

# $t$ -channel Single-top with complex-mass scheme matched to parton showers



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\*Work in progress with:

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Thanks to Rikkert Frederix and Pierre Artoisenet for discussions and help

## Purpose of this study

Progress in **pQCD** and **automation** have lead an improvement of the description of top quark final states

- in narrow-width approximation (NWA) [Bernreuther,Brandenberg,Si,Uwer,Campbell, Ellis,Tramontano,Melnikov,Schulze,Biswas,Scharf,...] ,
- and when top treated as offshell [Denner,Dittmaier,Kallweit,Pozzorini,Bevilacqua,Czakon,van Hameren,Papadopoulos,Worek,Falgari,Mellor,Signer,Gianuzzi,AP,Frerix, Frixione,Hirschi,Maltoni,Cascioli, Maierhoefer,Heinrich,Maier,Nisius,Schlenk,Winter,...] → see **J. Winter's** talk

**Next step:** match this improved fixed-order to parton shower (PS).

→ **NWA:** see **P. Nason's** talk

→ less work for the PS to do

→ top decay, finite-width effects all contained in hard event

**Focus/study:** (all in framework of `mg5-aMC@NLO` )

1. matching ***t*-channel single top** complex-mass scheme computation to PS
2. differences with other available approximations

## Complex-mass scheme [Denner et al]

Complex-mass scheme: a renormalization scheme that introduces  $\Gamma_t$  at the level of the Lagrangian:

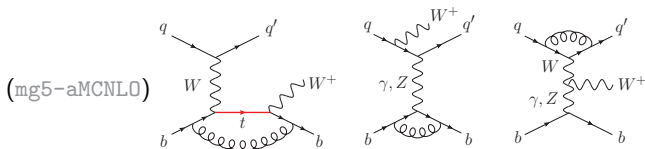
$$m_{t,0} = \mu_t + \delta\mu_t, \quad \text{with} \quad \mu_t^2 = m_t^2 - im_t\Gamma_t$$

$\mu_t$ : complex pole of top quark propagator  $\Rightarrow m_t = m_t^{\text{pole}}$

- ✓ allows for LO and NLO **gauge-invariant** calculations with finite-width effects
- ✓ **automatable** (see GoSam, mg5\_aMC@NLO, OpenLoops)

This gives us **increased perturbative control** of the hard process at fixed-order.

## $t$ -channel Single-top with off-shell & non-resonant effects



[AP, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni '13]

$$p p \rightarrow W^+ J_b J_{\text{light}} + X$$

resonant diagrams,  
non-resonant diagrams  
+ interferences

1.  $t$ -channel process in 5-flavour scheme (**massless  $bs$** )
2. final state **must** contain a tagged  $b$ -jet,  $J_b$ :
  - $J_b$  contains at least a  $b$  quark
  - $J_b$  has non-zero  $p_T$  (here choose  $p_T(J_b) > 25$  GeV)
3. CKM matrix diagonal in 3rd generation

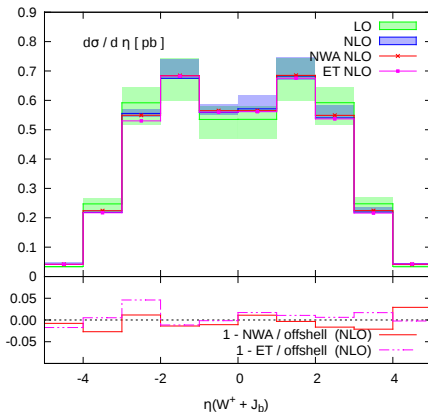
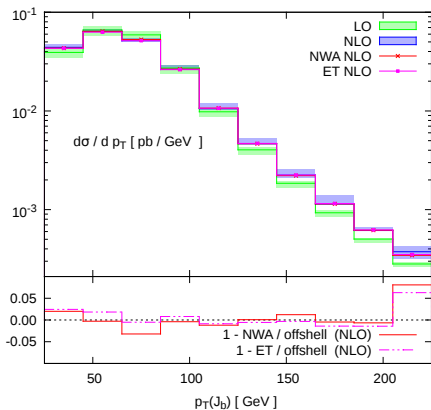
## Fixed order $t$ -channel $W^+ J_b J_{\text{light}}$ : setup

**Note:** chosen analysis cuts **enhance** resonant contributions

⇒ allow for a comparison between various approximations ✓

Compare:

- full **off-shell** result (complex-mass scheme):  $p_t^2 \neq m_t^2$
- **NWA**, as implemented in MCFM:  $p_t^2 = m_t^2$   
[Campbell, Ellis, Tramontano '04, Heim, Cao, Schwienhorst, Yuan, Mueller '09, '11]
- **Effective theory (ET) approach**  $\sim$  pole-expansion:  $p_t^2 \sim m_t^2$   
[Falgari, Mellor, Signer '10]

