

Higher Harmonic Jet Tomography as a Probe of Fluctuating Initial Condition Geometries in A+A

Barbara Betz

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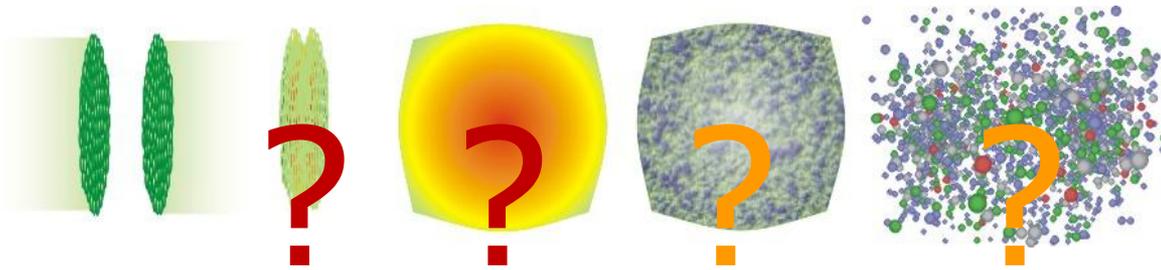


Alexander von Humboldt
Stiftung/Foundation

[arXiv:1102.5416 \[nucl-th\]](https://arxiv.org/abs/1102.5416)



Motivation



S. Bass, Talk Quark Matter 2001

→ Two basic questions:

- Is the medium weakly-coupled (pQCD) or strongly-coupled (AdS/CFT)?
- What are the initial conditions (Glauber or CGC)?

→ Two observables characterizing the medium:

- jet quenching: signal for creation of opaque matter (QGP)

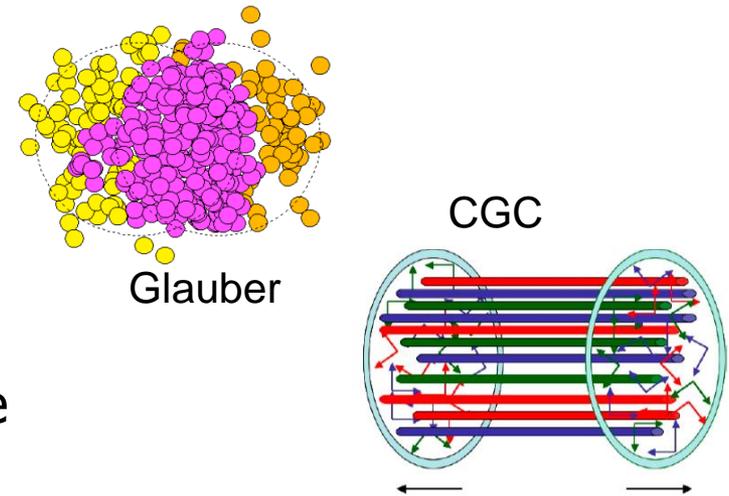
defined via:
$$R_{AA}(p_T) = \frac{1/\sigma_{A+A} d\sigma^{A+A}/dp_T}{\langle N_{\text{coll}} \rangle / \sigma_{p+p} d\sigma^{p+p}/dp_T}$$

- elliptic flow: signal for creation of a (nearly) perfect fluid

defined via:
$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left[1 + 2 \sum_{n=1}^{\infty} v_n \cos(n\phi) \right]$$

The Connection

- Glauber Model and CGC differ by:
 - initial temperature gradients
 - initial high- p_T parton distribution
 - distance travelled by each parton
 leading to a different opacity estimate



- Elliptic flow is sensitive to the path length dependence of energy loss, scaling as $dE/dx \sim |z|$:

$z=1$: pQCD

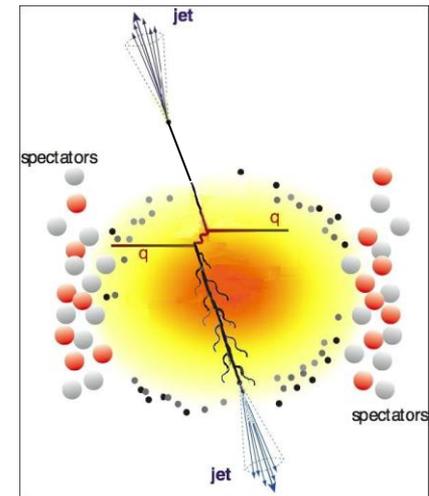
M. Gyulassy et. al., PRL **85** (2000), 5535

$z=2$: AdS/CFT (on-shell partons)

$z>2$: AdS/CFT (**off-shell** partons)

S. Gubser et. al., JHEP **0810** (2008), 052;

P. Chesler et.al., PRD **79** (2009) 125015



Energy-Loss Mechanisms

- First investigation of $R_{AA}(N_{part})$ and $v_2(N_{part})$ for $p_T > 5$ GeV hadrons is based on

J. Jia et. al., PRC **82** (2010), 024902

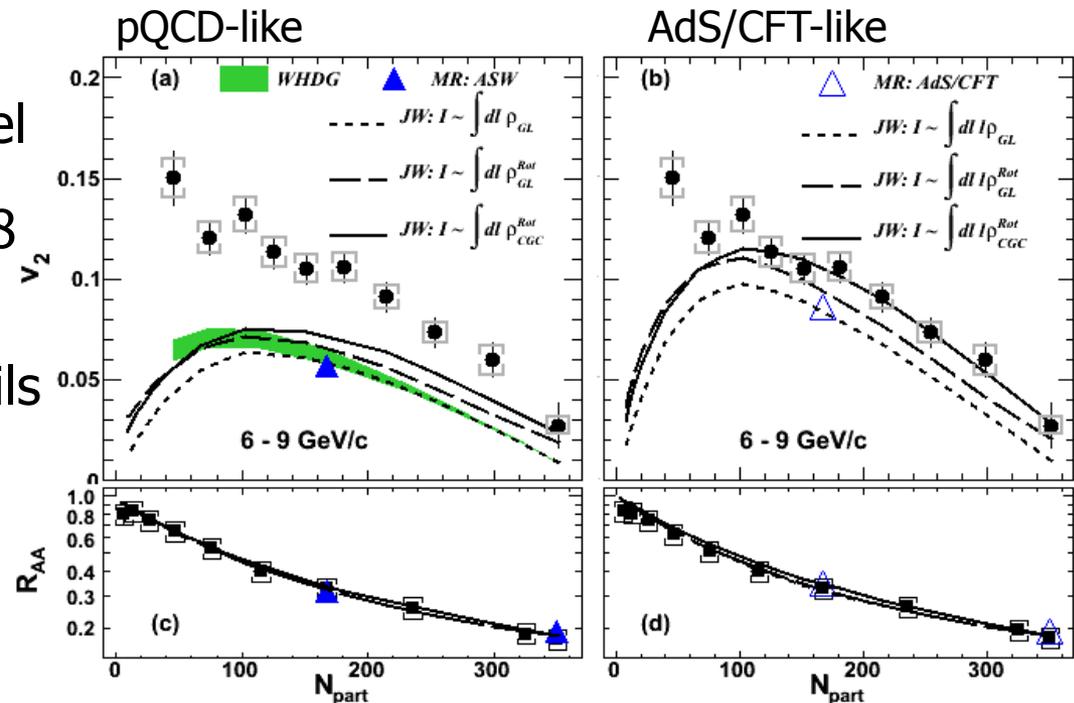
$$R_{AA}(N_{part}) = \langle e^{-\kappa I_m} \rangle$$

$$I_m = \int_0^\infty dl l^{m-1} \rho(\vec{r} + l\hat{v}), m = 1, 2, \dots$$

$$v_2 = \langle e^{-\kappa I} \cos 2(\phi - \Psi_{part}) \rangle$$

→ simple jet absorption model

- Once $R_{AA}(N_{part}=350) \sim 0.18$ for 0-5% π^0 data
 - pQCD-like energy loss fails to reproduce $v_2(N_{part})$
 - AdS/CFT-like energy loss describes data for CGC initial conditions



