

# Top mass dependence on kinematic variables and colour reconnection



Pedro Ferreira da Silva (CERN)  
*on behalf of the ATLAS and CMS collaborations*  
TOP LHC WG meeting 21<sup>st</sup>-23<sup>rd</sup> May 2014



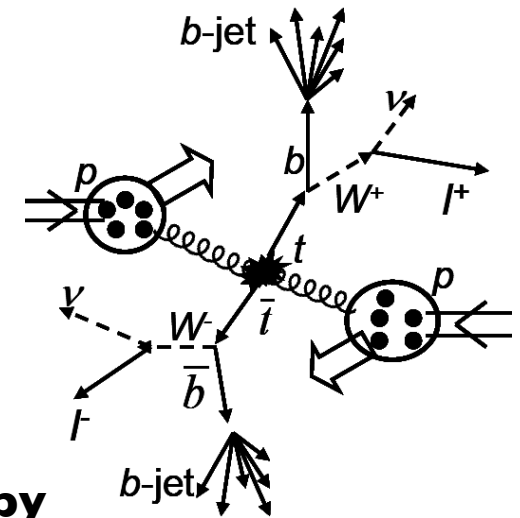


# Introduction

- **Top quark mass from hadron colliders**

- use final state to reconstruct top mass and its kinematics ►
- high precision single measurements and final combination

$\sigma(m_t) < 0.5\% m_t$  (see O. Brandt's talk and [arXiv:1403.4427](https://arxiv.org/abs/1403.4427))



- **Final uncertainty in world combination is dominated by**

## Jet Energy Scale

0.14% $m_t$  - in-situ (scales with  $\int Ldt$ )

0.14% $m_t$  - b JES

0.11% $m_t$  - non-flavour specific JES

## Modelling of the signal

0.22% $m_t$  - MC

0.18% $m_t$  - colour reconnection

0.13% $m_t$  - Initial/Final state radiation

Can improve  
@LHC with

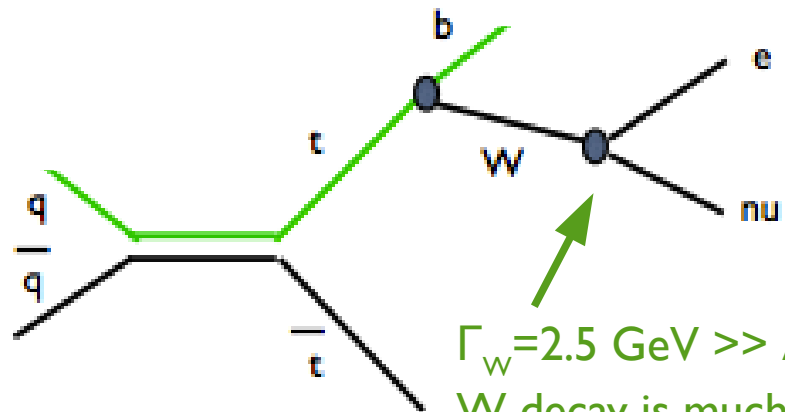
*more data and dedicated analysis,  
e.g. from  $Z/\gamma+b$  studies or 3D fit as  
in ATLAS-CONF-2013-046*

*dedicated measurements in different phase  
space regions of top production+decay*

# Anatomy of a top quark event

adapted from M. Mangano @ TOP2013

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$$\Gamma_W = 2.5 \text{ GeV} \gg \Lambda_{\text{QCD}}$$

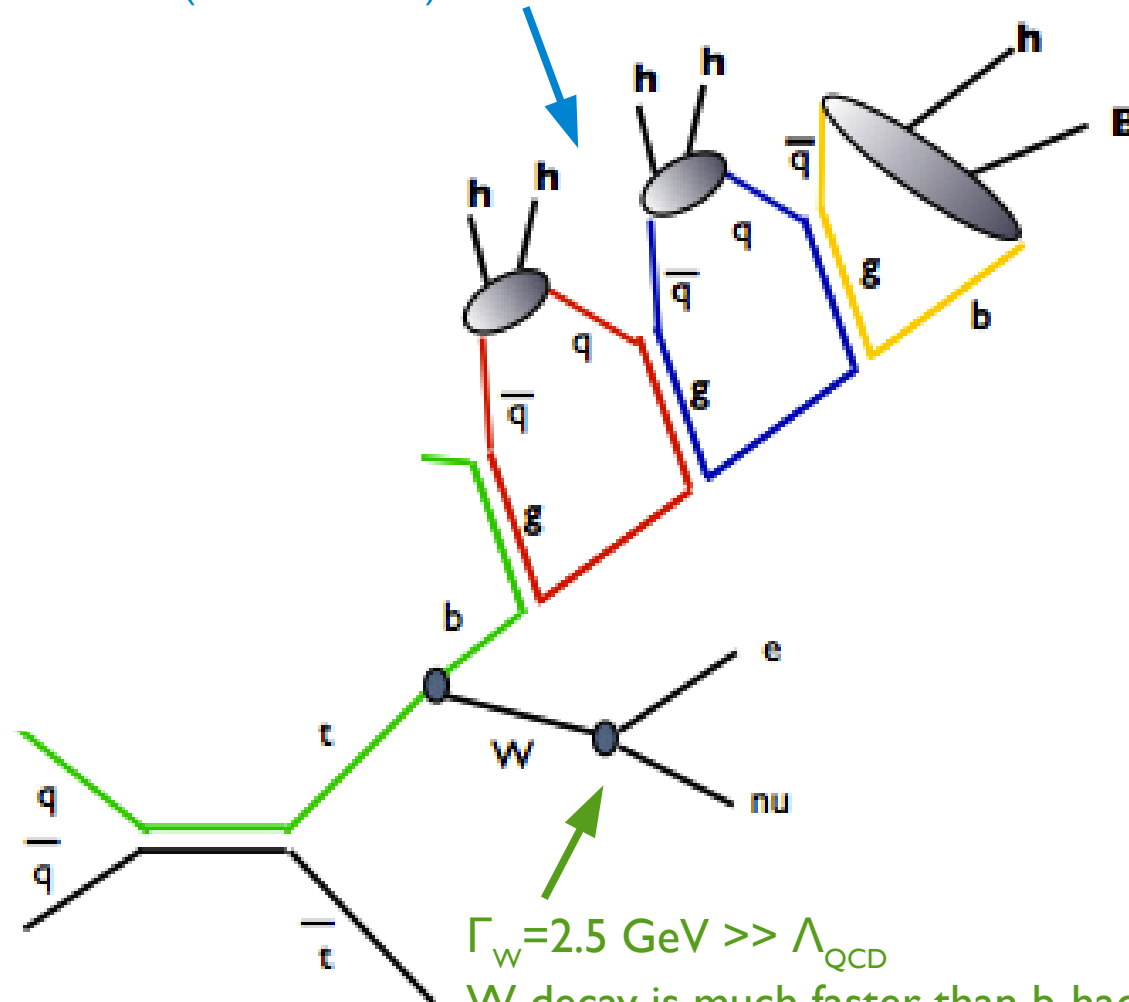
W decay is much faster than b-hadronization time scale → **EWK dynamics “factorize”** in a top event, see S. Nauman-Emme's and A. Mitov's talks

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Controlled by **shower evolution**, residual sensitivity to hadronization model (out-of-cone), see Tancredi's and G. Corcella's talks



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$W$  decay is much faster than  $b$ -hadronization time scale  $\rightarrow$  **EWK dynamics “factorize”** in a top event, see S. Nauman-Emme's and A. Mitov's talks

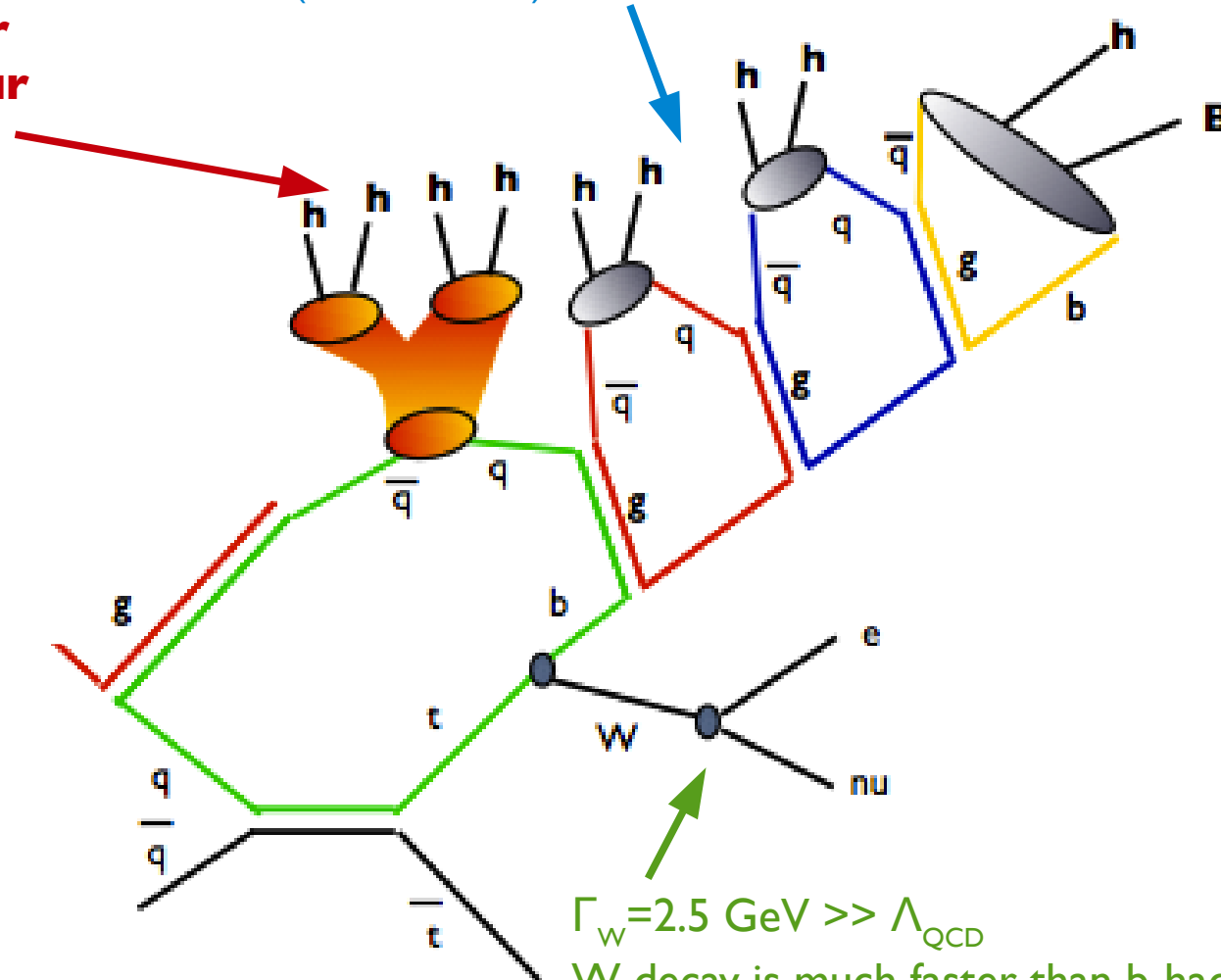
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Controlled by **shower evolution** and **colour reconnection**:  
ambiguous “paternity”

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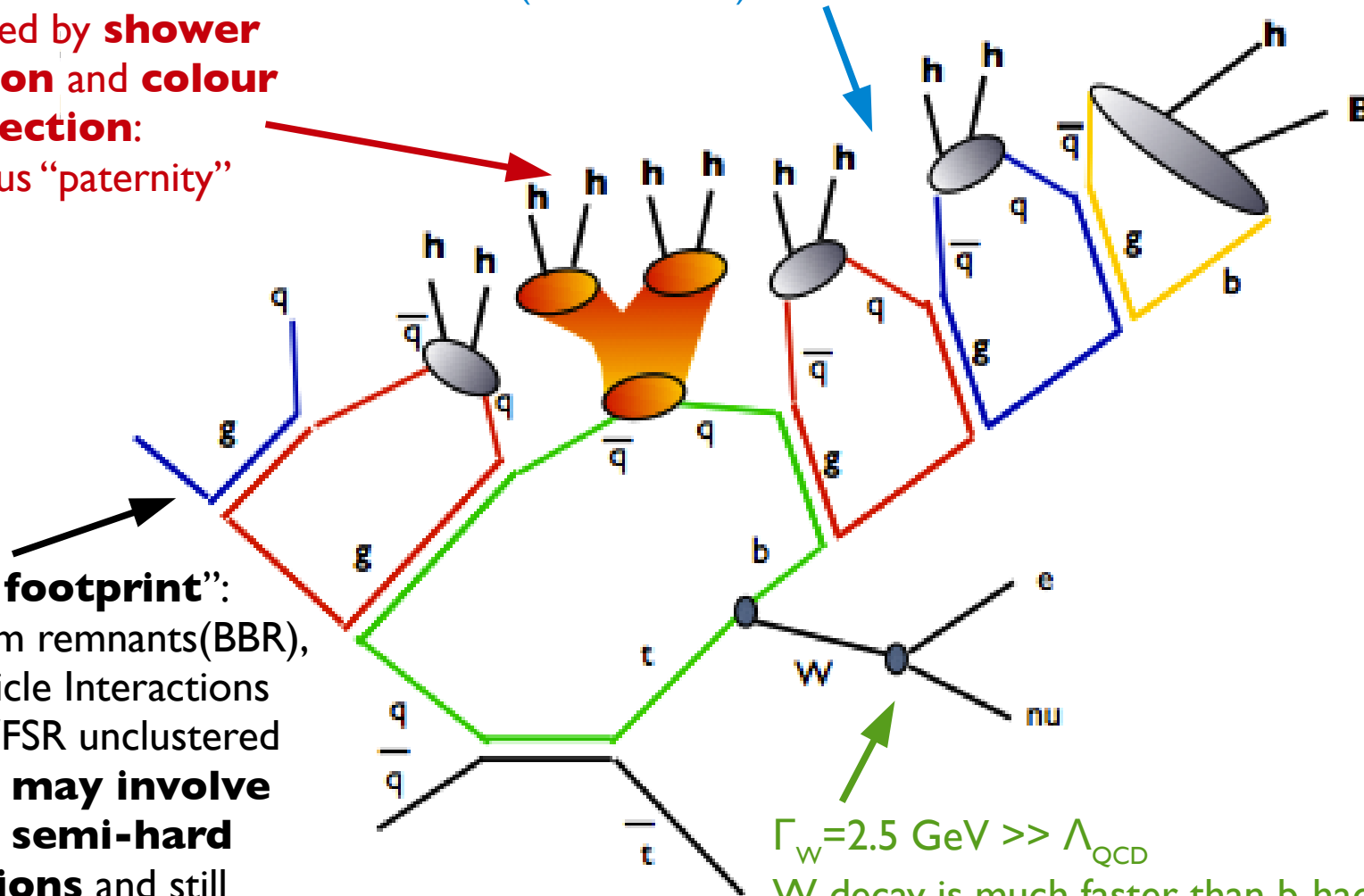
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Controlled by **shower evolution**, residual sensitivity to hadronization model (out-of-cone), see Tancredi's and G. Corcella's talks

Controlled by **shower evolution** and **colour reconnection**: ambiguous “paternity”

“**Proton footprint**”:  
Beam-beam remnants (BBR),  
Multi Particle Interactions (MPI), ISR/FSR unclustered into b-jets **may involve soft and semi-hard interactions** and still connect to the “core” of a top quark event



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# Probing the anatomy of a top quark event

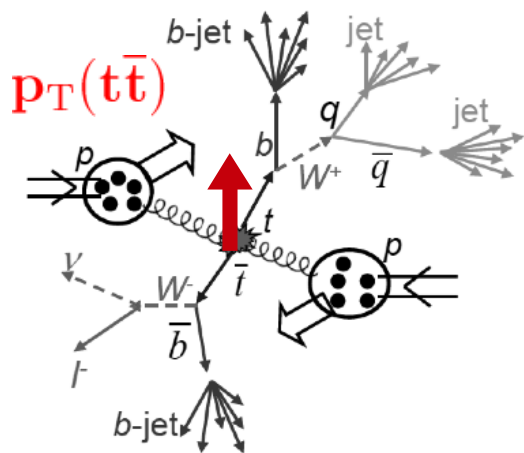
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We present data studies of possible kinematic biases in the measurement of the top-quark mass based on the invariant mass of its decay products. The effects observed are well reproduced by simulations based on MadGraph, Powheg, and MC@NLO with tunes including and excluding the effects of colour reconnection.

# $m_t$ differential measurements

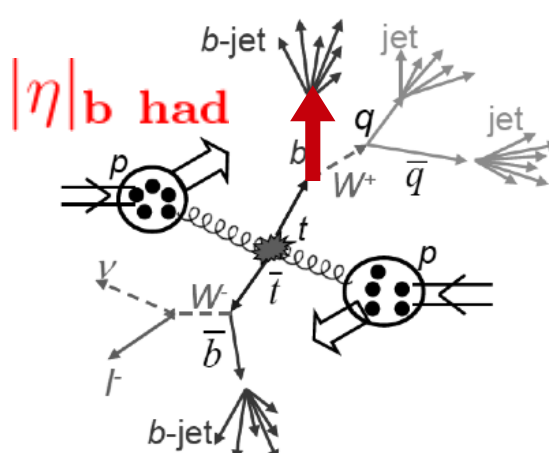
- We rely on MC-based **models of the top production and decay chain**
  - particular models for underlying event (UE), colour reconnection (CR) are taken into account
  - do these tools describe our data in the different phase space regions?
  - can we find sensitivity to different components in top quark  $p_T$ , b-quark rapidity, charge, etc.?
- Choose **representative observables which can potentiate particular effects**

## Radiation effects



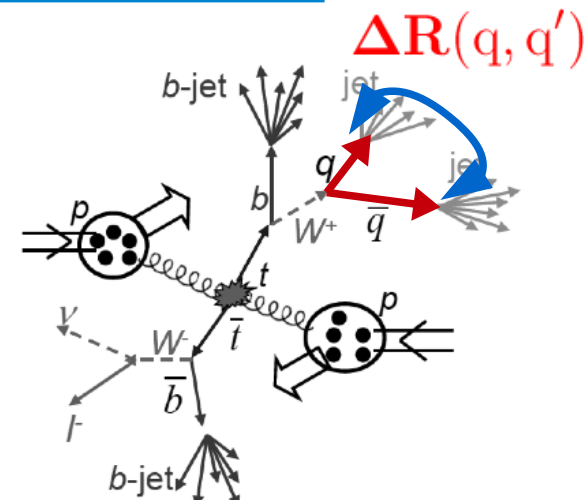
$H_T$   $m_{t\bar{t}}$   $p_{T,t\bar{t}}$   
Jet multiplicity

## b-quark kinematics



$p_{T,b, had}$   $|\eta_{b, had}|$   
 $\Delta R_{b\bar{b}}$   $\Delta\phi_{b\bar{b}}$

## Colour reconnection



$\Delta R_{q\bar{q}}$   $\Delta\phi_{q\bar{q}}$   
 $p_{T,t, had}$   $|\eta_{t, had}|$



# Strategy for differential measurements

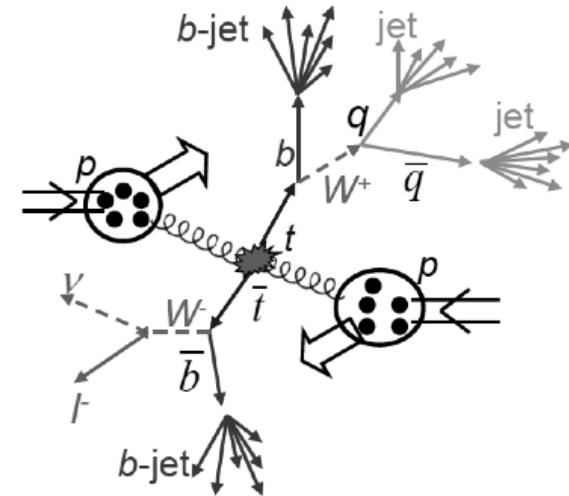
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- **Study performed at 7 and 8 TeV**

- using golden l+jets channel
- JHEP 12 (2012) 105 and CMS-PAS-TOP-14-001

- **Inclusive measurement**

- High purity selection (2 b-tags)
- choose 2 best permutations from kinematic fit
- include resolutions,  $m(\text{top})=m(\text{anti-top})$ ,  $m_W=80.4$  GeV
- apply ideogram method for  $(m_t, \text{JES})$
- event-per-event likelihood using both permutations