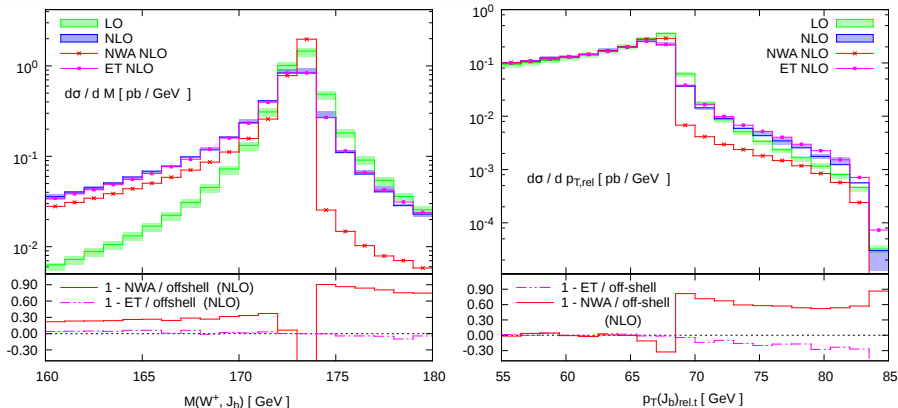
Fixed order  $t$ -channel  $W^+ J_b J_{\text{light}}$  : results1

→ difference between NWA and off-shell approaches **small**  $\sim \mathcal{O}(\Gamma_t/m_t) \sim 1\text{-}2\%$

→ NWA curves lie within scale uncertainty bands of off-shell result ✓

→ no visible differences in shape ✓

## Fixed order $t$ -channel $W^+ J_b J_{\text{light}}$ : results2



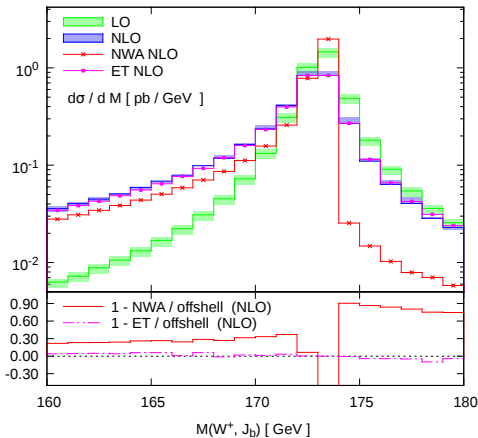
→ difference between NWA and off-shell approaches **sizeable** (expected)

→ finite-width effects **important** for shapes near and beyond peaks

Similar studies/conclusions (single top &  $t\bar{t}$ ): [Falgari et al. '10,'11,'13, Bevilacqua et al. '11, Denner et al. '11,'12, Frederix '13, Cascioli et al. '13, Heinrich et al. '13]

## Fixed order $t$ -channel $W^+ J_b J_{\text{light}}$ : $M(W^+, J_b)$

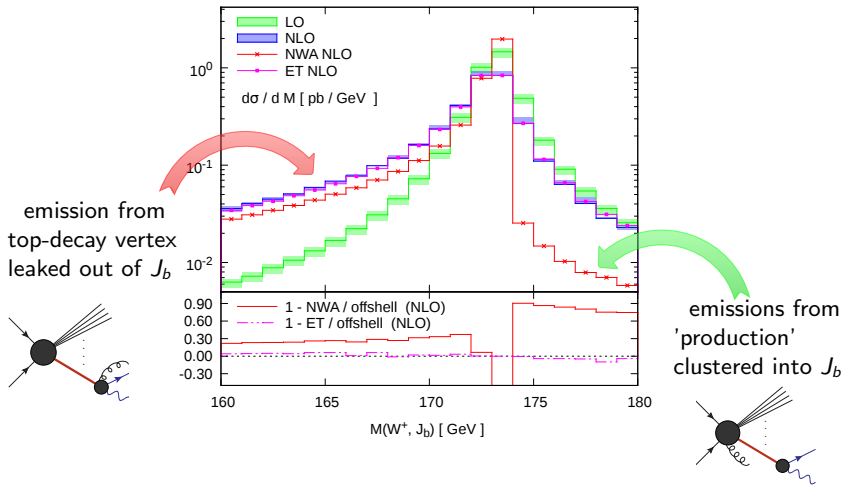
**NWA**, though not designed to describe this, gives us an understanding of the structure behind the offshell distribution (which can be clouded in full offshell result):





