

Measuring the Higgs Self-Couplings

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Outline

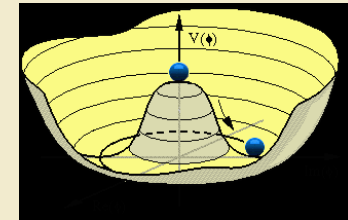
- Why measure the Higgs-self couplings?
- What do we expect?
 - Standard Model
 - Beyond the Standard Model
- Some phenomenology

How far from the SM prediction
can the HH rate get?

SM Higgs Mechanism

- Standard Model includes complex Higgs SU(2) doublet

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix} = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix}$$



- With SU(2) x U(1) invariant scalar potential

$$V = \mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$

- If $\mu^2 < 0$, then spontaneous symmetry breaking
- Minimum of potential at:

$$\langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$

$$\Phi \rightarrow e^{i\varpi^a \cdot \sigma^a / v} \begin{pmatrix} 0 \\ \frac{h+v}{\sqrt{2}} \end{pmatrix}$$

After symmetry breaking

$$V = -\frac{M_H^2}{2}H^2 + \lambda_3 H^3 + \lambda_4 H^4$$

- HHH and HHHH couplings prediction of theory

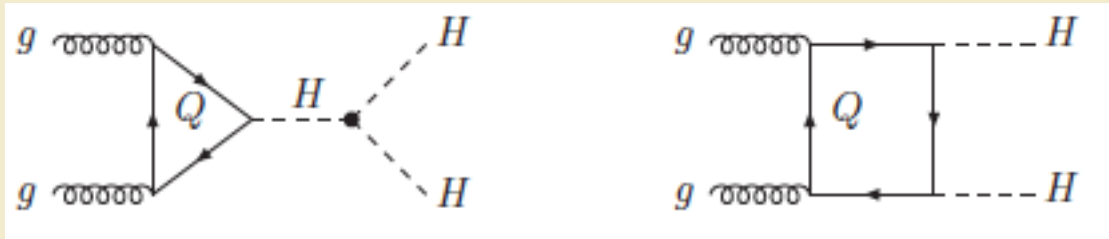
- They are perturbative $\lambda_3 = \frac{M_H^2}{2v} \sim .13v$ $\lambda_4 = \frac{M_H^2}{8v^2}$

- Calculations sensible

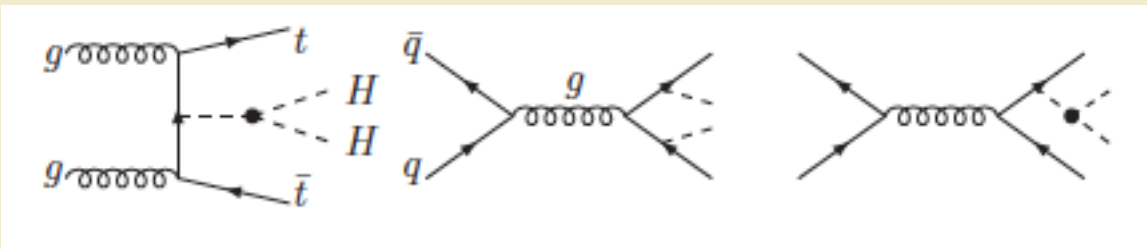
- In general $V = \sum_n \frac{c_n}{\Lambda^{2n}} \left(\Phi^\dagger \Phi - \frac{v^2}{2} \right)^{2+n}$

Corrections to relationship between λ_3 and λ_4 of $O(1/\Lambda^2)$

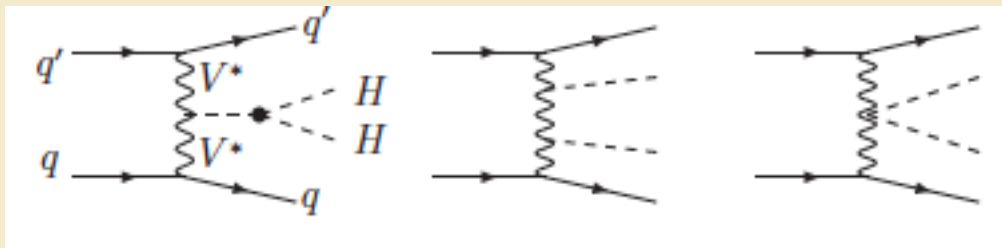
Production of HH



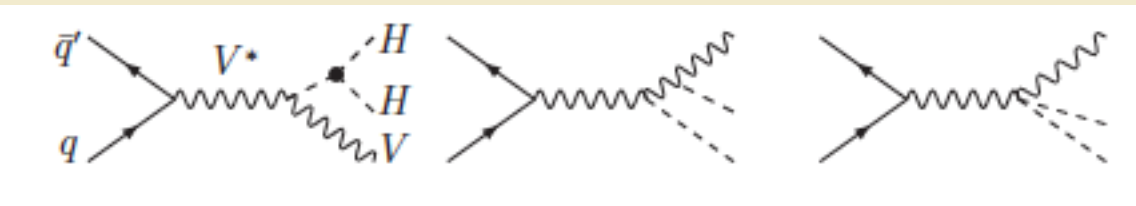
Sensitive to heavy colored particles (eg stops or top partners)