A. Adare et al, Phys. Rev. Lett. **105**, 142301 (2010)

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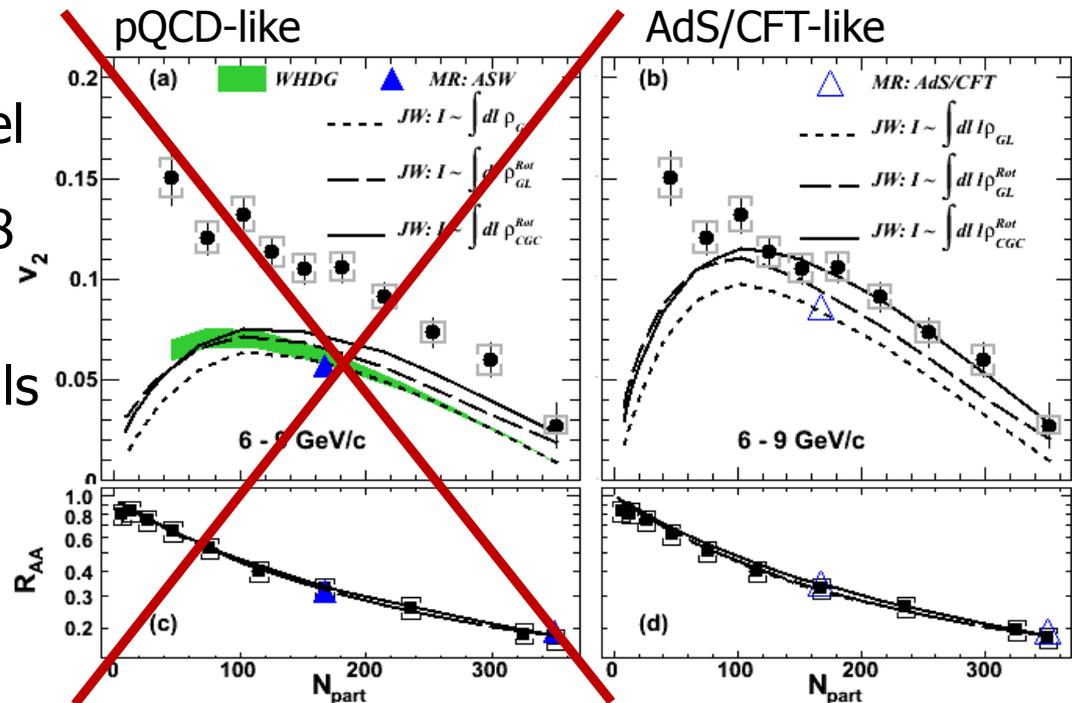
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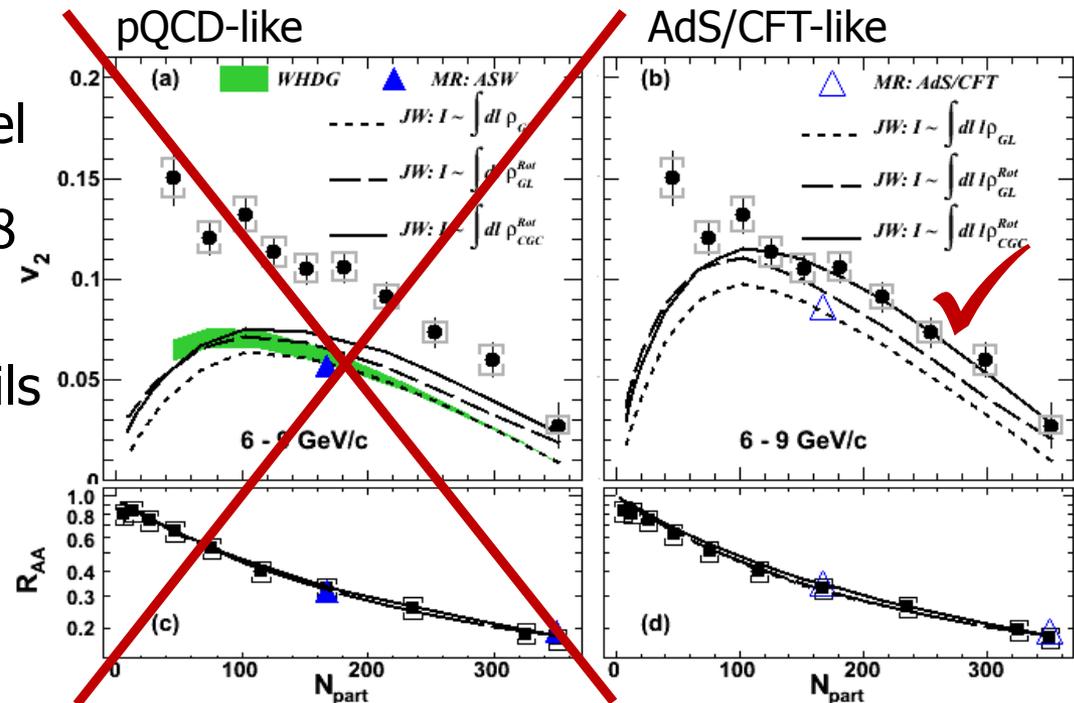
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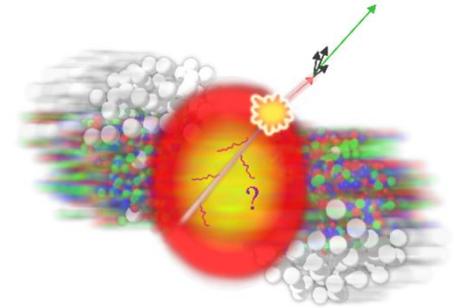
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A. Adare et al, Phys. Rev. Lett. 105, 142301 (2010)

Choosing an ansatz for the energy loss

$$\frac{dE}{dx}(\vec{x}_0, \phi, \tau) = -\kappa P^a \tau^z T^{z-a+2}[\vec{x}_0 + \hat{n}(\phi)\tau, \tau]$$



P : momentum of the jet(s)

a, z : parameters controlling the jet-energy and path-length dependence

κ : being fixed thus that $R_{AA}(N_{\text{part}}=350) \sim 0.18$ for most central data

and considering Bjorken expansion via

$$T(\vec{x}, \tau) = T_0(\vec{x}) \left(\frac{\tau_0}{\tau} \right)^{1/3}$$

$\tau_0 = 1\text{fm}$, one can determine the $R_{AA}(N_{\text{part}})$ & $v_n(N_{\text{part}})$

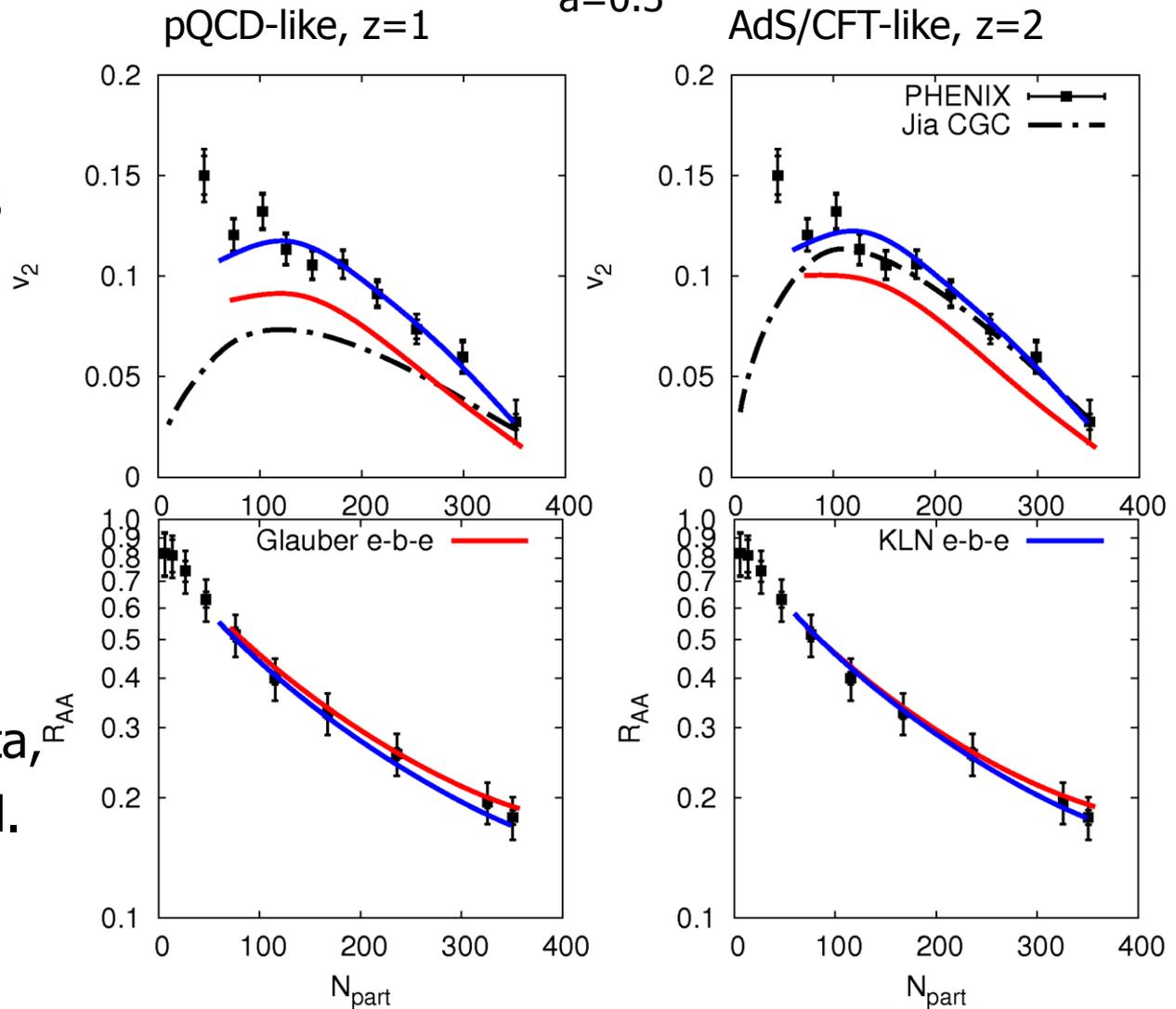
R_{AA} and v_2

→ Having fixed κ for $R_{AA}(N_{part}=350) \sim 0.18$
 $R_{AA}(N_{part})$ can be reproduced

→ $z=1$: CGC in. cond. close to data
 $z=2$: CGC in. cond. still describe data, R_{AA} Glauber in. cond. getting closer

⇒ **NO** striking big difference between pQCD and AdS/CFT

$a=0.3$



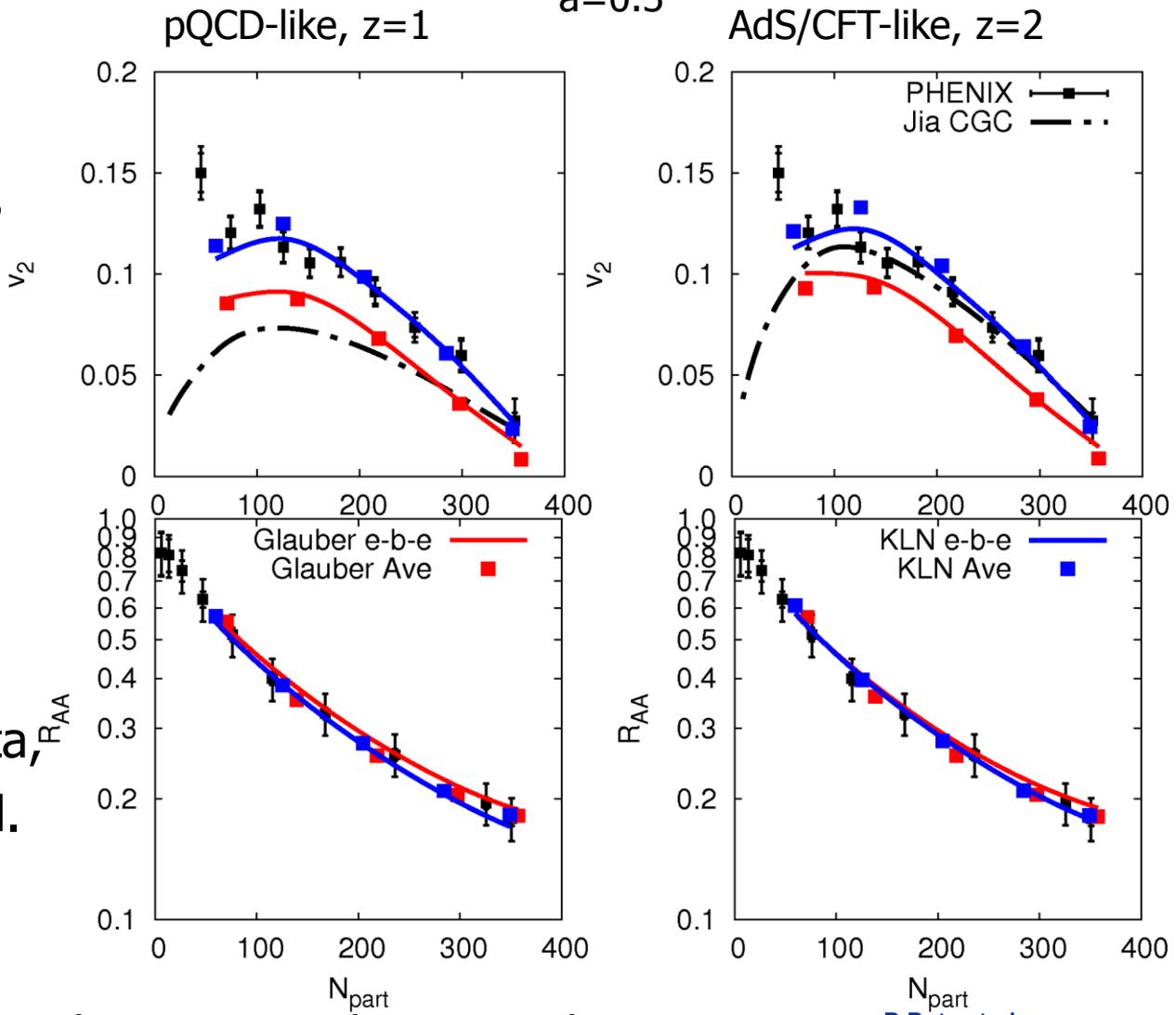
N_{part}
 B.Betz et al.,
 arXiv:1102.5416 [nucl-th]

