

# Top Modelling Systematic Uncertainty in Top Mass Measurements

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- MC generator systematics
- Additional radiation from  $t\bar{t}$  system
- Parton Density function in ME
- Parton shower and fragmentation
- b-fragmentation

# Recent measurements

## CMS 2012

**l+jets** JHEP 12 (2012) 105

kinematic fit to reconstruct  $M_{\text{top}}$

ideogram method:

Likelihood function to test compatibility of event kinematics with top decay hypothesis

all good permutations are used

2d fit  $M_{\text{top}}$  and JSF

**dilepton** EPJ C 72 (2012) 220

matrix element weighting techniques to reconstruct  $M_{\text{top}}$

probability the  $t\bar{t}$  kinematics fulfils given mass hypothesis

best mass hypothesis is taken

**fully hadronic** EPJ C 74 (2012) 2758

1d ideogram method  $M_{\text{top}}$  and JSF

## CMS 2014

**l+jets** TOP-14-001

Following closely techniques in CMS 2012 l+jets

## ATLAS 2013

**l+jets** ATLAS-CONF-2013-046

kin. fit to reconstructed  $M_{\text{top}}$

template method

2d fit  $M_{\text{top}}$ , JSF exploiting  $M_W$  constrain

3d fit  $M_{\text{top}}$ , JSF and bJSF

(relative b-to-light JSF)

**dilepton** ATLAS-CONF-2013-077

kinematic fit to reconstruct mass

between lepton and b-quark from one top

1d template  $M_{\text{lb}}$

# Evaluation of Ttbar modelling systematics

## CMS

- **Radiation**  
Renormalisation and factorisation scale changed by factor of 2 in Madgraph+Pythia  
  
ME-PS matching threshold in Madgraph varied from from default 20 GeV by factor of 2
- **MC generator**  
Dilepton: MadGraph vs Powheg  
  
For 2014 l+jets:
  - MadGraph vs Powheg
  - $p_{T_{top}}$  reweighting
- **PDF**  
Based on CTEQ6,6  
For 2014 measurement: PDF4LHC prescription
- **Choice parton shower model and fragmentation**  
Included in jet response uncertainty  
b-fragmentation modelling varied

## ATLAS

- **Radiation**  
ISR/FSR PS starting scale changed by factor of 2 in ACERMC+Pythia  
  
Radiation systematics based on ALPGEN not yet used in top mass analysis
- **MC generator**  
MC@NLO+Herwig vs Powheg+Herwig (very different jet multiplicities, Alpgen does not contain top width)
- **PDF**  
based on CT10
- **Choice parton shower model and fragmentation**  
Also included in jet response uncertainty, but would like to cover other effects (parton->jet) evaluate, e.g. Powheg+Pythia vs Powheg+Herwig

# Constrains on additional radiation systematics in ATLAS

Take pragmatic approach: tune MCs to measured observables sensitive to radiations

Jet gap fraction measurement ATLAS EPJ C72 (2012) 2043

Dilepton channel with two b-tags

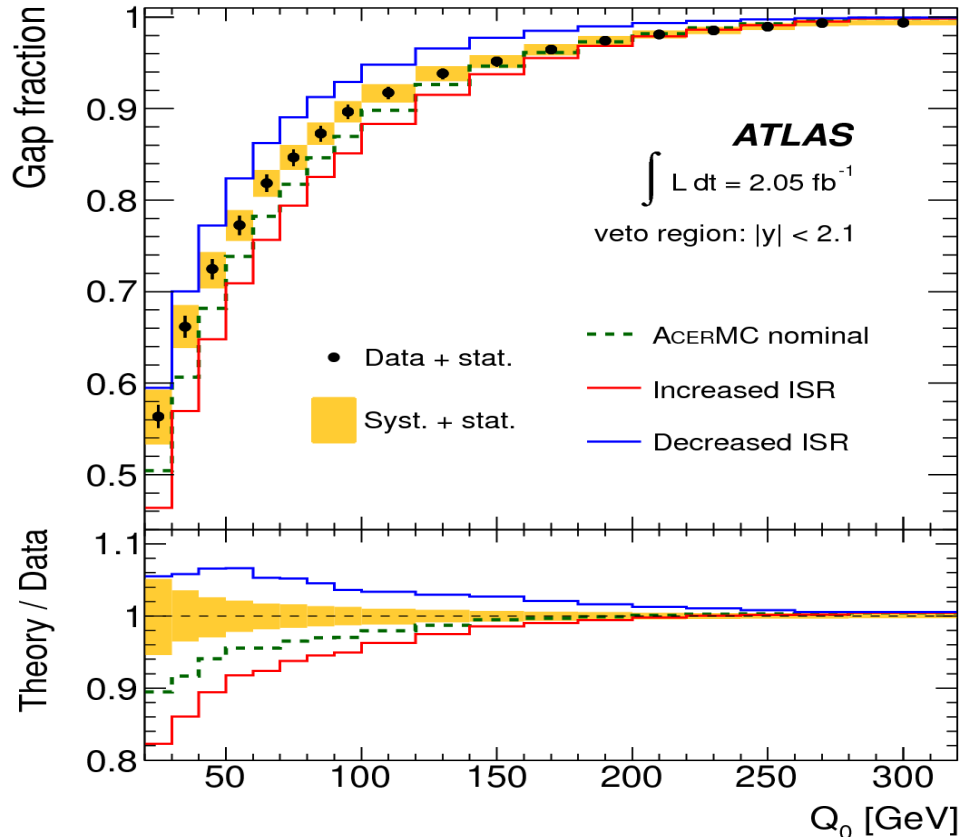
Fraction of events that do not have additional central jet above a pt-cut

See more details in

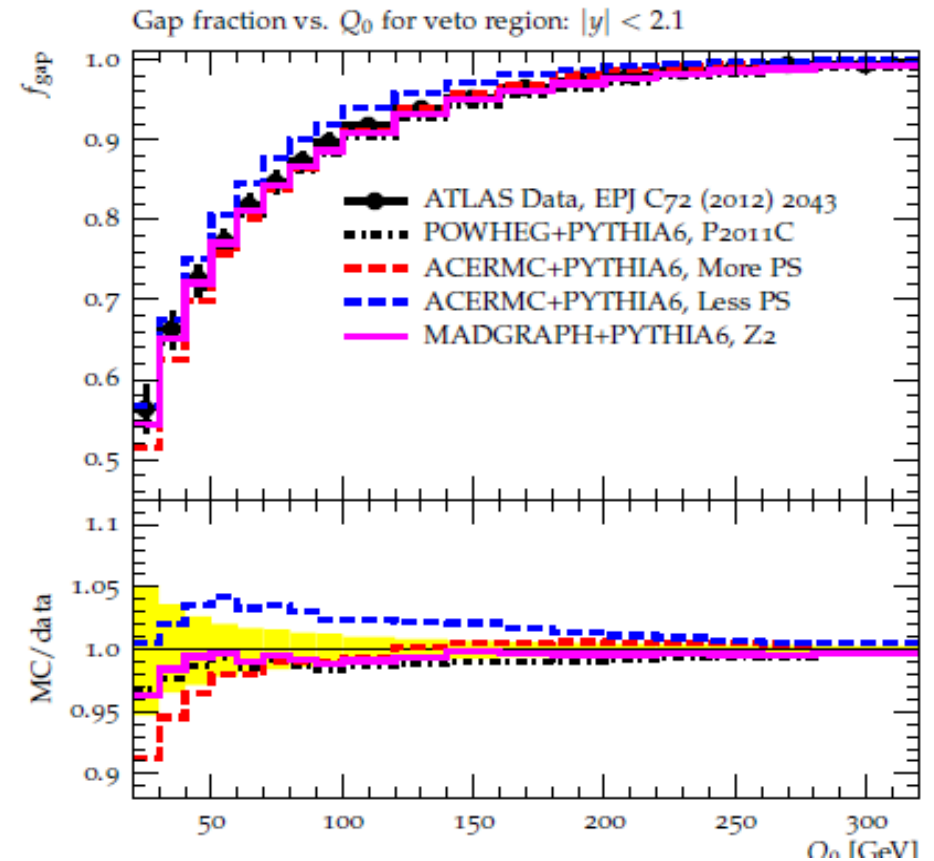
Liza Mijovic

ATLAS-PHYS-PUB-2014-005

Settings estimated before measurement



After tuning



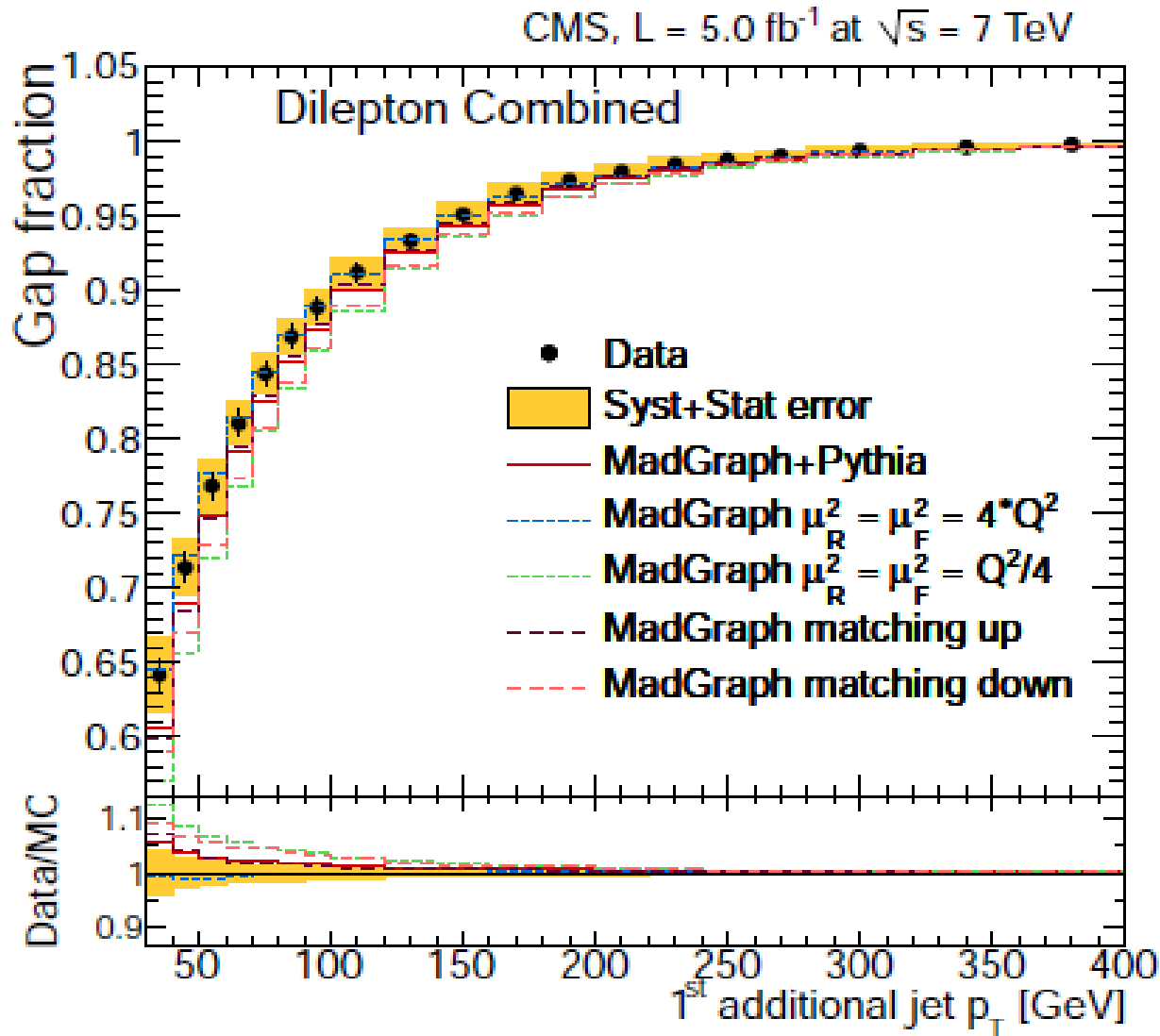
Reduction of systematics by tuning ISR/FSR parameter in ACERMC (see back-up for details)