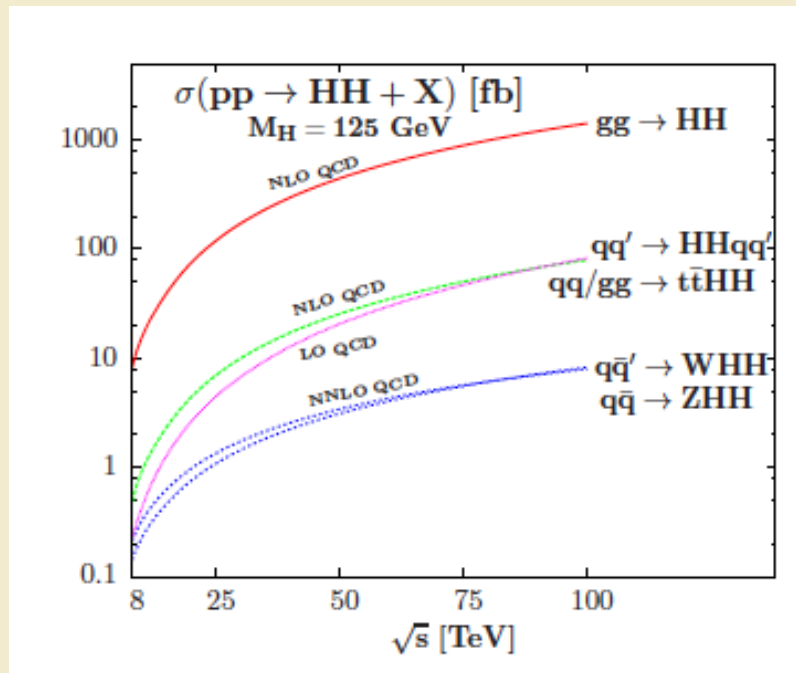
Sensitive to anomalous top-Higgs couplings



Sensitive to anomalous VVHH couplings



Small Rates



gg rate increases by a factor of ~ 40 when going from 14 TeV to 100 TeV

Gluon fusion is always the largest production channel

K factor ~ 2 for $gg \rightarrow HH$

Theory Uncertainties

- For $gg \rightarrow H$: PDF, α_s , scale uncertainties give $\pm \sim 15\text{-}20\%$ uncertainties
 - Theory frontier is understanding uncertainties in jet binning
- For $gg \rightarrow HH$ at 14 TeV: $\sigma_{gg \rightarrow HH} = 34 \text{ fb}^{+18\%+4\%}_{-15\%-4\%}$
 - Scale PDF
- Calculation includes QCD in $m_t \rightarrow \infty$ limit

Need more theory!

Two Higgs Production at LHC

- Cross section has spin-0 and spin-2 contributions

$$\frac{d\sigma(gg \rightarrow HH)}{dt} = \frac{\alpha_s^2}{32768\pi^3 v^4} \left(|F_0|^2 + |F_2|^2 \right)$$

- $M_H^2 \gg s, p_T^2$ (low energy theorem)

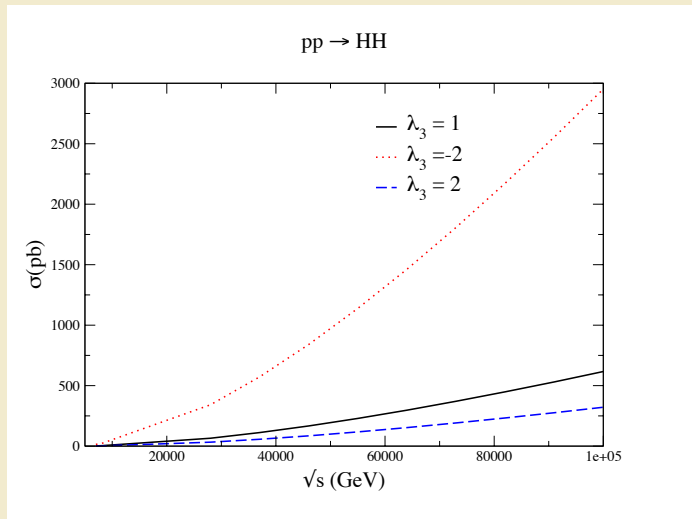
$$F_0 \rightarrow -\frac{4}{3} + \frac{4M_H^2}{s - M_H^2} (\lambda_3)$$

$$F_2 \rightarrow 0$$

HHH coupling (1 for SM)

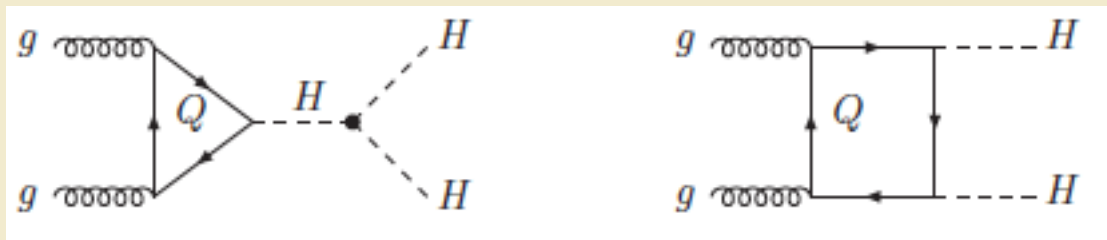
- For large s , dependence on λ_3 suppressed
- More sensitivity to negative λ_3
- Exact cancellation at threshold

