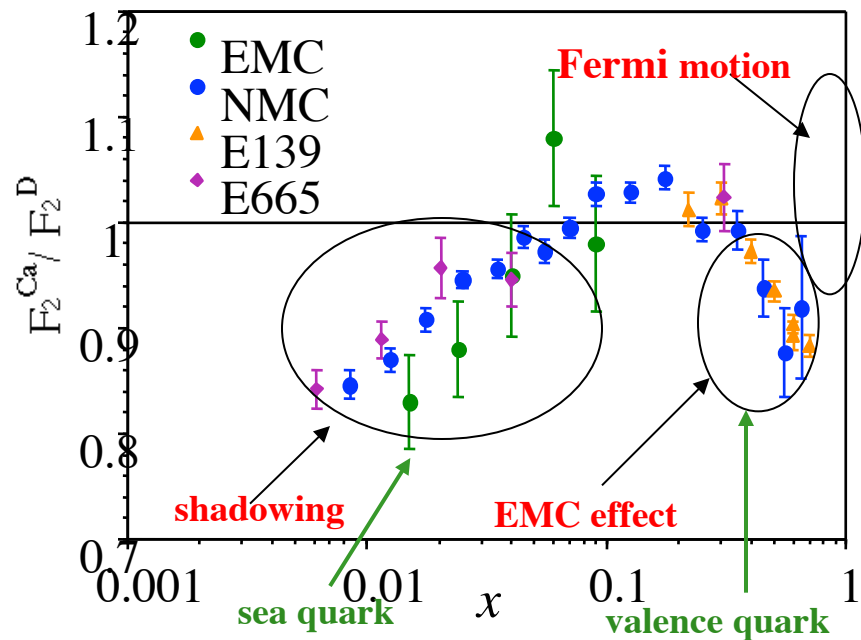
Nuclear Effects in Lepton-nucleus Interactions

- ◆ Target nucleon in motion - spectral functions (Benhar et al.)
- ◆ Certain reactions prohibited - Pauli suppression
- ◆ Quasi-elastic form factors are modified within the nuclear environment. (Butkevich / Kulagin, Tsushima et al.)
- ◆ SRC and Meson exchange currents: multi-nucleon initial states
- ◆ Produced topologies are modified by final-state interactions modifying topologies and reducing detected energy.
 - ▼ Convolution of $\delta\sigma(n\pi)$ formation zone uncertainties π -absorption uncertainties yield larger oscillation-parameter systematics
- ◆ **Cross sections and structure functions are modified and parton distribution functions within a nucleus are different than in an isolated nucleon. Observations from an on-going CTEQ analysis of nuclear parton distributions.**

Nuclear PDFs enter many Physics Analyses



Experimental Studies of (Parton-level) Nuclear Effects with Neutrinos: until recently - essentially NON-EXISTENT



- ◆ F_2 / nucleon changes as a function of A . Measured in $\mu/e - A$ not in $\nu - A$
- ◆ Good reason to consider nuclear effects are DIFFERENT in $\nu - A$.
 - ▼ Presence of axial-vector current.
 - ▼ SPECULATION: Stronger shadowing for $\nu - A$ but somewhat weaker “EMC” effect.
 - ▼ Different nuclear effects for valence and sea --> different shadowing for $x F_3$ compared to F_2 .

Two types of nPDF Analyses

- ◆ Use multiplicative factors to modify free proton PDFs.

Such as $f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A) f_i^{free\ proton}(x_N, \mu_0)$ used by

- ▼ Hirai, Kumano, Nagai [PRC 76, 065207 (2007), arXiv:0709.3038]
- ▼ Eskola, Paukkunen, Salgado [JHEP 04 (2009) 065, arXiv:0902.4154]
- ▼ de Florian, Sassot, Stratmann, Zurita [PRD 85, 074028 (2012), arXiv:1112.6324]

- ◆ Direct nuclear PDF extraction.

- ▼ nCTEQ [PRD 80, 094004 (2009), arXiv:0907.2357]

$$f_i^A(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{(A-Z)}{A} f_i^{n/A}(x, Q)$$

- ▼ The CTEQ nPDF framework is....

nCTEQ Framework

[PRD 80, 094004 (2009), arXiv: 0907.2357]

- ▶ Functional form of the **bound proton PDF** same as for the free proton (\sim CTEQ61 [hep-ph/0702159], x restricted to $0 < x < 1$)

$$x f_i^{p/A}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}, \quad i = u_v, d_v, g, \dots$$
$$\bar{d}(x, Q_0)/\bar{u}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} + (1 + c_3 x)(1-x)^{c_4}$$

- ▶ A -dependent fit parameters (reduces to free proton for $A = 1$)

$$c_k \rightarrow c_k(A) \equiv c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}}), \quad k = \{1, \dots, 5\}$$

- ▶ PDFs for nucleus (A, Z)

$$f_i^A(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{(A-Z)}{A} f_i^{n/A}(x, Q)$$

Details of the Fit – First no Neutrino Data

Charged-lepton DIS, DY and RHIC π^0

Fit properties:

- ▶ fit @NLO
- ▶ $Q_0 = 1.3\text{GeV}$
- ▶ using ACOT heavy quark scheme
- ▶ kinematical cuts: $Q > 2\text{GeV}$,
 $W > 3.5\text{GeV}$
- ▶ 708 (DIS & DY) + 32 (single π^0)
= 740 data points after cuts
- ▶ 16 free parameters

7 Gluon

7 Valence

2 Sea

$$\chi^2 / \text{dof} = 0.85$$

Error analysis:

- ▶ use Hessian method

$$\chi^2 = \chi_0^2 + \frac{1}{2} H_{ij} (a_i - a_i^0)(a_j - a_j^0)$$

$$H_{ij} = \frac{\partial^2 \chi^2}{\partial a_i \partial a_j}$$

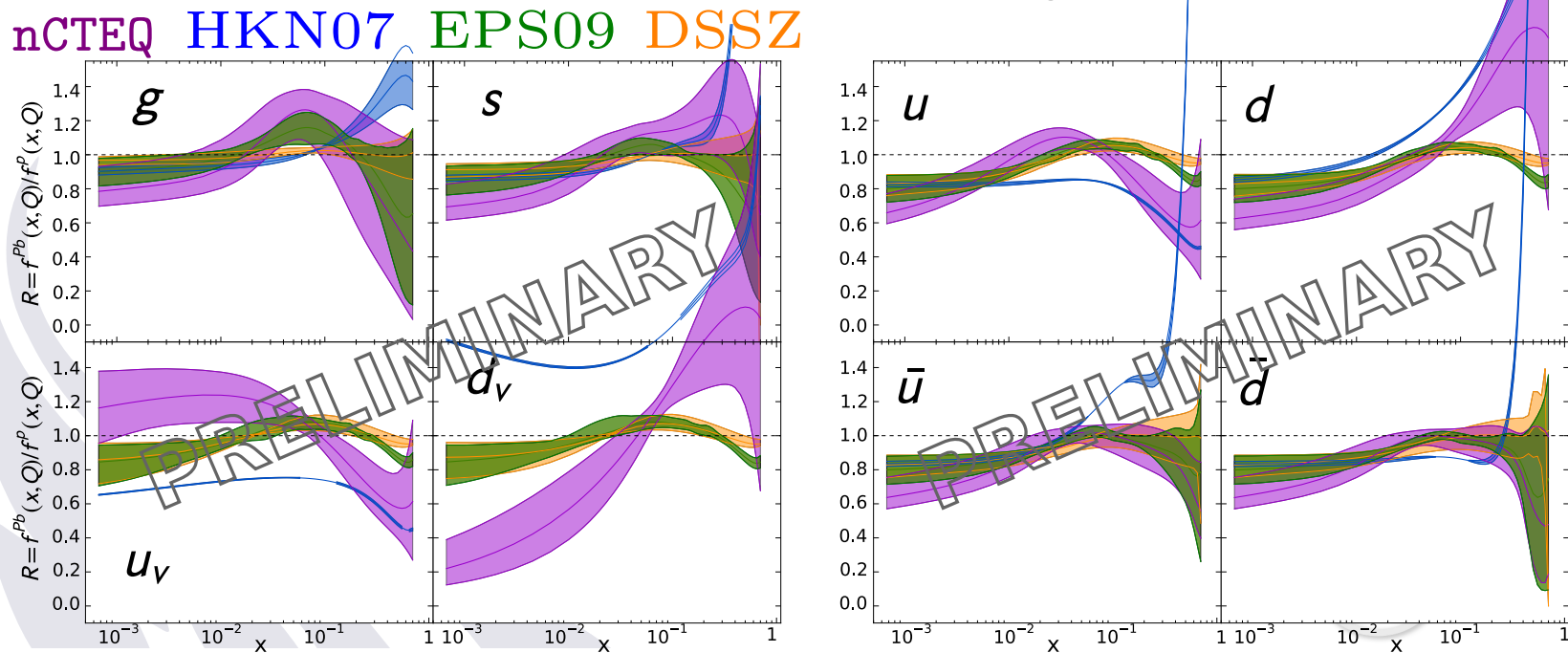
- ▶ tolerance $\Delta\chi^2 = 35$ (every nuclear target within 90% C.L.)
- ▶ eigenvalues span 10 orders of magnitude \rightarrow require numerical precision
- ▶ use noise reducing derivatives

nCTEQ Results – comparison with other sets

Nuclear correction factors
($Q = 10\text{GeV}$)

$$R_i(Pb) = \frac{f_i^{Pb}(x, Q)}{f_i^p(x, Q)}$$

- ▶ different solution for d -valence & u -valence compared to EPS09 & DSSZ
- ▶ sea quark nuclear correction factors similar to EPS09
- ▶ nuclear correction factors depend largely on underlying proton baseline

