

Hard Probes Overview

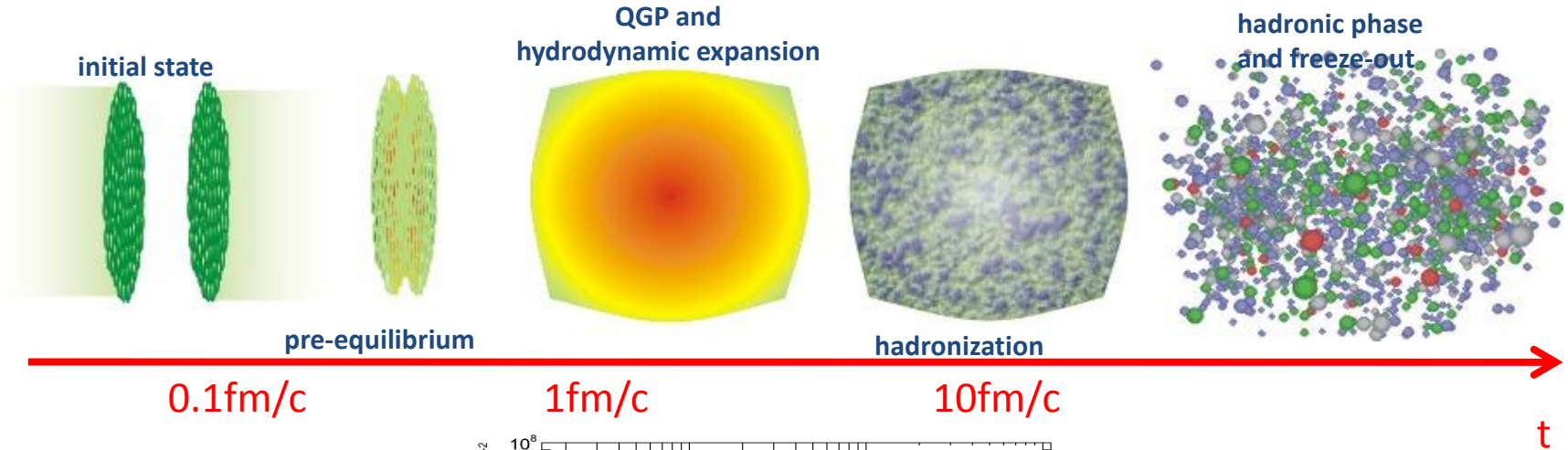
Guang-You Qin

Central China Normal University

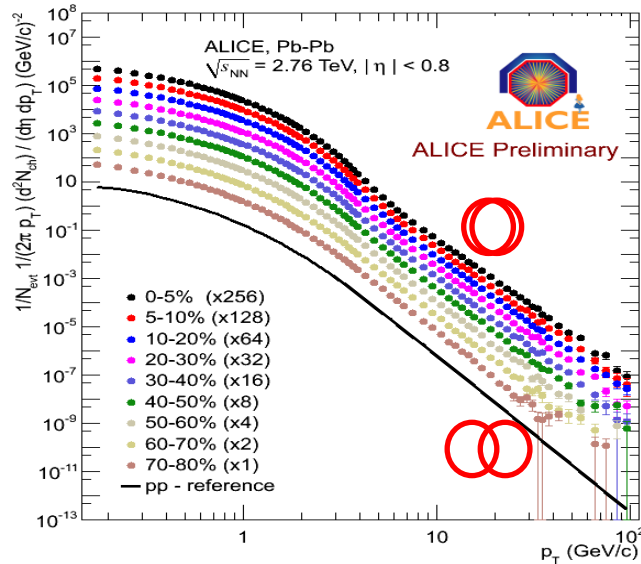
ATHIC 2014, August 5-8
Osaka, Japan



Probes of QGP in Heavy-Ion Collisions



Anisotropic Flow
...
Collectivity, Fluidity



Soft Probes



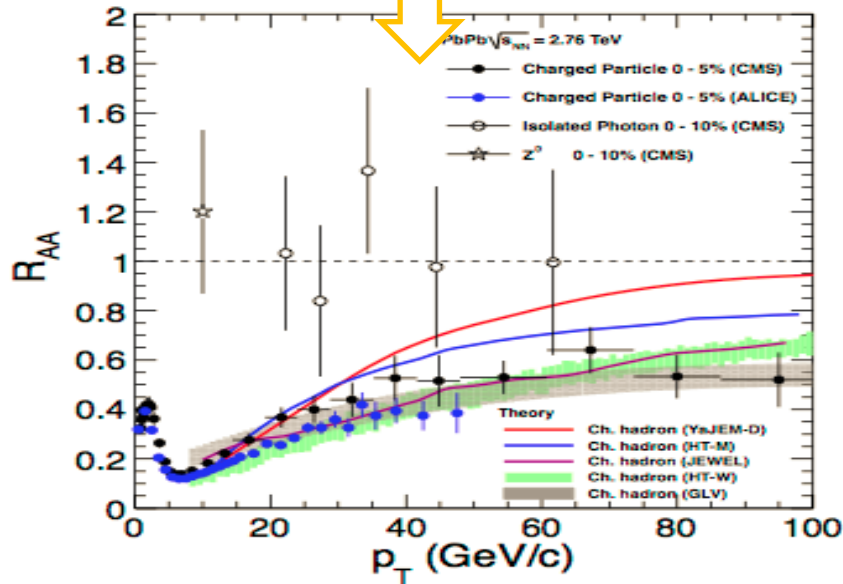
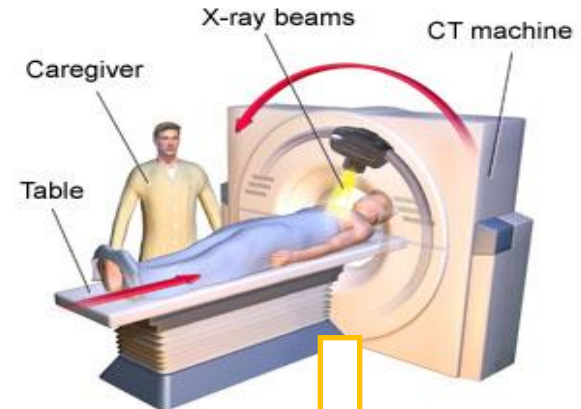
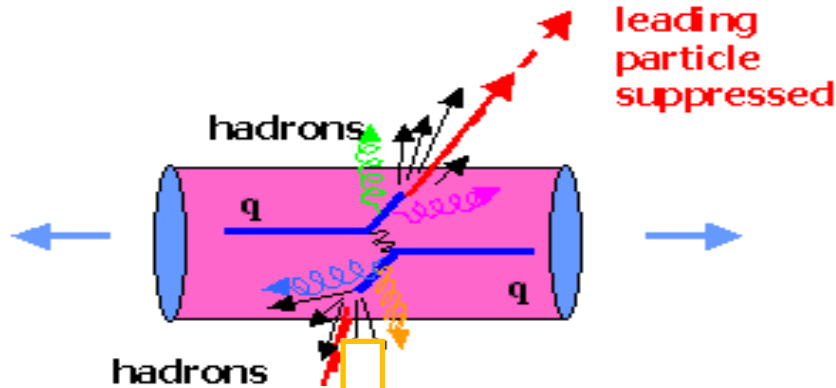
“jet” sec., August 6

