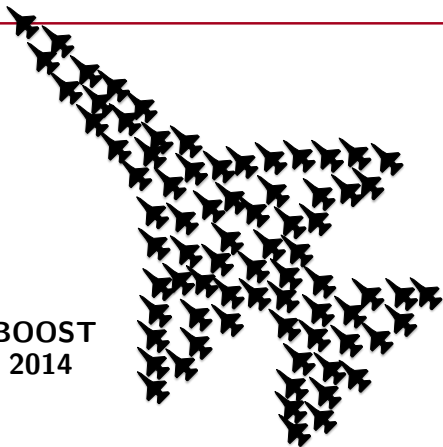


# Jets from Jets

*Re-clustering as a tool for large radius jet reconstruction and grooming at the LHC*



**BOOST  
2014**

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*SLAC, Stanford University*

*based on [arXiv:1407.2922](#)*

In collaboration with

**Pascal Nef**

**Ariel Schwartzman**

**Maximilian Swiatlowski**

# Introduction

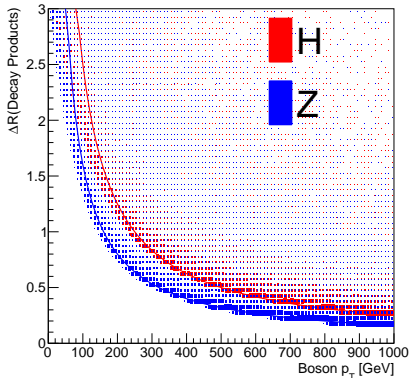
Angular separation of decay products for a massive  $\mathcal{P}$ , scales as  $2m_{\mathcal{P}}/p_T^{\mathcal{P}}$ .

→ jet radius parameter  $R$  should be process dependent and scale with  $p_T$ .

In practice, the LHC collaborations use a small number of  $R$  values.

There is a distinction between *large* radius jets and *small* radius jets.

From *large* radius jets, we have seen many studies probing the **top down** substructure of jets, at fine radial scales.



Why do we **not** optimize  $R$  **per process** and **per energy scale**?

# A Minor Setback: Jet Calibrations

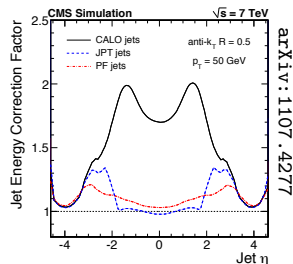
Algorithms are not optimized per analysis due to non-trivial calibrations:

**Calibration:** The corrections to a jet 4-vector so that  $\langle E^{\text{reco}}/E^{\text{truth}} \rangle = 1$  and is independent of  $\eta$ .

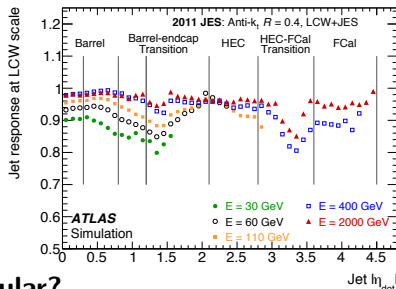
[Particle flow/Calorimeter cluster]

inputs to jets are calibrated,  
but need to correct for e.g.

particles that were missed, merged, or below noise thresholds, energy loss in un-instrumented regions, and correlations between particles.



arXiv:1107.4277



arXiv:1406.0076

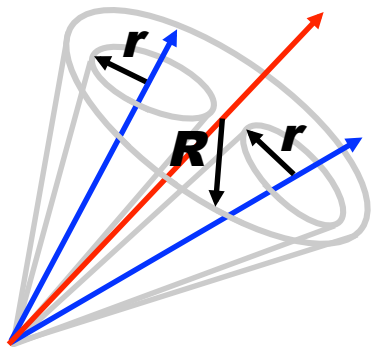
Can we make jet clustering more modular?