Small Rates



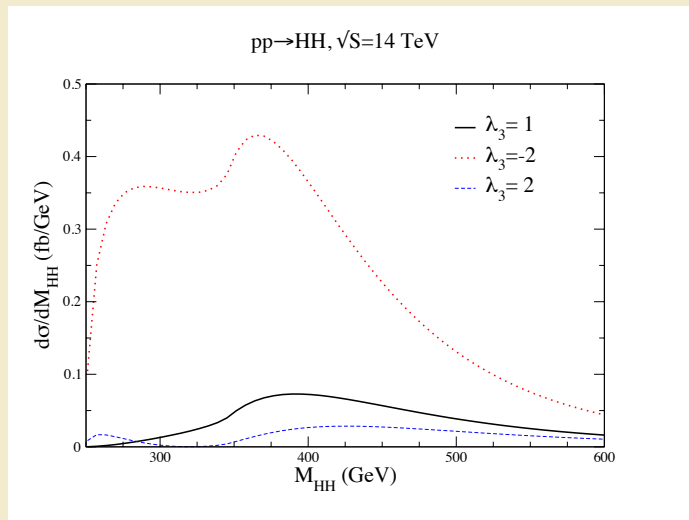
For $\sqrt{S}=14$ TeV,
 $K \sim 2$ in $m_t \rightarrow \infty$ limit
 (not in plot)