Jet Quenching
...
Color Opacity

This Talk

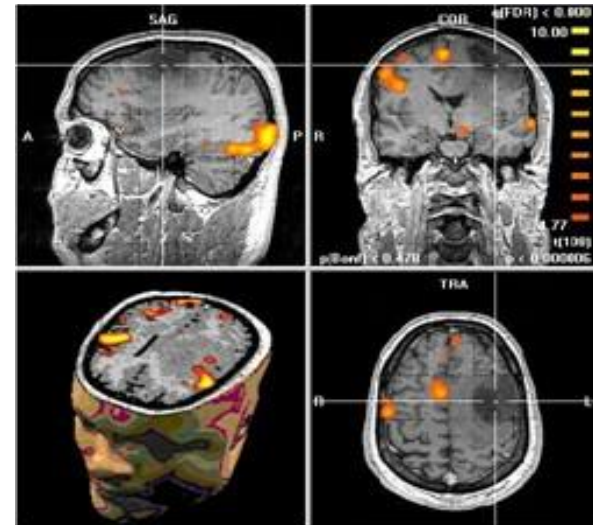
Hard Probes

Jet quenching & jet tomography

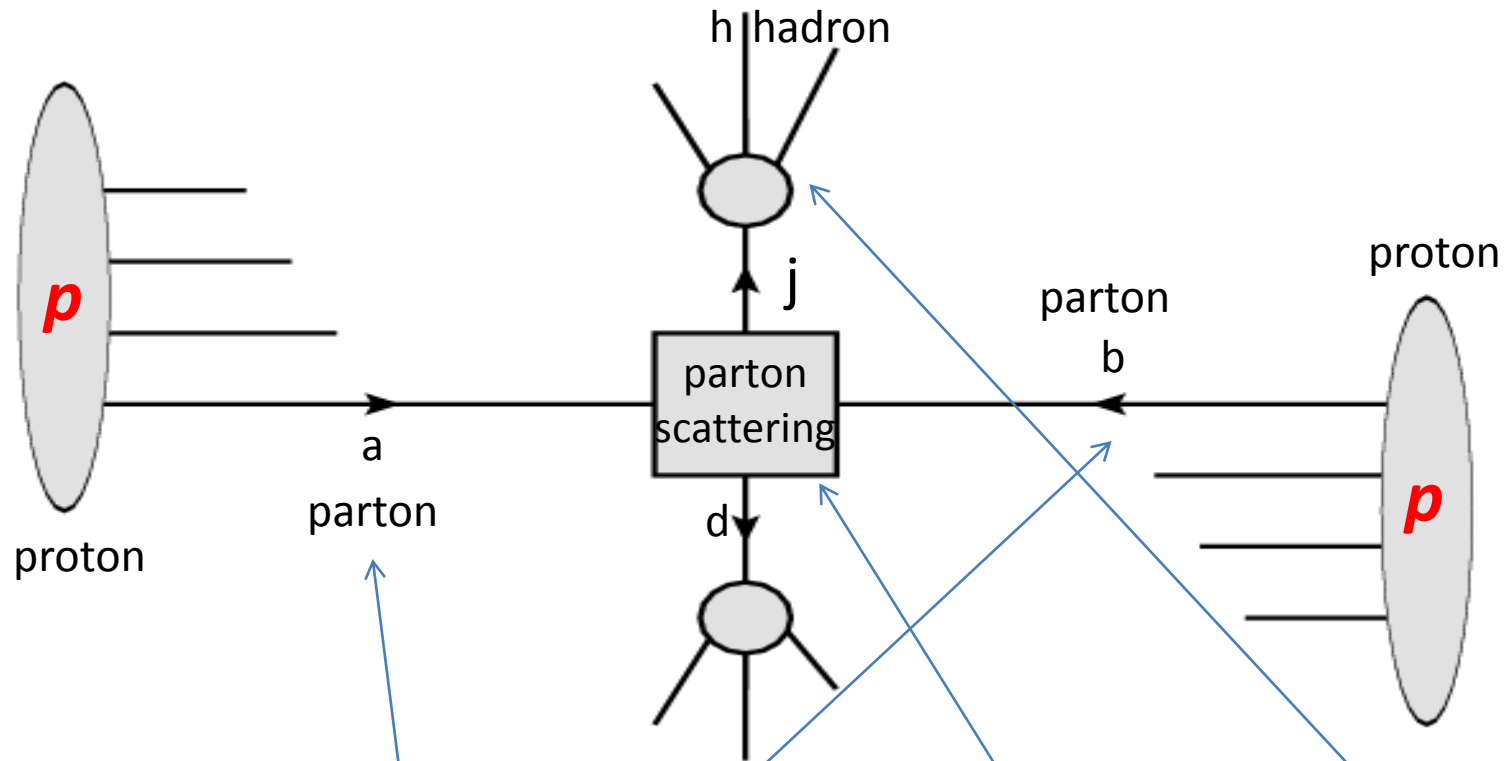


$$R_{AA} = \frac{dN^{AA} / d^2 p_T dy}{N_{coll} dN^{pp} / d^2 p_T dy}$$

Computerized Axial Tomography Scan



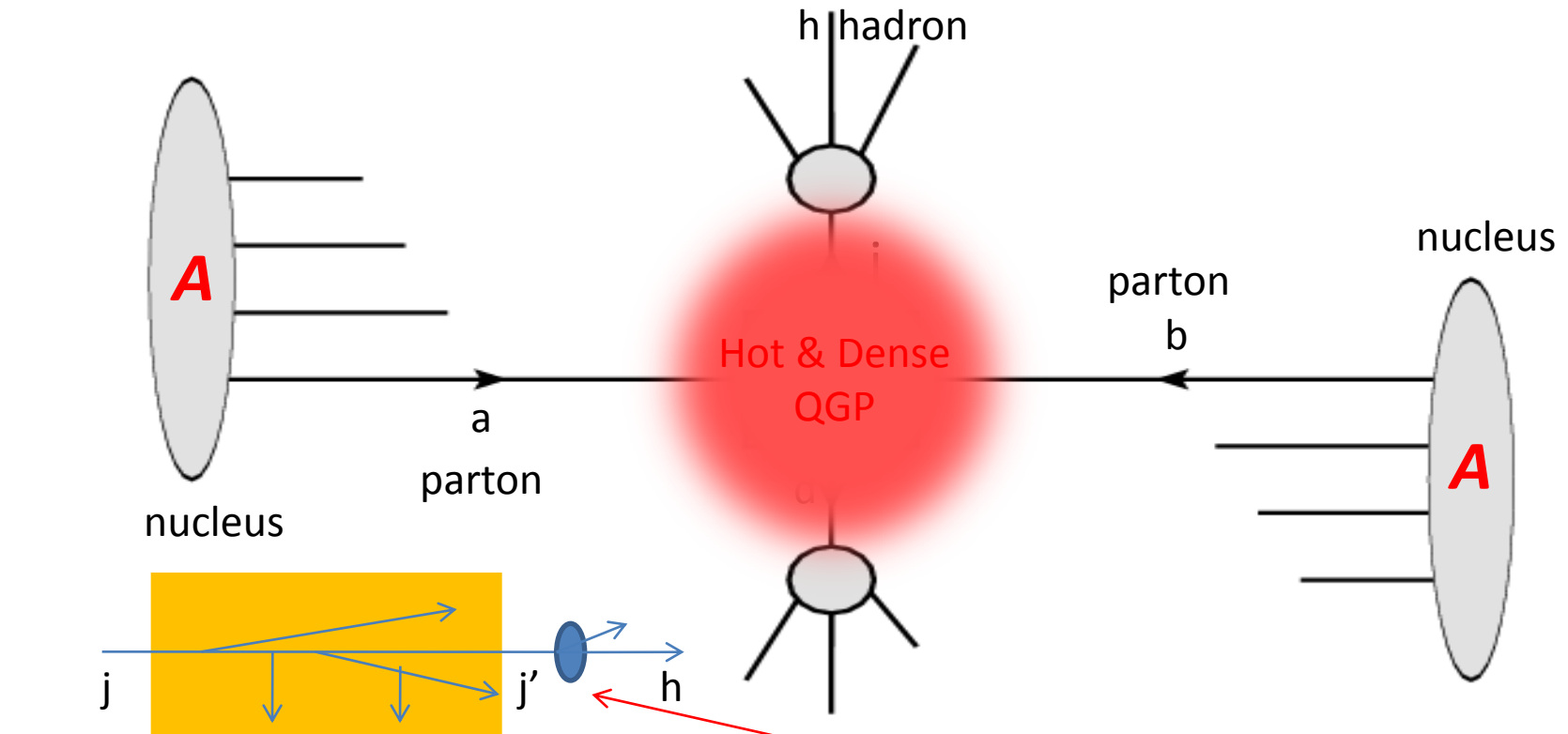
General framework of jet quenching study



$$d\sigma_h = \sum_{abjd} f_{a/A} \otimes f_{b/B} \otimes d\sigma_{ab \rightarrow jd} \otimes D_{h/j}$$

pQCD factorization: Large- p_T processes may be factorized into **long-distance** pieces in terms of **PDF & FF**, and **short-distance** parts describing **hard interactions** of partons.

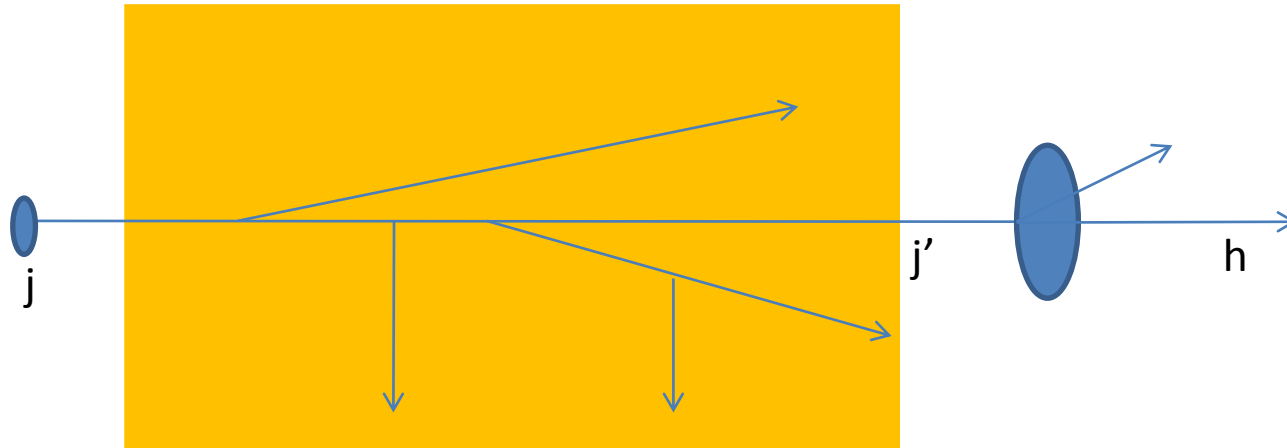
General framework of jet quenching study



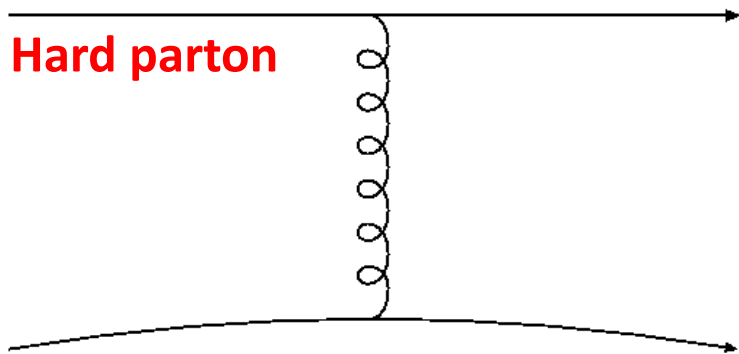
$$d\tilde{\sigma}_h = \sum_{abjd} f_{a/A} \otimes f_{b/B} \otimes d\sigma_{ab \rightarrow jd} \otimes \tilde{D}_{h/j}$$

$$d\tilde{\sigma}_h = \sum_{abjj'd} f_a \otimes f_b \otimes d\sigma_{ab \rightarrow jd} \otimes P_{j \rightarrow j'} \otimes D_{h/j'}$$

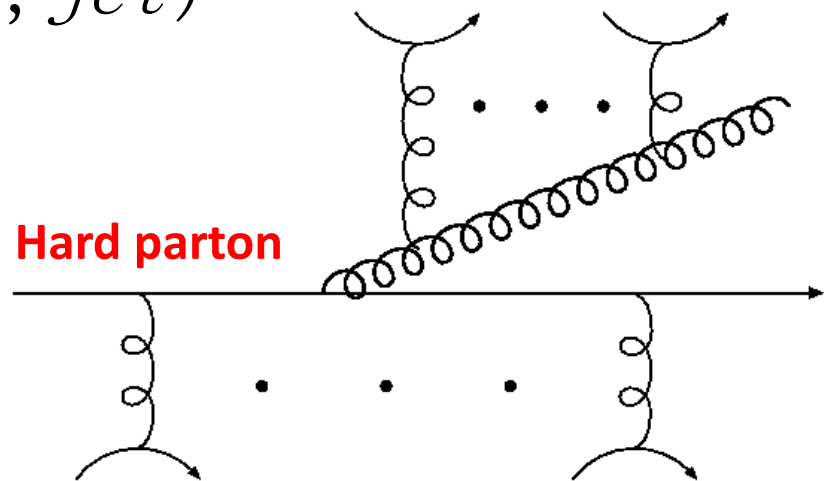
Jet evolution and energy loss in QGP



$$P_{j \rightarrow j'}(\text{medium, jet})$$



Elastic (collisional)



Inelastic (radiative)

Rad. E-loss

- **Single gluon emission**

- **Multiple soft scatterings (BDMPS-Z, ASW, AMY)**
- **Few hard scatterings (DGLV, HT)**
- **Recent developments:**
 - **AMY: finite L** (Caron-Huot, Gale 2010)
 - **GLV: finite dynamical medium** (Djordjevic, Heinz, 2008)
 - **DGLV: non-zero magnetic mass** (Djordjevic, Djordjevic, 2012)
 - **Higher Twist (HT): multiple scatterings** (Majumder 2012)

$$\frac{dN_g}{dxdk_{\perp}^2 dt}(T, E, \dots) = ?$$

BDMPS-Z: Baier-Dokshitzer-Mueller-Peigne-Schiff-Zakharov

ASW: Amesto-Salgado-Wiedemann

AMY: Arnold-Moore-Yaffe

DGLV: Djordjevic-Gyulassy-Levai-Vitev

HT: Wang-Guo-Majumder

- **Mutiple gluon emission**

- **Poisson convolution (BDMPS/ASW/DGLV)**

$$P(\Delta E) = \sum_{n=0}^{\infty} \frac{e^{-\langle N_g \rangle}}{n!} \left[\prod_{i=1}^n \int d\omega \frac{dI(\omega)}{d\omega} \right] \delta \left(\Delta E - \sum_{i=1}^n \omega_i \right)$$