# Jets from Jets: a modular way to cluster & calibrate

Introduce a new angular scale  $\mathbf{r} < \mathbf{R}$ ;  
Cluster radius  $\mathbf{r}$  jets into radius  $\mathbf{R}$  jets.

If chosen appropriately, the corrections  
and calibrations (and uncertainties!)  
from  $\mathbf{r}$  propagate to the large radius jets.

All that must be specified ahead of time  
is the small radius jet algorithm.



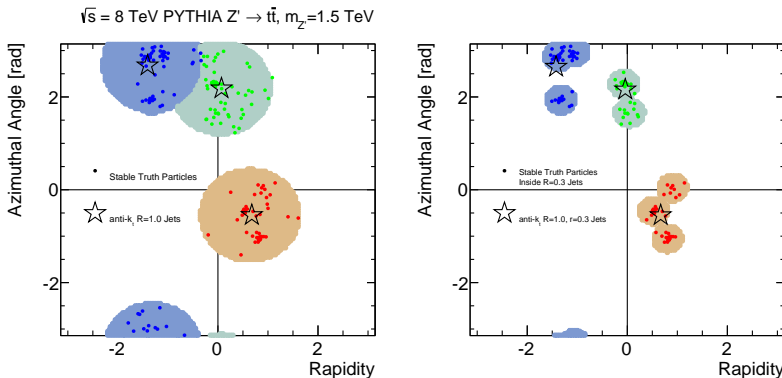
$\therefore$  Every **kinematic region** of **every analysis** for **every data-taking**  
condition can optimize the large radius parameter in order to maximize the  
sensitivity to particular physics scenarios.

N.B. The set of jets above a threshold  $p_T$  is IRC safe and so re-clustered jets inherit IRC safety.

# Re-clustered Jets

Small radius jets can only be reliably calibrated to a certain  $p_T$  threshold. This threshold scales with  $r$ , but is  $\sim 20$  GeV for  $r \sim 0.4$ .

→ Even without further considerations, re-clustering *grooms* the jets.

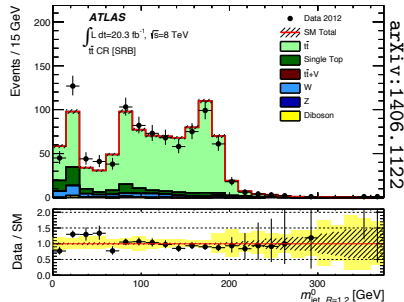
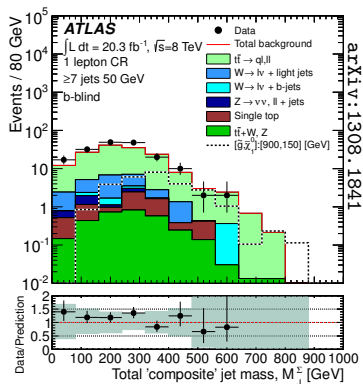


Also, the *effective area* (pileup sensitivity) of re-clustered jets is smaller.

# A Brief History in ... Re-clustering

Grouping small radius jets to form composite systems of objects has been used for quite some time - for instance in forming  $m_{j_1 \dots j_n}$  for jets  $j_i$ .

Re-clustering was pioneered in recent ATLAS SUSY searches:



0 Lepton Direct Stop Search: W/Top tag  
 with re-clustered jet (mass)

Inclusive multijets:  $M_J^\Sigma = \sum_i$  re-clustered jet  $i$  mass

# Something New: Re-clustered Grooming

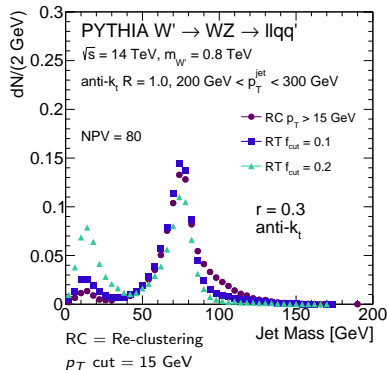
Example: re-clustered trimming (RT):

Drop all small radius  $r$  jets  $i$  re-clustered into the radius  $R$  jet  $J$  if

$$p_{T,i} < f_{\text{cut}} \times p_{T,J} = \sum_j p_{T,j}$$

Which adds a new parameter,  $f_{\text{cut}}$  – analogous to large radius jet trimming.