Sensitivity to HHH coupling

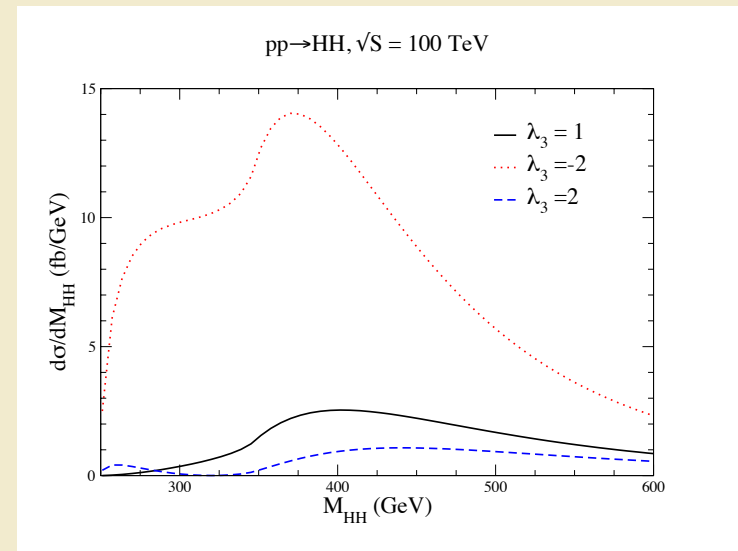


* Exact calculation, not low energy theorem

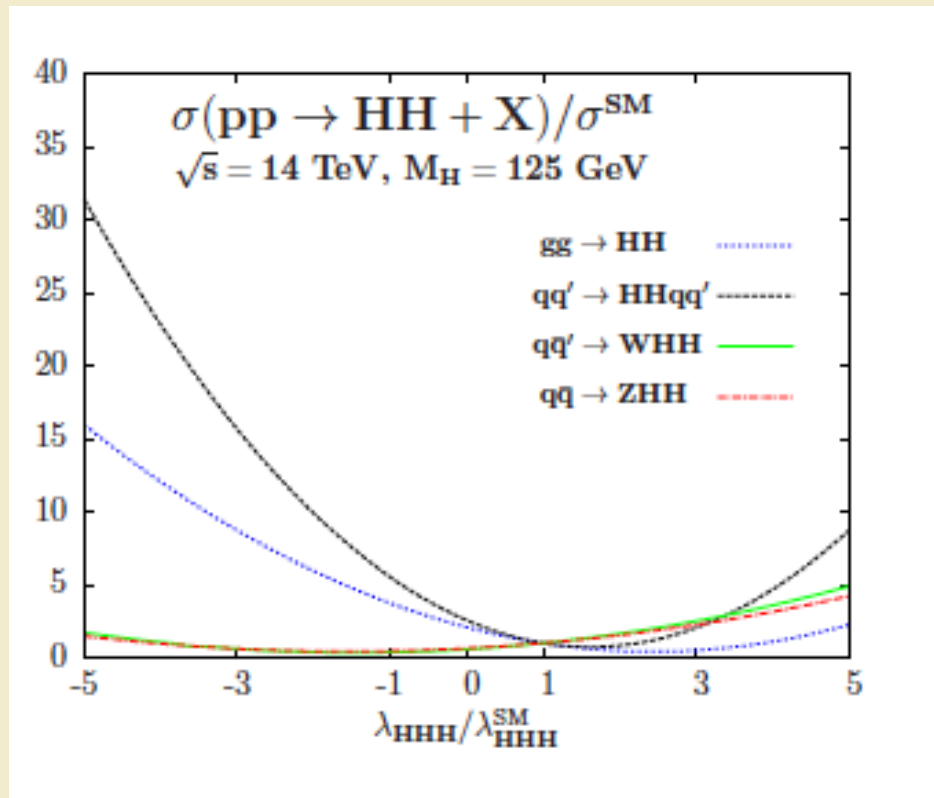
Distributions sensitive to λ_3



Gluon fusion



VBF is most sensitive channel to λ_3

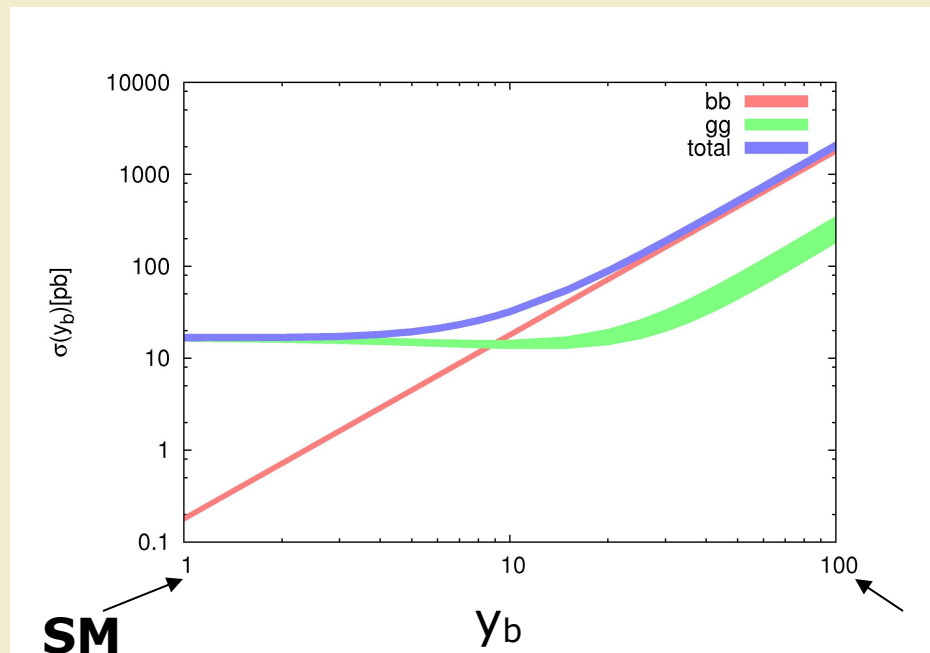


Fit $\sigma / \sigma_{\text{sm}}$ as a function of $\lambda / \lambda_{\text{sm}}$ to extract measurement of λ

The Role of b-loops in Single Higgs

K factor for b loops smaller than for top loops

b loops are 2-5% of SM $gg \rightarrow H$

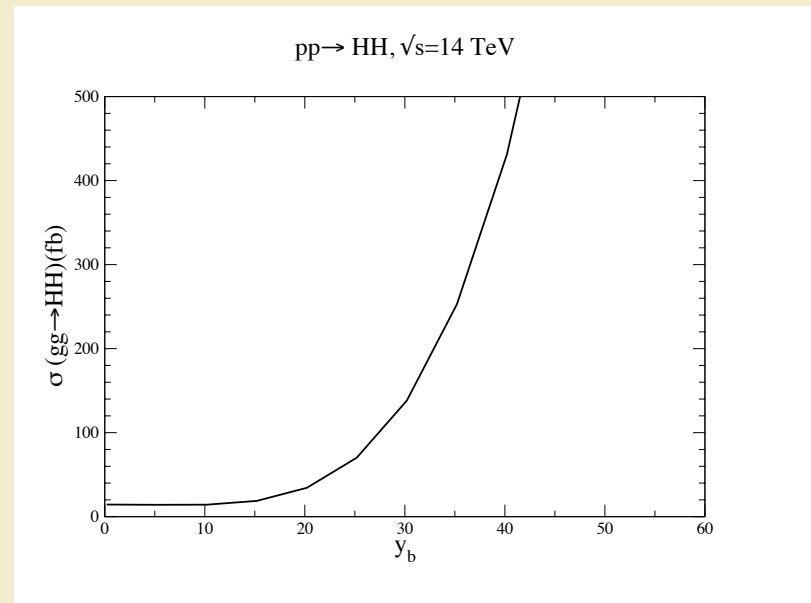
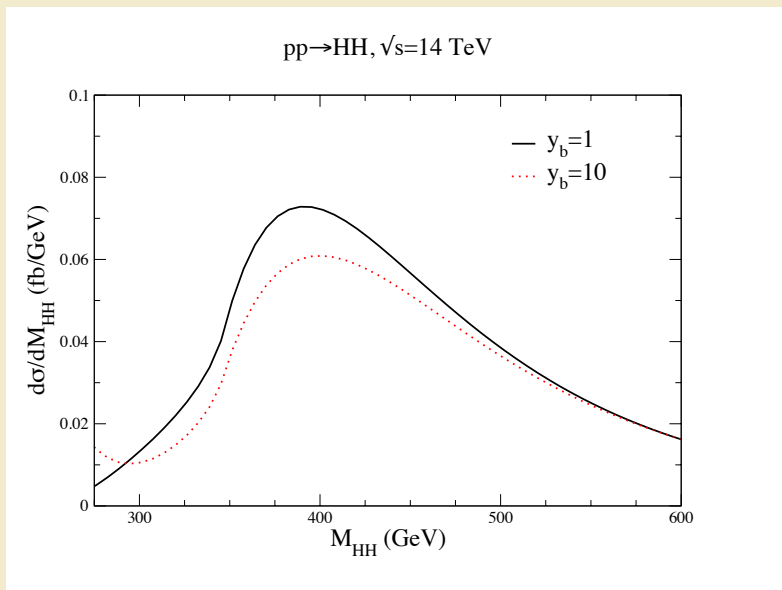


$$L \sim \frac{m_b}{v} y_b \bar{b} h H$$

**gg “only”
NLO**

Sensitivity to y_b

- Y_b comes in twice in box diagrams



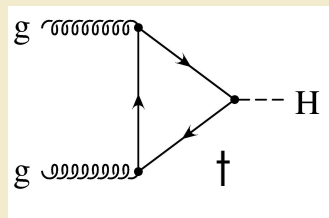
But we already know $y_b < 4$ from single Higgs production

Adding heavy fermions

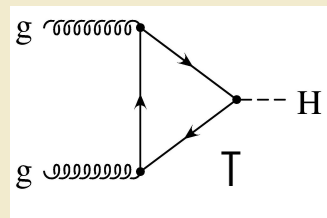
- Can't add new chiral generation:

$$\sigma(gg \rightarrow H) \rightarrow \sigma_{SM}(1 + N_F)^2$$

- Add vector fermions:
 - Left and right-handed fermions transform the same way under $SU(2)$: T_L and T_R