Permutations	Before fit	After fit, $P_{\text{gof}} > 0.2$ , and weight
Purity	94	96
Correct	13	44
Wrong	16	21
Un-matched	71	35

$$\mathcal{L}(\text{sample} | m_t, \text{JSF}) = \prod_{\text{events}} \left( \sum_{i=1}^n P_{\text{gof}}(i) \left( \sum_j f_j P_j(m_{t,i}^{\text{fit}} | m_t, \text{JSF}) \times P_j(m_{W,i}^{\text{reco}} | m_t, \text{JSF}) \right) \right)^{w_{\text{event}}}$$

combine all events

weight each permutation by kin. fit probability

probability of correct/wrong/un-matched permutation yielding  $(m_t, \text{JSF})$

pull events which have correct combinatorics

# Strategy for differential measurements

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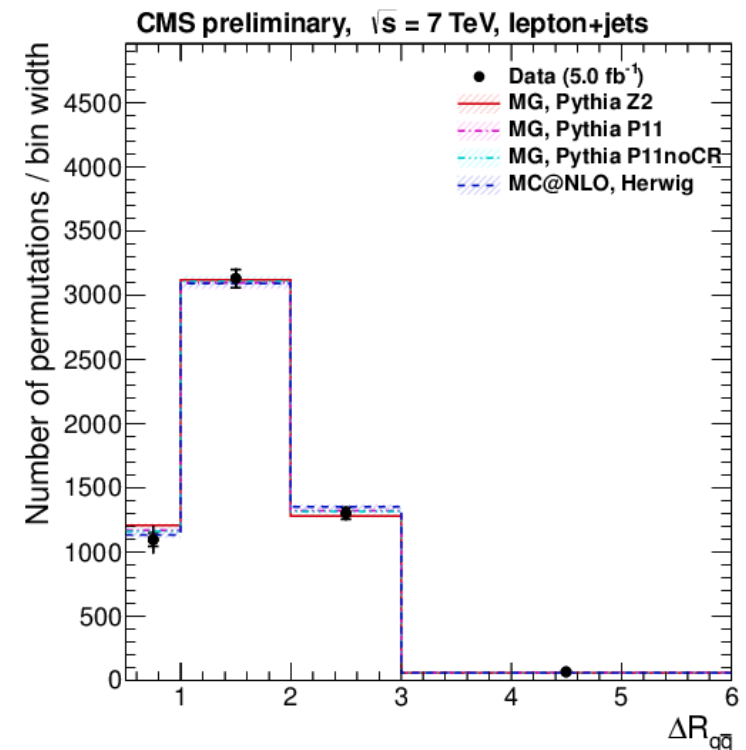
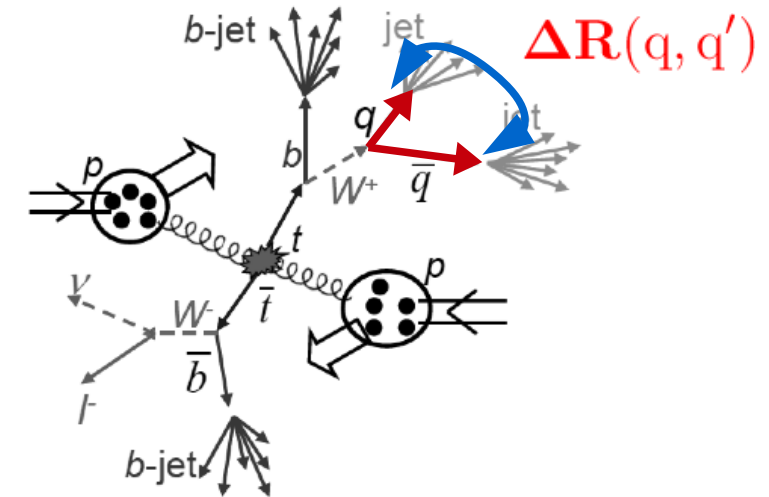
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- **Categorize** permutations according to kinematics



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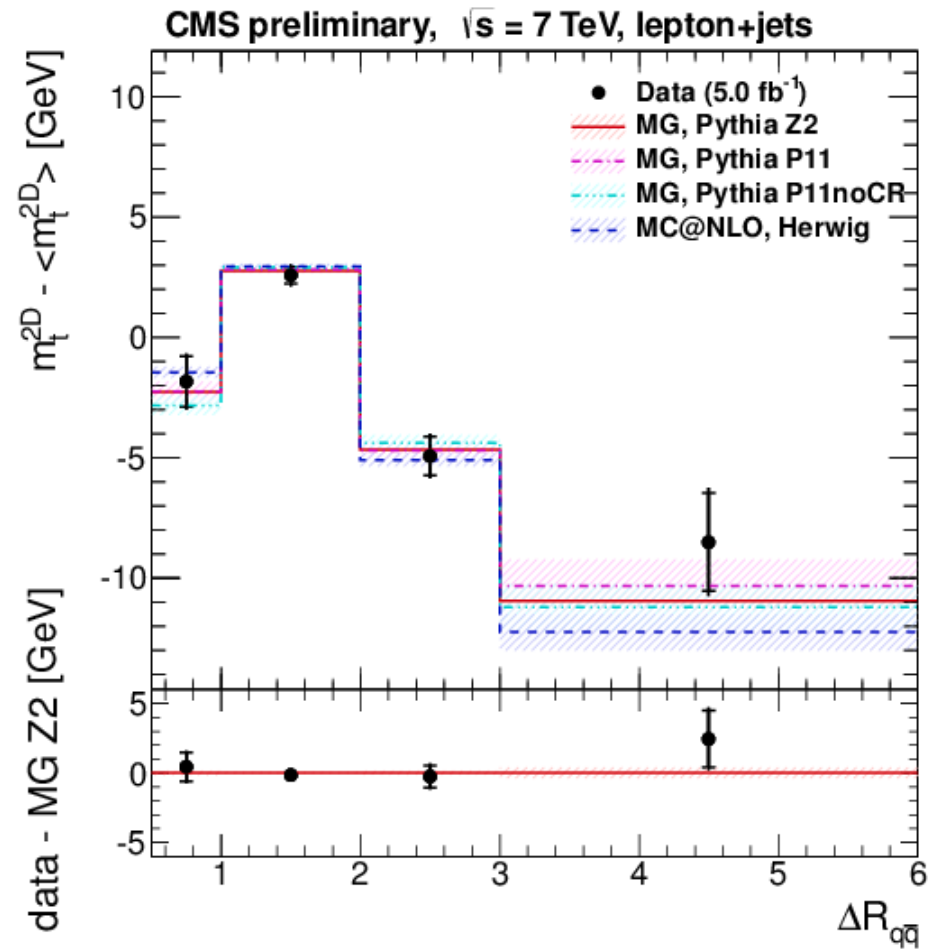
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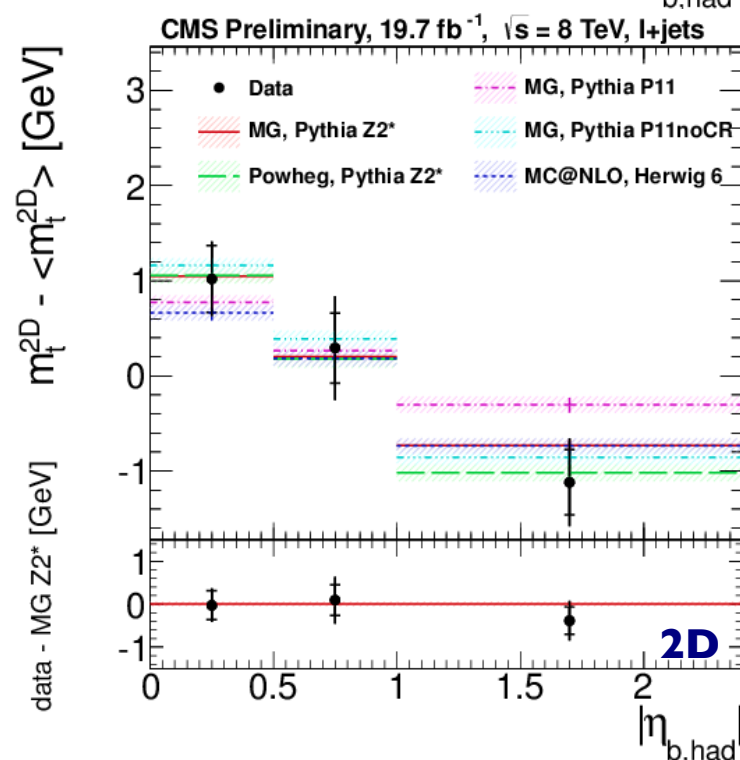
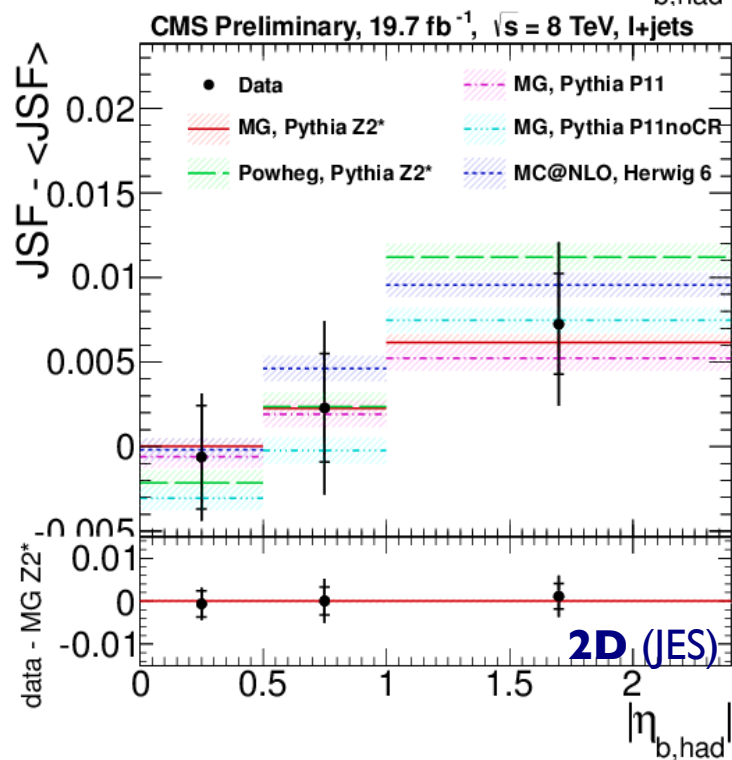
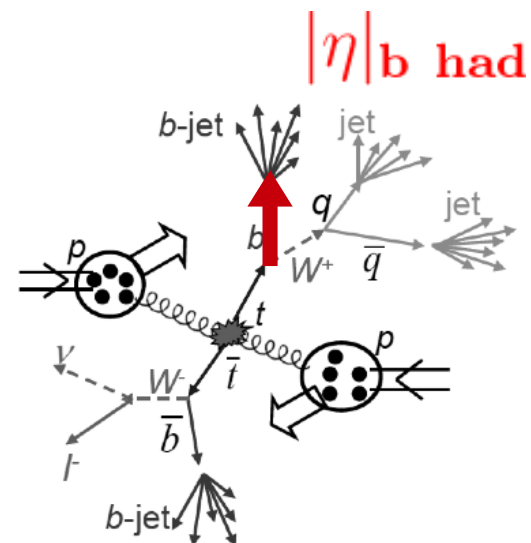
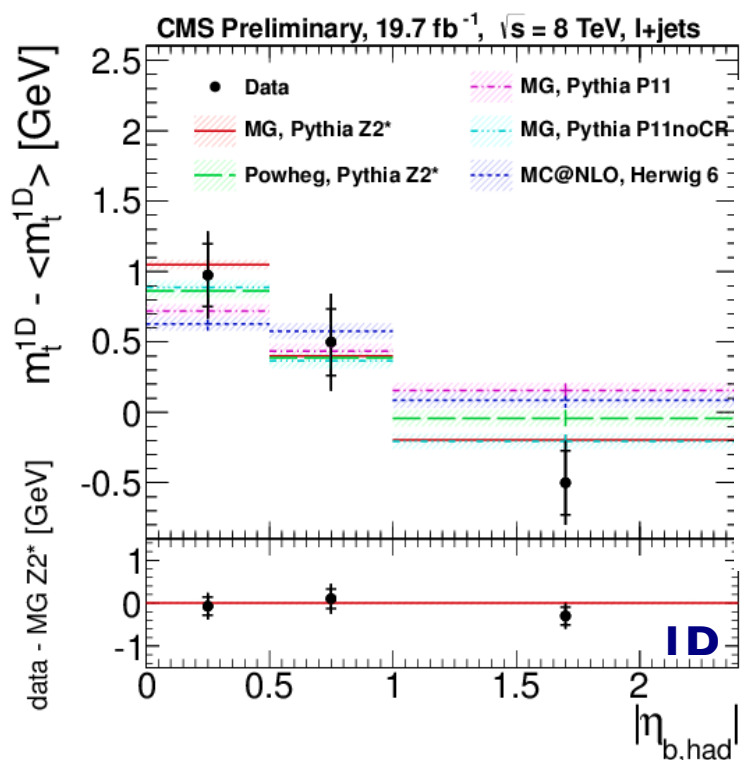
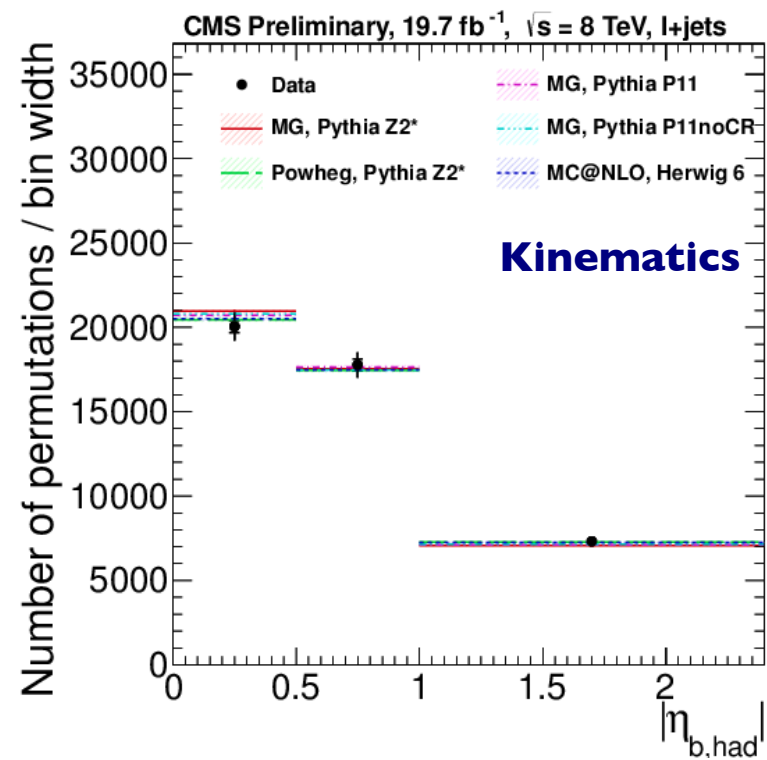
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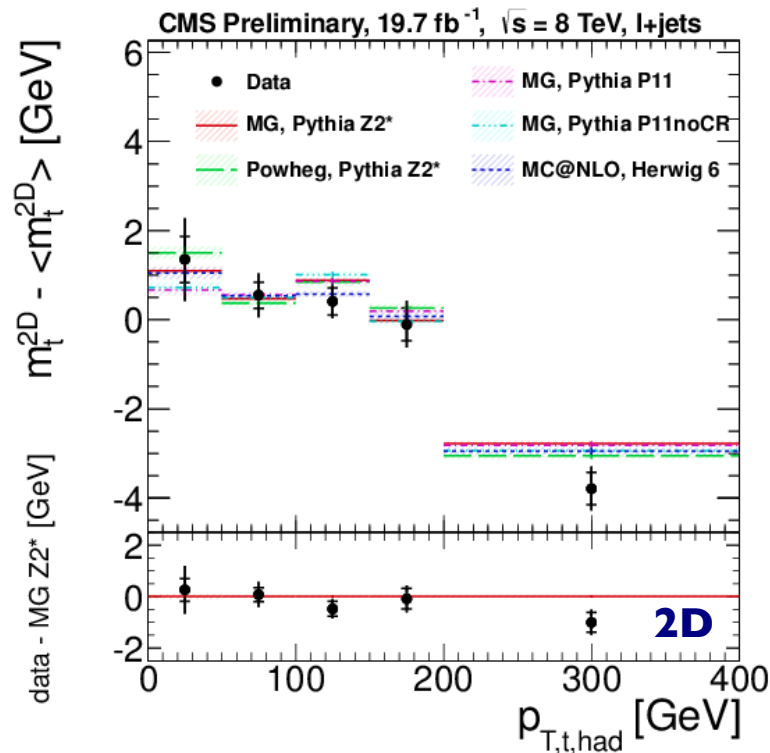
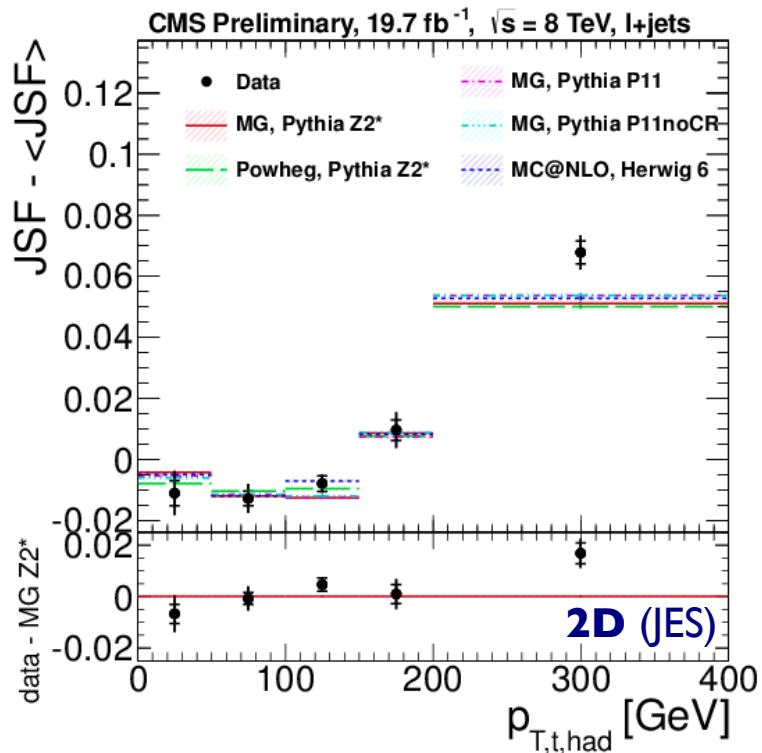
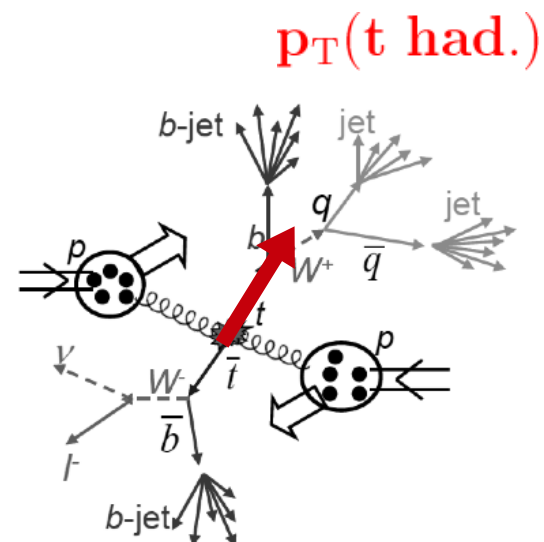
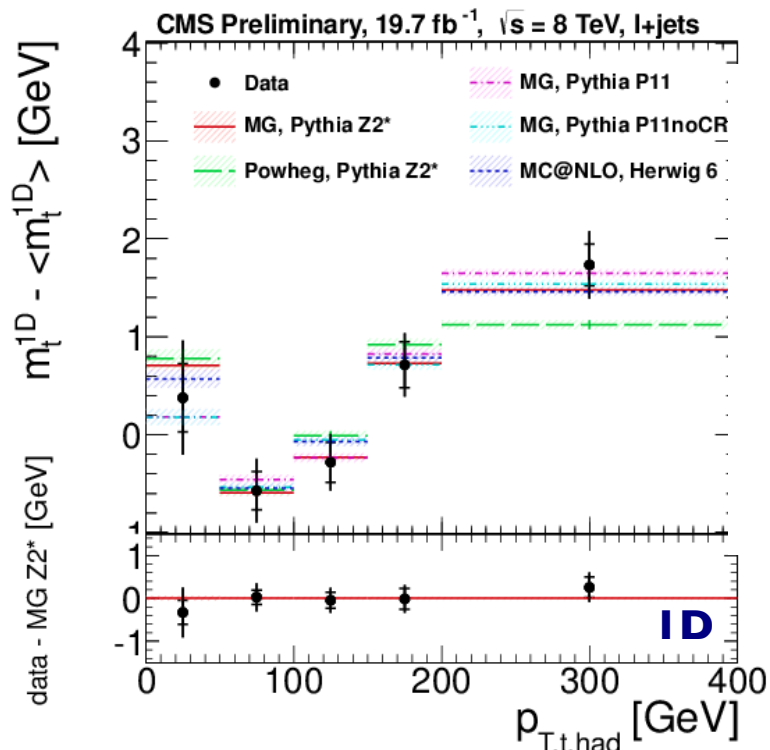
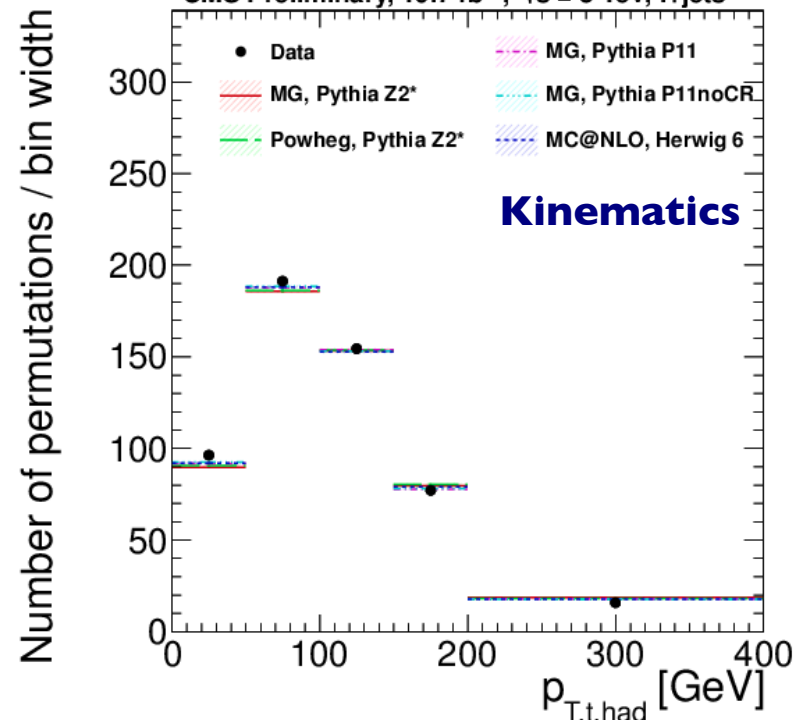
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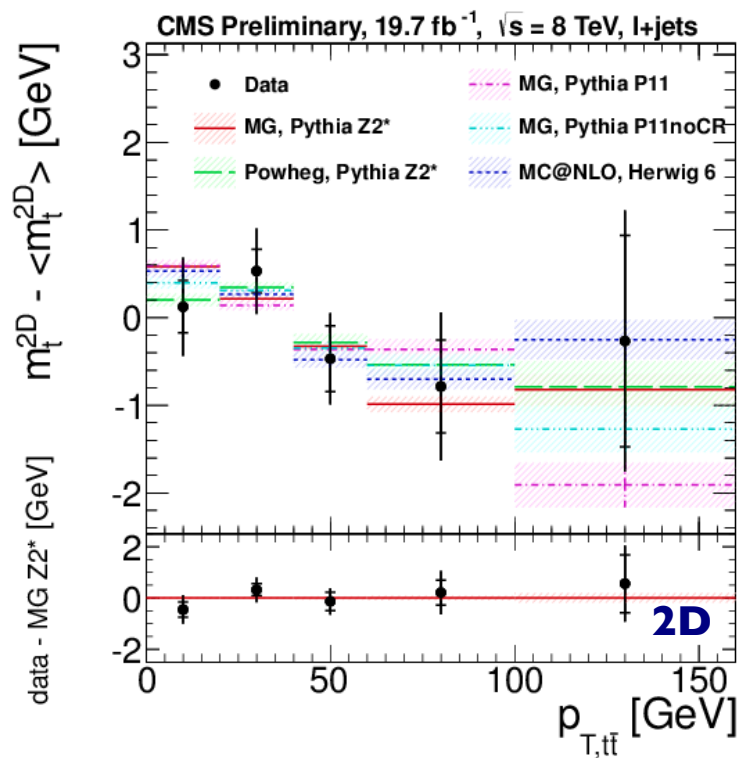
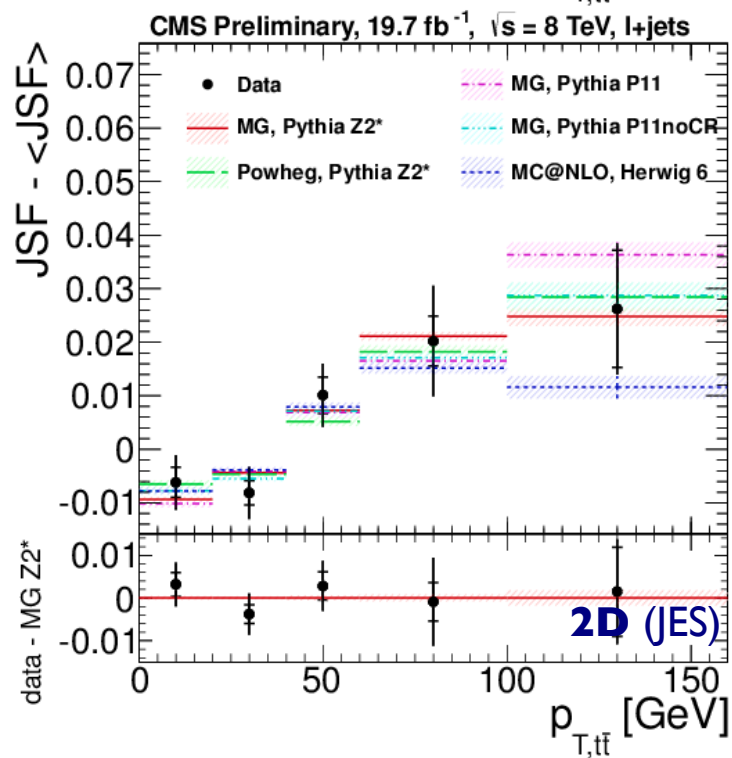
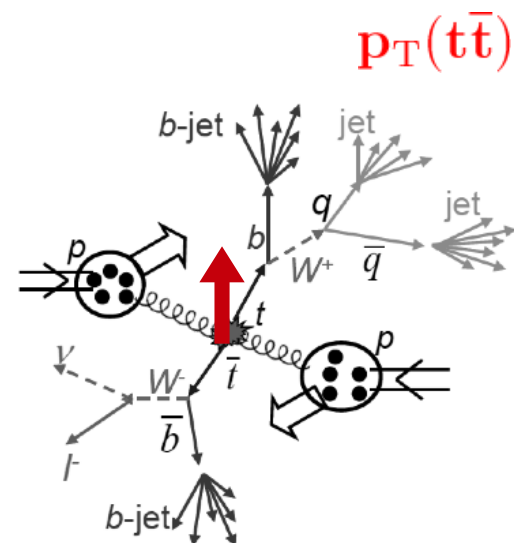
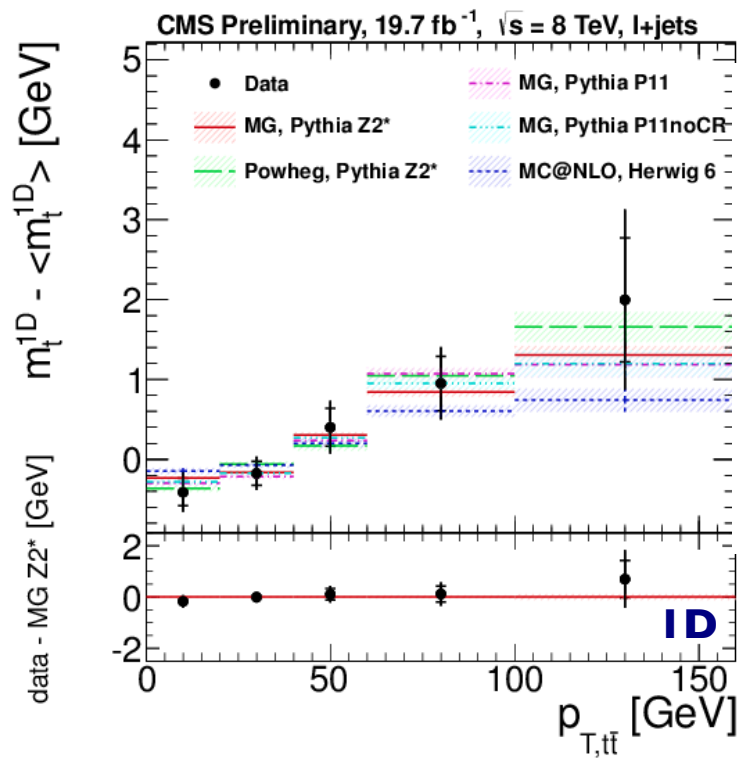
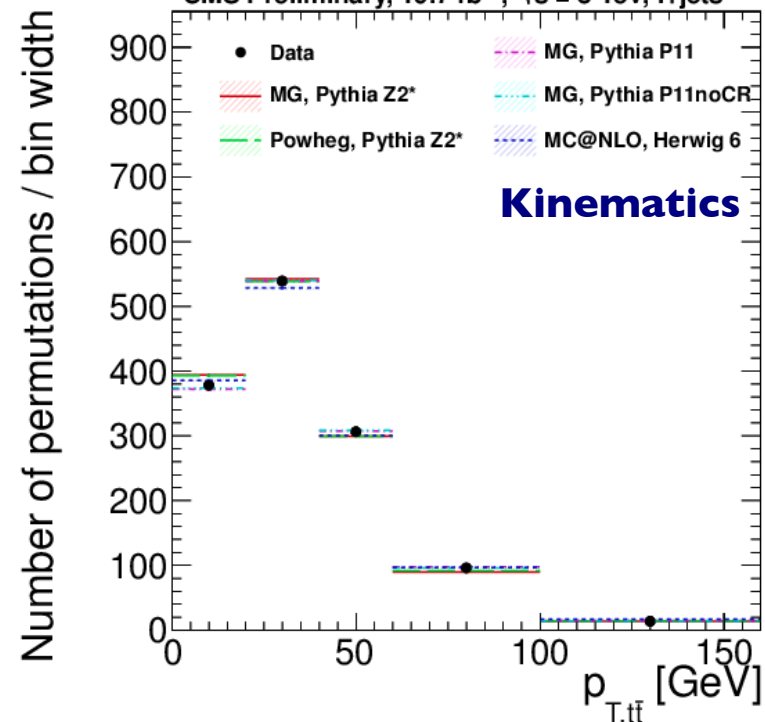
- fit  $(m_t, \text{JES})$  in data and in MC
- compare observed and expected (different models)



