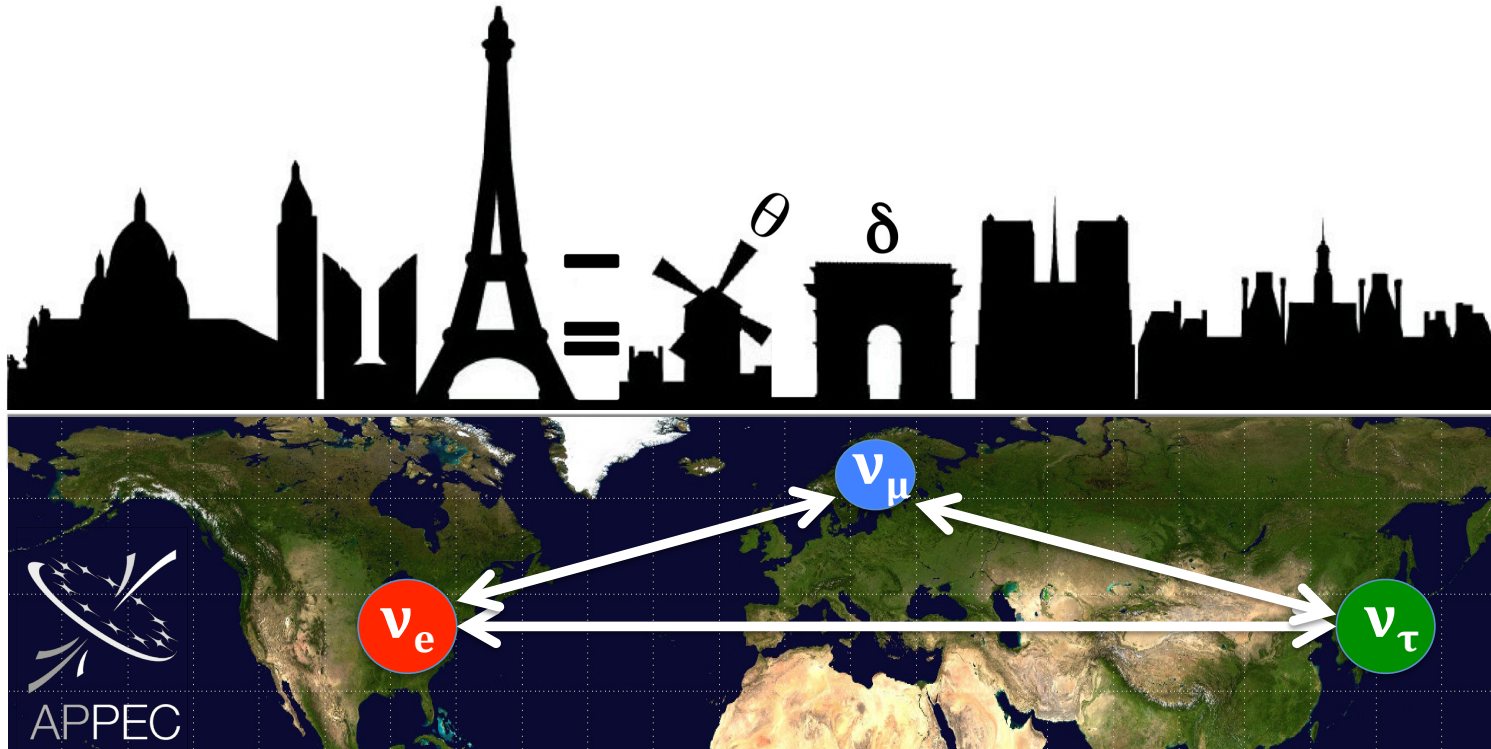


# Analysis of $3\nu$ mass-mixing parameters: 2014 status

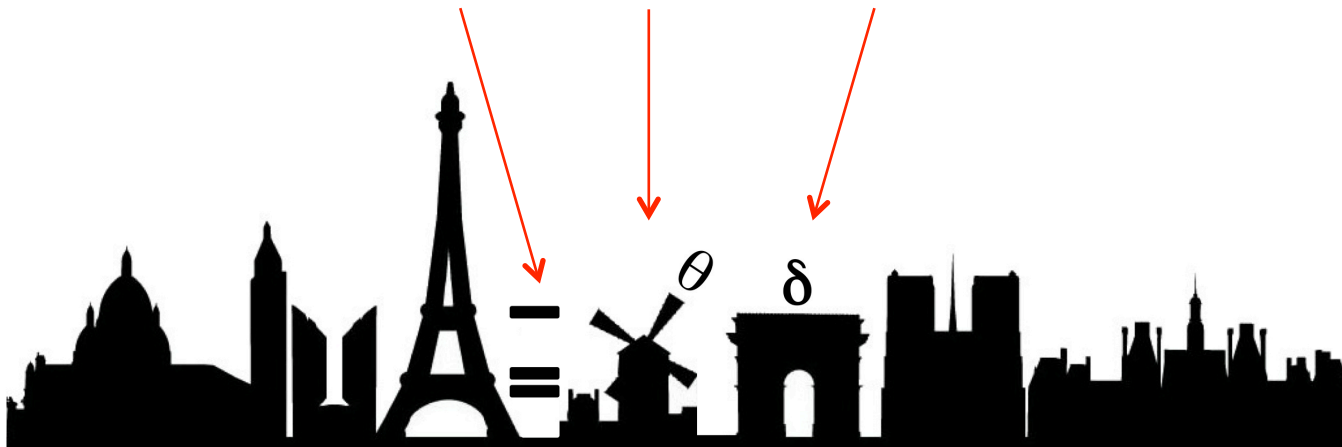


Eligio Lisi  
INFN, Bari, Italy

# Outline:

- Intro: data, notation, methodology
- **Status just before “Neutrino 2014”**
- Impact of (some)  $\nu$ 2014 new data
- **Absolute neutrino mass observables**

**Emphasis: hierarchy,  $\theta_{23}$  octant, CP phase (unknowns)**



Based on arXiv:1312.2878v2 + work done in collaboration with:  
F. Capozzi, G.L. Fogli, D. Montanino, A. Marrone, A. Palazzo

## 2014 Data sets:

**LBL Accelerators = K2K + T2K + MINOS**

**Solar = All Solar experiments**

**KL = KamLAND reactor expt**

**SBL Reactors = DChooz + RENO + DB**

**SK Atm = Super-K Atmospheric**

## 3ν oscillation parameters: Notation

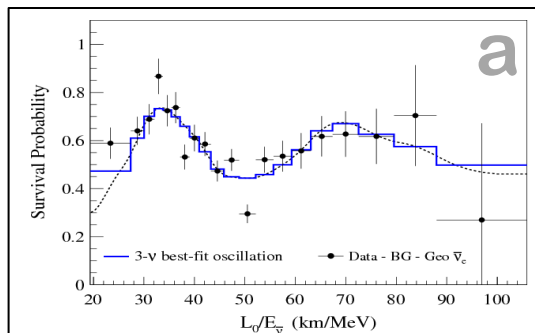
$\delta m^2$	=	$\Delta m^2_{21}$
$\theta_{12}, \theta_{23}, \theta_{13}, \delta$	=	as in PDG
$\delta$ range	=	$[0, 2\pi]$ (others prefer $[-\pi, +\pi]$ )
$\Delta m^2$	=	$(\Delta m^2_{31} + \Delta m^2_{32})/2$

(All parameters free to float in the global fit)

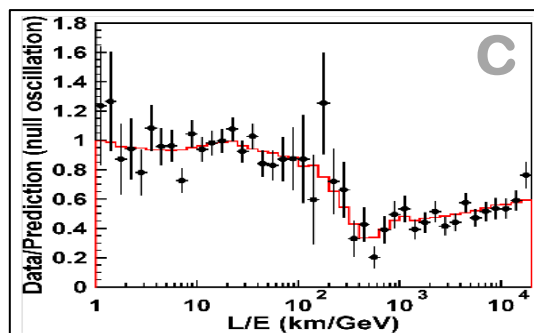
2014:  $1\sigma$  error on  $\Delta m^2 \approx 6 \times 10^{-5} \text{ eV}^2 < \delta m^2$  !

# $\alpha \rightarrow \beta$ transitions and dominant oscillation parameters probed so far:

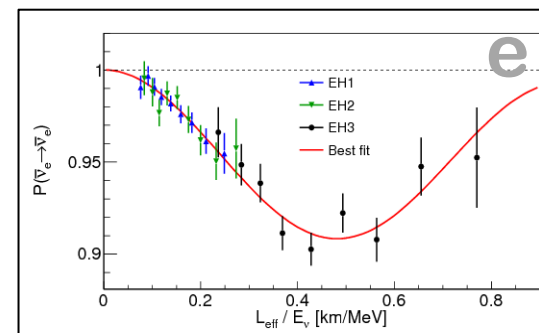
## $e \rightarrow e$ ( $\delta m^2, \theta_{12}$ )



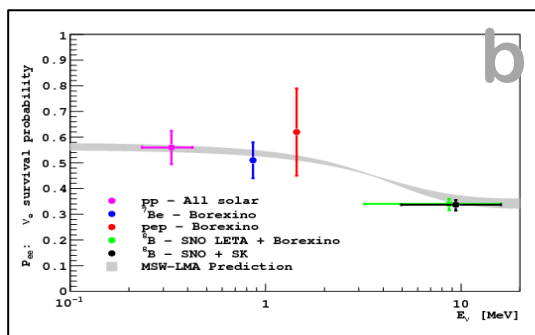
## $\mu \rightarrow \mu$ ( $\Delta m^2, \theta_{23}$ )



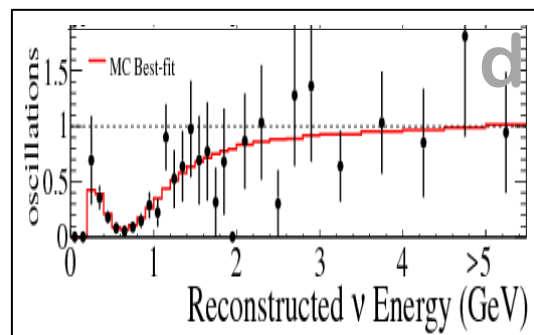
## $e \rightarrow e$ ( $\Delta m^2, \theta_{13}$ )



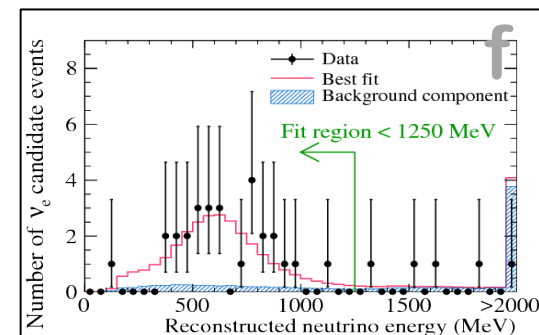
## $e \rightarrow e$ ( $\delta m^2, \theta_{12}$ )



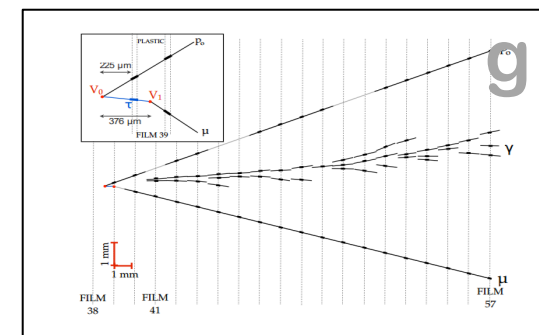
## $\mu \rightarrow \mu$ ( $\Delta m^2, \theta_{23}$ )



## $\mu \rightarrow e$ ( $\Delta m^2, \theta_{13}, \theta_{23}$ )



## $\mu \rightarrow \tau$ ( $\Delta m^2, \theta_{23}$ )



Data from various types of neutrino experiments: (a) solar, (b) long-baseline reactor, (c) atmospheric, (d) long-baseline accelerator, (e) short-baseline reactor, (f,g) long baseline accelerator (and, in part, atmospheric).

(a) KamLAND [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], MACRO, MINOS etc.; (d) T2K (plot), MINOS, K2K; (e) Daya Bay [plot], RENO, Double Chooz; (f) T2K [plot], MINOS; (g) OPERA [plot], Super-K atmospheric.

See also other talks at this Meeting.

## Combined analysis of data sets: Methodology

**LBL Accelerator** data are dominantly sensitive to  $(\Delta m^2, \theta_{23}, \theta_{13})$ . But, accurate constraints on these parameters do need  $(\delta m^2, \theta_{12})$  input from **Solar + KL** to compute sub-dominant effects.

It makes sense to combine from the start:  
**LBL Acc + Solar + KL**. Note: Solar + KL data carry a preference (“hint”) for  $\sin^2\theta_{13} \sim 0.02$

# Combined analysis of data sets: Methodology

Analysis includes increasingly rich data sets:

LBL Acc + Solar + KL

LBL Acc + Solar + KL + SBL Reactor

LBL Acc + Solar + KL + SBL Reactor + SK Atm.

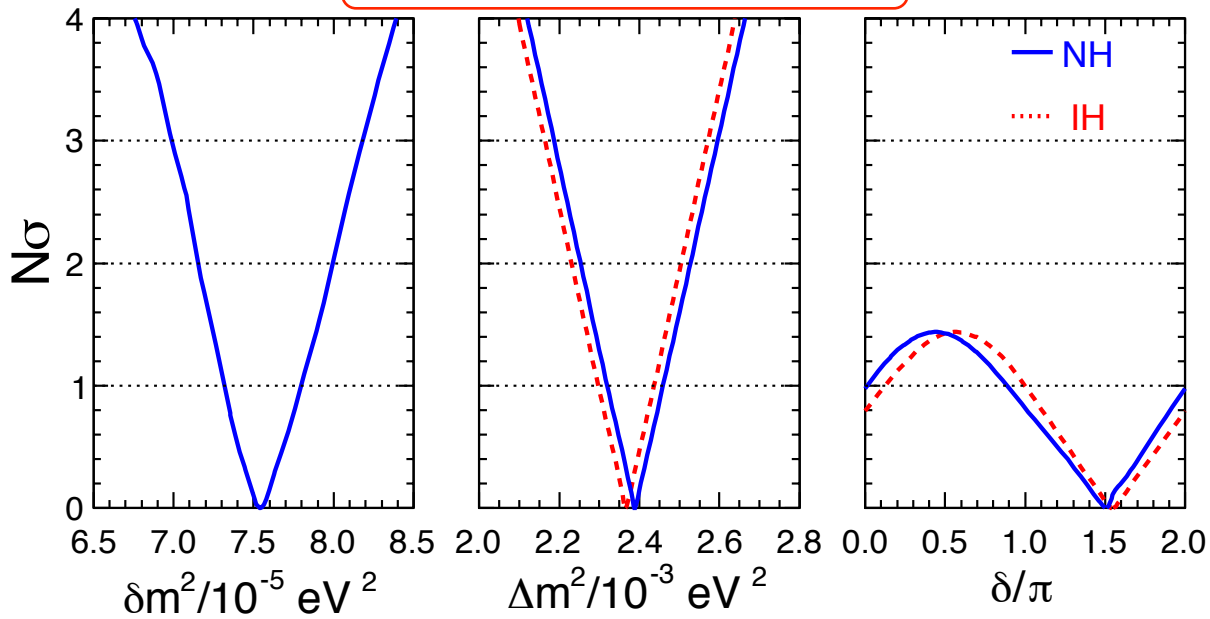
Figures: parameters not shown are marginalized away.

Contours are drawn at  $\Delta\chi^2 = 1, 4, 9 \rightarrow$

$N\sigma = 1, 2, 3$  for projections over single parameters.

