

Low p_T pion production in heavy-ion collisions at the LHC

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Statistical models of hadron production have become one of the cornerstones of our understanding of ultra relativistic heavy-ion collisions (and also of more elementary hadronic processes and e^+e^- annihilation)

(Becattini, Braun-Munzinger, Broniowski, Cleymans, Gaździcki, Gorenstein, Rafelski, Redlich, Satz, Stachel, Stock, ...)

The new data from the Large Hadron Collider (LHC) collected in Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV come as a big surprise: **the measured proton abundances do not agree with the most common version of the thermal model based on the grand-canonical ensemble**

Possible explanations:

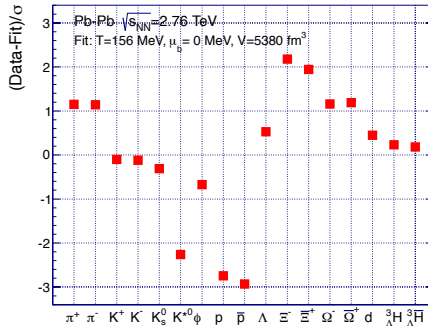
- hadronic rescattering in the final stage
(Becattini, Bleicher, Kollegger, Schuster, Steinheimer, Stock, PRL 111 (2013) 082302)
- hadronization and subsequent freeze-out taking place off chemical equilibrium
(Petran, Rafelski, PRC 88 (2013) 021901; Petran, Letessier, Petracek, Rafelski, PRC 88 (2013) 034907)

Motivation 1

Problems of thermal models with the proton yield

Results of the thermal equilibrium model

(Stachel, Andronic, Braun-Munzinger, Redlich, J.Phys.Conf.Ser. 509 (2014) 012019)

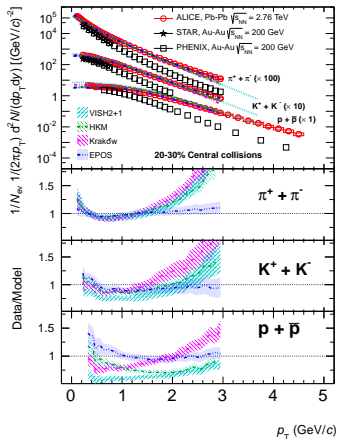
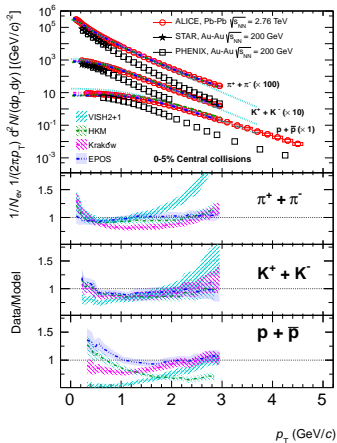


Besides the proton anomaly, the same LHC data exhibits another interesting feature — the low-transverse-momentum pion spectra show enhancement by about 25%–50% with respect to the predictions of various thermal and hydrodynamic models (ALICE papers compare experimental data to various hydro models, PRL 109 (2012) 252301, PRC 88 (2013) 044910)

Theory vs. Hydro comparison (ALICE, PRC 88 (2013) 044910)

most central

semi central



- **Gluon condensate** (Blaizot, Gelis, Liao, McLerran, Venugopalan, Nucl. Phys. A904-905 (2013) 829c; Blaizot, Liao, McLerran, Nucl. Phys. A920 (2013) 58, Blaizot, Lect. Notes Phys. 852 (2012) 1)
- **Coherent pion production found in three-body correlations by ALICE** (ALICE, Phys.Rev. C89 (2014) 024911)

In this talk I will argue that the two problems may be solved simultaneously within the chemical non-equilibrium model.

1. Cracow single-freeze out model
2. Non-equilibrium statistical model
3. Spectra of pions, kaons and protons
4. Spectra of other hadrons
5. Conclusions

1. Cracow single-freeze out model

1.1 Freeze-out hypersurface and flow

Single-freeze out model (Broniowski, Florkowski, PRL 87 (2001) 272302)

Monte-Carlo implementations, THERMINATOR 1 & 2 (Kisiel, Taluc, Broniowski, Florkowski, Comput. Phys. Commun. 174 (2006) 669; Chojnacki, Kisiel, Florkowski, Broniowski, Comput. Phys. Commun. 183 (2012) 746)

The spectra are calculated from the Cooper-Frye formula

$$\frac{dN}{dyd^2p_T} = \int d\Sigma_\mu p^\mu f(p \cdot u)$$

The freeze-out hyper surface is defined by the conditions

$$t^2 = \tau_f^2 + x^2 + y^2 + z^2, \quad x^2 + y^2 \leq r_{\max}^2$$

The flow has the Hubble form

$$u^\mu = x^\mu / \tau_f$$

There are only two independent parameters in the model: the product $\pi\tau_f r_{\max}^2$ defines the volume (per unit rapidity), the ratio r_{\max}/τ_f determines the shape (slope) of the spectra