Central CMS MC Madgraph+Pythia+Z2 tune describes ATLAS data well

# Constrains on additional radiation systematics in CMS

Variation inspired by theory, show a posteriori consistency with data (arXiv:1404.3171)

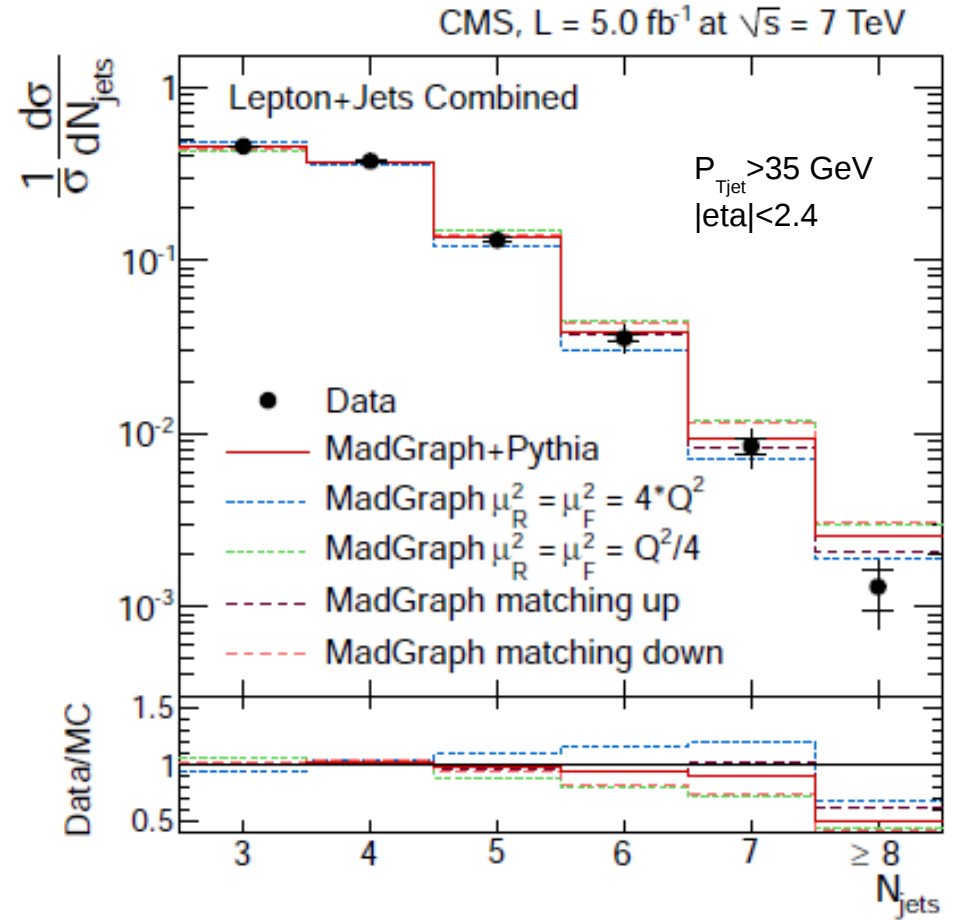
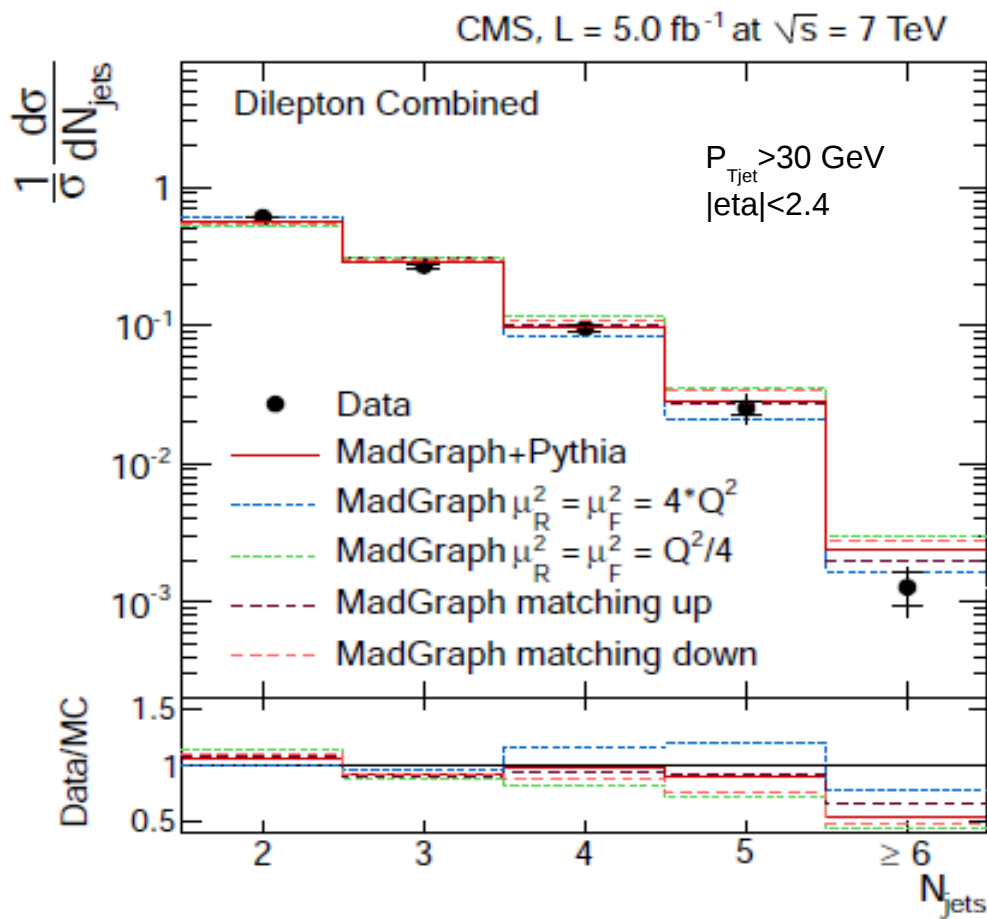
Renormalisation and factorisation scale changed by factor of 2 in Madgraph (LO multi-leg)  
ME-PS matching threshold in Madgraph varied from from default 20 GeV by factor of 2



Note, inverted ratio with respect to figures on previous slide

# Constraints on radiation systematics – Jet multiplicity

Jet multiplicity in dilepton and l+jet events (arXiv:1404.3171)



Data covered by systematics variations in MadGraph

# Radiation systematics

Uncertainties in MeV

Number in () provided for combination

Channel/Method	CMS		ATLAS	
	2012 standard	2014 standard	2013 standard	2013 3D
I+jets				
PDF	70	90	90	170
$\mu_r$ and $\mu_{fac}$	240	$120 \pm 130$		
ME-PS Matching	180	$150 \pm 130$		
AcerMC ISR/FSR			960	450
ME-generator	(20)	$230 \pm 140$	360	190

According to measurement sensitive to radiation, ATLAS and CMS variation should have similar effect  
Effect on top mass can depend on measurement techniques

ACERMC variations make much larger effect in ATLAS 2D measurement than CMS 2D

ATLAS 3D measurement gives reduced radiation systematics

Large reduction of radiation systematics in new CMS measurement  
(reduced statistical uncertainties ?)

Large statistical uncertainties in systematics uncertainty (as evaluated by new CMS)

# Radiation systematics

Uncertainties in MeV

Number is () provided for combination

Number with \* not included (max taken)

Channel/Method	CMS		ATLAS	
	2012 standard	2014 standard	2013 standard	2013 3D
<b>l+jets</b>				
PDF	70	90	90	170
$\mu_r$ and $\mu_{fac}$	240	$120 \pm 130$		
ME-PS Matching	180	$150 \pm 130$		
AcerMC ISR/FSR			960	450
ME-generator	(20)	$230 \pm 140$	360	190
<b>dilepton</b>				
PDF	90		120	
$\mu_r$ and $\mu_{fac}$	550		200*	
ME-PS Matching	190			
ME-generator	40		140	
AcerMC ISR/FSR			370	
<b>hadronic</b>				
PDF	60			
$\mu_r$ and $\mu_{fac}$	$220 \pm 340$			
ME-PS Matching	$240 \pm 340$			
ME-generator	(190)			
AcerMC ISR/FSR				

Quoted is  
1d method as in  
combination



# Treatment of statistical uncertainties in systematics evaluations

From CMS, EPJ C74 (2014) 2758

Table 2: Overview of systematic uncertainties. The total is defined by adding in quadrature the contributions from all sources, by choosing for each the larger of the estimated shift or its statistical uncertainty, as indicated by the bold script.