Small differences:  $f_{\text{cut}}$  is applied to a jet which has a small level of grooming already applied and which has been pileup corrected (not standard for the LHC experiments).

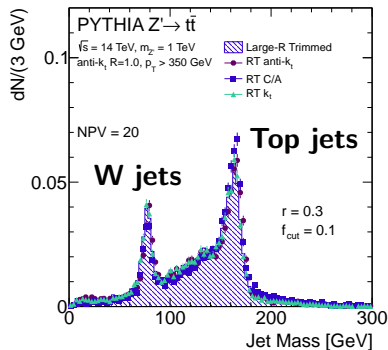
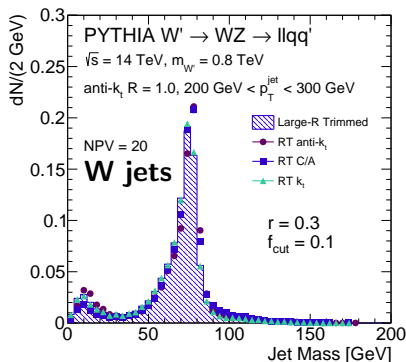


Recall:  $f_{\text{cut}}$  can be optimized per analysis and so can be  $p_T$  (and pileup) dependent.

# Re-clustered Trimmed Jets in Action

With low levels of pileup, there is not a large dependence on the radius  $r$  jet algorithm.

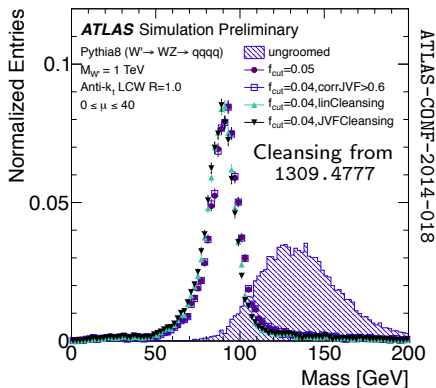
As expected, RT jets with  $k_t$   $r = 0.3$  jets and anti- $k_t$   $R = 1.0$  jets is nearly identical to the large  $R$  trimmed analogue with the same parameters.





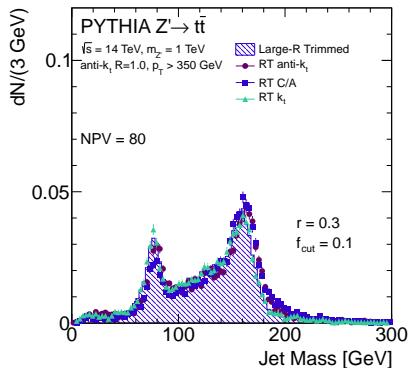
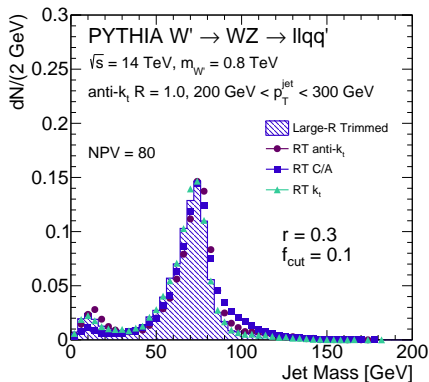
The modular structure of re-clustering easily allows for

- Pileup calibrations via  $\rho \times A^\mu$  for each radius  $r$  jet, and any residual  $\mu$  and NPV corrections that are needed
- Pileup jet removal via any one of many techniques.  
e.g. JVF/JVT, pileup ID, cleansing, etc.