$\sim \cos^2\theta$

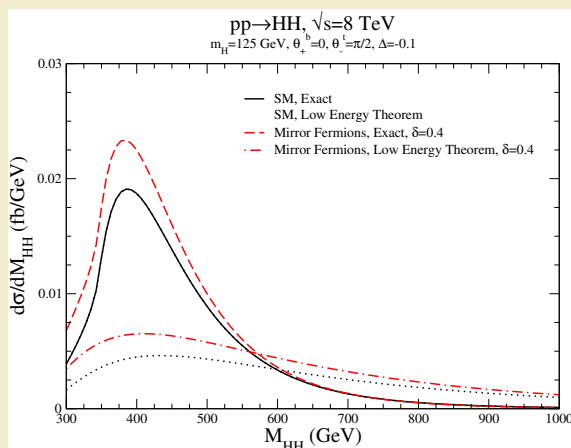


$\sim \sin^2\theta$

➡ Generically, hard to get far from Standard Model result

Double Higgs Rate: How big can it be?

- Toy model with top partners
 - Many restrictions on parameters from precision EW
 - Single Higgs rate always suppressed in these models
- $gg \rightarrow H$ rate assumed to be 90% of SM
- $gg \rightarrow HH$ rate can be increased by $< 20\%$ relative to SM



Optimal choice of parameters

Fairly general result: leading contributions to H and HH production in top partner models are similar to SM

Double Higgs in Composite Models

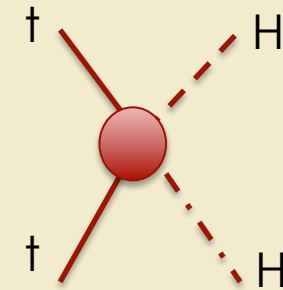
- MCHM5 model:
 - Top partners couple to Higgs
 - SM-like particles don't couple directly to Higgs
 - Higgs couplings scaled by parameter ζ
- Single Higgs production suppressed

$$R = \frac{\sigma(pp \rightarrow H)}{\sigma(pp \rightarrow H) |_{SM}} \sim (1 - 3\zeta)$$

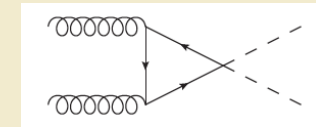
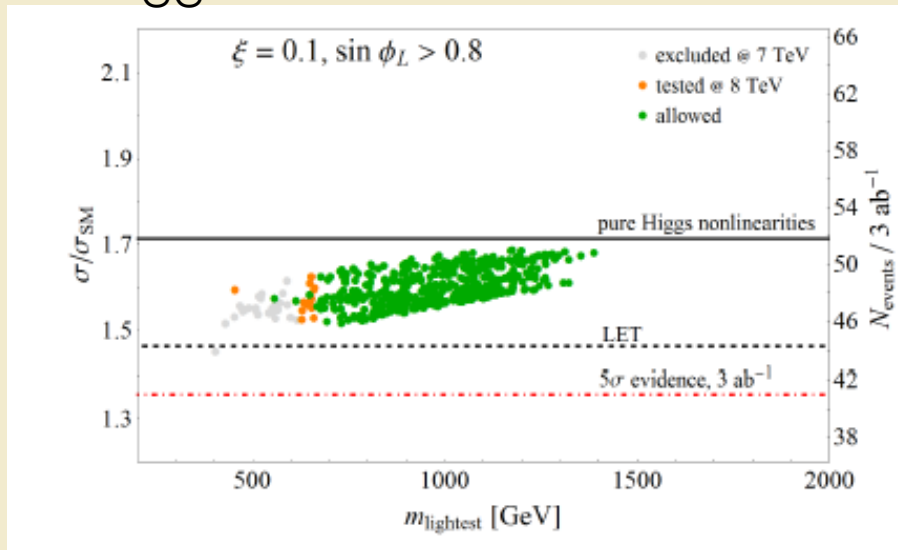
- Suppose $R_{\text{experimental}} > 0.8$
 - $\zeta < .07$

HH in Composite Models

- HH production enhanced
 - Enhancement grows with ξ
- New effect: ttHH vertex
 - Can have O(1) effects



gg → HH

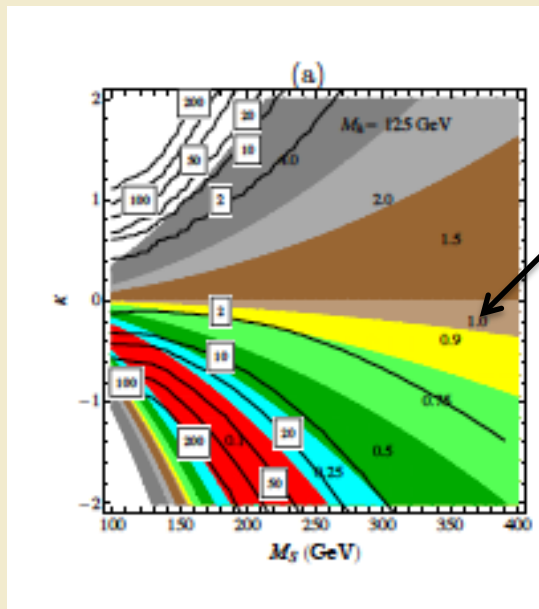
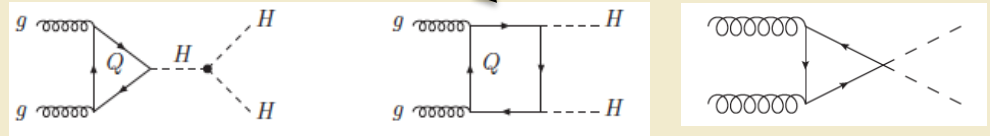