	1D analysis	2D analysis	
	$\delta_{m_t}$ (GeV)	$\delta_{m_t}$ (GeV)	$\delta_{\text{JES}}$
Fit calibration	<b>0.13</b>	<b>0.14</b>	<b>0.001</b>
Jet energy scale	$0.97 \pm 0.06$	$0.09 \pm 0.10$	$0.002 \pm 0.001$
b-JES	$0.49 \pm 0.06$	$0.52 \pm 0.10$	$0.001 \pm 0.001$
Jet energy resolution	$0.15 \pm 0.06$	$0.13 \pm 0.10$	$0.003 \pm 0.001$
b tagging	$0.05 \pm 0.06$	$0.04 \pm 0.10$	$0.001 \pm 0.001$
Trigger	$0.24 \pm 0.06$	$0.26 \pm 0.10$	$0.006 \pm 0.001$
Pileup	$0.05 \pm 0.06$	$0.09 \pm 0.10$	$0.001 \pm 0.001$
Parton distribution functions	$0.03 \pm 0.06$	$0.07 \pm 0.10$	$0.001 \pm 0.001$
Renormalization and factorization scale	$0.08 \pm 0.22$	$0.31 \pm 0.34$	$0.005 \pm 0.003$
ME-PS matching threshold	$0.24 \pm 0.22$	$0.29 \pm 0.34$	$0.001 \pm 0.003$
Underlying event	$0.20 \pm 0.12$	$0.42 \pm 0.20$	$0.004 \pm 0.002$
Color reconnection effects	$0.04 \pm 0.15$	$0.58 \pm 0.25$	$0.006 \pm 0.002$
Multijet background	$0.13 \pm 0.06$	$0.60 \pm 0.10$	$0.006 \pm 0.001$
Total	1.21	1.23	0.013

Need to increase MC statistics for systematics variation samples, if possible  
 Need to learn how to reduce statistical fluctuations on systematics uncertainties  
 Taking maximum of statistical uncertainty and mean not the only possibility

# Hadronisation systematics

## CMS 2011

### b-JES:

b-jet response in between light-quark/gluon response  
Therefore take Pythia/Herwig++ for light quark/gluons  
as b-jet uncertainty

## CMS 2014

### b-JES

Compare Pythia/Herwig++ for each jet flavour  
For light-quarks, gluons and b-quark uncertainty is evaluated  
separately and added in quadrature

### b-fragmentation

Bowler-Lund fragmentation re-tuned to ALEPH and DELPHI data  
Difference between this retune and Pythia Z2 tune is uncertainty

### Semi-leptonic B hadron decays

Semi-leptonic branching varied by -0.45 and +0.77% for  
 $B^0$  and  $B^{+}$  Hadrons (from PDG)

Quoted separately and not included in final result  
MC@NLO+Herwig vs Powheg+Pythia Z2 tune

- approach avoids possible double counting  
when changing pythia/herwig
- detector response on particle jet
  - b-fragmentation
  - $p_{Ttop}$  modelling

## ATLAS

### b-JES

- Dedicated b-JES based on MC  
Pythia/Herwig  
b-fragmentation function  
Pythia nominal/tuned Bowler-Lund  
(tuned to LEP data)
- Validation with data in situ  
(limited precision)

Parton shower and fragmentation  
effects on  $T_{b\bar{b}}$  event topology  
exchange Pythia/Herwig  
to cover:

- choice of parton shower
- hadronisation effect  
(string vs cluster)
- underlying event
- b-fragmentation
- B-Hadron decay tables

- possible double counting  
with other systematics:
- effect of detector response on  
particle jet → detector jet
  - underlying event
  - b-fragmentation

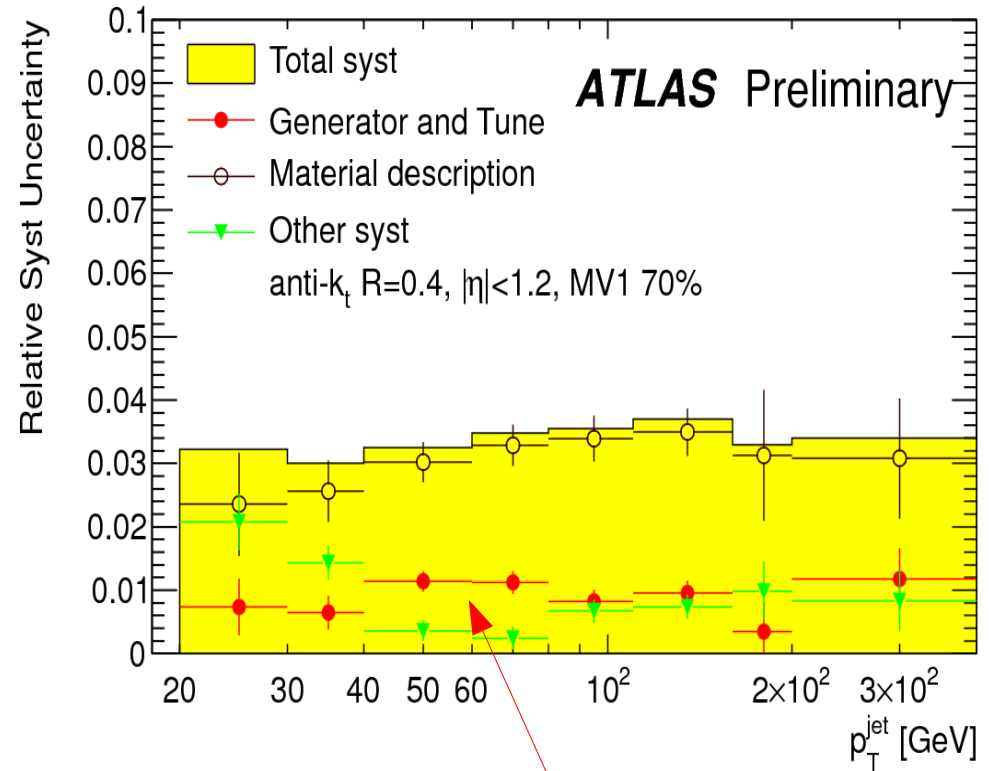
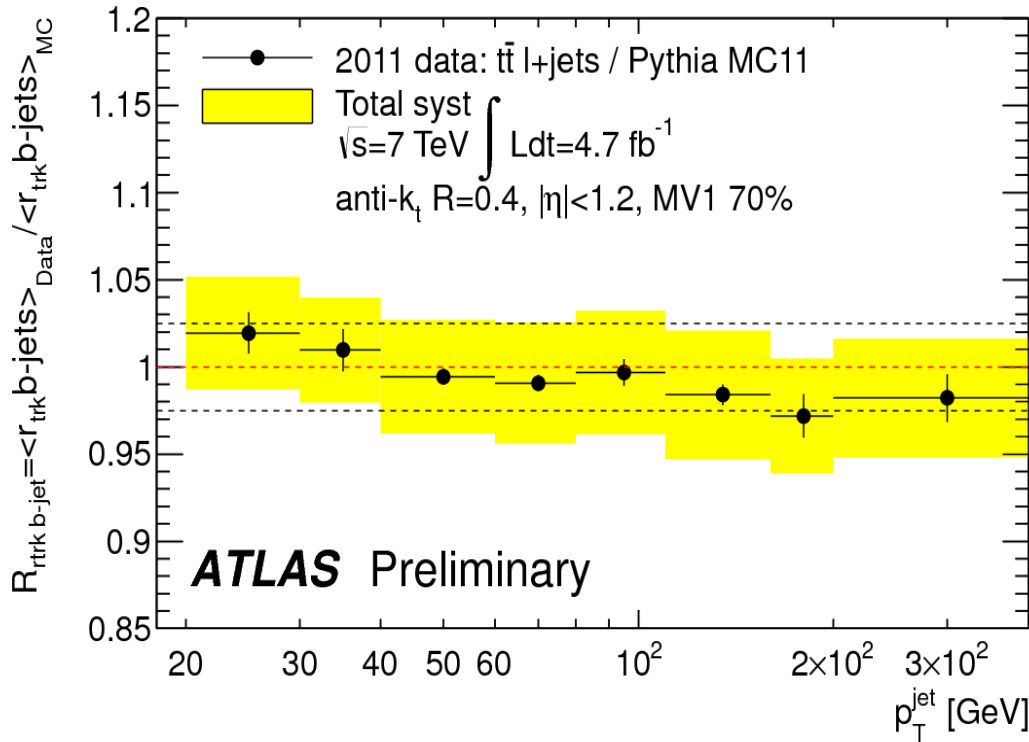
# b-Jet response validation in ATLAS data

Study jet response comparing calorimeter to track jets in  $t\bar{t}$  events

$$r_{\text{trk}} = \frac{\sum \vec{p}_T^{\text{track}}}{p_T^{\text{jet}}}$$

compare data to MC

Uncertainty then given by Calo-to-track response in Data/MC for systematic variations



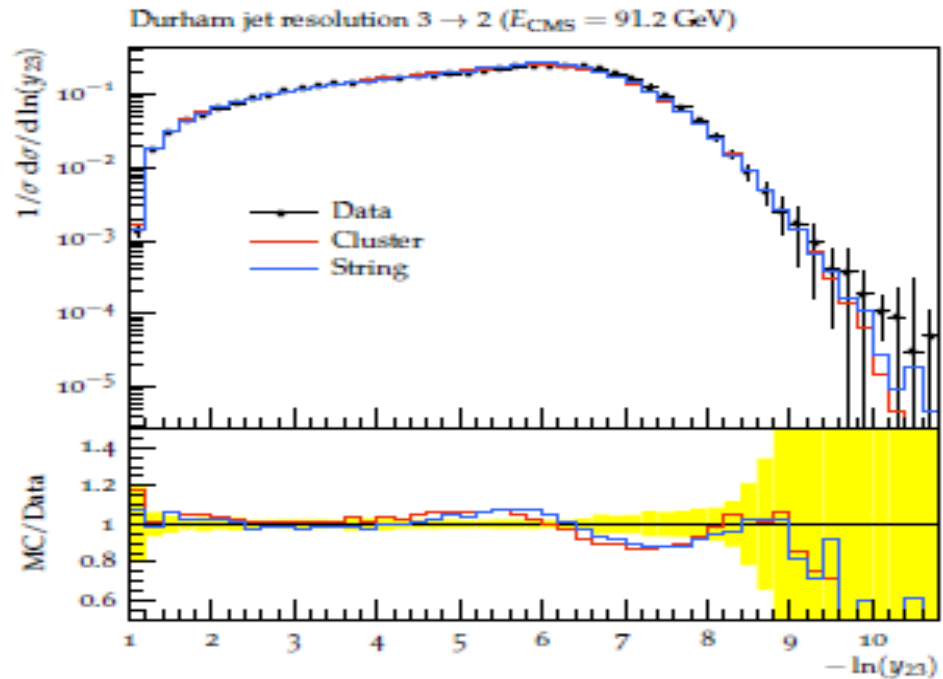
Calo-to-track response ratio well described by Powheg+Pythia  
Difference due to generator and Pythia/Herwig is small !

**Generator and tune**  
Powheg+Herwig vs MC@NLO+Herwig  
Powheg+Herwig vs Powheg+Pythia

# Study of cluster vs string fragmentation in Sherpa

Particle-level study using Sherpa 2.1:

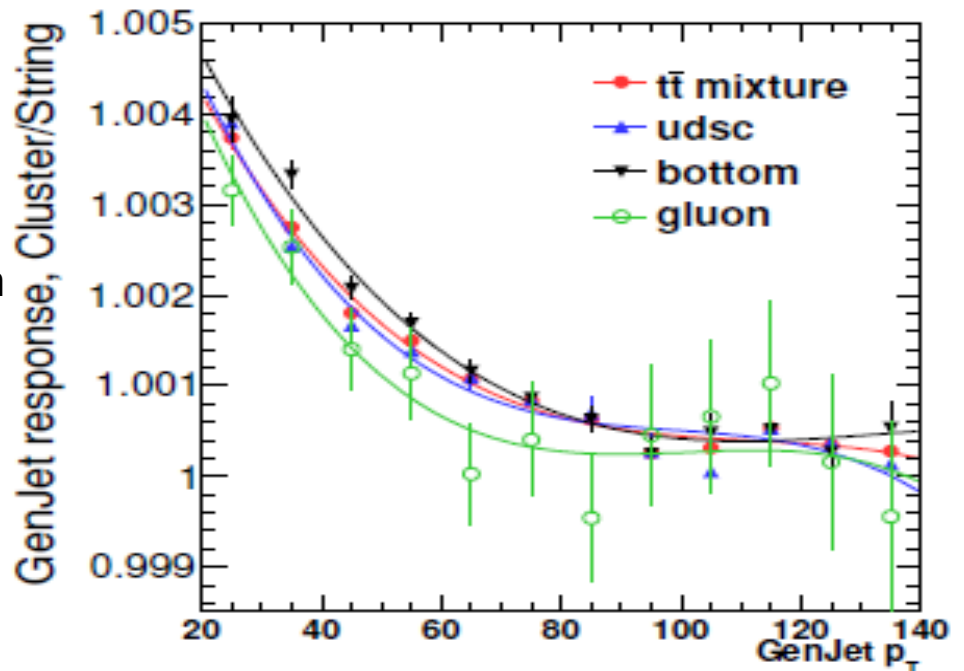
- use same pT-ordered parton shower (CShower++)
- exchange
  - in-built sherpa cluster fragmentation (AHADIC++, Hadrons++)
  - Pythia 6.4.18 for lund string fragmentation