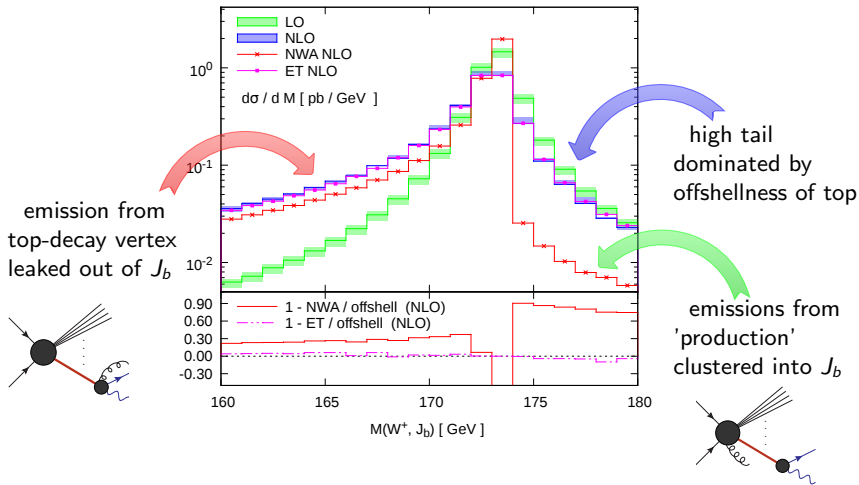
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## Matching to shower: studies

Aim to stay as close as possible to previous parton-level (fixed-order) study, in order to compare to features found there.

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$$p_T(J_b) > 25 \text{ GeV} \quad p_T(J_{\text{light}}) > 25 \text{ GeV}$$
$$140 < M(W^+, J_b) < 200 \text{ GeV}$$

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Study  $W^+ b_j$  matched to PS:

- with two different PSMCs: [Herwig6](#) and [Pythia8](#).
- at hadron level (stable  $B$ -hadrons), but no underlying event
- use MC-truth to ensure fulfillment of key requirement: [b-jet definition](#)
  - locate  $B$ -hadron from outgoing  $b$ -parton from hard process
  - thus [correctly](#) identify  $b$ -jet
  - (multiple  $b$ -jets possible due to  $g \rightarrow b\bar{b}$  splittings in shower phase)

## Matching to shower: onshell tops

Stable top events: easy to deal with

hard process:  $pp \rightarrow t j + X$

- top **always** written into LesHouches event, as a final state particle
  1. hard event showered (with showering off top quark included)
  2. top decay,  $t \rightarrow W^+ b$  attached
  3. further showering off  $b$ -parton, hadronization, etc ...

One wants to understand, since the PS preserves invariant mass of top in event,

- effect of onshell assumption on observables?

**Also easy:** including decay including spin-correlations (MADSPIN) - but also get LO finite-width effects

## Matching to shower: offshell tops, ambiguities, worries

Given that the final state is  $W^+ bj$ , should a 'top' ever be written in the event??

hard process:  $pp \rightarrow W^+ J_b J_{\text{light}} + X$

### NO

- does this even make sense: every event will contain some non-resonant contribution??
- deciding whether or not there is an intermediate top is, formally, a gauge-dependent procedure, based on  $(W^+, b)$ -virtuality

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### YES

- potential to spoil resonance structure/pattern if top **never** written (hard emissions off  $b$ -parton by shower, not captured in  $b$ -jet)
- writing the top in the event results in the parton shower preserving  $M(W^+, b)$  (or  $M(W^+, b, g)$ ), which is something that, at the hard event level is NLO correct (via use of the complex-mass scheme).
- want hadron-level result to reflect the fact that the dominant contributions **are** resonant ones

## Matching to shower: offshell tops: event-structure

Writing top in events done via the procedure:

- define a 'top' momentum:  $p_t^\mu = p_W^\mu + p_b^\mu$  (+ $p_g^\mu$ )
- if:  $\sqrt{p_t^2 - m_t^2} < x_{\text{cut}}\Gamma_t \rightarrow$  write intermediate top in event
- if:  $\sqrt{p_t^2 - m_t^2} > x_{\text{cut}}\Gamma_t \rightarrow$  omit intermediate top from event

$x_{\text{cut}} = 0 \Rightarrow 0\%$  intermediate tops,  $x_{\text{cut}} = \infty \Rightarrow 100\%$  intermediate tops