The phase-space distributions include all well established resonances from PDG, the primordial distributions in the local rest frame have the form

$$f_i = g_i \int \frac{d^3 p}{(2\pi)^3} \frac{1}{\Gamma_i^{-1} \exp(\sqrt{m^2 + p^2}/T) \pm 1}$$

2. Non-equilibrium statistical model

2.1 Fugacity

Parameterization of the fugacity as in SHARE

(Torrieri, Steinke, Broniowski, Florkowski, Lefessier, Rafelski, Comput. Phys. Commun. 167 (2005) 229)

$$\tau_i = (\lambda_q \gamma_q)^{N_q^i} (\lambda_s \gamma_s)^{N_s^i} (\lambda_{\bar{q}} \gamma_{\bar{q}})^{N_{\bar{q}}^i} (\lambda_{\bar{s}} \gamma_{\bar{s}})^{N_{\bar{s}}^i}$$

$$\lambda_q = \lambda_{\bar{q}}^{-1}, \lambda_s = \lambda_{\bar{s}}^{-1}, \gamma_q = \gamma_{\bar{q}}, \gamma_s = \gamma_{\bar{s}}$$

N_q^i and N_s^i are the numbers of light (u, d) and strange (s) quarks in the i th hadron, while $N_{\bar{q}}^i$ and $N_{\bar{s}}^i$ are the numbers of the antiquarks in the same hadron

using the Gell-Mann–Nishijima formulas one finds

$\lambda_q = \exp(\mu_B/3T)$ and $\lambda_s = \exp((-3\mu_S + \mu_B)/3T)$, which gives

$$\tau_i = \gamma_q^{N_q^i + N_{\bar{q}}^i} \gamma_s^{N_s^i + N_{\bar{s}}^i} \exp\left(\frac{\mu_B B_i + \mu_S S_i}{T}\right)$$

2. Non-equilibrium statistical model

2.2 Fugacity and chemical potentials

At the LHC, in the central rapidity region the baryon number density and strangeness are negligible, $\mu_B \approx \mu_S \approx 0$

$$\mathcal{r}_i \approx \gamma_q^{N_q^i + N_{\bar{q}}^i} \gamma_s^{N_s^i + N_{\bar{s}}^i}$$

The parameters γ_q and γ_s are equivalent to the chemical potentials $\mu_q/T = \ln \gamma_q$ and $\mu_s/T = \ln \gamma_s$

$$\mathcal{r}_i \approx \exp \left(\frac{\mu_q (N_q^i + N_{\bar{q}}^i) + \mu_s (N_s^i + N_{\bar{s}}^i)}{T} \right)$$

The new potentials are connected with the conservation of the SUM of the number of quarks and antiquarks during the hadronization process, similarly as μ_B and μ_S are connected with the conservation of the DIFFERENCE of the quark and antiquark numbers. Rafelski: This must be so, since the entropy is conserved during the hadronization process (the entropy is a measure of the sum of the quarks and antiquarks). This argument is convincing if the hadronization process is fast and there is no significant volume expansion

2. Non-equilibrium statistical model

2.3 Critical value of γ_q

There is an upper bound on γ_q and γ_s because of Bose-Einstein condensation, the singularities may appear in the Bose-Einstein distributions of primordial pions and kaons.

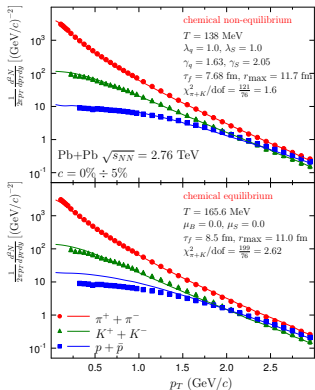
For pions, the value of γ_s is irrelevant, and

$$\gamma_q^{\text{critic}} = \exp\left(\frac{m_{\pi^0}}{2T}\right)$$

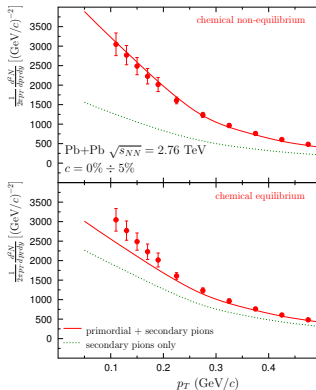
Interestingly, the fits to the ratios of hadron abundances yield γ_q which is very close to the critical value.

3. Spectra of pions, kaons and protons

most central events

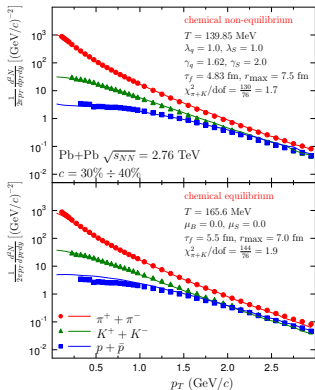


linear scale

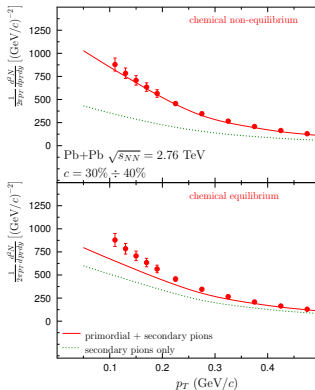


3. Spectra of pions, kaons and protons

semi central events



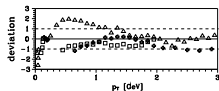
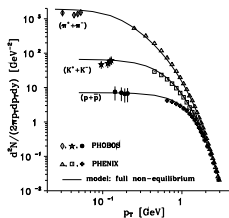
linear scale



