

NLO QCD corrections to $WWb\bar{b}$

“And how they may impact the determination of the top quark mass parameter using the m_{lb} method”.

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NLO QCD corrections to $WWb\bar{b}$ production and their impact on top quark mass measurements



[Top LHC WG Meeting – CERN]

Jan Winter *

– MPP Munich, Germany –



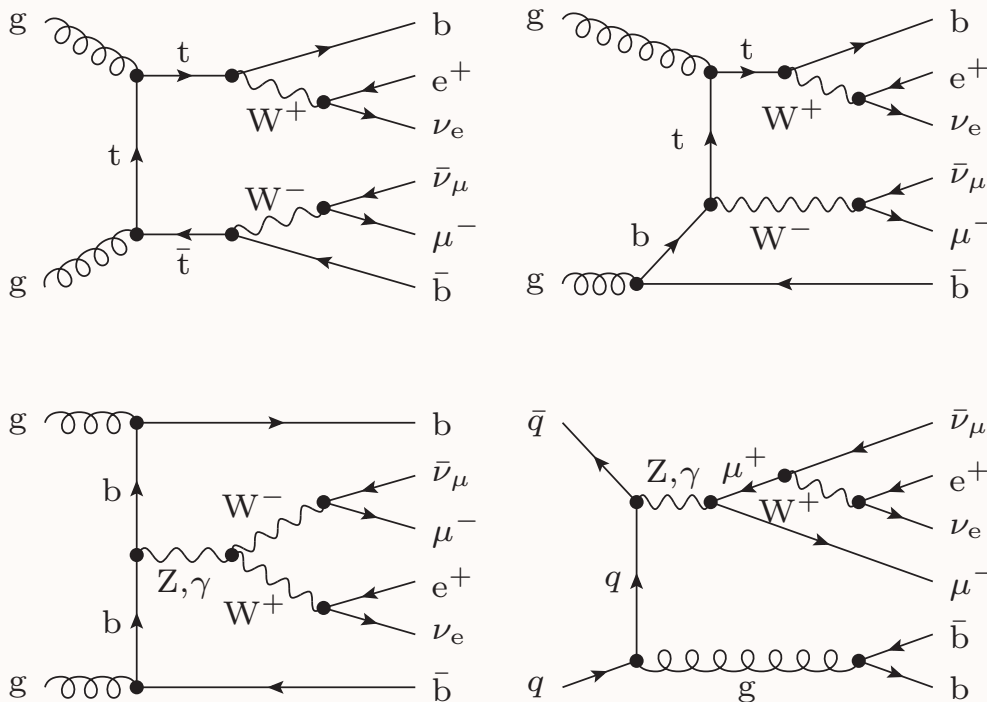
→ *Based on work presented in arXiv:1312.6659.*

- *$WWb\bar{b}$ calculations at QCD NLO.*
- *Top quark mass determination and scale uncertainties.*
- *Summary & conclusions.*
- *Open questions, suggestions and discussion.*

* Work in collaboration with G. Heinrich, A. Maier, R. Nisius and J. Schlenk

$WWb\bar{b}$ production at NLO

→ Some introductory remarks on $WWb\bar{b}$ production at NLO in QCD.



- full NLO treatment includes double-, single- and non-resonant contributions
- complex-mass scheme
- finite top-quark and W width effects
- first done in massless b-quark approximation [DENNER ET AL. ARXIV:1012.3975, ARXIV:1207.5018] [BEVILACQUA ET AL. ARXIV:1012.4230]
- earlier done in NWA where production and decay factorize (neglected contributions are suppressed by powers of $\Gamma_t/m_t \lesssim 1\%$) [MELNIKOV, SCHULZE, ARXIV:0907.3090]

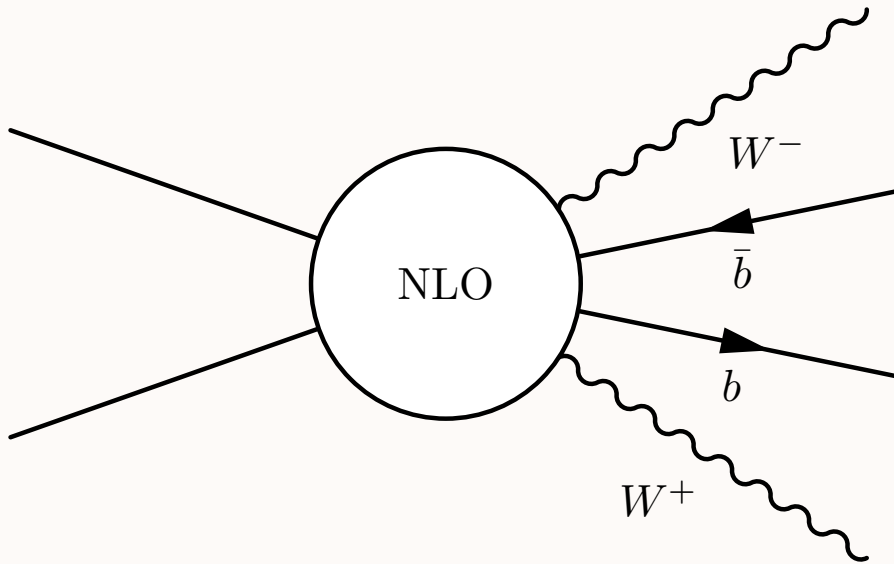
→ Our parton level calculations ...

- use the **GoSam+Sherpa** combined generator package (current versions, GoSam 2.0 and Sherpa 2.1).
- **Sherpa** for calculating Born, real corrections and infrared subtractions [GLEISBERG ET AL, ARXIV:0811.4622]
- **GoSam** for calculating virtual corrections [CULLEN, VANDEURZEN, GREINER, HEINRICH ET AL, ARXIV:1404.7096]
- 5-flavour scheme, massless b-quarks, two resonant W decaying leptonically @ LO respecting spin correlations

⇒ [HEINRICH, MAIER, NISIUS, SCHLENK, WINTER, ARXIV:1312.6659]

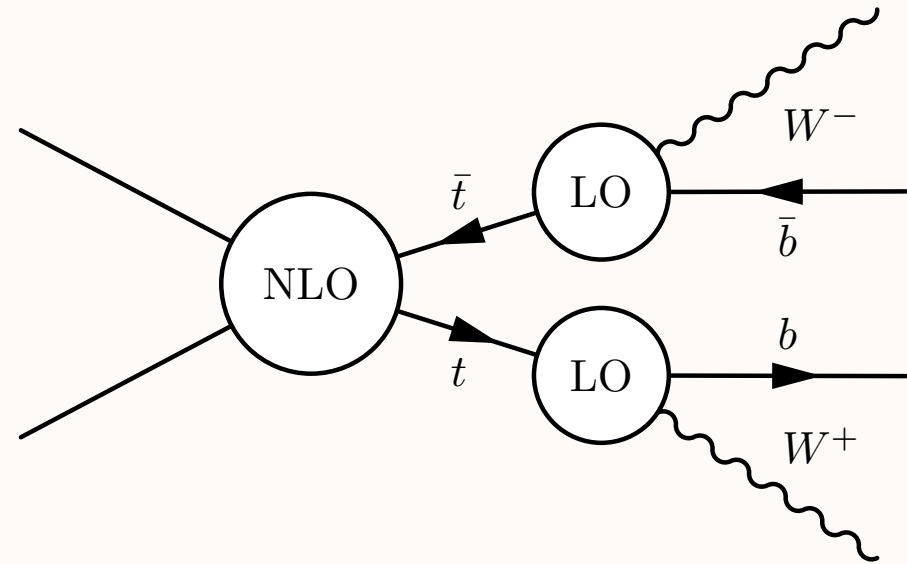


Full versus factorized approach



full ($WWb\bar{b}$)

- full NLO description of the $WWb\bar{b}$ final state ($2 \rightarrow 4$ processes)
- includes NLO effects in top quark decays and non-resonant contributions



factorized ($t\bar{t}$)

- NLO $t\bar{t}$ production ($2 \rightarrow 2$ processes) with LO decays attached and spin correlations preserved
 - standard description for the NLO core in NLO+PS matching
- Calculations used for pure parton level analyses, i.e. m_t is not a MC mass; we use a pole mass.



Top quark mass (parameter) determination from the shape of the invariant mass distribution of the charged lepton and b-jet in $WWb\bar{b}$ production (dilepton channel).