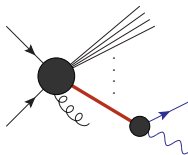
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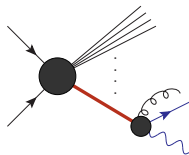
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Care with definition of intermediate top



$$p_t = p_W + p_b$$



$$p_t = p_W + p_b + p_g$$



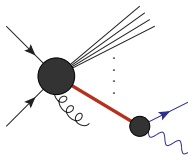
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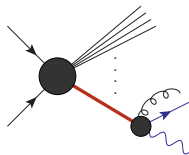
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Care with definition of intermediate top



$$p_t = p_W + p_b$$

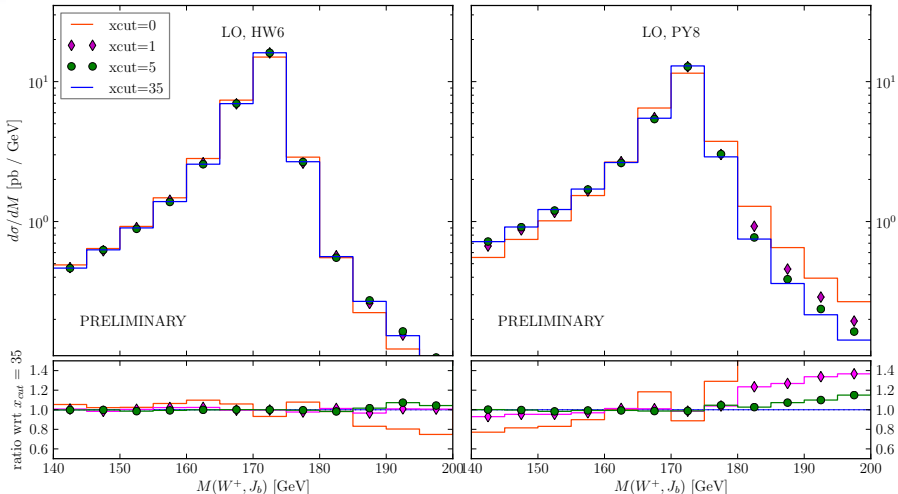


$$p_t = p_W + p_b + p_g$$

✓ done consistently in mg5-aMC@NLO

(for NLO, veto shower emissions off intermediate tops, to prevent double counting)  
(HW6: thanks to B. Webber)

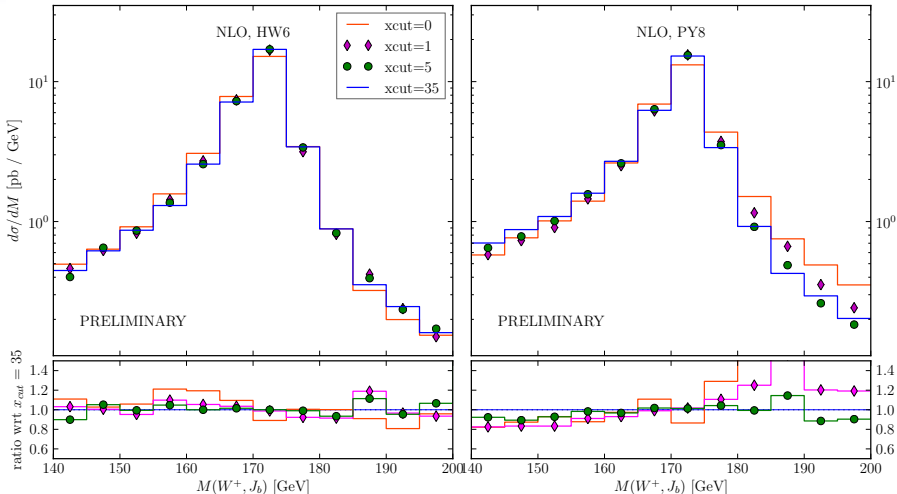
## Variation of top in event: effect on resonance



$x_{\text{cut}} = \{0, 1, 5, 35\} \Rightarrow \{0, 65, 90, 98\}\%$  events contain intermediate tops

→Herwig6: stable, Pythia8: larger effects in high tail

## Variation of top in event: effect on resonance



→ near peak, only  $x_{\text{cut}} = 0$  shows large deviations from  $x_{\text{cut}} = 35$