- **Rate equation (AMY)**

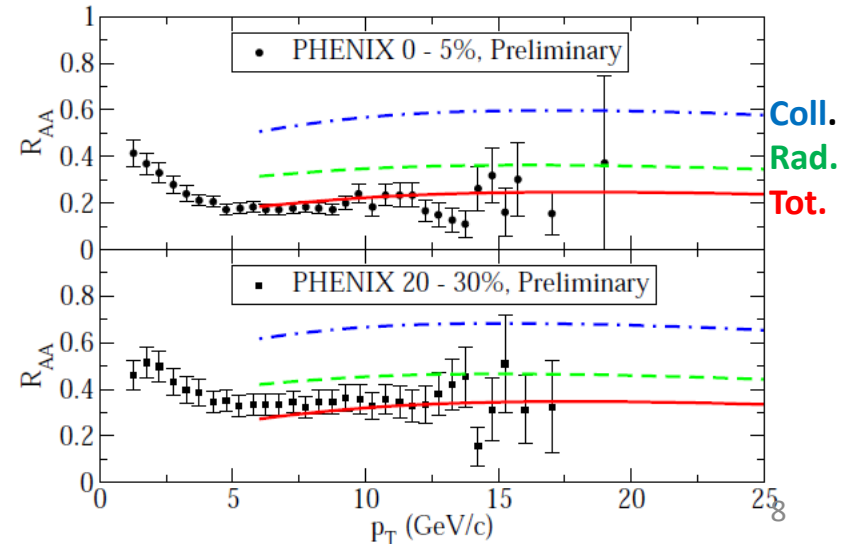
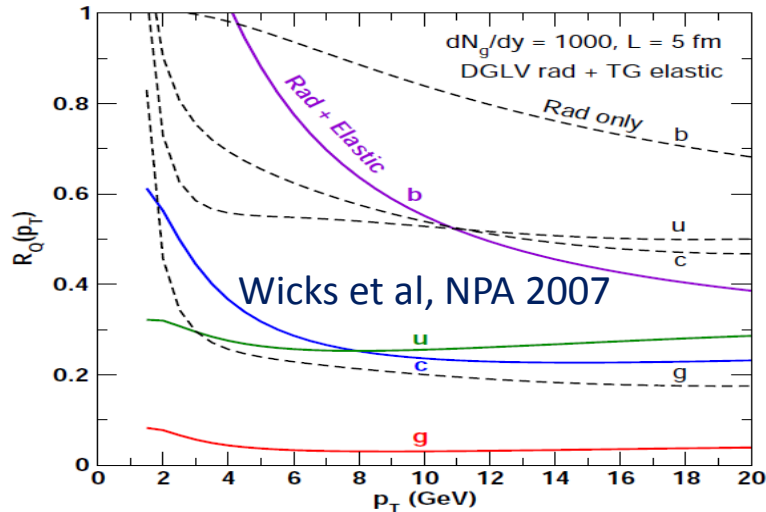
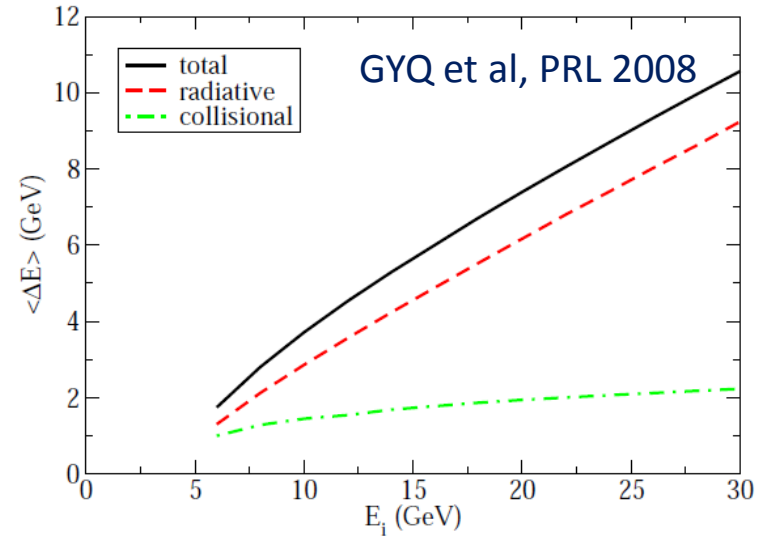
$$\frac{df(p, t)}{dt} = \int dk f(p + k, t) \frac{d\Gamma(p + k, k)}{dkdt} - \int dk f(p, t) \frac{d\Gamma(p, k)}{dkdt}$$

- **DGLAP-like evolution equation (HT)**

$$\frac{\partial \tilde{D}(z, Q^2)}{\partial \ln Q^2} = \frac{\alpha_s}{2\pi} \int \frac{dy}{y} P(y) \int d\zeta^- K(\zeta^-, q^-, y, Q^2) \tilde{D}\left(\frac{z}{y}, Q^2\right)$$

Coll. E-loss

- **First studied by Bjorken:**
 - Bjorken 1982; Bratten, Thoma 1991; Thoma, Gyulassy, 1991; Mustafa, Thoma 2005; Peigne, Peshier, 2006; Djordjevic (GLV), 2006; Wicks et al (DGLV), 2007; GYQ et al (AMY), 2008...
- **Main findings:**
 - dE/E small compared to rad. for large E
 - Sizable contribution in R_{AA} calculation (especially for heavy flavors)
 - Important for studying full jet energy loss and medium response (see later)



Jet quenching parameter

Jet transport coefficient:

$$\hat{q} = \frac{d\langle \Delta p_{\perp}^2 \rangle}{dt} = \int \frac{dk_{\perp}^2}{(2\pi)^2} k_{\perp}^2 \frac{d\sigma}{dk_{\perp}^2} \approx \frac{4\pi\alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{\mu+}(0) F_{\mu}^+(y^-) \rangle$$

BDMPS-Z (Baier-Dokshitzer-Mueller-Peigne-Schiff-Zakharov) $\Delta E_{\text{rad}} \approx \alpha_s N_c \hat{q} L^2$

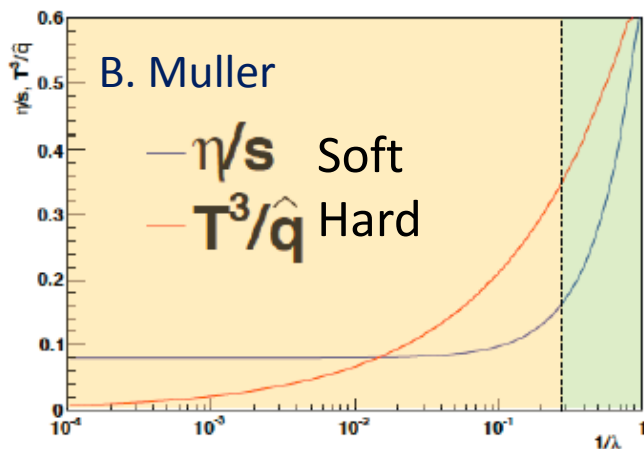
Higher-Twist (Wang-Guo-Majumder)

$$\frac{dN_g}{dx dk_{\perp}^2 dt} = \frac{2\alpha_s}{\pi} P(x) \frac{\hat{q}}{k_{\perp}^4} \sin^2\left(\frac{t - t_i}{2\tau_f}\right)$$

ASW: Amesto-Salgado-Wiedemann

AMY: Arnold-Moore-Yaffe

DGLV: Djordjevic-Gyulassy-Levai-Vitev



At weak coupling:

$$\frac{T^3}{\hat{q}} \approx \# \frac{\eta}{s}$$

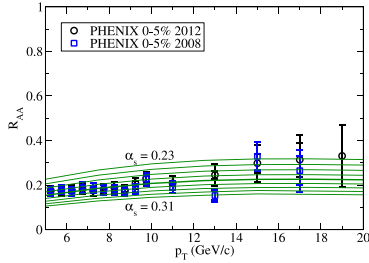
At strong coupling:

$$\frac{T^3}{\hat{q}} \ll \# \frac{\eta}{s}$$

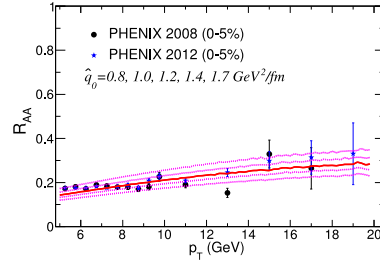
If they can be determined precisely, we may figure out how (at what scale) QGP becomes strongly coupled (from a weakly-coupled high T regime)

Jet quenching @ RHIC & LHC

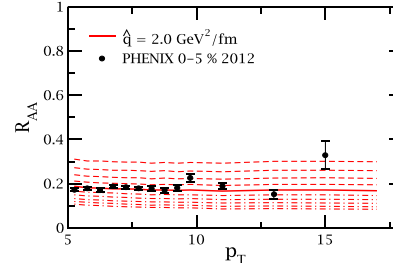
McGill-AMY



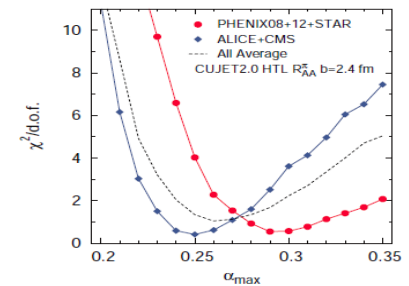
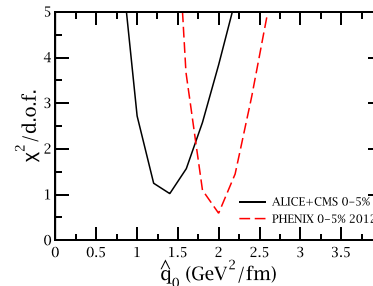
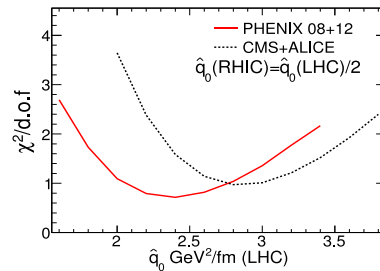
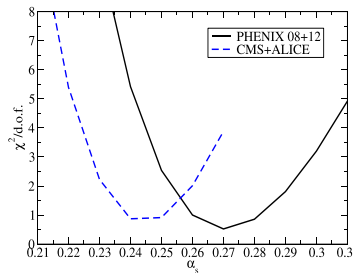
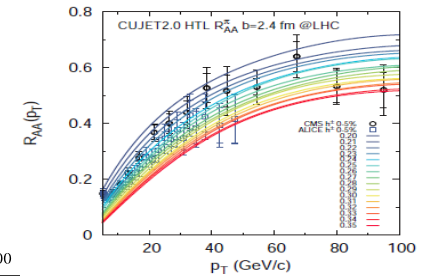
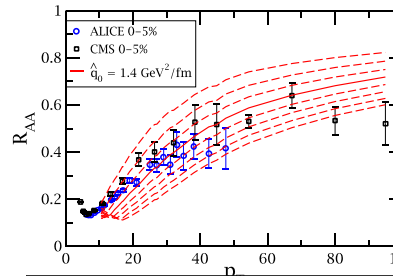
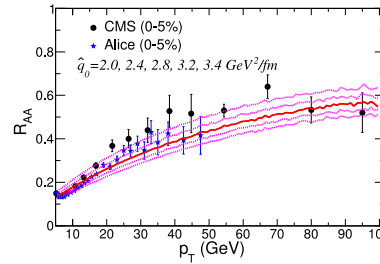
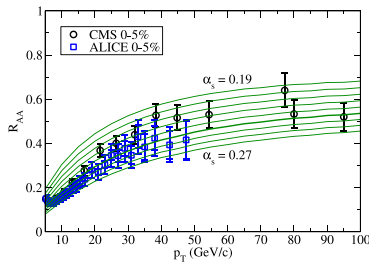
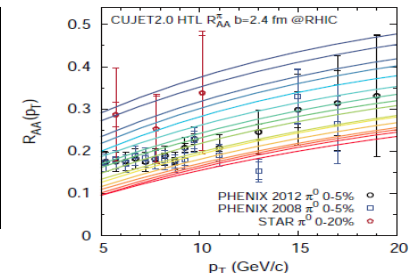
HT-BW