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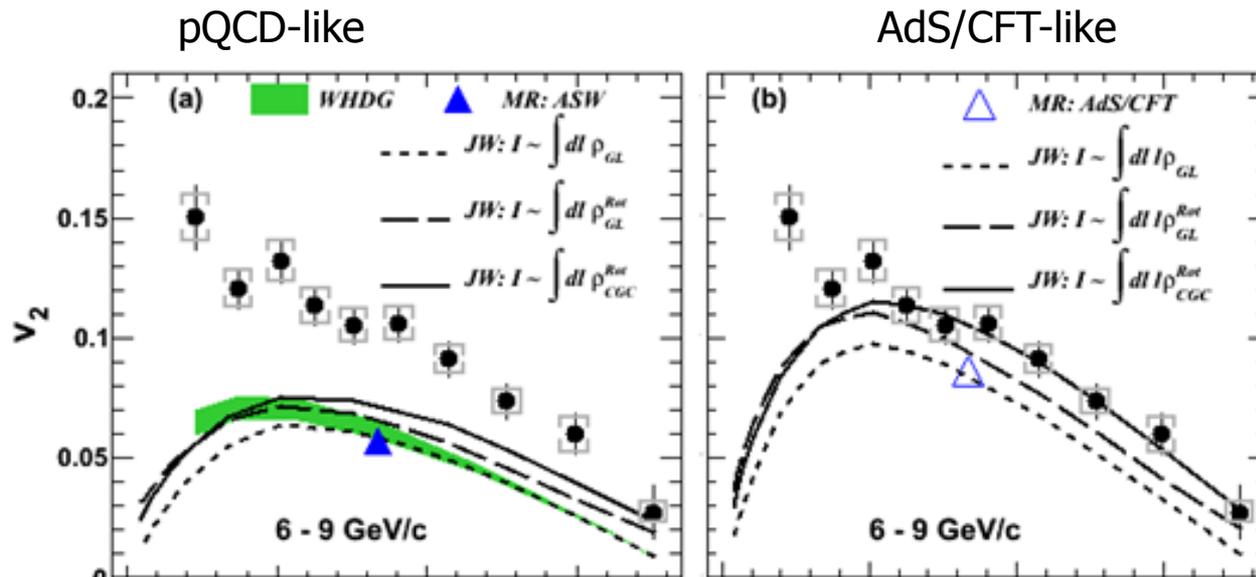


⇒ Similar results for event-by-event and averaged scenarios!

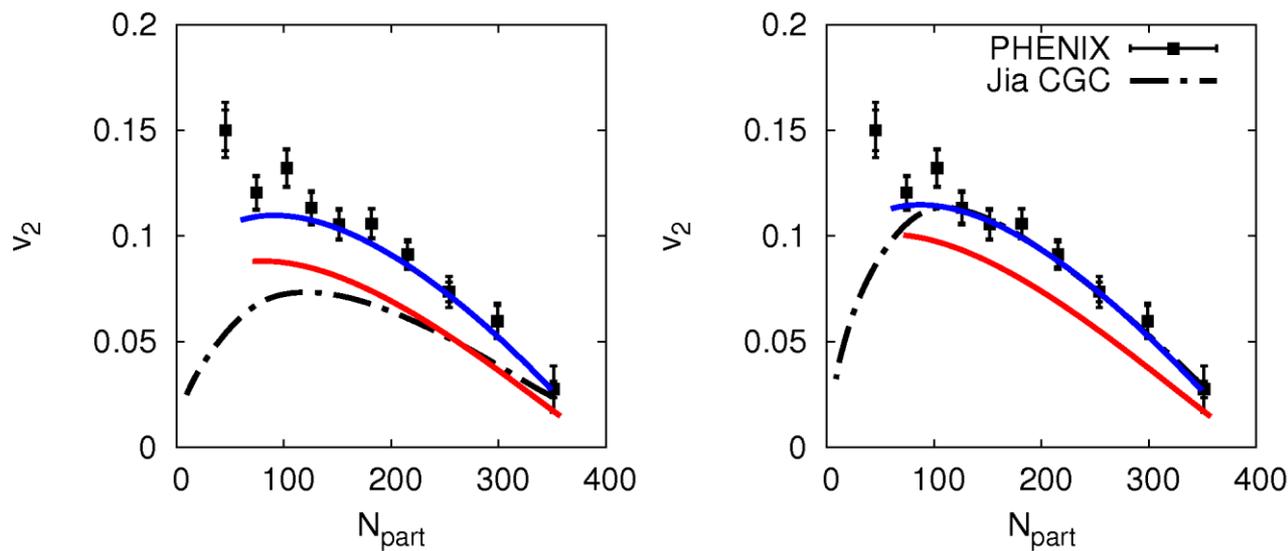
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Differences

Adare et al, Phys. Rev. Lett.
105, 142301 (2010)



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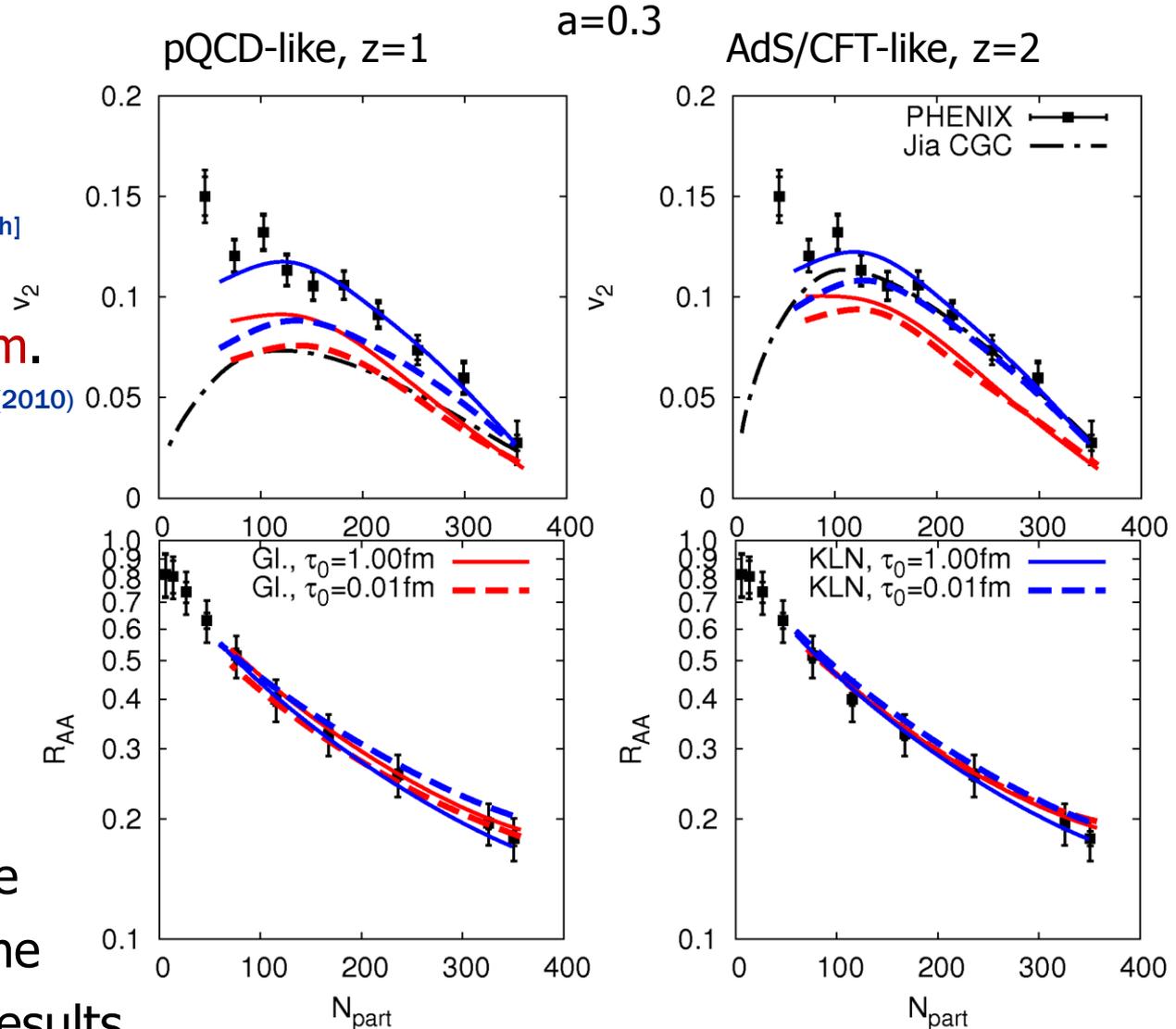


Initial time

- We chose $\tau_0 = 1\text{fm}$.
H. Song et al., arXiv:1011.2783[nucl-th]

- Jia's model has $\tau_0 = 0\text{fm}$.
A. Adare et al, Phys. Rev. Lett. **105**, 142301 (2010)

⇒ A smaller τ_0 reduces the $v_2(N_{\text{part}})$ for both pQCD-like and AdS/CFT-like energy loss and increases the difference between the pQCD and AdS/CFT results



B. Betz et al., in preparation

The role of τ_0

$\tau_0 = 1\text{fm} \rightarrow$ **Assumption**: NO energy loss within 1fm

- pQCD does not give excuse for this ansatz,

$\tau_0 = 0\text{fm}$ most natural assumption

Adare et al, Phys. Rev. Lett. **105**, 142301 (2010)