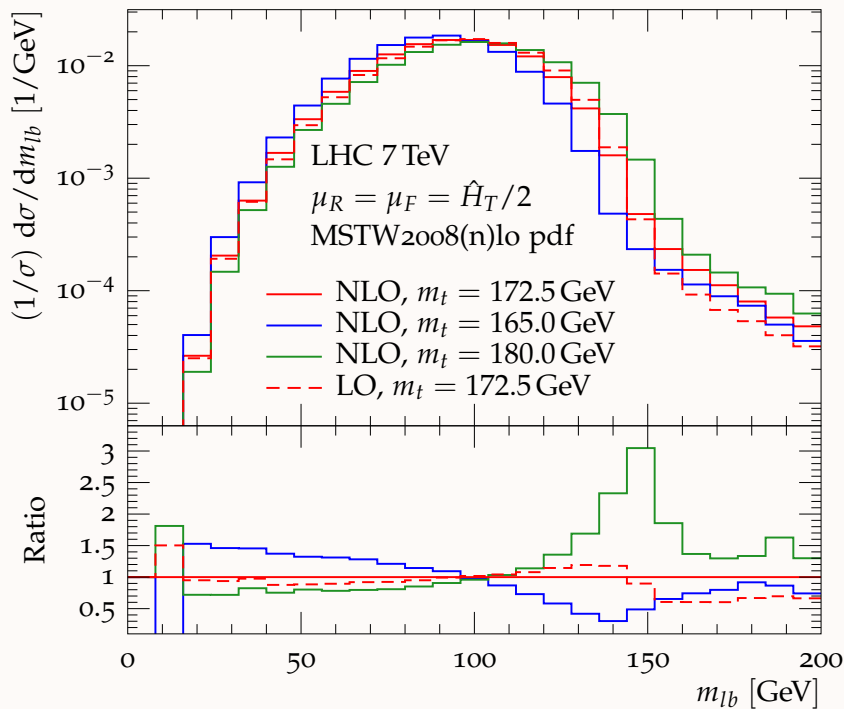


Invariant mass of b-jet and charged lepton

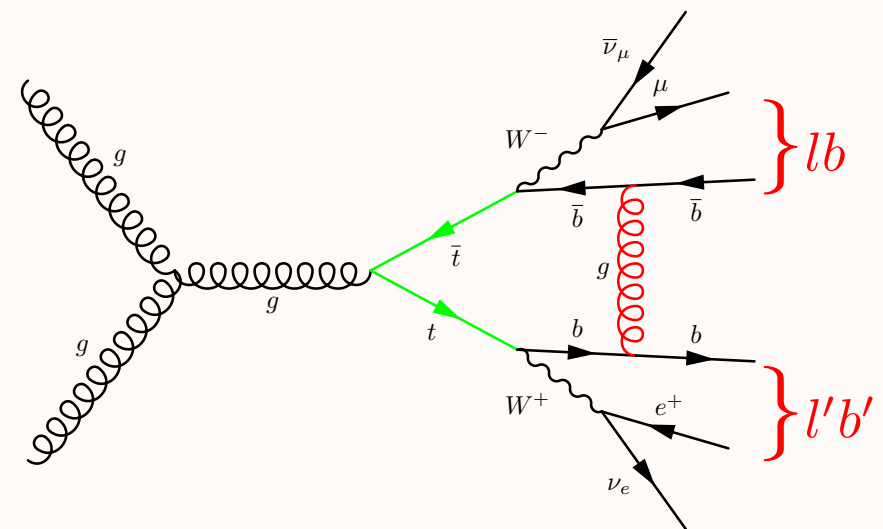
➔ **Parton-level NLO calculations for $W^+W^-b\bar{b}$ based on GoSam+Sherpa framework.**

(full & factorized calc., 5-flavour scheme, massless b-quarks, two resonant W decaying leptonically @ LO)

- Definition: $m_{lb}^2 = (p_{b\text{-jet}} + p_l)^2$ (and criteria to deal with combinatorial problem)
 - The m_{lb} distribution is sensitive to varying the top quark mass \rightarrow NLO calculations for different m_t .
 - Analysis and kinematical requirements according to ATLAS measurement as described in [ATLAS-CONF-2013-077]; in particular: use lepton b-jet pairing minimizing sum of both m_{lb} and average
- ➔ Suitable observable for template fit to precisely measure the top quark mass.



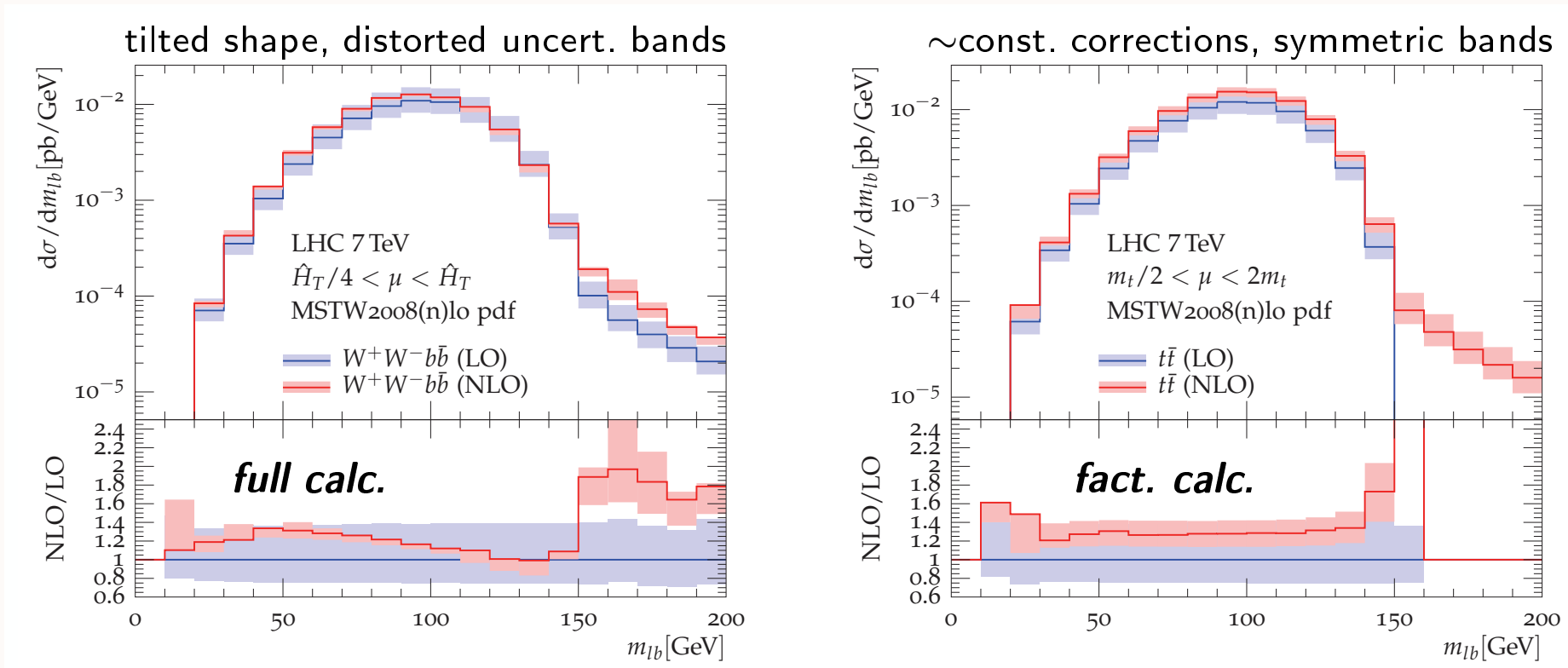
← shape predictions from full QCD NLO $WWb\bar{b}$



The m_{lb} distribution at NLO and scale variations

➔ *Parton-level NLO calculations for $W^+W^-b\bar{b}$ based on GoSam+Sherpa framework.*

(full & factorized calc., 5-flavour scheme, massless b-quarks, two resonant W decaying leptonically @ LO)



▶ Important NLO corrections to the shape of m_{lb}

▶ Values of m_{lb} larger than $\sqrt{m_t^2 - m_W^2}$ are kinematically forbidden in narrow width approximation at LO

• follow ATLAS strategy: use charged-lepton b-jet pairing minimizing sum of both m_{lb} and average.



Note on the inclusive cross section

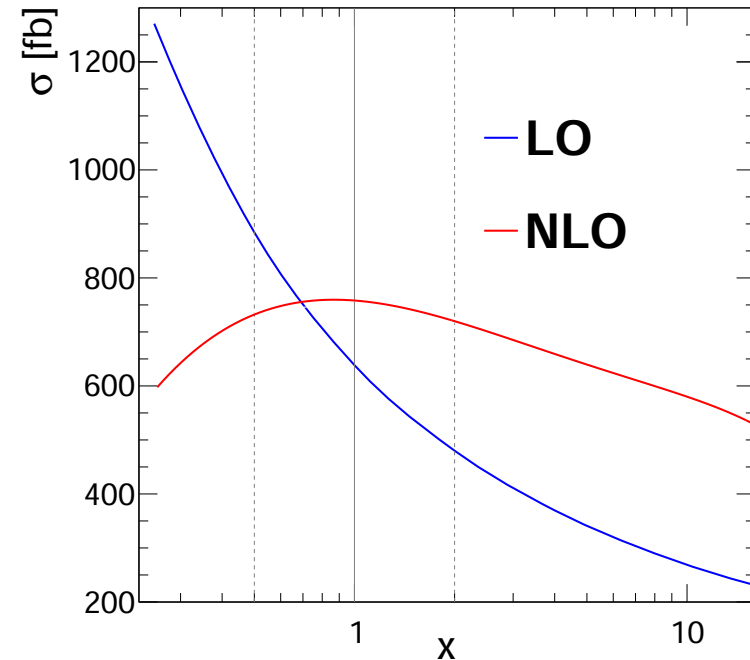
[FROM J. SCHLENK]

→ *Parton-level NLO calculations for $W^+W^-b\bar{b}$ based on GoSam+Sherpa framework.*

Renormalization and
Factorization scale:

$$\mu = \frac{\hat{H}_T}{2} = \frac{1}{2} \sum_i p_{T,i}$$

Scalar sum over transverse
momenta of all final state
particles



$$x = \frac{\mu}{\hat{H}_T/2}$$

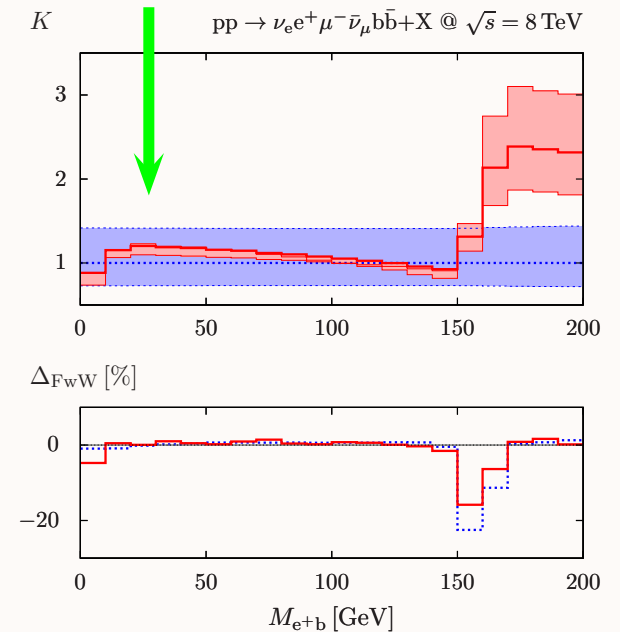
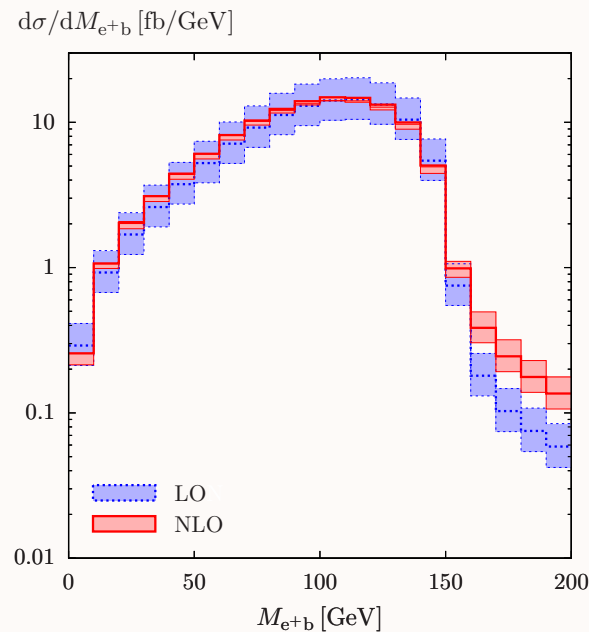
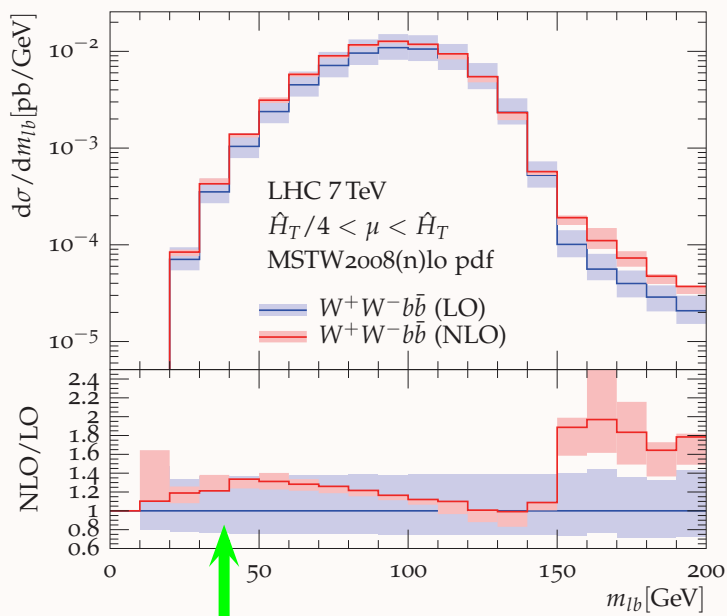


Qualitative comparison of m_{lb} predictions

[DENNER, DITTMAYER, KALLWEIT, POZZORINI, ARXIV:1207.5018]

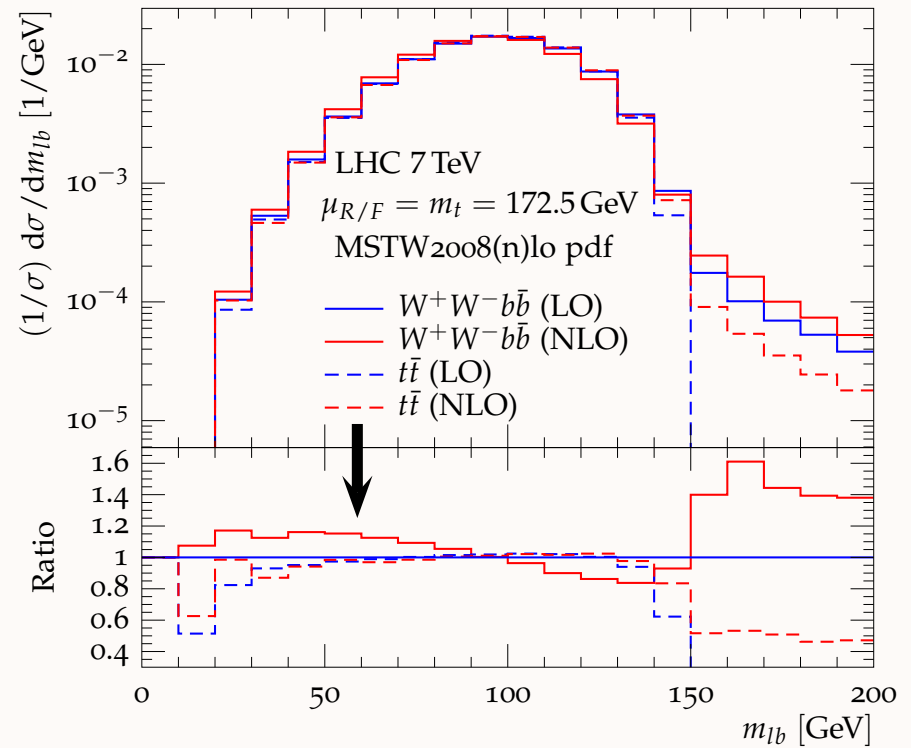
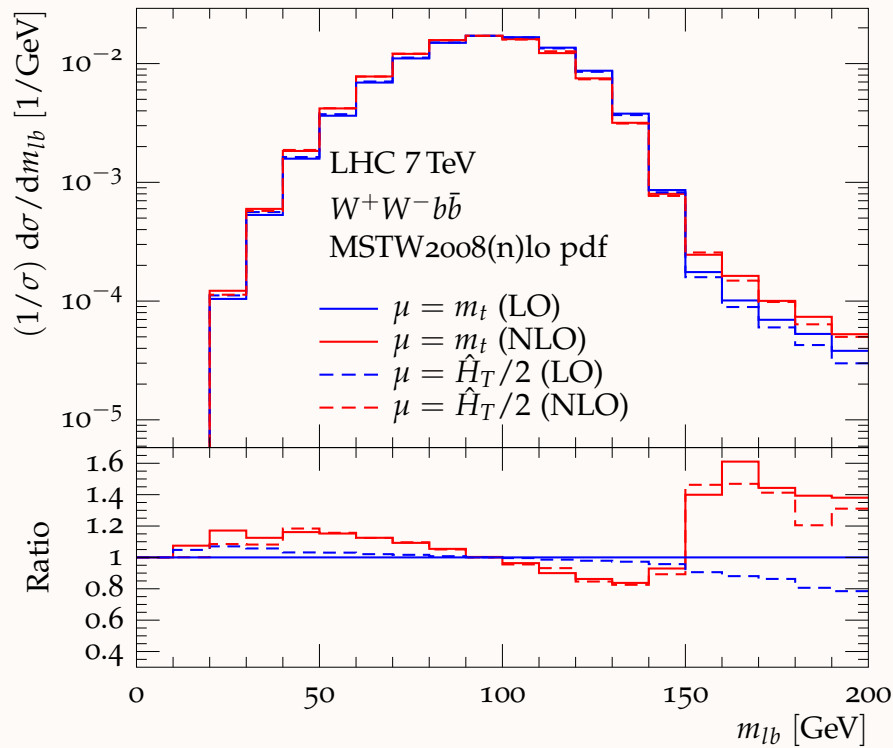
➔ $WWb\bar{b}$: NLO corrections strongly affect the shape of m_{lb}

- similar features → agreement on qualitative level only, noting the differences however:
- different LHC energies & kinematical constraints (cuts), slightly different observable (a truth m_{lb})
- different dynamical scale choice (transverse mass of tops)
- non-resonant and off-shell effects due to finite W boson width
- different treatment of b-quark initial states



Normalized m_{lb} : shape comparisons & cross-checks

- analysis strongly driven by shape of the distribution (rate comes in only through number of events passing acceptance/analysis cuts)

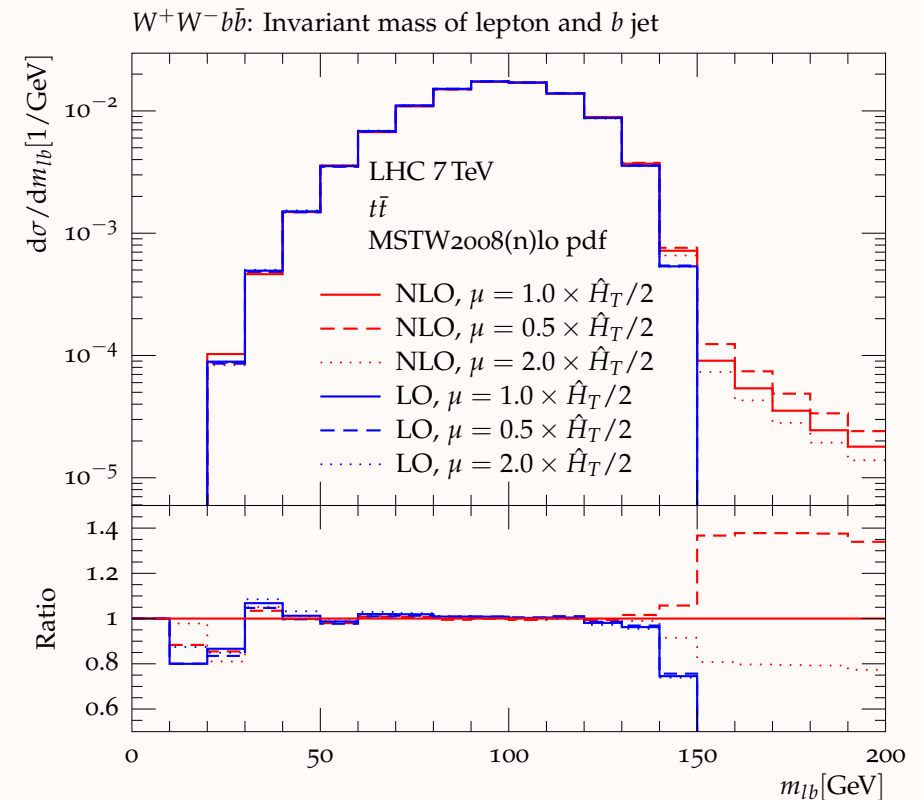
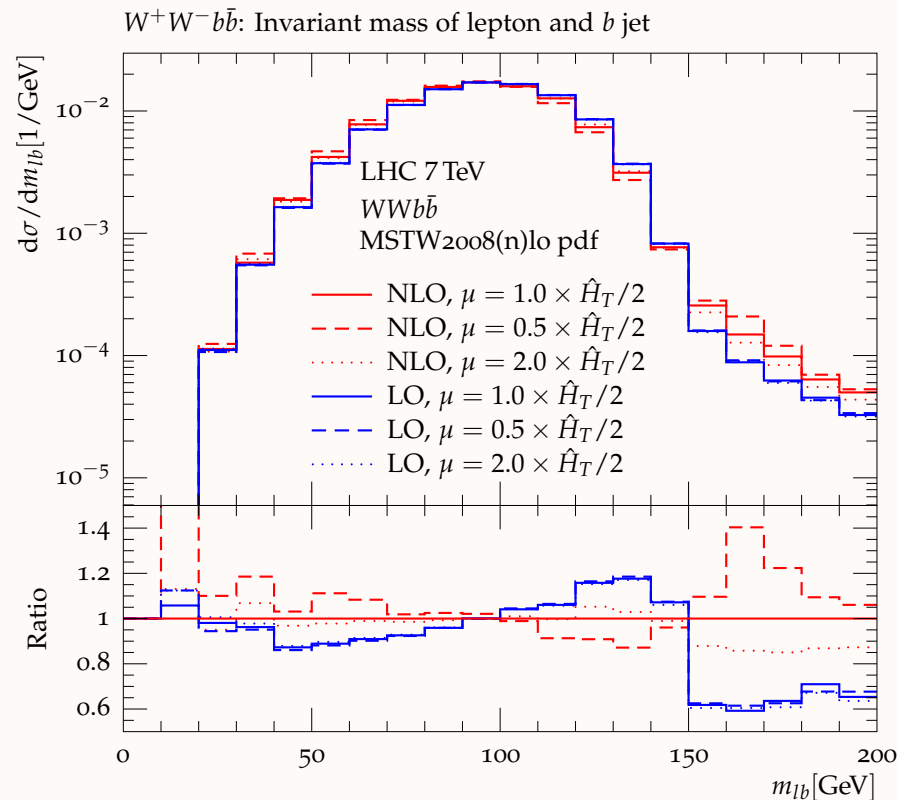