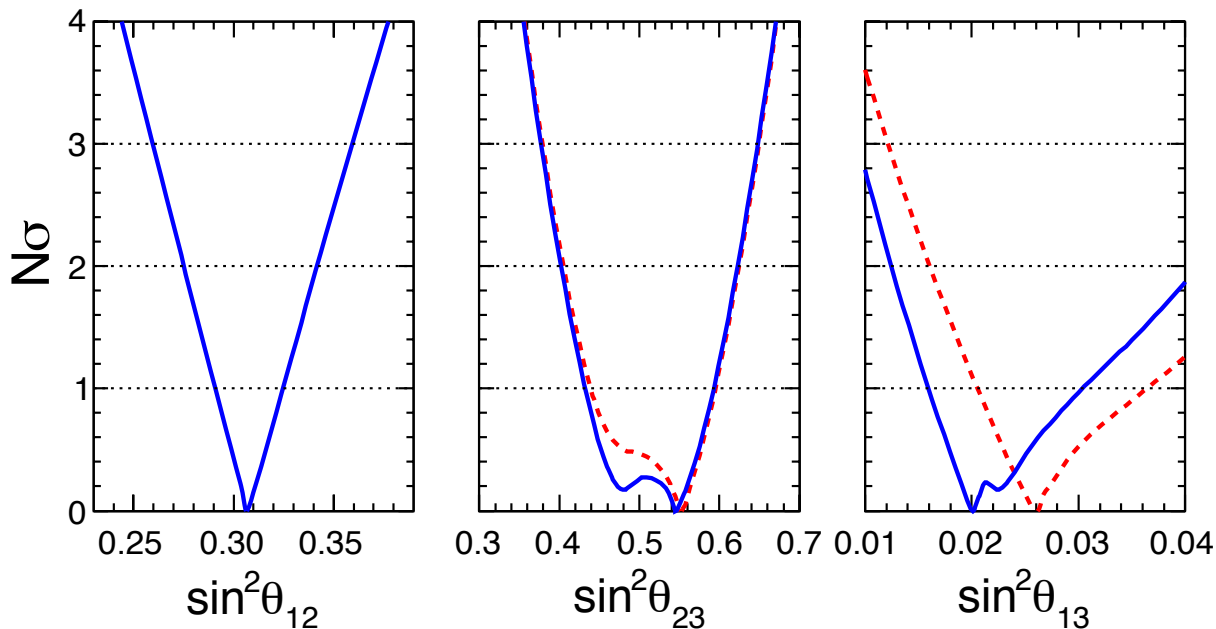
End of Intro. **Results on single parameters**  $\rightarrow$   
[with all data available just before Nu2014]

# LBL Acc + Solar + KL



Upper and lower bound on all oscill. parameters but  $\delta$

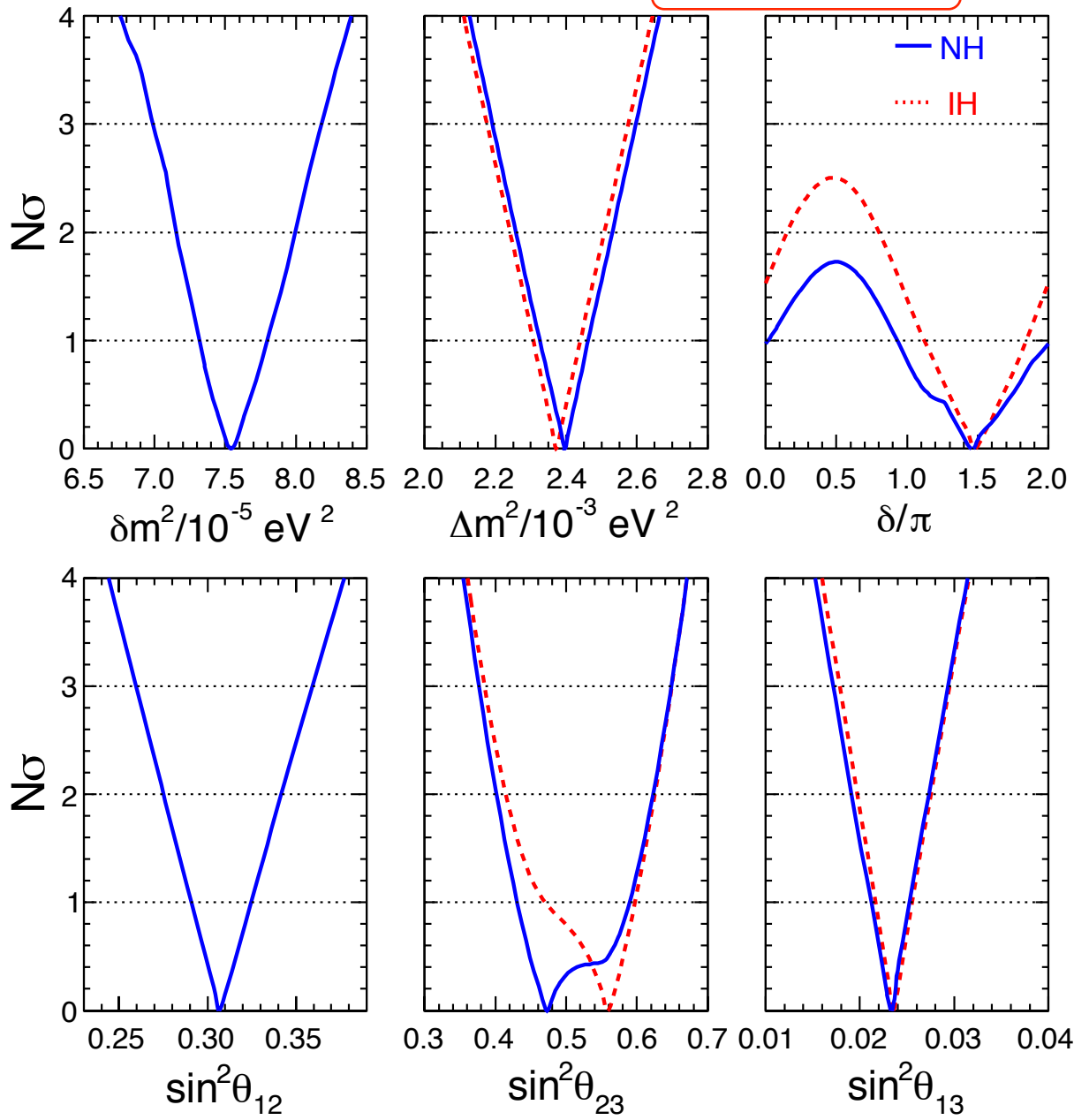
Slight preference for  $\delta \sim 1.5 \pi$



Slight preference for nonmaximal  $\theta_{23}$  and for 2nd octant



LBL Acc + Solar + KL + **SBL Reactors**

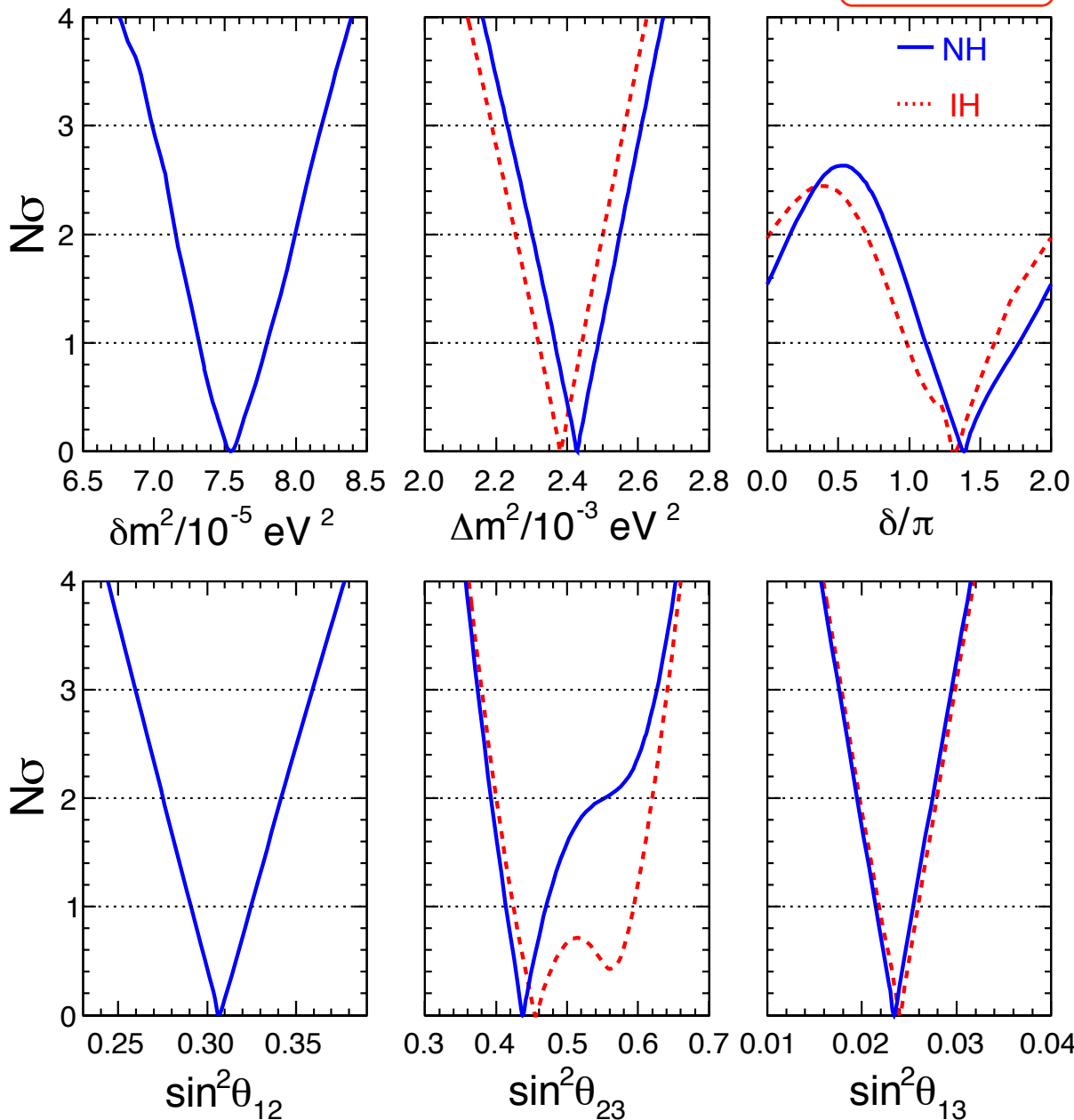


Strong  $\theta_{13}$  bounds

Still a preference for  $\delta \sim 1.4-1.5 \pi$

Slight preference for nonmax  $\theta_{23}$  but octant flips with hierarchy

LBL Acc + Solar + KL + SBL Reactors + SK Atm



Some effects on the  $\nu_\mu \rightarrow \nu_\tau$  dominant parameters ( $\Delta m^2, \theta_{23}$ )

**Preference**  
for  $\delta \sim 1.4 \pi$   
and, in NH, for  
 $1 < \delta/\pi < 2$   
( $\sin\delta < 0$  @90% CL)

Preference for  
nonmaximal  $\theta_{23}$  and  
1<sup>st</sup> octant in NH;  
much weaker in IH.  
Somewhat fragile.

# $N\sigma$ ranges for single parameters (pre-Neutrino'14):

TABLE I: Results of the global  $3\nu$  oscillation analysis, in terms of best-fit values and allowed 1, 2 and  $3\sigma$  ranges for the  $3\nu$  mass-mixing parameters. See also Fig. 3 for a graphical representation of the results. We remind that  $\Delta m^2$  is defined herein as  $m_3^2 - (m_1^2 + m_2^2)/2$ , with  $+\Delta m^2$  for NH and  $-\Delta m^2$  for IH. The CP violating phase is taken in the (cyclic) interval  $\delta/\pi \in [0, 2]$ . The overall  $\chi^2$  difference between IH and NH is insignificant ( $\Delta\chi^2_{I-N} = -0.3$ ).

Parameter	Best fit	$1\sigma$ range	$2\sigma$ range	$3\sigma$ range
$\delta m^2/10^{-5} \text{ eV}^2$ (NH or IH)	7.54	7.32 – 7.80	7.15 – 8.00	6.99 – 8.18
$\sin^2 \theta_{12}/10^{-1}$ (NH or IH)	3.08	2.91 – 3.25	2.75 – 3.42	2.59 – 3.59
$\Delta m^2/10^{-3} \text{ eV}^2$ (NH)	2.43	2.37 – 2.49	2.30 – 2.55	2.23 – 2.61
$\Delta m^2/10^{-3} \text{ eV}^2$ (IH)	2.38	2.32 – 2.44	2.25 – 2.50	2.19 – 2.56
$\sin^2 \theta_{13}/10^{-2}$ (NH)	2.34	2.15 – 2.54	1.95 – 2.74	1.76 – 2.95
$\sin^2 \theta_{13}/10^{-2}$ (IH)	2.40	2.18 – 2.59	1.98 – 2.79	1.78 – 2.98
$\sin^2 \theta_{23}/10^{-1}$ (NH)	4.37	4.14 – 4.70	3.93 – 5.52	3.74 – 6.26
$\sin^2 \theta_{23}/10^{-1}$ (IH)	4.55	4.24 – 5.94	4.00 – 6.20	3.80 – 6.41
$\delta/\pi$ (NH)	1.39	1.12 – 1.77	0.00 – 0.16 $\oplus$ 0.86 – 2.00	—
$\delta/\pi$ (IH)	1.31	0.98 – 1.60	0.00 – 0.02 $\oplus$ 0.70 – 2.00	—

**Fractional errors (defined as 1/6 of  $\pm 3\sigma$  ranges):**

$$\begin{aligned}
 \delta m^2 & \quad 2.6 \% \\
 \Delta m^2 & \quad 2.6 \% \\
 \sin^2 \theta_{12} & \quad 5.4 \% \\
 \sin^2 \theta_{13} & \quad 8.5 \% \\
 \sin^2 \theta_{23} & \quad \sim 10 \%
 \end{aligned}$$

No significant hierarchy preference from global fit [ $\Delta\chi^2(I-N)=-0.3$ ]  
 Weak preference for first octant (more fragile after T2K 2014 data).  
**Intriguing hint of nonzero CP violation, with  $\sin\delta < 0 \dots$  (\*)**

(\*) Similar CP hint: Gonzalez-Garcia, Maltoni, Schwetz, Salvado 2013/14; SK, T2K official data analyses 2013/14.

# CP violation requires genuine $3\nu$ oscillations, distinct from $2\nu$ limits...

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2 January 1978

## TIME REVERSAL VIOLATION IN NEUTRINO OSCILLATION

Nicola CABIBBO\*

*Laboratoire de Physique Théorique et Hautes Energies, Paris, France\*\**

Received 11 October 1977

We discuss the possibility of CP or T violation in neutrino oscillation. CP requires  $\nu_\mu \leftrightarrow \nu_e$  and  $\bar{\nu}_\mu \leftrightarrow \bar{\nu}_e$  oscillations to be equal. Time reversal invariance requires the oscillation probability to be an even function of time. Both conditions can be violated, even drastically, if more than two neutrinos exist.



# CP violation requires genuine $3\nu$ oscillations, distinct from $2\nu$ limits...

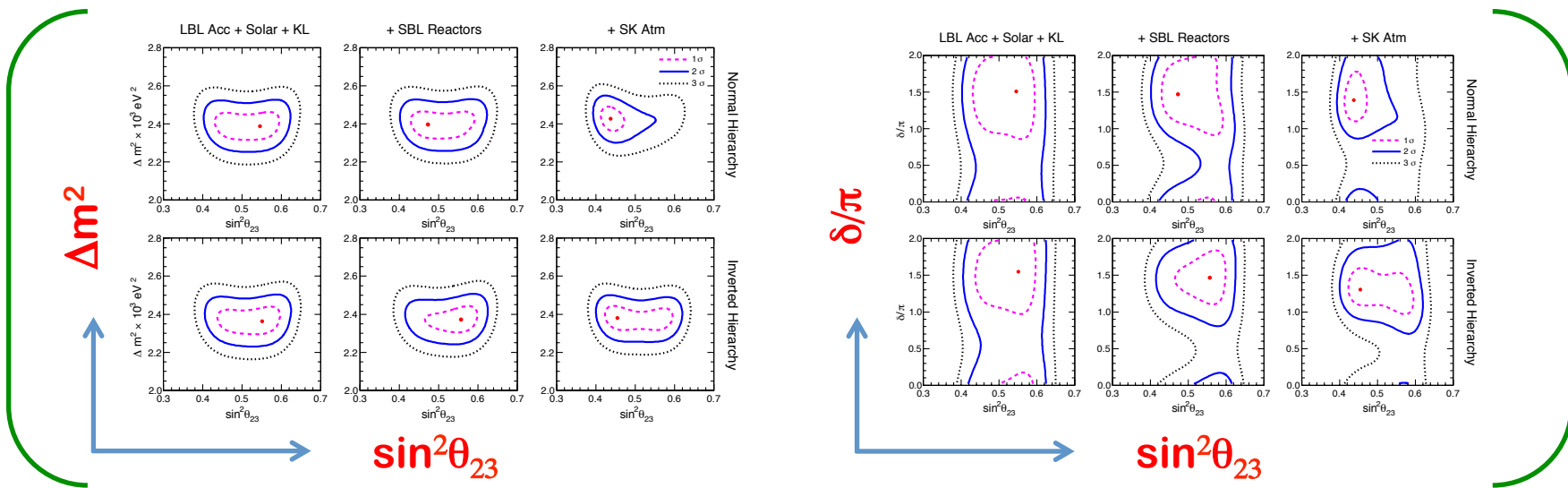
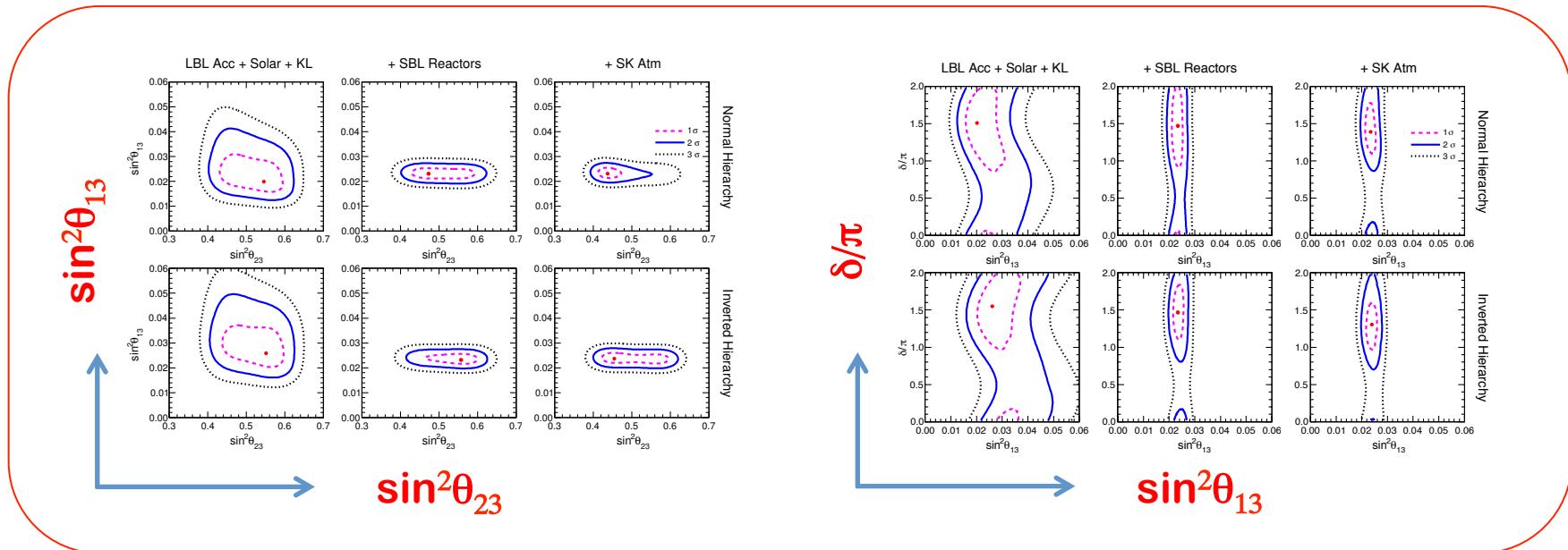
- 3 mixing angles should be nonvanishing ✓
- 2 mass gaps should be nonvanishing ✓
- 1 Dirac phase should be nonvanishing ...