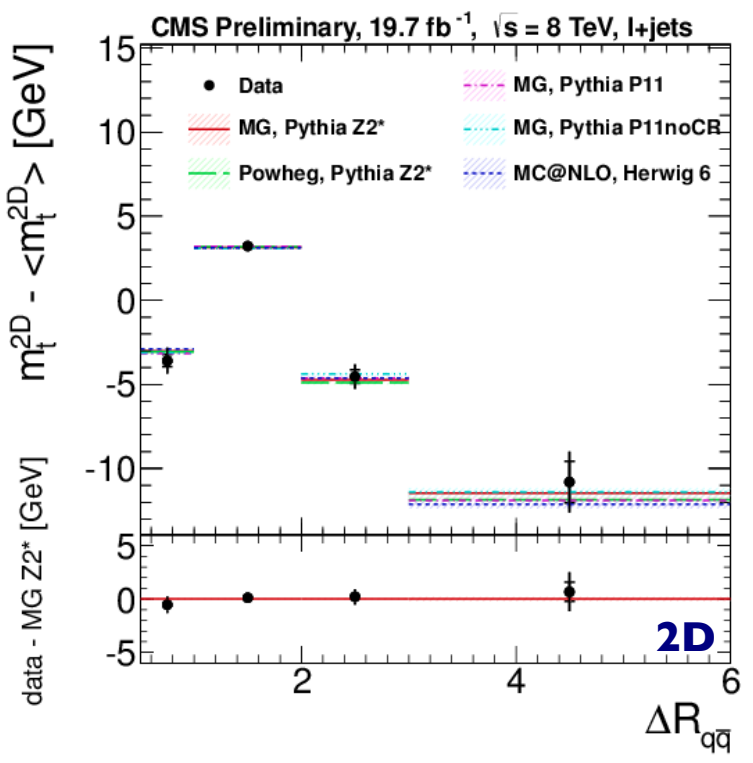
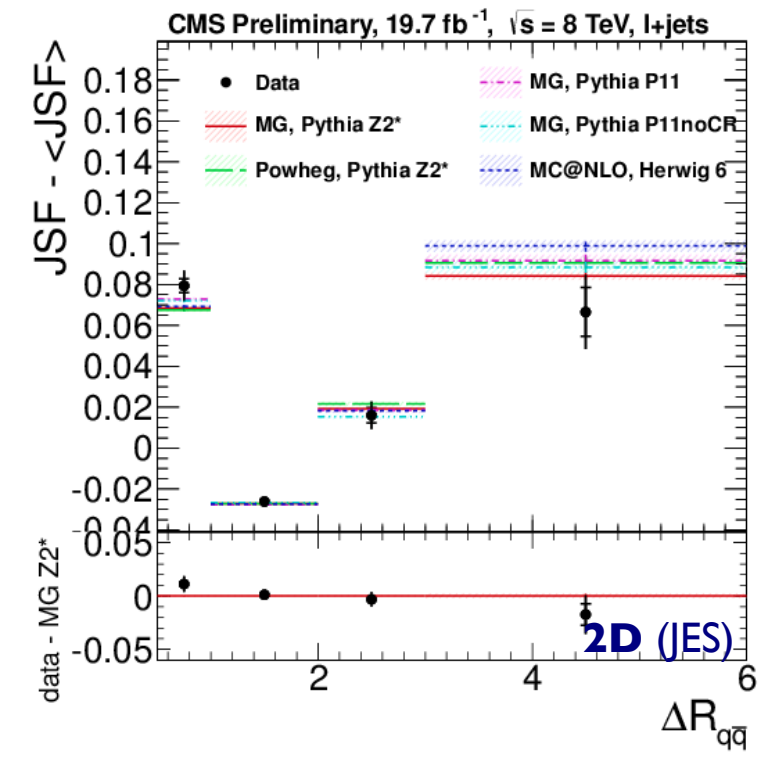
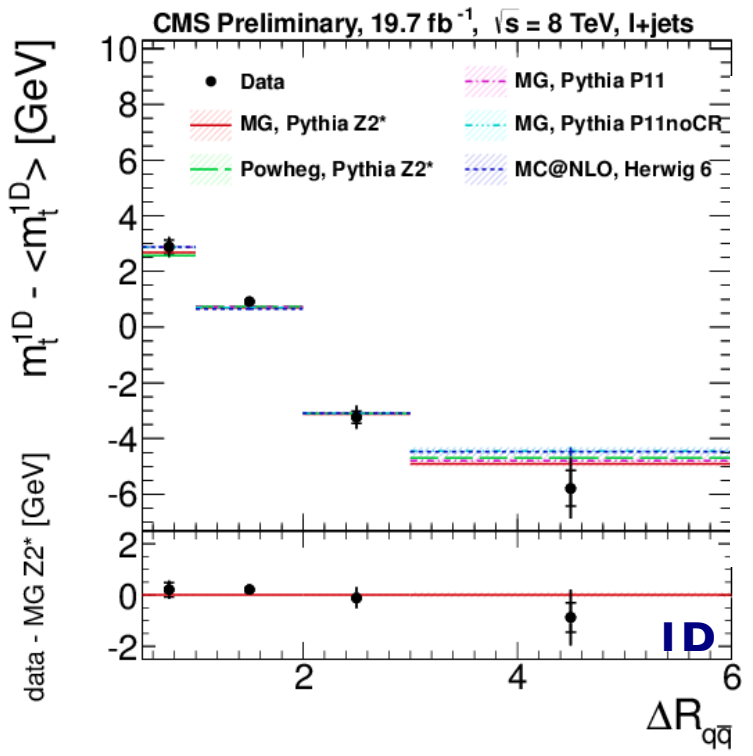
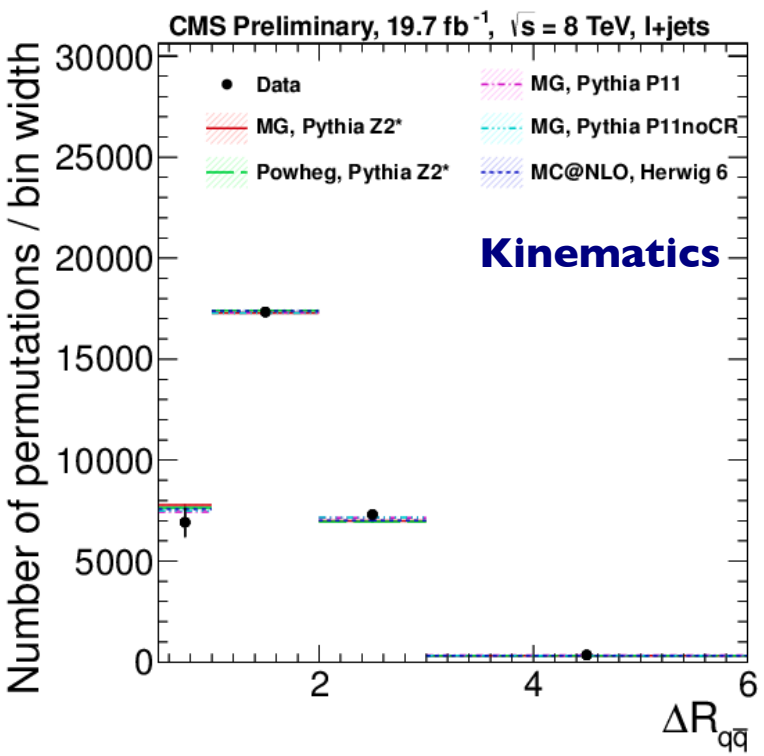
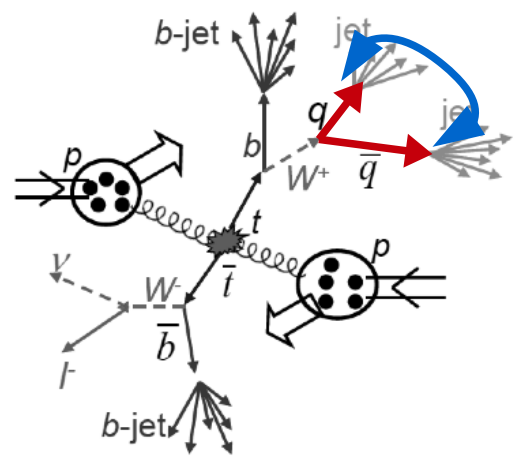








$\Delta R(q, q')$



# $m(\text{top})-m(\text{anti-top})$ is also a differential measurement

... if CPT is conserved

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## ● ATLAS - PLB 728C (2014) 363-379