- left: small effect of different scale choices on normalized distributions
- right: for full NLO $WWb\bar{b}$, shape change is drastic while shapes of others are similar



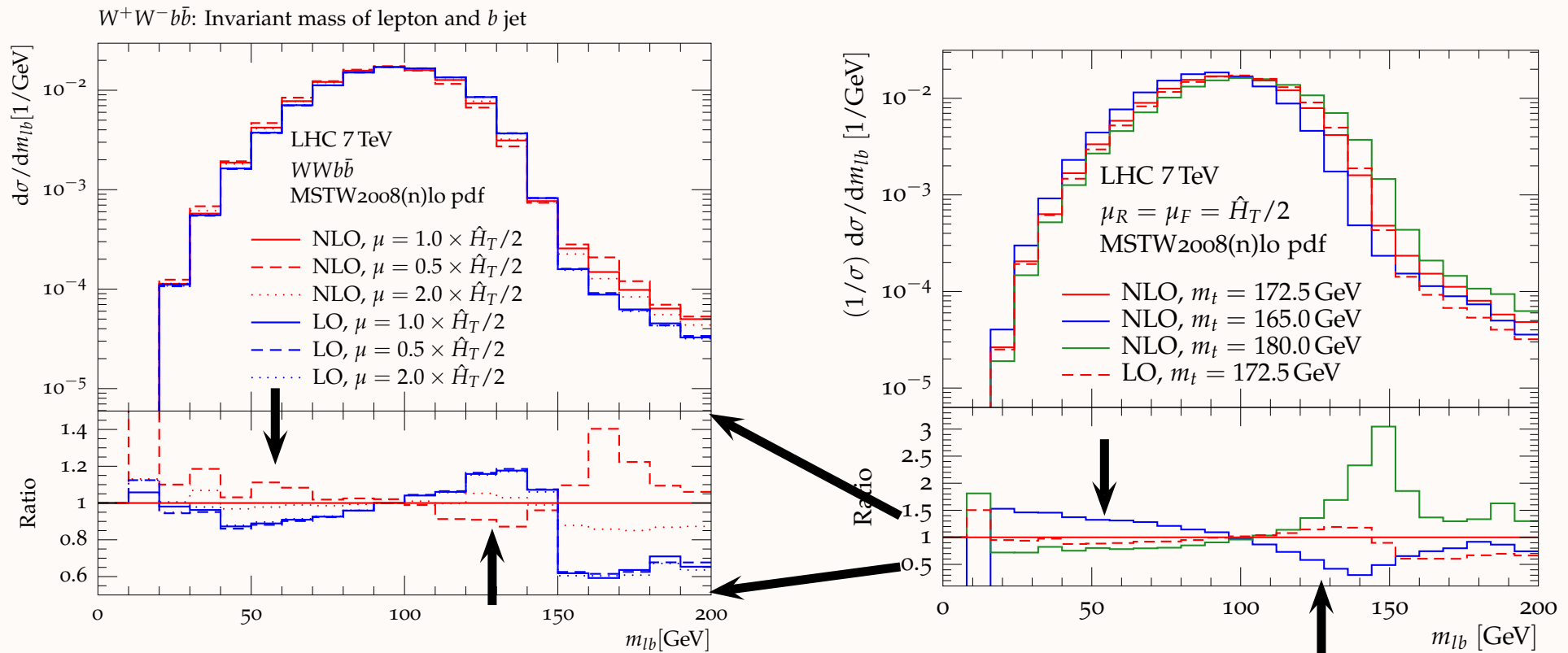
Normalized m_{lb} : scale versus m_t variation

- shape modifications as a result of varying scales by factors of two
- left panel, for the full approach \rightarrow visible
- right panel, for the factorized approach \rightarrow only in tails



Normalized m_{lb} : scale versus m_t variation

- shape modifications as a result of varying scales by factors of two
- left panel, for the full approach \rightarrow visible



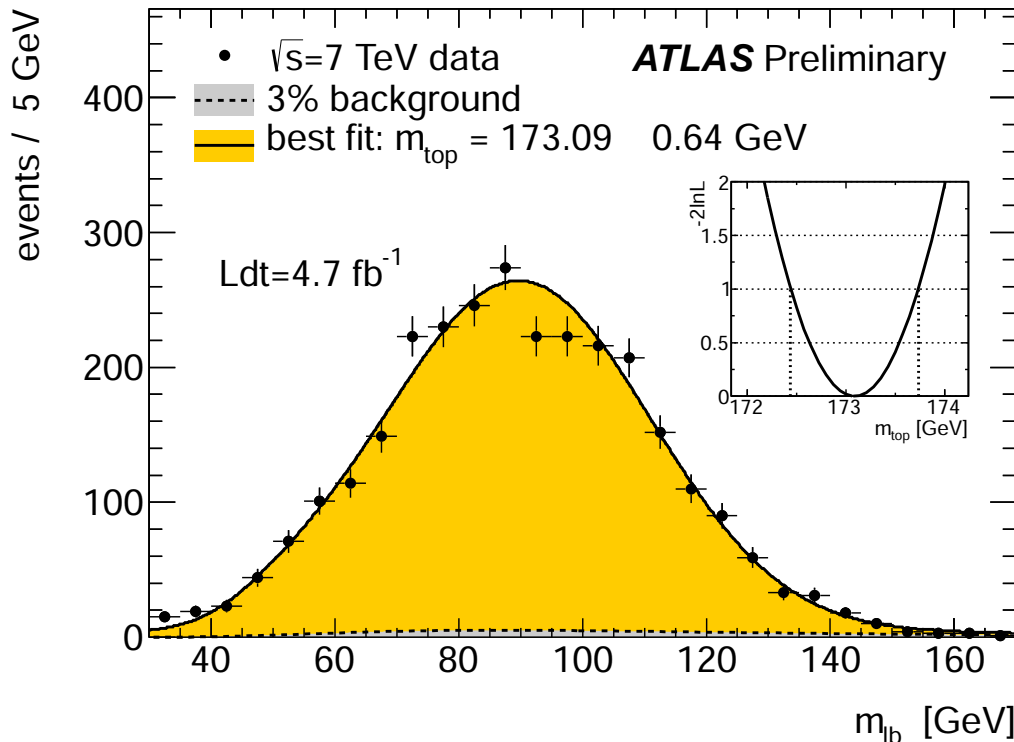
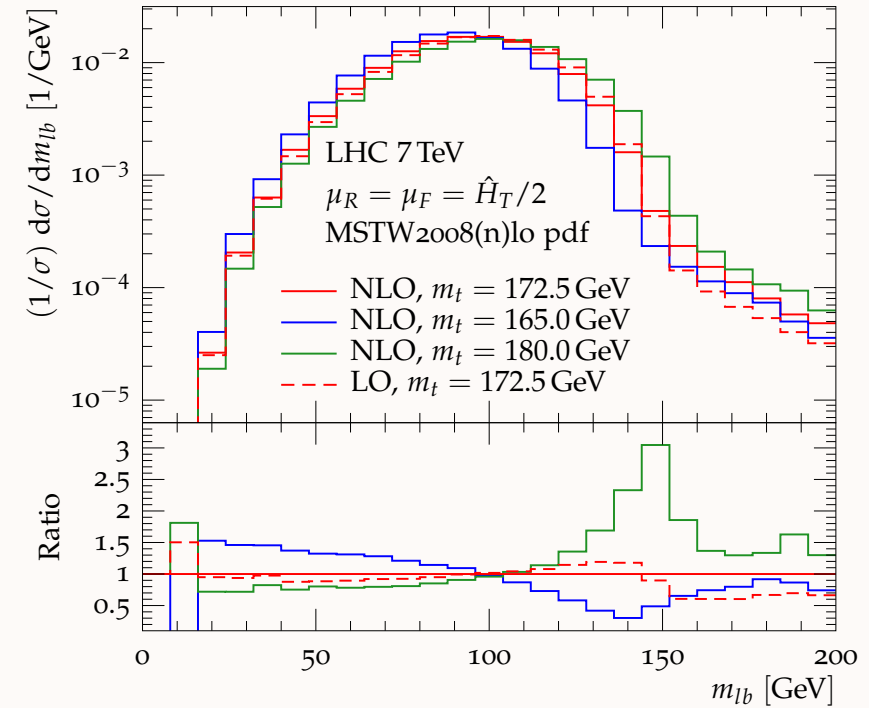
- scale factor variation mimics shape changes as induced by different m_t values \rightarrow uncertainty
- @NLO: scale down corresponds to lower mass
- fit mass and scale simultaneously, but would resulting choice work for other distributions (eg. $m_{t\bar{t}}$)?