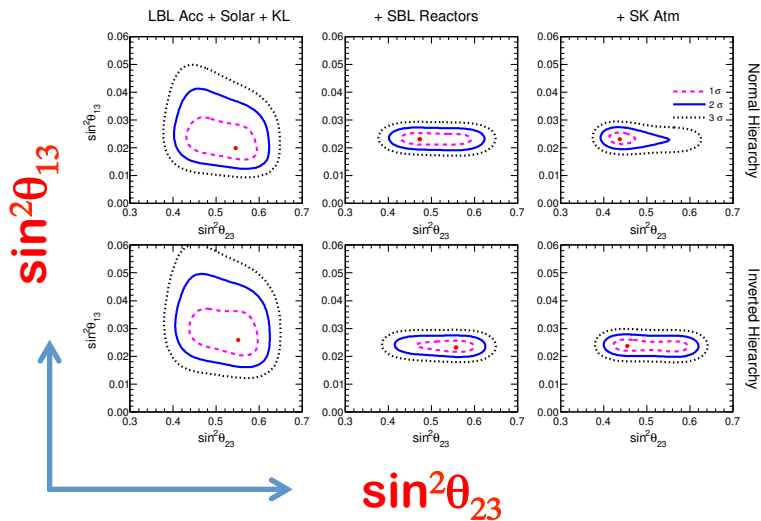
Nature has already provided us with 5  
favorable conditions at **terrestrial scales ...**

**Let us hope that the 6<sup>th</sup> is also realized**

[and, if neutrinos are Majorana... CPV bonanza with 2 more phases ! ]

# From variances to covariances: analysis of 2D plots

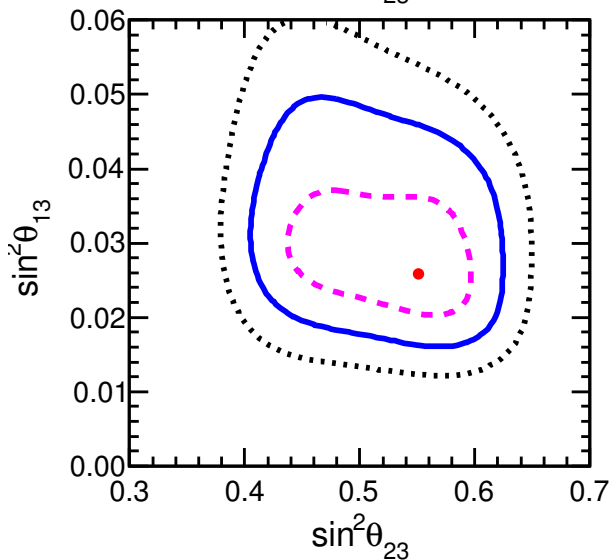
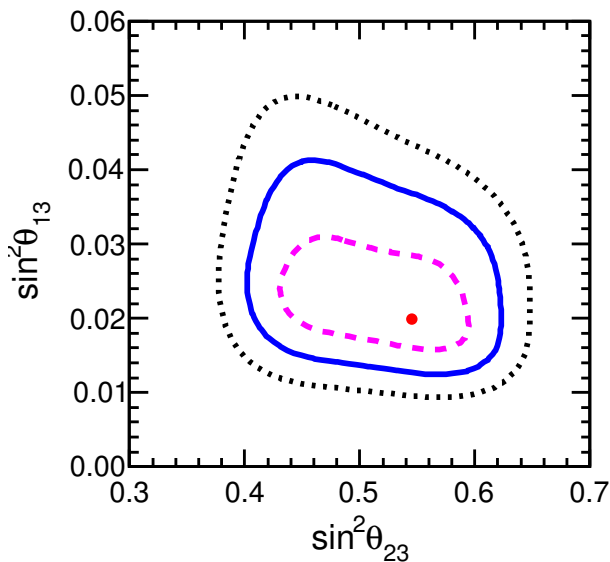




Leading appearance amplitude at LBL Acc.  $\sim \sin^2\theta_{23} \sin^2(2\theta_{13})$   
 $\rightarrow$  anticorrelates  $\theta_{23}$  and  $\theta_{13}$

Leading disappearance amplitude at SBL Reac.  $\sim \sin^2(2\theta_{13})$   
 Subleading disappearance effects in Solar + KL  $\sim \sin^2\theta_{13}$   
 $\rightarrow$  indirectly help in selecting high/low  $\theta_{23}$

LBL Acc + Solar + KL



MINOS disappearance prefers nonmaximal mixing (still wins over T2K preference for  $\sim$ maximal)  $\rightarrow$  two degenerate minima for  $\theta_{23}$

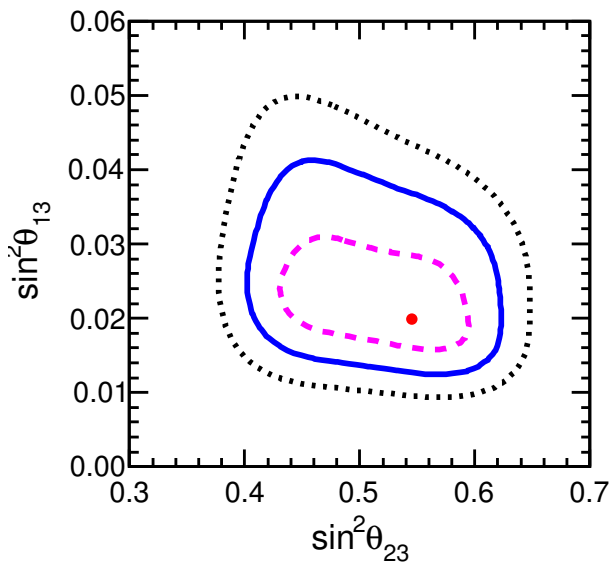
**T2K + MINOS appearance anticorrelate the minima with  $\theta_{13}$ : the higher  $\theta_{23}$ , the lower  $\theta_{13}$**

Contours extend to relatively high  $\sin^2\theta_{13}$  to accommodate the relatively “strong” T2K appearance signal, especially in IH

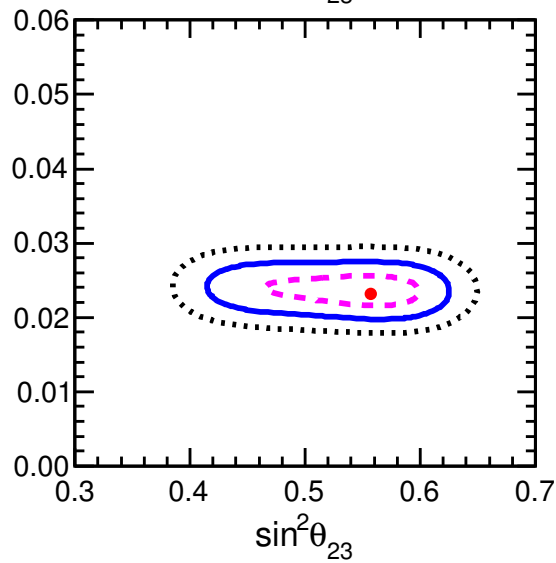
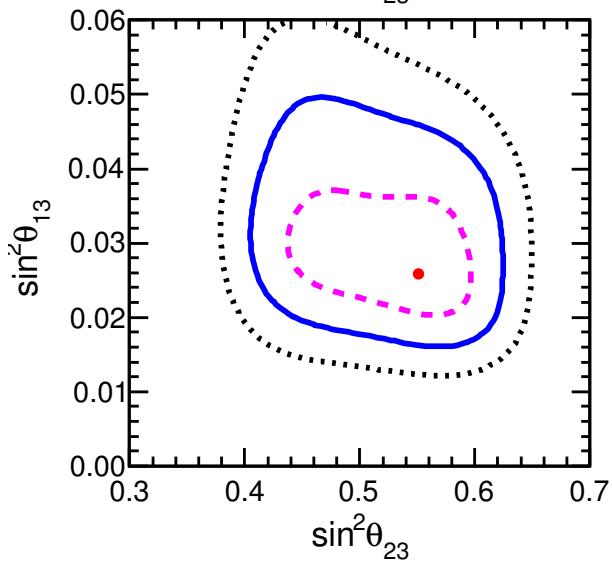
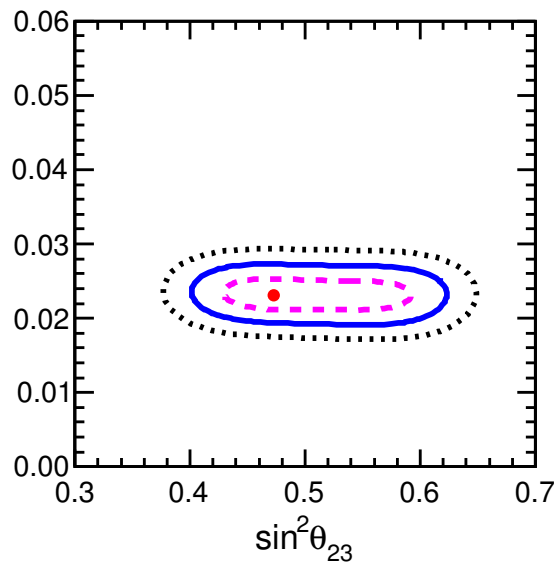
**In the combination, Solar + KL data lift the degeneracy and prefer the second octant solution, associated with “low”  $\sin^2\theta_{13} \sim 0.02$**



LBL Acc + Solar + KL

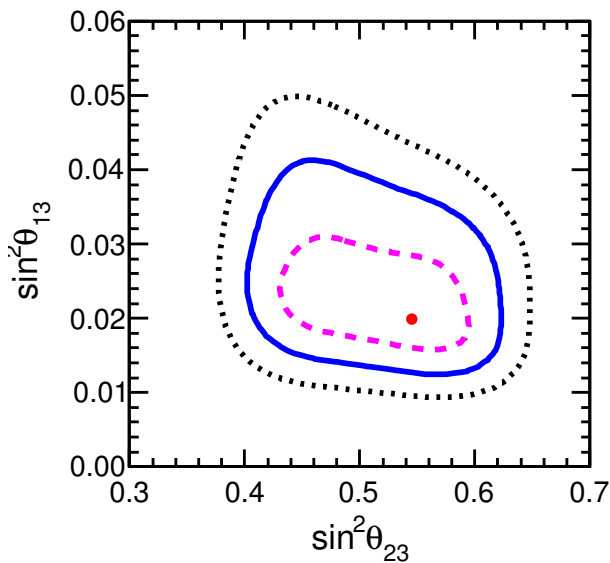


+ SBL Reactors

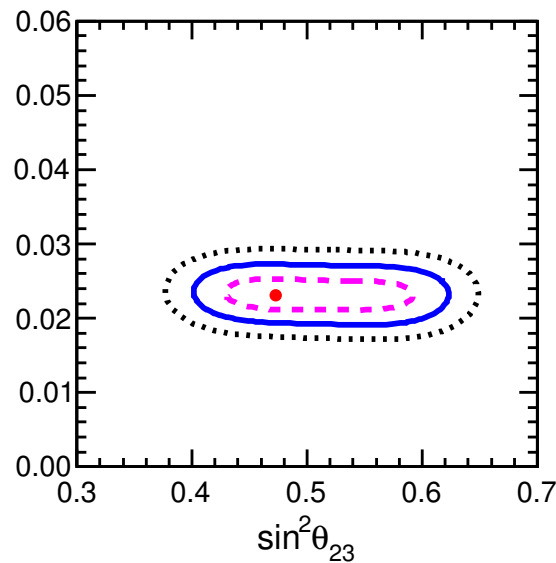


Reactor data prefer  $\sin^2\theta_{13} \sim 0.023$ , slightly higher than Solar+KL: enough to flip the octant in NH, but not enough to do so in IH.

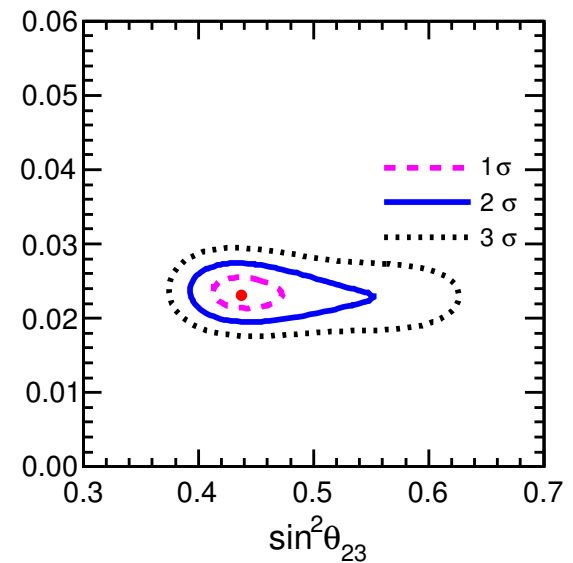
LBL Acc + Solar + KL



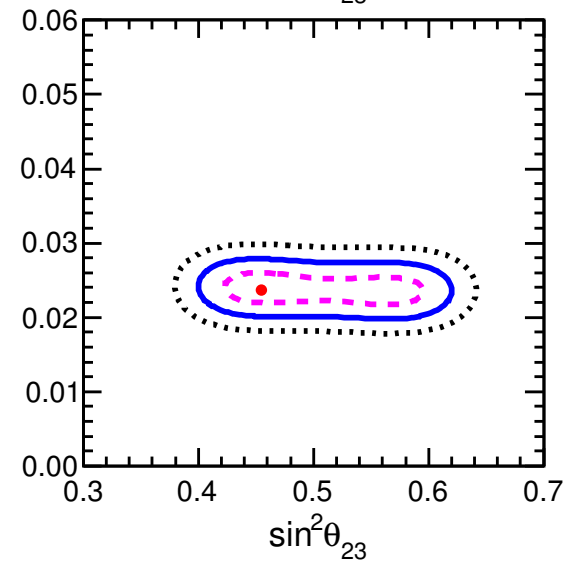
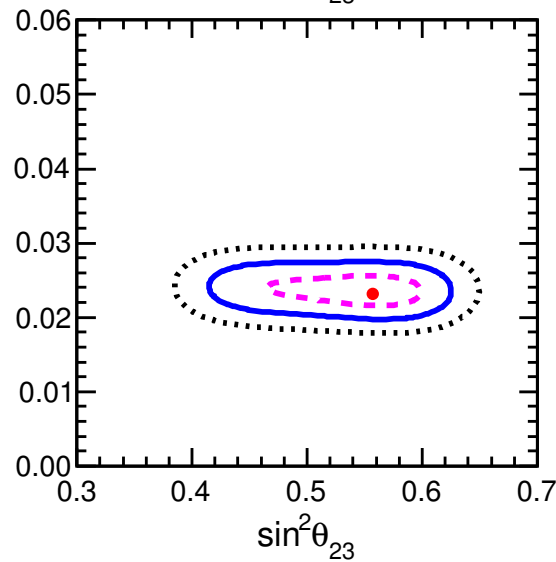
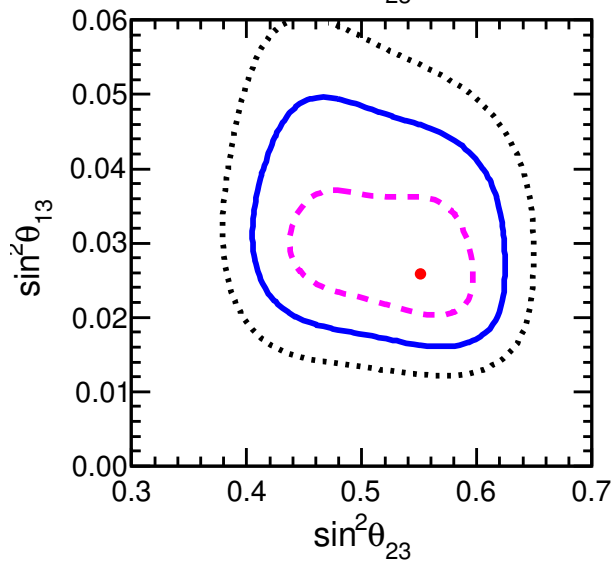
+ SBL Reactors