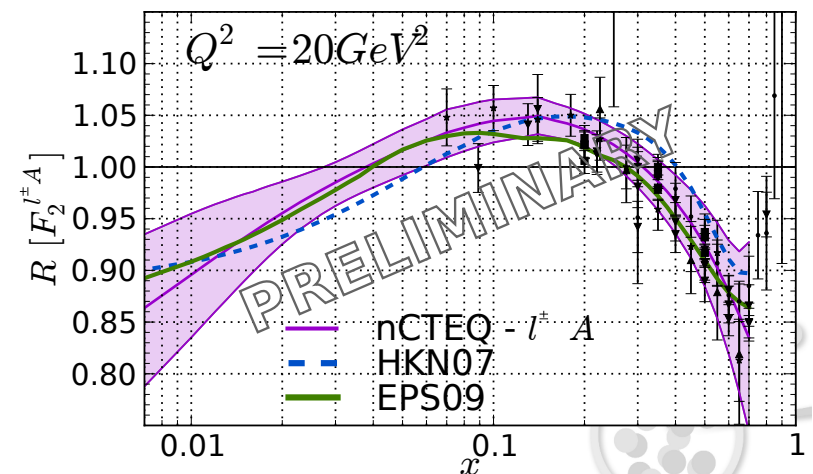
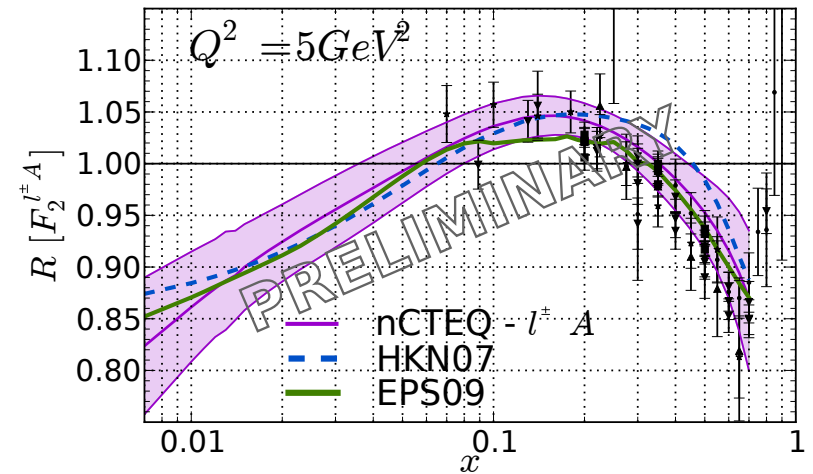


nCTEQ Results - continued

- ◆ Structure Function Ratio and comparison with other nPDF sets.

$$R = \frac{F_2^{Fe}(x, Q)}{F_2^D(x, Q)}$$

- ◆ Reasonable agreement of the ratios even though differences in the individual partons



Now bring in Neutrinos
: F_2^{ν} Nuclear Effects Analyses

Nuclear PDFs from neutrino deep inelastic scattering

**I. Schienbein (SMU & LPSC-Grenoble, J-Y. Yu (SMU)
C. Keppel (Hampton & JeffersonLab) J.G.M. (Fermilab),
F. Olness (SMU), J.F. Olness (Florida State U)**

Also analyses by:

K. Eskola, V. Kolhinen and C. Salgado
and

D. de Florian, R. Sassot, P. Zurita and M. Stratmann

Extraction of Nuclear PDFs and Nuclear Correction Factors from ν -A Scattering

- ◆ PDF Parameterized at $Q_0 = 1.3$ GeV as

$$xf_i(x, Q_0) = \begin{cases} A_0 x^{A_1} (1-x)^{A_2} e^{A_3 x} (1+e^{A_4 x})^{A_5} & : i = u_v, d_v, g, \bar{u} + \bar{d}, s, \bar{s}, \\ A_0 x^{A_1} (1-x)^{A_2} + (1+A_3 x)(1-x)^{A_4} & : i = \bar{d}/\bar{u}, \end{cases}$$

- ◆ PDFs for a nucleus are constructed as:

$$f_i^A(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{(A-Z)}{A} f_i^{n/A}(x, Q)$$

- ◆ Resulting in nuclear structure functions:

$$F_i^A(x, Q) = \frac{Z}{A} F_i^{p/A}(x, Q) + \frac{(A-Z)}{A} F_i^{n/A}(x, Q)$$

- ◆ The differential cross sections for CC scattering off a nucleus::

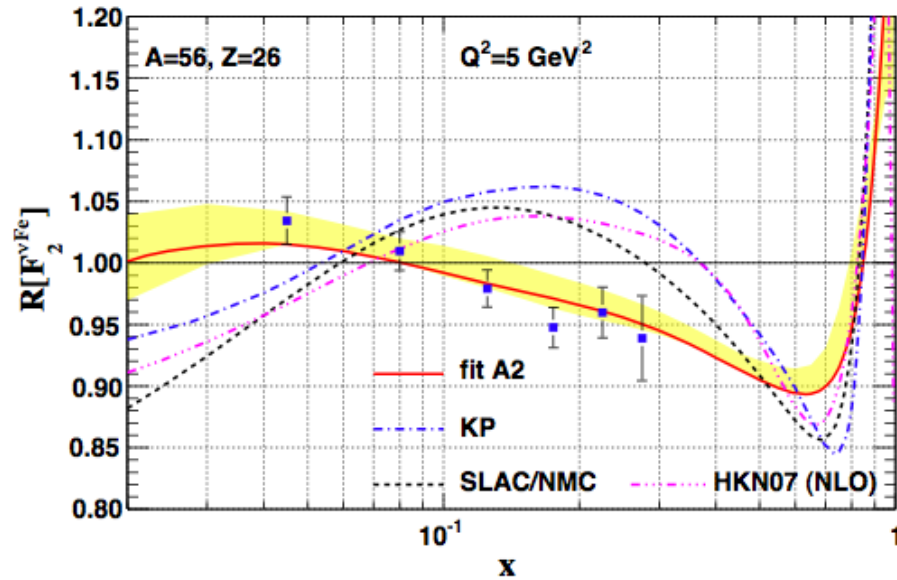
$$\begin{aligned} \frac{d^2\sigma}{dx dy} {}^{(\bar{\nu})A} &= \frac{G^2 ME}{\pi} \left[\left(1 - y - \frac{Mxy}{2E}\right) F_2 {}^{(\bar{\nu})A} \right. \\ &\quad \left. + \frac{y^2}{2} 2xF_1 {}^{(\bar{\nu})A} \pm y\left(1 - \frac{y}{2}\right) xF_3 {}^{(\bar{\nu})A} \right] \end{aligned}$$

CTEQ High-x Study: nuclear effects

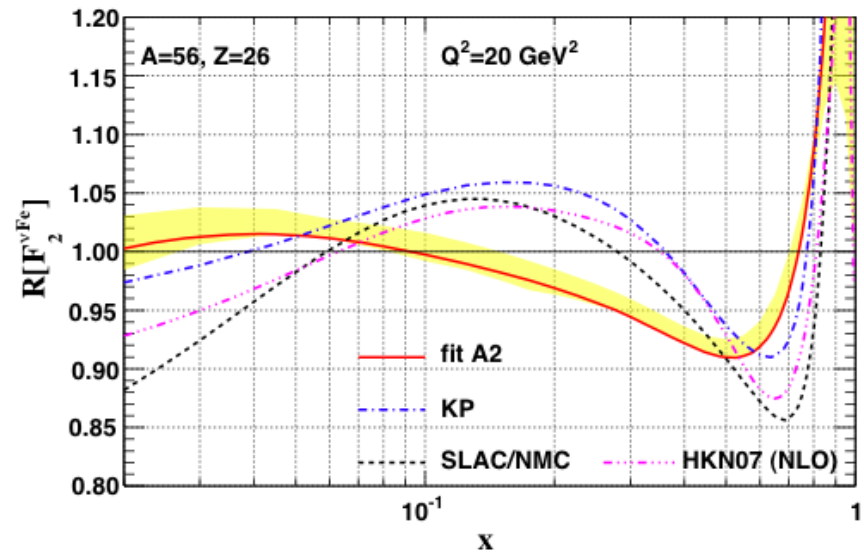
Use nucleon pdf's to form denominator in ratios

- ◆ Form reference fit mainly nucleon (as opposed to nuclear) scattering results:
 - ▼ BCDMS results for F_2^p and F_2^d
 - ▼ NMC results for F_2^p and F_2^d/F_2^p
 - ▼ H1 and ZEUS results for F_2^p
 - ▼ CDF and DØ result for inclusive jet production
 - ▼ CDF results for the W lepton asymmetry
 - ▼ E-866 results for the ratio of lepton pair cross sections for pd and pp interactions
 - ▼ E-605 results for dimuon production in pN interactions.
- ◆ Correct for deuteron nuclear effects

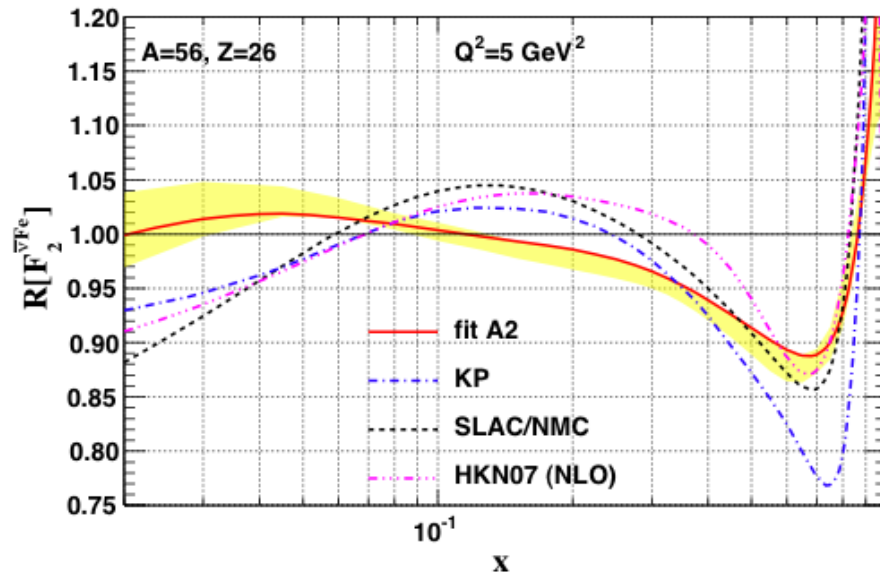
F_2 Structure Function Ratios: ν -Iron



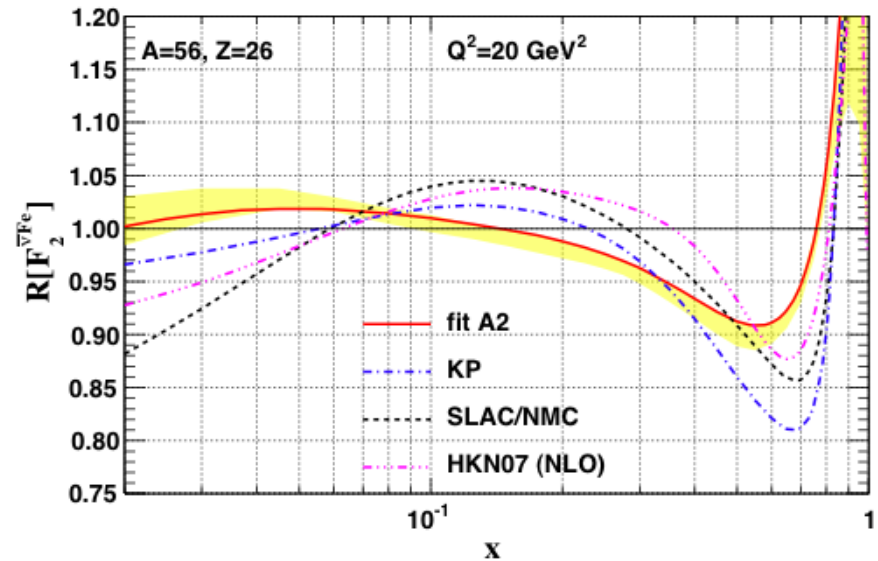
$$\frac{F_2(\nu + \text{Fe})}{F_2(\nu + [n+p])}$$