- describes formation time of hydrodynamics

\rightarrow no pressure at early times, everything is free flow

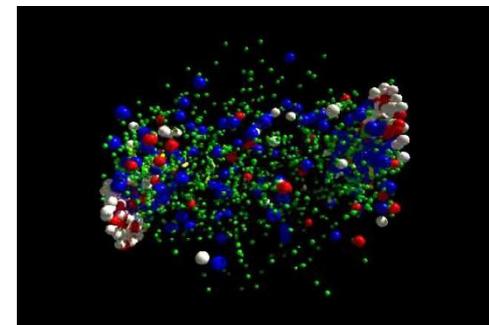
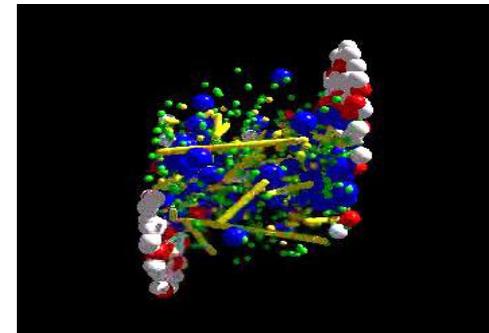
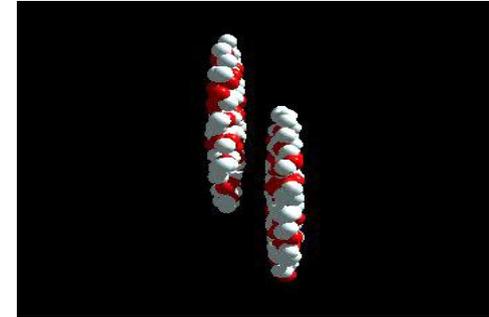
$\tau_0 = 1\text{fm} \rightarrow$ essentially **equivalent** to AdS/CFT

energy loss suppression of early times

- AdS/CFT: $dE/dx \sim l^2$ accounts for absence of energy loss $< 1\text{fm}$.

$\Rightarrow v_2(\text{high- } p_T)$ **not** sensitive to long distance $dE/dx \sim l^1$
 vs. $dE/dx \sim l^2$, **but** to short distance properties $< 1\text{fm}$!

\Rightarrow **Only** the corona is seen!

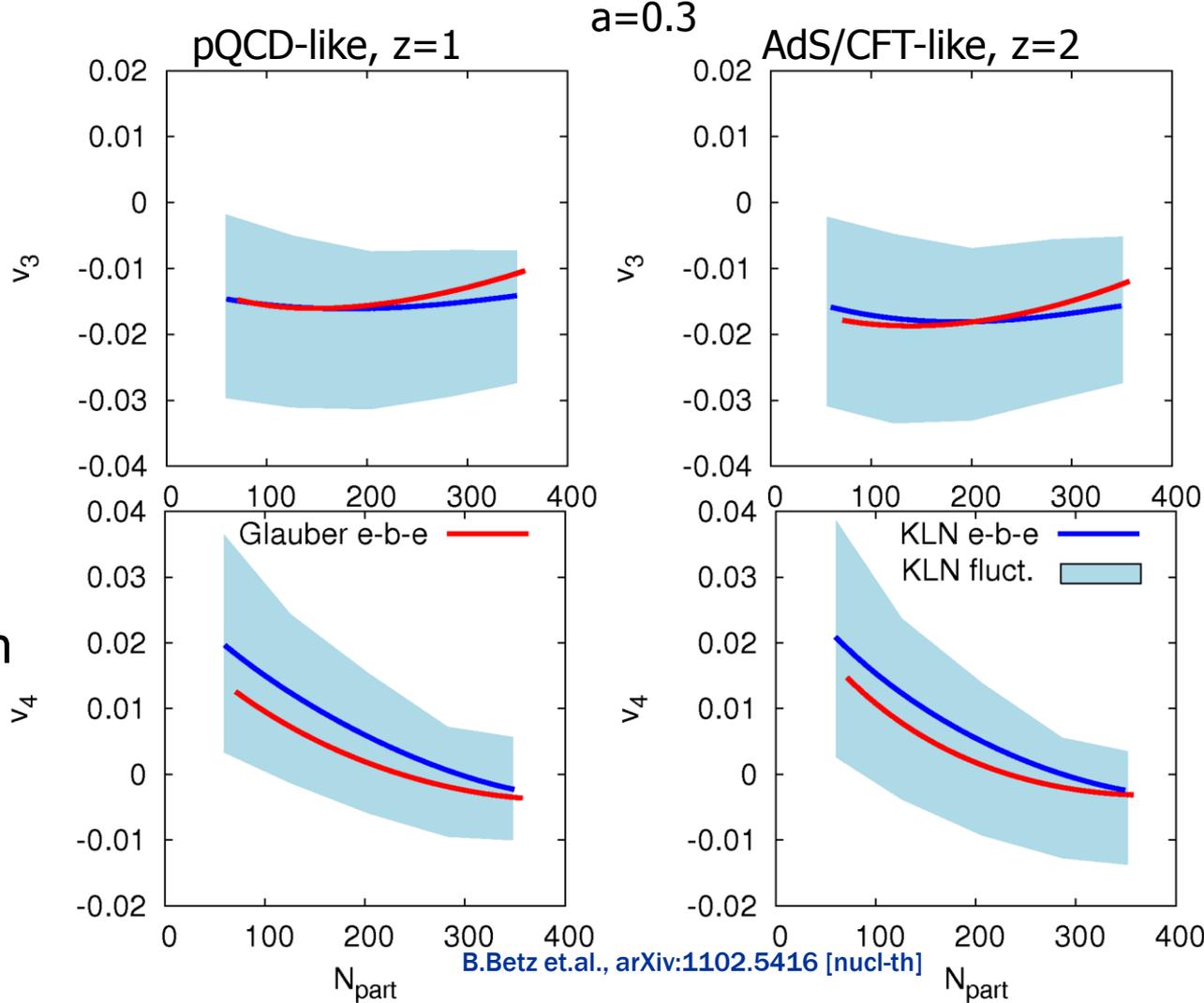


UrQMD Simulation, H. Weber

Higher Harmonics

v_3 and v_4 similar for Glauber and KLN initial conditions

→ **Not** suitable to distinguish between Glauber and CGC initial conditions



→ Higher harmonics are more sensitive to local gradients, but also to event-by-event fluctuations → larger $v_{3,4}$ fluctuations

B.Betz et al., arXiv:1102.5416 [nucl-th]

Fragmentation

Nuclear modification factor

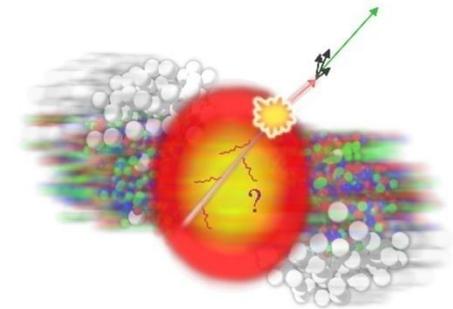
$$R_{AA}^{\pi}(p_{\pi}) = \frac{\sum_{\alpha=q,g} \int_{z_{min}}^1 \frac{dz}{z} d\sigma_{\alpha} \left(\frac{p_{\pi}}{z} \right) R_{AA}^{\alpha} \left(\frac{p_{\pi}}{z} \right) D_{\alpha \rightarrow \pi} \left(z, \frac{p_{\pi}}{z} \right)}{\sum_{\alpha=q,g} \int_{z_{min}}^1 \frac{dz}{z} d\sigma_{\alpha} \left(\frac{p_{\pi}}{z} \right) D_{\alpha \rightarrow \pi} \left(z, \frac{p_{\pi}}{z} \right)}$$

z : momentum of the observed pion

p_{π} : fractional momentum of the quarks and gluons

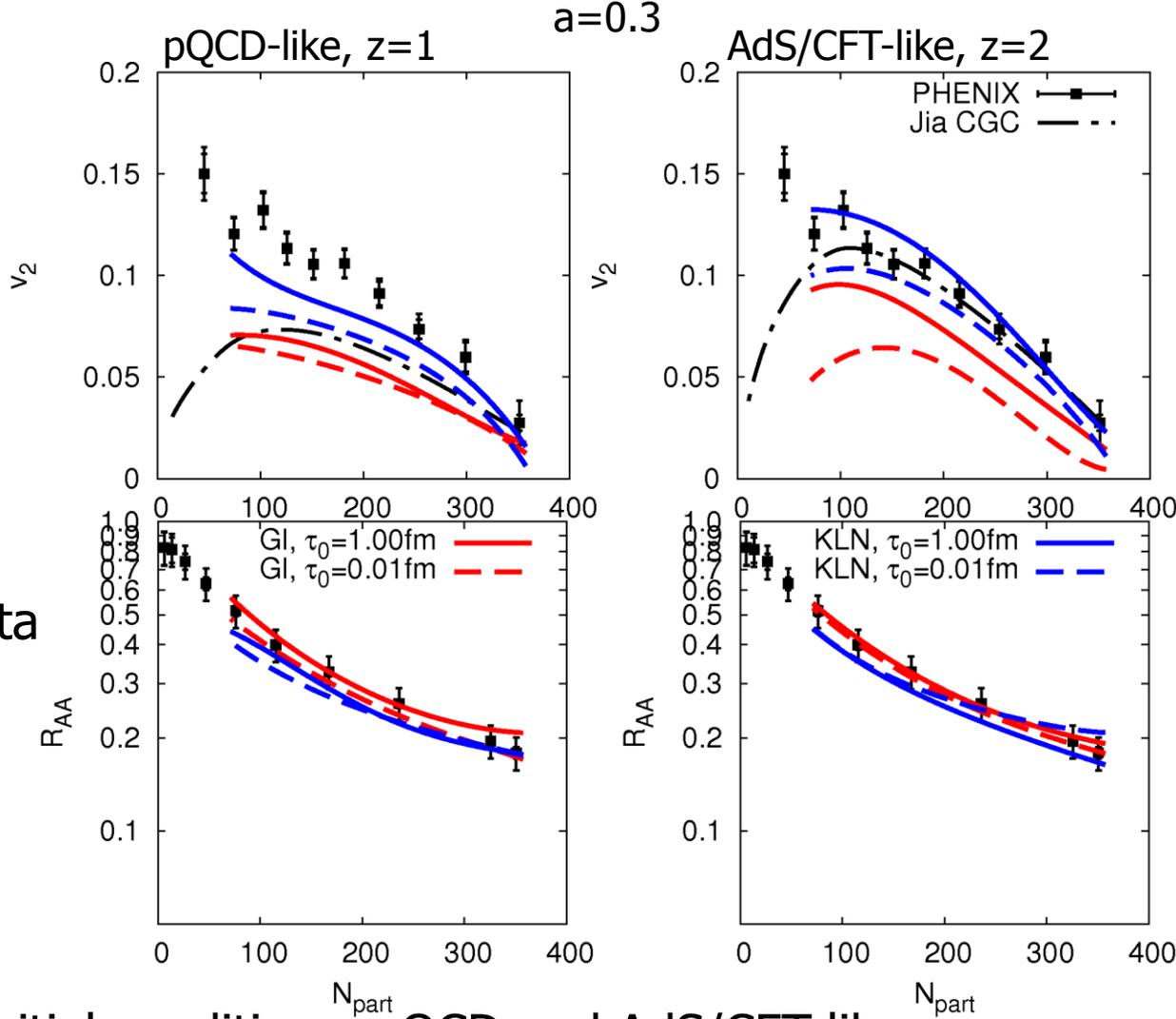
$d\sigma_{\alpha} \left(\frac{p_{\pi}}{z} \right)$: fitted pQCD cross-sections for quarks and gluons