Number of $b\bar{b}\gamma\gamma$ events
(1 tagged b jet)

One more model

- Add colored octet scalars with mixing to SM H: $\kappa\phi\phi H^2$
- Motivation:
 - large coupling to gluons
 - $\phi\phi HH$ vertex

New scalars



Single H/single H SM less than #

Boxes #: ratio of HH to HH(SM)

Same story.... Knowing single Higgs production rate restricts double Higgs possibilities

Double Higgs Production

- If fermion masses arise from electroweak symmetry breaking, they have the form

$$O_{LE} = \frac{\alpha_s}{24\pi} G_{\mu\nu}^A G^{A,\mu\nu} \log\left(\frac{H^+ H}{v^2}\right) = \frac{\alpha_s}{12\pi} G_{\mu\nu}^A G^{A,\mu\nu} \left(\frac{H}{v} - \frac{H^2}{2v^2}\right)$$

- A general expansion could also generate

$$O_{eff} = \frac{\alpha_s}{4\pi} C_1 G_{\mu\nu}^A G^{A,\mu\nu} \left|\frac{H^+ H}{v^2}\right|^2 = \frac{\alpha_s}{4\pi} C_1 G_{\mu\nu}^A G^{A,\mu\nu} \left(\frac{H}{v} + \frac{H^2}{2v^2}\right)$$

- Measuring single and double Higgs production is window into source of EWSB, but probe the same operators

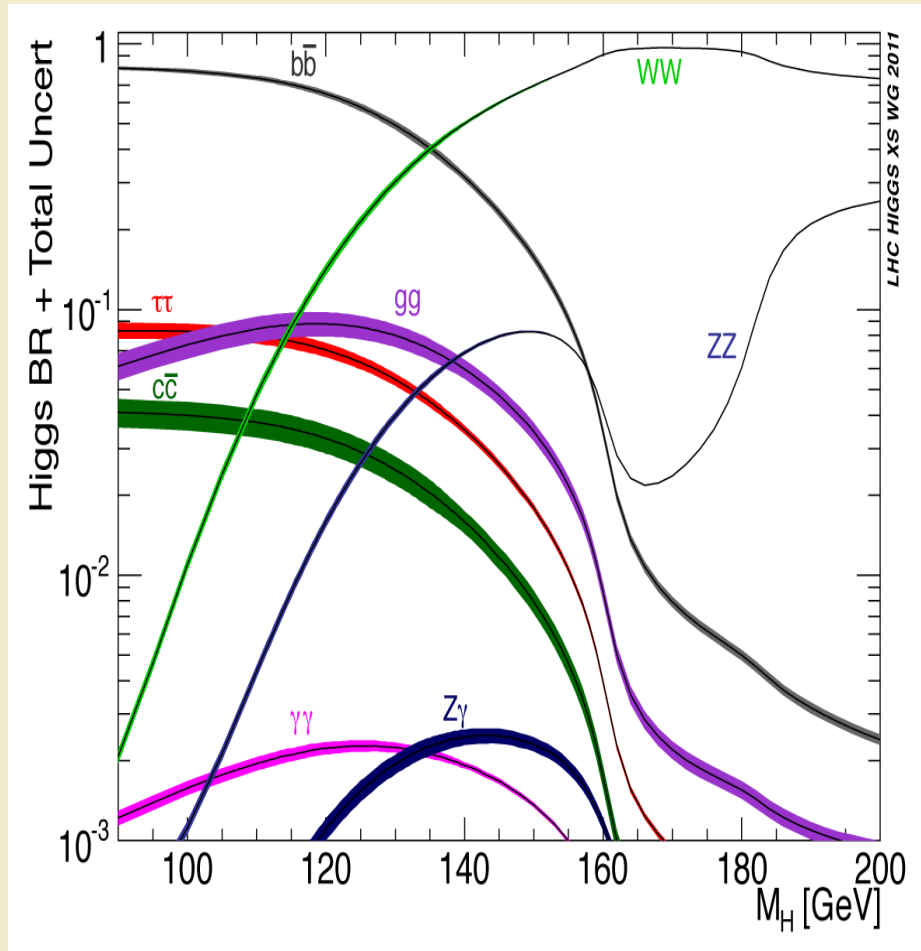
The Bottom Line

- Since single Higgs production rate is $\sim SM$
- Hard to get double Higgs production much more than $\sim 2Xs SM$ in models with only one Higgs
- No general theorem....it's proof by exhaustion

Models with multiple Higgs can get enhancements from resonance production,
 $gg \rightarrow H \rightarrow hh$