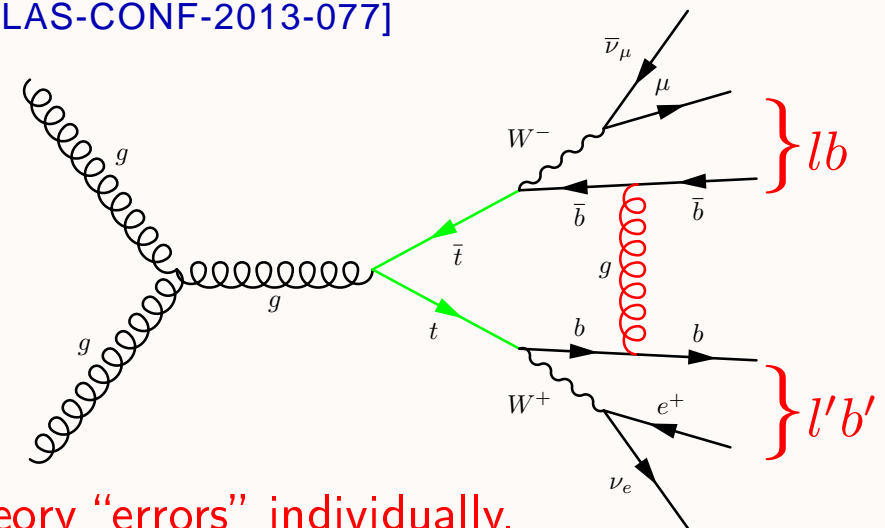
Top quark mass determination using the m_{lb} method

Parametrize “your” theory (m_{lb} predictions).

- Full QCD NLO prediction for $W^+W^-b\bar{b}$ in dilepton channel: m_{lb} distribution is sensitive to top quark mass.
 - ATLAS uses one-dim. template method to determine m_t . Theory uncertainty has been estimated to 0.8 GeV.
- Verify size of th. uncertainties using more advanced calc's!



[ATLAS-CONF-2013-077]

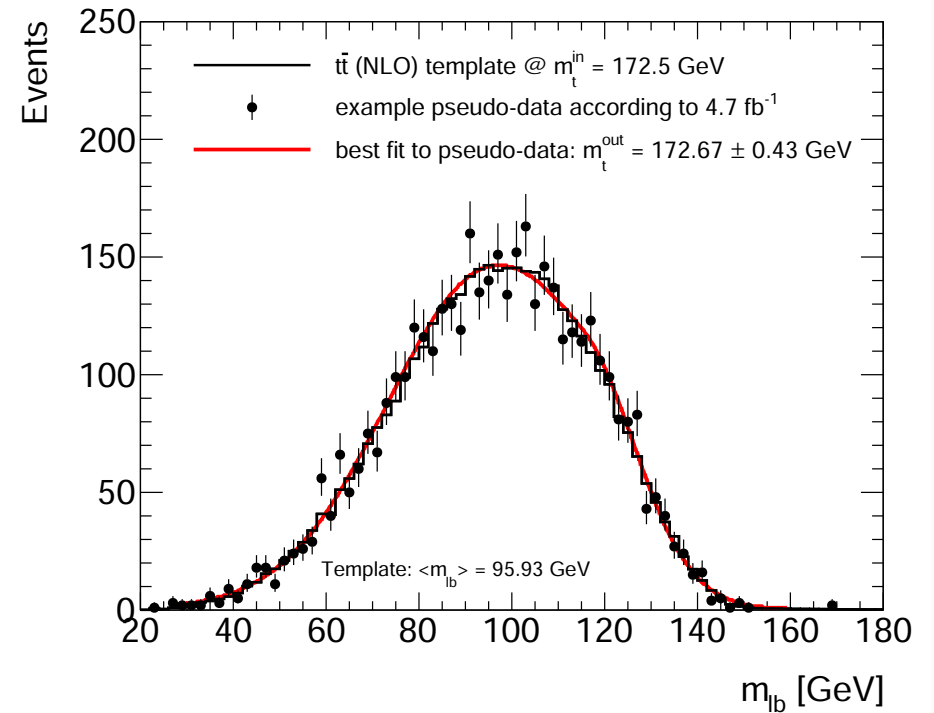
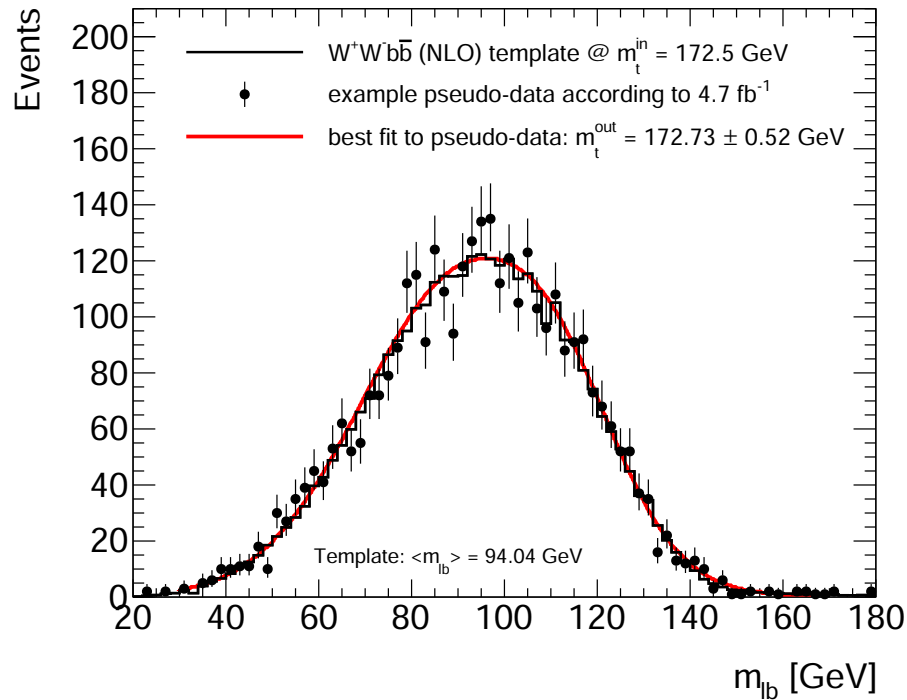
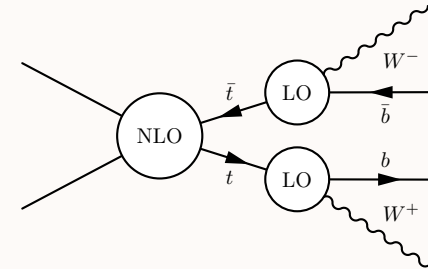
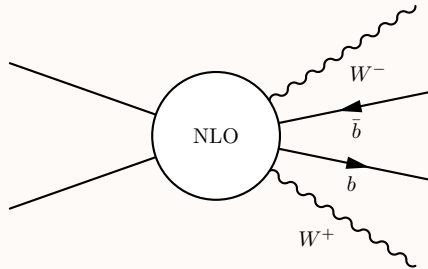


➔ Use pseudo-data to study different types of theory “errors” individually.



NLO templates vs pseudo-data

➔ Representative examples for full (left) and factorized (right) NLO calculation.



- pseudo-data (black points) are generated from the NLO distributions (black histograms) at m_t^{in}
- fit with NLO templates (parametrization) gives m_t^{out} → best fit to pseudo-data (red line)