$D_{\alpha \rightarrow \pi} \left(z, \frac{p_{\pi}}{z} \right)$: fragmentation functions for quarks and gluons



R_{AA} and v_2 for π 's

- $R_{AA}(N_{part})$ can be described
- $z=1$: CGC in. cond. close to data, Glauber fails to describe v_2 data
- ⇒ A smaller τ_0 reduces the $v_2(N_{part})$



⇒ For $\tau_0=1\text{fm}$ and CGC initial conditions, pQCD and AdS/CFT-like energy loss close to the data

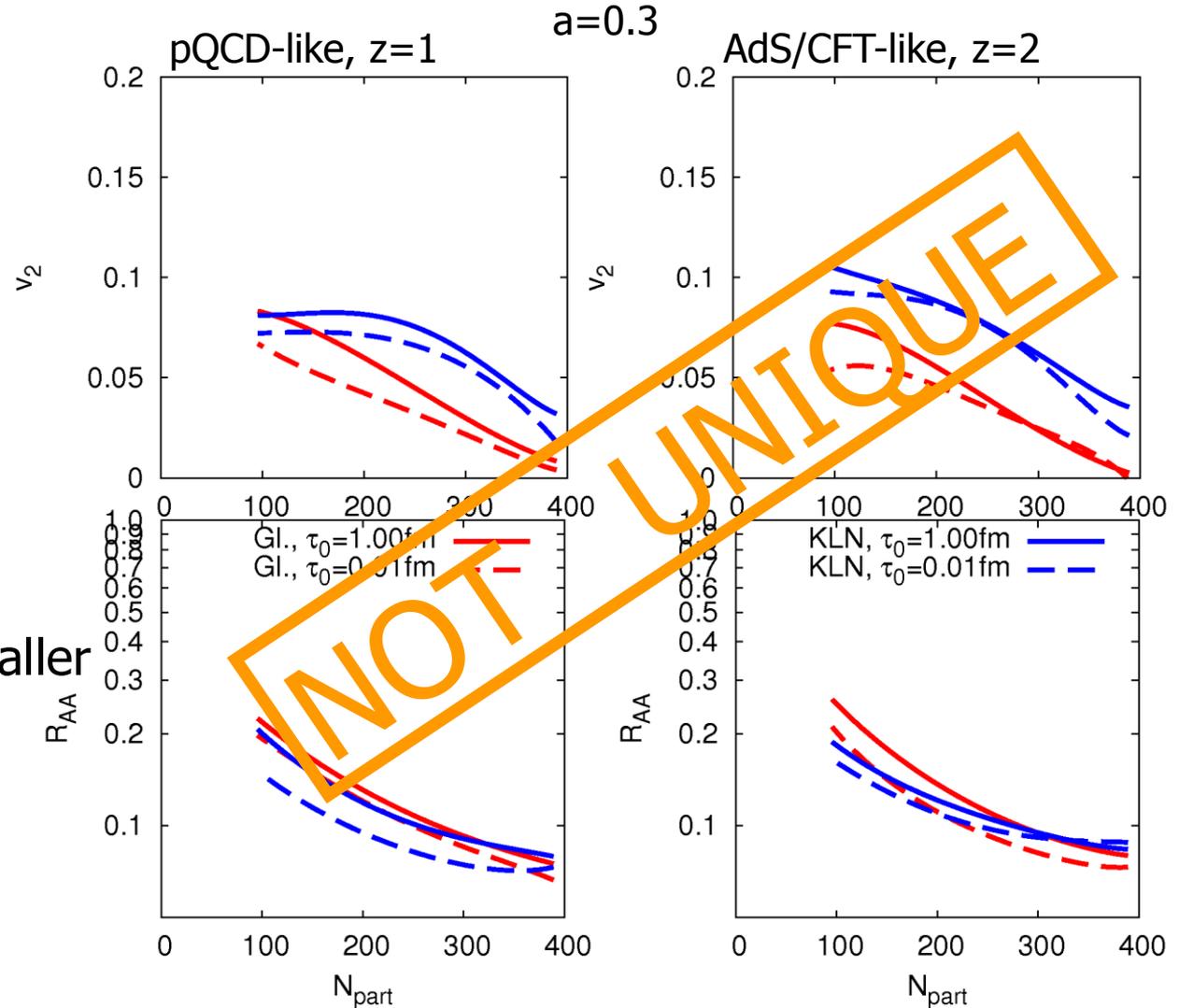
B.Betz et.al., in preparation

LHC conditions for π 's

→ $R_{AA}(N_{part})$ decreases as a function of energy

→ CGC in. cond. lead to larger v_2

→ CGC- v_2 flattens for smaller N_{part}



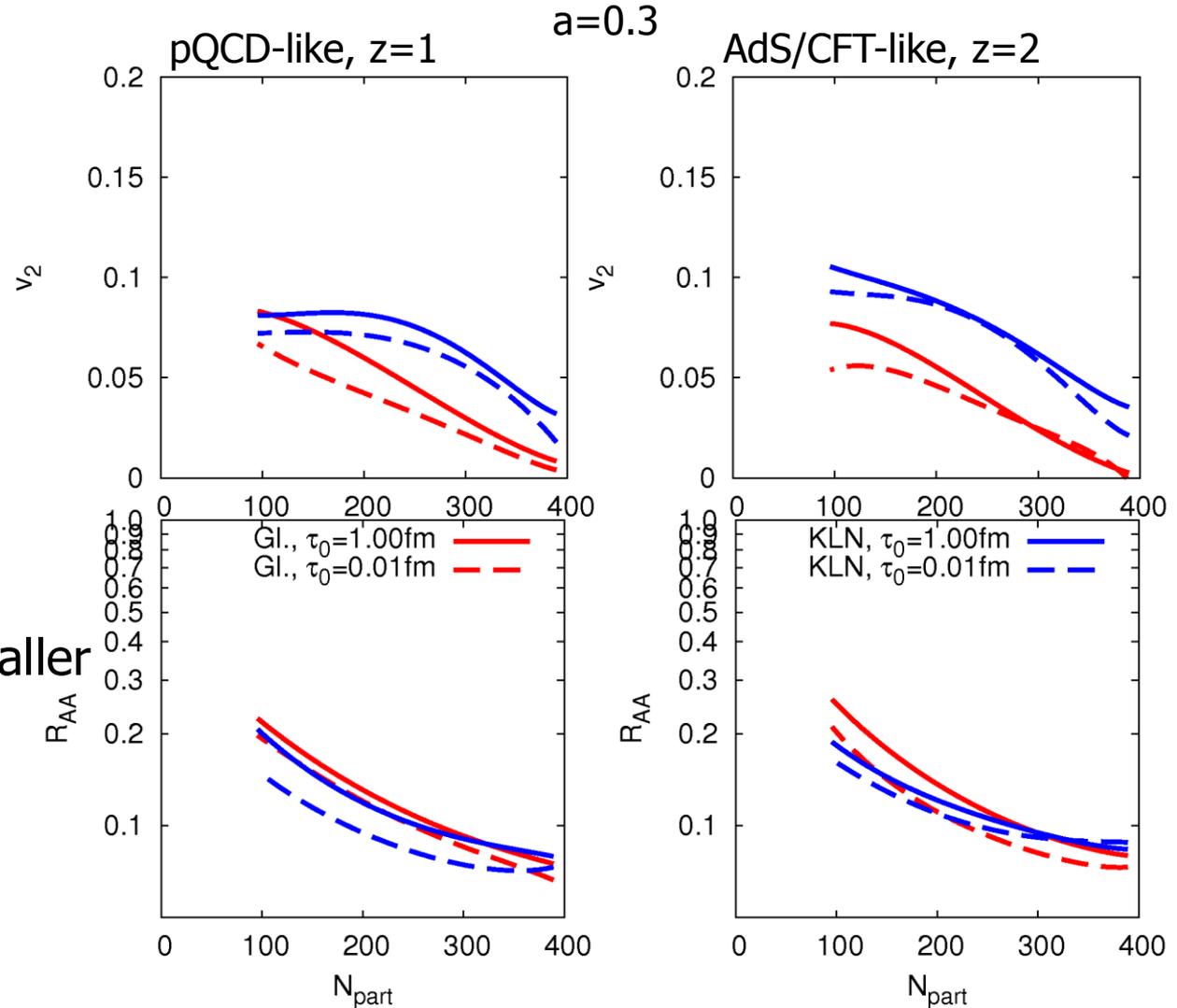
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B.Betz et.al., in preparation

LHC conditions for π 's

ALICE:

R. Snellings, $v_2\{SP\}$, p.17 v_2

H. Appelshäuser, $\pi^{+/-}$, p.24

ATLAS:

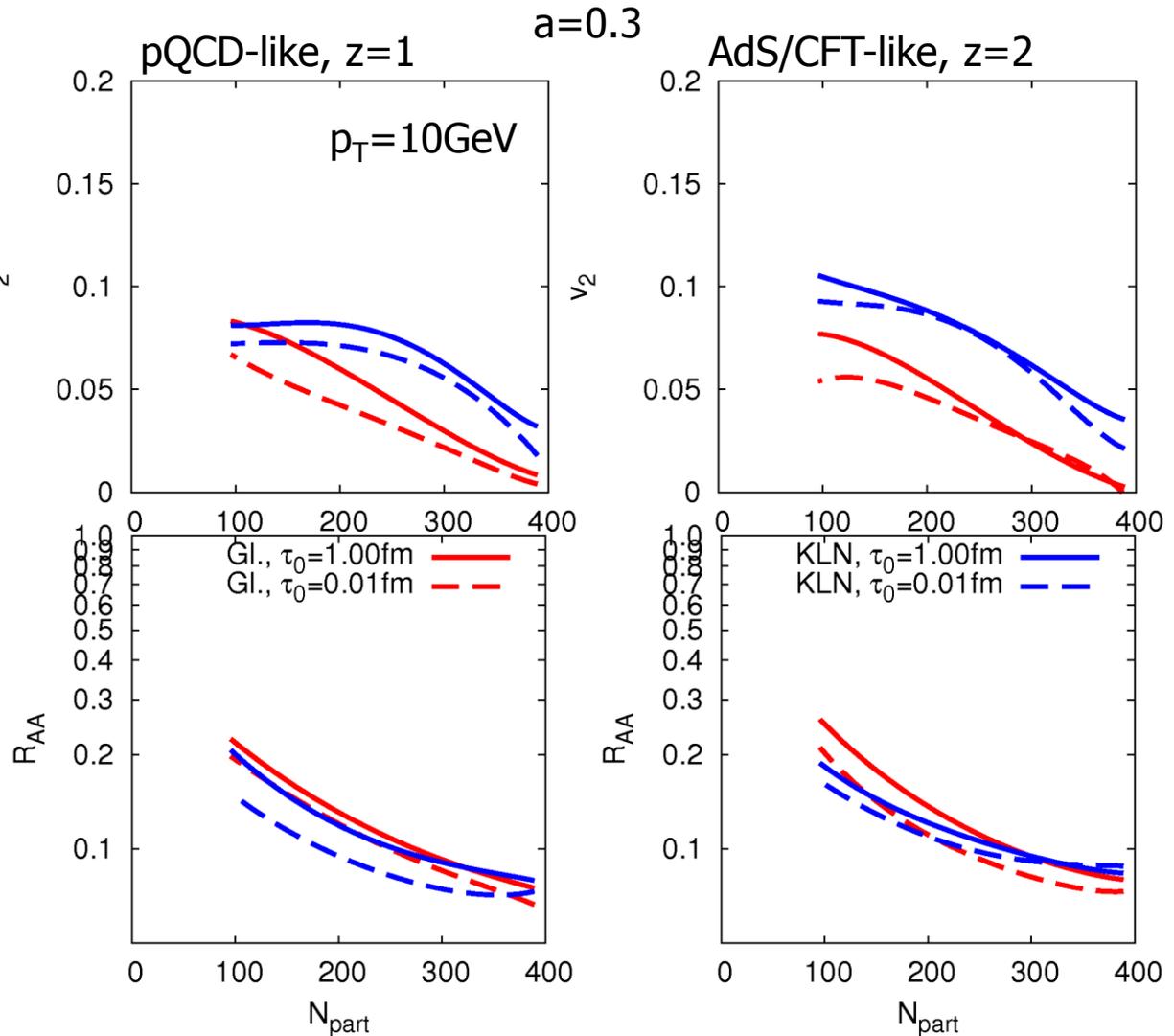
J. Jia, $h^{+/-}$, p.10

CMS:

J. Velkovska, $v_2\{EP\}$, p.8

Y.-J. Lee, $h^{+/-}$, p.26

$p_T \sim 9.5\text{GeV}$



B.Betz et.al., in preparation

LHC conditions for π 's

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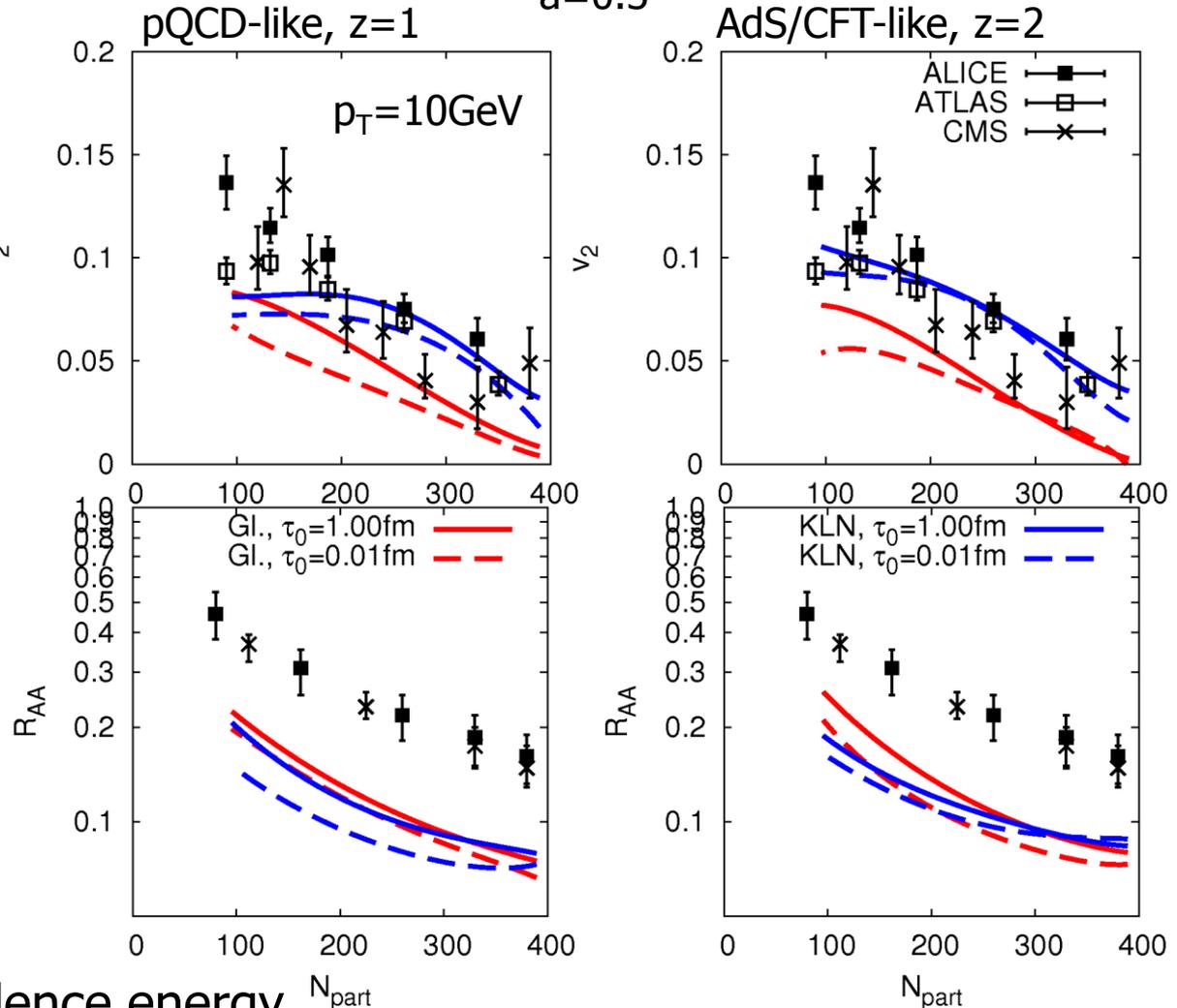
Y.-J. Lee, $h^{+/-}$, p.26

$p_T=9.5\text{GeV}$

→ Puzzle: Density dependence energy N_{part}

loss fails to describe R_{AA} (WHDG/DGLV)

$a=0.3$



B.Betz et al., in preparation

Talk W. Horowitz, QM 2011

W. Horowitz et al., arXiv:1104.4958[hep-ph]

Conclusions

- Introduced a generic energy loss model, exploring $dE/dx \sim P^a$ and l^z with a dimensionless coupling κ
- gets close to the $v_2(N_{\text{part}})$ data in the pQCD-case for KLN initial conditions for $\tau_0 = 1\text{fm}$ at RHIC energies, even after fragmentation
- Discussed the role of the initial time τ_0
 - ⇒ $v_2(\text{high- } p_T)$ @ RHIC is sensitive to short distance properties $< 1\text{fm}$,
 - ⇒ suggesting that either weak coupling + $\tau_0 \sim 1\text{fm}$ or strong coupling
 - ↳ features energy loss suppression at early times
 - ⇒ Only the corona is seen (RHIC)
 - ⇒ Puzzle: Density dependence energy loss fails to describe R_{AA} @LHC

Backup

Nuclear modification factor

$$R_{AA}(\vec{x}_0, \phi, N_{part}) = \exp[-\chi(\vec{x}_0, \phi, P_f)]$$

with

$$\chi(\vec{x}_0, \phi, P_f) = \left(\frac{1 + a - n}{1 - a} \right) \ln \left[1 - \frac{K}{P_0^{1-a}} I(a, z, \phi, \vec{x}_0) \right]$$

$$I(a, z, \phi, \vec{x}_0) = \int_{\tau_0}^{\infty} \tau^z T^{z-a+2}[\vec{x}_0 + \hat{n}(\phi)\tau, \tau] d\tau$$

$n \sim 6$: spectral index

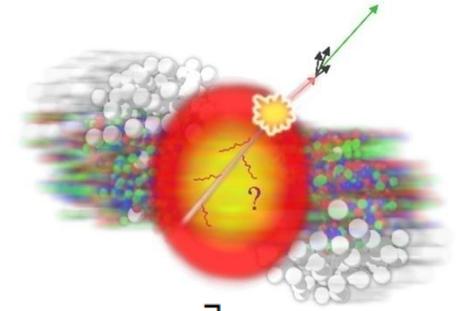
$K = \kappa (1-a)$

$$R_{AA}(N_{part}) = \frac{\int R_{AA}(\vec{x}_0, \phi) T_{AA}(\vec{x}_0) d\vec{x}_0 d\phi / (2\pi)}{\int T_{AA}(\vec{x}_0) d\vec{x}_0}$$

T_{AA} : Glauber

$T_{AA} = \rho^2 / P_0^2$: CGC

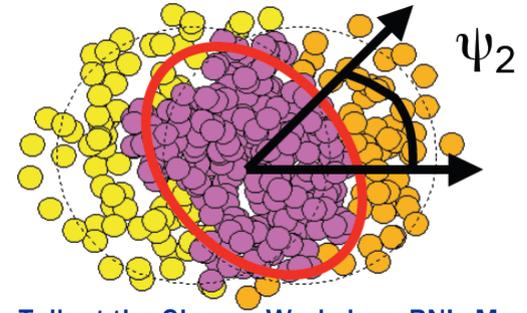
H. Drescher et. al., PRC 76 (2007) 024905