+ SK Atm

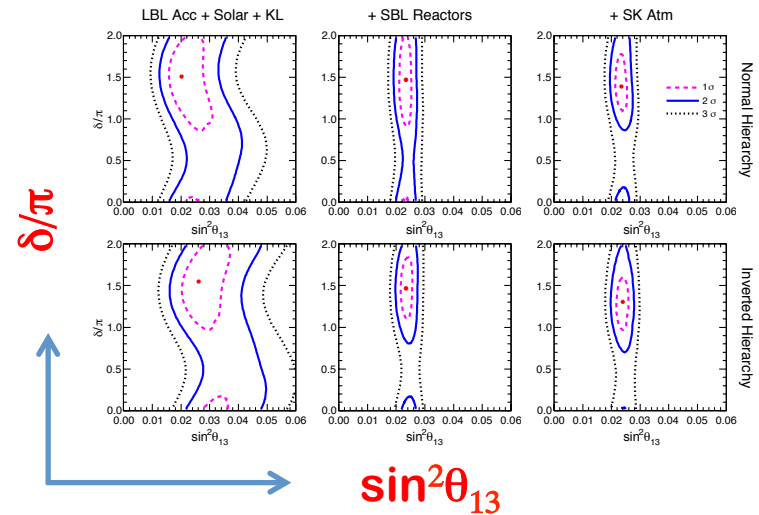


Normal Hierarchy



Inverted Hierarchy

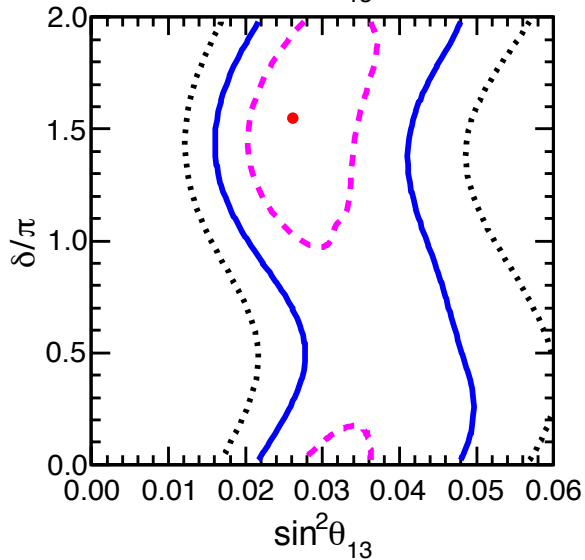
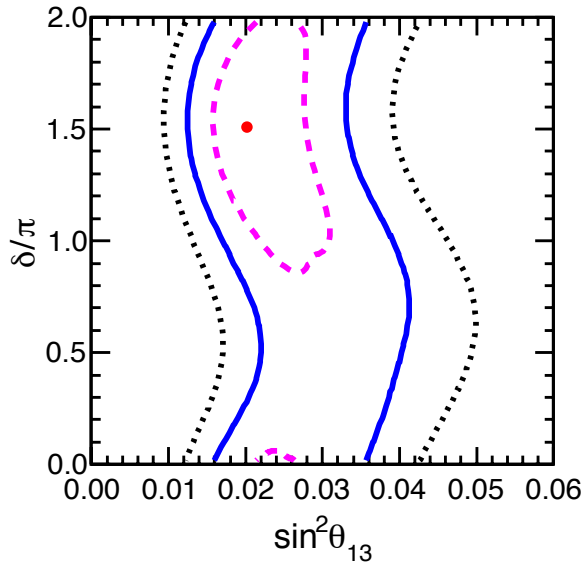
**SK atm: In our analysis we still find an overall preference of these data for 1st octant. But, global balance for  $\theta_{23} < \pi/4$  somewhat fragile**



Leading appearance amplitude at LBL Acc.  $\sim \sin^2\theta_{23} \sin^2(2\theta_{13})$   
 $\rightarrow$  uncertainty on  $\theta_{23}$  somewhat affects subleading terms

Subleading CPV appearance amplitude for  $\nu$   $\sim -\sin\delta$   
 $\rightarrow$  T2K signal maximized for  $\sin\delta \sim -1$  ( $\delta \sim 1.5\pi$ )

LBL Acc + Solar + KL



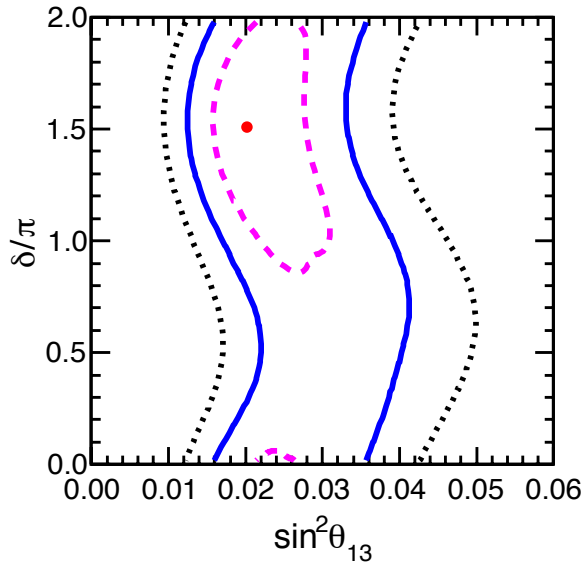
Each wavy band is in part determined by superposition of “two bands” for the two  $\theta_{23}$  octants [it was more evident in previous fits]

For the relatively “low” value  $\sin^2\theta_{13} \sim 0.02$  preferred by Solar + KL data, appearance  $\nu$  signal in T2K maximized by subleading CP-odd term for  $\sin\delta < 0$  [i.e.,  $1 < \delta/\pi < 2$ ]

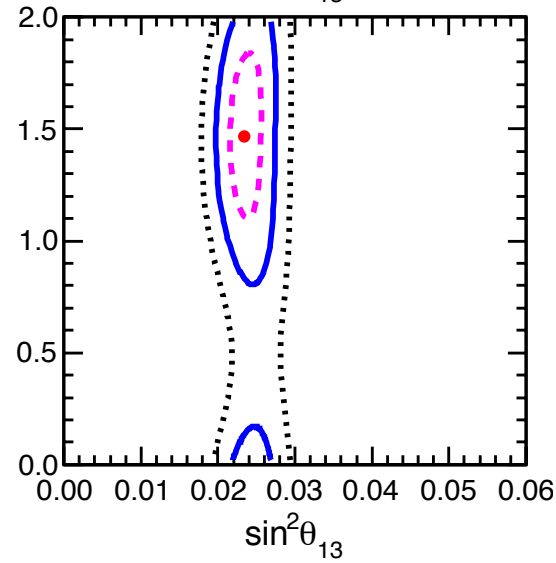
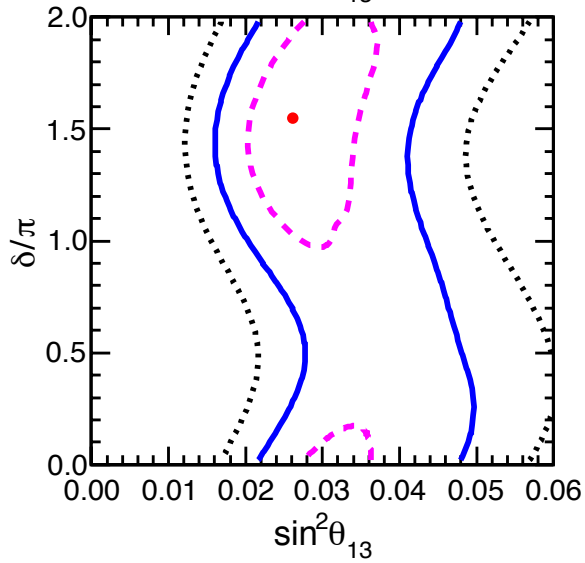
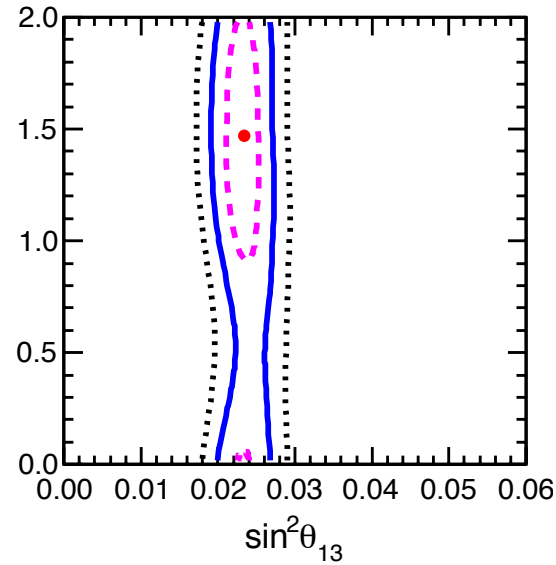
Best agreement with relatively “strong” T2K appearance signal is for  $\delta/\pi \sim 1.5$ , irrespective of the hierarchy.

This trend wins over weaker MINOS appearance signal, which tend to prefer  $\sin\delta > 0$  at best fit.

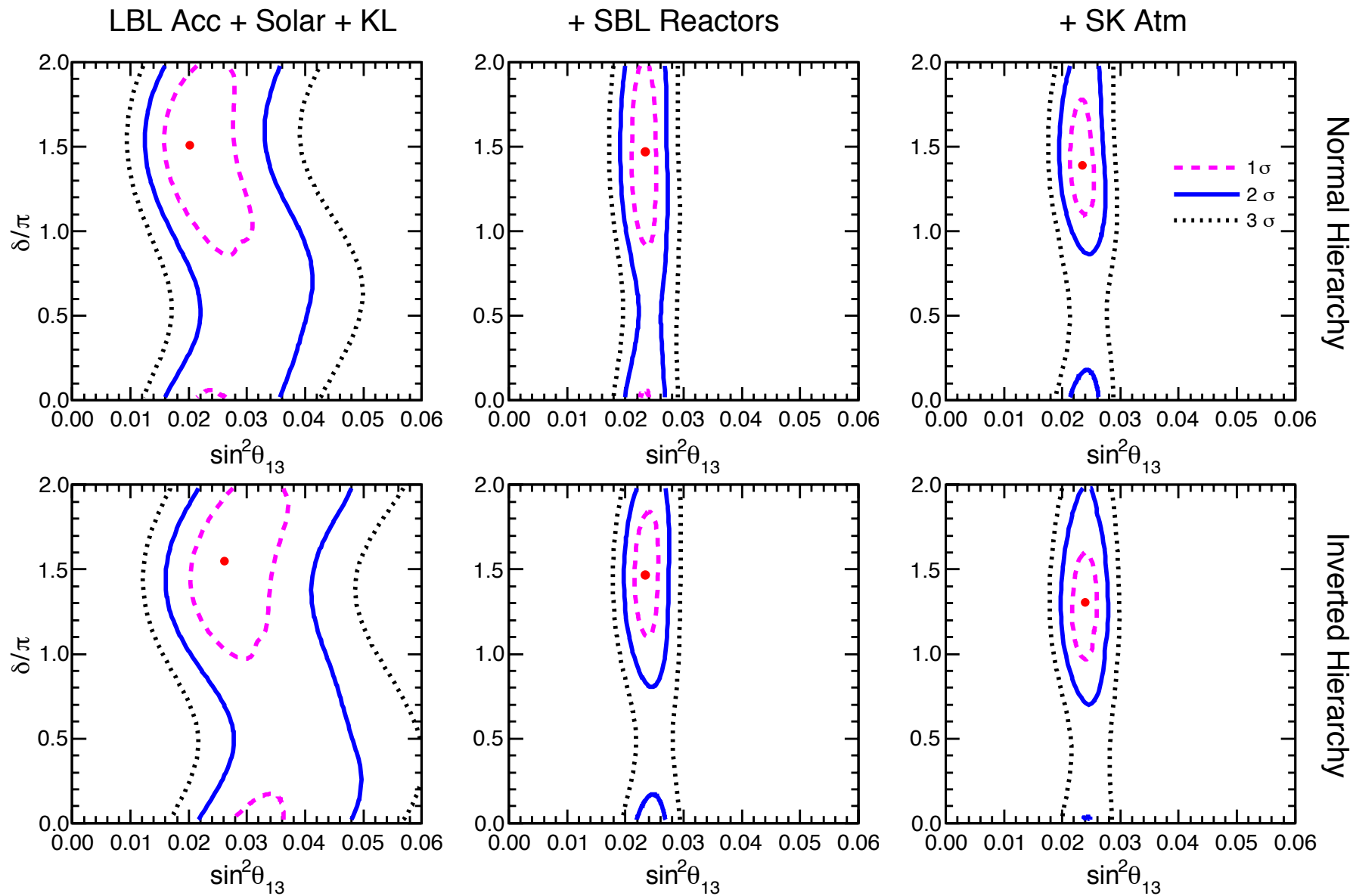
LBL Acc + Solar + KL



+ SBL Reactors



**Reactor data shrink the band around  $\sin^2\theta_{13} \sim 0.023$ , a bit higher than Solar+SK but still on the leftmost side of the band: preference for  $\delta/\pi \sim 1.5$  persists**



**SK atm: in combination, these data further shrink the allowed regions and slight lower the preferred value to  $\delta/\pi \sim 1.3-1.4$**

# Impact of (some) “Neutrino 2014” data: SBL reactors

**Daya Bay: gives more stringent bounds on  $(\Delta m^2, \sin^2\theta_{13})$**

In particular:  $\sin^2\theta_{13} = (2.15 \pm 0.13) \times 10^{-2}$

(a bit lower and with 6.0% error, wrt 8.5% in our previous fit)

**RENO: claims observation of new reactor component at ~4-6 MeV**

Double Chooz: sees ~5 MeV bump but with lower significance

[Rumors: Presumably seen also by Daya Bay ? ...]