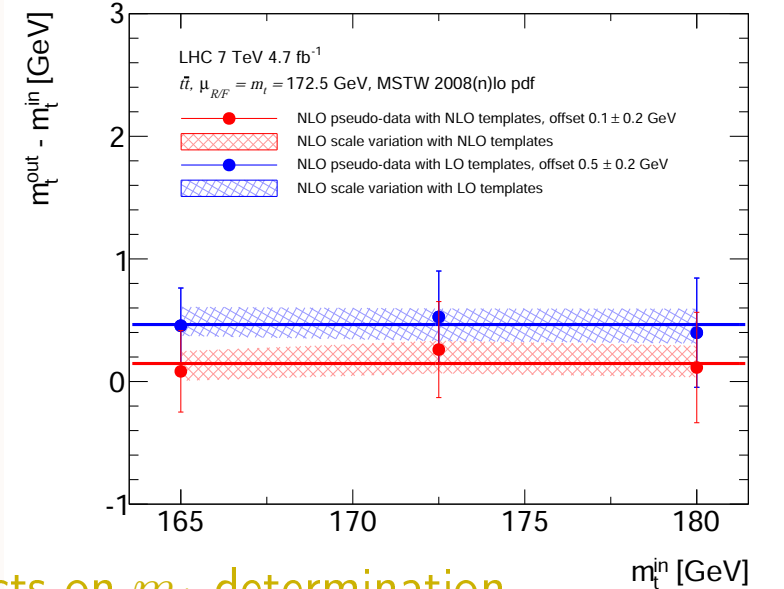
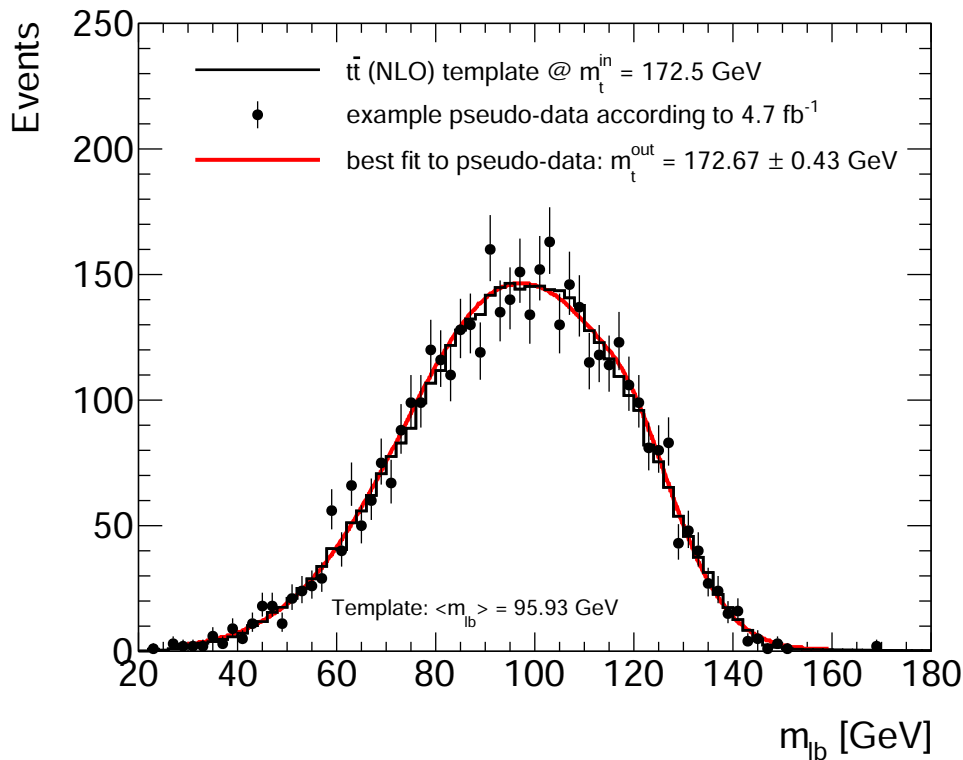
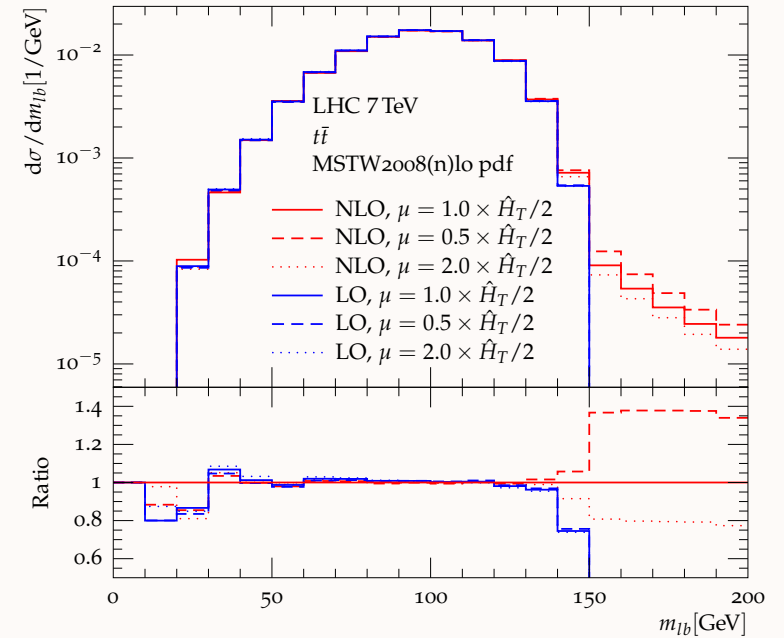
Scale uncertainties and the m_{lb} method

[HEINRICH, MAIER, NISIUS, SCHLENK, WINTER, ARXIV:1312.6659]

Single out effect of NLO scale uncertainties on top mass.

- Use m_{lb} method in a parton-level analysis where we assume that data follows factorized QCD NLO prediction for $t\bar{t}$ with subsequent dilepton decays at LO [pseudo-data].
- Apply/test against the theories given by default scale choice NLO and LO predictions (templates) [hypotheses].

$W^+W^-b\bar{b}$: Invariant mass of lepton and b jet



➔ Based on NLO $t\bar{t}$ + LO decays, only small effects on m_t determination.



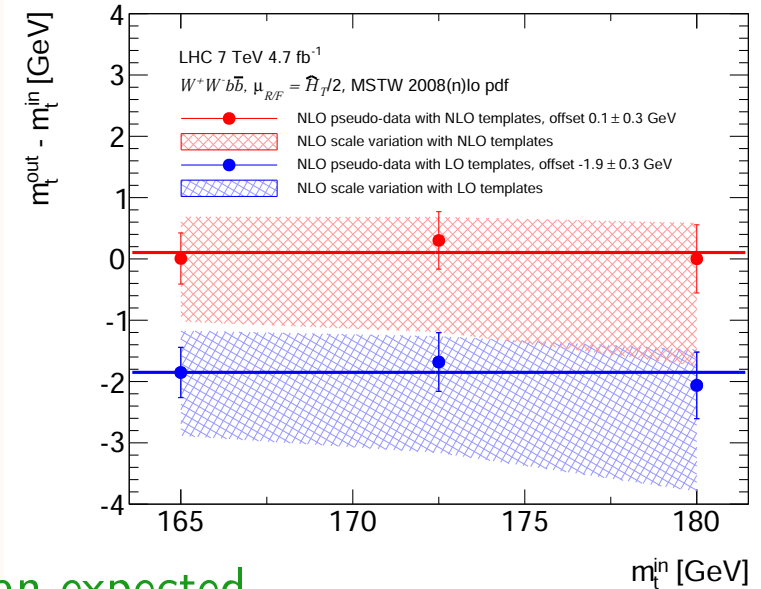
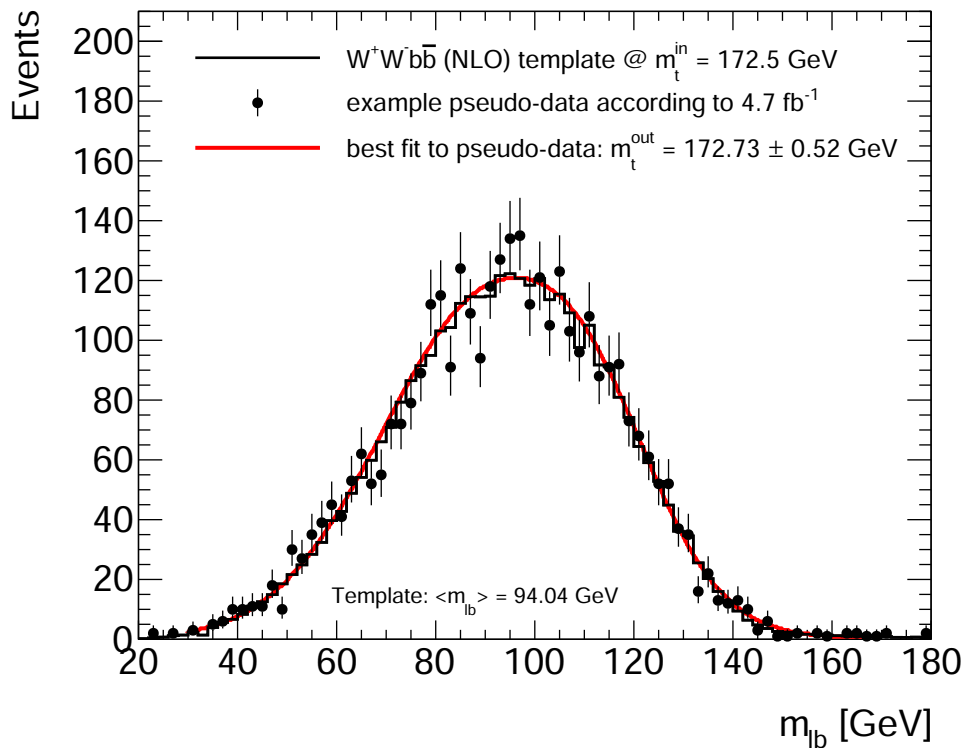
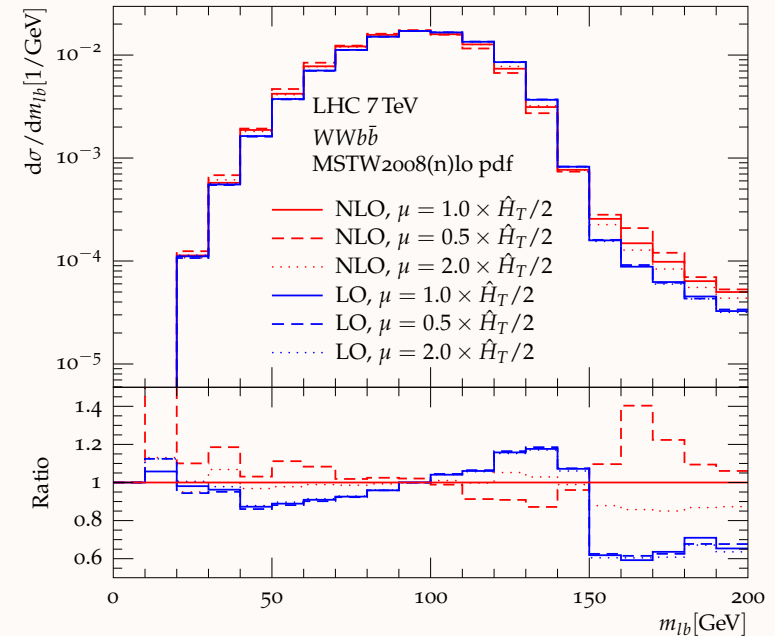
Scale uncertainties and the m_{lb} method

[HEINRICH, MAIER, NISIUS, SCHLENK, WINTER, ARXIV:1312.6659]

Single out effect of NLO scale uncertainties on top mass.

- Use m_{lb} method in a parton-level analysis where we assume that data follows full QCD NLO prediction for dileptonic $W^+W^-b\bar{b}$ [pseudo-data].
- Apply/test against the theories given by default scale choice NLO and LO predictions (templates) [hypotheses].