# RT Jets with High Pileup

The distribution of pileup corrected (via  $\rho \times A^\mu$ ) Large  $R$  trimmed jets changes shape similarly to pileup corrected radius  $r$  jets, RT.

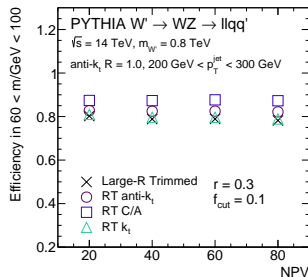
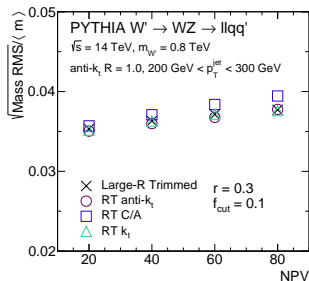
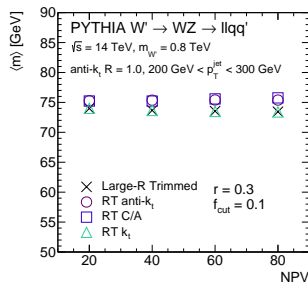


C/A jets seem to perform the worst, but this may also be an  $f_{\text{cut}}$  dependent statement as the jet area varies by algorithm.

# Quantitative comparison - radius $r$ jet algorithm

For  $r = 0.3$  and  $f_{\text{cut}} = 0.1$ ,

- The average mass is NPV stable
- Window efficiency is NPV stable
- C/A has the highest window efficiency, but worst resolution



# Determining the size of $r$

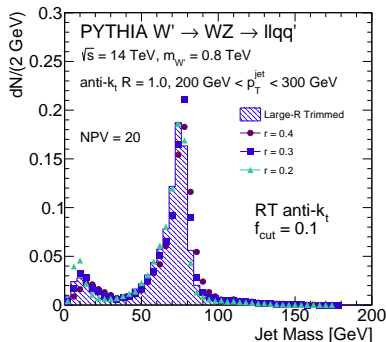
Aside from the algorithm type, the only parameter that must be decided ahead of time is  $r$ .

## Pros for smaller $r$

Less sensitive to pileup (scales with  $r^2$ )  
Resolve finer structure

## Cons for smaller $r$

Larger residual calibration (as  $r \rightarrow 0$ ,  
back to topo-clusters and PF objects)  
Detector granularity ( $r \lesssim 0.1$ )  
Phenomenological modeling ( $r \lesssim 0.1$ )

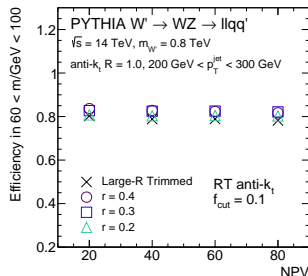
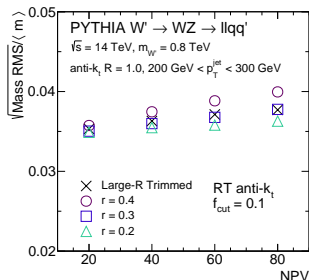
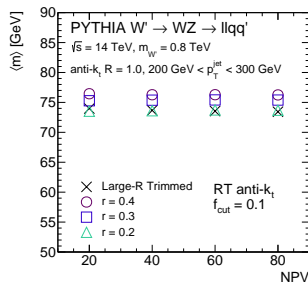


N.B. RT provides for a natural transition between ‘Large’ and ‘small’ radius jets, based on the number of re-clustered (radius  $r$ ) jets.