Validate set-up in  $e^+e^-$  data  
 Shown are differential jet rate at 91.2 GeV  
 (other variables similar quality)

Look at particle jet response with respect to  
 Selected parton for string and cluster fragmentation

Difference between cluster/string model  
 and jet flavours on jet response  
 Are very small



# Jet shape

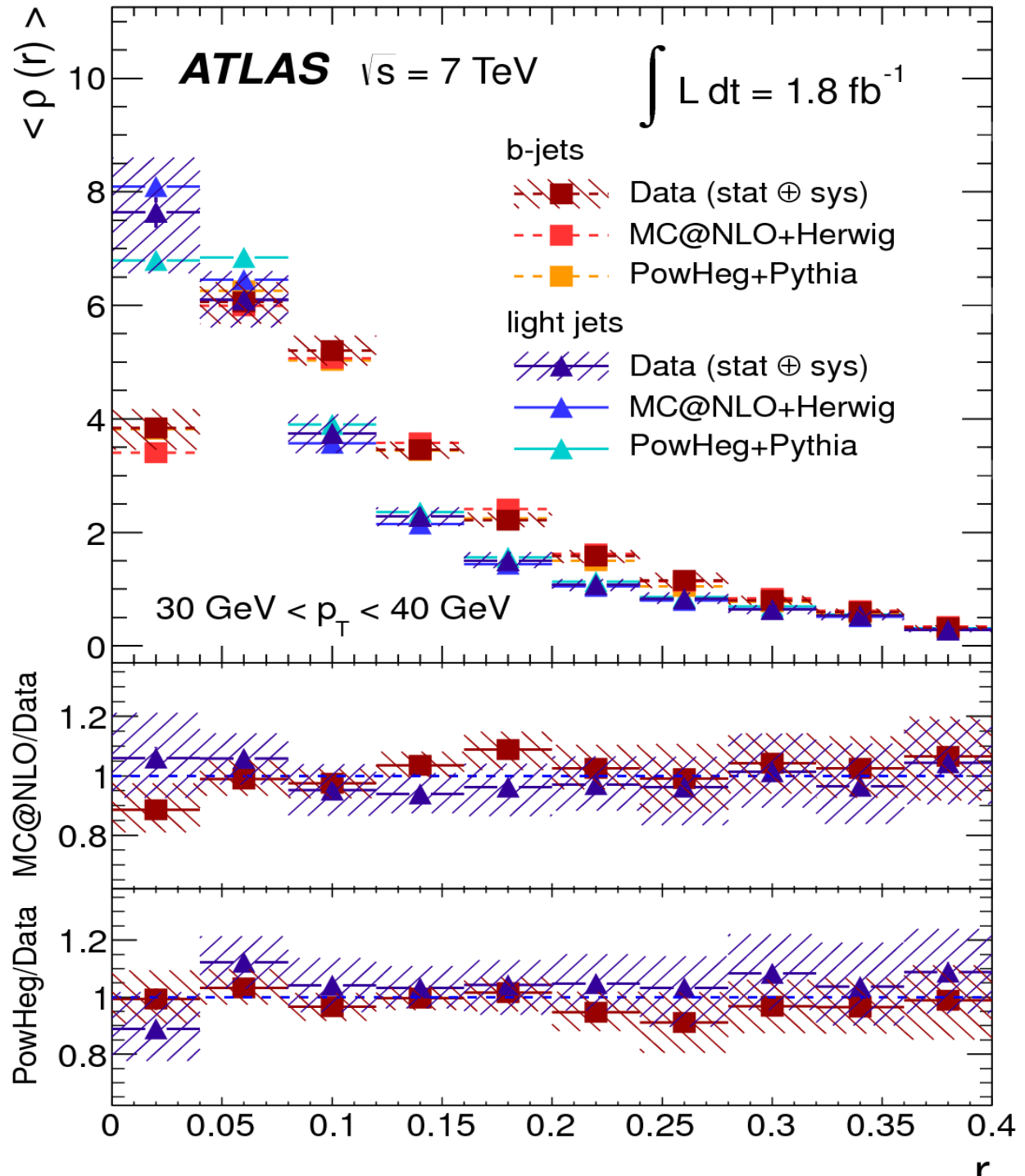
Measurement of differential jet shape in  $t\bar{t}$  events (EPJ C73 (2013) 2676)

Jet shape:  
Transverse energy in annulus around jet axis

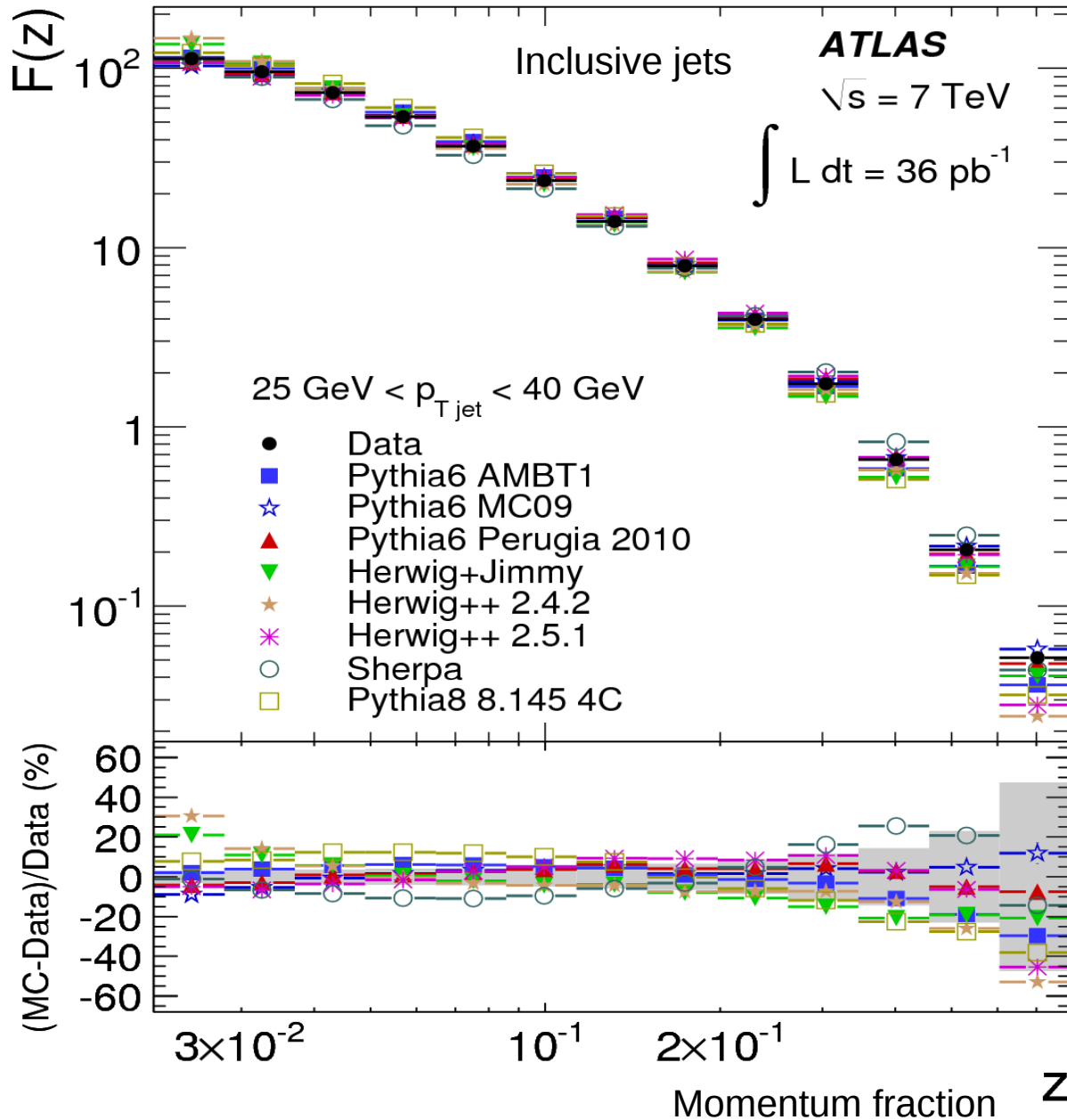
$$\rho(r) = \frac{1}{\Delta r} \frac{p_T(r - \Delta r/2, r + \Delta r/2)}{p_T(0, R)}$$

B-jets are wider than light-quark jets from W-decay

Both Powheg+Pythia and MC@NLO+Herwig describe data for light jets from W-decay and b-jets