→ large deviations for Pythia8 in high tail seem to improve

## How well do approximations to full $W^+bj$ fair?

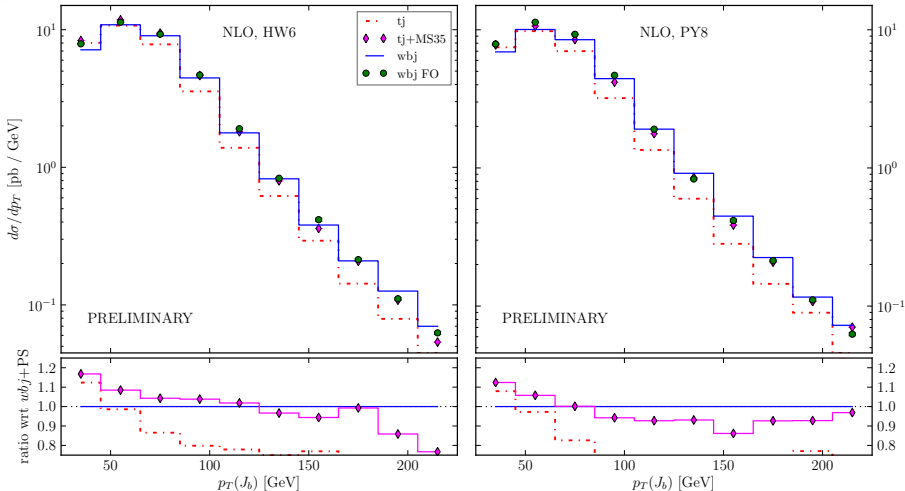
Armed with full  $W^+bj$  + shower: important to compare to various approximations available and that have been used so far ...

- $tj$  + shower
  - NLO single top with onshell, stable top events
  - top decays performed internally by PS
- $tj$  + spin-correlations + shower
  - NLO single top with onshell, stable top events
  - events decayed with MADSPIN\*  
( ✓ production-decay spin-correlations, ✓ LO offshell effects)

\* [MADSPIN: Artoisenet, Frederix, Mattelaer, Rietkerk '12]

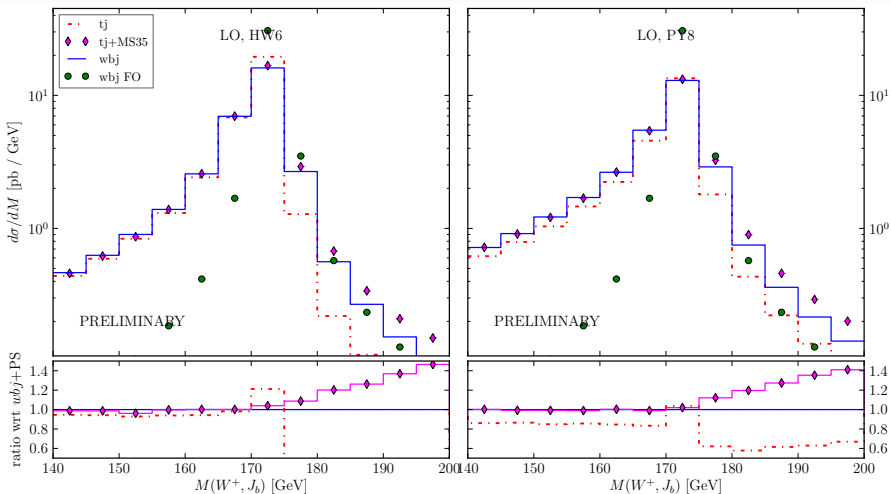
[Frixione, Laenen, Motylinski, Webber '06]

## Comparison of available approximations



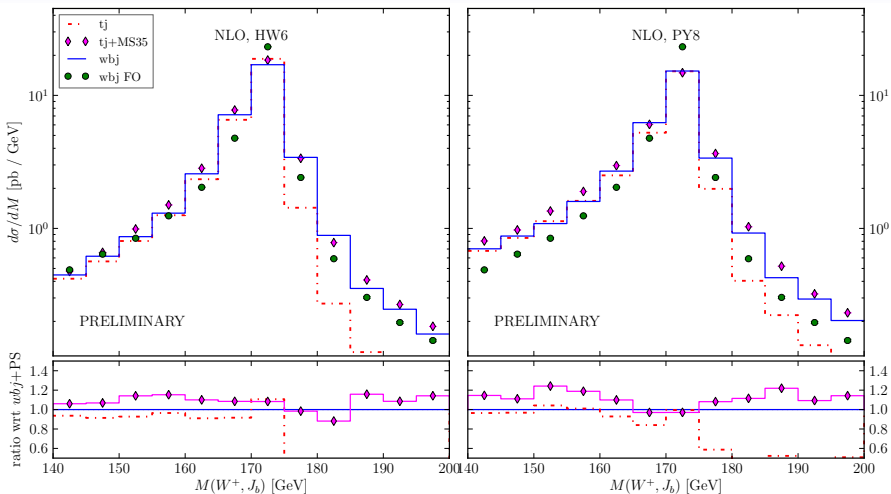
For observables sensitive to top decay, start seeing differences in shape

## Comparison of available approximations



Importance of offshellness for **shape** shows up already at LO, at and beyond peak (note similar pattern to fixed-order  $M(W^+, J_b)$ )

