

Monte Carlo Tools for Jet Quenching

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Why jets and why
MC?

Jets in p+p

Jets in A+A

Non-eikonal kinematics

Multiple gluon emission &
LPM-effect

k_{\perp} -broadening

Recoils, medium modelling,
background

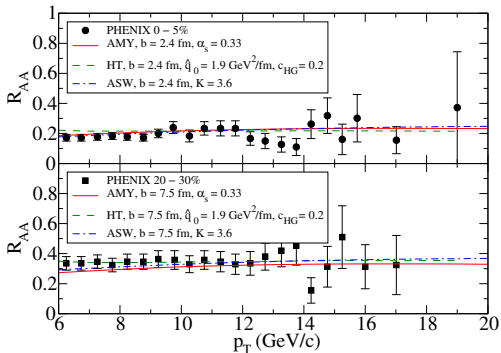
Hadronisation

Conclusions

Motivation for investigating jets

Theoretical considerations

- ▶ **single-inclusive** quantities do not fully constrain models



Bass *et al.*, Phys. Rev. C 79 (2009) 024901

- ▶ **sub-leading fragments** more discriminating
not well modelled by analytic calculations

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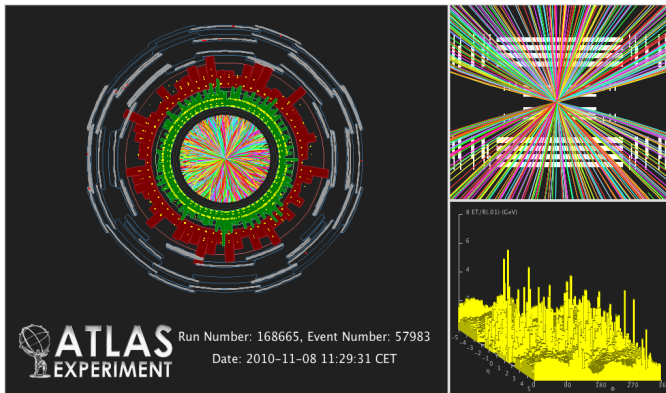
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Experimental needs

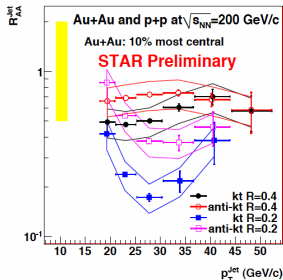
- ▶ need reliable tools to disentangle jets from background



Motivation for investigating jets

Experimental needs

- ▶ need reliable tools to disentangle jets from background
- ▶ in particular, need to understand
 - ▶ response of jet finders to quenched jets (\rightarrow jet shapes)
 - ▶ jet area, background, fluctuations
 - ▶ jet induced medium modifications



Bruna for the STAR Collaboration, J. Phys. Conf. Ser. 230 (2010) 012009

- ▶ requires running jet finders on theory prediction

Baseline: QCD Parton Shower in Vacuum

- ▶ collinear divergences in real emission matrix elements
- ▶ in collinear region factorisation to all orders

$$d\sigma_{n+1} \approx d\sigma_n \frac{dt}{t} \frac{d\phi}{2\pi} dz \frac{\alpha_s}{2\pi} \mathcal{P}(z)$$

$t : k_{\perp}^2 \approx Q^2 \approx \vartheta^2 \rightarrow$ hardness of splitting

\rightarrow large logarithms \rightarrow need to be resummed to all orders

- ▶ evolution equation (DGLAP) with ordering variable t
- ▶ define Sudakov form factor as

$$S(t_1, t_2) = \exp \left\{ - \int_{t_1}^{t_2} \frac{dt}{t} \int dz \frac{\alpha_s}{2\pi} \mathcal{P}(z) \right\}$$

Baseline: QCD Parton Shower in Vacuum

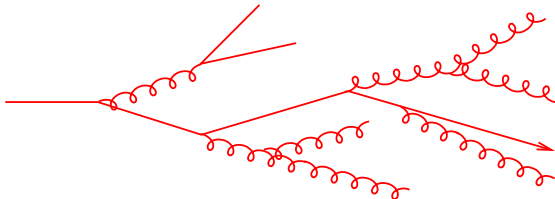
- ▶ evolution equation can be integrated

$$f(x, t) = \mathcal{S}(t_0, t) f(x, t_0) + \int_{t_0}^t \frac{dt'}{t'} \mathcal{S}(t', t) \int \frac{dz}{z} \frac{\alpha_s}{2\pi} \mathcal{P}(z) f(x/z, t')$$