# Quantitative comparison - small radius $r$

For anti- $k_t$  and  $f_{\text{cut}} = 0.1$ ,

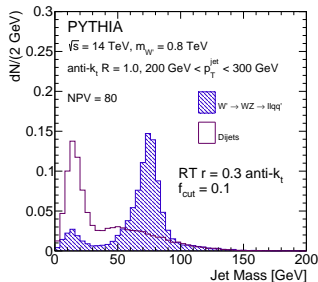
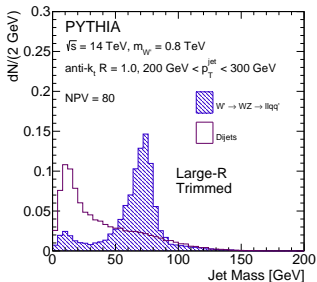
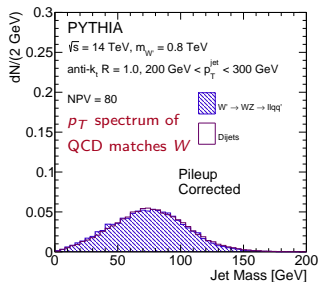
- The average mass is NPV stable
- Window efficiency is NPV stable
- Smaller  $r$  is better in terms of the resolution performance



# Background

So far, focused only on RT when there is hard structure - what about for the QCD background?

- Similar behavior for RT and large  $R$  trimmed.
- Subtle differences that depend on  $f_{\text{cut}}$  and the algorithm.



# Re-clustering and Jet Substructure

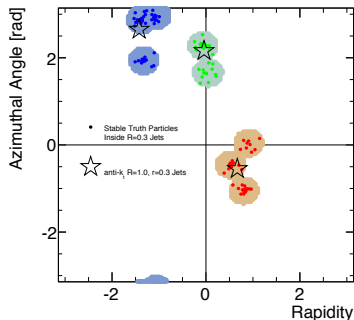
Instead of the **top-down** approach to substructure, in the re-clustering paradigm, there is **bottom-up** substructure.

Some variables come fully calibrated as a result of the re-clustering process:

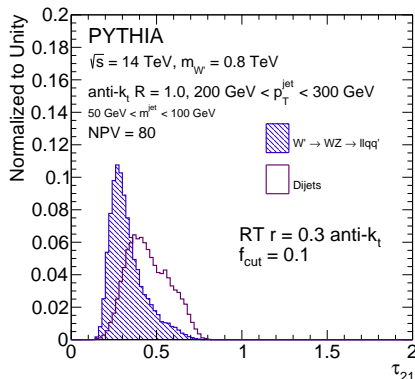
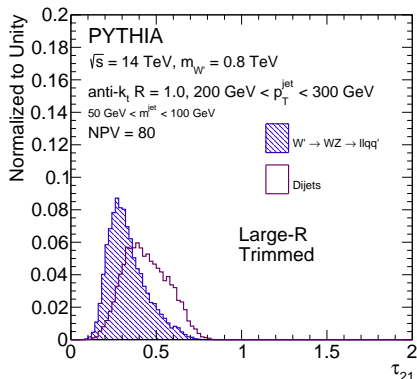
- 1 (Jet Mass)
- 2 Number of subjets
- 3 Number of  $b$ -tagged subjets
- 4  $\sqrt{d_{ij}}$

For other variables, constituents are inherited from the radius  $r$  jets.

- 1  $N$ -subjettiness ratios  $\tau_{ij}$
- 2 Width, energy correlations, pull, etc.



Qualitatively, similar structure when using the trimmed jet constituents and the inherited radius  $r$  constituents in RT.

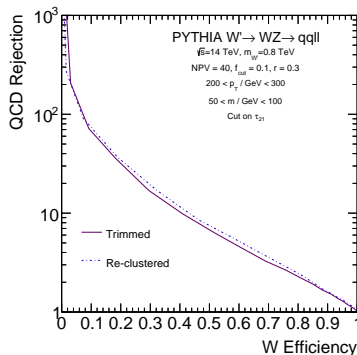




For a fixed signal efficiency, the QCD rejection is very comparable between RT and large  $R$  trimming.

Some information is 'lost' in the removed (sub)jets, which impacts both methods.