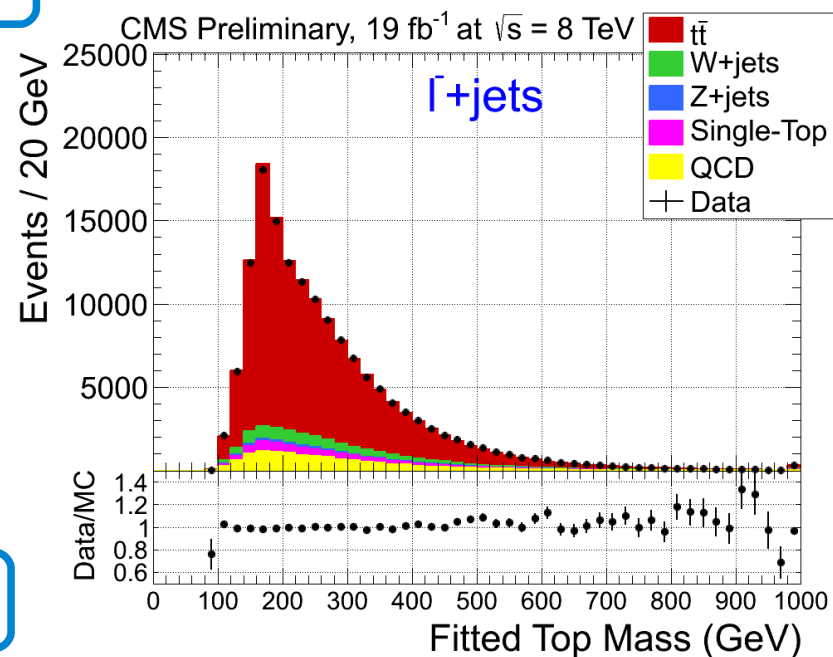
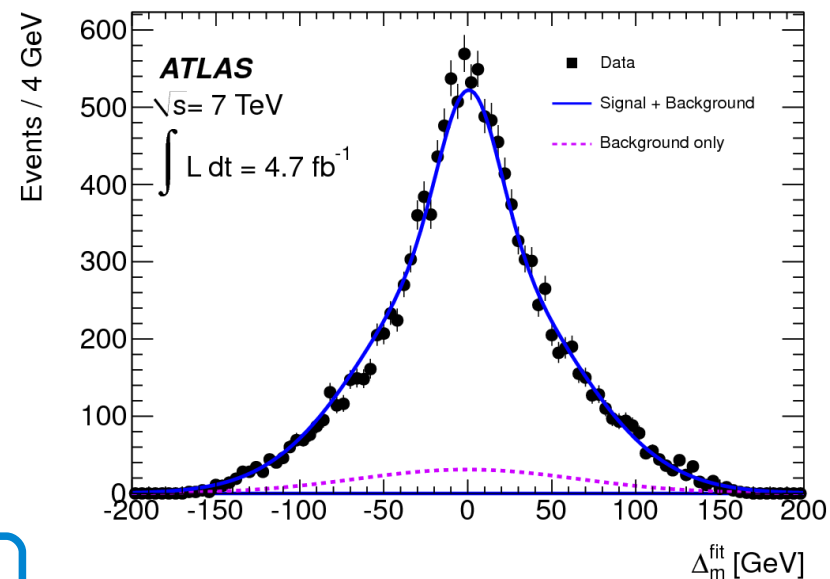
- 1 lepton, 4 jets, 2 b-tags,  $ME_T$
- $\Delta m_t$  is computed event-by-event
- measure  $\Delta m_t$  and  $N_{\text{bkg}}$  from likelihood fit
- dominated by uncertainty on b-hadron decays model  
(compare EvtGen / Pythia)

$$\Delta m \equiv m_t - m_{\bar{t}} = 0.67 \pm 0.61 (\text{stat}) \pm 0.41 (\text{syst}) \text{ GeV}$$

## ● CMS – CMS PAS TOP-12-031

- 1 lepton, 4 jets, 2 b-tags
- measure  $m_t$  inclusive in  $l+/\bar{l}$  sample with kinematic fit + ideogram method (no JES in-situ constraint)
- uncertainty on  $\Delta m_t$  dominated by b / anti-b response  
(upper bound derived from simulation)

$$\Delta m_t = -272 \pm 196 (\text{stat.}) \pm 122 (\text{syst.}) \text{ MeV}$$





# Summary of $m_t$ differential distributions

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- For each variable compute  $\chi^2$  variable to **quantify deviations with respect to predictions**

→ global  $\chi^2$  computed using  $m_t^{\text{1D}}$  and JES : independent measurements

Effect	Observable	$m_t^{\text{1D}} \chi^2$		JES $\chi^2$		$m_t^{\text{2D}} \chi^2$		ndof
		7 TeV	8 TeV	7 TeV	8 TeV	7 TeV	8 TeV	
Colour reconnection	$\Delta R_{q\bar{q}}$	1.01	2.87	3.41	3.66	1.49	0.83	3
	$\Delta\phi_{q\bar{q}}$	2.31	-	2.18	-	2.89	-	3
	$p_{\text{T},t,\text{had}}$	9.40	0.89	7.83	12.03	2.89	5.76	4
	$ \eta_{\text{T},t,\text{had}} $	0.41	5.56	3.33	1.22	3.17	1.14	3
Radiation effects	$H_{\text{T}}$	3.18	6.19	1.19	9.18	2.24	7.54	4
	$m_{t\bar{t}}$	2.52	2.16	2.98	4.69	2.25	3.22	4/5
	$p_{\text{T},t\bar{t}}$	3.39	1.02	1.67	1.22	2.18	1.33	4
	Jet mult.	1.47	4.24	2.00	0.10	1.56	1.16	2
b-quark kinematics	$p_{\text{T},b,\text{had}}$	0.81	2.57	2.35	5.80	2.17	2.17	4
	$ \eta_{\text{T},b,\text{had}} $	2.64	1.15	0.30	0.08	0.48	0.72	2
	$\Delta R_{b\bar{b}}$	4.87	0.37	2.61	1.63	8.01	1.77	3
	$\Delta\phi_{b\bar{b}}$	2.87	-	3.86	-	6.86	-	3
“EWK” kinematics	$p_{\text{T},q,\text{had}}$	-	4.04	-	8.39	-	1.28	4
	$ \eta_{\text{T},W,\text{had}} $	-	3.36	-	3.79	-	6.27	2
	$p_{\text{T},q,\text{had}}$	-	1.59	-	8.06	-	1.60	4
	$ \eta_{\text{T},W,\text{had}} $	-	1.41	-	1.09	-	1.35	3
$\chi^2/\text{ndof}$		<b>68.68/78 (p-val=0.77) at 7 TeV</b> <b>93.67/94 (p-val=0.49) at 8 TeV</b>						

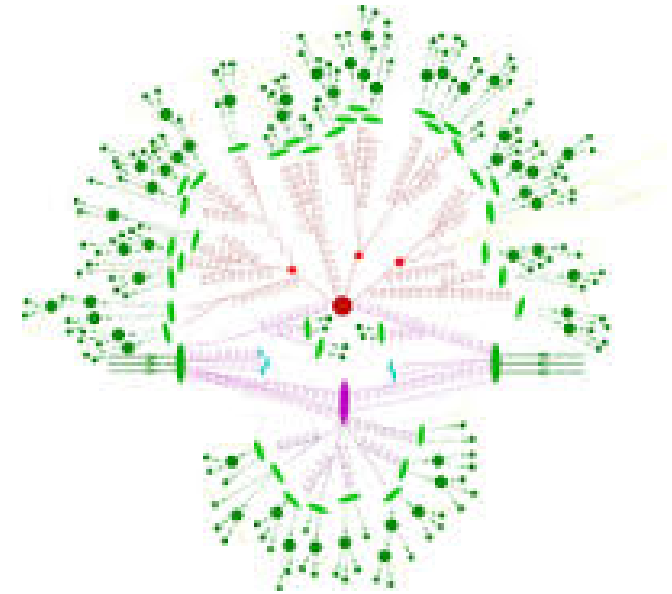
- **The top mass observable is used as a probe of the top quark event anatomy**
- **No significant deviation is found with respect to nominal calibration**
  - Baseline: Madgraph+Pythia6 Z2\*
  - The extracted top mass is stable in all corners of phase space and for all models considered
- **With more statistics (i.e. LHC Run II and beyond)**
  - establish robustness of top mass result in more detail and with better precision
  - tune models in-situ using data or simply exclude extreme models
  - use this method to compare “our” favorite MC tool to well-defined QCD calculations (cf. [arXiv:1405.4781](https://arxiv.org/abs/1405.4781))

# Mapping the proton footprint in a top quark event

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Exploratory studies of the underlying event (UE) activity are performed using tt candidate events  
A good agreement is found using MadGraph plus the Pythia 6 Tune Z2\* simulation.

- **Particle density is large at hadron colliders** ►
- In PYTHIA this is generated with a **high string density**
  - **driven by MPI** with contributions from ISR/FSR
  - colour assignments from pQCD may be modified by npQCD
  - $N_c=3$  → which partons belong together in colour singlets
  - colour reconnection may potentiate non-linear dynamics

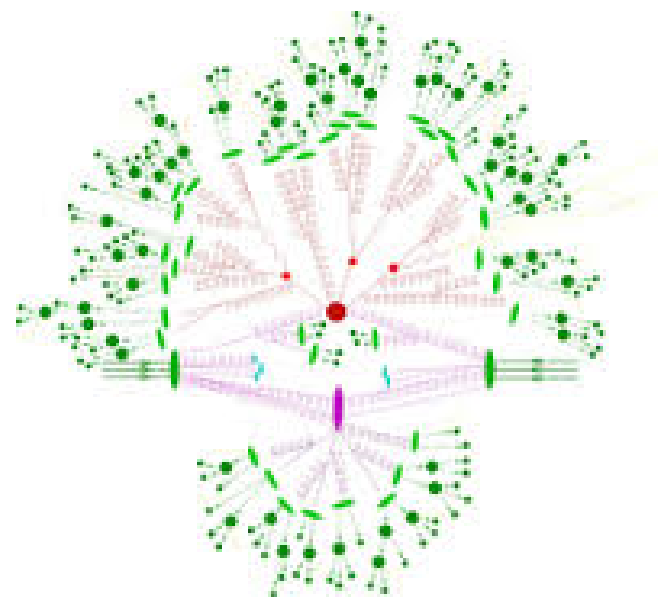




# Exploring further colour reconnection effects

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## Typical algorithm in PYTHIA

$$P_{\text{reconnect}} = 1 - (1 - \chi)^{N_{\text{MPI}}}$$

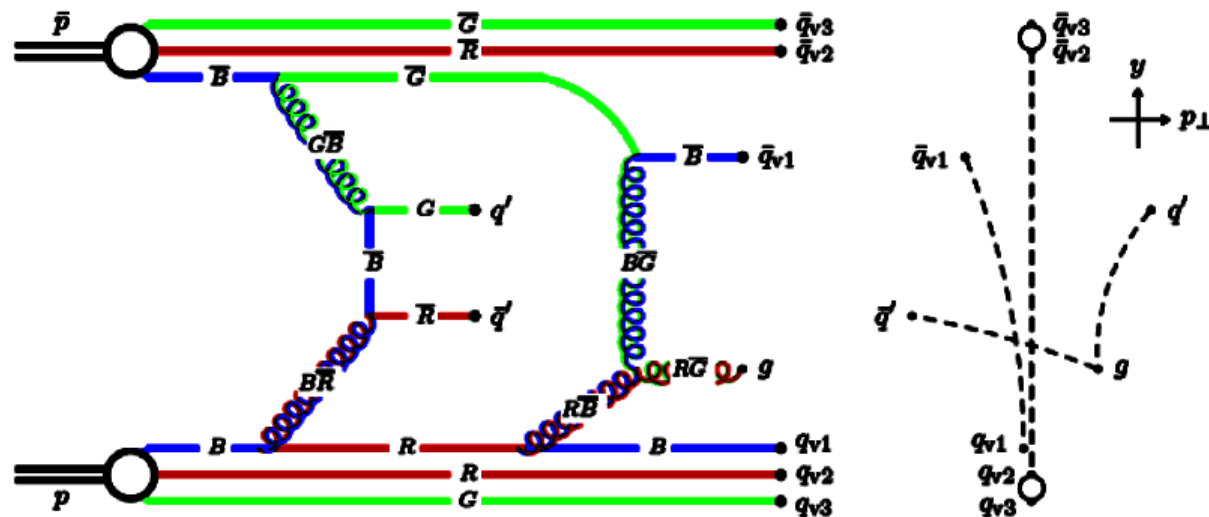
↑ strength parameter
↑ # MPI

- Each string candidate for reconnection
- Try possible reconnections, by minimizing

$$\lambda \sim \sum_{i,j} \ln \left( \frac{m_{ij}^2}{m_0^2} \right)$$

↑ reference
~1 GeV

- ~12 models available...

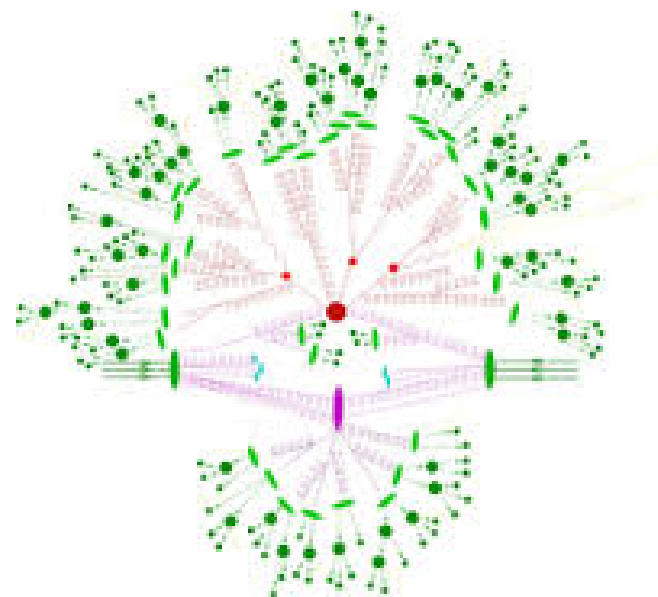


adapted from T. Sjostrand @ ISMD 2013 and arXiv:1310.8073

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## Typical test in $m_{top}$ analysis

- quote the difference between two alternative UE tunes
- Perugia I I and Perugia I I noCR (cf. PRD82:074018,2010)

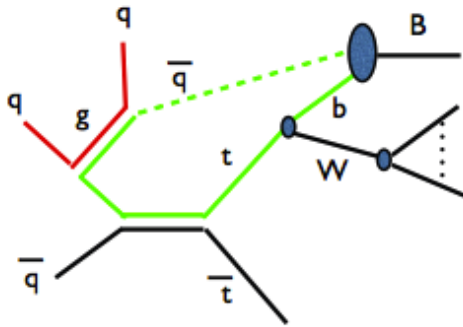
Does it tell us something useful?

Channel	$\sqrt{s}$ (TeV)	Analysis	$\Delta m_t$ (GeV)		
			1D fit	2D fit	3D fit
$\ell\ell'$	7	EPJC 72 (2012) 2202†	0.13	-	-
		EPJC 73 (2013) 2494	0.57	-	-
		ATLAS-CONF-2012-082	1.2	-	-
		ATLAS-CONF-2013-077†	0.29	-	-
	8	CMS-PAS-TOP-13-030	0.26	-	-
$\ell$ +jets	7	EPJC72 (2012) 2046	0.62	0.55	-
		ATLAS-CONF-2013-046†	-	0.03	0.32
	8	JHEP 12 (2012) 105†	0.07	0.54	-
		CMS-PAS-TOP-14-001	0.08	0.07	-
	8	CMS-PAS-TOP-13-030	0.35	-	-
All jets	7	EPJC 74 (2014) 2758†	0.15	0.58	-

# Experimental handles to test CR for top

- $\langle p_T \rangle = \langle p_T \rangle(N_{ch})$  is sensitive to CR ▶

- **Top is an unstable coloured particle:  $t \rightarrow Wb$**  ▼

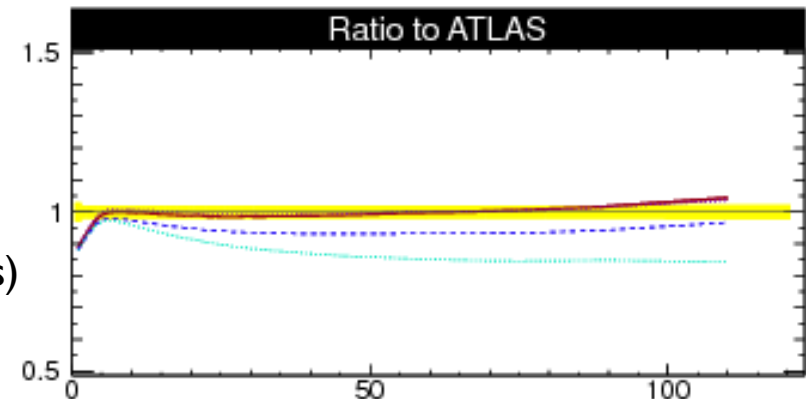
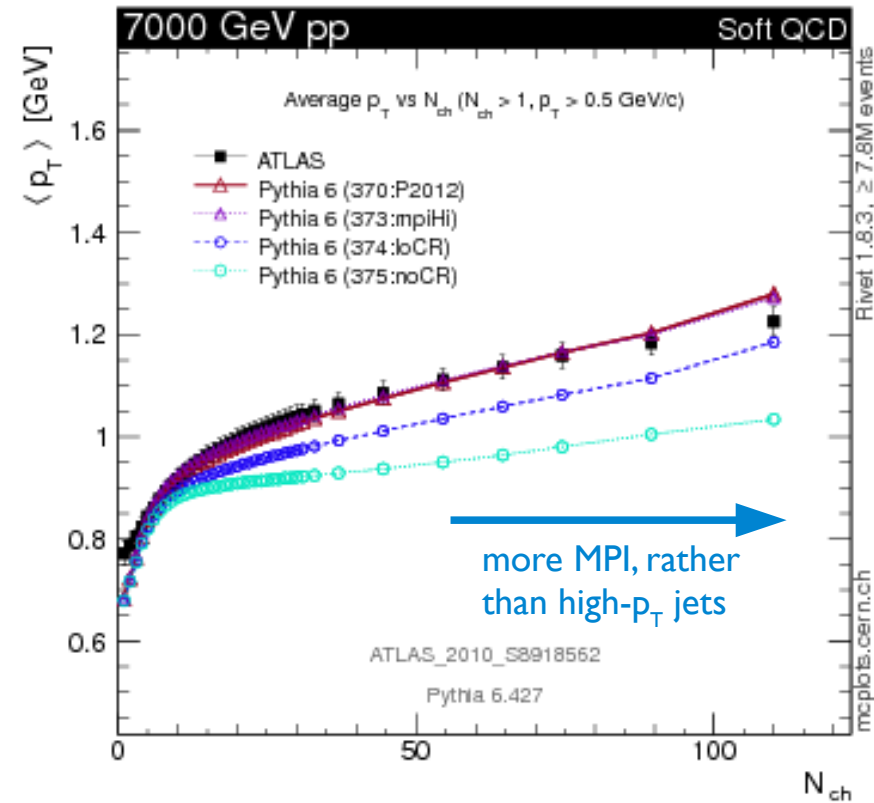


- b is for sure connected to somewhere else in the event
- $(W \rightarrow) qq'$  may or may not remain as a separate singlet
- $(W \rightarrow) lv$  is CR independent, but top kinematics dependent

- With **LHC Run I statistics:**

- limited sensitivity from  $dm_t/dx$  measurements (previous slides)
- gain insight from looking to softer effects in top pair events

source: mcplots.cern.ch



# Probing the Underlying Event with top quarks

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CMS PAS-TOP-13-007

- Use **dilepton final states to probe the UE**

- pure final state (96% pure after 2 b-tags)

- cleaner subtraction of hard-process

(remove all particle-flow candidates associated to b-tagged jets and leptons)

- **Factorize recoil effects event-by-event**

- use transverse mass estimator

$$\vec{p}_T^{t\bar{t}} \approx \vec{p}_T^e + \vec{p}_T^\mu + \vec{p}_T^{b_1} + \vec{p}_T^{b_2} + \vec{p}_T$$