HT-M



CUJET



GYQ, et al, PRL 2008

Chen, Hirano, Wang,
Wang, Zhang, PRC 2011

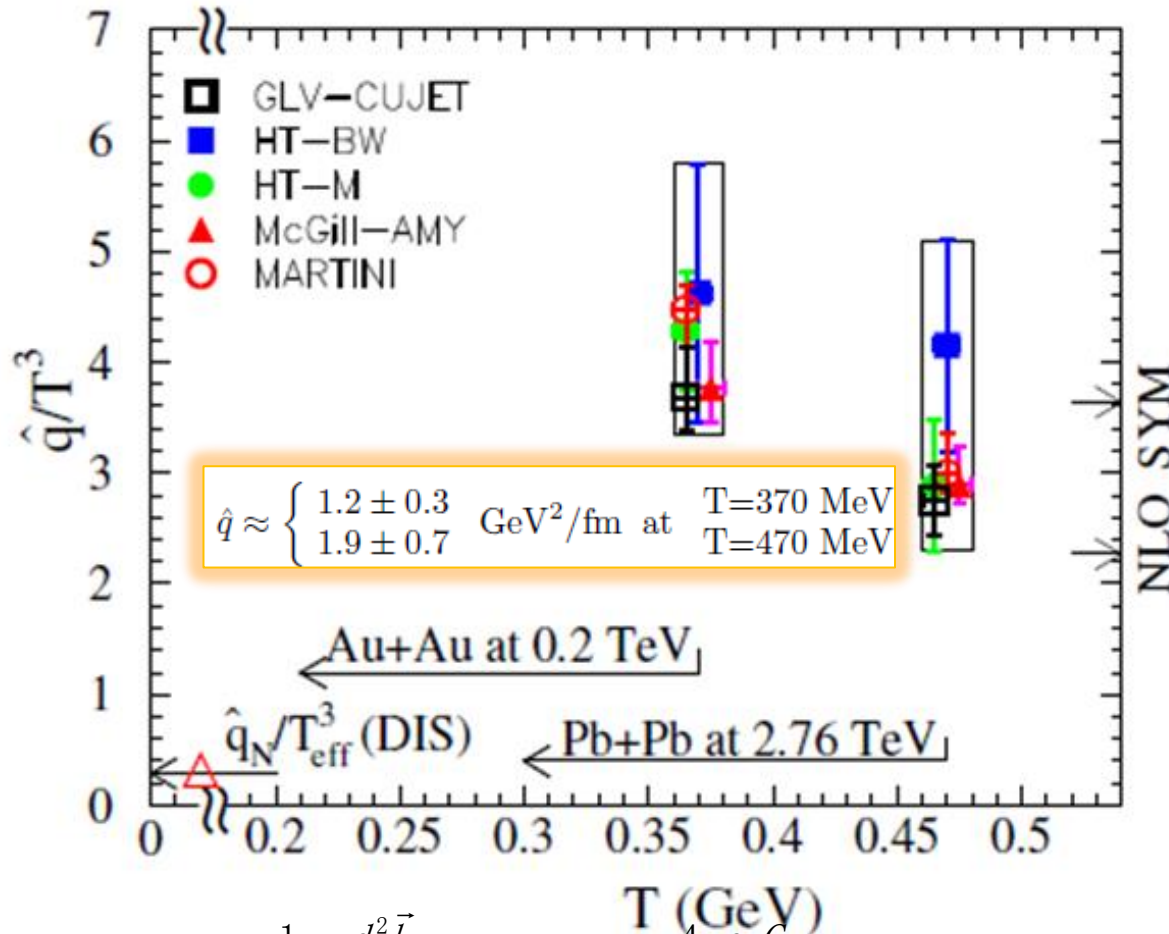
Majumder, Chun,
PRL 2012

Xu, Buzzatti, Gyulassy,
arXiv: 1402.2956



, arXiv:1312.5003 [nucl-th]

Extracting jet quenching parameter



McGill-AMY:

GYQ, Ruppert, Gale, Jeon, Moore, Mustafa, PRL 2008

HT-BW:

Chen, Hirano, Wang, Wang, Zhang, PRC 2011

HT-M:

Majumder, Chun, PRL 2012

GLV-CUJET:

Xu, Buzzatti, Gyulassy, arXiv: 1402.2956

MARTINI-AMY:

Schenke, Gale, Jeon, PRC 2009

NLO SYM:

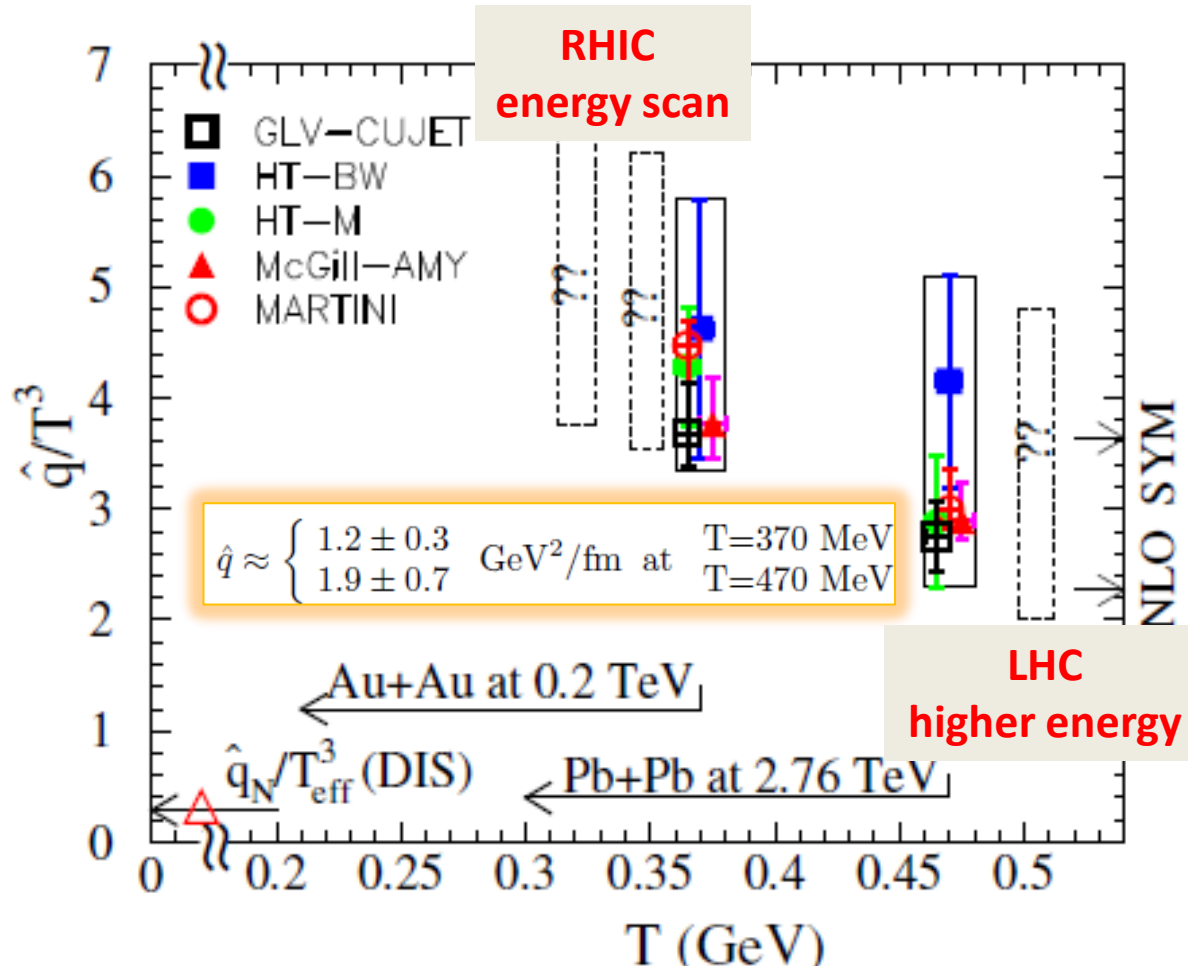
Zhang, Hou, Ren, JHEP 2013

$$\hat{q} = \frac{1}{L} \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} k_\perp^2 P(\vec{k}_\perp, L) \approx \frac{4\pi\alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{\mu+}(0) F_\mu^+(y^-) \rangle$$



, arXiv:1312.5003 [nucl-th]

Extracting jet quenching parameter



McGill-AMY:

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MARTINI-AMY:

Schenke, Gale, Jeon, PRC 2009

NLO SYM:

Zhang, Hou, Ren, JHEP 2013

JET Collaboration,

arXiv:1312.5003 [nucl-th]

$$\hat{q} = \int \frac{dk_{\perp}^2}{(2\pi)^2} k_{\perp}^2 \frac{d\sigma}{dk_{\perp}^2} \approx \frac{4\pi\alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{\mu+}(0) F_{\mu}^{+}(y^-) \rangle$$

Map the temperature dependence of jet transport parameters

q^{hat} from lattice

$$\hat{q} = \frac{1}{L} \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} k_\perp^2 P(\vec{k}_\perp, L)$$

$$P(\vec{k}_\perp, L^-) = \int \frac{d^2 \vec{k}'_\perp}{(2\pi)^2} e^{-i\vec{k}'_\perp \cdot \vec{y}_\perp} P(\vec{y}_\perp, L^-)$$

$$P(\vec{y}_\perp, L^-) = \frac{1}{N_c} \text{Tr} \langle \mathcal{W}(\vec{y}_\perp, L^-) \rangle$$

$$\frac{dP(\vec{y}_\perp, L^-)}{dL} = -V(\vec{y}_\perp) P(\vec{y}_\perp, L^-)$$

$$V(\vec{y}_\perp) = \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} (1 - e^{i\vec{k}_\perp \cdot \vec{y}_\perp}) C(\vec{k}_\perp)$$

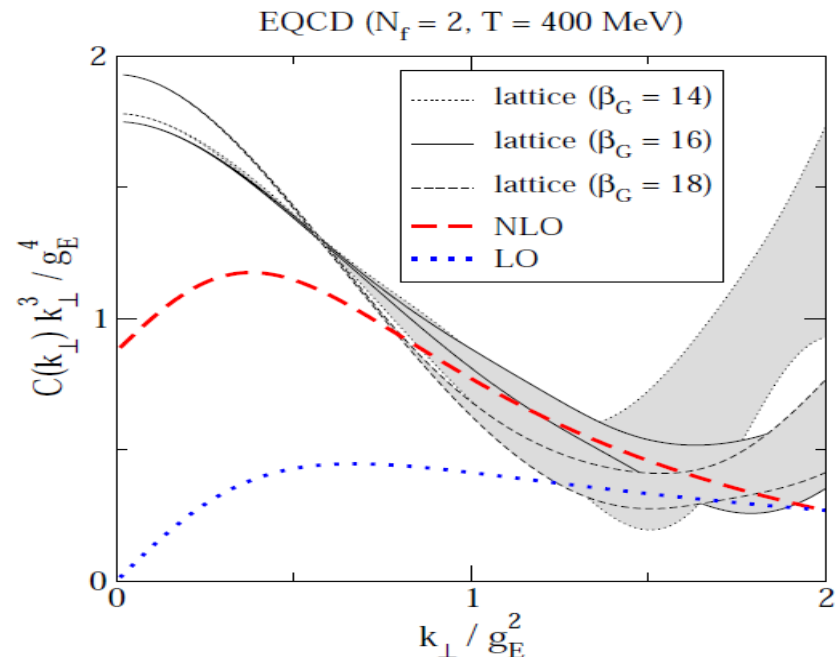
Majumder, PRC 2013; Panero, Rummukainen, Schafer, PRL 2014; Laine, Rothkopf, JHEP 2013; arXiv:1310.2413; Caron-Huot, PRD 2009; Benzke, Brambilla, Escobedo, Vairo, JHEP 2013; D'Eramo, Lekaveckas, Liu, Rajagopal, JHEP 2013



$$\hat{q} \approx \begin{cases} 1.2 \pm 0.3 \\ 1.9 \pm 0.7 \end{cases} \text{ GeV}^2/\text{fm} \text{ at } \begin{matrix} T=370 \text{ MeV} \\ T=470 \text{ MeV} \end{matrix}$$