$W^+W^-b\bar{b}$: Invariant mass of lepton and b jet

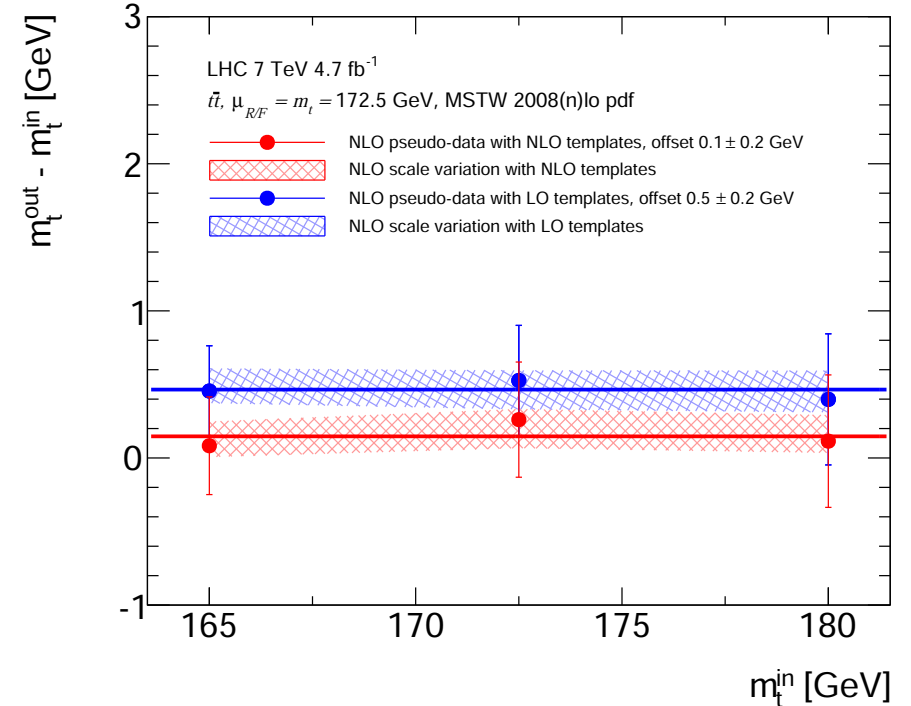
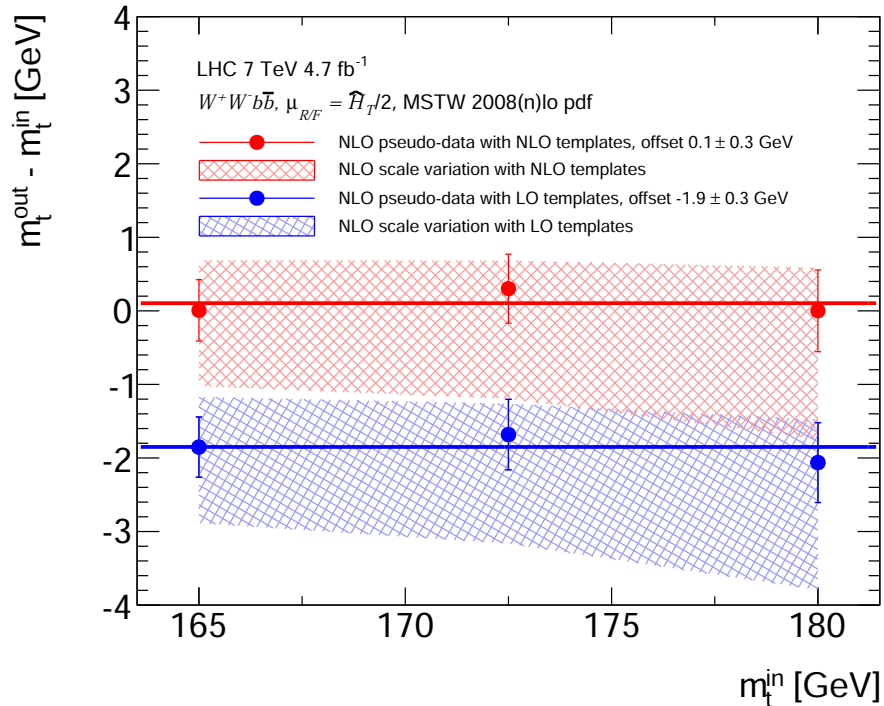
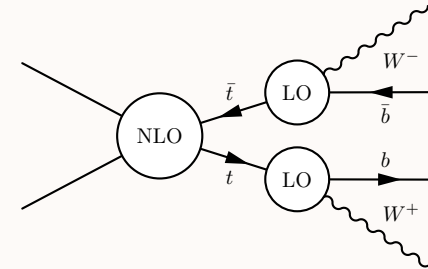
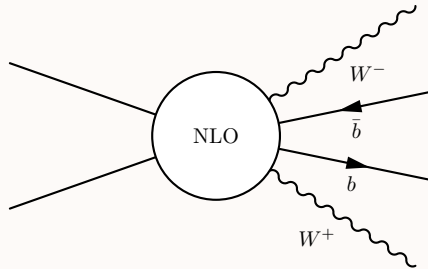


➔ Impacts top quark mass determination more than expected.



Summary

➔ Full (left) vs factorized (right) NLO calculation: results for mass shifts.



- larger shift btwn NLO & LO description (~ 1.9 GeV) as compared to factorized approach (~ 0.5 GeV)
- significantly larger uncertainties from scale variations for full approach ($^{+0.6}_{-1.0}$ GeV vs ± 0.2 GeV)



Summary.

Calculation of the NLO QCD corrections to $WWb\bar{b}$ production using the parton level combined event generator GoSam+Sherpa.

NLO effects studied in the context of the top quark mass measurement based on the m_{tb} template method (well defined framework for our pure parton level analysis).

Shape uncertainties from scale variations of the full NLO QCD corrections to $WWb\bar{b}$ production result in larger theory errors on the top quark mass determination than expected.



Discussion, preliminary results & questions.

Validation ongoing to disentangle effects from radiative corrections in decay, non-resonant contributions and finite-width treatment (NLO in “decay” seems crucial).

Parton shower and hadronization effects? Hadron-level predictions wanted.

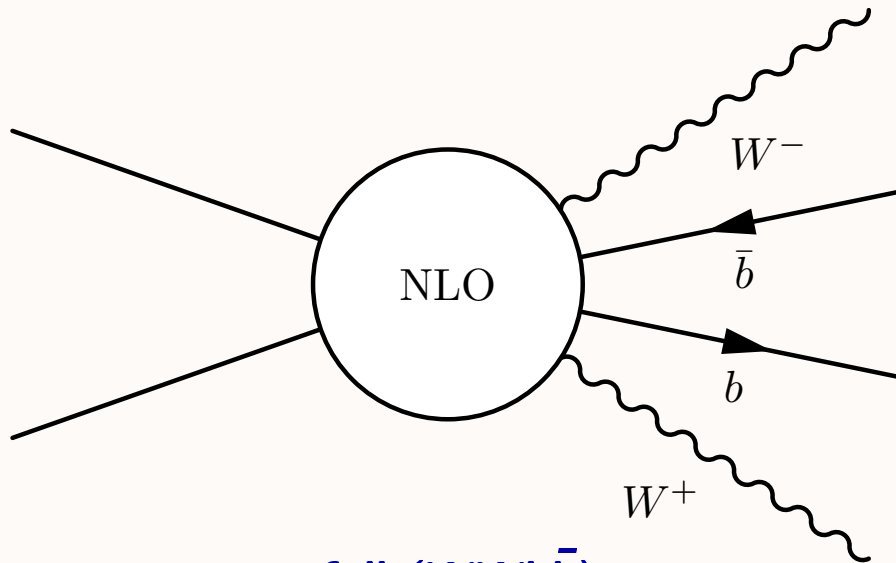
Phase-space regions and/or observables less affected by scale uncertainties (or, on the contrary, where they dominate over m_t dependence to fix scale with data).

Using improved calculations, what are the effects on other top quark mass analyses?

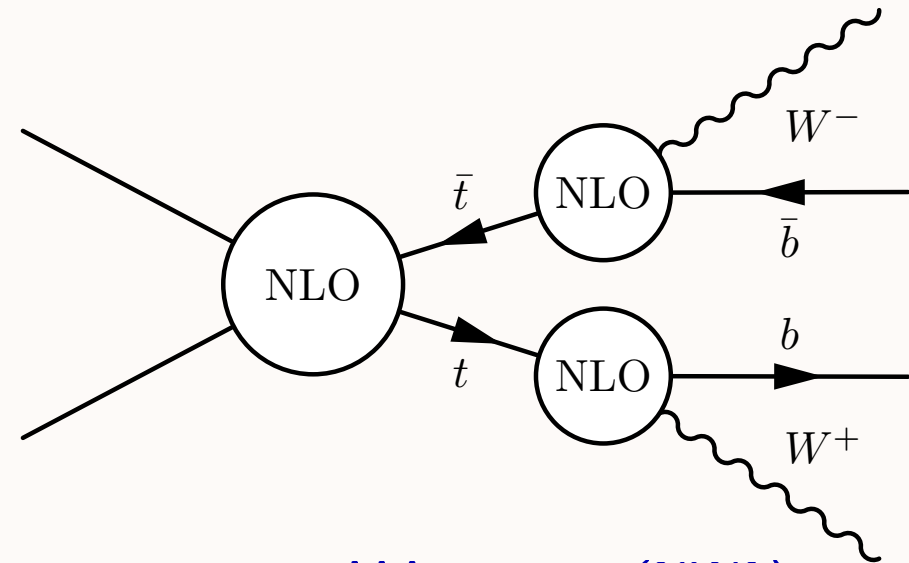


Radiation in the decay

[BISWAS, MELNIKOV, SCHULZE, ARXIV:1006.0910]



full ($WWb\bar{b}$)



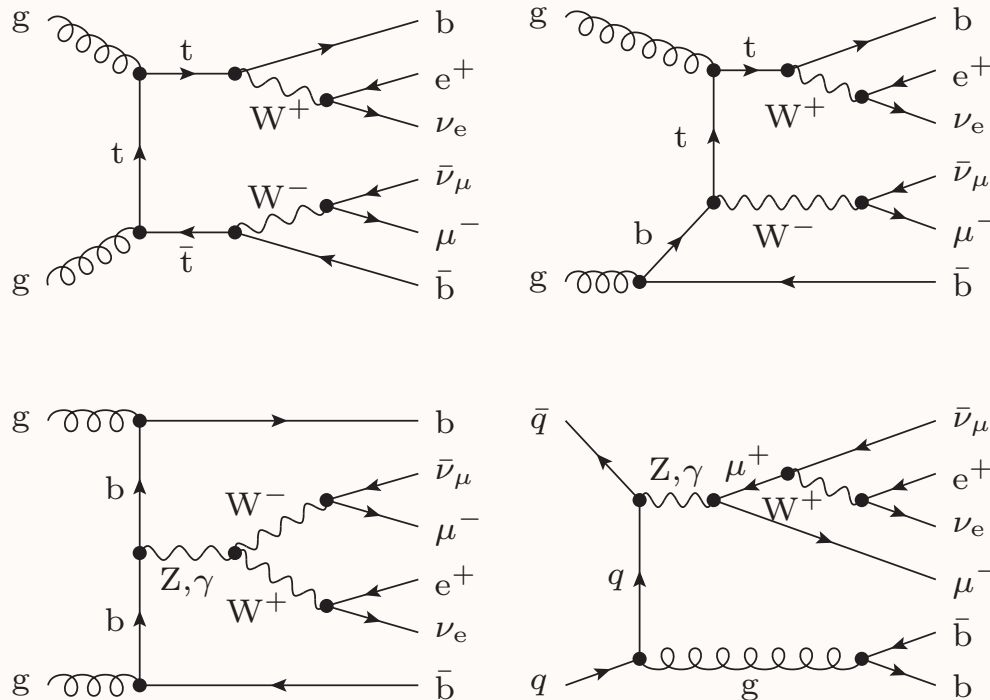
narrow width approx. (NWA)

- full NLO description of the $WWb\bar{b}$ final state ($2 \rightarrow 4$ processes)
- includes NLO effects in top quark decays and non-resonant contributions
- comparison will help disentangle effects from NLO decays and non-resonant contributions
- choose different scales in the production and decay ... becomes testable
- to what extent are radiative decay corrections well modelled by shower in NLO+PS (how do we assess the uncertainties related to these shower emissions)
- also in **reference**, an estimator related to m_t obtained from moment of $m_{lb} \rightarrow$ experimental alternative?