Generic Energy Loss Model COLUMBIA UNIVERSITY IN THE CITY OF NEW YORK

Having fixed κ , the harmonics can be calculated

$$v_n(N_{part}) = \frac{\int d\phi \cos \{n [\phi - \psi_n]\} R_{AA}(\phi)}{\int d\phi R_{AA}(\phi)}$$



B. Alver, Talk at the Glasma Workshop, BNL, May 2010

determining the angle with the reaction plane

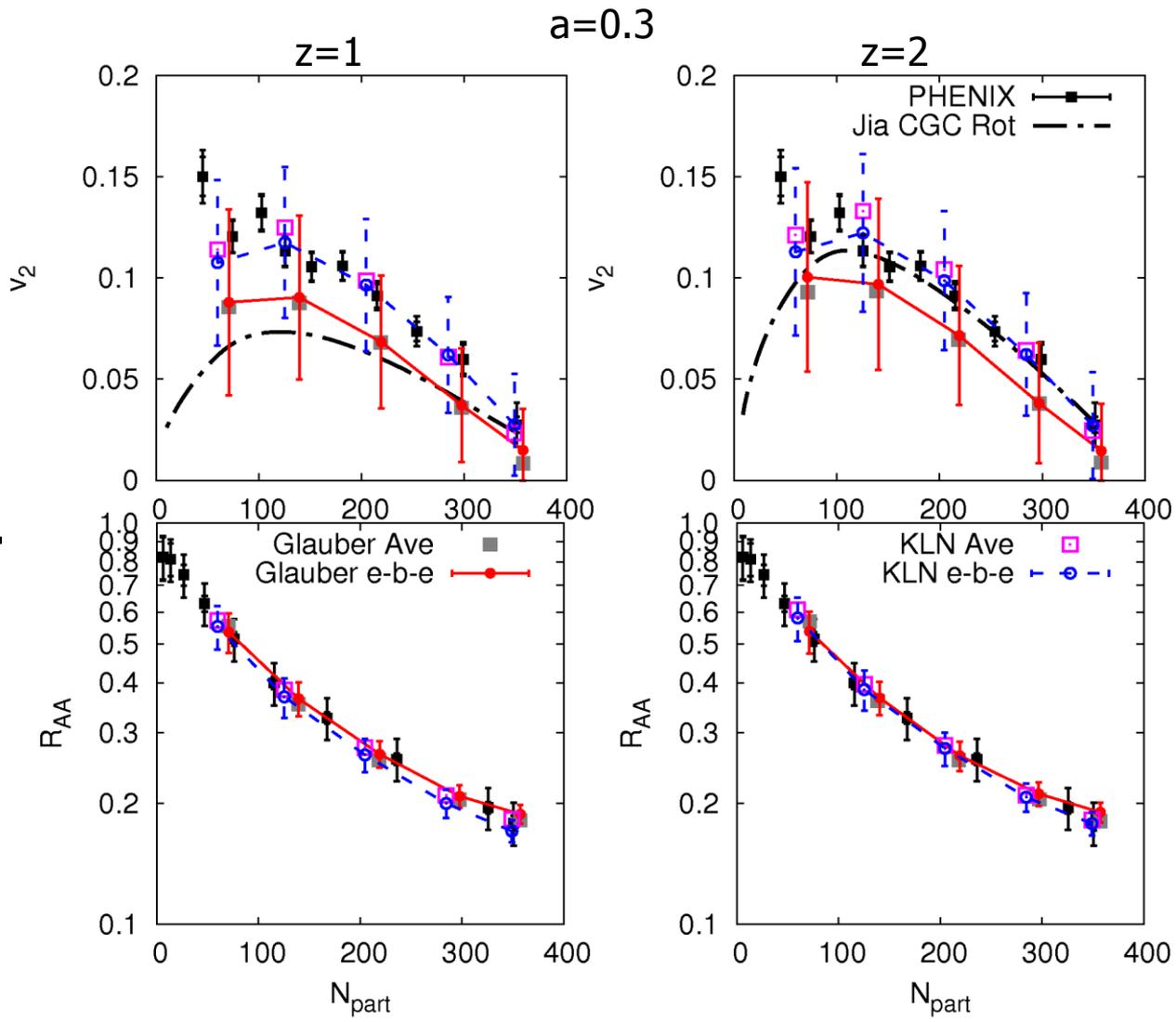
$$\psi_n(t) = \frac{1}{n} \tan^{-1} \frac{\langle r \sin(n\phi) \rangle}{\langle r \cos(n\phi) \rangle}$$

and the Fourier density components are given by

$$e_n(t) = \frac{\sqrt{\langle r^2 \cos(n\phi) \rangle^2 + \langle r^2 \sin(n\phi) \rangle^2}}{\langle r^2 \rangle}$$

R_{AA} and v_2

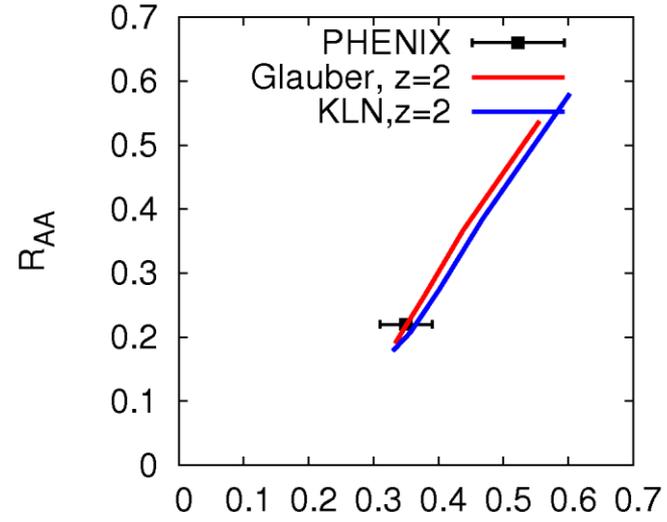
- Having fixed κ for $R_{AA}(N_{part}=350) \sim 0.18$
 $R_{AA}(N_{part})$ can be reproduced
- $z=1$: CGC in. cond. close to data
- $z=2$: Glauber in. cond. getting closer
- Small fluctuations for $R_{AA}(N_{part})$
 large fluctuations for $v_2(N_{part})$
- **Not** straightforward to distinguish between initial conditions



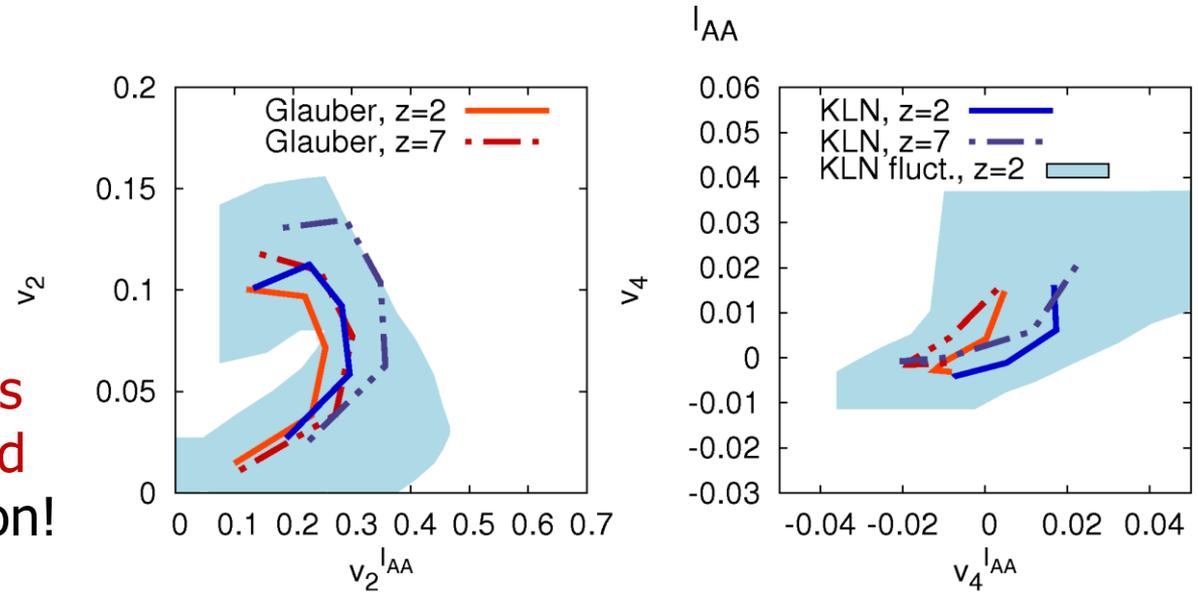
B.Betz et al., arXiv:1102.5416 [nucl-th]

R_{AA} vs. I_{AA} , and v_n vs. v_n^{IAA}

- Extend to dijet analysis, **but** considering $\kappa_{away} = \kappa$
 - In contrast to Jia's model, we fit the R_{AA} vs. I_{AA}
- J. Jia et.al., arXiv:1101.0290 [nucl-th]



- v_n vs. v_n^{IAA} :
 - clear shift between Glauber and CGC model
- It is necessary to **always** determine the mean **and** the width of a correlation!