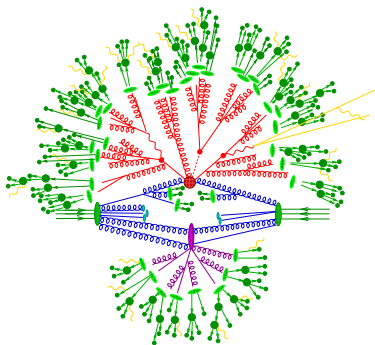
- ▶ $\mathcal{S}(t_0, t)$ probability for no emission between t and t_0
- ▶ suitable for MC implementation → parton shower
- ▶ resums real emissions to all orders

to leading logarithmic accuracy

- ▶ includes virtual corrections via unitarity
- ▶ comment: regularised soft and collinear divergences
→ observables better be infra-red and collinear safe



State of the art MC's in p+p



(multi-purpose event generators: HERWIG, PYTHIA, SHERPA)

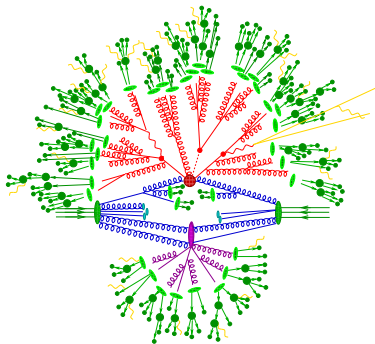
matrix elements: fixed order perturbation theory (LO or NLO)

final state parton shower: resummation of collinear/soft logarithms (LL)

initial state parton shower: like final state parton shower

hadronisation: non-perturbative QCD: modelling

Situation in A+A



matrix elements: unmodified due to high scale

final state parton shower: no general theory,
only calculations for special cases

e.g. single gluon radiation spectrum in eikonal limit

initial state parton shower: found to be unmodified at RHIC
except for pdf's

hadronisation: probably modified, no theoretical guidance

Embedding the parton shower in a medium

- ▶ in quantum mechanics no **instantaneous** processes
- ▶ in particular: **timescale** for gluon radiation

$$\tau_{\text{vac}} \approx \frac{\omega}{k_{\perp}^2} \approx \frac{1}{\sqrt{t}} \cdot \frac{E}{\sqrt{t}}$$

- ▶ time dilation **delays** decoherence of **energetic** fragments
- ▶ in medium: **transverse momentum** through **interactions**

$$\tau_{\text{med}} \approx \frac{\omega}{k_{\perp}^2} \approx \frac{\omega}{\hat{q}\tau_{\text{med}}} \Rightarrow \tau_{\text{med}} \approx \sqrt{\frac{\omega}{\hat{q}}}$$

- ▶ **soft** emissions decohere **first** and at **large angles**
- ▶ **hard core as in vacuum + soft large angle radiation?**
qualitative agreement with ATLAS & CMS results
- ▶ clarify by measurements of **intra-jet distributions** (FF's)

Established MC models

▶ HIJING:

- ▶ medium induced parton splitting process
- ▶ complete HI events

Wang, Gyulassy, Phys. Rev. D **44** (1991) 3501

Deng, Wang, Xu, arXiv:1008.1841

▶ HYDJET++/PYQUEN:

- ▶ gluon radiation sampled from BDMPS spectrum
- ▶ elastic scattering
- ▶ complete HI events

Lokhtin, Snigirev, Eur. Phys. J. C **45** (2006) 211

Lokhtin *et al.*, Comput. Phys. Commun. **180** (2009) 779

▶ JEWEL:

- ▶ unified ME+PS description for all emissions

work in progress

- ▶ elastic scattering
- ▶ simulates only parton shower + hadronisation

Zapp, Ingelman, Rathsman, Stachel, Wiedemann, Eur. Phys. J. C **60** (2009) 617

Zapp, Stachel, Wiedemann, Phys. Rev. Lett. **103** (2009) 152302

Established MC models

▶ Q-PYTHIA/Q-HERWIG:

- ▶ modified splitting function derived from BDMPS
- ▶ simulates only jets

Armesto, Cunqueiro, Salgado, Eur. Phys. J. C **63** (2009) 679

Armesto, Corcella, Cunqueiro, Salgado, JHEP **0911** (2009) 122

▶ YaJEM:

- ▶ medium interactions transfer virtuality to partons
(\rightarrow radiative energy loss)
- ▶ and degrade their energy
- ▶ simulates only jets