# Jet fragmentation



Fragmentation function

$$F(z, p_{T \text{ jet}}) \equiv \frac{1}{N_{\text{jet}}} \frac{dN_{ch}}{dz},$$

Charged particle  
Momentum fraction

$$z = \frac{p_{\text{jet}} \cdot p_{ch}}{|p_{\text{jet}}|^2},$$

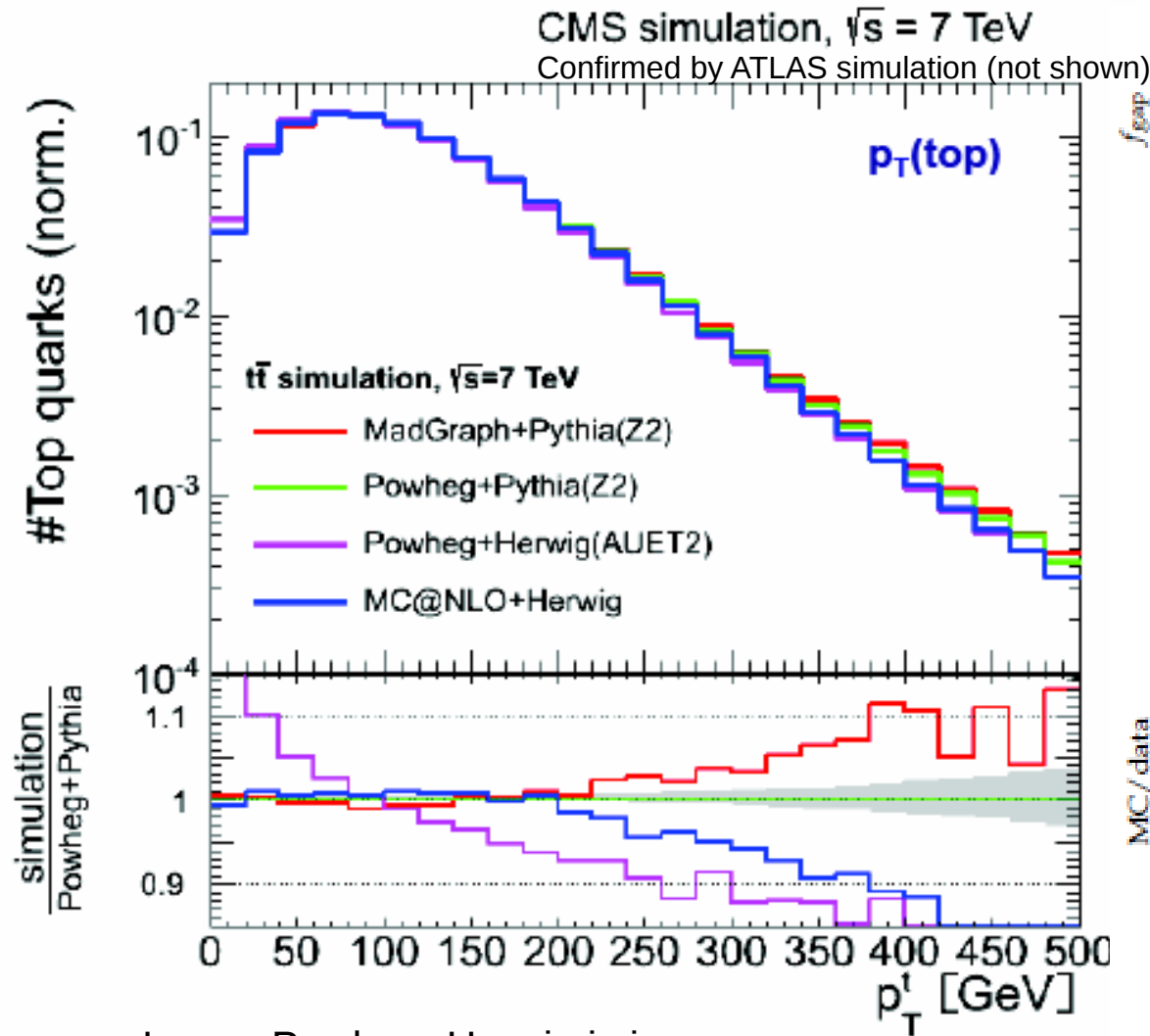
Within measurement precision  
present MCs describe data

Herwig is worse, but still ok

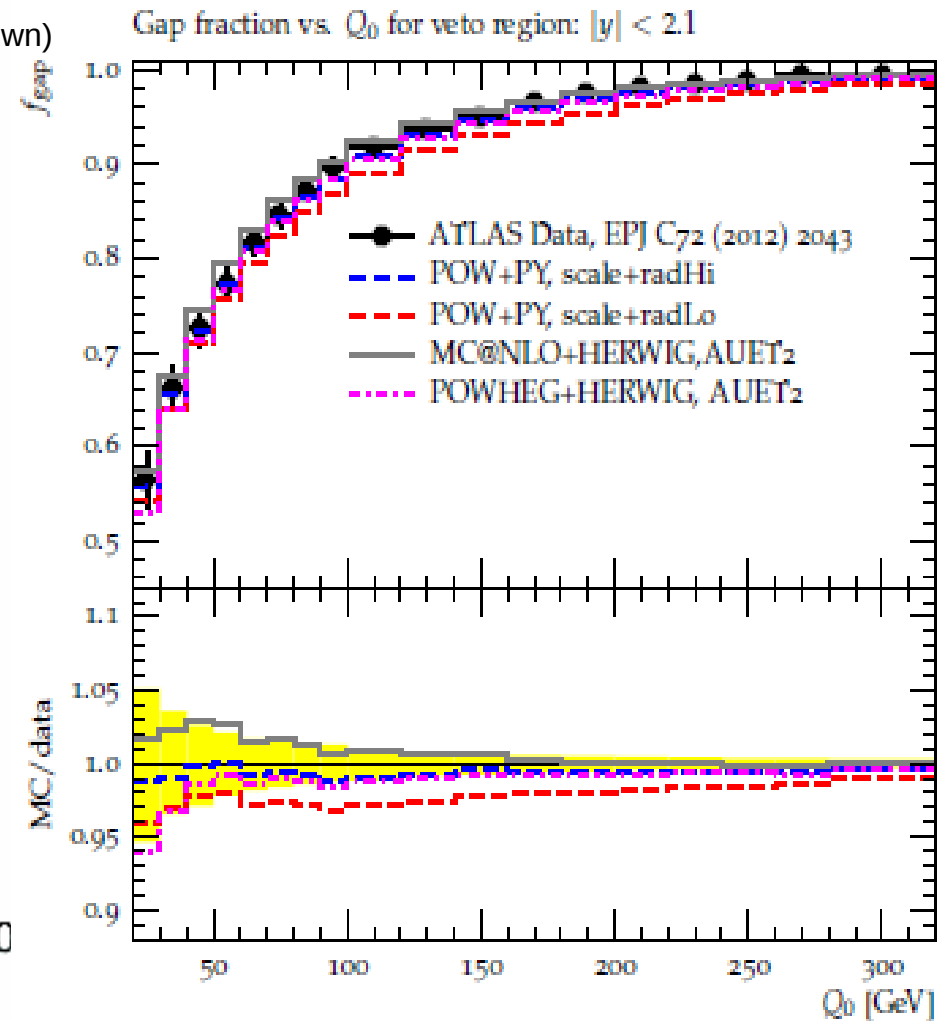
-> would be interesting to  
have this measurement for  
b-jets

# Ttbar event topology for Pythia Herwig parton showers

When switching from Pythia to Herwig in Powheg, changes in the ttbar event kinematics are observed e.g. shown by M. Aldaya/F. Spano in last TopLHC meeting



In  $p_{T\text{top}}$  Powheg+Herwig is in better agreement with data (not shown)



Powheg+Herwig describes additional radiation

# Overview of hadronisation systematics

Uncertainties in MeV

Number with () provided for combination, not included in main result

\* not included in main result

Channel/Method	CMS		ATLAS	
	2011 standard	2014 standard	2012 standard	2012 3D
l+jets	(580)	330*	1300	270
dilepton	(760)	-	440	
hadronic	(930)	-	-	-

ATLAS 2D method has large uncertainty due to Pythia/Herwig (1.3 GeV !)

Reduced by 3D method fitting b-JSF relative to light-quark JSF

(at the cost of increasing detector uncertainty since sensitive to pt-dependence of uncertainties)

2011 CMS uncertainties from ATLAS/CMS top mass combination note

Hadronisation uncertainty is sizeable compared to total systematics

(50-90% of total uncertainty depending on channel)

New CMS measurement reduced uncertainty, but still about 50% of total uncertainty

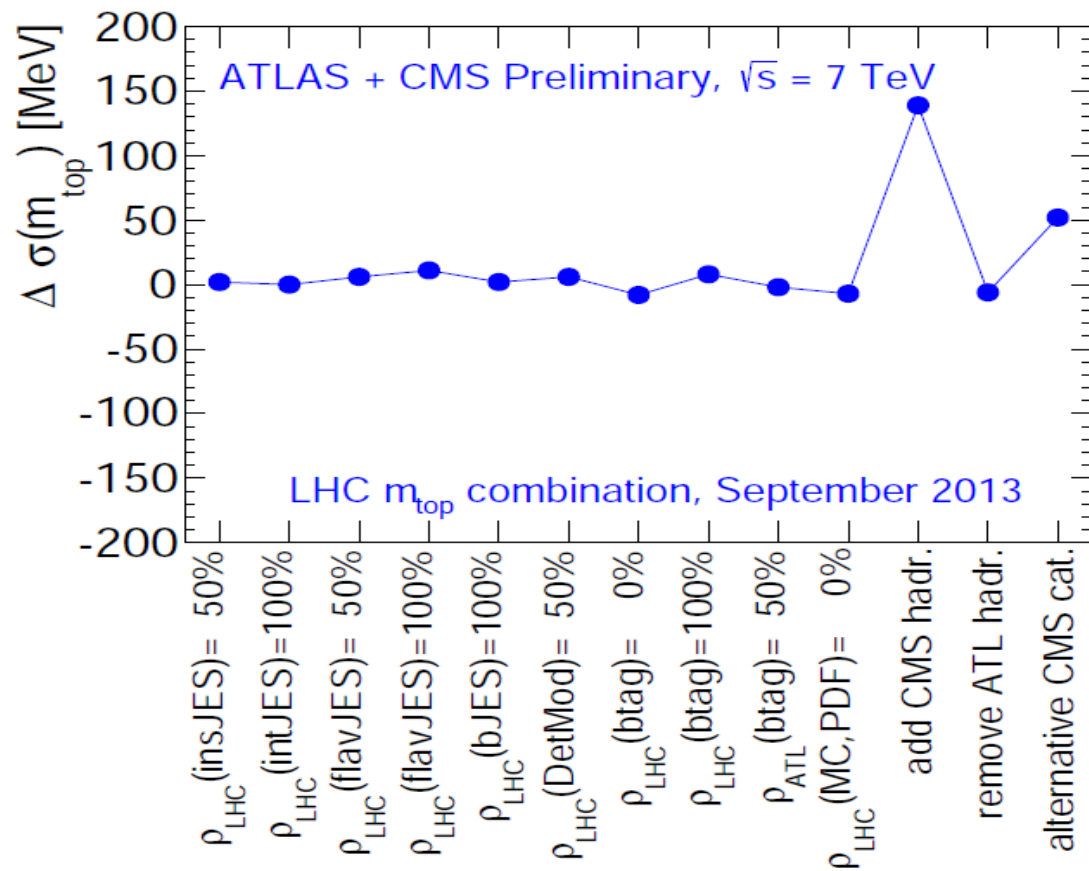
Agreed last year to evaluate double counting between Pythia/Herwig with other systematics, e.g. by re-calibrating jets with Herwig (instead of Pythia) → still ongoing