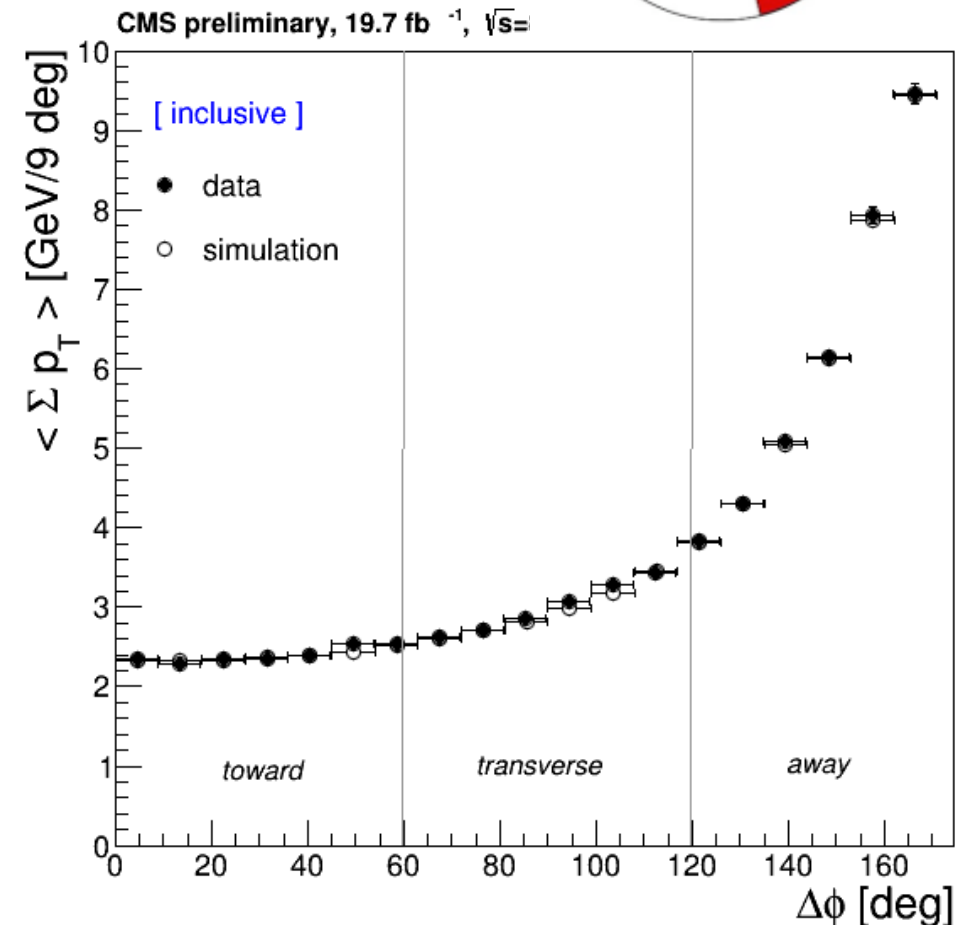
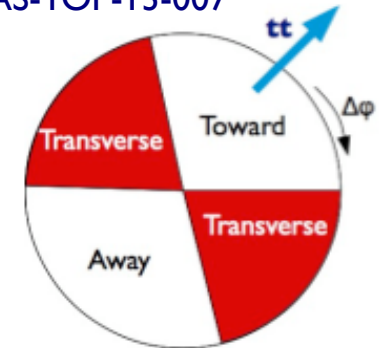
- compute  $\Delta\phi$  with respect to  $p_T(tt)$

- **Characterize soft activity through:**

- Charged multiplicity –  $N_{ch}$

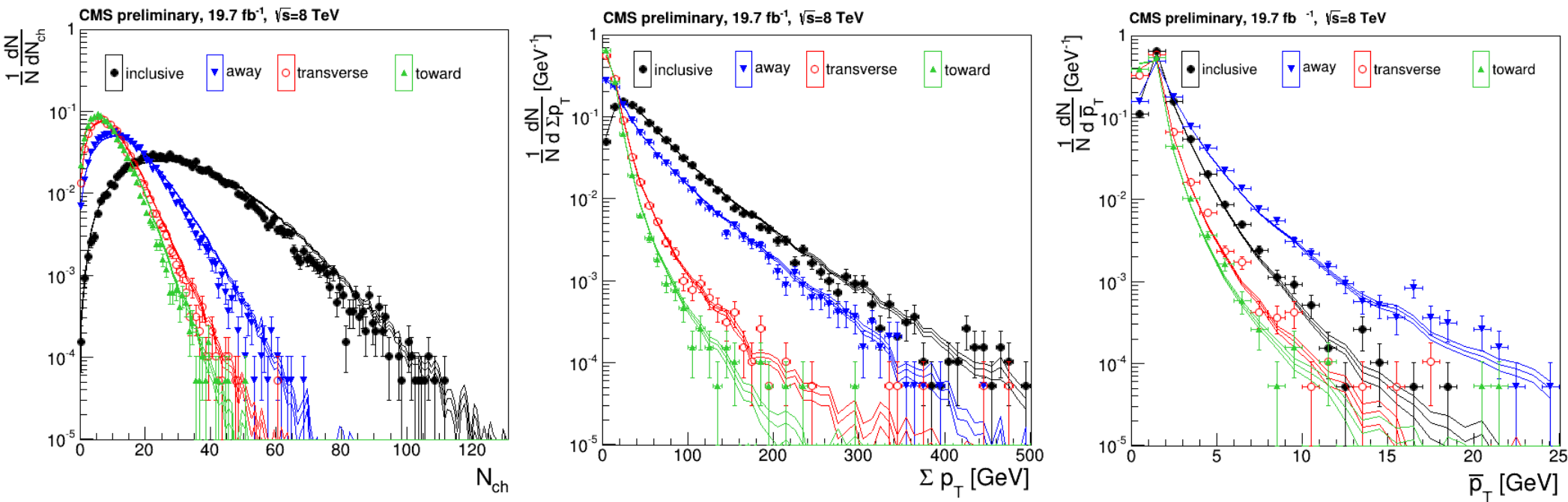
- Flux of transverse momentum –  $\Sigma p_T$

- Average  $p_T$  per charged particle -  $\langle p_T \rangle$





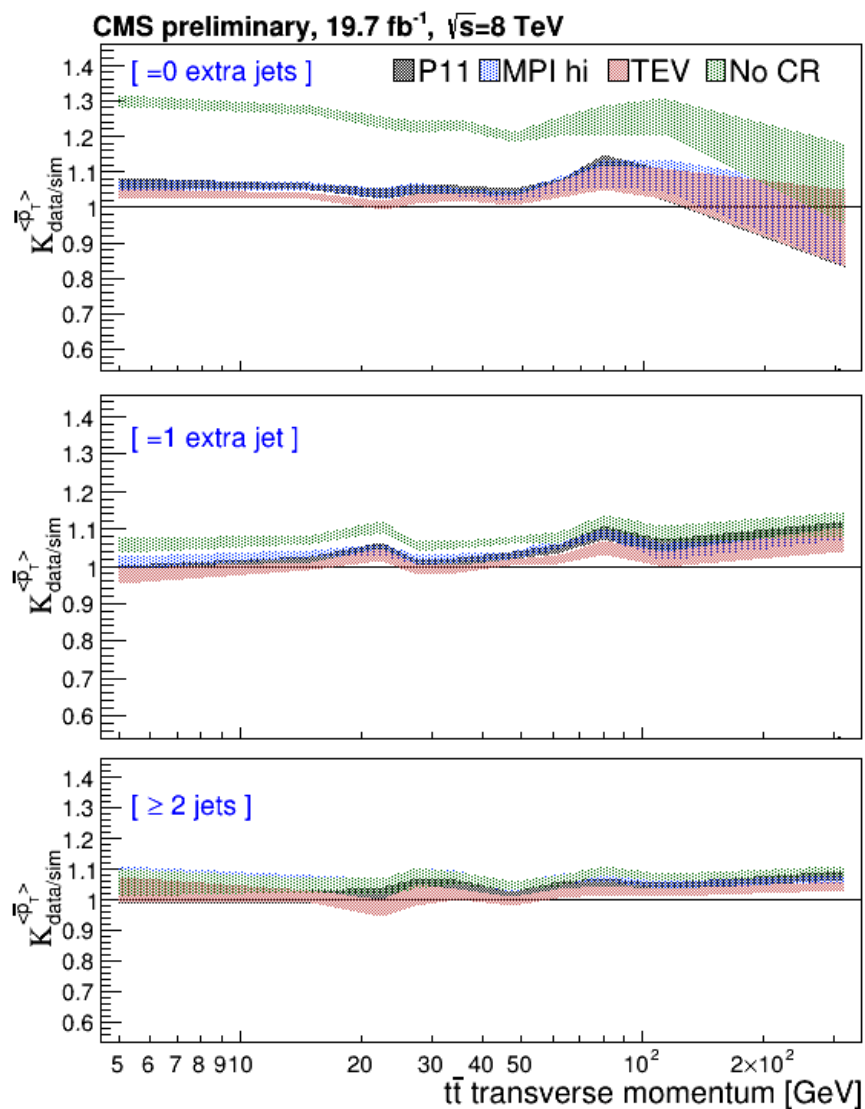
- **Toward region** has lower multiplicities and softer  $p_T$  spectrum
- **Away region** dominated by recoil increase of particle multiplicity correlated with ISR
- Comparison with the **Madgraph+Pythia6 Z2\*** default used in CMS
  - slightly smaller multiplicities observed in data but well reproduced  $p_T$  flux



# CR effects in top pair events

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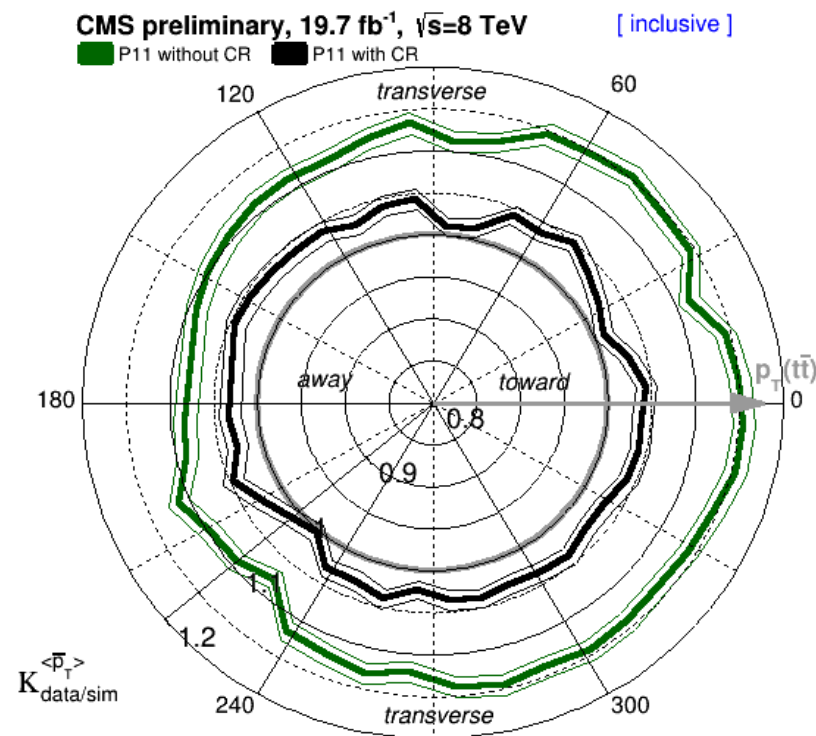
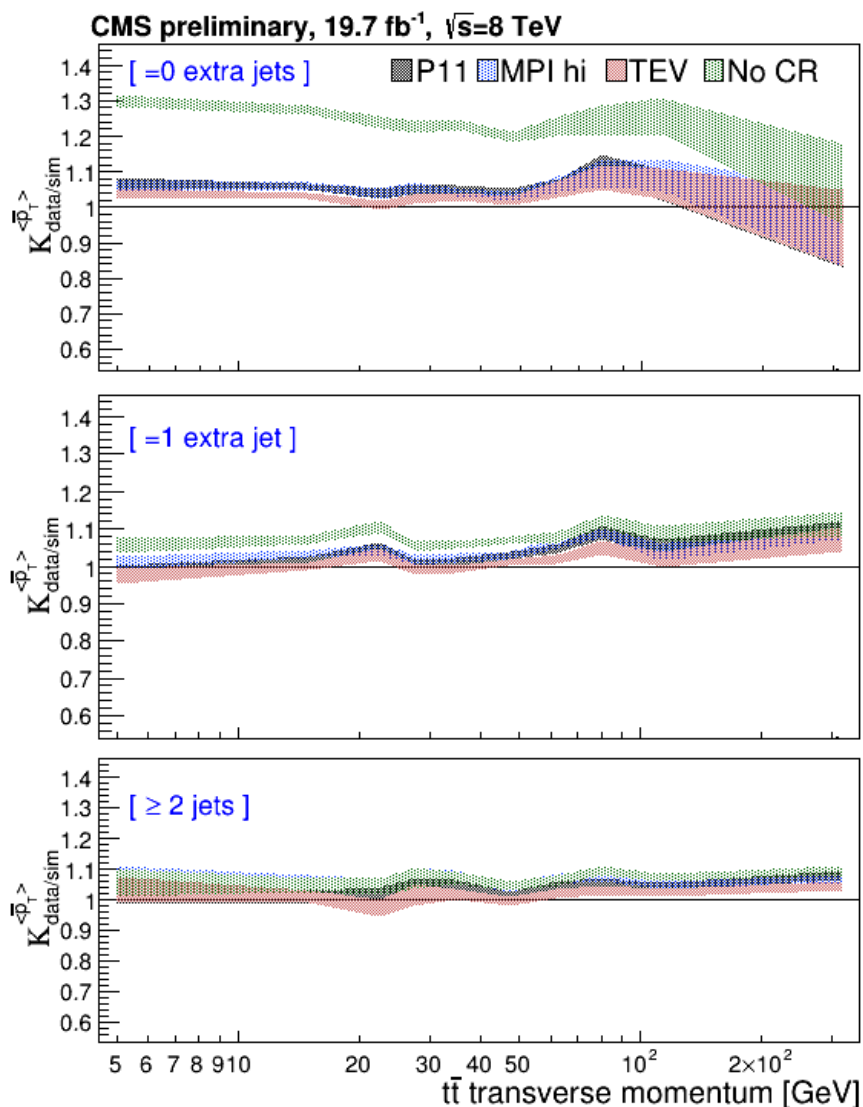
- For the **average  $p_T$  per particle** consider the **data/simulation ratio**
- Characterize as function of  $p_T(tt)$



# CR effects in top pair events

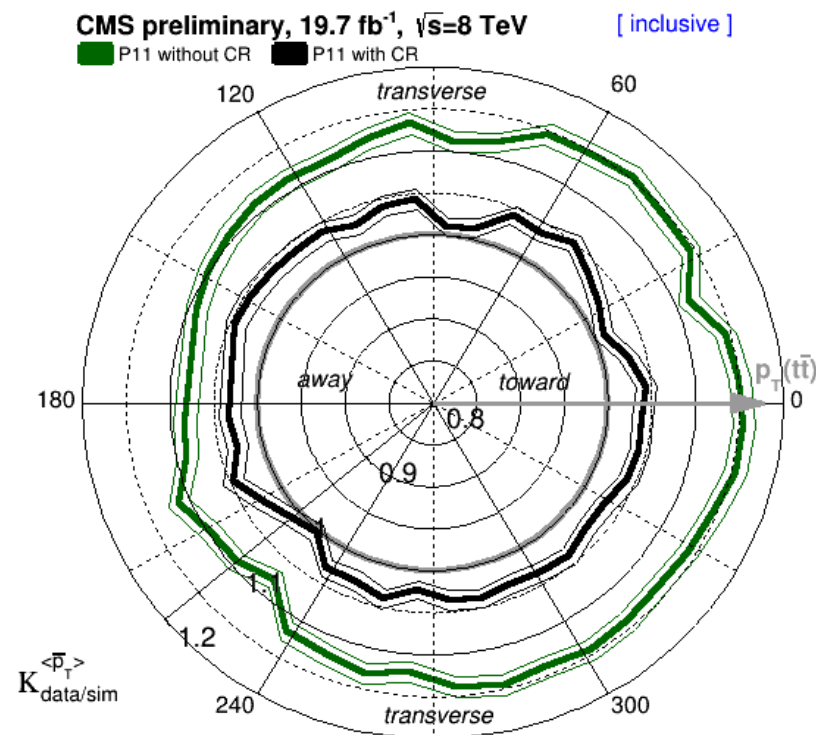
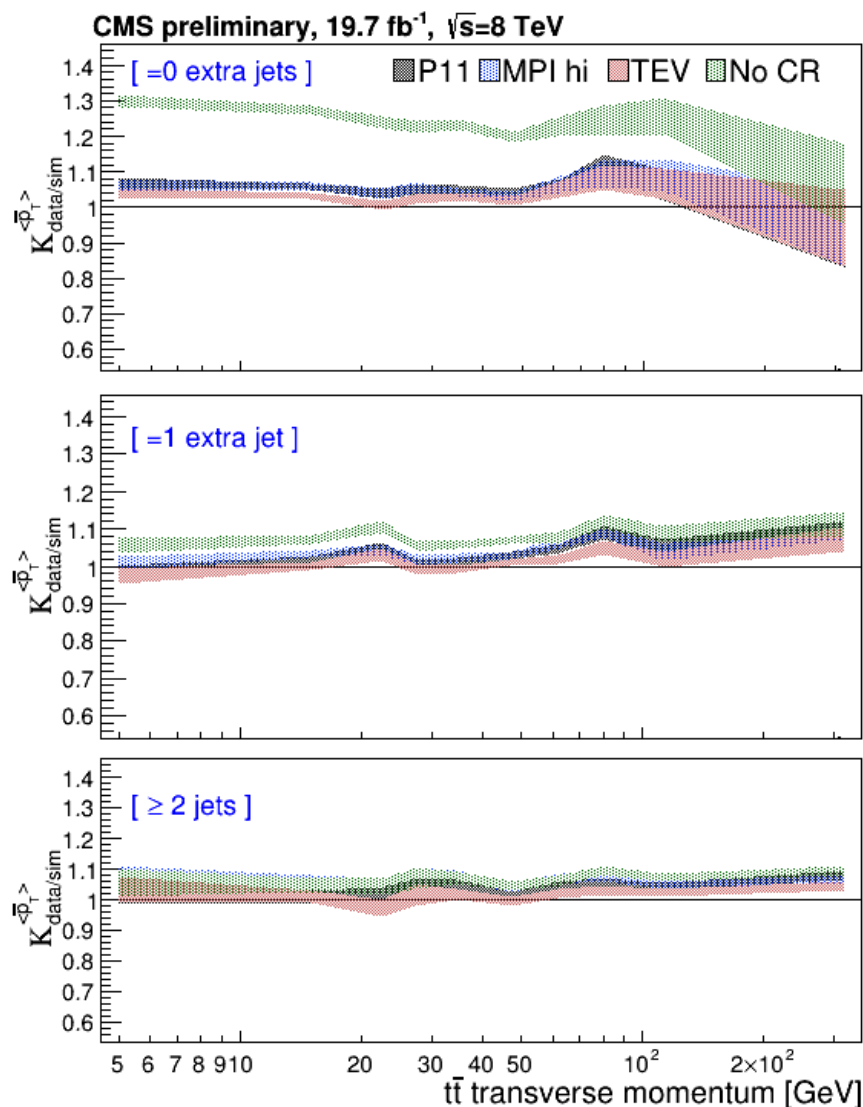
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- For the **average  $p_T$  per particle** consider the **data/simulation ratio**
- Characterize as function of  $p_T(tt)$  or as function of the event-by-event angle  $\Delta\phi$



# CR effects in top pair events

- For the **average  $p_T$  per particle** consider the **data/simulation ratio**
- Characterize as function of  $p_T(tt)$  or as function of the event-by-event angle  $\Delta\phi$