Higgs portal model (tuned) can get $\sim Xs 20\%$ enhancement of hh rate

HH decays



Channels studied:

$$HH \rightarrow b\bar{b}\gamma\gamma$$

$$HH \rightarrow b\bar{b}\tau^+\tau^-$$

$$HH \rightarrow b\bar{b}W^+W^-$$

Measuring HH Production

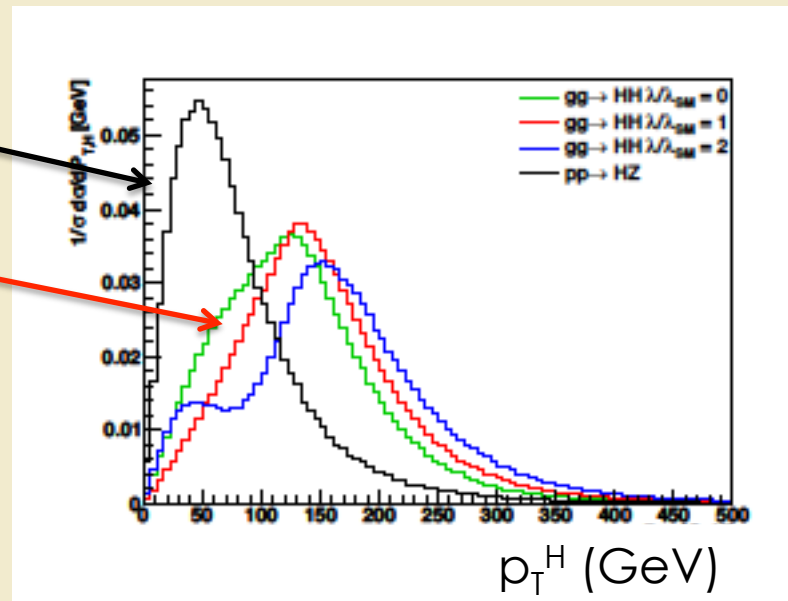
- Higgs are boosted

$gg \rightarrow HH$

Background from ZH

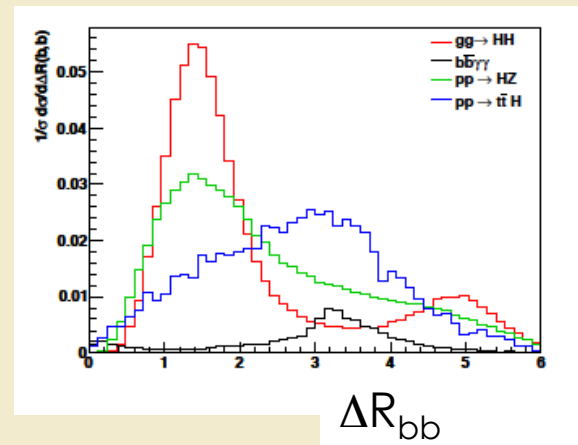
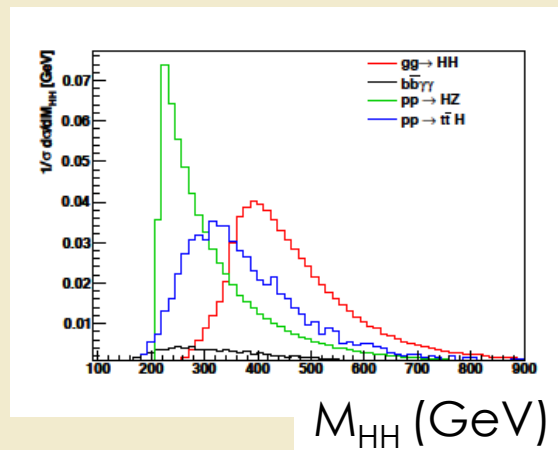
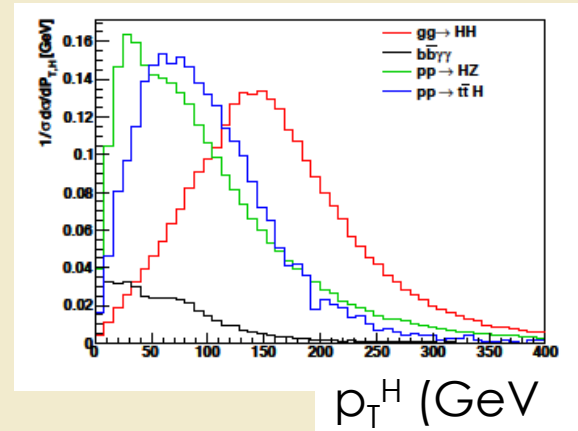
SM

In boosted regime,
less sensitivity to λ_3



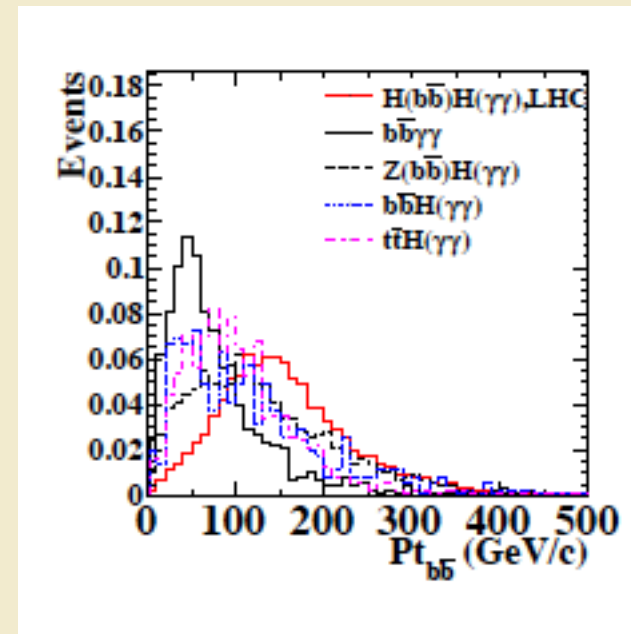
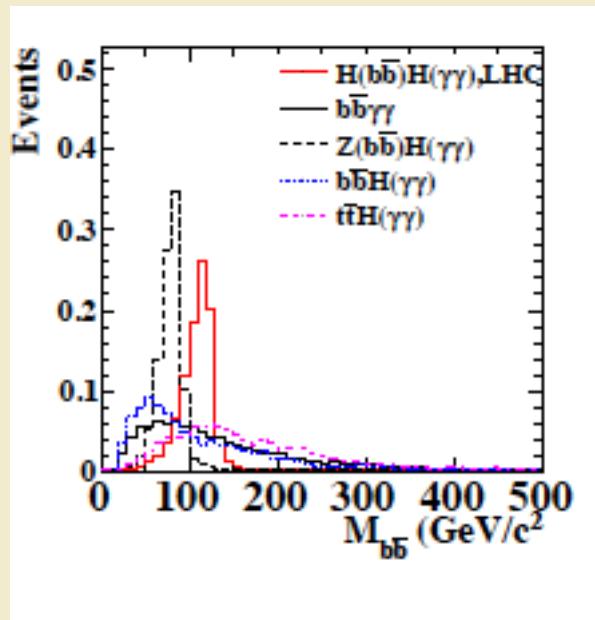
14 TeV: HH \rightarrow bb $\gamma\gamma$