Quenched SU(2): $\hat{q} \approx 1.3 - 3.3 \text{ GeV}^2/\text{fm} @ T = 400 \text{ MeV}$

Lattice EQCD: $\hat{q} \approx 6 \text{ GeV}^2/\text{fm} \pm 20\% @ RHIC$



Discrepancy is unclear so far and needs further investigation

Renormalization of q^{hat}

- **Radiative correction to transverse momentum broadening $\langle p_{\perp}^2 \rangle$** (Wu, JHEP 2011; Liou, Mueller, Wu, NPA 2013)

$$\langle p_{\perp}^2 \rangle_{rad} = \hat{q}_0 L \left[C_2 \frac{\alpha_s N_c}{\pi} \ln^2 \left(\frac{L}{\tau_0} \right) + C_1 \frac{\alpha_s N_c}{\pi} \ln \left(\frac{L}{\tau_0} \right) + C_0 \right]$$

$$\tau_0 \approx 1/T \ll L$$

- **The double-logarithmic corrections may be absorbed into a redefinition of jet quenching parameter q^{hat}** (Iancu, arXiv:1403.1996; Blaizot, Mehtar-Tani, arXiv:1403.2323)

$$\hat{q}(\tau) = \hat{q}_0 \left[1 + \frac{\bar{\alpha}}{2} \ln \left(\frac{\tau}{\tau_0} \right) \right]$$

$$\frac{\partial \hat{q}(\tau, Q^2)}{\partial \ln \tau} = \int_{\hat{q}\tau}^{Q^2} \frac{dq^2}{q^2} \bar{\alpha} \hat{q}(\tau, q^2)$$

- **For large media, anomalous length dependence of q^{hat} and mean energy loss**

$$\hat{q}(L) \propto L^{\gamma}, \quad \langle p_{\perp}^2 \rangle \propto \hat{q}_0 L^{1+\gamma}, \quad \langle \Delta E \rangle \propto \hat{q}_0 L^{2+\gamma}$$

$$\gamma = 2\sqrt{\bar{\alpha}} = 2\sqrt{\alpha_s N_c / \pi}$$

Renormalization of q^{hat}

- Calculate NLO QCD corrections to transverse momentum broadening in hadron production in SIDIS

$$\frac{d\langle k_{\perp}^2 \sigma \rangle_{NLO}}{dz} = \sigma_0 T_{qg}(x, 0, 0, \mu_f^2) \otimes H_{NLO}(x, x_B, Q^2, \mu_f^2) \otimes D(z, \mu_f^2)$$

- Collinear divergence is factorized into the redefinition of PDF & twist-4 quark-gluon correlation function

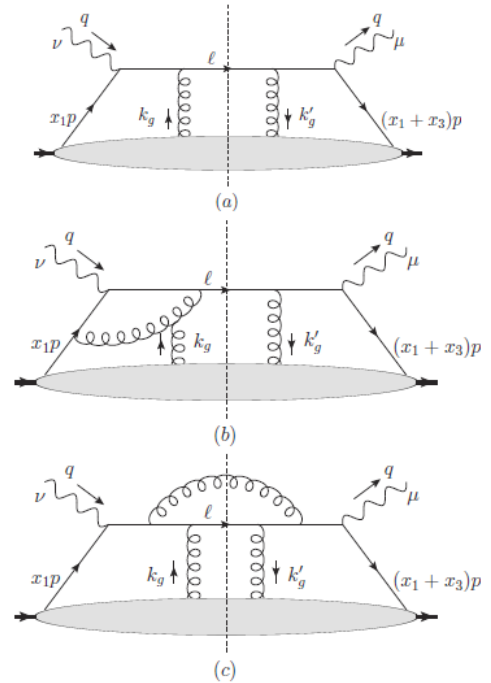
$$\frac{\partial}{\partial \ln \mu_f^2} T_{qg}(x_B, 0, 0, \mu_f^2) = \frac{\alpha_s}{2\pi} \int_{x_B}^1 \frac{dx}{x} \left[\mathcal{P}_{qg \rightarrow qg} \otimes T_{qg} + P_{qg}(\hat{x}) T_{gg}(x, 0, 0, \mu_f^2) \right]$$

- Neglecting the momentum and spatial correlations of two nucleons

$$T_{qg}(x_B, 0, 0, \mu_f^2) \approx \frac{N_c}{4\pi^2 \alpha_s} f_{q/A}(x_B, \mu_f^2) \int dy^- \hat{q}(\mu_f^2, y^-)$$

- The scale dependence of q^{hat}

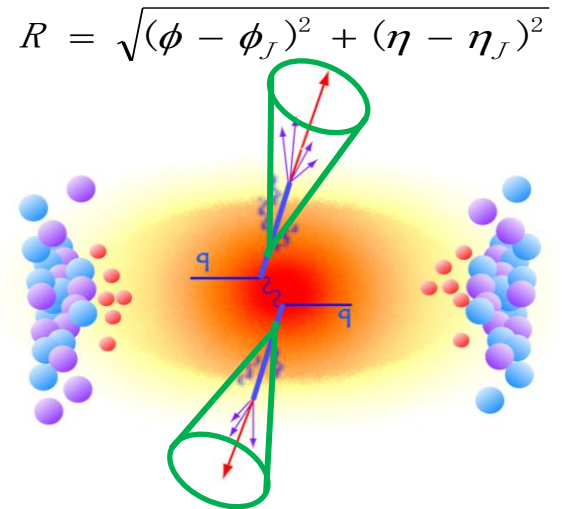
$$\frac{\partial \hat{q}(\mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s}{2\pi} C_A \ln\left(\frac{1}{x_B}\right) \hat{q}(\mu^2) \quad \hat{q}(\mu^2) = \hat{q}(\mu_0^2) \exp\left[\frac{\alpha_s}{2\pi} C_A \ln\left(\frac{1}{x_B}\right) \ln\left(\frac{\mu^2}{\mu_0^2}\right)\right]$$



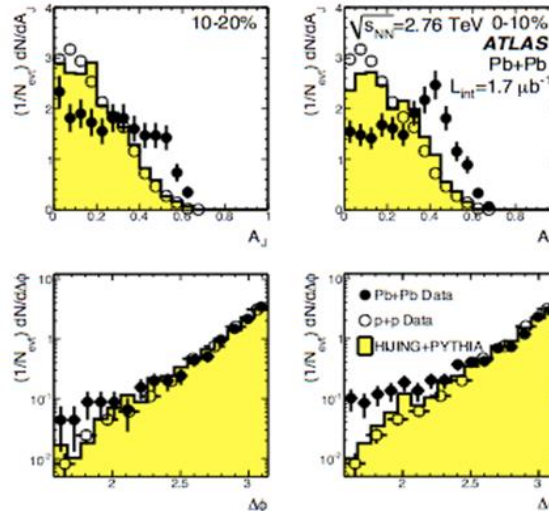
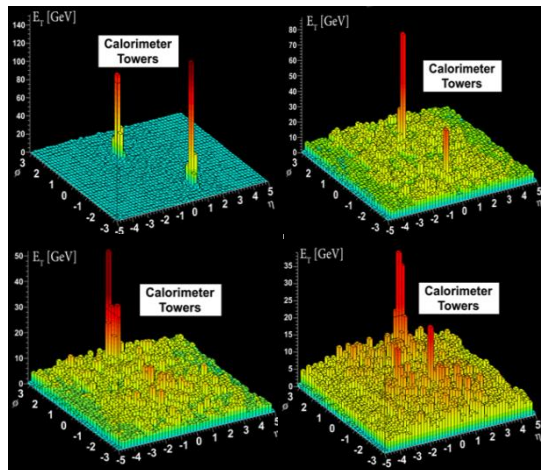
Kang, Wang, Wang, Xing, PRL 2014

Full jet

- **Recombining hadron/parton fragments, hoping to get the original parton energy/momentum**
- **Full jets might be more discriminative with sub-leading fragments**
- **Significant contribution from background in AA collisions; need reliable tools to disentangle jets from background**



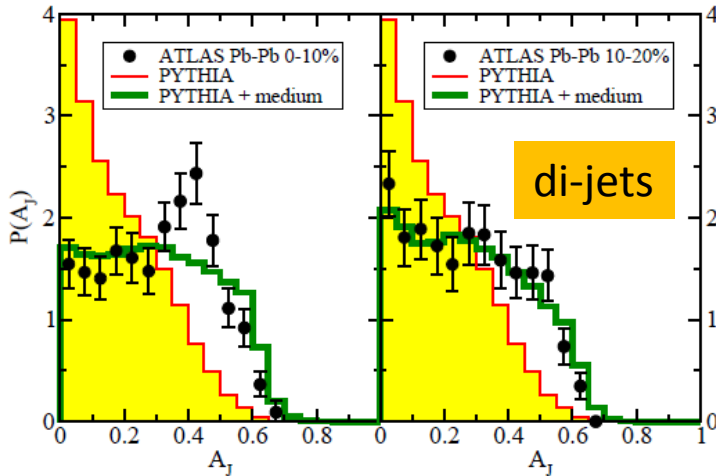
$$R = \sqrt{(\phi - \phi_J)^2 + (\eta - \eta_J)^2}$$