B. Betz et.al., arXiv:1102.5416 [nucl-th]

Path-length dependence

■ Study the path-length dependence at $b=8\text{fm}$:

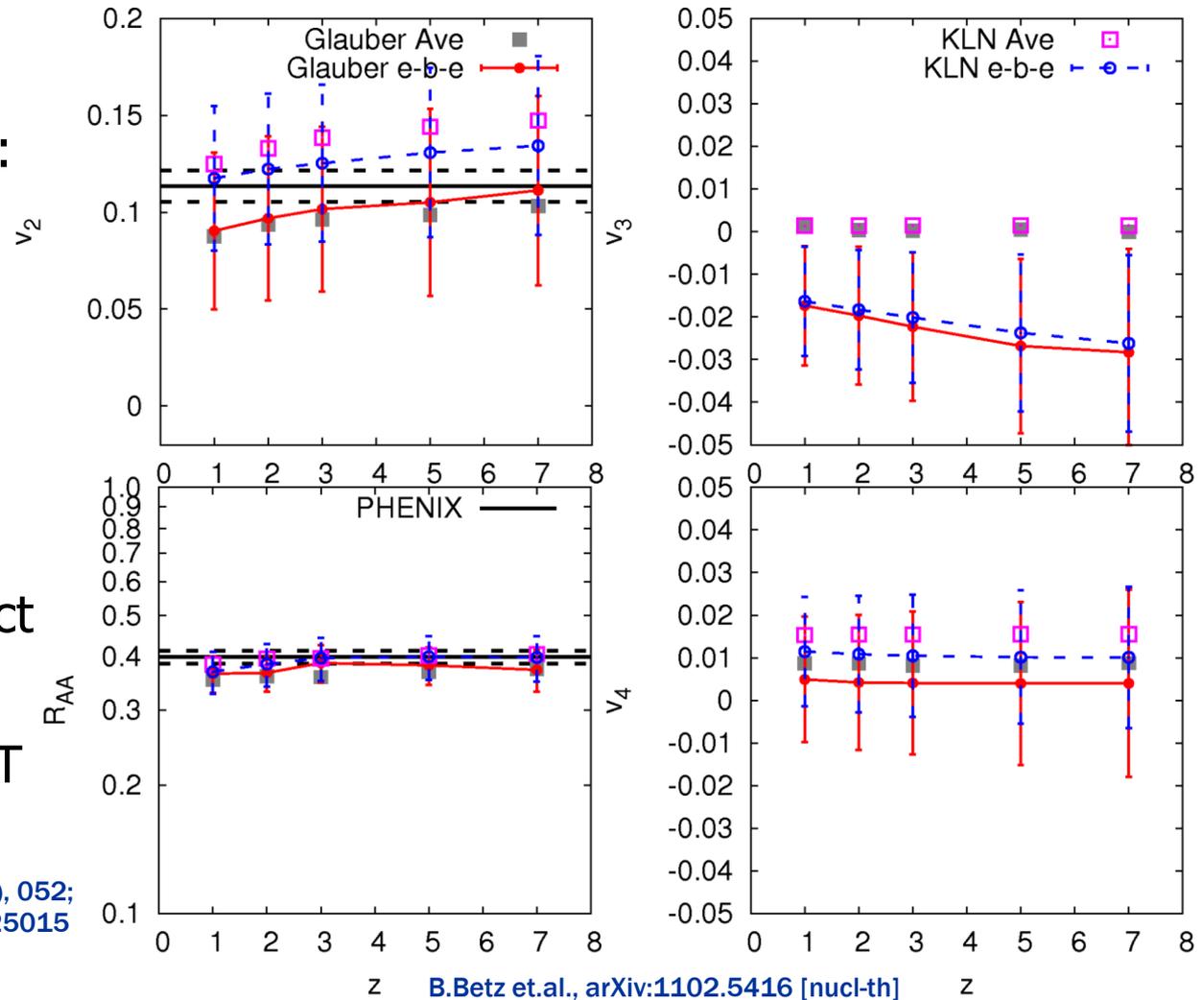
- Once R_{AA} is fixed via κ ,
- sensitivity remains mostly for v_2 and v_3

➡ small saturation effect occurs for larger z

→ described by AdS/CFT

off-shell partons

S. Gubser et al., JHEP 0810 (2008), 052;
P. Chesler et al., PRD 79 (2009) 125015



Insensitivity of higher v_n 's

- Why are the v_n 's at high- p_T so insensitive to initial conditions while the v_n 's of soft particles are?
 - viscous forces are driven by *local gradients*
 - jet absorption is driven by *global differences* in the integrated $\langle -\kappa P^a \tau^z T^{z-a+2} \rangle$
- These two effects are different, especially event-by-event
 - Glauber and CGC in. cond. are tuned to reproduce the observed multiplicities
 - $\langle T \rangle$ is *similar*, even if *local gradients* of T are different
- ⇒ Hydrodynamics and tomography lead to very different results.

Differences

Nuclear modification factor for the generic energy loss model

$$R_{AA} = \left\{ 1 - \frac{K}{P_0^{1-a}} \underbrace{\int_{\tau_0}^{\infty} \tau^z T^{z-a+2} [x_0 + \hat{n}(\phi)\tau, \tau_0] d\tau}_I \right\}^{(n-1-a)/(1-a)}$$

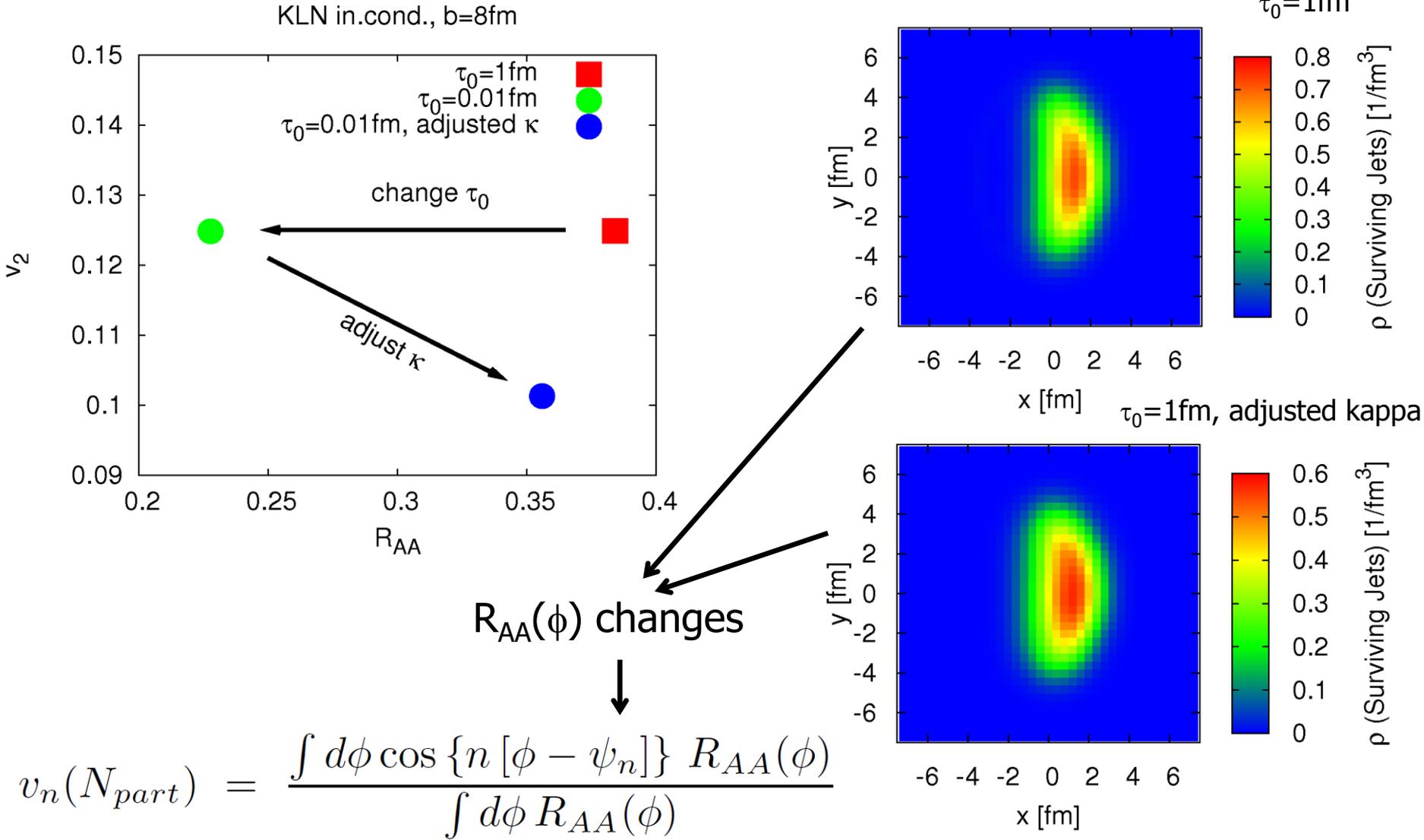
$K = \kappa (1-a)$, leads to the line integral ($a=0, z=1$)

$$I = \int_{\tau_0}^{\infty} T_0^2 [x_0 + \hat{n}(\phi)\tau] d\tau = \int_{\tau_0}^{\infty} \rho_0^{2/3} [x_0 + \hat{n}(\phi)\tau] d\tau$$

Line integral according to [A. Adare et al, PRL 105, 142301 \(2010\)](#) → The powers matter!

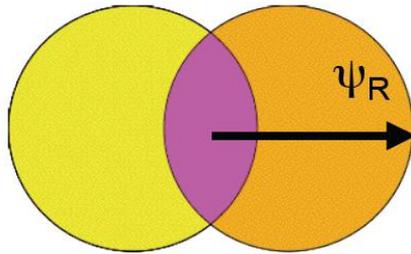
$$I_{m=1} = \int_{\tau_0}^{\infty} dl \rho(\vec{r} + l\vec{v})$$

Differences



Initial Fluctuations I

Glauber initial conditions:



$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left(1 + \sum 2v_n \cos(n(\phi - \psi_R)) \right)$$

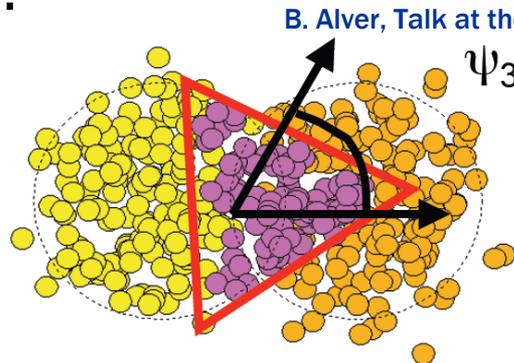
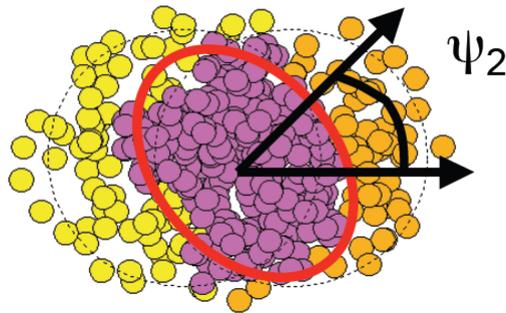
$$v_2 = \langle \cos(2(\phi - \psi_R)) \rangle$$

$$v_3 = 0$$

P. Sorensen J. Phys. G **37**, 094011 (2010),
 B. Alver et al., Phys. Rev. C **81**, 054905 (2010)

→ due to symmetry, odd Fourier components vanish

Fluctuating initial conditions:



B. Alver, Talk at the Glasma Workshop, BNL, May 2010

$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left(1 + \sum 2v_n \cos(n(\phi - \psi_n)) \right)$$

$$v_2 = \langle \cos(2(\phi - \psi_2)) \rangle$$

$$v_3 = \langle \cos(3(\phi - \psi_3)) \rangle$$

→ higher Fourier components may occur