## Comparison of available approximations



→ similar pattern as LO for  $tj$

→ MADSPIN performs better at NLO, improvement of high tail shape

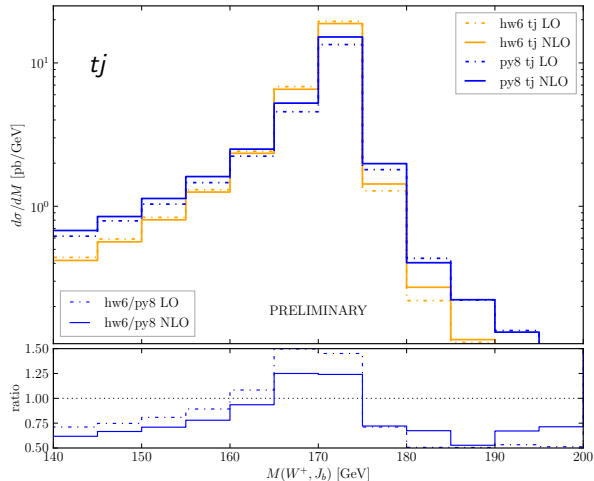
## Comparison of showers: Herwig6 vs Pythia8

Also important to compare PSMCs against each other *directly*.

- highlights intrinsic differences between parton showers, hadronization models
- agreement between showers *should* get better going LO  $\rightarrow$  NLO
- the more information goes into hard event, the closer the results after showering with different MCs *should* get  
(less freedom for PS to add decays, 1st emission from  $b$ -parton,... )  
 $\Rightarrow$  the better the approximation, the better the agreement between showers *should* be

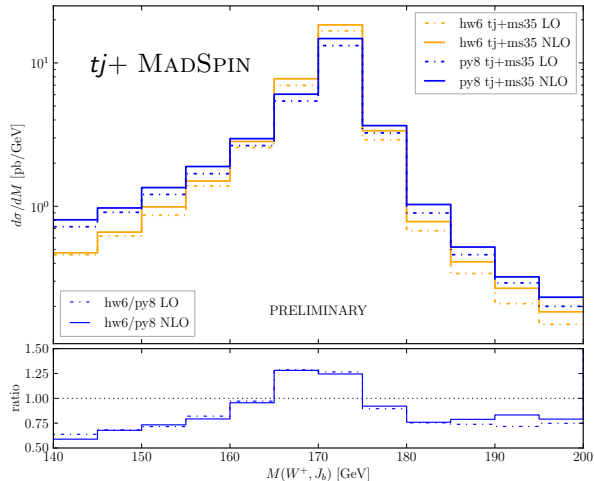


## Herwig6 vs Pythia8



→ distribution almost completely **shaped by shower**  
 (with exception of high tail, where real emission from production contributes)

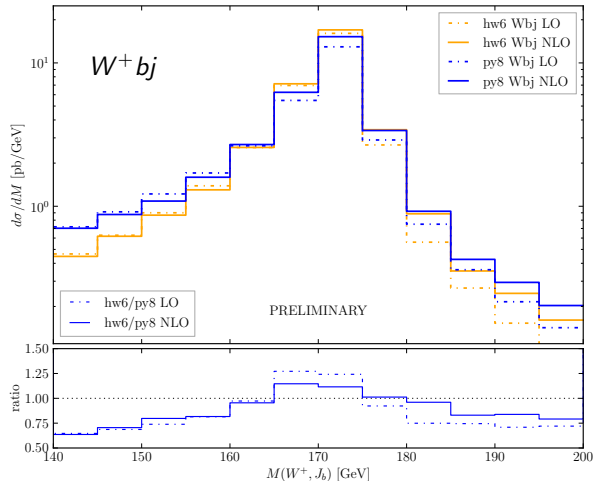
## Herwig6 vs Pythia8



→ addition of LO top decay & LO offshellness improves agreement in high tail wrt  $tj+PS$

→ no real improvement for LO → NLO

## Herwig6 vs Pythia8



→ sizeable differences between showers remain at tails

✓ significant improvement though at resonance and in high tail  
going  $tj \rightarrow tj + \text{MADSPIN} \rightarrow W^+ bj$  and NLO

## Conclusions & Outlook

### Studied:

- $t$ -channel single top, with **full offshell effects** matched to PS
- **ambiguities** involved when matching complex-mass scheme to PS
- how various approximations and showers compare

### Outcomes:

- writing **intermediate top** in event: reasonable, despite procedure being formally gauge-dependent
- shower effects can be large in tails of distributions e.g.  $M(W^+, J_b)$
- $m_t$ -sensitive distributions can show large differences between approximations (expected)

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By no means a closed topic of study. **Comparison to data** would be both extremely interesting and useful for MC development.