Renk, Phys. Rev. C **78** (2008) 034908

Renk, Phys. Rev. C **79** (2009) 054906

▶ MARTINI:

- ▶ based on AMY transition rates
- ▶ + elastic scattering transition rate
- ▶ simulates only jets

Schenke, Gale, Jeon, Phys. Rev. C **80** (2009) 054913

Non-eikonal kinematics

Problems with eikonal kinematics

- ▶ analytical calculations require: $E \gg \omega \gg k_{\perp} \gg \Lambda_{\text{QCD}}$
- ▶ RHIC and LHC kinematics: $E \gtrsim \omega \gtrsim k_{\perp} \gtrsim \Lambda_{\text{QCD}}$
- ▶ large **uncertainties** due to kinematic ambiguities

Consequences of non- eikonal kinematics

- ▶ phase space restrictions due to **E/p-conservation**

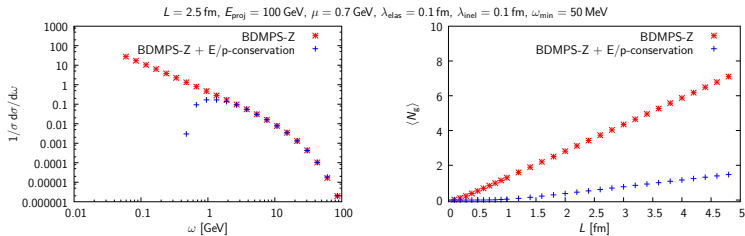
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Consequences of non- eikonal kinematics

- ▶ phase space restrictions due to **E/p-conservation**
- ▶ **dynamical** scattering centres
 - collisional energy loss
 - radiation off scattering centres
- ▶ no clear distinction between **elastic & inelastic scattering**
- ▶ no clear separation of **vacuum & medium radiation**

Non-eikonal kinematics

From a MC perspective

- ▶ energy-momentum conservation: no problem
- ▶ elastic vs. inelastic scattering: needs unified description
in preparation
- ▶ dynamical scatterings centres: difficult for models based on effective descriptions
e.g. modified splitting functions
 - ▶ collisional energy loss: typically neglected or added as separate process
 - ▶ radiation off scattering centres: model dependent
first steps in preparation
- ▶ vacuum vs. medium radiation: models use either unified description or assume complete factorisation

Multiple gluon emission & LPM-effect

Problems with analytic calculations

- ▶ single gluon radiation only + probabilistic iteration
- ▶ affected by E/p non-conservation in eikonal limit
- ▶ unclear how multiple gluon emissions interplay

first theoretical progress: radiation off colour dipole

Mehtar-Tani, Tywoniuk, arXiv:1105.1346 & Casalderrey-Solana, Iancu, arXiv:1105.1760

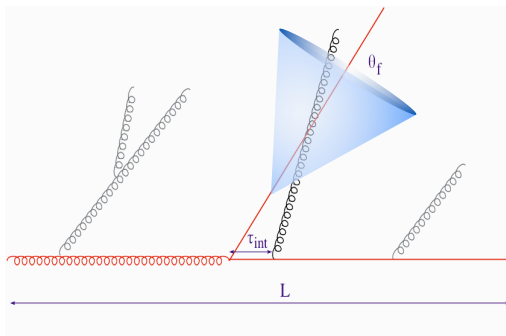
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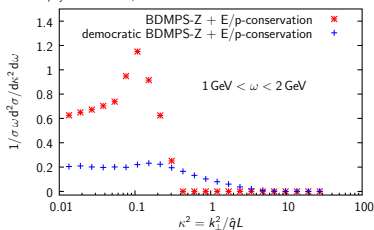
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Consequences of multiple gluon emission

- ▶ radiated gluons radiate → democratic treatment

$L = 2.5$ fm, $E_{\text{proj}} = 100$ GeV, $\mu = 0.7$ GeV, $\lambda_{\text{elas}} = 0.1$ fm, $\lambda_{\text{inel}} = 0.1$ fm, $\omega_{\text{min}} = 50$ MeV



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Consequences of multiple gluon emission

- ▶ radiated gluons radiate → democratic treatment
- ▶ energy loss not meaningful quantity
need to observe entire fragmentation pattern
- ▶ E/p conservation crucial for multi-parton final states
- ▶ theory without democratic treatment not suitable for jet-phenomenology

Multiple gluon emission & LPM-effect

From a MC perspective: LPM-effect

- ▶ **LPM-effect**: typically **effective description** of single gluon radiation
- ▶ **probabilistic** and **local** formulation of LPM-interference