$WWb\bar{b}$ production at NLO: massive b-quarks

➔ *New development: bottom quark mass included in calculation.*



- full NLO treatment includes double-, single- and non-resonant contributions
- complex-mass scheme
- finite top-quark and W width effects
- first done in massless b-quark approximation [DENNER ET AL. ARXIV:1012.3975, ARXIV:1207.5018] [BEVILACQUA ET AL. ARXIV:1012.4230]
- earlier done in NWA where production and decay factorize (neglected contributions are suppressed by powers of $\Gamma_t/m_t \lesssim 1\%$) [MELNIKOV, SCHULZE, ARXIV:0907.3090]

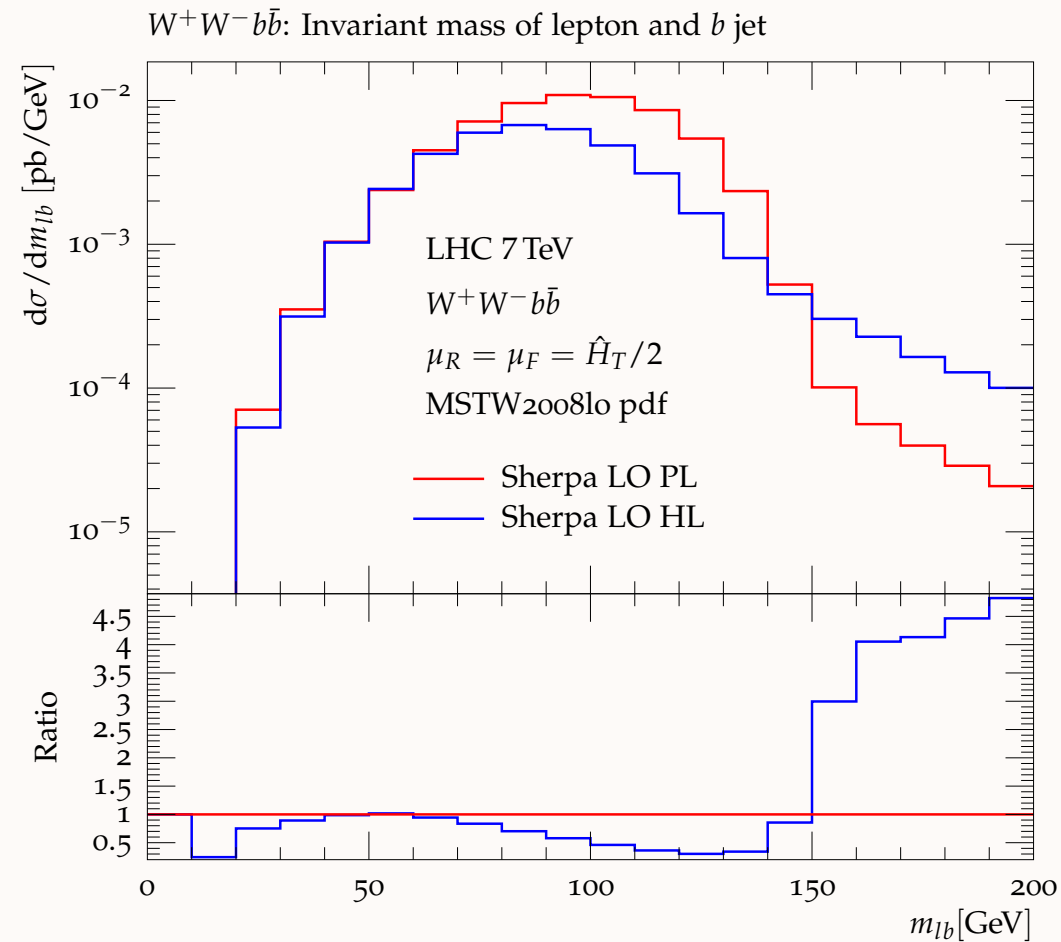
- off-shell and single-top contributions more important in phase-space regions with unresolved b-quarks
- only accessible in calculations with massive b-quarks in the 4-flavour (4F) scheme
- in the 4F, fully differential NLO description of both FS b-jets → permits application of jet vetoes
- → gauge-invariant separation of narrow-top-width contribution and finite-width remainder
- results provided recently by two groups:

[FREDERIX, ARXIV:1311.4893] [CASCIOLI, KALLWEIT, MAIERHÖFER, POZZORINI, ARXIV:1312.0546]



What to expect from showering and hadronization?

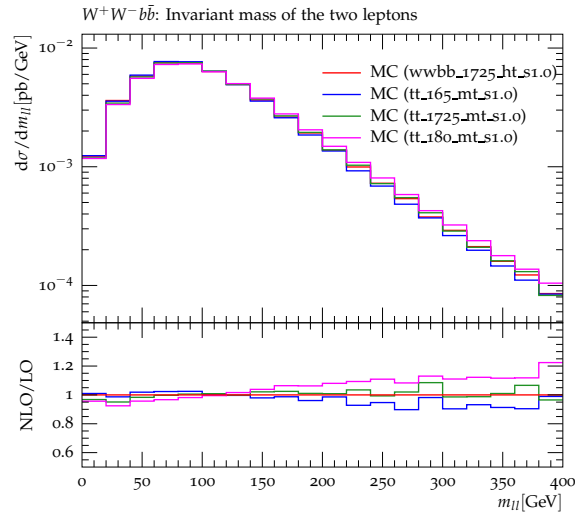
- only **PRELIMINARY** result
- transition region between peak and tail washed out



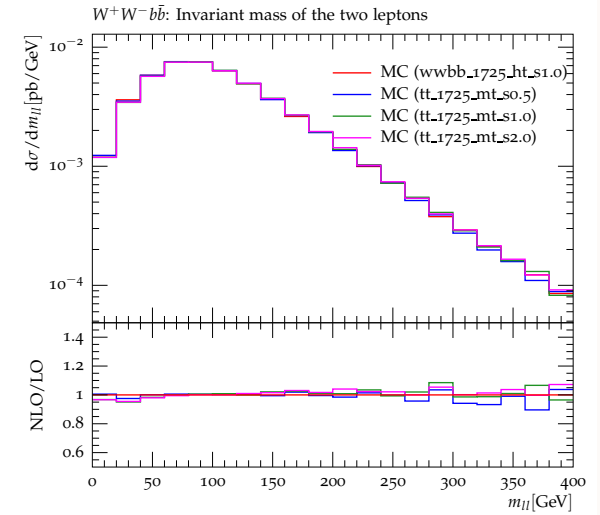
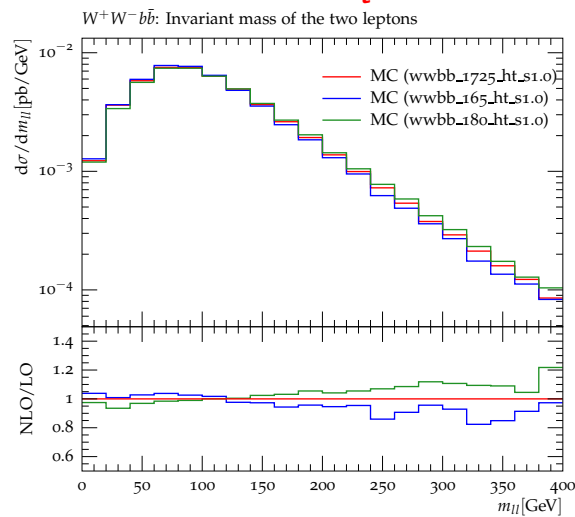
Other observables?

- less sensitive to m_t , but “cleaner” observable \rightarrow better systematics?
- pay-off comes with more data ...

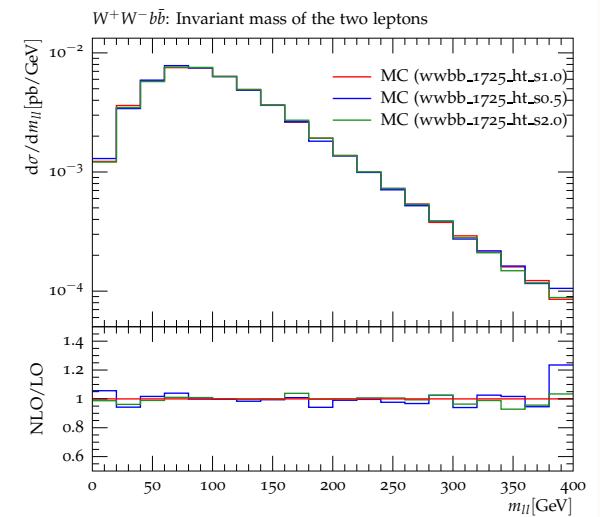
m_{ll}



m_t variation



scale variation



fact.

full



The end.