→ all this will feed into  $W^+W^-b\bar{b}$  ( $t\bar{t}$ ), main  $m_t$ -measurement process

## Backup slides

## Setup: fixed-order & for matching to PS

Parameter setup:

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$m_t = 173.2 \text{ GeV}$	$\Gamma_t^{\text{nlo}}(\mu = m_t/2) = 1.3569\text{GeV}$
$m_Z = 91.1876 \text{ GeV}$	$m_W = 80.3980 \text{ GeV}$
MSTW2008NLO PDF set	$V_{tb} = 1$

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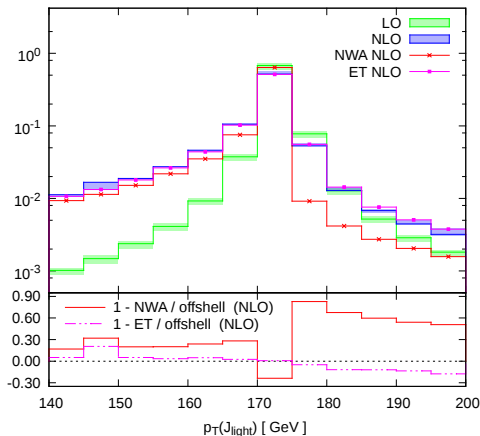
Analysis setup:

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$$\begin{aligned}
 p_T(J_b) > 25 \text{ GeV} & \quad p_T(J_{\text{light}}) > 25 \text{ GeV} \\
 |\eta(J_b)| < 4.5 & \quad |\eta(J_{\text{light}})| < 4.5 \\
 140 < M(W^+, J_b) < 200 \text{ GeV} &
 \end{aligned}$$


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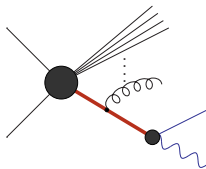
## Fixed-order $M(W^+, J_b)$ , wider range



- ET slowly diverges from full complex-mass scheme result for higher  $M(W^+, J_b)$
- ⇒ indicates resonant/non-resonant interferences & fully non-resonant contributions grow in importance

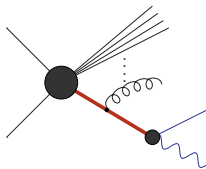


## Radiating off intermediate tops



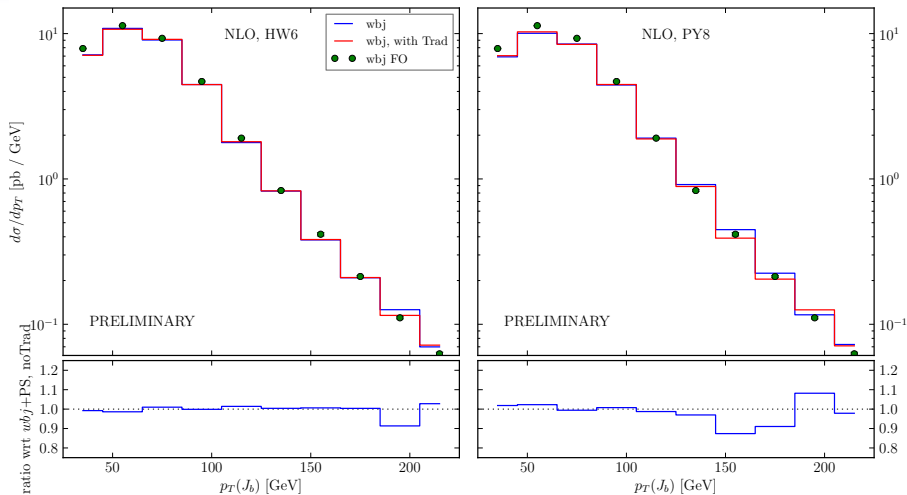
- NLO complex-mass scheme computation contains non-divergent real emissions off intermediate top propagators (potential soft singularity screened by  $\Gamma_t$ )
- **IF** top written in event, danger of double-counting emissions when shower radiates off top!  
(MC subtraction terms only cure divergent real emissions)