F_2 Structure Function Ratios: $\bar{\nu}$ -Iron

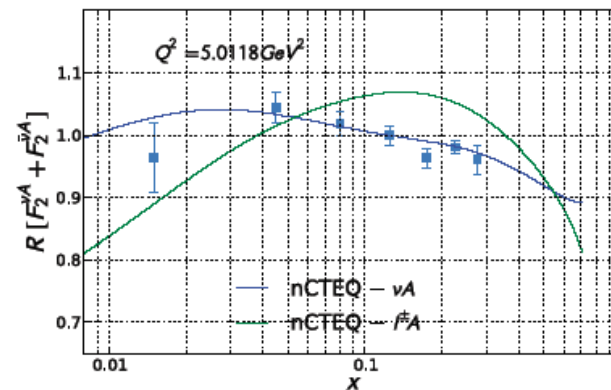
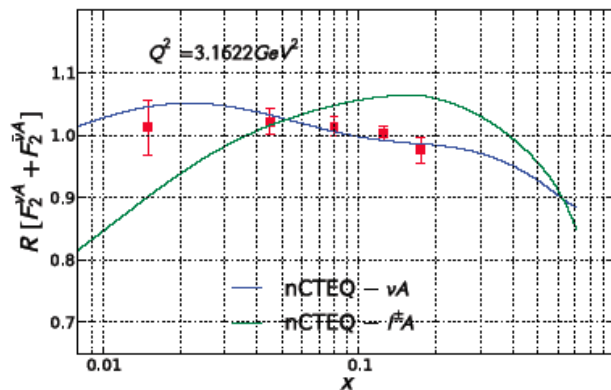
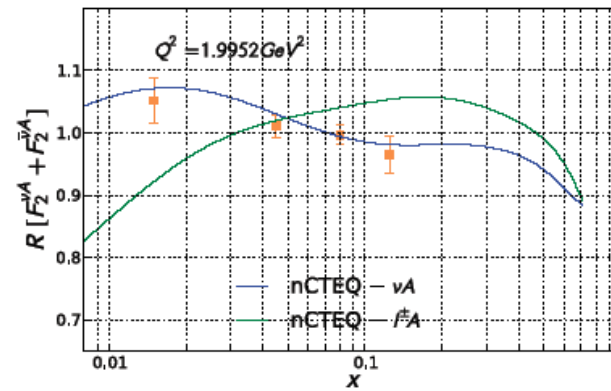
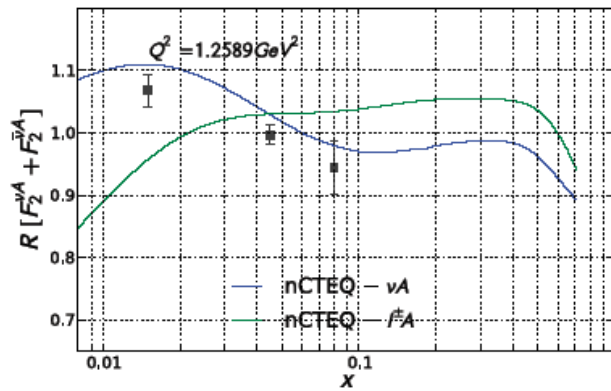


$$\frac{F_2(\bar{\nu} + \text{Fe})}{F_2(\bar{\nu} + [n+p])}$$



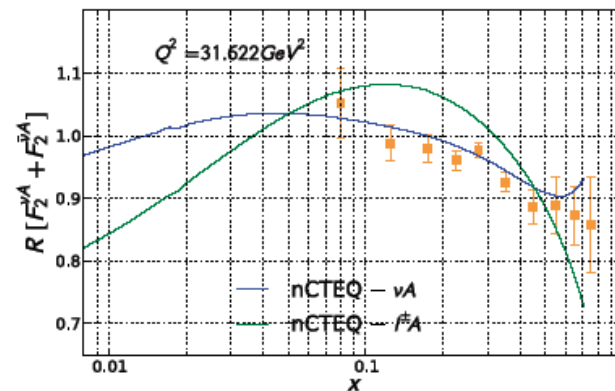
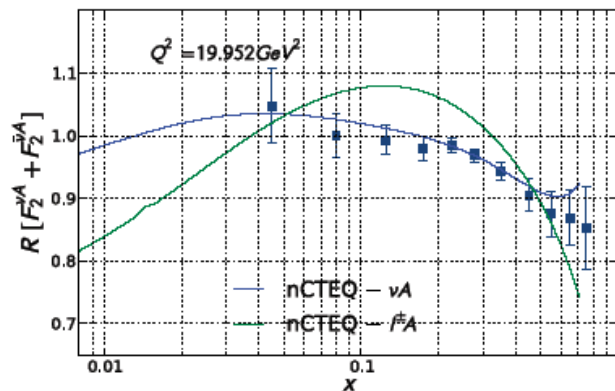
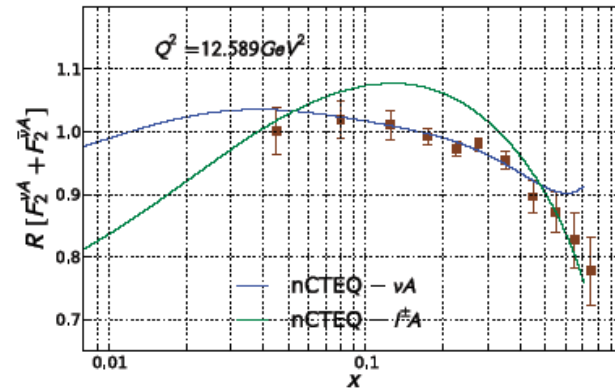
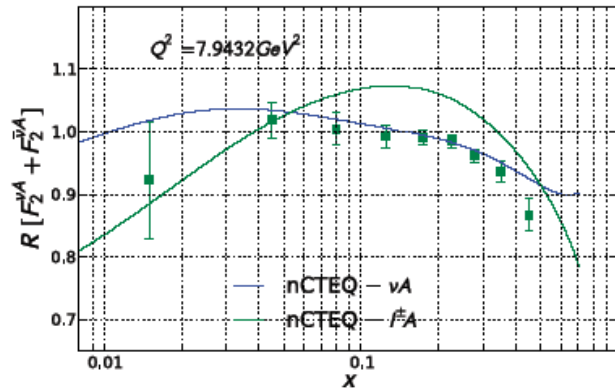
A More-Detailed Look at Differences

- ◆ NLO QCD calculation of $\frac{F_2^{\nu A} + F_2^{\bar{\nu} A}}{2}$ in the ACOT-VFN scheme
 - ▼ charge lepton fit undershoots low-x data & overshoots mid-x data
 - ▼ low- Q^2 and low-x data cause tension with the shadowing observed in charged lepton data



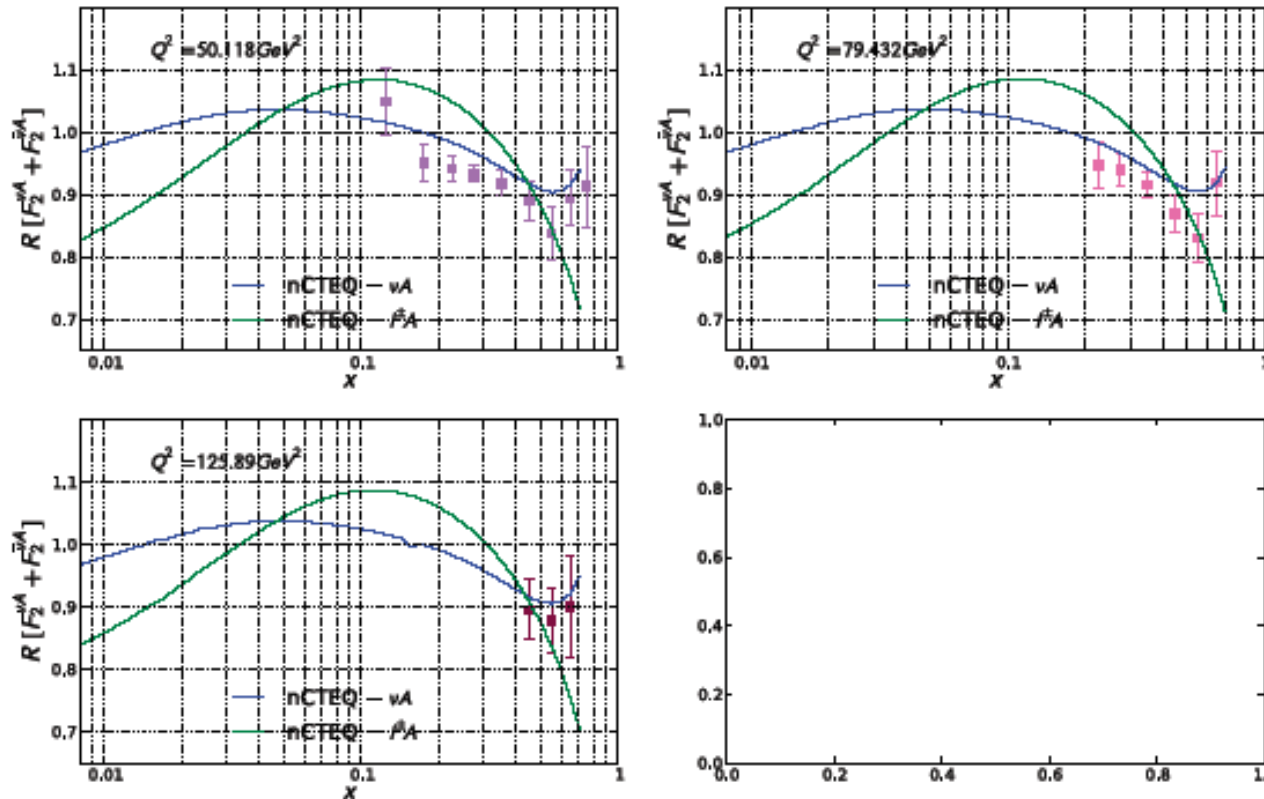
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Can we fit the combined νA , ℓA and DY data