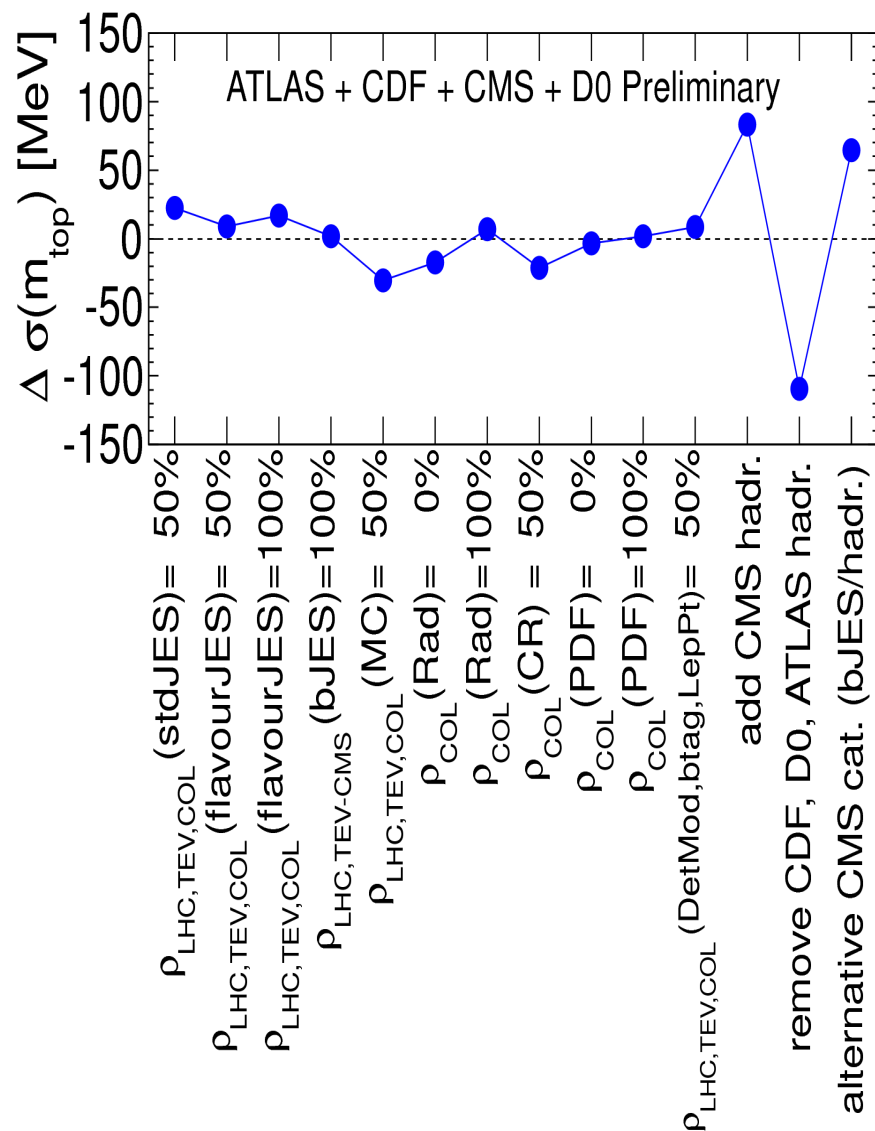
# Effect of hadronisation systematics treatment in combinations

Influence of hadronisation systematics treatment in combinations:

ATLAS/CMS combination ATLAS-CONF-2013-102

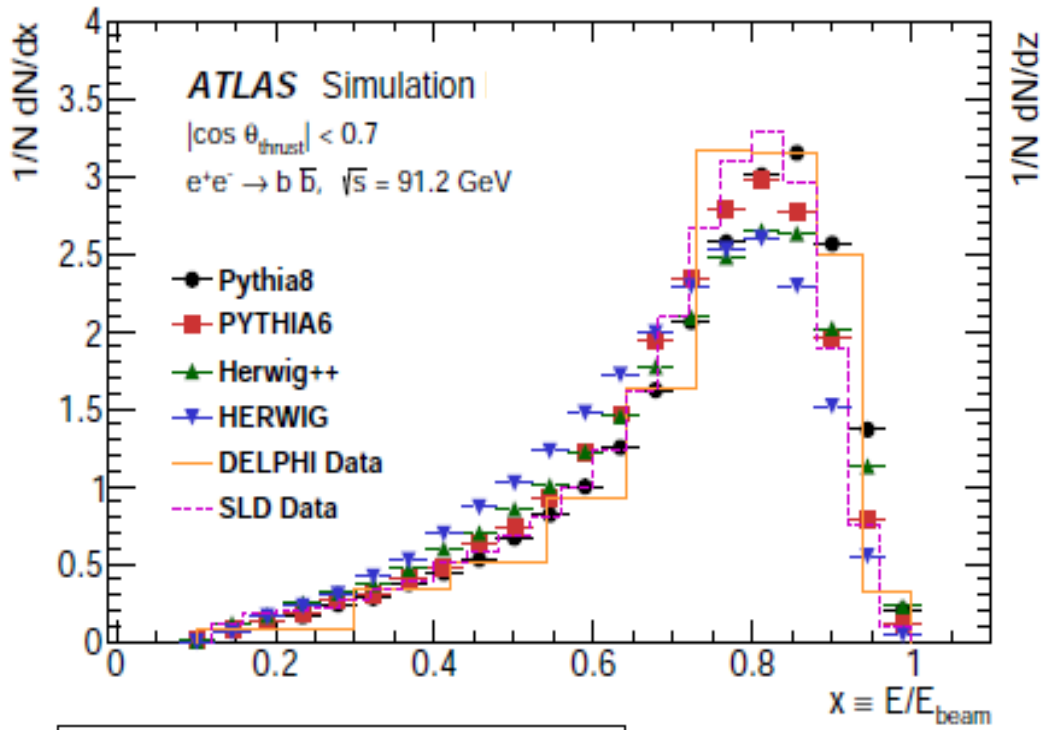


World combination ATLAS-CONF-2014-008



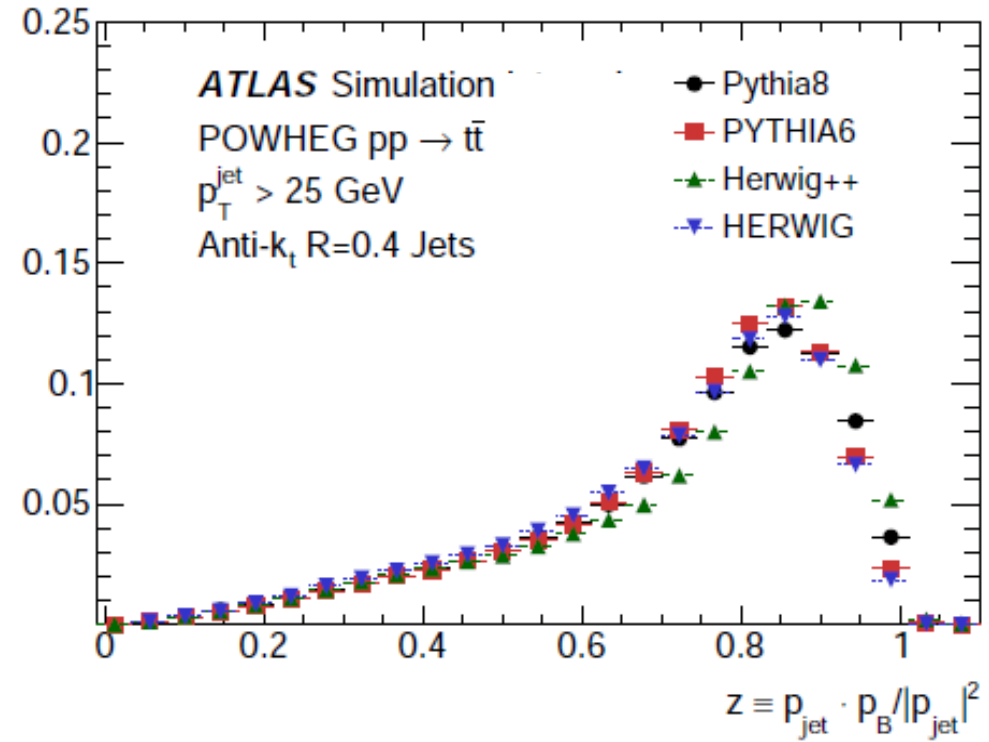
# B-fragmentation

Electron-positron collisions



mean	$E_B/E_{\text{beam}}$
Pythia8	$0.7303 \pm 0.0005$
PYTHIA6	$0.7090 \pm 0.0005$
Herwig++	$0.7012 \pm 0.0006$
HERWIG	$0.6782 \pm 0.0005$
Delphi Data	$0.699 \pm 0.011$
SLD Data	$0.709 \pm 0.005$

Proton-proton ttbar events



Fragmentation function with respect to anti-kt jet  $R=0.4$   $|\eta| < 2.4$   
 Containing B-hadron with  $p_T > 5 \text{ GeV}$

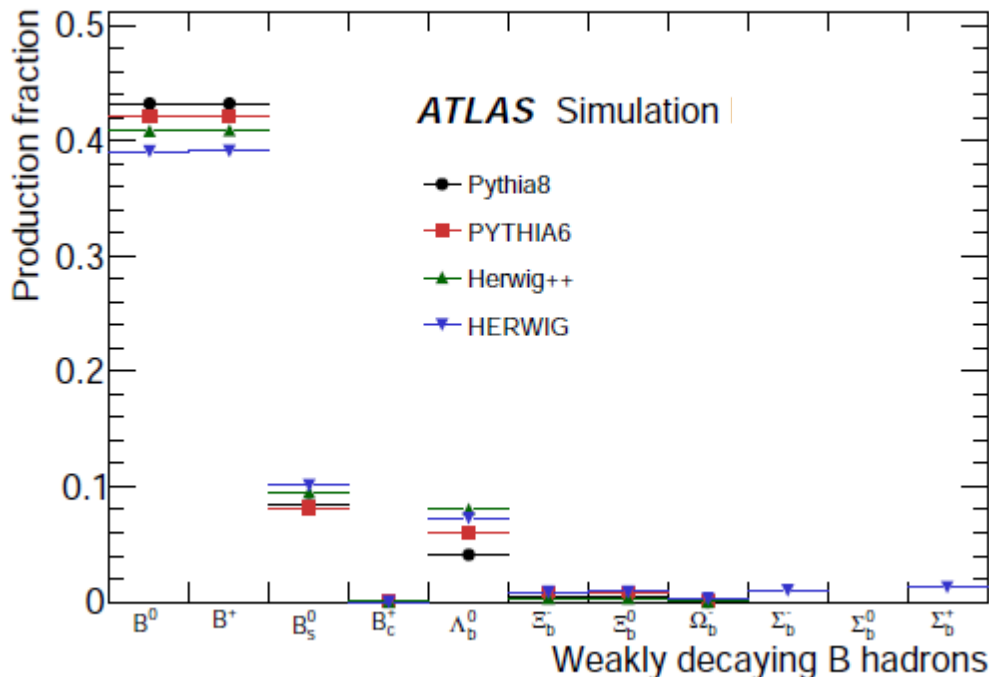
Herwig++ has harder fragmentation

Herwig softer fragmentation in  $e^+e^-$ , but similar to other MCs in proton-proton