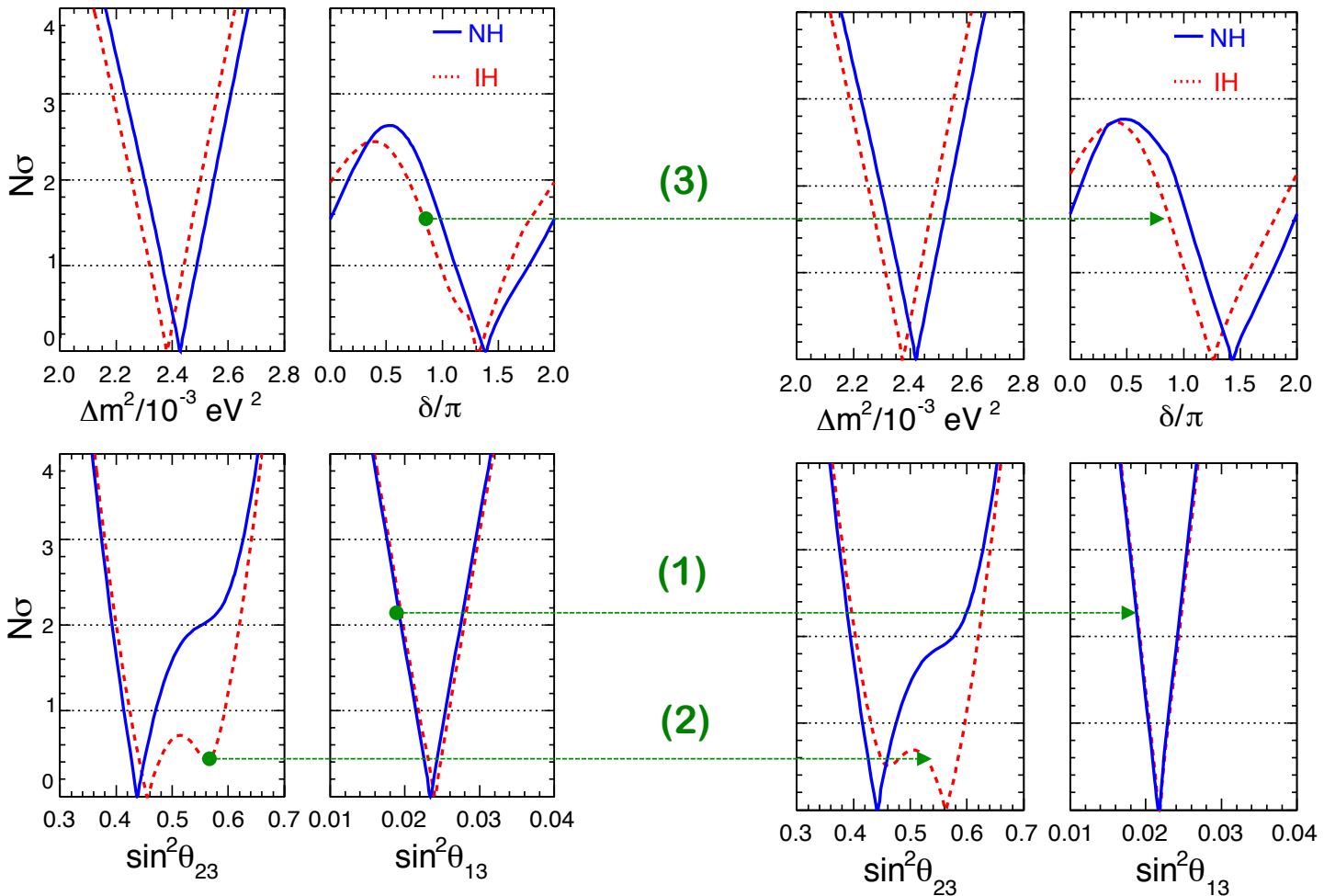
**In any case:  $(\Delta m^2, \sin^2\theta_{13})$  parameter estimate from near-far comparison seems robust under this possible new reactor comp.**

**Pragmatic attitude:**

**While waiting for a clarification of the ~5 MeV “bump” origin, let us take the dominant Daya Bay 2014 bounds at face value →**

pre- Neutrino 2014

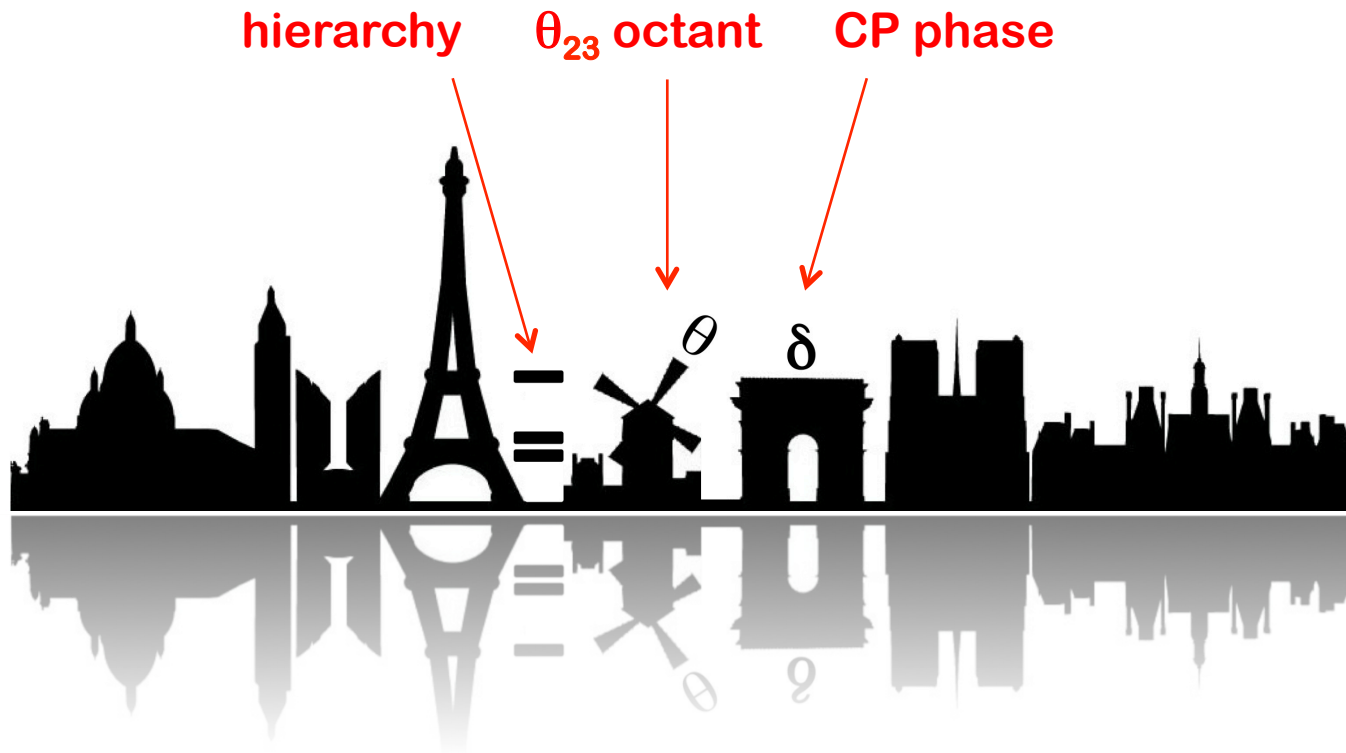
+ Daya Bay 2014 (prelim.)



- (1) Significantly more precise (and slightly lower)  $\sin^2 \theta_{13}$
- (2) 2<sup>nd</sup> octant of  $\theta_{23}$ : less disfavored in NH, favored in IH, via anticorr. with  $\theta_{13}$
- (3) Slightly sharper bounds on  $\delta$ , via interplay of SBL reac. with LBL accel.
- (4) NH/IH: no hint,  $\Delta\chi^2(\text{I-N})=+0.1$



# Recap of hints on unknowns →



pre-V2014

post-V2014

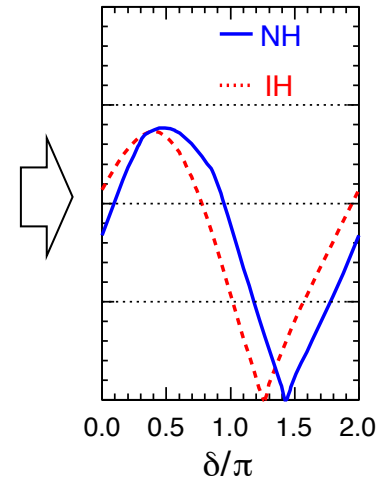
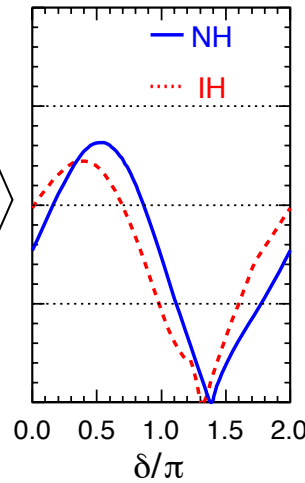
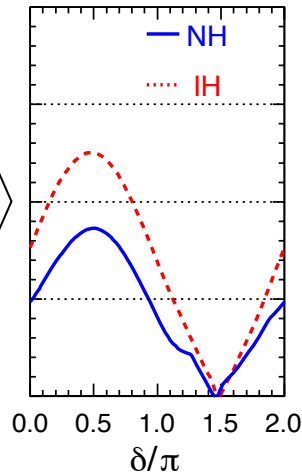
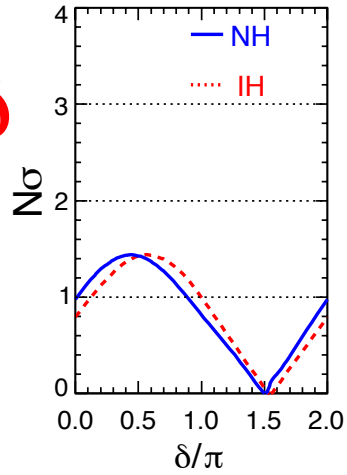
LBL+Sol+KL

+SBL Reac

+SK atm

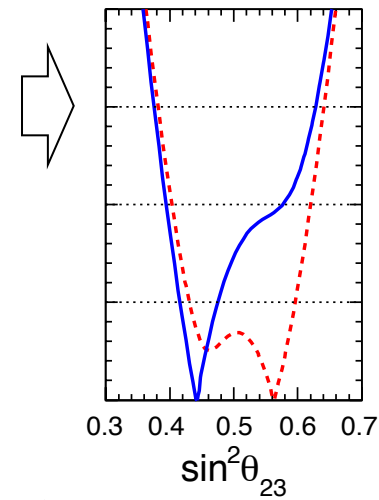
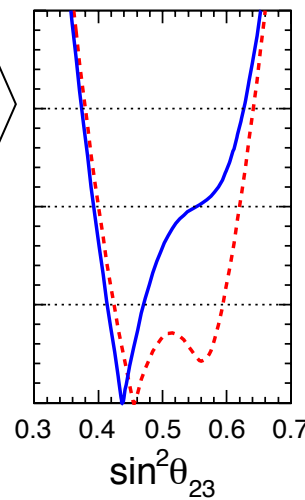
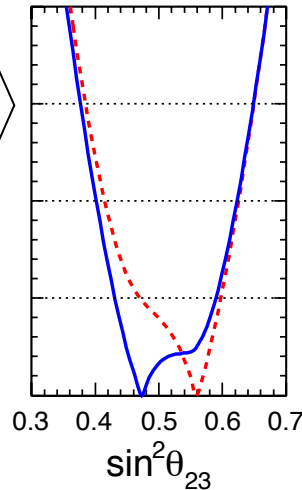
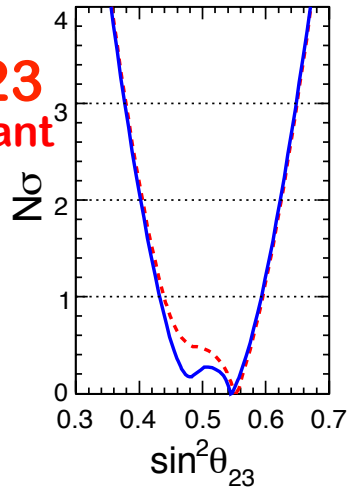
+Daya Bay'14 (prelimin.)

$\delta$



intriguing,  
 $\sin \delta < 0$   
favored

$\theta_{23}$   
octant



unstable,  
fragile

$\Delta\chi^2$   
(IH-NH)

-1.4

-1.1

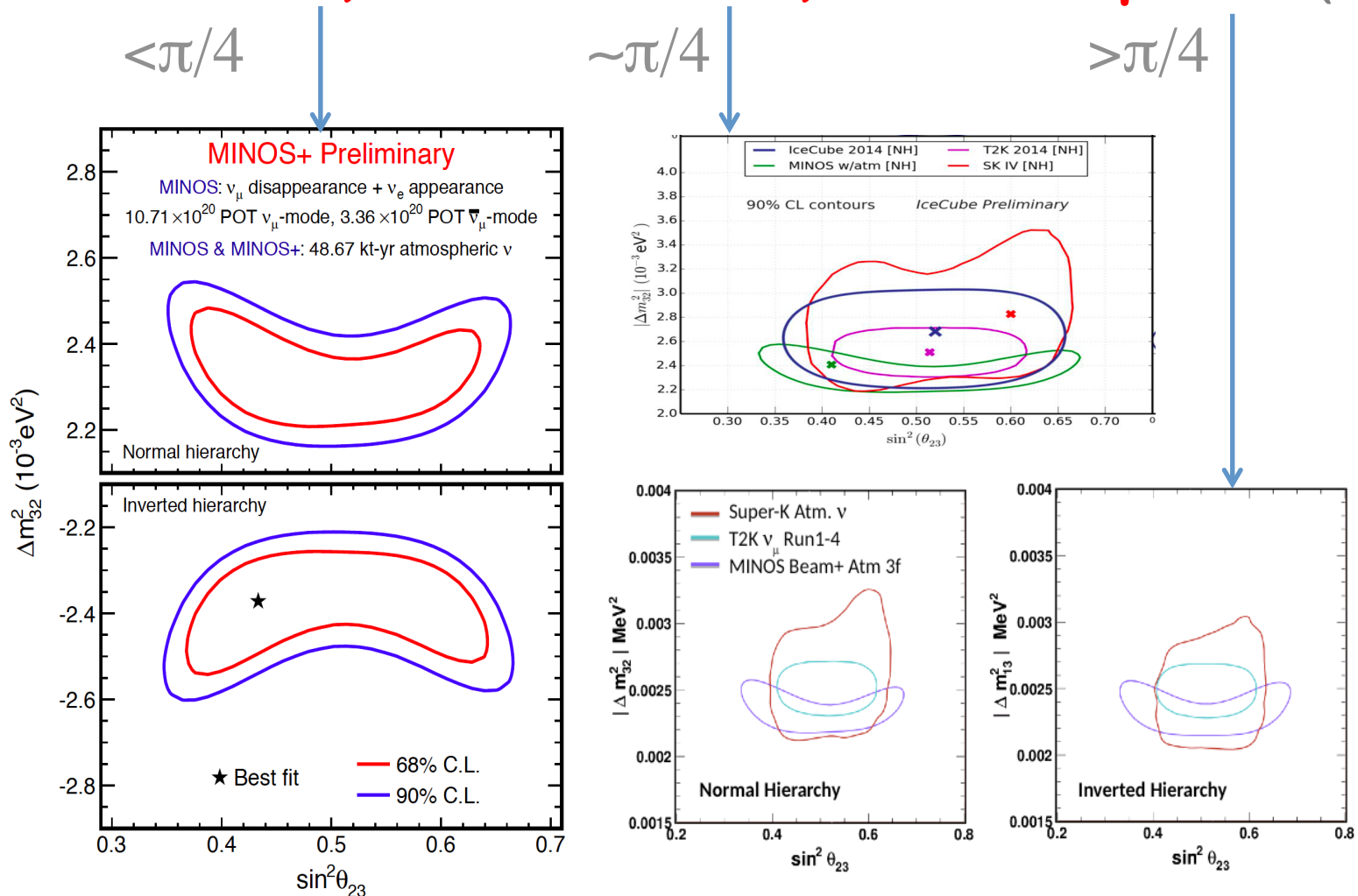
-0.3

-0.1

irrelevant

Current instability of octant (best fit) reflected in other new data presented at Neutrino 2014:

**MINOS+, IceCube atm., SK atm update (\*)**



(\*) To be included in our global analysis; work in progress.

## Status of absolute $\nu$ mass observables $\rightarrow (m_\beta, m_{\beta\beta}, \Sigma)$

In the 3 $\nu$  framework:

$\beta$  decay, sensitive to the “effective electron neutrino mass”:

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$

$0\nu\beta\beta$  decay: only if Majorana. “Effective Majorana mass”:

$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

**Cosmology:** Dominantly sensitive to sum of neutrino masses:

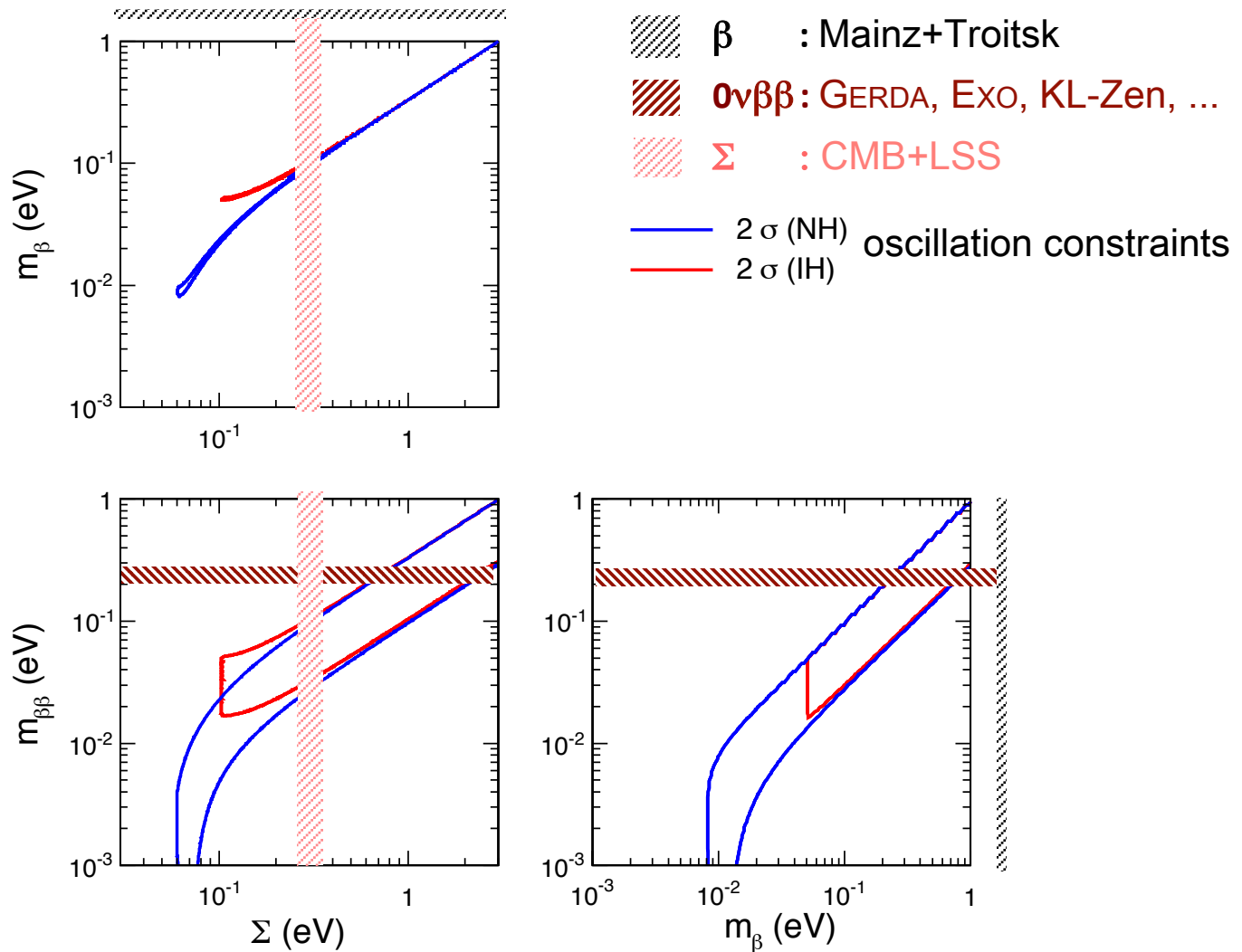
$$\Sigma = m_1 + m_2 + m_3$$

Note 1: These observables may provide handles to distinguish NH/IH.