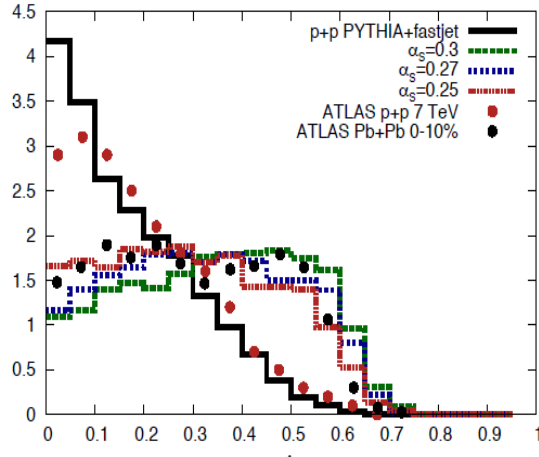
- **Strong modification of dijet E imbalance distribution**
- **Angular distribution is largely unchanged**
- **Implying significant E loss for subleading jets**

$$A_J = \frac{p_{T,1} - p_{T,2}}{p_{T,1} + p_{T,2}} \quad 16$$

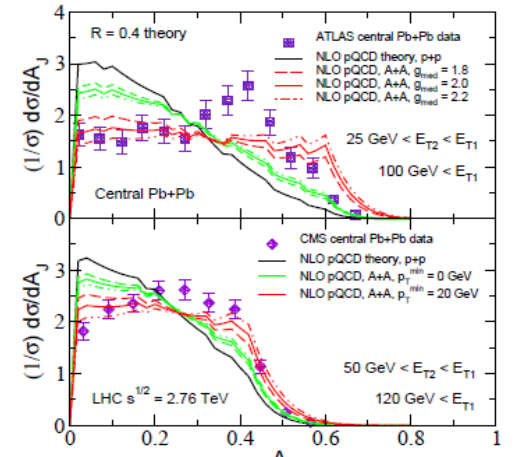
Energy imbalance of di-jets and γ -jets



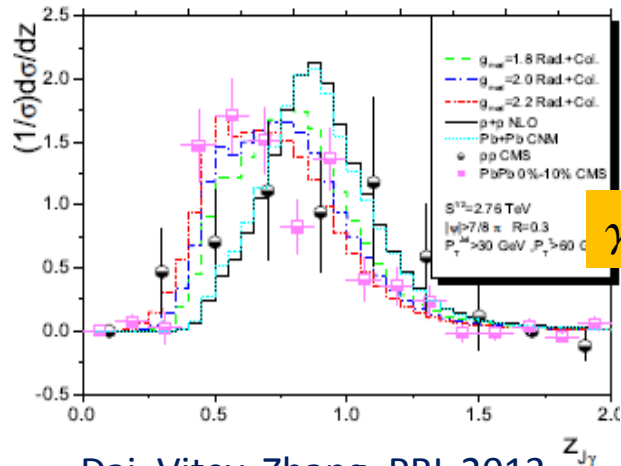
GYQ, Muller, PRL, 2011



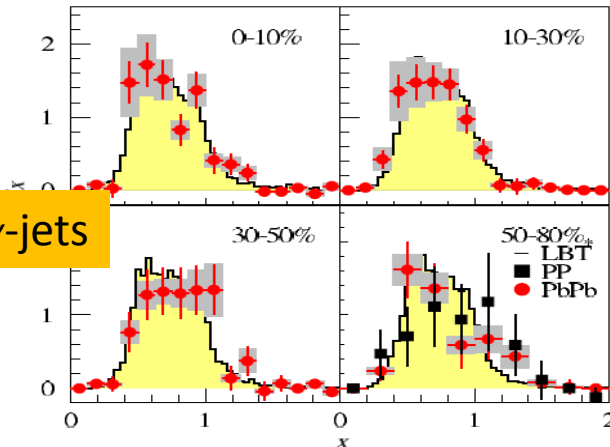
Young, Schenke, Jeon, Gale, PRC, 2011



He, Vitev, Zhang, 2011



Dai, Vitev, Zhang, PRL 2013

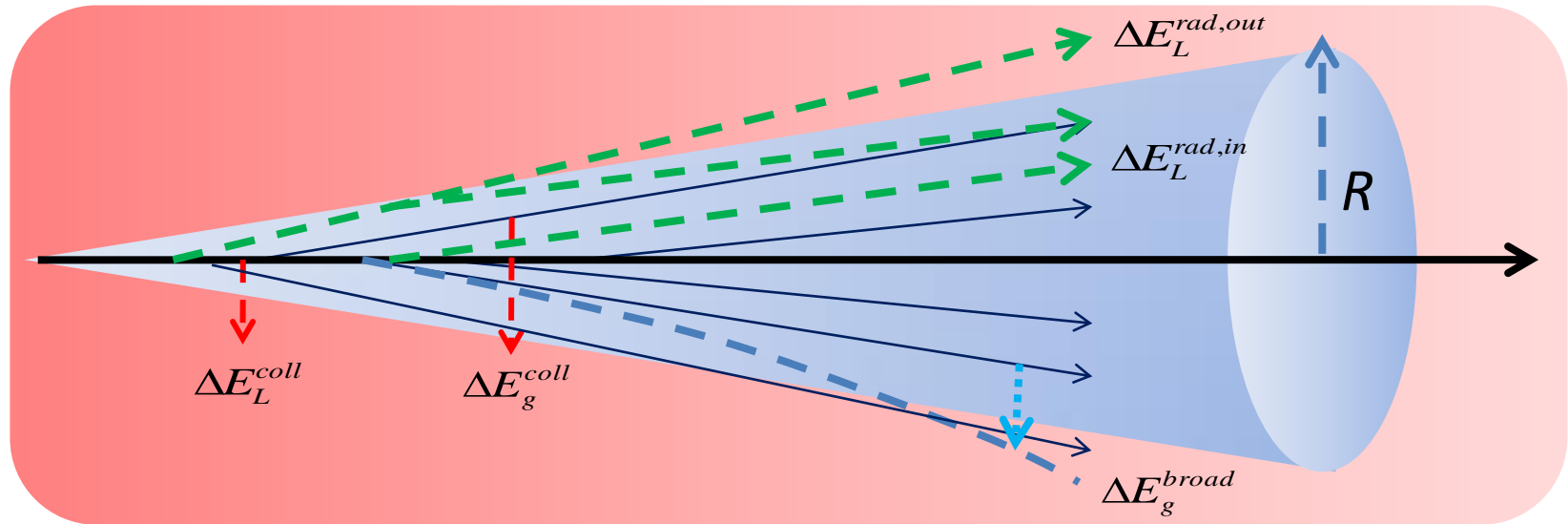


Wang, Zhu, PRL 2013

$$A_J = \frac{p_{T,1} - p_{T,2}}{p_{T,1} + p_{T,2}}, \quad Z_{J\gamma} = \frac{p_{T,\gamma}}{p_{T,J}}$$

The shift of the distribution can be well explained by energy loss based models

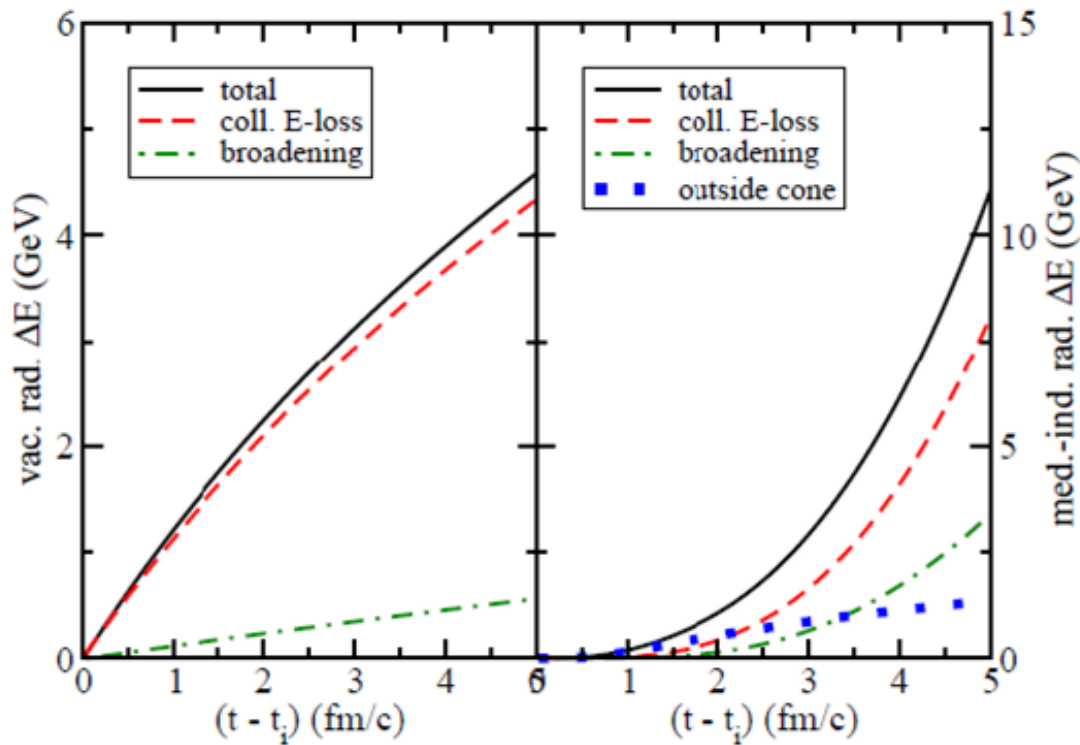
Jet shower evolution in medium



$$\frac{df_g(\omega, k_{\perp}^2, t)}{dt} = \hat{e} \frac{\partial f_g}{\partial \omega} + \frac{1}{4} \hat{q} \nabla_{k_{\perp}}^2 f_g + \frac{dN_g^{med}}{d\omega dk_{\perp}^2 dt}$$

$$\begin{aligned} E_{\text{tot}} &= E_{\text{in}} + E_{\text{lost}} \\ &= E_{\text{in}} + E_{\text{out}}(\text{radiation}) + E_{\text{out}}(\text{broadening}) + E_{\text{th}}(\text{collision}) \end{aligned}$$

Full jet energy loss



Collisional energy loss of radiated partons or medium absorption of soft radiations gives large contribution

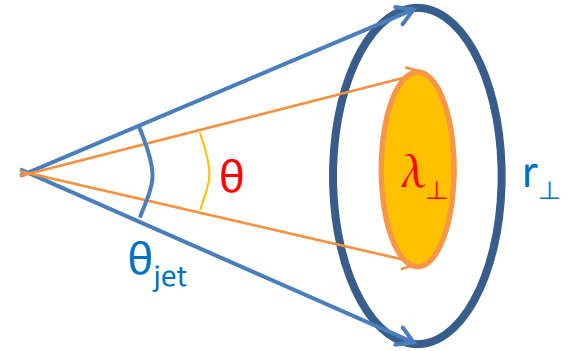
Jet collimation mechanism: soft partons are stripped off by the medium (Casalderrey-Solana, Milhano, Wiedemann, JPG 2011)

Similar findings (Blaizot, Iancu, Mehtar-Tani, PRL 2013; Tywoniuk, Mehtar-Tani, arXiv: 1401.8293)

$$\begin{aligned}
 E_{\text{tot}} &= E_{\text{in}} + E_{\text{lost}} \\
 &= E_{\text{in}} + E_{\text{out}}(\text{radiation}) + E_{\text{out}}(\text{broadening}) + E_{\text{th}}(\text{collision})
 \end{aligned}$$

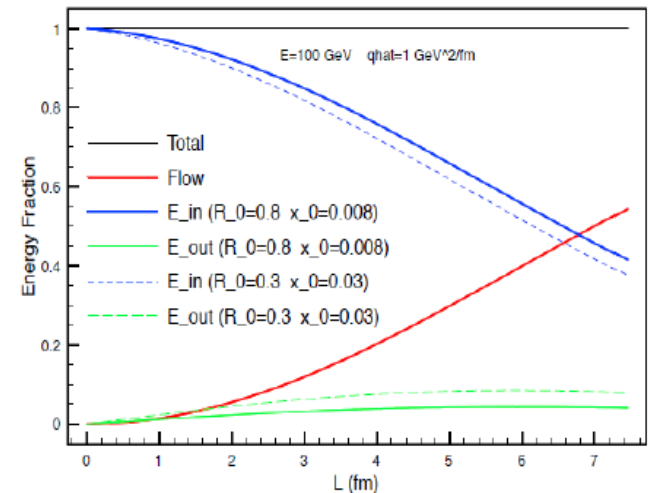
Energy flows to soft gluons

- **If medium color field varies over jet transverse size r_{\perp} , then jet color coherence will be rapidly lost via re-scattering, opening up the phase space for soft (large angle) emissions** (Armesto, Ma, Mehtar-Tani, Salgado, Tywoniuk, Iancu, Casalderrey-Solana, Blaizot, Dominguez, 2011, 2012)
- **Use probability description & solve rate equation to study multiple gluon emissions** (Blaizot, Iancu, Mehtar-Tani, PRL 2013; Tywoniuk, Mehtar-Tani, arXiv: 1401.8293)
- **Jet energy is rapidly degraded into many soft gluons carrying $O(T)$ energy**
- **Three different phase spaces for radiated gluons, separated by two scales x_0 & x_{th}**
- **Color decoherence manifests in the final state as the excess of soft particles**