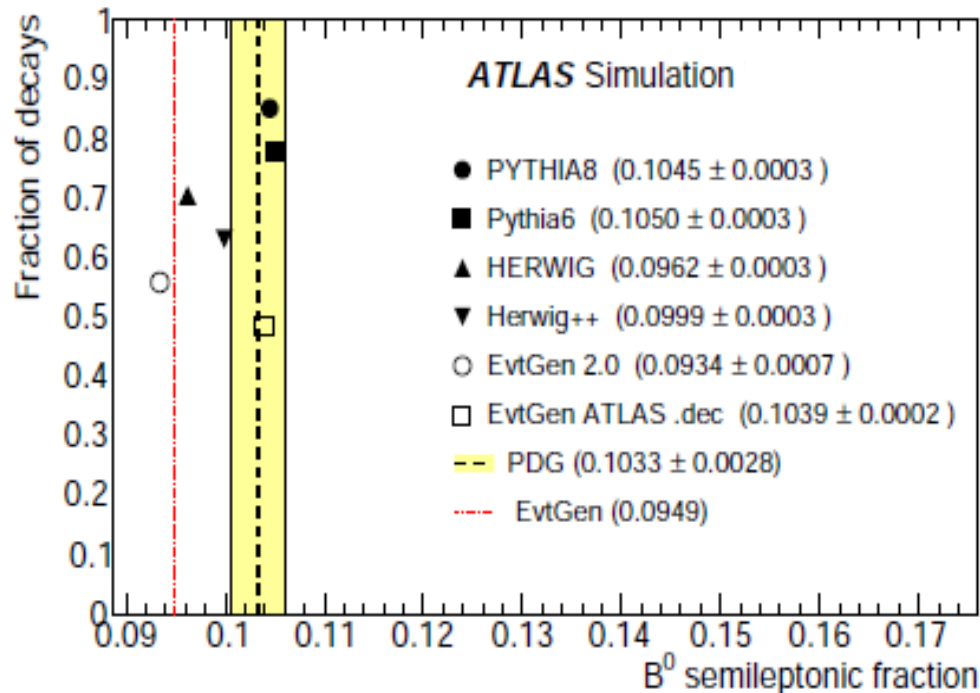
# B-hadron multiplicities and decays

ATLAS started to systematically compare b-fragmentation, B-hadron multiplicities and B-hadron decays (lifetimes, semi-leptonic branching, charged multiplicities) in various MC generators  
 Similar CMS effort presented by M Seidel in November TopLHC meeting

Match any B-Hadrons with  $pt > 5$  GeV to jets and study B-hadron species:



Semi-leptonic decay fractions



Species	Pythia8	PYTHIA6	Herwig++	HERWIG	Reference PDG
$B^+$	43.2	42.1	40.9	39.1	40.2 ± 0.7
$B^0$	43.2	42.2	40.9	39.1	40.2 ± 0.7
$B_s^0$	8.4	8.2	9.5	10.1	10.4 ± 0.6
Baryons	5.1	7.3	8.6	11.7	9.3 ± 1.5

EVTGen commissioning ongoing allows to use same b-fragmentation properties in all MCs and to define dedicated uncertainty

All MCs in reasonable agreement, Pythia8 has low Baryon fraction

# Conclusion

Radiation systematics can be constrained by dedicated measurement (jet multiplicities and fraction of events with additional jet activity)

The variations chosen by ATLAS (ACERMC ISR/FSR or ALPGEN ren&fac scale)  
by CMS (Madgraph ren&fac scale)

Have similar effect on these measurements

The effect on the top mass measurements depends on the techniques

No consensus on treatment of hadronisation systematics

CMS treats this as cross-checks and claims all effects are included in jet energy scale uncertainty and b-fragmentation

ATLAS can not exclude effects on overall event topology (e.g.  $p_{Ttop}$ ) and would like to keep effect on ME+PS merging

Good news is that all numbers are meanwhile available.

The possible double counting on many modelling effects is hard to evaluate  
In my view, all uncertainties should be evaluated  
However, it is not clear, if added in quadrature or taking maximum of various effects is better (also given the large statistical uncertainties)

B-fragmentation needs more attention. Measurements are needed !

# Back-up

# Settings and Samples

## ATLAS settings for radiation systematics

ACERMC + PYTHIA6 AUET2B LessPS and MorePS	ACERMC 3.8 + PARP(67), PARP(64), PARP(72), PARJ(82) variations	PYTHIA6 v6.426	$Q = 2mt$	CTEQ611	AUET2B
ALPGEN + PYTHIA6, P2011	ALPGEN v2.14	PYTHIA6 v6.425	$Q = \sqrt{\sum m_T^2}$ , with $m_T^2 = m^2 + p_T^2$	CTEQ5L	Perugia 2011
ALPGEN as_down,radHi	same settings as ALPGEN + PYTHIA6, P2011 but with ren. scale in ME and PS varied simultaneously by factor 0.5 and UE retune				Perugia 2011 radHi
ALPGEN as_down,radLo	same settings as ALPGEN + PYTHIA6, P2011 but with ren. scale in ME and PS varied simultaneously by factor 2.0 and UE retune				Perugia 2011 radLo

## CMS settings for radiation systematics

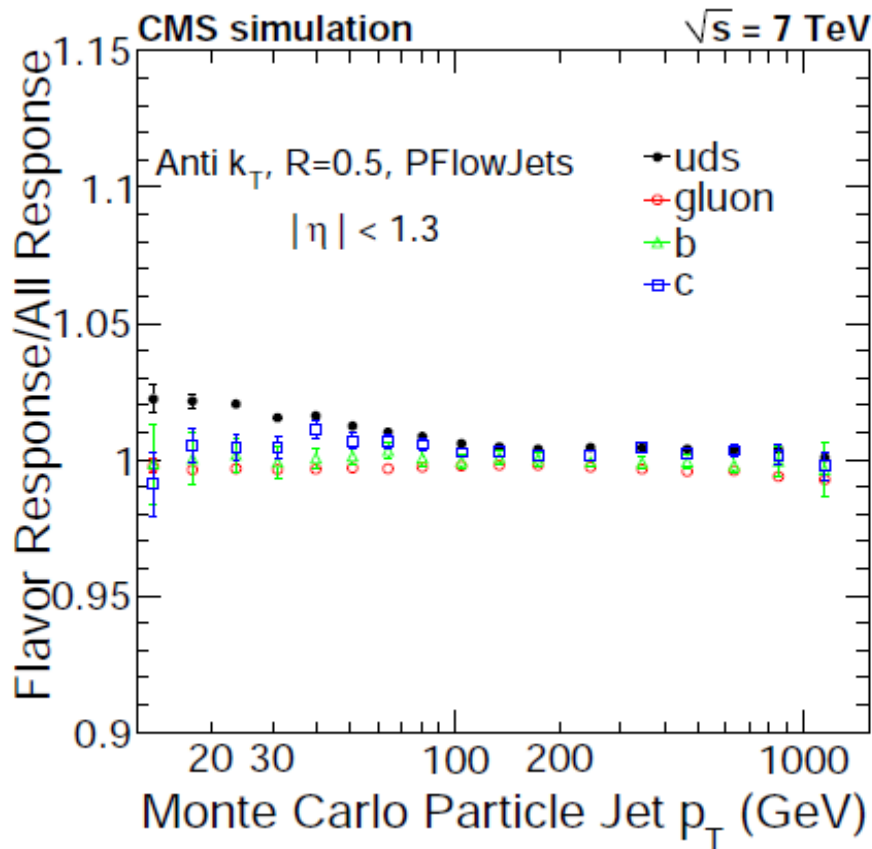
MADGRAPH + PYTHIA6, Z2 (used in 7 TeV analyses)	MADGRAPH v5.1.1.0	PYTHIA6 v6.424	$Q = \sqrt{m_i^2 + \sum p_T^2(jet)}$	CTEQ61	Z2
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	CMS MADGRAPH +PYTHIA6	ATLAS ALPGEN +PYTHIA6	ATLAS ACERMC +PYTHIA6 7 TeV (8 TeV)
<b>nominal sample settings</b>			
FSR: PARP(72)	0.25 GeV	0.26 GeV	0.26 (0.527) GeV
ISR: PARP(64)	1.0	1.0	1.0 (0.68)
PARP(61)	0.25 GeV	0.26 GeV	0.26 (0.192) GeV
ME: alpsfact/ktfac	1.0	1.0	-
<b>Less PS (as_down,radLo) sample settings</b>			
FSR: PARP(72)	0.125 GeV	0.13 GeV	0.11 (0.150) GeV
ISR: PARP(64)	4.0	-	3.50 (4.08)
PARP(61)	-	0.13 GeV	same as nominal
ME: alpsfact/ktfac	2.0	2.0	-
<b>More PS (as_up,radHi) sample settings</b>			
FSR: PARP(72)	0.50 GeV	0.52 GeV	0.37 (0.425) GeV
ISR: PARP(64)	0.25	-	0.90 (1.02)
PARP(61)	-	0.52 GeV	same as nominal
ME: alpsfact/ktfac	0.5	0.5	-

# Detector response to jets in CMS simulation

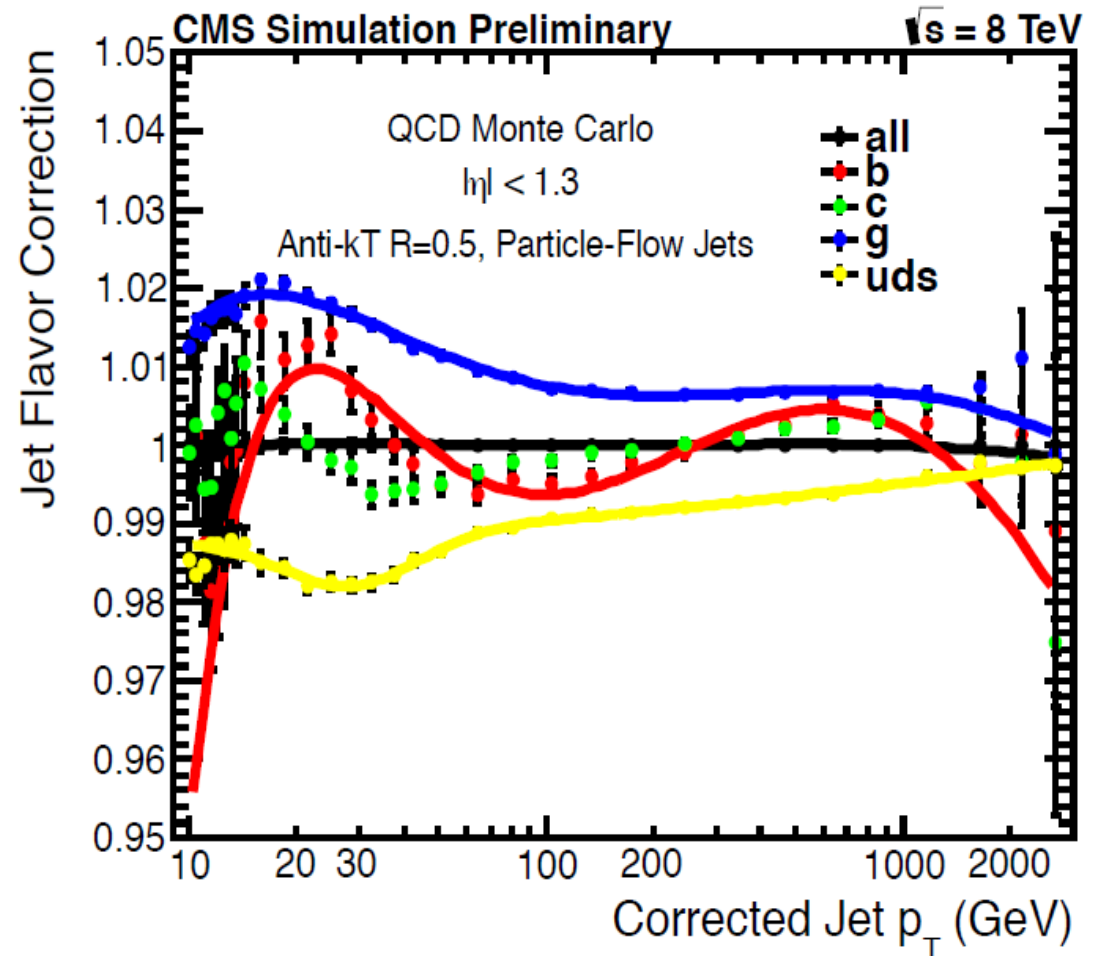
## B-JES: CMS 2011

b-jet response in between light-quark/gluon response  
 taken Pythia/Herwig++ for light quark/gluons as  
 b-jet uncertainty