? **Kovarik**, Yu, Keppel, Morfin, Olness, Owens, **Schienbein**, Stavreva

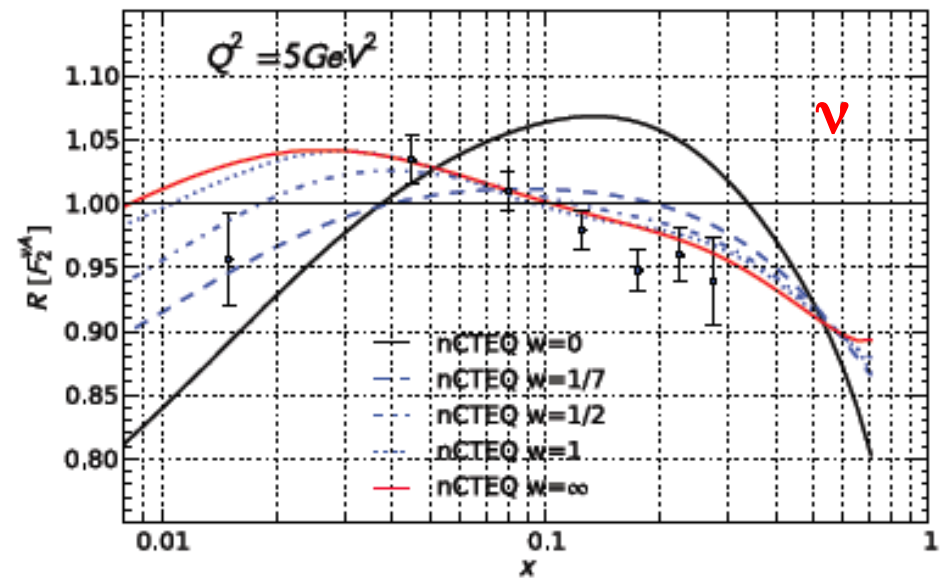
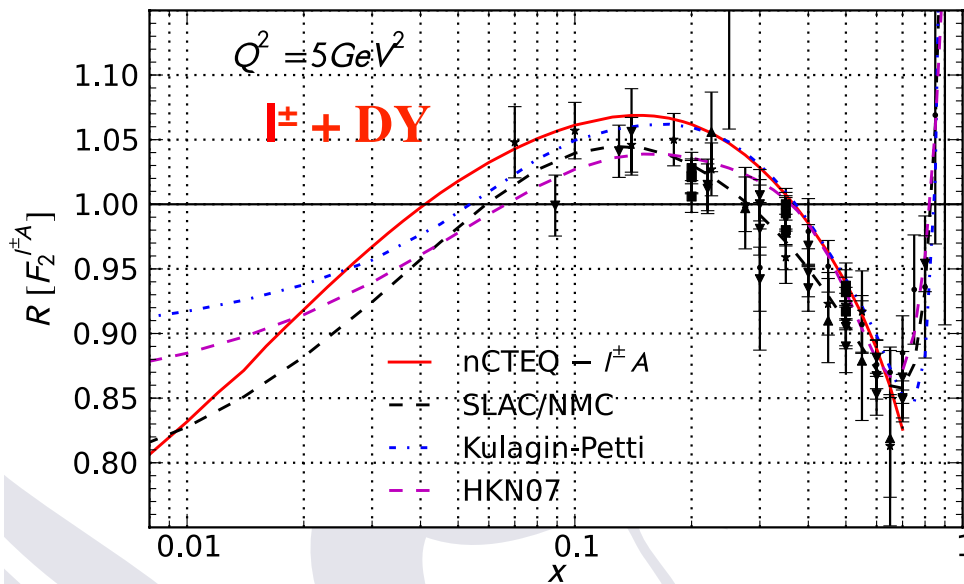
- ◆ Take the analysis of $\ell^\pm A$ data sets (built in A -dependence)
 - ▼ Schienbein, Yu, Kovarik, Keppel, Morfin, Olness, Owens,
 - ▼ PRD80 (2009) 094004
- ◆ For $\ell^\pm A$ take $F_2(A) / F_2(D)$ and $F_2(A) / F_2(A')$ and DY $\sigma(pA) / \sigma(pA')$
 - ▼ 708 Data points with $Q > 2$ and $W > 3.5$
- ◆ Use **8 Neutrino data sets** —
 - ▼ NuTeV cross section data: νFe , $\bar{\nu} Fe$
 - ▼ NuTeV dimuon off Fe data —
 - ▼ CHORUS cross section data: νPb , $\bar{\nu} Pb$
 - ▼ CCFR dimuon off Fe data
- ◆ Initial problem, with standard CTEQ cuts of $Q > 2$ and $W > 3.5$
neutrino data points (3134) far outnumber $\ell^\pm A$ (708).

Try to Find a Simultaneous Fit to Both l^\pm and ν

Weight the neutrino contribution

- ◆ Analysis of fits with different weights of neutrino DIS (using correlated errors)

Weight	Fit name	l data	χ^2 (/pt)	ν data	χ^2 (/pt)	total χ^2 (/pt)
$w = 0$	decut3	708	639 (0.90)	-	-	639 (0.90)
$w = 1/7$	glofac1a	708	645 (0.91)	3134	4710 (1.50)	5355 (1.39)
$w = 1/4$	glofac1c	708	654 (0.92)	3134	4501 (1.43)	5155 (1.34)
$w = 1/2$	glofac1b	708	680 (0.96)	3134	4405 (1.40)	5085 (1.32)
$w = 1$	global2b	708	736 (1.04)	3134	4277 (1.36)	5014 (1.30)
$w = \chi^2 / d.o.f. = 0.89$	global2a	708	-	3134	4192 (1.33)	4192 (1.33)



Quantitative χ^2 Analysis of a Combined Fit

- ◆ Up to now we are giving a qualitative analysis. Consider next quantitative criterion based on χ^2
- ◆ Introduce “tolerance” (T). Condition for compatibility of two fits: The 2nd fit χ^2 should be within the 90% C.L. region of the first fit χ^2
- ◆ Charged: 638.9 ± 45.6 (best fit to charged lepton and DY data)
- ◆ Neutrino: 4192 ± 138 (best fit to only neutrino data)

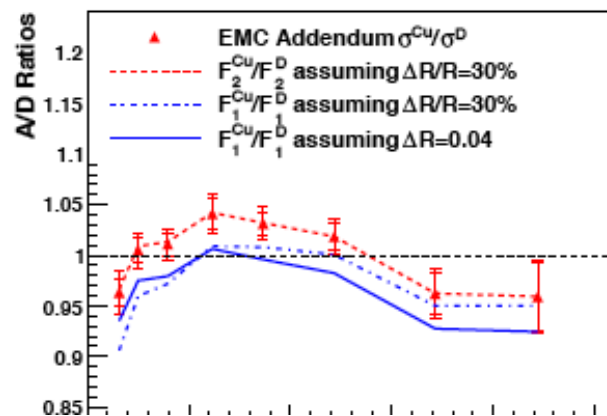
Weight	Fit name	ℓ data	χ^2	ν data	χ^2	total χ^2 (/pt)
$w = 0$	decut3	708	639	-	nnnn NO	639 (0.90)
$w = 1/7$	glofac1a	708	645 YES	3134	4710 NO	5355 (1.39)
$w = 1/4$	glofac1c	708	654 YES	3134	4501 NO	5155 (1.34)
$w = 1/2$	glofac1b	708	680 YES	3134	4405 NO***	5085 (1.32)
$w = 1$	global2b	708	736 NO	3134	4277 YES	5014 (1.30)
$w = \infty$	nuanua1	-	nnn NO	3134	4192	4192 (1.33)

Others Do NOT Find this Difference between l^\pm and ν

- ◆ The analyses of K. Eskola et al. and D. de Florian et al. do not find this difference between l^\pm -A and ν -A scattering.
- ◆ They do not use the full covariant error matrix rather adding statistical and systematic errors in quadrature.
- ◆ They do not use the full double differential cross section rather they use the extracted structure functions which involve assumptions:
 - ▼ Assume a value for $\Delta x F_3$ ($= F_3^{\nu} - F_3^{\bar{\nu}}$) from theory.
 - ▼ Assume a value for $R = F_L / F_T$.
- ◆ If nCTEQ makes these same assumptions, than a combined solution of l^\pm -A and ν -A scattering can be found.

If Difference between both I^{\pm} -A and ν -A persists?

- ◆ In neutrino scattering, low- Q^2 is dominated by the (PCAC) part of the axial-vector contribution of the longitudinal structure function F_L .
- ◆ Shadowing is led by F_T and the shadowing of F_L lags at lower x .



V. Guzey et al. arXiv 1207.0131

- ▼ F_1 (Blue) is purely transverse and F_2 (Red) is a sum of F_T (F_1) and F_L
- ▼ This could be a contributing factor to such a difference.
- ◆ Another idea also from Guzey and colleagues is the observation that

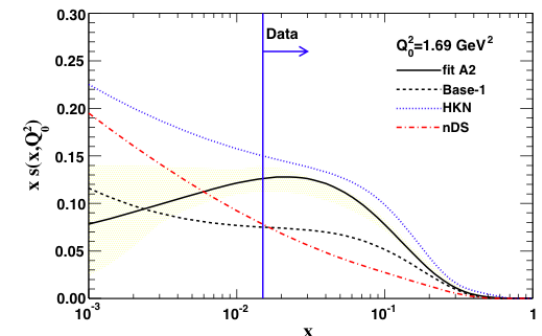
If Difference between both l^\pm -A and ν -A persists?

- ◆ Another idea also from Guzey and colleagues is the observation that (in leading order):

$$\frac{d\sigma^{\nu A}}{dx dy} = \frac{G_F^2 M_W^4}{(Q^2 + M_W^2)^2} \frac{ME}{\pi} 2x [d^A + s^A + (1-y)^2(\bar{u}^A + \bar{c}^A)]$$