Note 2: Majorana case gives a new source of CPV (unconstrained)

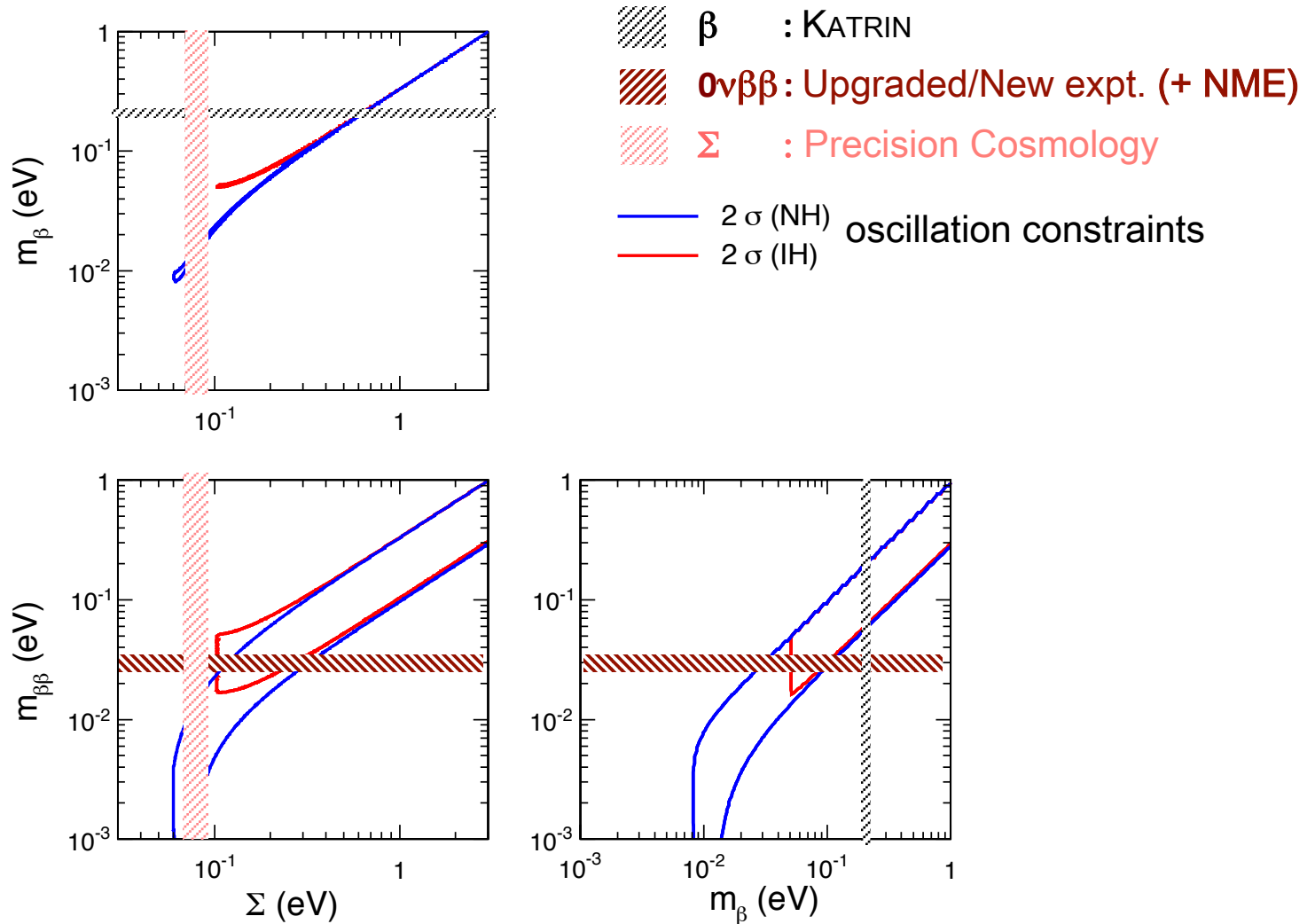
Note 2: The three observables are correlated by oscillation data  $\rightarrow$

# Upper limits on $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ (up to some syst.) + osc. constraints\*



\*arXiv:1205.5254 by Fogli, Lisi, Marrone, Montanino, Palazzo, Rotunno

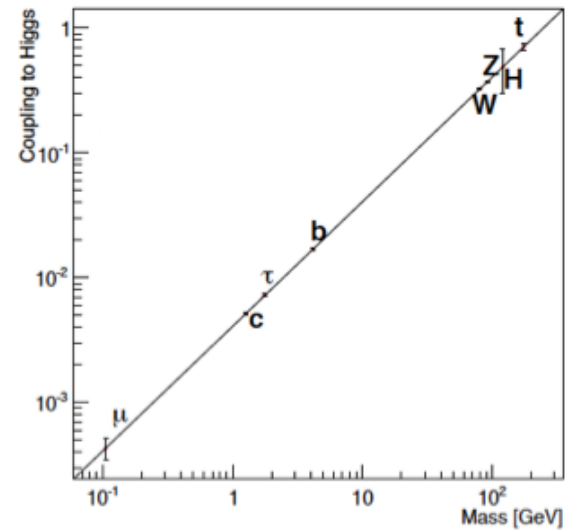
# Upper limits on $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ in $\sim 10$ years ?



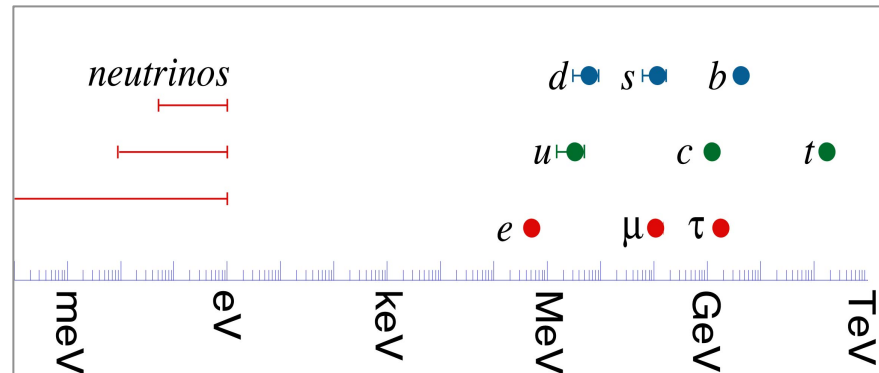
Large phase space for **discoveries about  $\nu$  mass and nature.**

# Towards a bigger picture...

## 1. Test Higgs sector

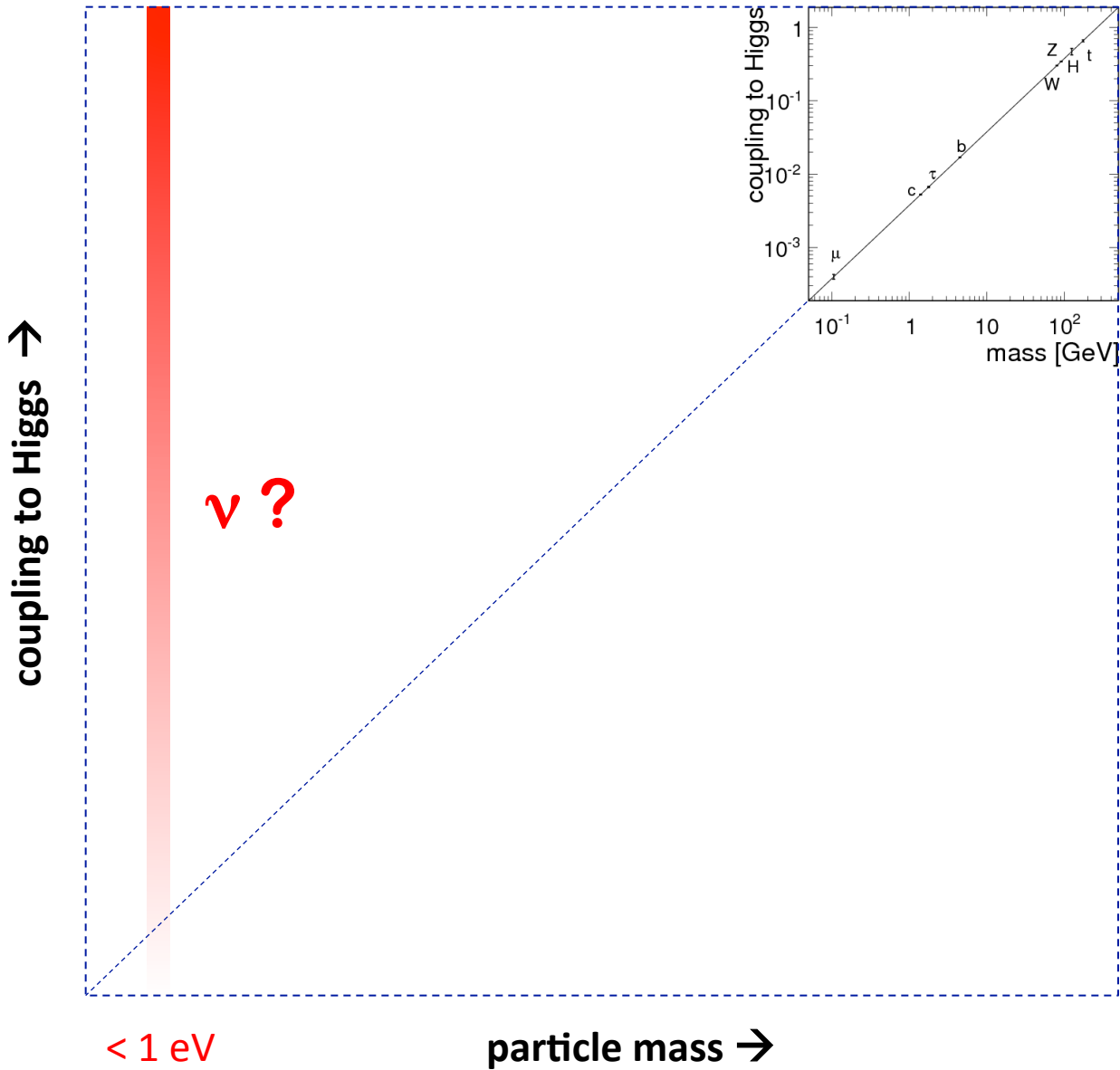


## 2. Find $\nu$ masses



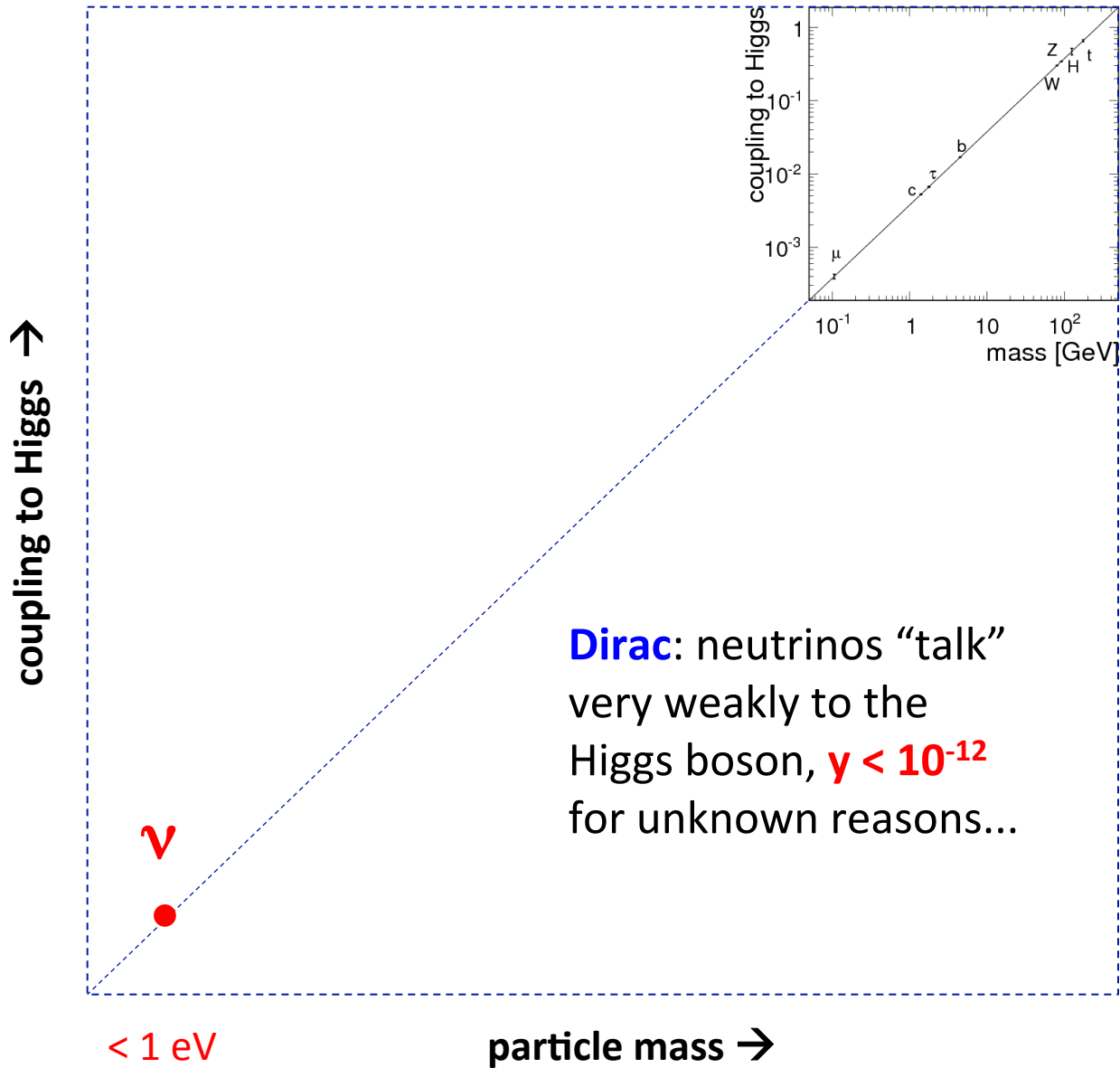
1 + 2

Where are the  $\nu$ 's on this plot? Why are they so light?