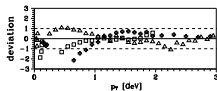
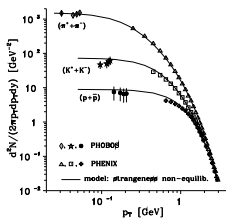
3. Spectra of pions, kaons and protons at RHIC

Dariusz Prorok, Phys. Rev. C75 (2007) 014903

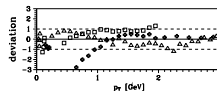
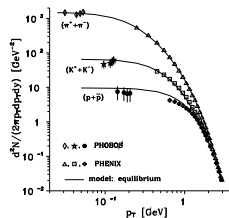
Chemical non eq.



Strangeness non eq.



Equilibrium

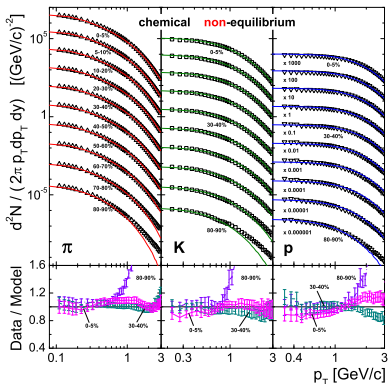


3. Spectra of pions, kaons and protons

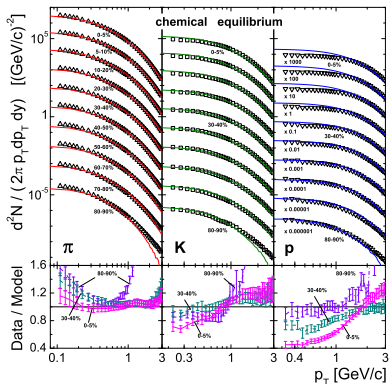
3.3 Centrality dependence

Complete set of pion, kaon, and proton spectra for different centralities

Chemical non-equilibrium



Chemical equilibrium

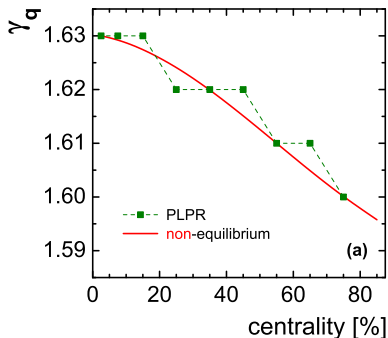


3. Spectra of pions, kaons and protons

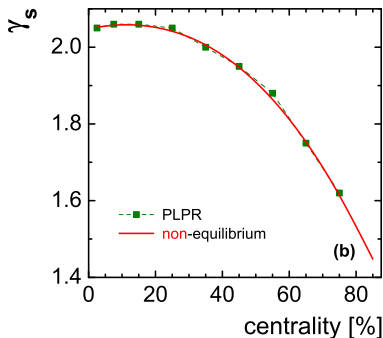
3.3 Centrality dependence

Centrality dependence of γ 's inferred from the fit to the pion, kaon and proton spectra

γ_q

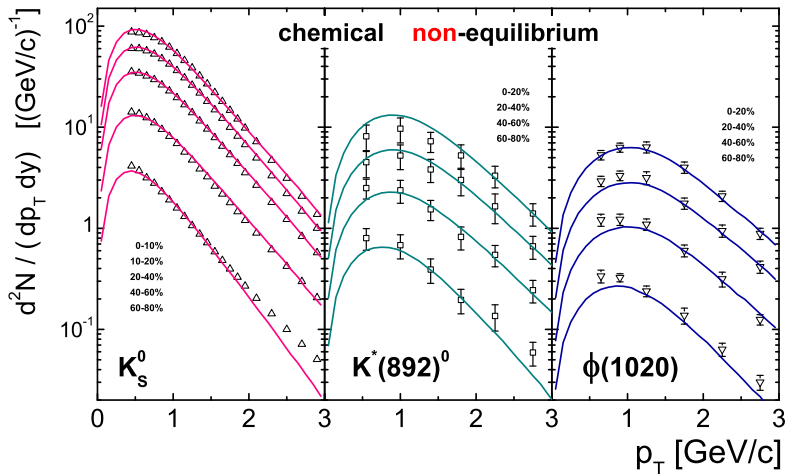


γ_s



4. Spectra of other hadrons

Predictions for other hadrons



- The non-equilibrium thermal model combined with the single-freeze-out scenario explains very well the spectra of pions, kaons, and protons.
- It eliminates the proton anomaly and explains the low- p_T enhancement of pions.
- This enhancement may be interpreted as a signature of the onset of pion condensation in heavy-ion collisions at the LHC energies.
- It would be interesting to measure the pion spectrum at smaller values of p_T than those available at the moment.