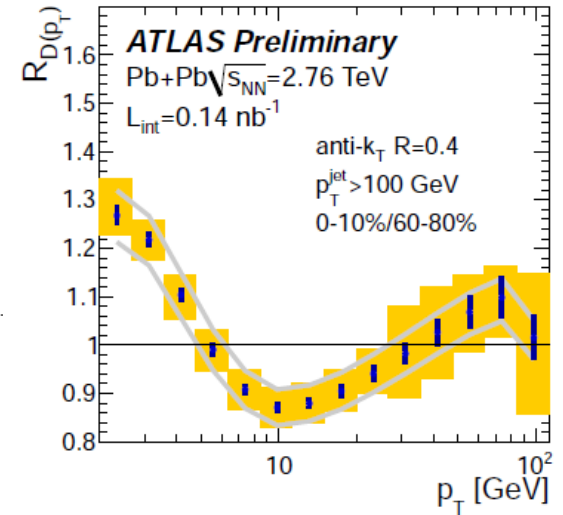
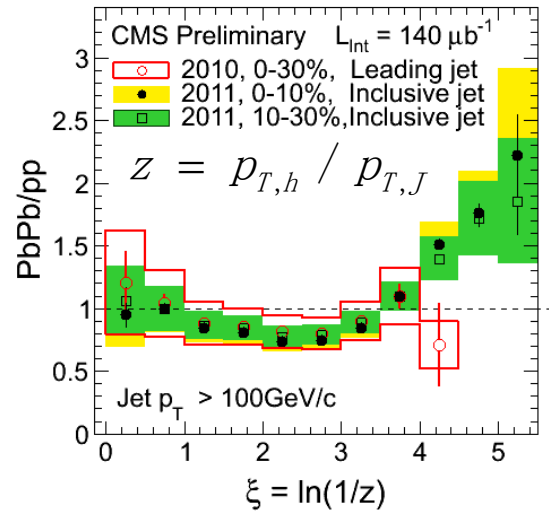
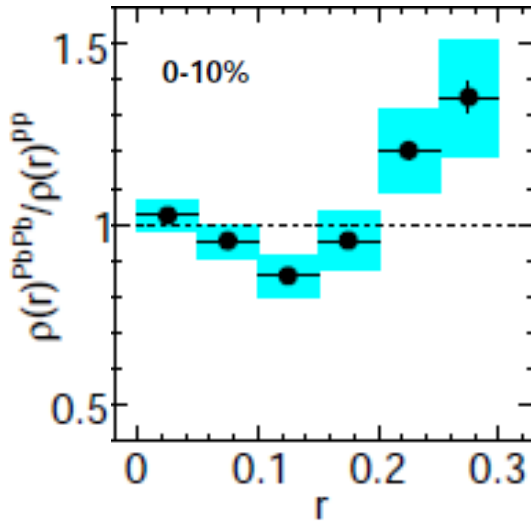
$$r_{\perp} = \theta_{jet} L$$

$$\lambda_{\perp} = 1 / k_{\perp} = 1 / (\theta \omega) = \sqrt{\hat{q} L}$$



$$E_{tot} = E_{in}(x > x_0) + E_{out}(x_{th} < x < x_0) + E_{flow}(x < x_{th})$$

Full jet substructure



Medium modification of jet fragment profiles

- **Little change** @ small r
- **Depletion** @ intermediate r, z, p_T
- **Excess** @ large r ; low & high z, p_T

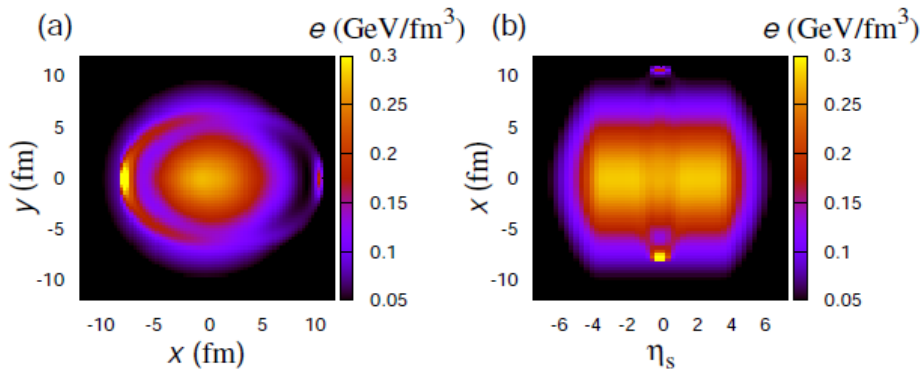
Many details affect jet substructure

- **Recoiled partons & medium response** (Wang, Zhu, PRL 2013)
- **Different hadronization mechanisms: fragmentation and coalescence** (Ma, PRC 2013)
- **Sophisticated experimental jet finding conditions (biased jets?) are needed to compare theory and data** (Ramos, Renk, arXiv:1401.5283)

Medium response to lost energy

Where does the lost energy go?

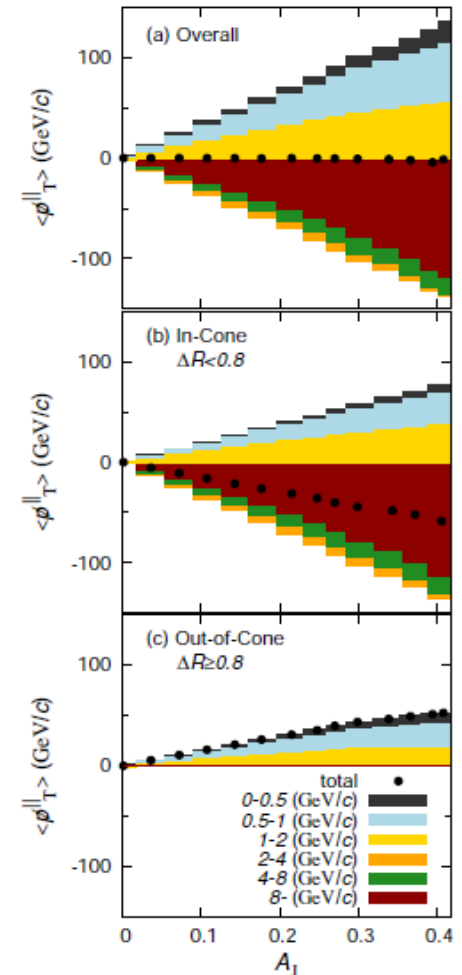
- Hard partons lose energy in medium; some of lost energy is deposited into medium and makes medium excitations



Tachibana, Hirano, arXiv:1402.6469

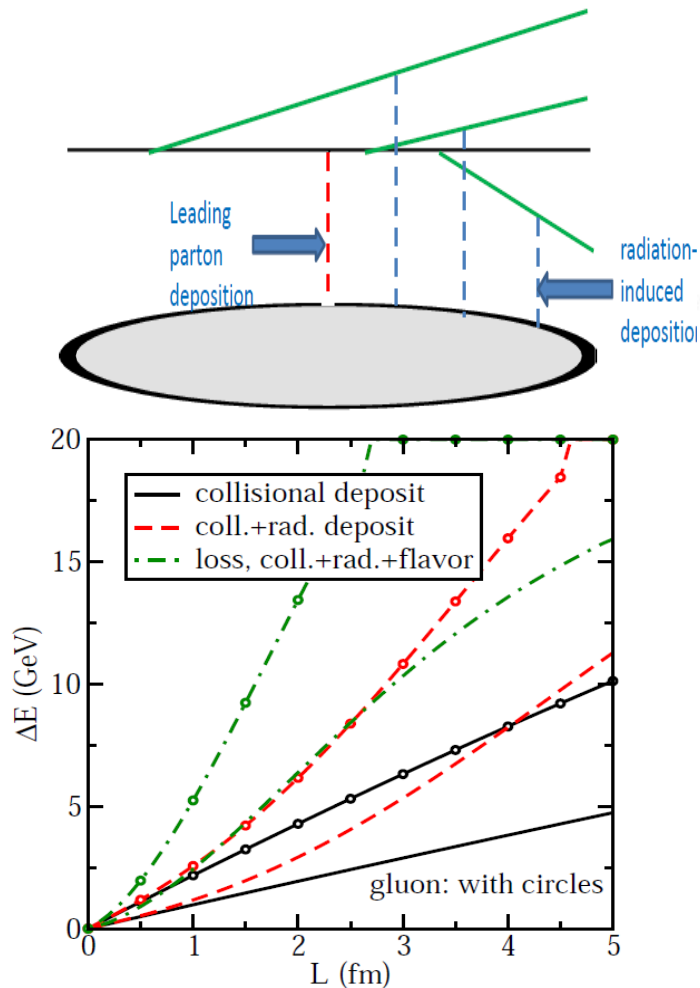
See Yasuki Tachibana's talk

- Simulate medium response to back-to-back 2 parton propagation using (3+1)-D ideal hydrodynamics
- The redistribution of deposited energy through hydrodynamic evolution consistent with CMS result, i.e., the lost energy is carried by soft particles at large angles

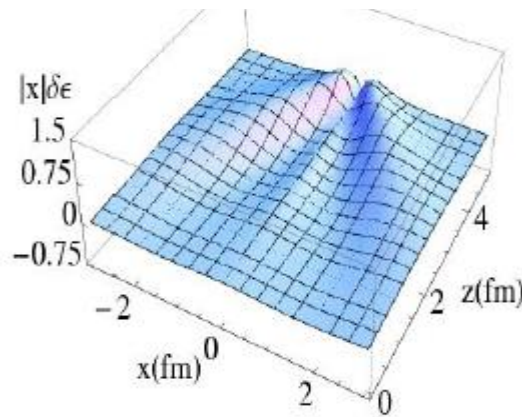


Full jet energy deposition & medium response

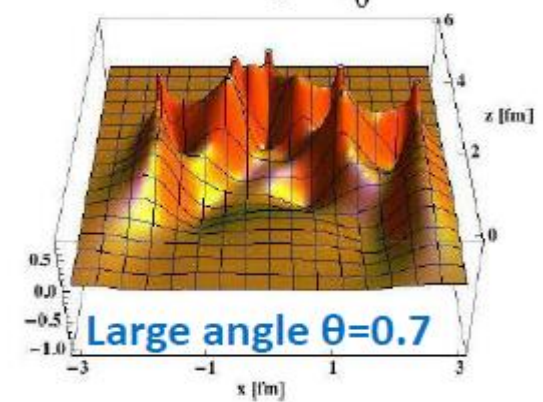
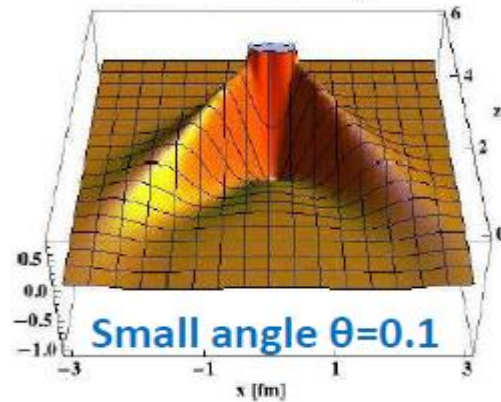
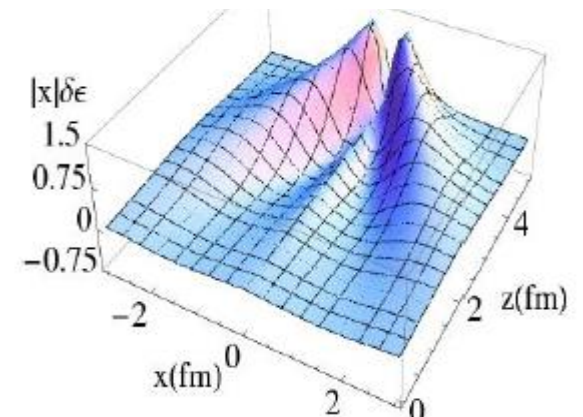
Energy deposition & medium response for jet showers are different from single partons