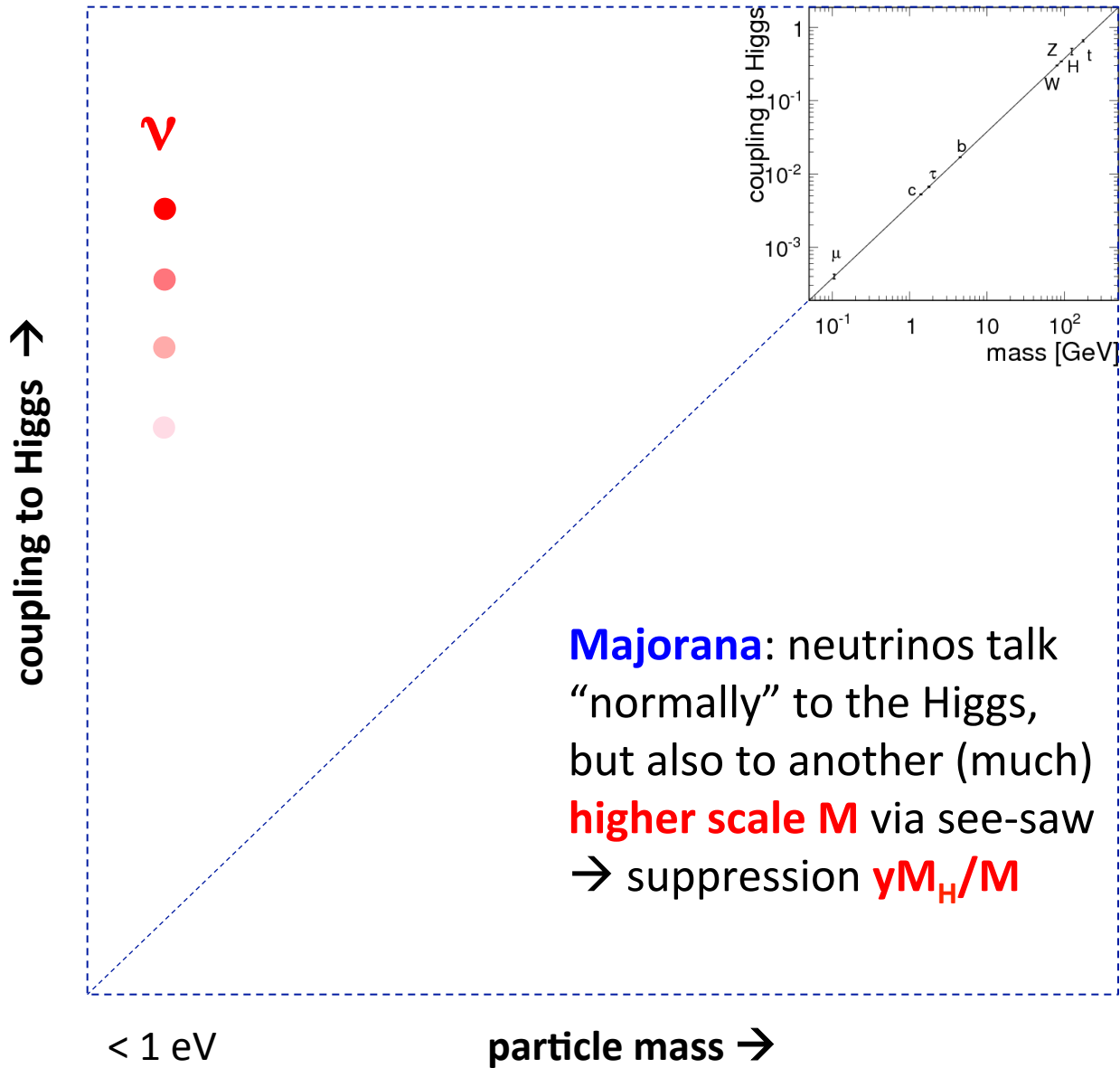




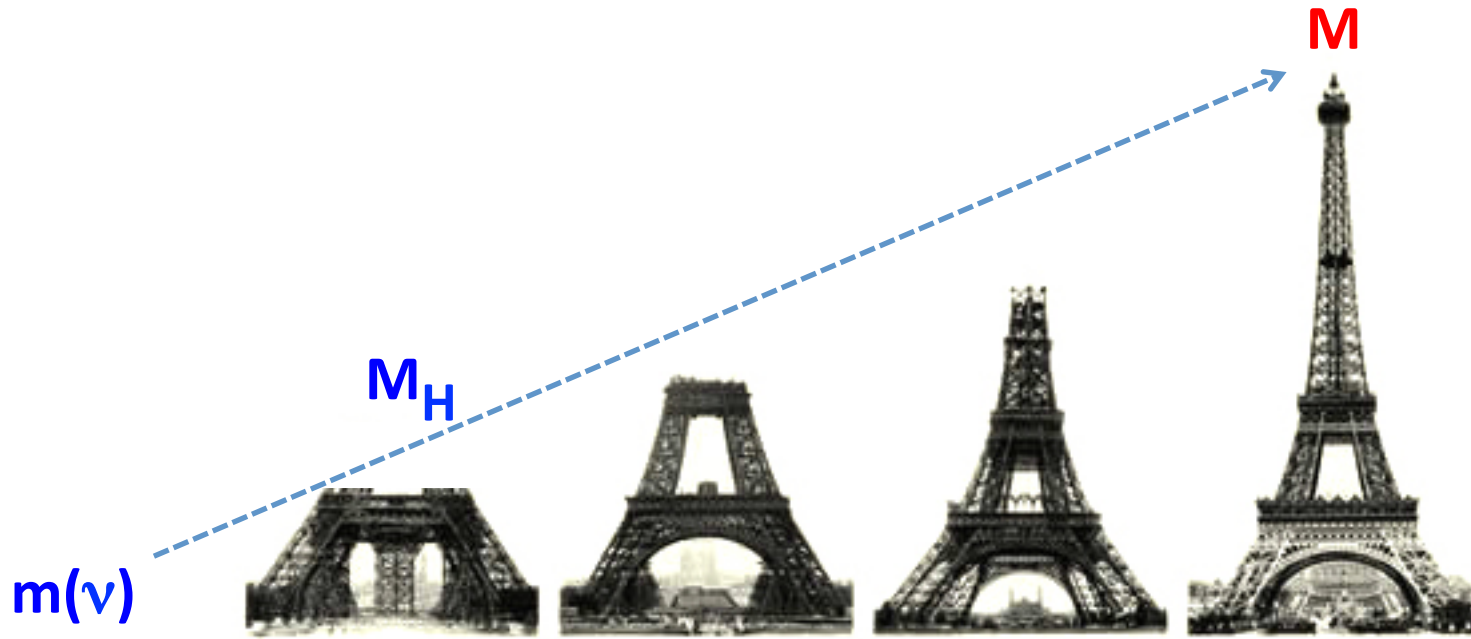
# Options:



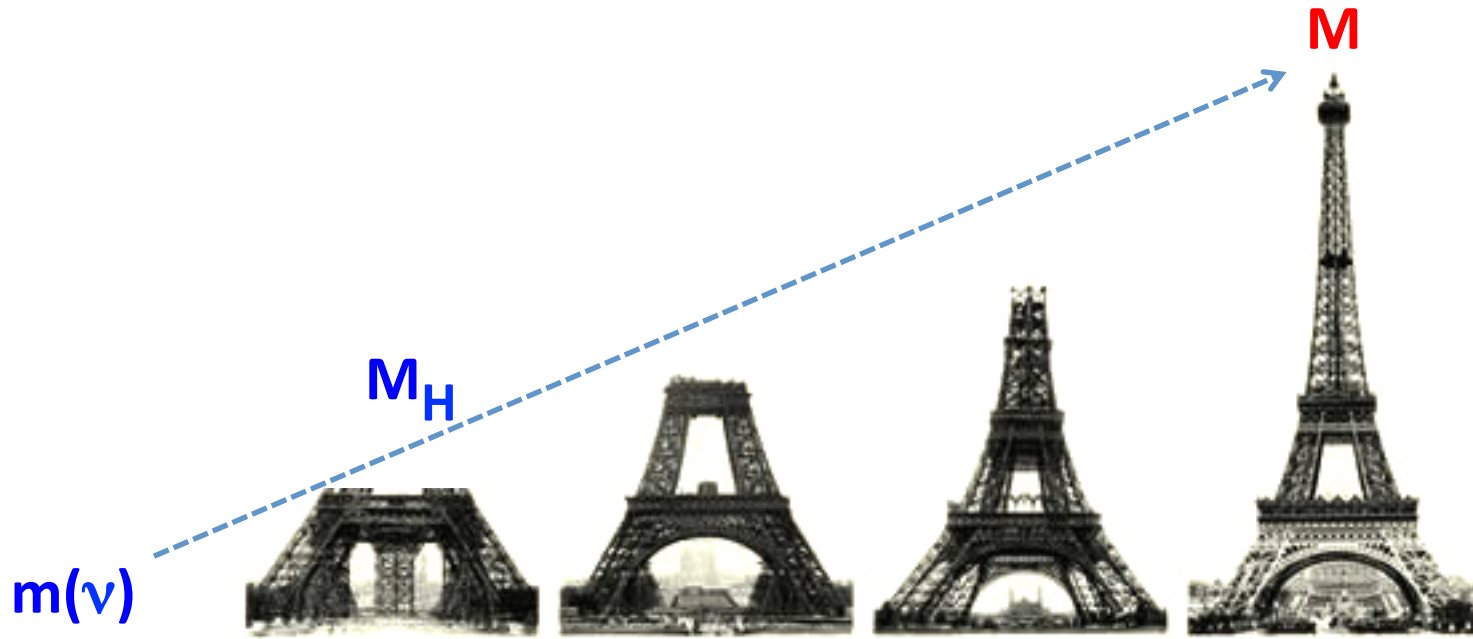
# Options:



The  $\nu$  flavor sector (masses, mixings and phases) may thus offer a great opportunity to probe **new physics beyond the EW scale ...**

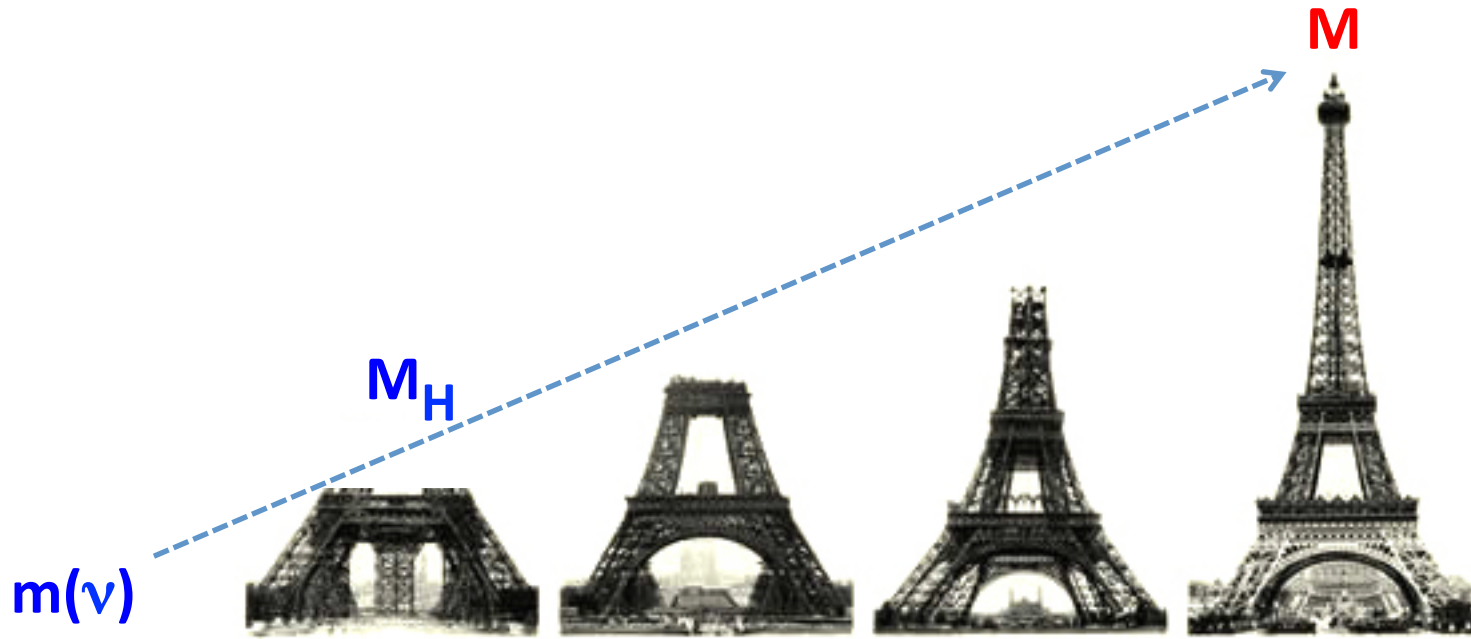


The  $\nu$  flavor sector (masses, mixings and phases) may thus offer a great opportunity to probe **new physics beyond the EW scale ...**



**... with the help of increasingly large infrastructures!**

The  $\nu$  flavor sector (masses, mixings and phases) may thus offer a great opportunity to probe **new physics beyond the EW scale ...**



**... with the help of increasingly large infrastructures!**

Thank you for your attention.

# Backup slides

# Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix

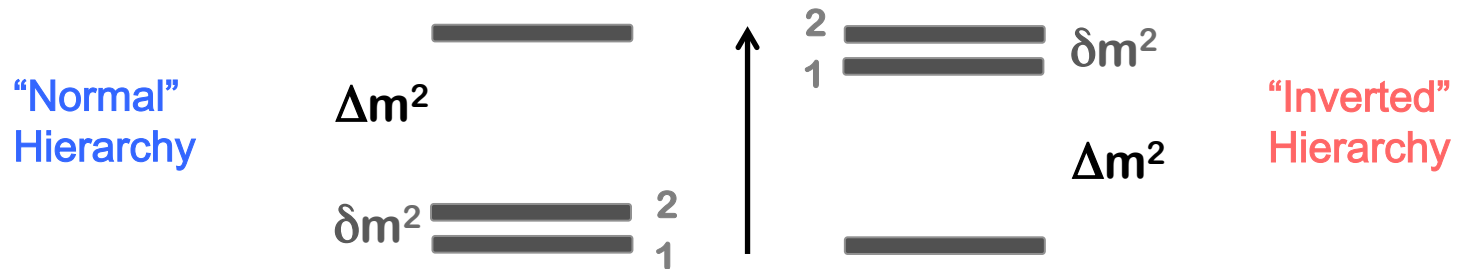
$$U_{\alpha i} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha/2} & 0 \\ 0 & 0 & e^{i\beta/2} \end{bmatrix}$$

[ only if Majorana ]

Mixing angles  $\theta_{23}$ ,  $\theta_{13}$ ,  $\theta_{12}$ : known ✓

CP-violat. phase(s)  $\delta$  ( $\alpha$ ,  $\beta$ ): unknown ✗

## Mass-squared spectrum (up to absolute scale)



[ + contribution in matter  $\sim G_F \cdot E \cdot \text{density}$  ]

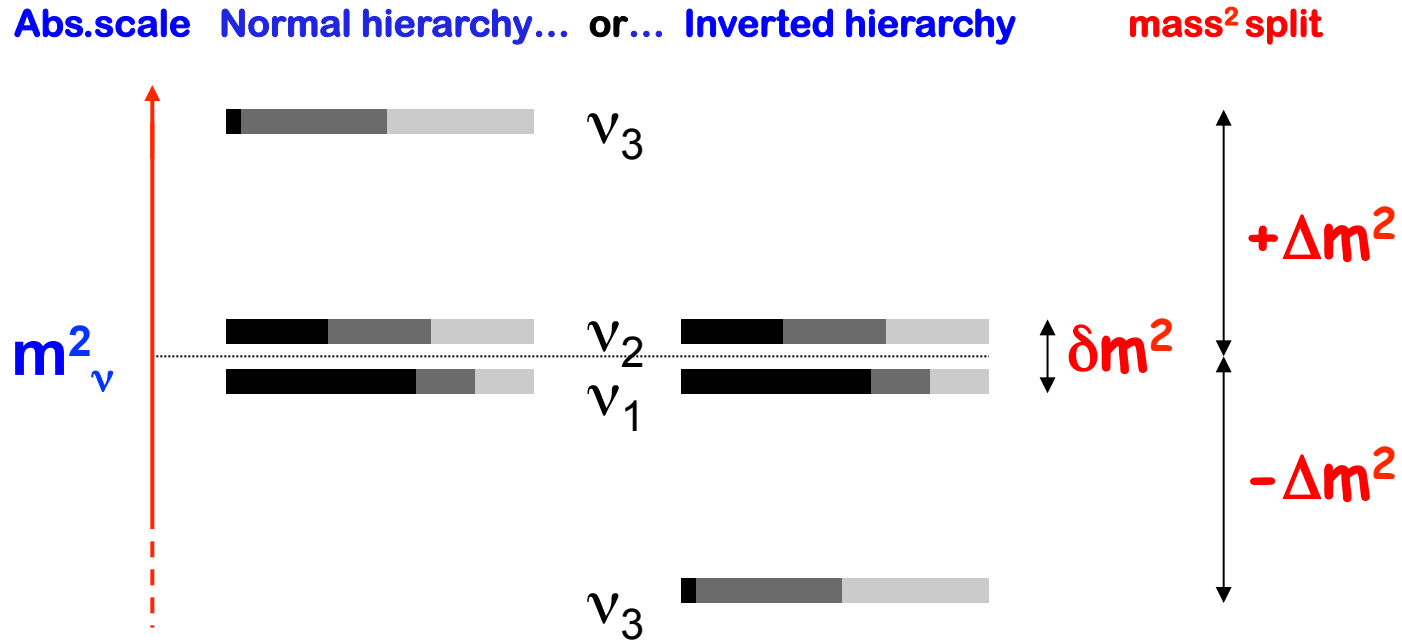
$\delta m^2$ ,  $\Delta m^2$ : known ✓

Matter effects (solar  $\nu$ ): ✓

Hierarchy: unknown ✗

# Current 3 $\nu$ picture in just one slide (with 1-digit accuracy)

Flavors =  $e \ \mu \ \tau$



Knowns:

$$\delta m^2 \sim 8 \times 10^{-5} \text{ eV}^2$$

$$\Delta m^2 \sim 2 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{12} \sim 0.3$$

$$\sin^2 \theta_{23} \sim 0.5$$

$$\sin^2 \theta_{13} \sim 0.02$$

Unknowns:

$\delta$  (CP)

$\text{sign}(\Delta m^2)$

$\text{octant}(\sin^2 \theta_{23})$

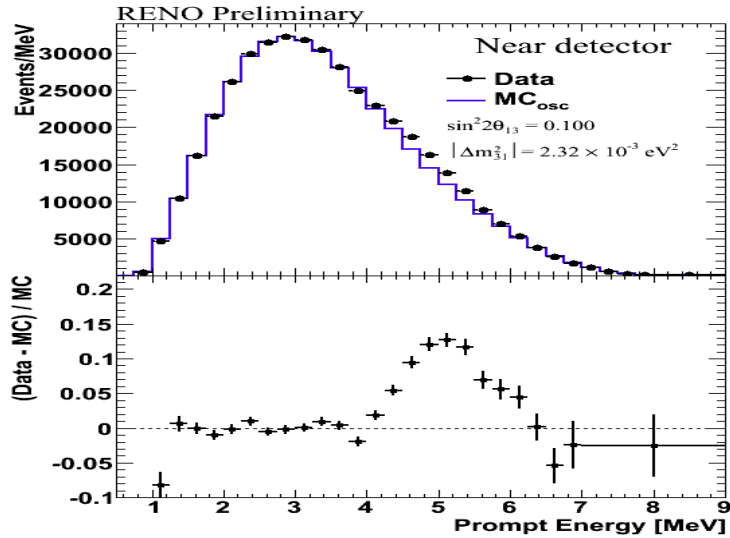
absolute mass scale

Dirac/Majorana nature

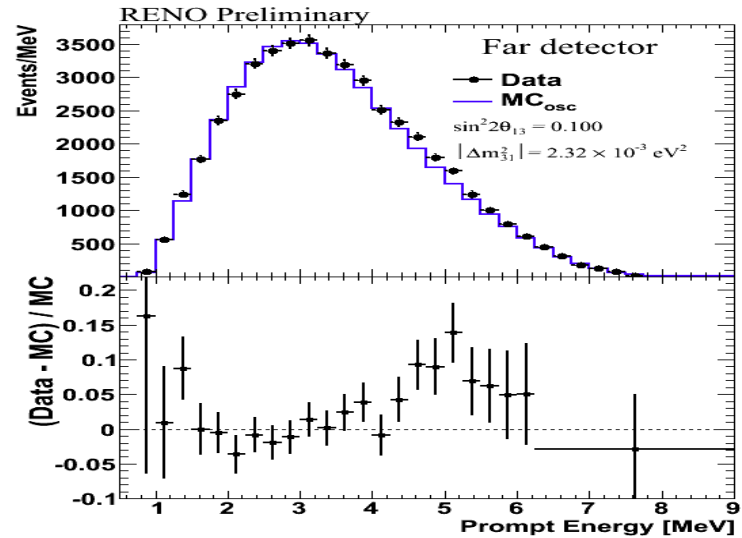


# Reactor spectra at Neutrino 2014

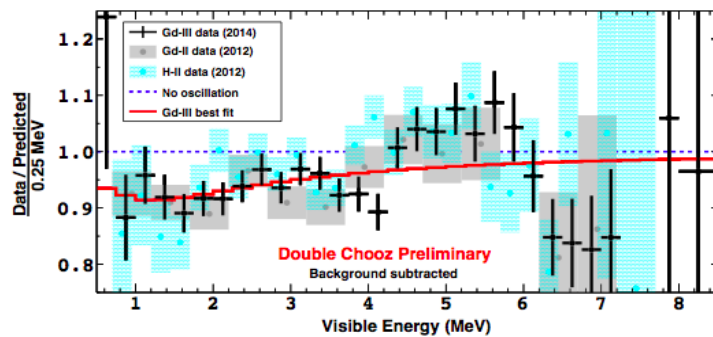
## RENO near



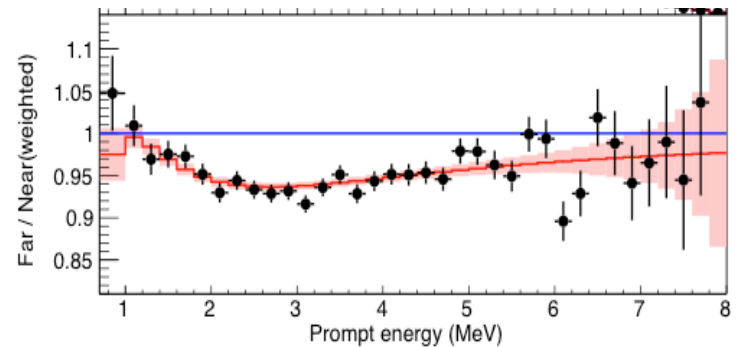
## RENO far



## DC far/predicted



## Daya Bay far/near

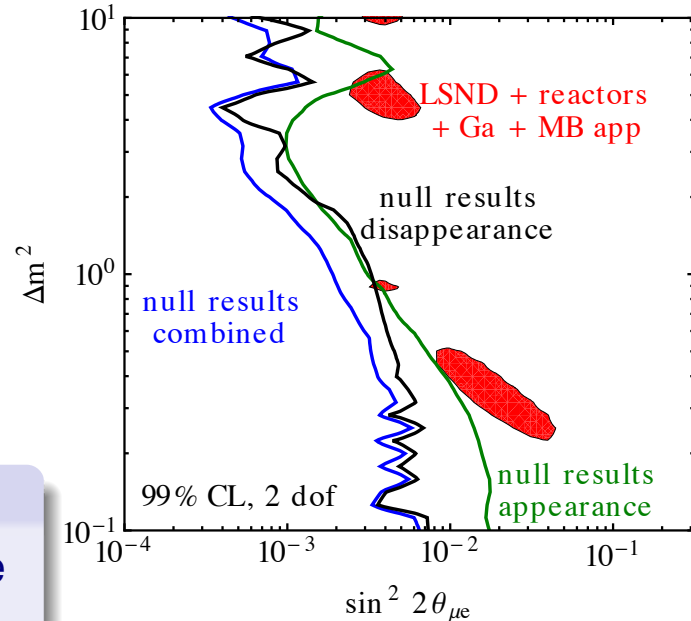


# Sterile neutrinos: J. Kopp at $\nu$ 2014

## The global oscillation fit

JK Machado Maltoni Schwetz, arXiv:1303.3011

3 + 1 Severe **tension** between appearance and disappearance and between exp's with and without a signal



Parameter goodness of fit (PG) test:

Compares  $\chi^2_{\min}$  from global and separate fits to test **compatibility of 2 data sets**

	$\chi^2_{\min}/\text{dof}$	GOF	$\chi^2_{\text{PG}}/\text{dof}$	PG
3+1	712/(689 - 9)	19%	18.0/2	$1.2 \times 10^{-4}$

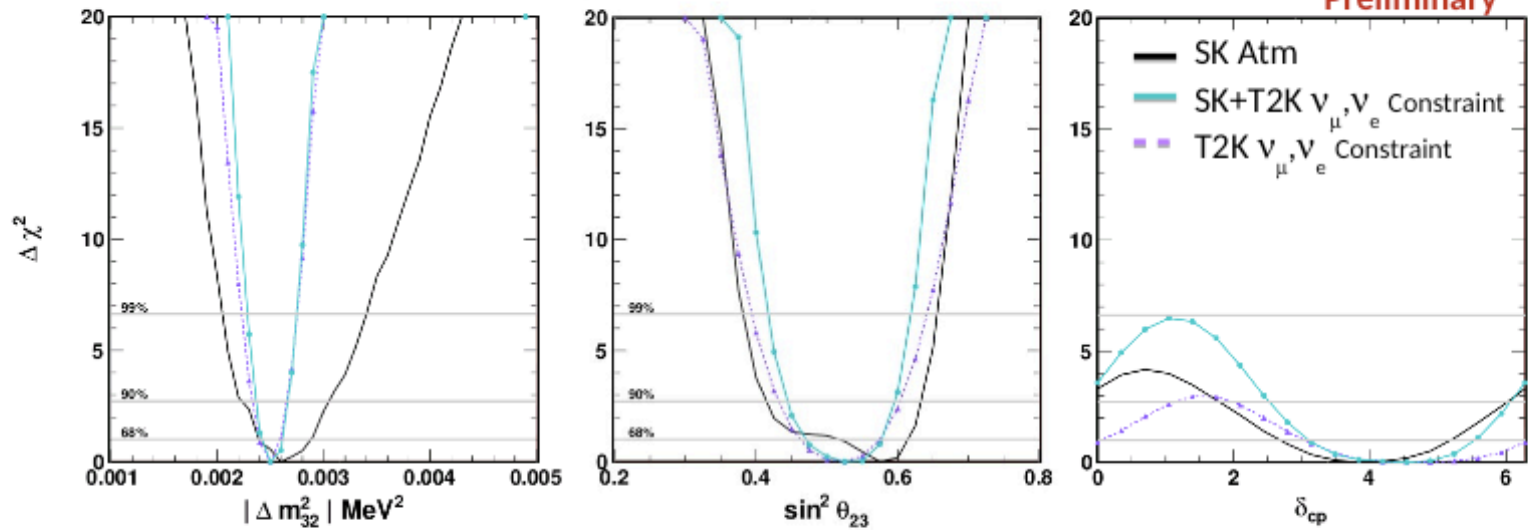
# Sterile neutrinos: J. Kopp summary at $\nu$ 2014

- Sterile neutrinos are **theoretically well motivated** and **phenomenologically useful**
- **Tension** between **appearance** and **disappearance** searches
- **Neutrino 2014**: several interesting new limits
  - ▶ Will increase the tension
  - ▶ Qualitative conclusions strengthened
- **Cosmology disfavors**  $N_\nu \geq 4$ , especially for  $m_{\nu_s} \gtrsim 0.23$  eV.  
(if BICEP-2 is included, this conclusion would change)
- **Many mechanisms** for making sterile neutrinos **fully consistent with cosmology**
  - ▶ **Example: hidden sector gauge force**
  - ▶ Can additionally **solve small scale structure problems** if coupled also to **dark matter**
- Sterile neutrinos and **dark matter searches**
  - ▶ **Direct searches: non-standard neutrino signals** in DM detectors
  - ▶ **Indirect searches: limits on DM annihilation in the Sun** modified by active–sterile oscillations

# R. Wendell – SK atmospheric at $\nu$ 2014

19

Theta13 Fixed SK + T2K  $\nu_\mu, \nu_e$  (External Constraint) NH



Fit (543 dof)	$\chi^2$	$\theta_{13}$	$\delta_{cp}$	$\theta_{23}$	$\Delta m_{23} (x10^{-3})$
SK + T2K (NH)	578.2	0.025	4.19	0.55	2.5
SK + T2K (IH)	579.4	0.025	4.19	0.55	2.5

■  $\chi^2_{IH} - \chi^2_{NH} = -1.2$  (-0.9 SK only)

■ CP Conservation ( $\sin\delta_{cp} = 0$ ) allowed at (at least) 90% C.L. for both hierarchies

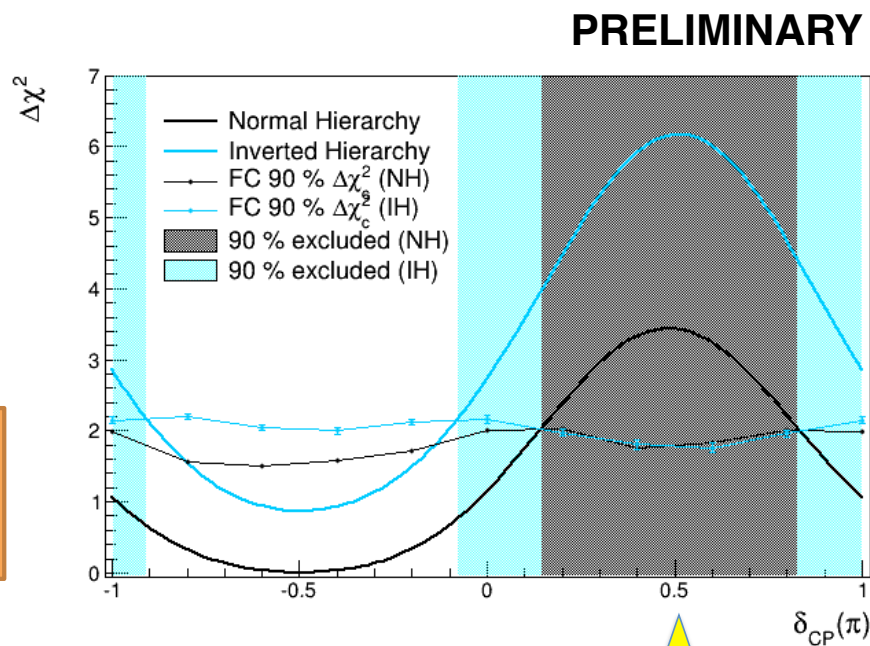
# T2K: C. Walter at Neutrino 2014

## T2K Joint $\nu_\mu + \nu_e$ Analysis: Constraints on $\delta_{CP}$

*Likelihood ratio fit  
to both  $\nu_\mu + \nu_e$   
event samples*

Plot includes constraint  
from reactor experiments  
as given by PDG 2013.

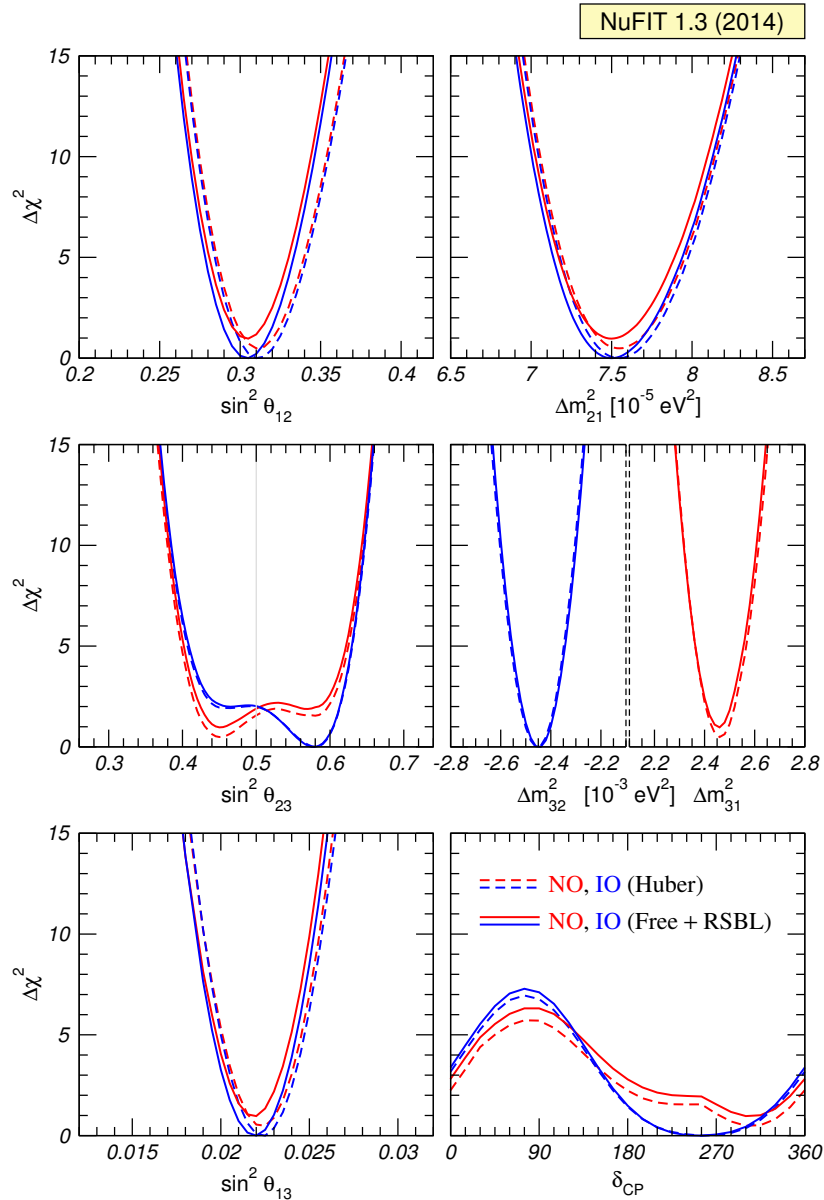
T2K has a slight hint for the  
normal hierarchy with a value  
of  $\delta_{CP}$  of  $-\pi/2$



**FUTURE -> Neutrino + Antineutrino running!**



# Gonzalez-Garcia, Maltoni, Salvado, Schwetz'14



# Forero, Tortola, Valle '14

