# FIAS Frankfurt Institute for Advanced Studies

# Phase transitions in chiral fluid dynamics including dissipation and noise

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#### Motivation

- The system created in a heavy-ion collision is finite, very dynamic and inhomogeneous.
- Nonequilibrium effects play an important role at the phase transition in heavy-ion collisions.
- We propagate the order parameter of chiral symmetry explicitly. It is coupled to a realistic fluid dynamical description of the expansion of the fireball. These models are called chiral fluid dynamics [1,2].
- We extend chiral fluid dynamics by consistently including dissipation and noise and existing Langevin studies of chiral symmetry [3,4,5] by consistently taking the back reaction of the fields on the finite and dynamic heat bath into account.



#### The quark-meson model

The starting point for the coupled system is the quark-meson model

$$\mathcal{L} = \overline{q} \left[ i \gamma^{\mu} \partial_{\mu} - g \left( \sigma + i \gamma_{5} \tau \vec{\pi} \right) \right] q + \frac{1}{2} (\partial_{\mu} \sigma \partial^{\mu} \sigma) + \frac{1}{2} (\partial_{\mu} \vec{\pi} \partial^{\mu} \vec{\pi}) - U(\sigma, \vec{\pi}) \,.$$

In the mean-field approximation the thermodynamic potential to one-loop level at

#### Time evolution of the coupled system



 $\mu = 0$  is given by

$$\Omega(\sigma, ec{\pi}, T) = U(\sigma, ec{\pi}) - 2d_qT\int rac{\mathrm{d}^3 p}{(2\pi)^3} \ln\left(1 + \exp\left(-rac{E}{T}
ight)
ight)$$
 ,

For a small coupling the transition is a crossover, for g = 3.63 the potential becomes flat at  $T_c = 139.88$  MeV (critical point). For g = 5.5 one finds two degenerate minima at  $T_c = 123.27$  MeV (first order phase transition).



#### **Coupled dynamics**

Within the formalism of the 2PI effective action one can selfconsistently [6,7] derive the dynamics of the  $\sigma$  mean field and the quark fluid [8]. The  $\sigma$  field is propagated according to a Langevin equation

 $\partial_{\mu}\partial^{\mu}\sigma + \frac{\delta U}{\delta\sigma} + g\rho_{s} + \eta\partial_{t}\sigma = \xi$ with a damping term  $\eta$  and the noise field  $\xi$ . For  $\mathbf{k} = 0$  $\eta = g^{2}\frac{d_{q}}{\pi}\left(1 - 2n_{\mathrm{F}}(\frac{m_{\sigma}}{2})\right)\frac{(\frac{m_{\sigma}^{2}}{4} - m_{q}^{2})^{\frac{3}{2}}}{m_{\sigma}^{2}}$ 

 $\langle \tilde{\xi}(t)\tilde{\xi}(t')\rangle = \frac{1}{V}\delta(t-t')m_{\sigma}\eta \coth\left(\frac{m_{\sigma}}{2T}\right)$ .



Figure: The relaxation of the  $\sigma$  field and its fluctuations averaged over an inner sphere. In a scenario with a first order phase transition the  $\sigma$  field relaxes more slowly than for a scenario with a critical point, where we see oscillations due to the vanishing damping at the phase transition [10].



Below  $T_c$ : damping by the interaction with the hard pions  $\eta = 2.2/\text{fm}$  [4]. The quark fluid evolves according to energy-momentum conservation. Here, approximation of an ideal fluid:

$$\partial_{\mu}T_{q}^{\mu\nu}=S$$

The source term describes the energy dissipation from the field to the fluid

$$\partial_{\mu} T^{\mu\nu}_{\sigma} = -(\mathbf{g}\rho_{s} + \eta\partial_{t}\sigma)\partial^{\nu}\sigma$$

and the energy flow from the fluid to the field provided by the noise field  $\xi$ . It is obtained from the total energy of the field [9]

 $E_{\sigma} = 1/2\partial_t \sigma^2 + 1/2\vec{\nabla}\sigma^2 + U(\sigma)$ 

Figure: The time evolution of the temperature of the quark fluid and its fluctuations averaged over an inner sphere. During the relaxational process of the  $\sigma$  field one observes the reheating effect in a scenario with a first order phase transition [10].

### Intensity of $\sigma$ fluctuations







Figure: Deviation of the  $\sigma$  field from equilibrium for a scenario with a critical point and a first order phase transition [10].

## $t/{ m fm}$

Figure: The intensity of  $\sigma$  fluctuations in a critical point scenario [10].

 $t/\mathrm{fm}$ 

Figure: The intensity of  $\sigma$  fluctuations in a scenario with a first order phase transition [10].

#### **References**

[1] I. N. Mishustin and O. Scavenius, Phys. Rev. Lett. 83 (1999) 3134.
[2] K. Paech, H. Stoecker and A. Dumitru, Phys. Rev. C 68 (2003) 044907.
[3] C. Greiner and B. Muller, Phys. Rev. D 55 (1997) 1026.
[4] T. S. Biro and C. Greiner, Phys. Rev. Lett. 79 (1997) 3138.
[5] D. H. Rischke, Phys. Rev. C 58 (1998) 2331.
[6] J. M. Luttinger, J. C. Ward, Phys. Rev. 118 (1960) 1417-1427.
[7] G. Baym, L. P. Kadanoff, Phys. Rev. 124 (1961) 287-299.
[8] MN, S. Leupold, C. Herold, M. Bleicher, [arXiv:1105.0622 [nucl-th]].
[9] MN, S. Leupold, M. Bleicher, [arXiv:1105.1396 [nucl-th]].
[10] MN, M. Bleicher, S. Leupold, I. Mishustin, [arXiv:1105.1962 [nucl-th]].

#### Summary

We presented a model of chiral fluid dynamics which consistently includes damping and noise.
Energy-momentum conservation is obtained by taking the back reaction on the heat bath into account.
We observed the nonequilibrium effects of supercooling and reheating.
Enhanced *σ* fluctuations at the first order phase transition were found.