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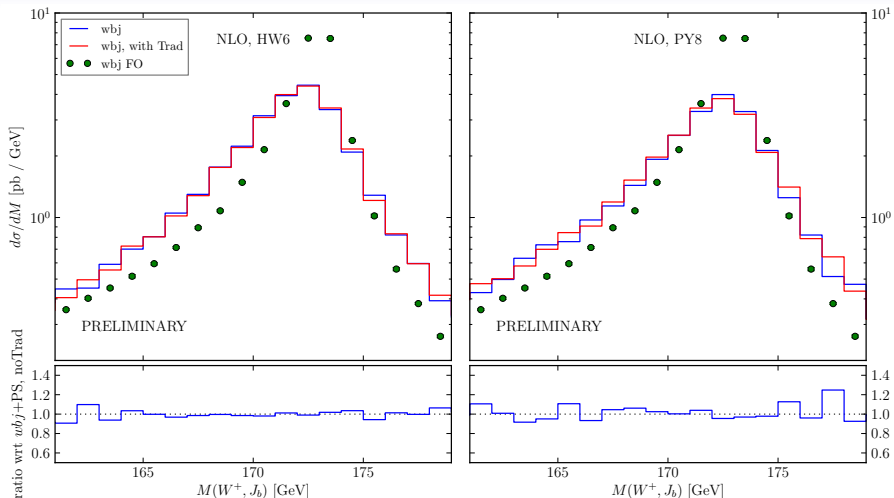
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- **IF** top written in event, danger of double-counting emissions when shower radiates off top!  
(MC subtraction terms only cure divergent real emissions)
- $W^+ b j$  NLO: **forbid** radiation from intermediate tops [HW6: thanks to B. Webber]
- crude - but effect of radiation off intermediate top is generically **small**

## Effect of radiation from top



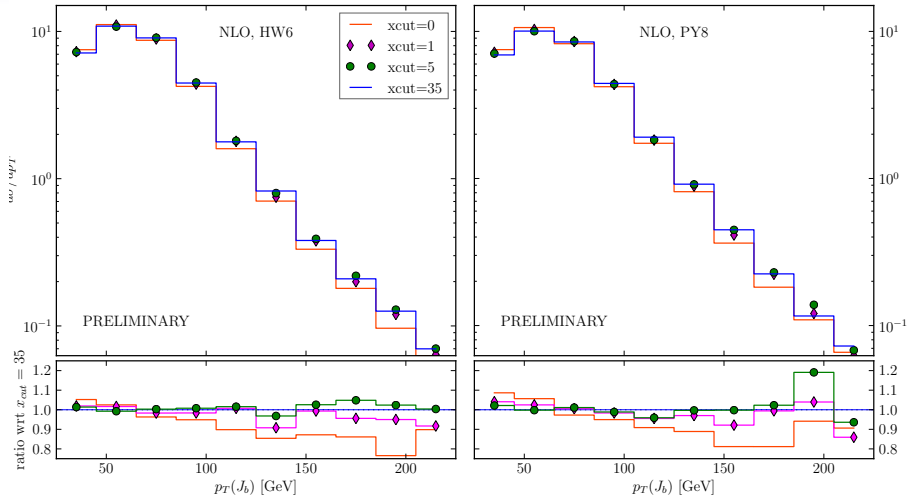
→ no / small effect on  $p_T$  spectrum of  $b$ -jet

## Effect of radiation from top

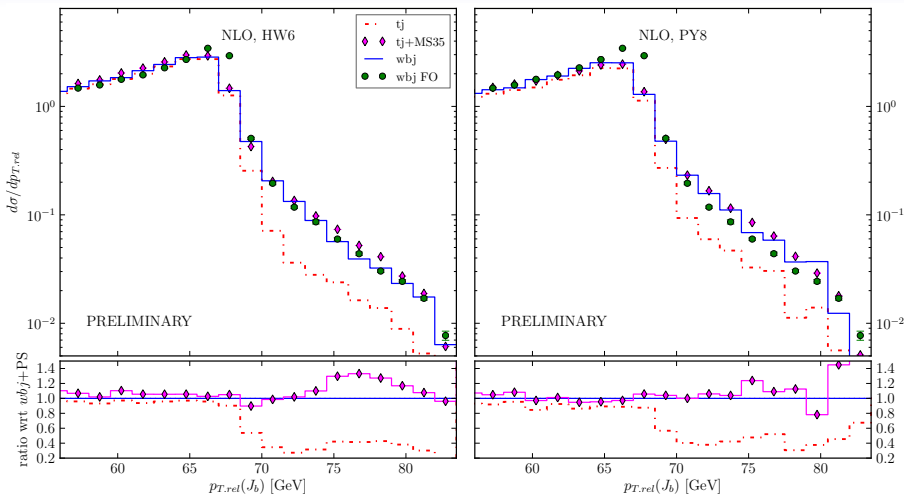


→ e.g. no effect on invariant mass of reconstructed top

# Varying $x_{\text{cut}}: p_T(J_b)$



## Comparing approximations: $p_{T,rel.}(J_b)$



→ large distortions of shape of edge  $tj$

→ expect same for other distributions with sharp edges:  $M(J_b, I^+)$ ,  $M_T(J_b, I^+, \nu_e)$