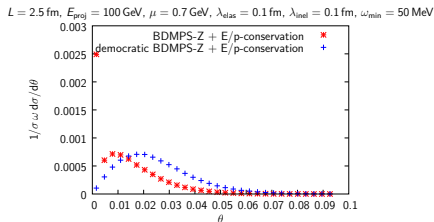
Zapp, Stachel, Wiedemann, Phys. Rev. Lett. 103 (2009) 152302 & arXiv:1103.6252

Multiple gluon emission

- ▶ **probabilistic iteration** sometimes involving **formation time** arguments
- ▶ iteration involves **model dependent** assumptions
- ▶ **democratic treatment** normally easy to achieve
except for scattering centre
- ▶ common assumption: partons radiate **independently**
supported by Casalderrey-Solana's & Iancu's results

Challenges

- ▶ affects **response** of **jet algorithms** to quenched jets
- ▶ analytic calculations: Brownian motion
- ▶ sensitive to
 - ▶ **energy-momentum conservation**
 - ▶ **democratic radiation**



- ▶ contamination by **energetic recoils**

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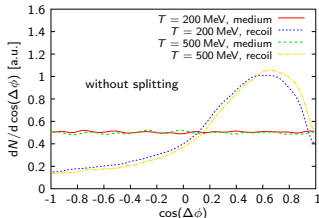
From a MC perspective

- ▶ assumptions about transverse dynamics vary from **collinear emission** to **parton shower kinematics**
- ▶ room for improvements of **microscopic dynamics**

Recoils, medium modelling, background

Challenges

- ▶ jets **modify** the **background** in their vicinity
- ▶ important for experimental **background subtraction**
- ▶ and interesting in its own right
 - interplay weakly & strongly coupled regimes**
- ▶ goal: **unified description** of jets and medium evolution
- ▶ first approaches:
 - ▶ track recoiling scattering centres



Zapp, Ingelman, Rathsmann, Stachel, Wiedemann, Eur. Phys. J. C **60** (2009) 617

- ▶ hydrodynamics with source terms Neufeld, Renk, arXiv:1001.5068 and many more

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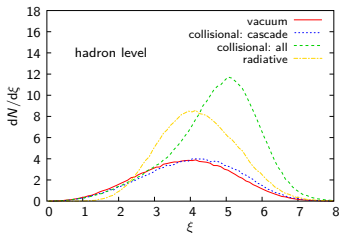
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From a MC perspective

- ▶ most MC's use **hydro calculations** as medium model
→ effect of jet in medium difficult to quantify
good potential for HIJING
- ▶ some convert it into **population** of **scattering centres**
→ model dependence
- ▶ **jet quenching MC's** not designed to describe
background modifications
description relies on ordering of scales
- ▶ **parton cascades** not (yet) designed for detailed
treatment of **jet evolution**
largely based on scattering integrals

Challenges

- ▶ conceptually **interesting** but **difficult** question
inherently non-perturbative
- ▶ common assumption: **hadronisation in vacuum**
- ▶ but medium does change **colour structure**
- ▶ not clear how **jet** and **medium** hadronisation **interplay**
- ▶ potentially large **uncertainties**
- ▶ even within **factorised approach**



Hadronisation

From a MC perspective

- ▶ all models assume hadronisation in vacuum
- ▶ some models allow **modifications** of the **colour topology**
- ▶ nearly all rely on **Lund string fragmentation** model
except for Q-HERWIG
- ▶ desirable: investigation of systematics
e.g. study different assumptions about colour topology
- ▶ not all implemented prescriptions are **infra-red** and **collinear safe**
- ▶ little effort to implement **alternative ideas**
e.g. pre-hadron formation should be suitable for MC's

Conclusions

- ▶ theoretical and experimental arguments for going from **single-inclusive** observables to **jets**
- ▶ raises important **conceptual** (and technical) **issues**
- ▶ **theory tool**: **Monte Carlo generators**
 - ▶ describe jets on basis of **multi-particle** final states
 - ▶ account **dynamically** for jet – medium interactions
 - ▶ **versatile** to explore **conceptual** issues
 - ▶ **jet finders** and entire **analyses** can run on **MC events**
 - ▶ have to rely on **phenomenological modelling**
- ▶ ultimately: **unified** description of **jet** & **medium evolution**
- ▶ expect **major progress** in next years
- ▶ and fruitful **interaction** between **experimentalists** and **theorists**