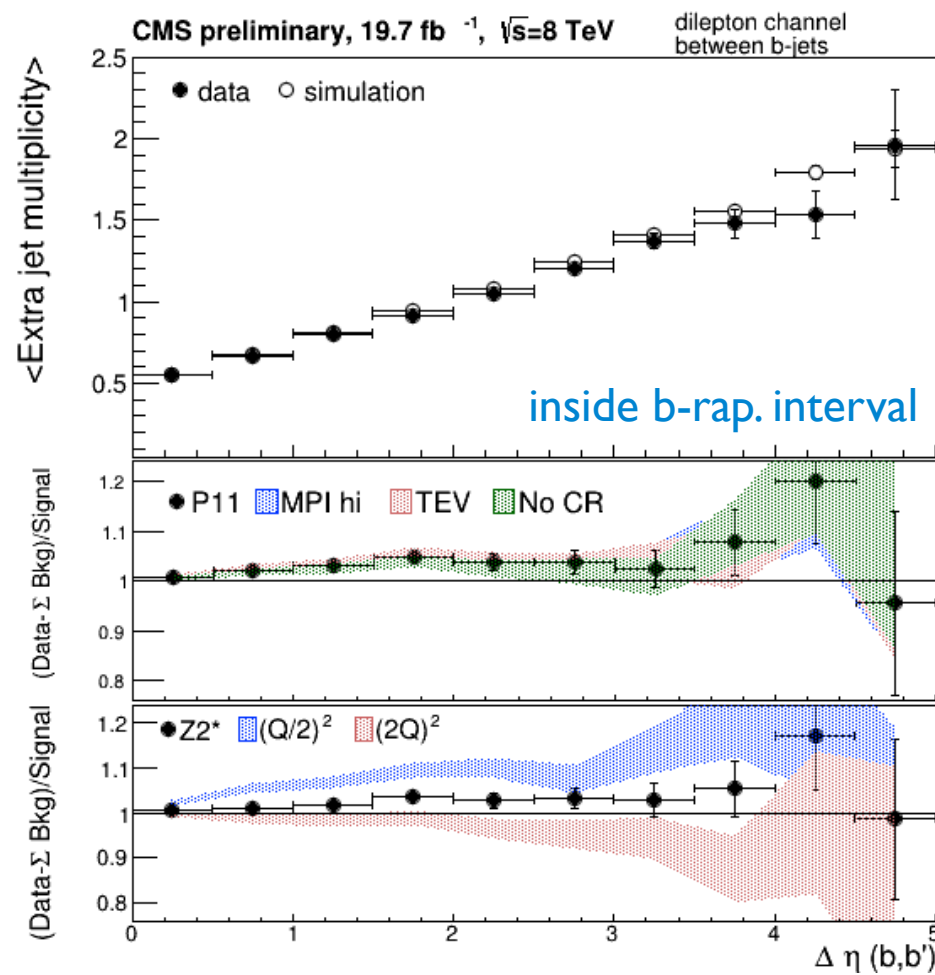
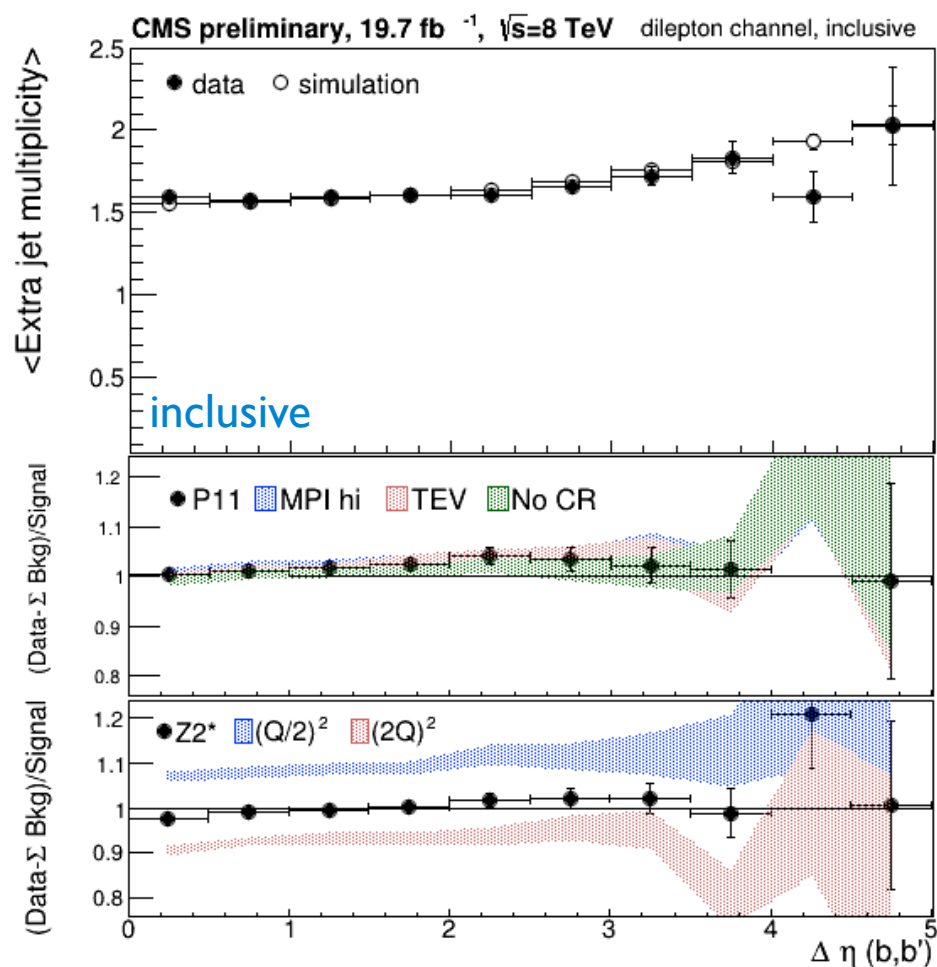


- **CR model is crucial**
  - when system is close to rest
  - along the  $t\bar{t}$  direction
- What is being tested with noCR?

# b-rapidity-interval related effects

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- **Counting extra jets** ( $p_T > 20$  GeV) inclusively or inside the b-rapidity interval
  - **no sensitivity to CR** : mostly dependent on QCD scale choice
  - good agreement with the default choice in Madgraph+Pythia6





- **We have mapped the “proton footprint” in top quark events**
- **Fair agreement is found with MinBias-derived tune**
  - Madgraph+Pythia6 Z2\* based
  - Extreme models do not describe the data and offer conservative envelopes
- **Colour reconnection effects (Pythia model)**
  - “CR on” confirmed in top pair events: pronounced for systems at rest and along tt direction
  - “CR off” is excluded by the data
  - Observed effect CR on/off for top mass generally small (<0.1 GeV in the latest measurements)
  - is CR on/off, with a single tune, ending its days in  $m_{\text{top}}$  analysis ?
  - shouldn't we look at other models? attempt to trace an emerging pattern from comparison?

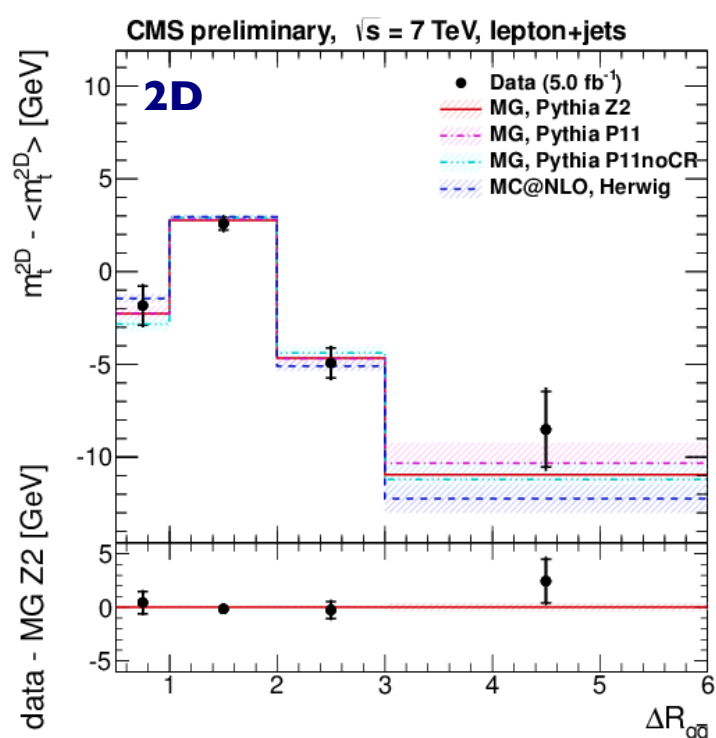
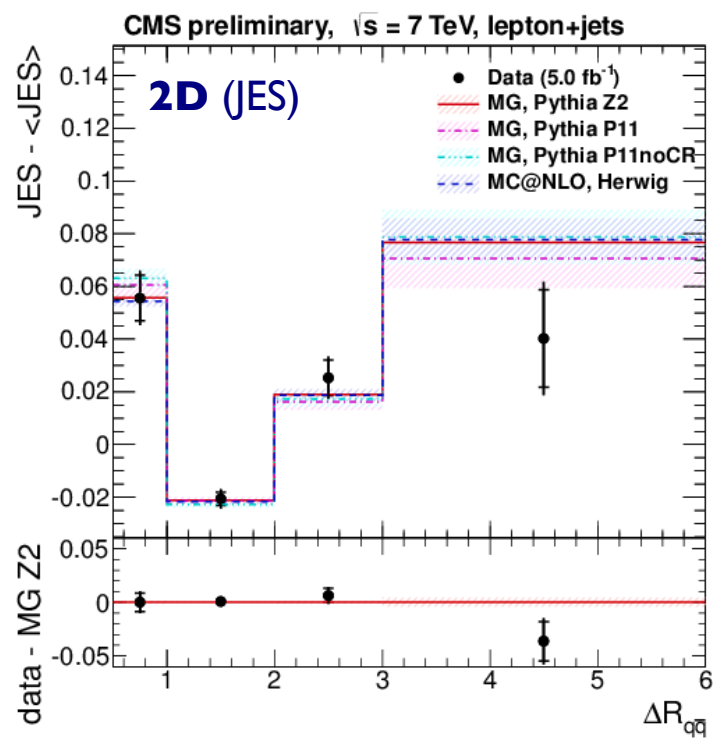
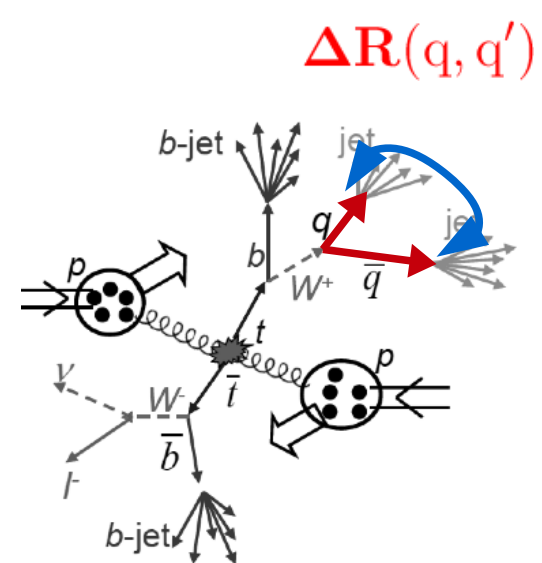
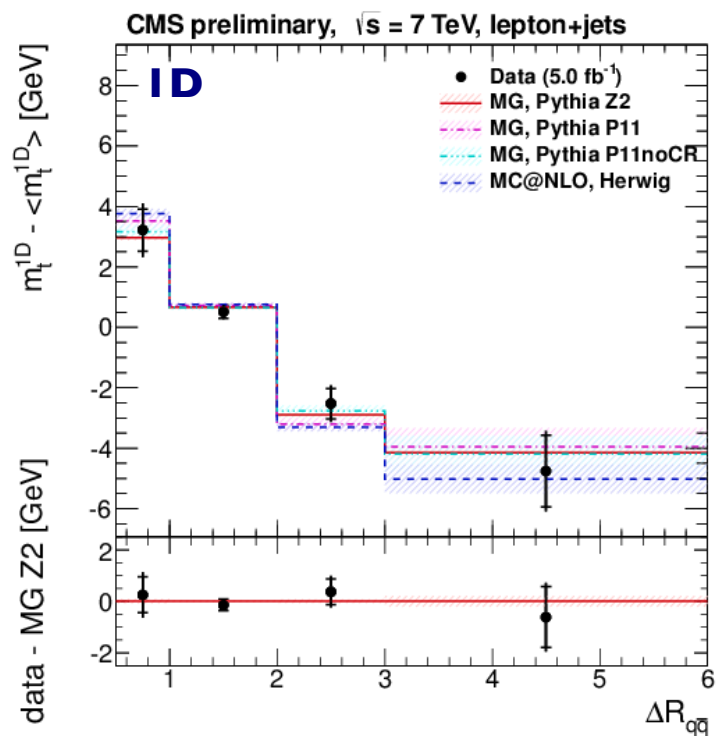
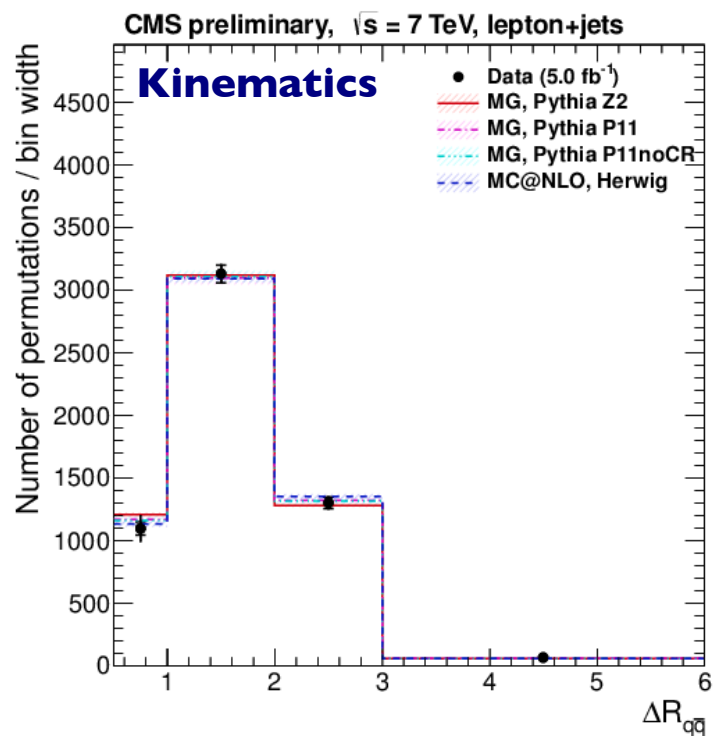
# Summary

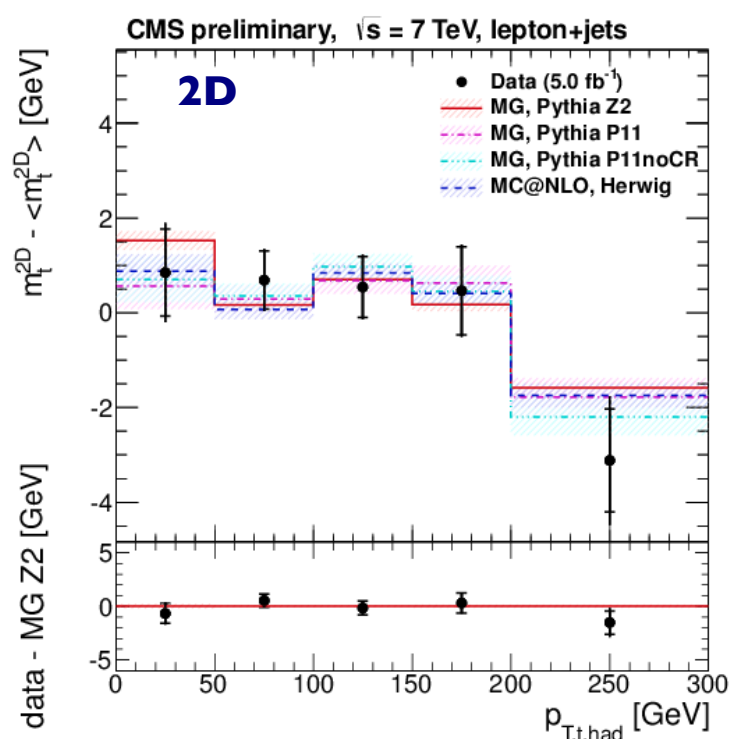
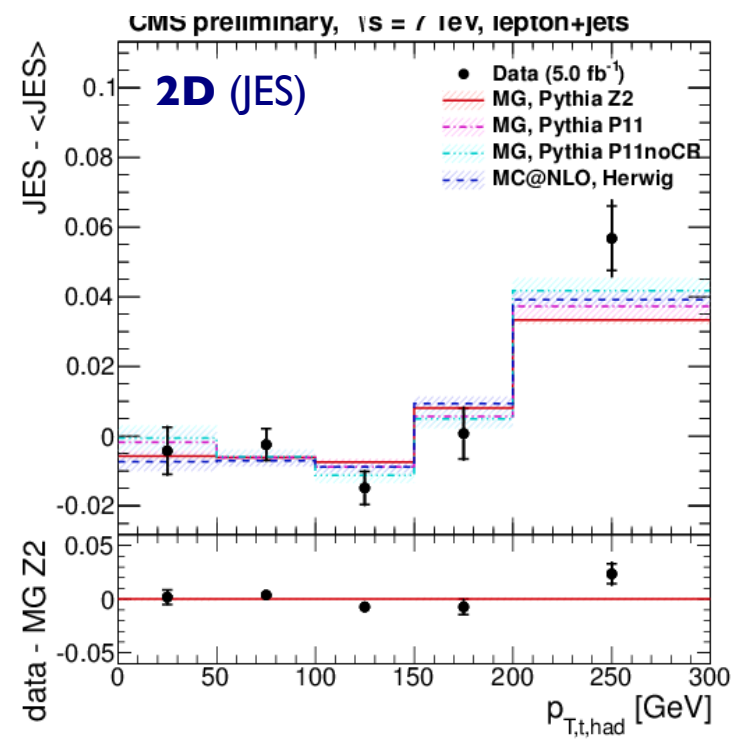
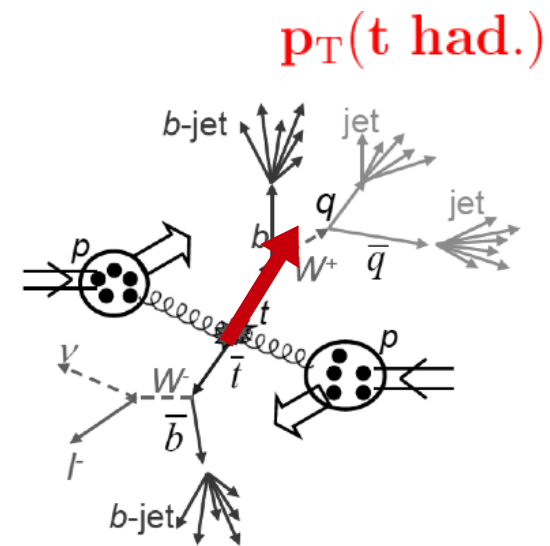
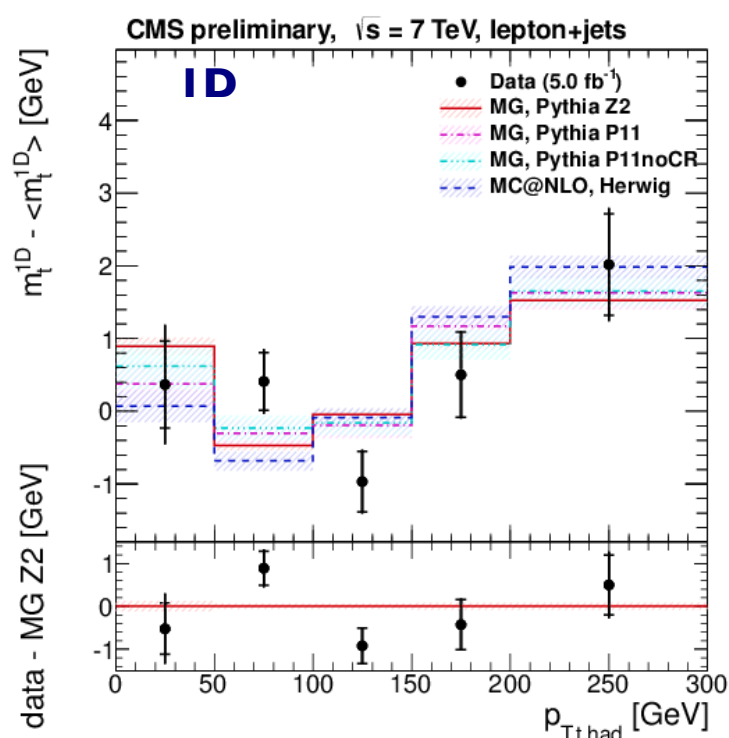
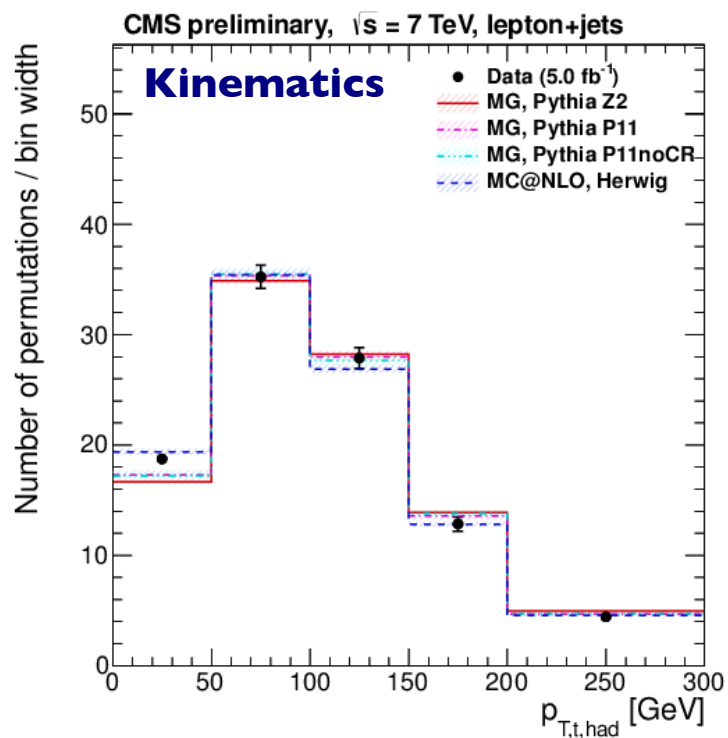
Trying to understand our  $m_{\text{top}}$  measurements we have probed top quark events as Pollock would:  
"the strangeness will wear off and I think we will discover the deeper meanings...".  
We aim to have a better understanding of the fine details in a near future.