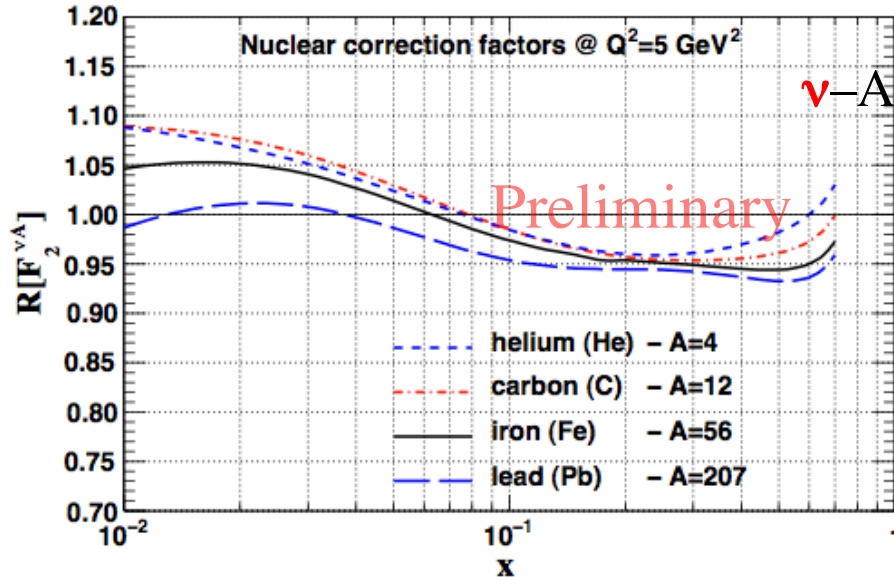
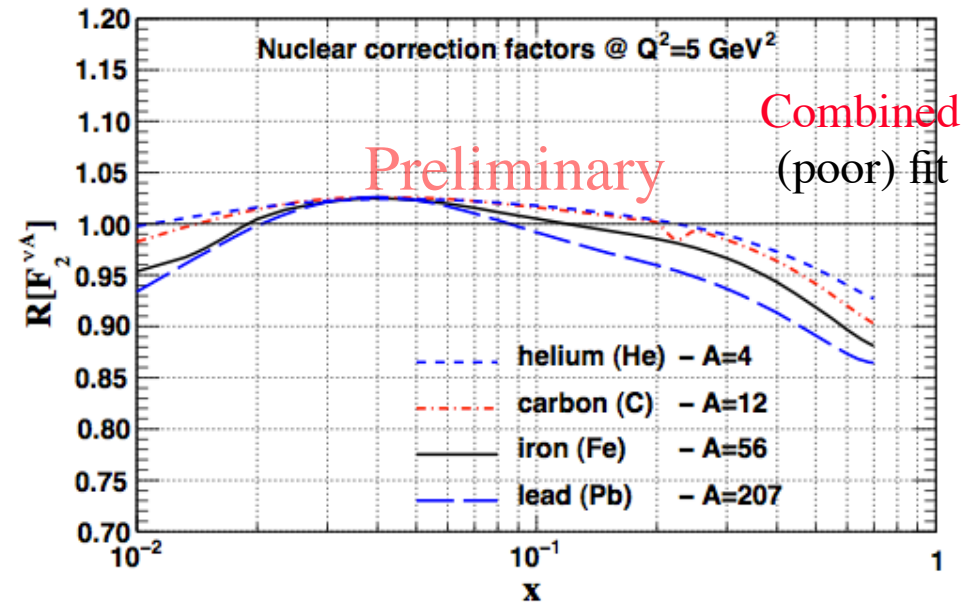
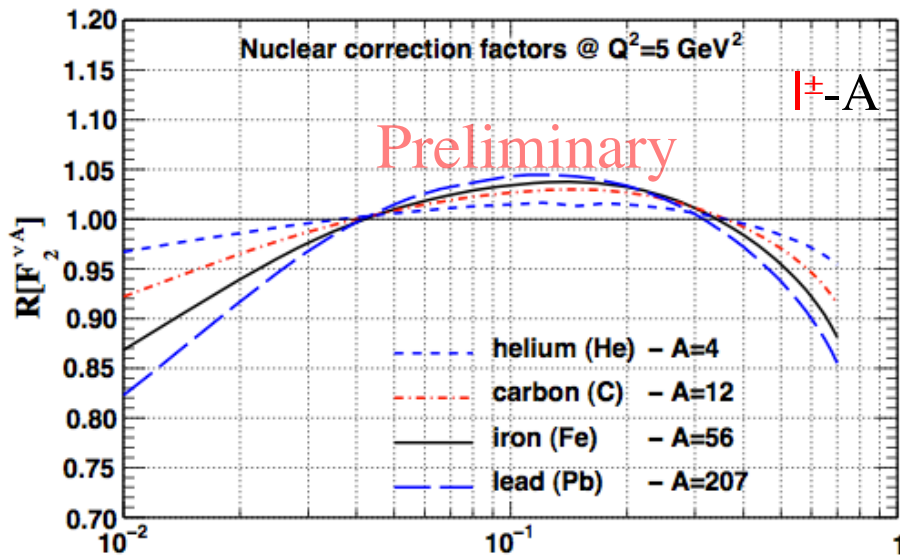
$$\frac{d\sigma^{\bar{\nu} A}}{dx dy} = \frac{G_F^2 M_W^4}{(Q^2 + M_W^2)^2} \frac{ME}{\pi} 2x [d^{\bar{A}} + s^{\bar{A}} + (1-y)^2(u^A + c^A)]$$

- ▼ In the shadowing region at low- x , y is large and the σ are primarily probing the d- and s-quarks.
- ◆ This is very different from l^\pm scattering where the d- and s-quarks are reduced by a factor of 4 compared to the u- and c-quarks.
 - ▼ If shadowing of the d- or s-quarks is negligible this would explain the NuTeV result.
 - ▼ Diminished shadowing of the nuclear s-quark is suggested by early extraction of nPDFs by nCTEQ.



What could MINER ν A Contribute?

Preliminary Predictions for MINER ν A Targets



Ongoing analysis of MINER ν A LE DIS neutrino sample with average Q^2 of 4 GeV^2

Summary and Conclusions

- ◆ The CTEQ nPDF fits - without neutrino input - build in the A-dependence and now provide the error associated with each nPDF
- ◆ There are indications from **one** experiment using **one** nucleus that **ν -induced parton-level nuclear effects are different** than l^{\pm} -nuclear effects.
 - ▼ Based on nuclear corrections factors R and the tolerance criterion, there is no good compromise fit to the $l^{\pm}A + DY + \nu A$ data.
- ◆ If these differences between $l^{\pm}A$ and νA scattering persist, the difference in shadowing, at least, may (partially) be due to the large contribution of F_L at low Q^2 in νA scattering and/or shadowing of the strange quark.
- ◆ Need systematic **experimental** study of **ν -induced nuclear effects in A and D_2 such as MINER ν A in the ME Beam.**

Additional Details

Global Analysis Procedure

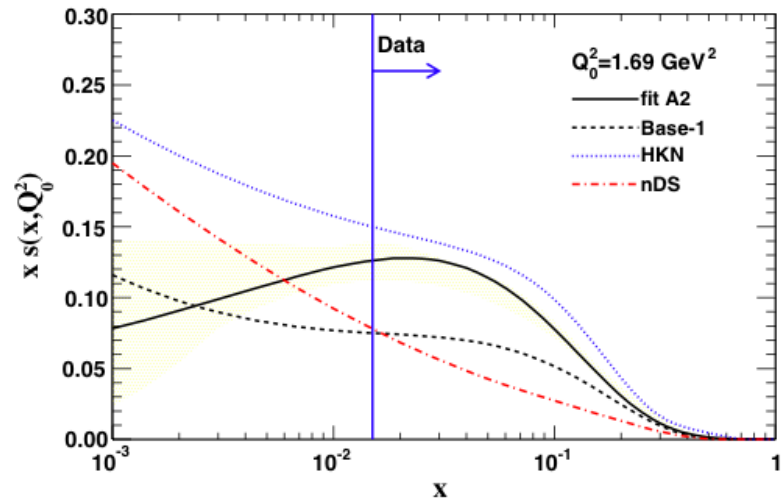
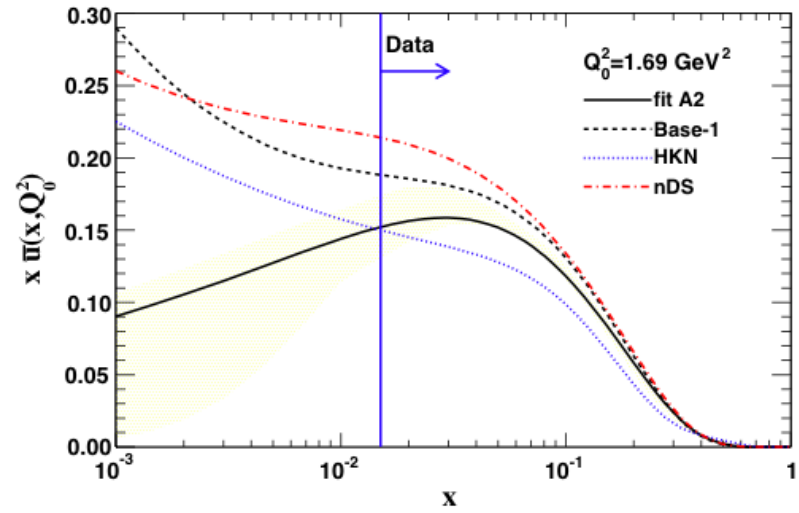
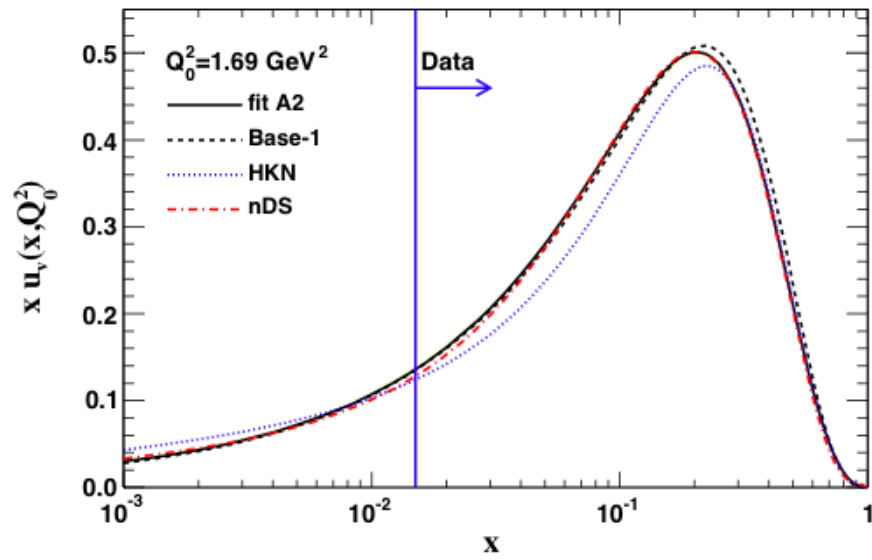
1. Parametrize PDFs at low initial scale $\mu = Q_0 = 1.3\text{GeV}$:

$$f(x, Q_0) = f(x; a_0, a_1, \dots) = a_0 x^{a_1} (1-x)^{a_2} P(x; a_3, \dots)$$

2. Use DGLAP equation to evolve $f(x, \mu)$ from $\mu = Q_0$ to $\mu = Q_{\text{max}}$.
3. Define and minimize appropriate χ^2 function (with respect to parameters a_0, a_1, \dots)

$$\chi^2(\{a_i\}) = \sum_{\text{experiments}} w_n \chi_n^2(\{a_i\})$$
$$\chi_n^2(\{a_i\}) = \sum_{\text{data points}} \left(\frac{\text{data} - \text{theory}(\{a_i\})}{\text{uncertainty}} \right)^2$$

Iron PDFs



Kulagin-Petti Model of Nuclear Effects

hep-ph/0412425

- ◆ Global Approach -aiming to obtain quantitative calculations covering the complete range of x and Q^2 available with thorough physics basis for fit to data.