**Alternative:** assign constituents by  $\Delta R$   
(drawback: increases pileup sensitivity)



It is expected that for similar parameters, RT and standard trimming will perform similarly - however in practice RT could outperform standard grooming techniques because it can be optimized per  $p_T$  bin.

# Data Storage and Speed

Though not the main motivation, there are further benefits in re-clustering from a computational perspective<sup>†</sup>.

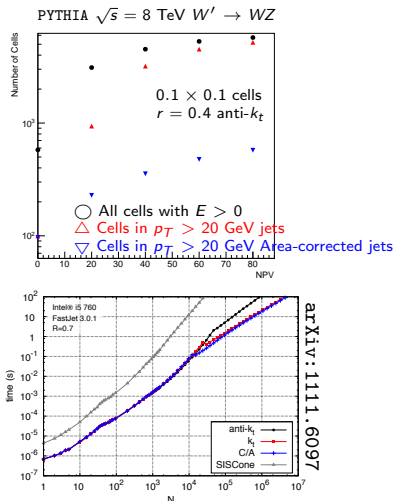
## Storage

After computing  $\rho$ , there is no longer a need to store calorimeter objects not contained inside jets above the  $p_T$  threshold.

## Speed

Fastjet is very fast! But if you have  $m$  algorithms, then  $N \log(N)$  becomes  $MN \log(N)$ , whereas for re-clustering, the additional step takes  $\sim$  no time.

<sup>†</sup>Thanks to T. Farooque, M. Casolino, and A. Juste for pointing us to this side benefit!



# The Next Steps: Validating Calibrations

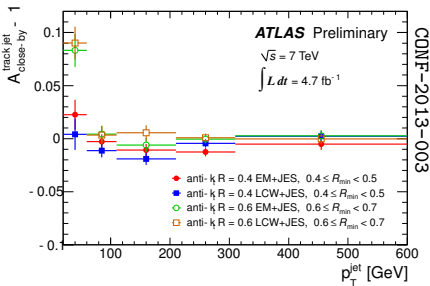
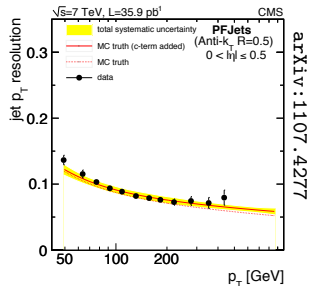
There are two effects which could lead to mis-calibrated re-clustered jets:

**Thresholds** Even though  $\langle p_{T,r}^{\text{reco}} / p_{T,r}^{\text{true}} \rangle = 1$ , a non-zero resolution and a falling  $p_T$  spectrum can induce  $\langle p_{T,R}^{\text{reco}} / p_{T,R}^{\text{truth}} \rangle \neq 1$ .

**Nearby-jets** Inclusively,  $\langle p_{T,r}^{\text{reco}} / p_{T,r}^{\text{true}} \rangle = 1$ , but when jets are very nearby, the response may differ from one on average.

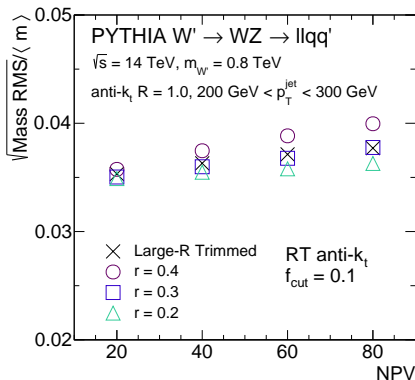
These also impact large  $R$  groomed jets, but can be calibrated away.

→ Requires further study by the experimental collaborations.



## Re-clustering is a very modular paradigm for clustering jets

- The flexibility allows for jet algorithm optimization per analysis
- There is a natural scheme for corrections, calibrations, and uncertainties
- Re-clustering can accommodate jet grooming
- Jet substructure is inherited from the radius  $r$  jets



**Its now up to the experimental collaborations to study re-clustering as an alternative/complement for Run II and beyond!**

# BACKUP