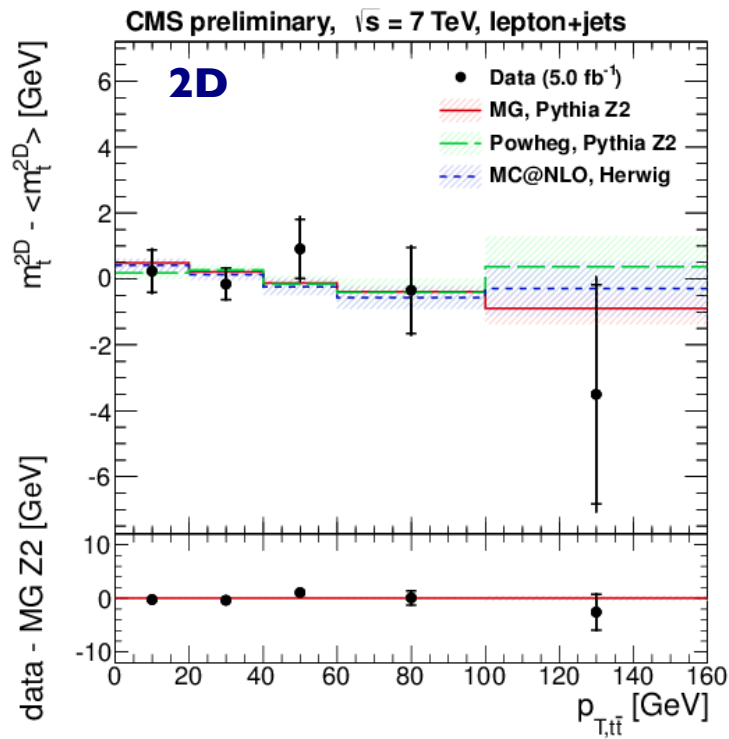
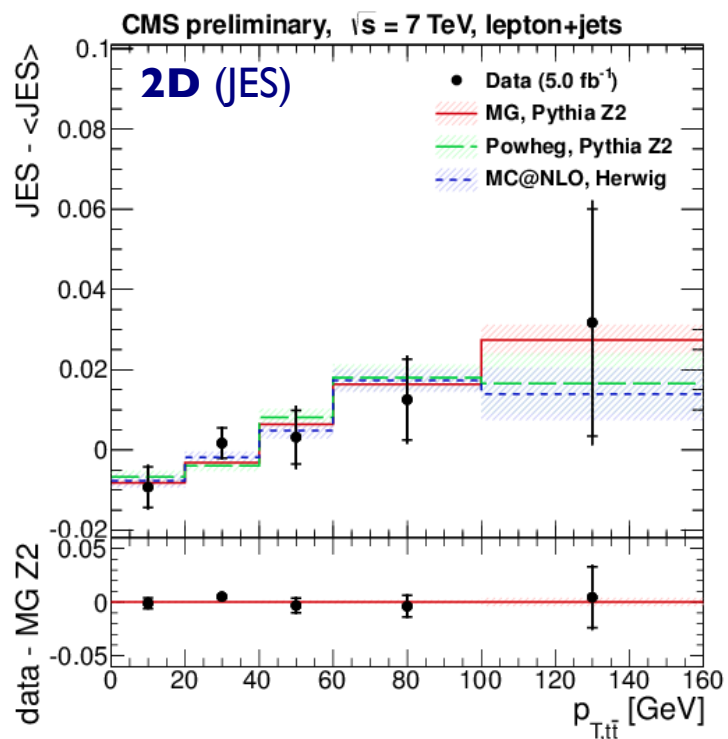
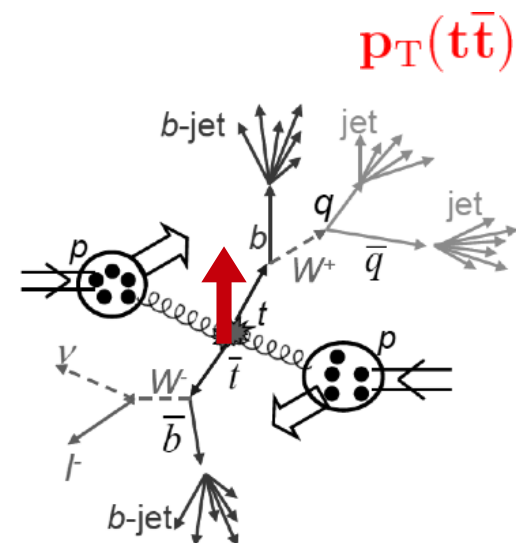
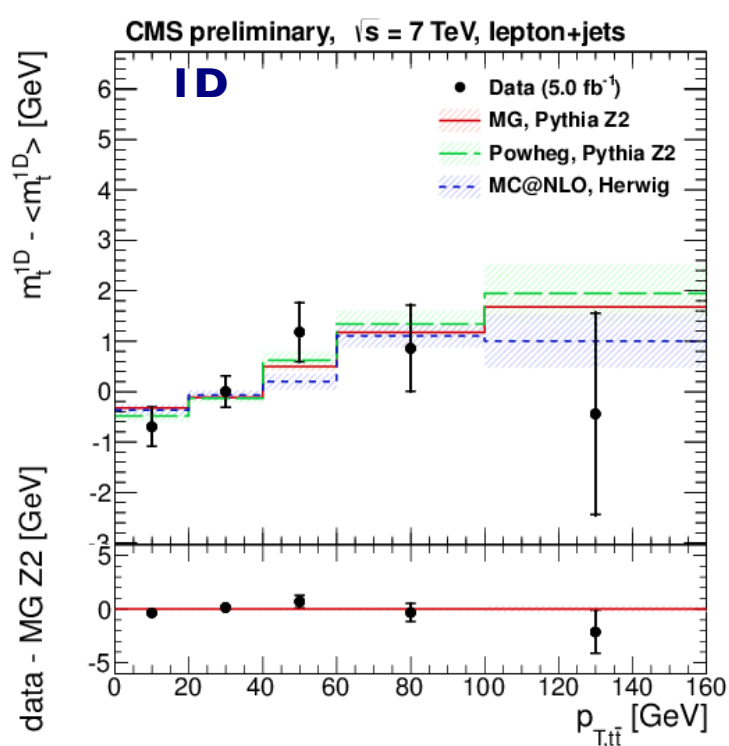
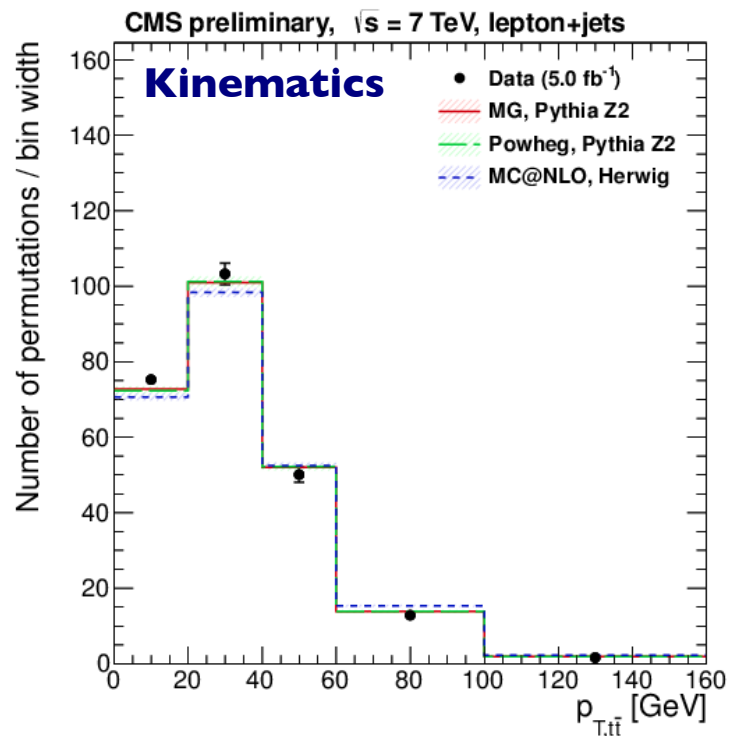
- **“Standard” mass measurements adopt the MC definition of  $m_{\text{top}}$** 
  - 0.73 GeV uncertainty ( $0.43\% m_{\text{top}}$ )  $\sim 4 \Lambda_{\text{QCD}}$  !
  - inclusive phase-space calibration is performed
  - robustness tested against different theory models and experimental uncertainties
- **Data can be used to image in finer detail a top quark event**
  - differential measurements do not reveal significant biases for different variables
  - UE studies show evidence for colour reconnection effects in top pairs
- Strategy for **future  $m_{\text{top}}$  measurements should consider these approaches**
  - show consistency of top mass definition with your favorite MC
  - constrain/exclude in-situ some of the uncertainties

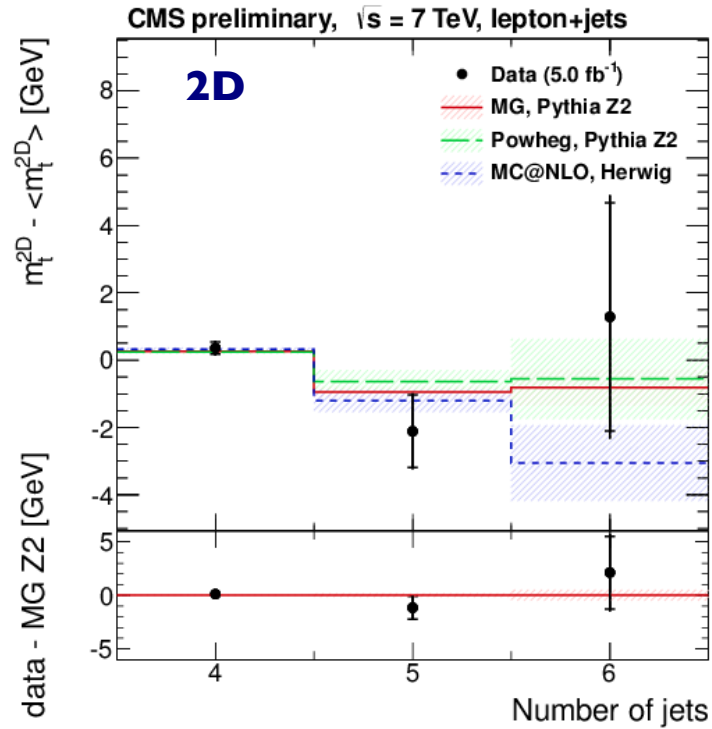
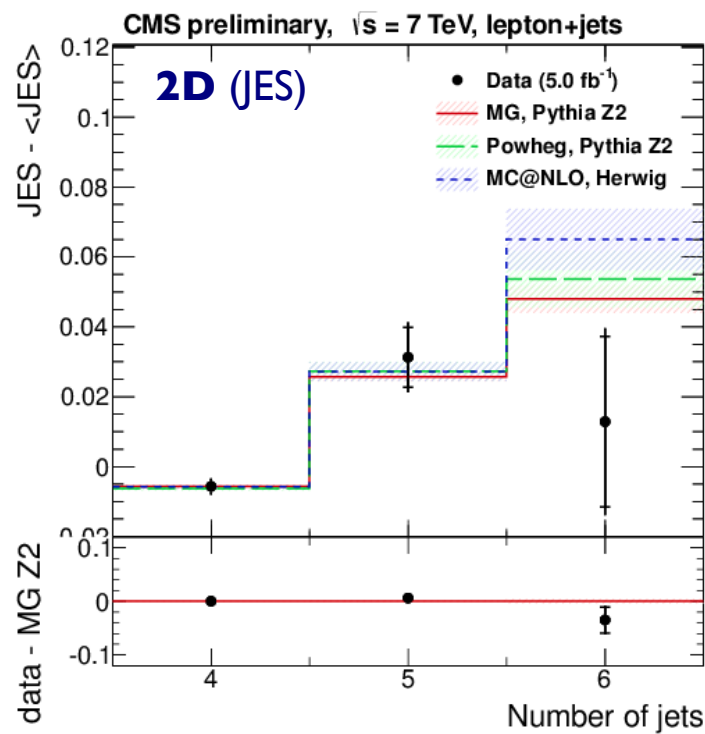
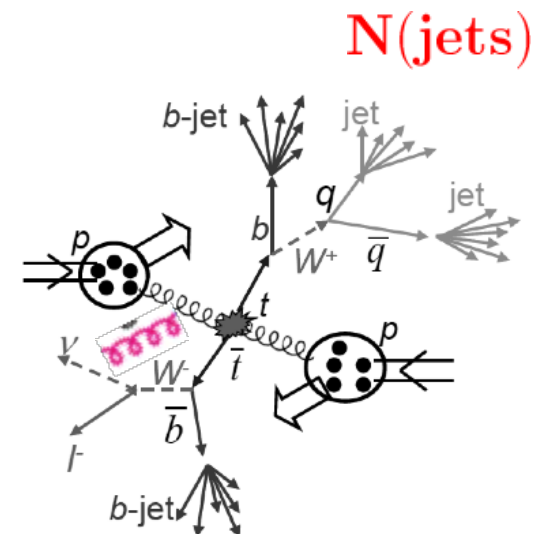
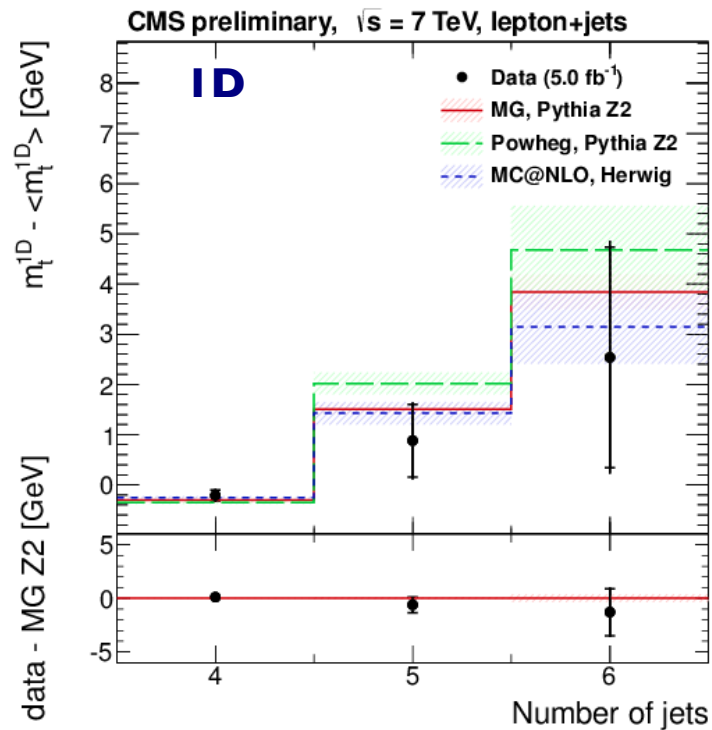
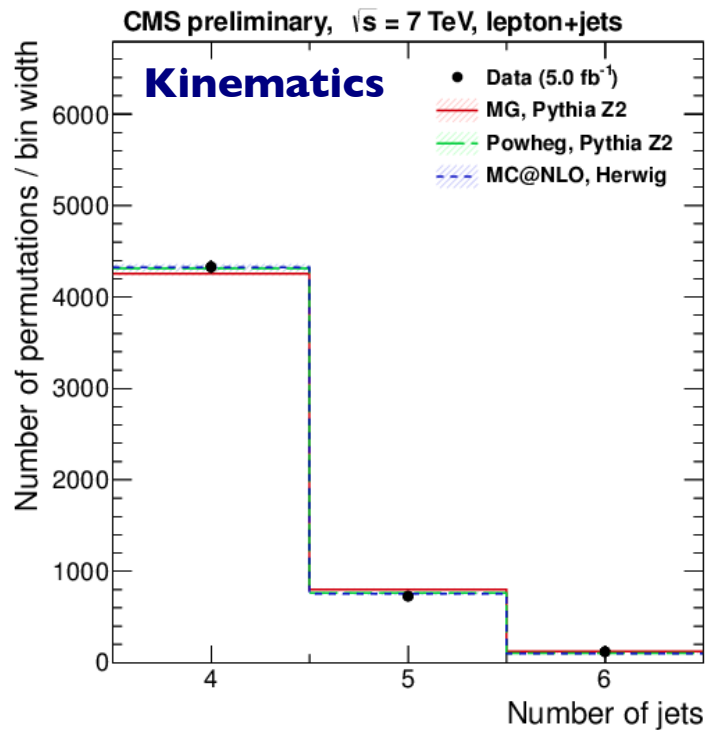
**Backup**