- ◆ Different effects on structure functions (SF) are taken into account:

$$F_i^A = F_i^{p/A} + F_i^{n/A} + F_i^{\pi/A} + \delta F_i^{\text{coh}}$$

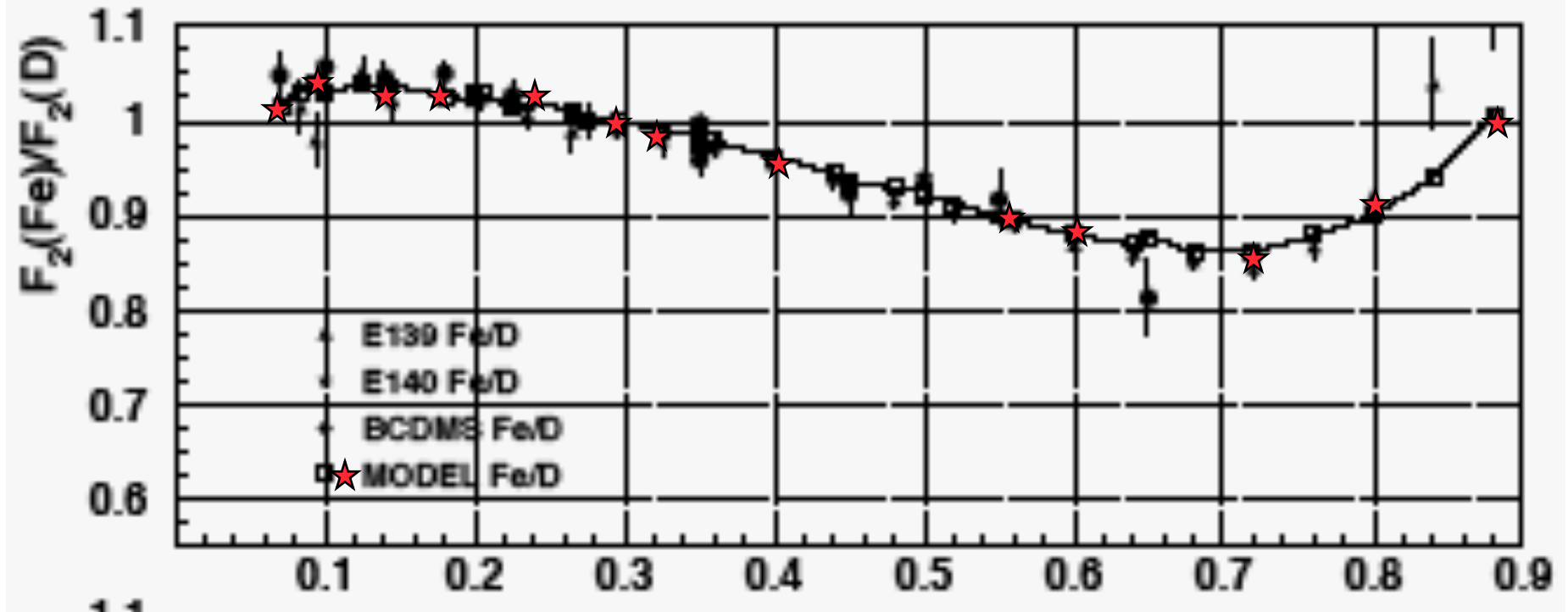
- $F_i^{p(n)/A}$ bound proton(neutron) SF with *Fermi Motion, Binding (FMB) and Off-Shell effect (OS)*
 - $F_i^{\pi/A}$ *nuclear Pion excess correction (PI)*
 - δF_i^{coh} *contribution from coherent nuclear interactions: Nuclear Shadowing (NS)*
- ◆ **Fermi Motion** and **Binding** in nuclear structure functions is calculated from the convolution of nuclear spectral function and (bound) nucleon SFs:
 - ◆ Since bound nucleons are off-mass shell there appears dependence on the nucleon virtuality $\kappa^2 = (M + \varepsilon)^2 - k^2$ where we have introduced an **off-shell structure function $\delta f_2(x)$**

$$F_2(x, Q^2, k^2) = F_2(x, Q^2) \left(1 + \delta f_2(x) (k^2 - M^2) / M^2 \right)$$

- ◆ Leptons can scatter off mesons which mediate interactions among bound nucleons yielding a **nuclear pion correction**

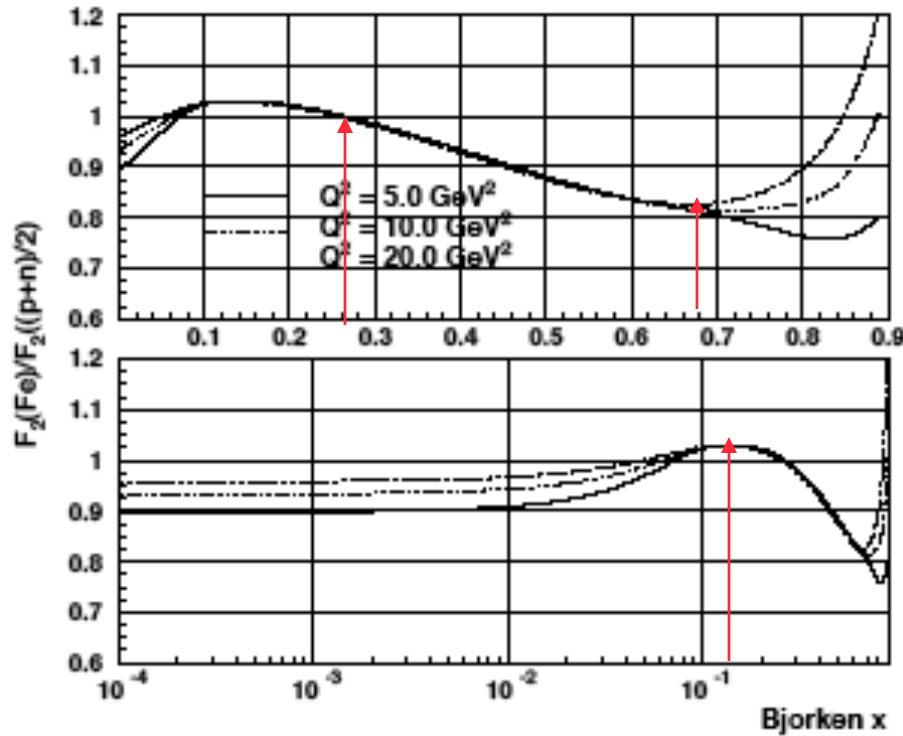
Kulagin-Petti compared to e/ μ +Fe data

$$F_2(e/\mu+Fe) / F_2(e/\mu+D)$$

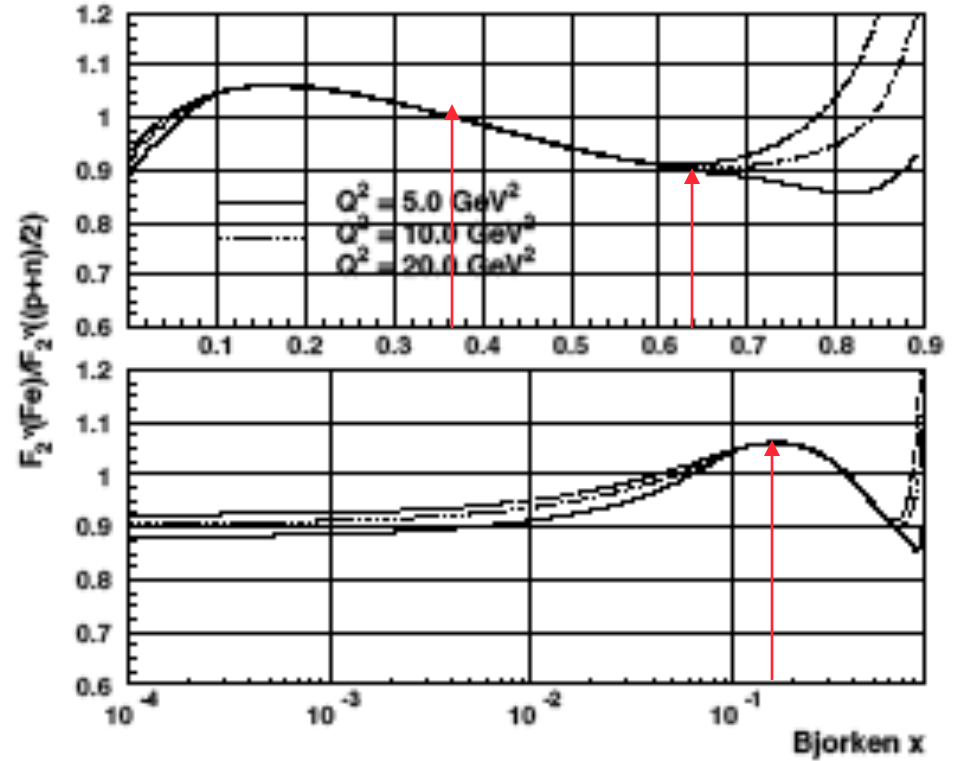


Charged Lepton

$F_2(\mu+\text{Fe}) / F_2(\mu+\text{N})$ compared to $F_2(\nu+\text{Fe}) / F_2(\nu+\text{N})$