## B-JES CMS 2014

Compare Pythia/Herwig++ for each jet flavour  
 For light-quarks, gluons and b-quark uncertainty  
 is evaluated separately and added in quadrature

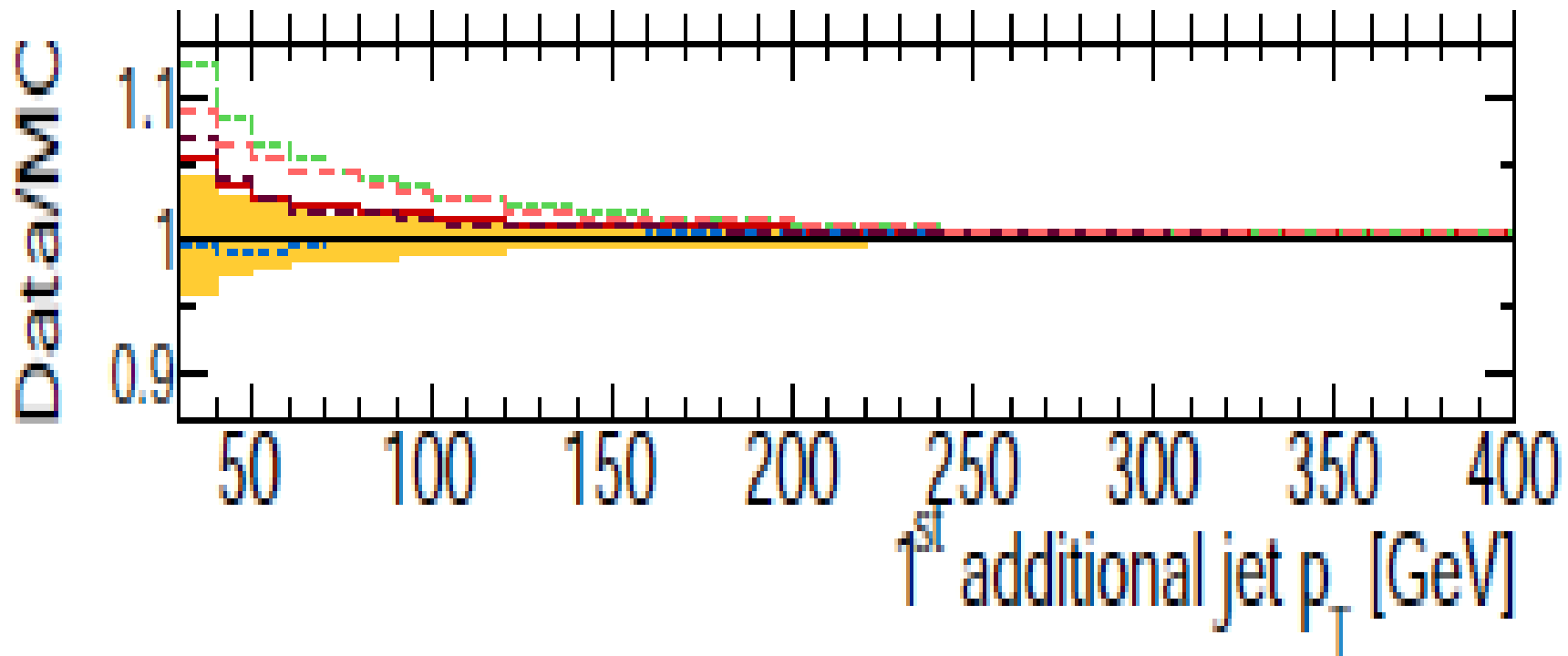


These results are based on Herwig++

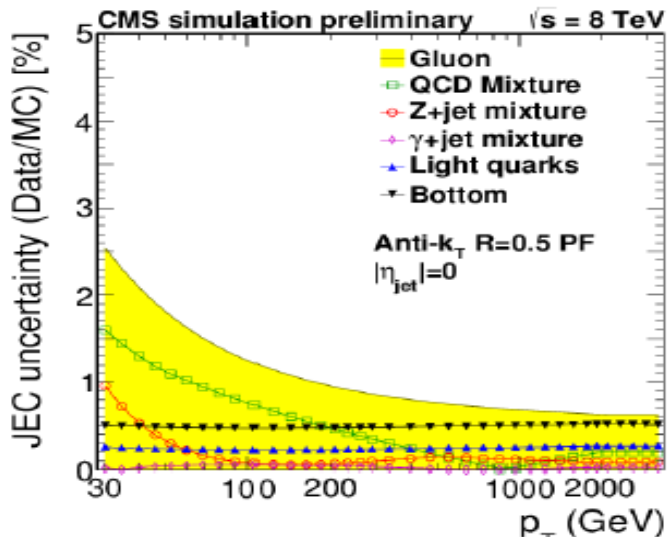
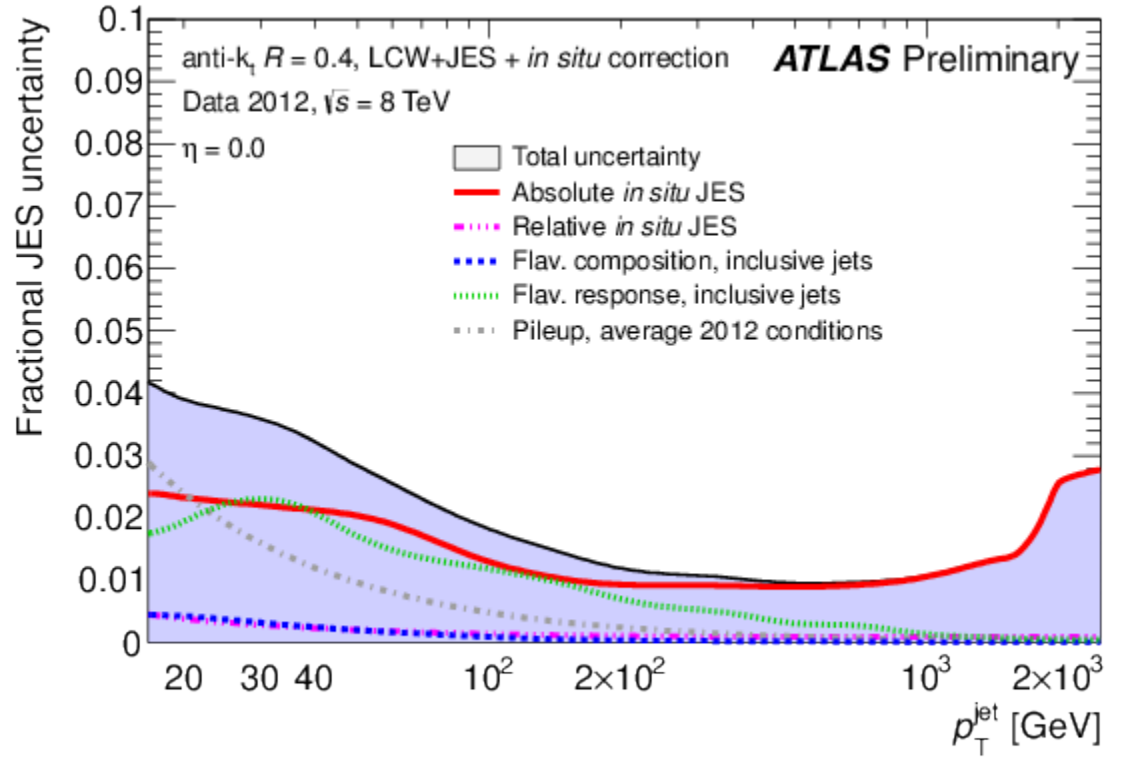
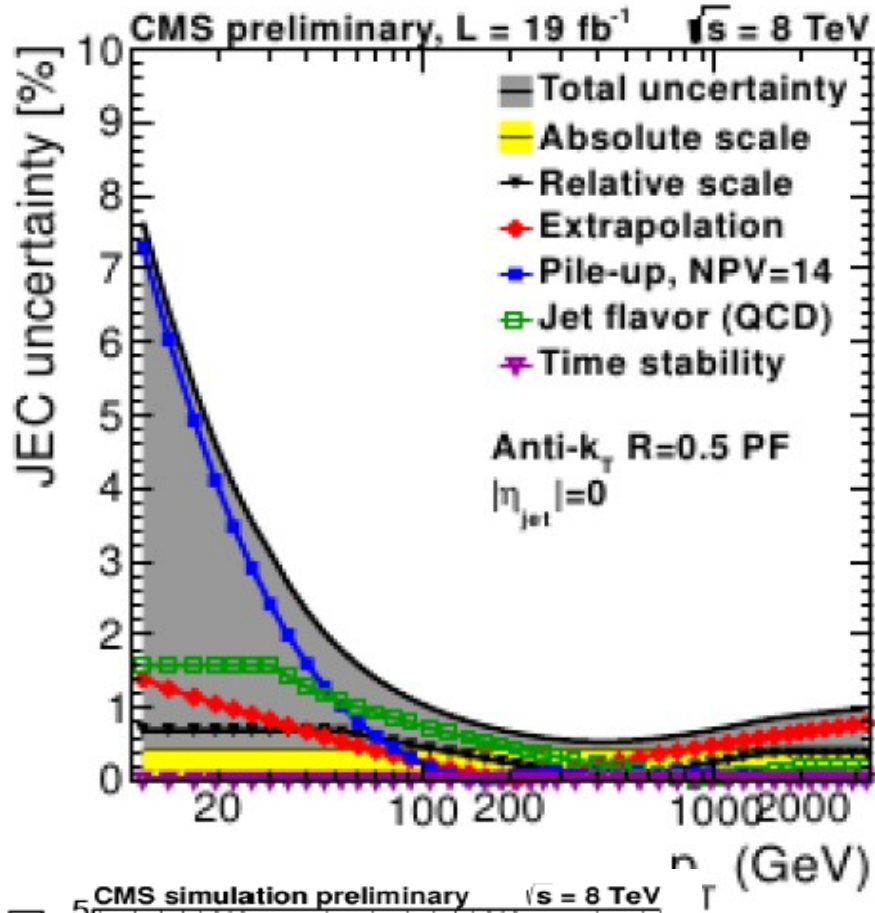
-> CMS and ATLAS need to move to  $t\bar{t}$  MC with Herwig++ (work ongoing)

# Additional Radiation Systematics CMS

- MadGraph+Pythia
- MadGraph  $\mu_R^2 = \mu_F^2 = 4 \cdot Q^2$
- MadGraph  $\mu_R^2 = \mu_F^2 = Q^2/4$
- - - MadGraph matching up
- - - MadGraph matching down







CMS

ATLAS

	20	50	100	20	50	100
JES	20	50	100	20	50	100
pile-up	2%	1%	0.4%	1.5%	1%	0.1%
flavour	1.5%	1%	0.8%	2%	1.5%	1.2%
total	3%	2%	1.2	4%	3%	1.8%