Single parton



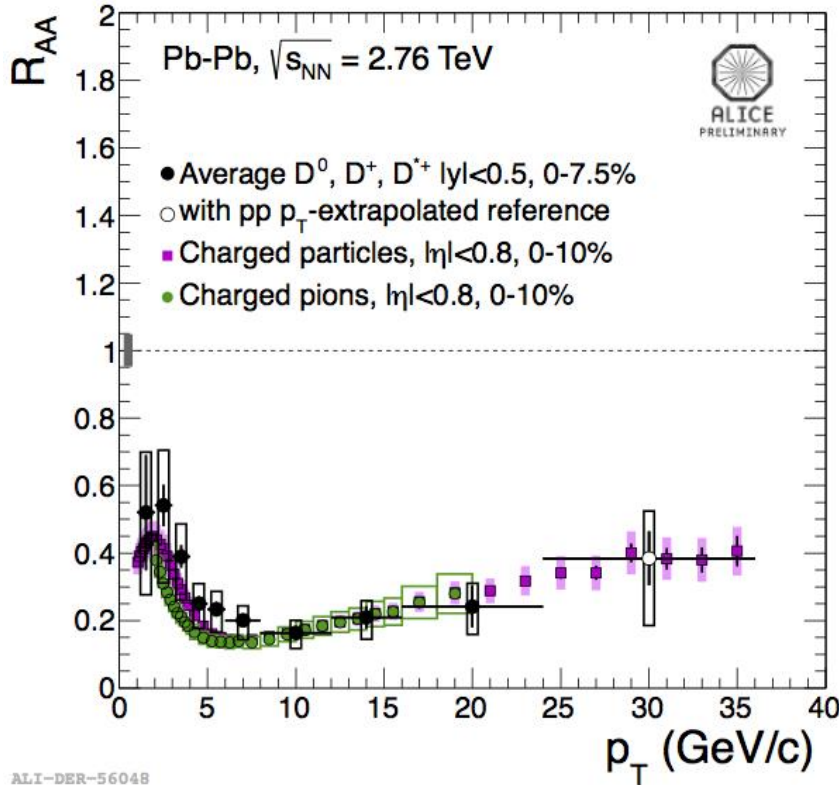
Parton shower



GYQ, Majumder, Song, Heinz, PRL 2009; Neufeld, Muller, PRL 2009 ; Neufeld, Vitev, PRC 2012

Jet + hydro, see Sangwook Ryu's talk, August 6

Heavy flavors

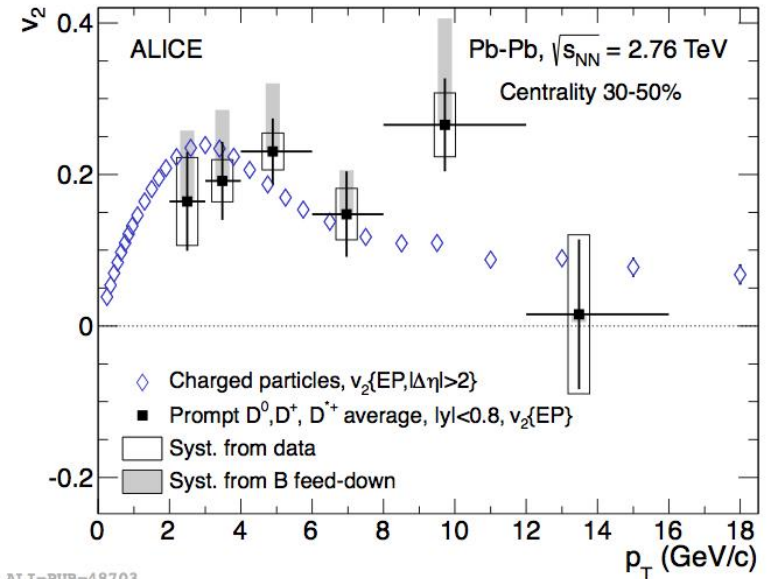


ALI-DER-56048

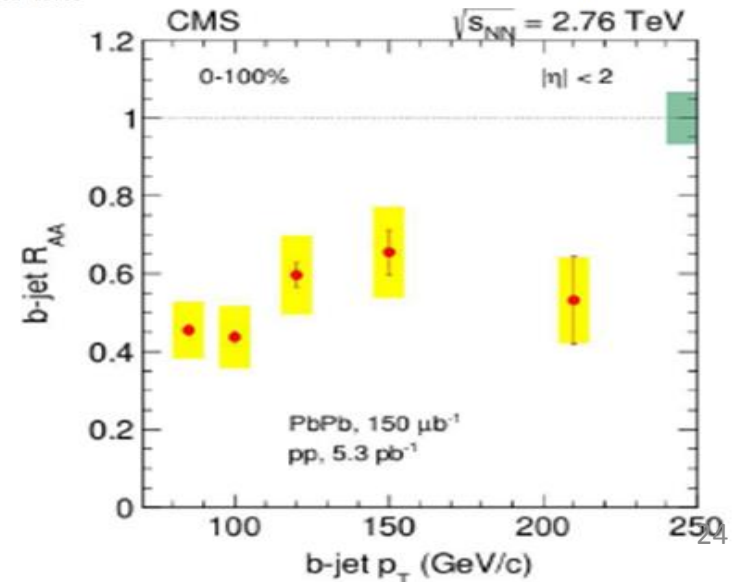
Heavy quarks are expected to lose less energy in QGP due to finite masses

Strong suppression and flow anisotropy have been observed for heavy flavor mesons and tagged jets!

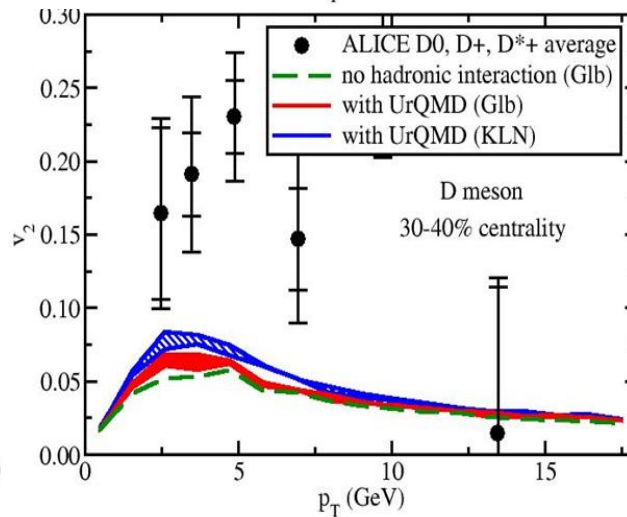
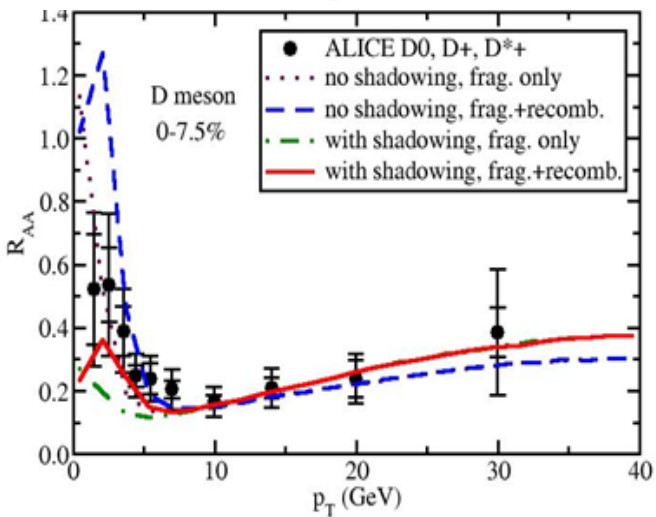
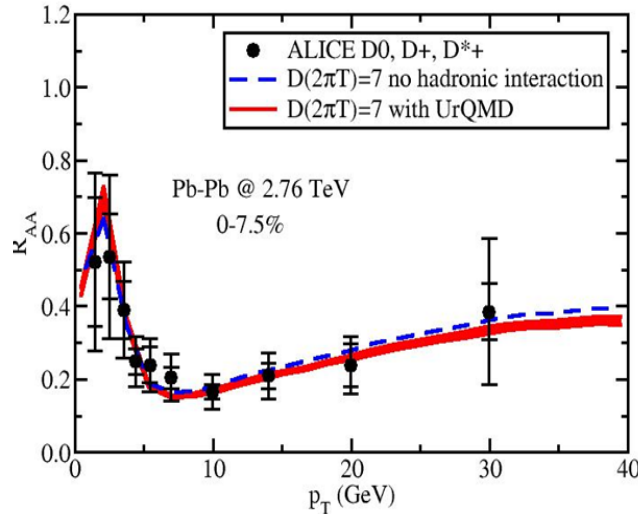
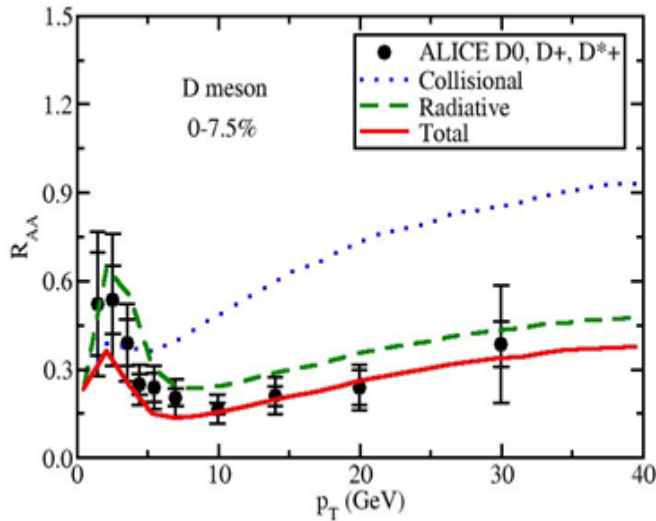
“heavy flavor” sec. August, 6



ALI-PUB-48703



Heavy flavors



**Collisional energy loss
dominate low p_T ,
radiative energy loss
dominates high p_T**

**Recombination gives
sizable contribution at
intermediate p_T**

**Rescatterings of D
mesons in hadron gas
increases a little bit
quenching at high p_T
and enhancement at
low p_T**

**Large v_2 difficult for
the model**

Summary

- **Systematic studies of jet quenching at RHIC and the LHC**
 - Discrepancy of q^{hat} from JET Collaboration and Lattice needs further investigation
 - Map out the temperature dependence of q^{hat}
- **Progress in NLO jet broadening (q^{hat} renormalization)**
 - Full NLO energy loss calculation to be developed
- **Full jet energy loss**
 - Soft components of jets easily lost due to jet-medium interaction
 - Need more detailed study of full jet substructure
- **Progress in studying medium response to lost energy**
 - Thermalization of lost energy not fully understood
 - Need simulate jet transport/evolution and medium response simultaneously
- **Heavy flavors**
 - radiative & collisional, fragmentation & recombination, partonic + hadronic interactions
 - Large v_2