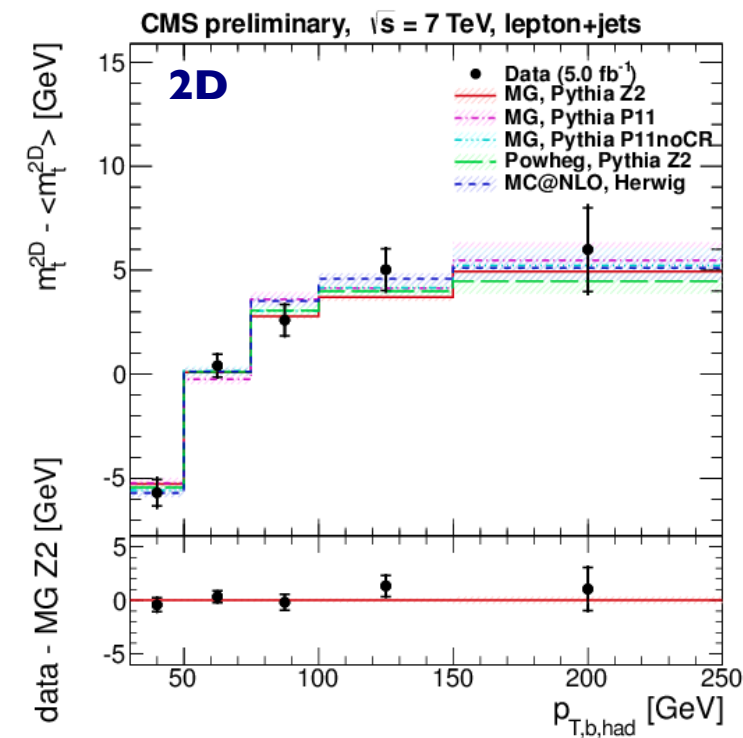
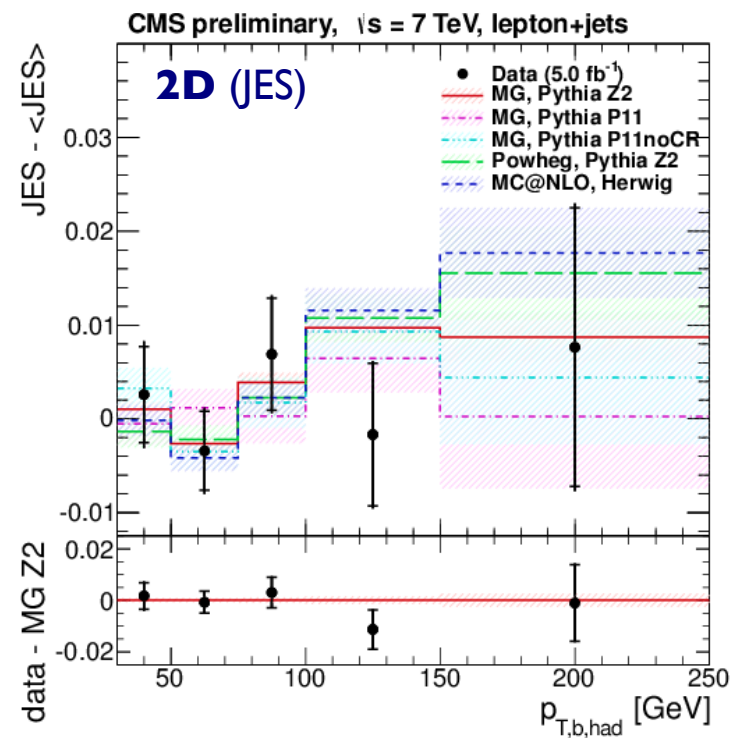
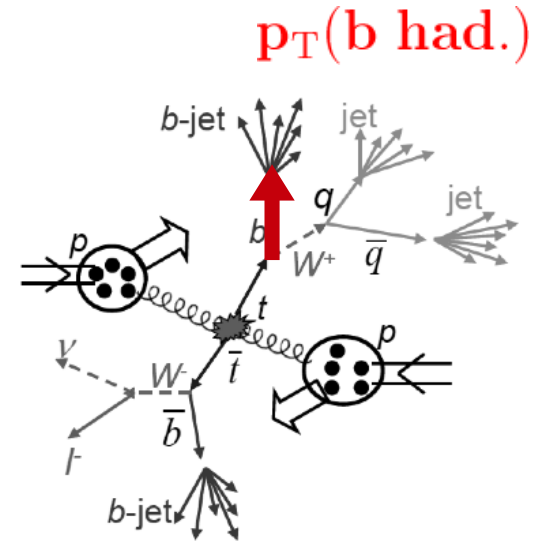
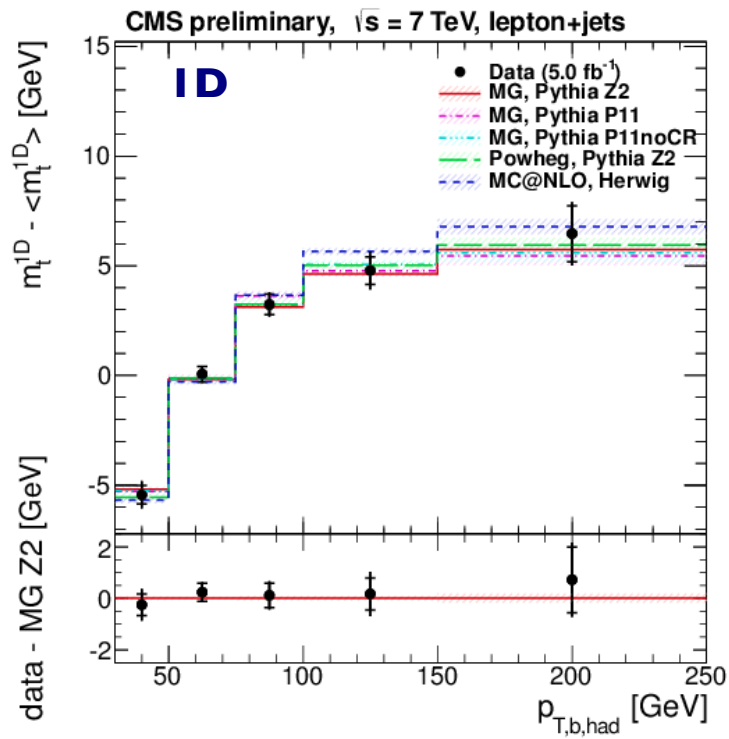
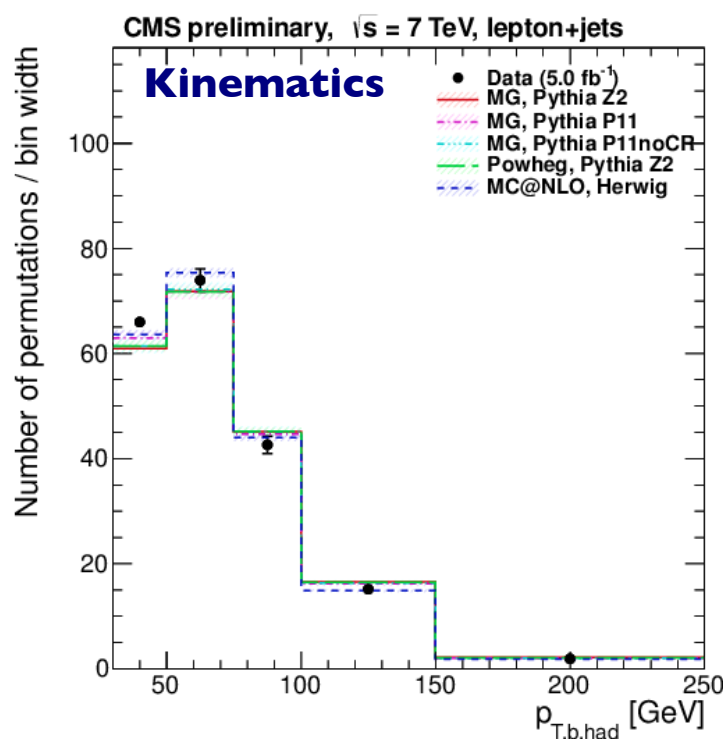


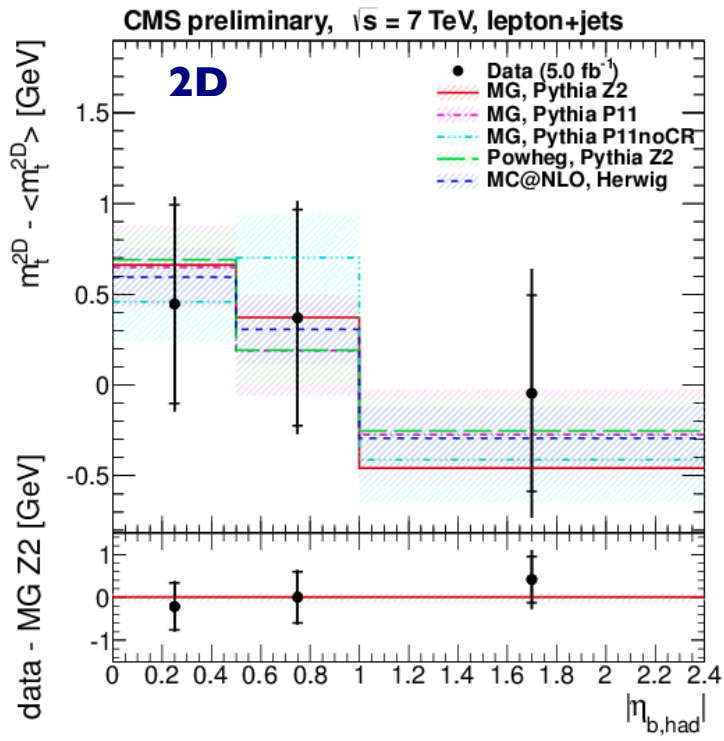
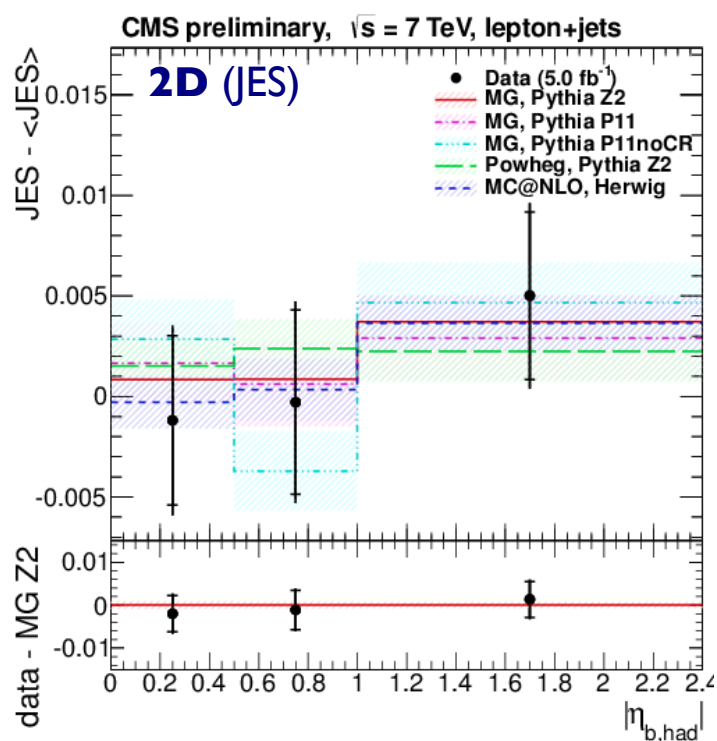
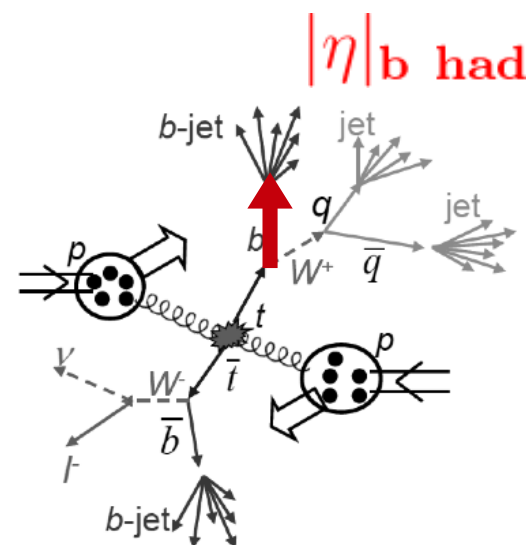
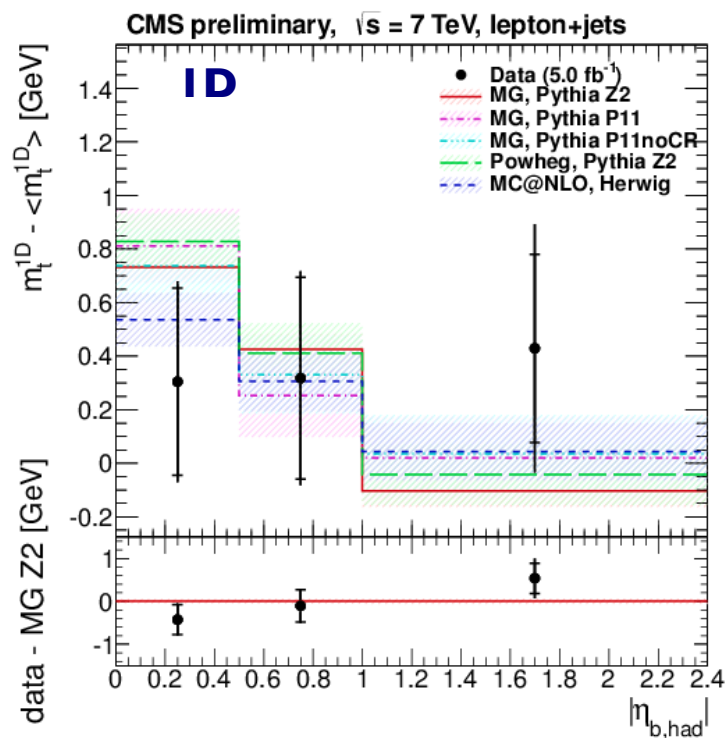
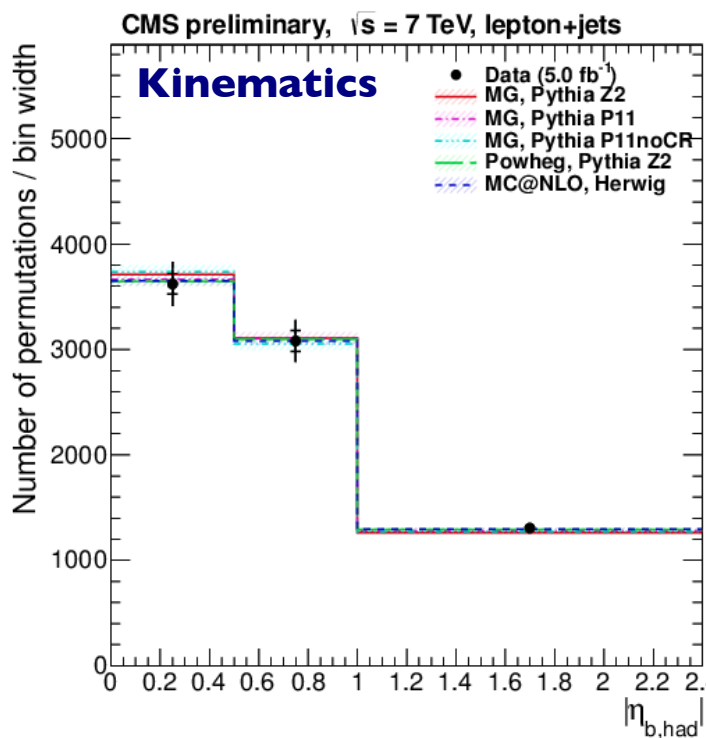


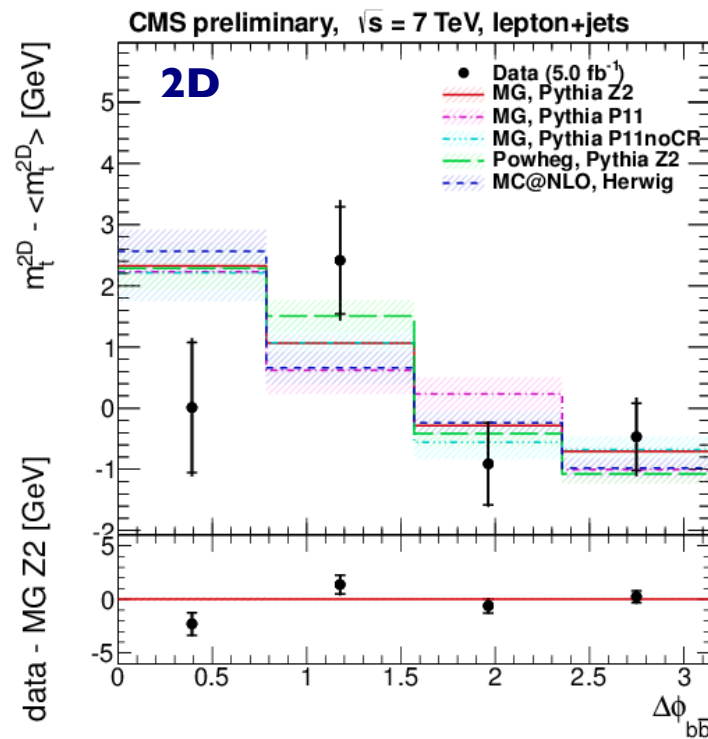
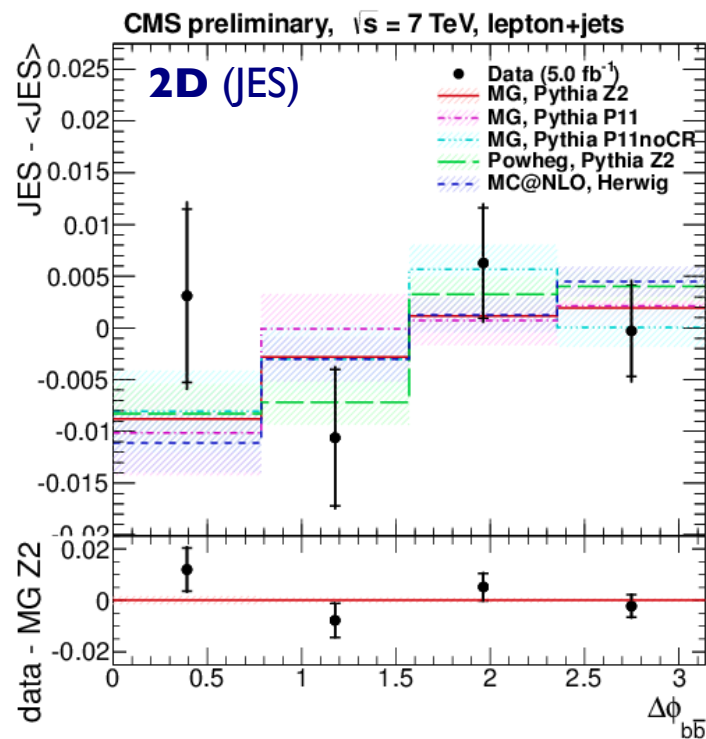
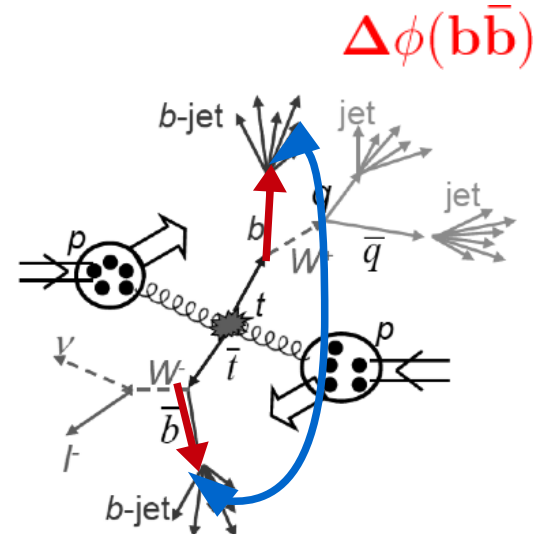
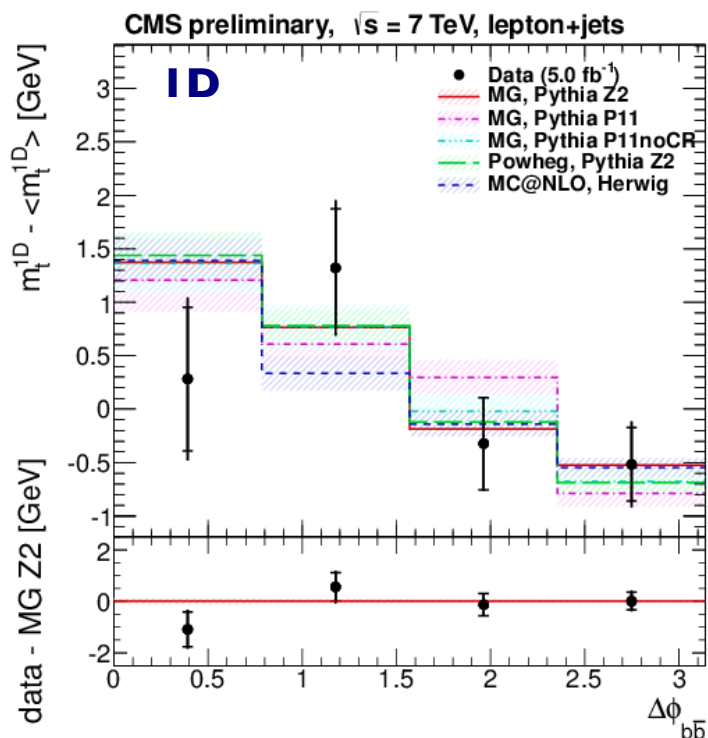
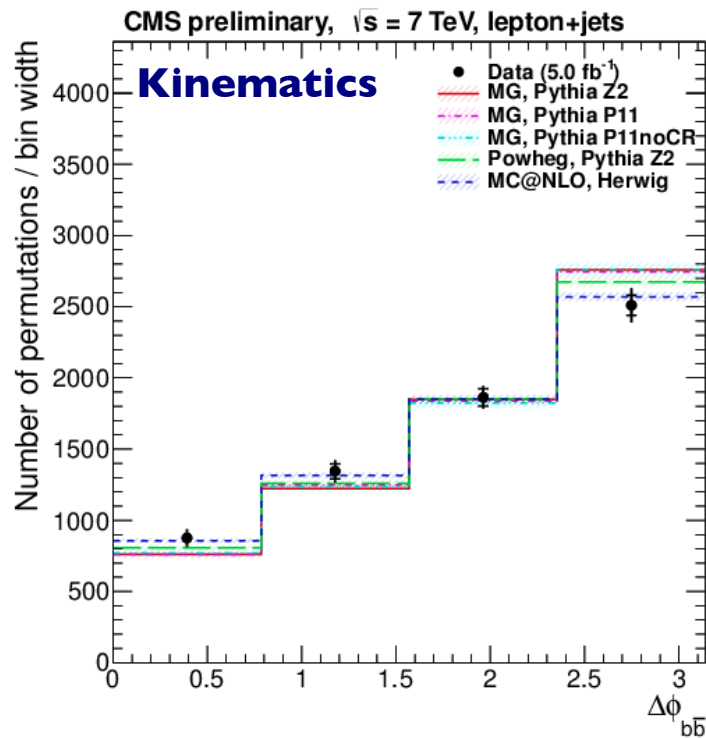














# Average $p_T$ per particle

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