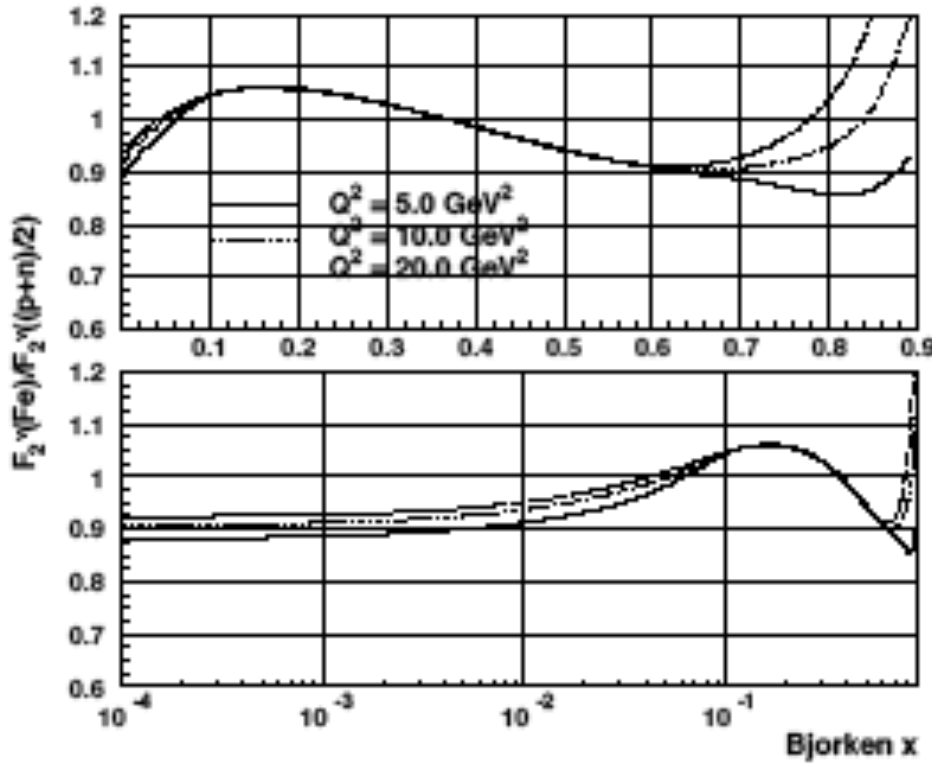
Charged Lepton



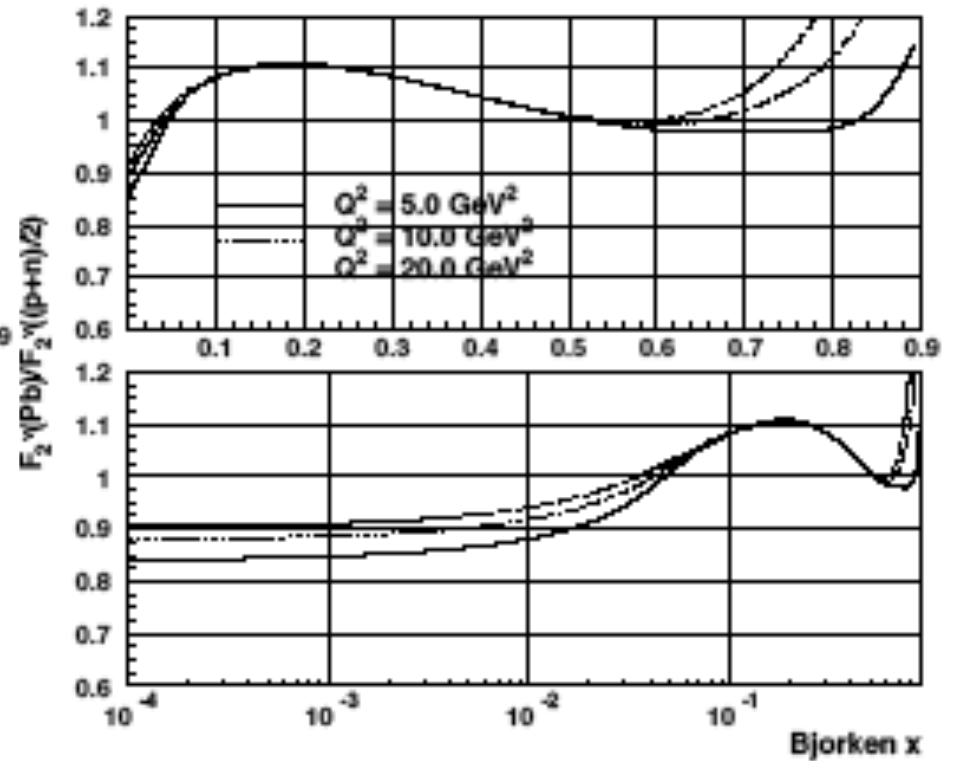
Neutrino

$$F_2(\nu+A) / F_2(\nu+N)$$

(n excess included in effect)

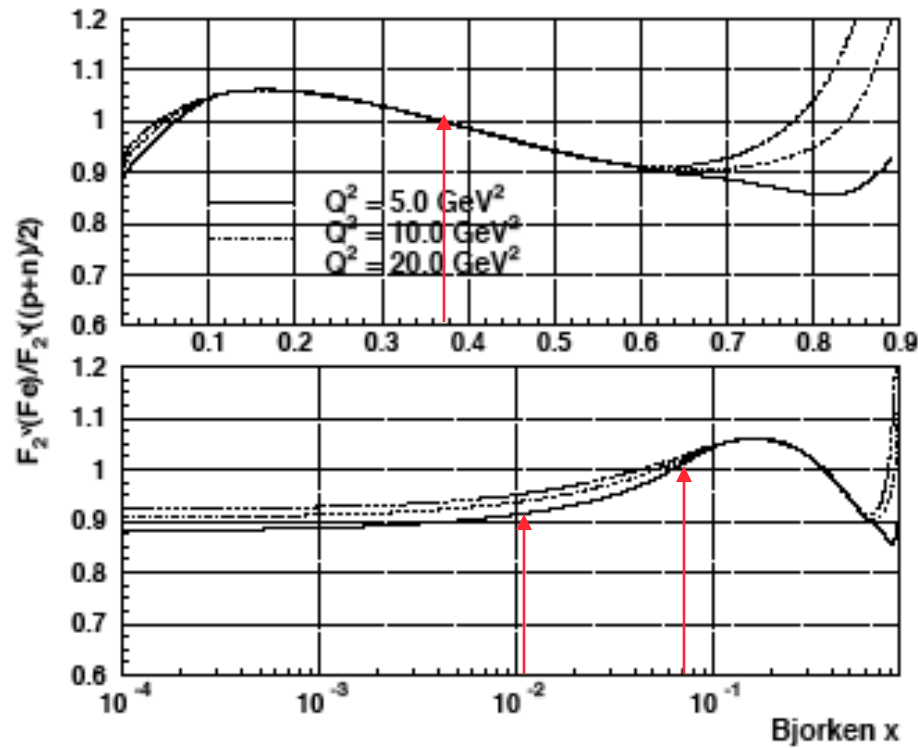


Fe

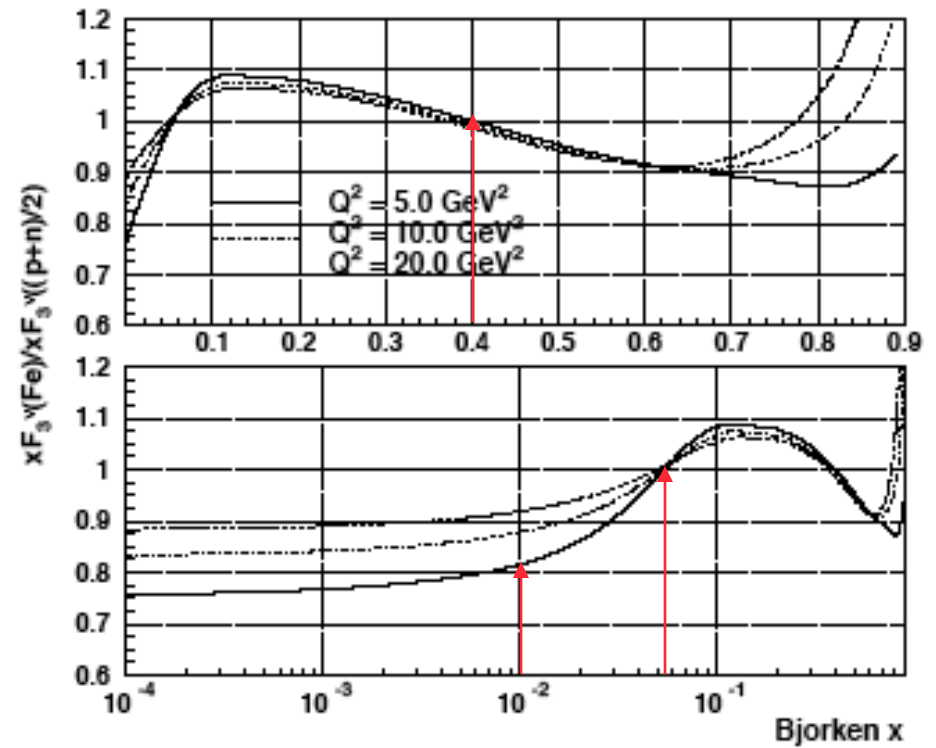


Pb

Kulagin-Petti: ν -Fe Nuclear Effects



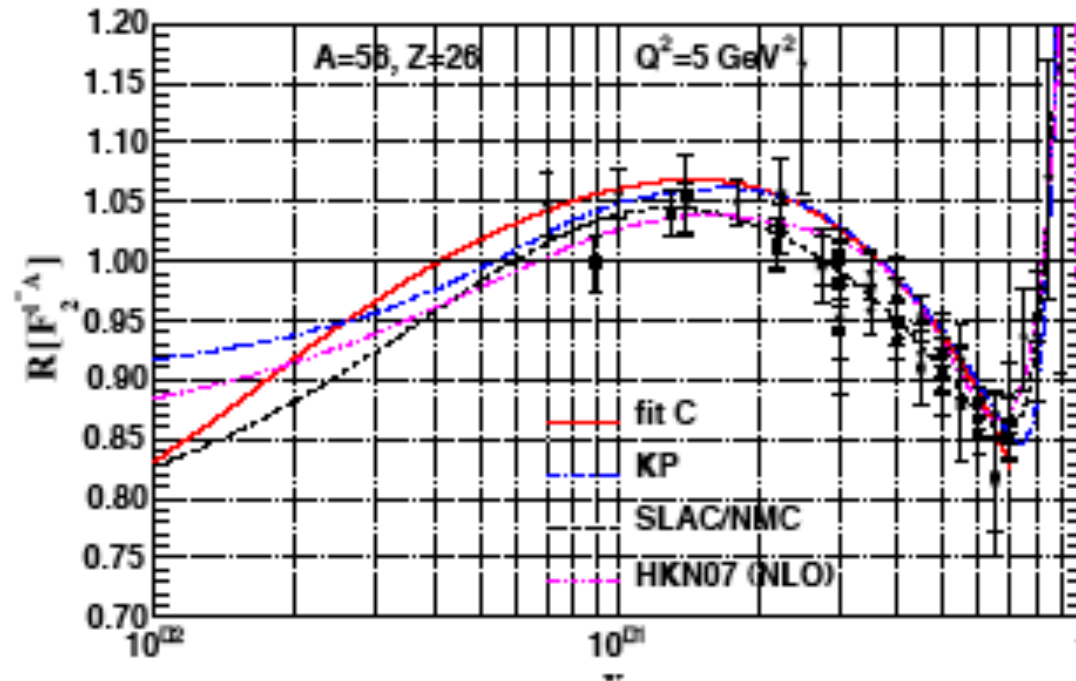
F_2



$x F_3$

Nuclear Structure Function Corrections

Q^\pm (Fe/D₂)

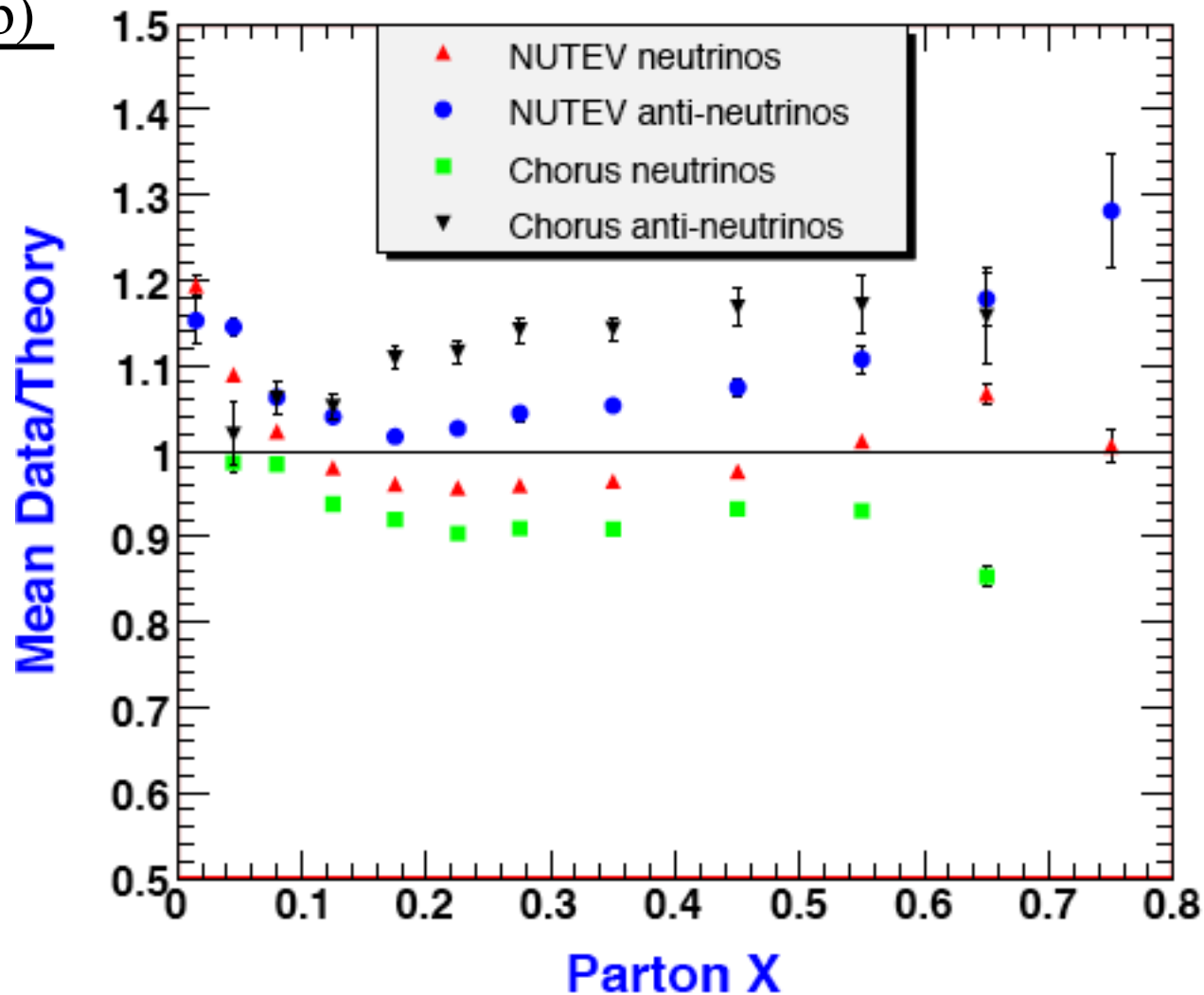


- ◆ F_2 / nucleon changes as a function of A . Measured in $\mu/e - A$, not in $\nu - A$
- ◆ Good reason to consider nuclear effects are DIFFERENT in $\nu - A$.
 - ▼ Presence of axial-vector current.
 - ▼ Different nuclear effects for valance and sea --> different shadowing for xF_3 compared to F_2 .

NuTeV $\sigma(\text{Fe})$ & CHORUS $\sigma(\text{Pb})$ ν scattering (un-shifted) results compared to reference fit

Kulagin-Petti nuclear corrections

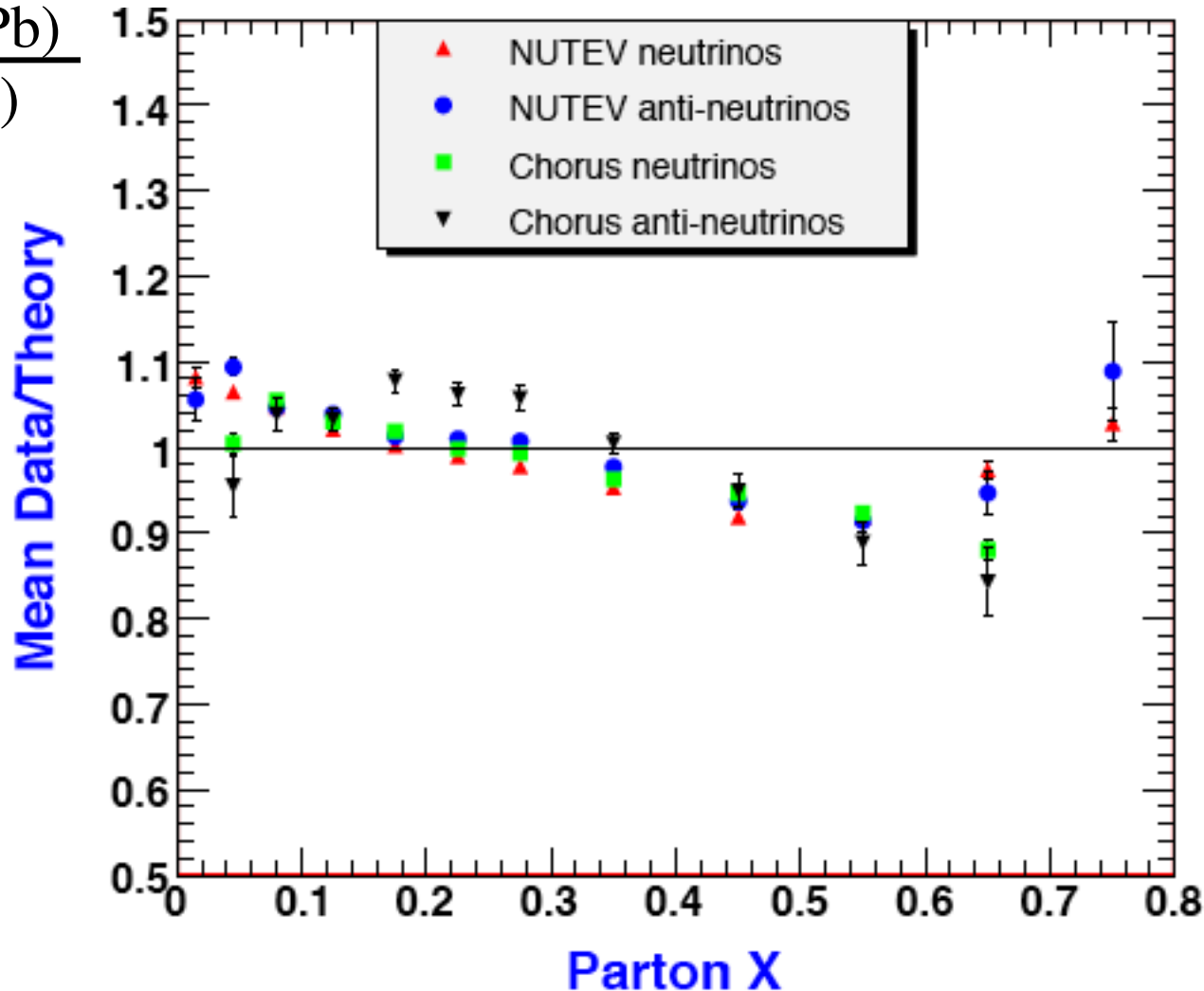
$$\frac{\sigma(\text{Fe or Pb})}{\sigma(n+p)}$$



NuTeV(Fe) and CHORUS (Pb) ν scattering (unshifted) σ results compared to reference fit

no nuclear corrections

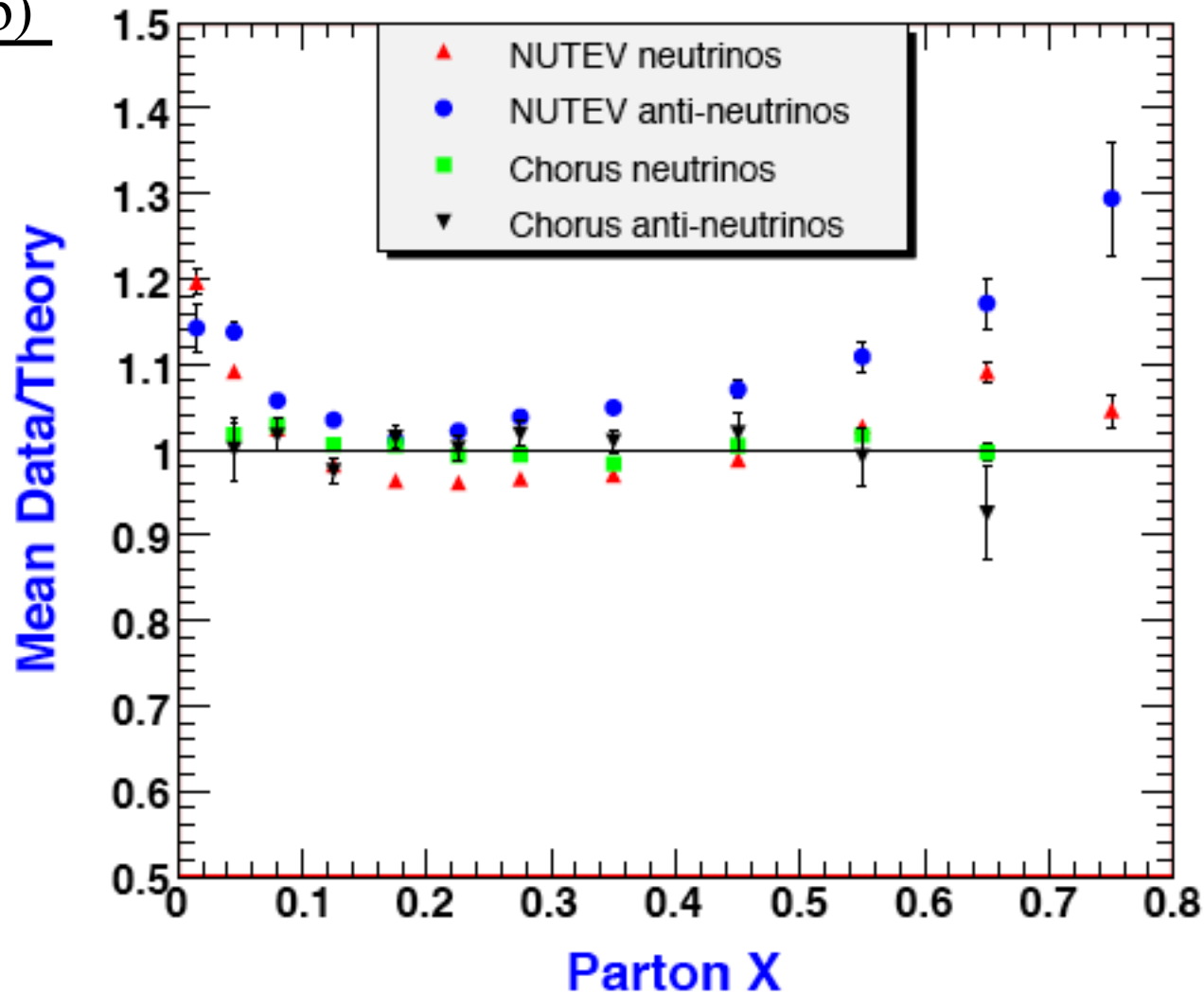
$$\frac{\sigma(\nu\text{Fe or } \nu\text{Pb})}{\sigma(\nu''n+p'')}$$



NuTeV $\sigma(\text{Fe})$ & CHORUS $\sigma(\text{Pb})$ ν scattering (shifted) results compared to reference fit

Kulagin-Petti nuclear corrections

$$\frac{\sigma(\text{Fe or Pb})}{\sigma(n+p)}$$



Comparison of Data to the Kulagin-Petti Model

thanks to Roberto Petti