- Cut based analysis
- $s/\sqrt{B} \sim 16$ with **51 signal events** in 3 ab^{-1}



Snowmass Simulation: 14/33/100 TeV: $HH \rightarrow b\bar{b}\gamma\gamma$

- Delphes simulation framework



Snowmass Simulation: $HH \rightarrow b\bar{b}\gamma\gamma$

- Before cuts:

Samples	Gen. cuts	HL-LHC		TeV33		TeV100	
		$\sigma \cdot B$ (fb)	Event	$\sigma \cdot B$ (fb)	Events	$\sigma \cdot B$ (fb)	Events
$H(b\bar{b})H(\gamma\gamma)$		0.0892	80000	0.545	80000	3.73	80000
$b\bar{b}\gamma\gamma$	$E_{t_{j,b,\gamma}} > 20, 20, 25$	294	1033875	1085	952811	5037	763962
$Z(b\bar{b})H(\gamma\gamma)$	$E_{t_{j,b,\gamma}} > 20, 0, 20$	0.109	97168	0.278	82088	0.876	68585
$b\bar{b}H(\gamma\gamma)$	$E_{t_{j,b,\gamma}} > 20, 0, 20$	2.23	120617	9.843	110663	50.49	99611
$t\bar{t}H(\gamma\gamma)$	$E_{t_{j,b,\gamma}} > 20, 0, 20$	0.68	83491	4.76	71790	37.26	63904


- After cuts:

$$\frac{d(\sigma/\sigma_{SM})}{d(\lambda_3/\lambda_{3,SM})} \sim -0.8$$

Samples	HL-LHC (3 ab^{-1})			TeV33 (3 ab^{-1})			TeV100 (3 ab^{-1})		
	$\sigma \cdot Br$ (fb)	Acc. (%)	Expect Evnts	$\sigma \cdot Br$ (fb)	Acc. (%)	Expect Evnts	$\sigma \cdot Br$ (fb)	Acc. (%)	Expect Evnts
$HH(b\bar{b}\gamma\gamma)$	0.089	6.2	16.6	0.545	5.04	82.4	3.73	3.61	403.9
$b\bar{b}\gamma\gamma$	294	0.0045	40.1	1085	0.0039	126.4	5037	0.00275	415.4
$Z(b\bar{b})h(\gamma\gamma)$	0.109	1.48	4.86	0.278	1.41	11.8	0.875	1.57	41.2
$b\bar{b}h(\gamma\gamma)$	2.23	0.072	4.82	9.84	0.084	24.8	50.5	0.099	150.5
$t\bar{t}h(\gamma\gamma)$	0.676	0.178	3.62	4.76	0.12	16.5	37.3	0.11	124.2
Total B	-	-	53.4	-	-	179.5	-	-	731.3
S/\sqrt{B}	-	-	2.3	-	-	6.2	-	-	15.0

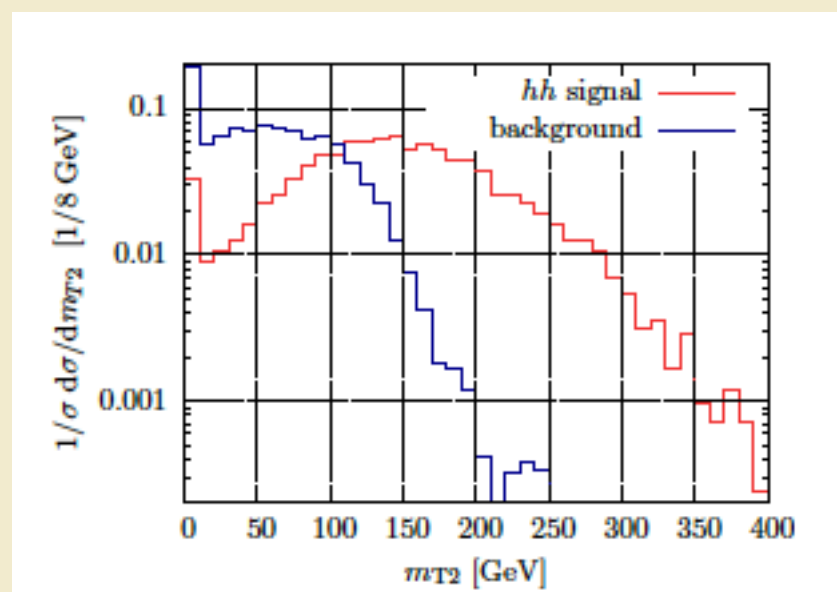
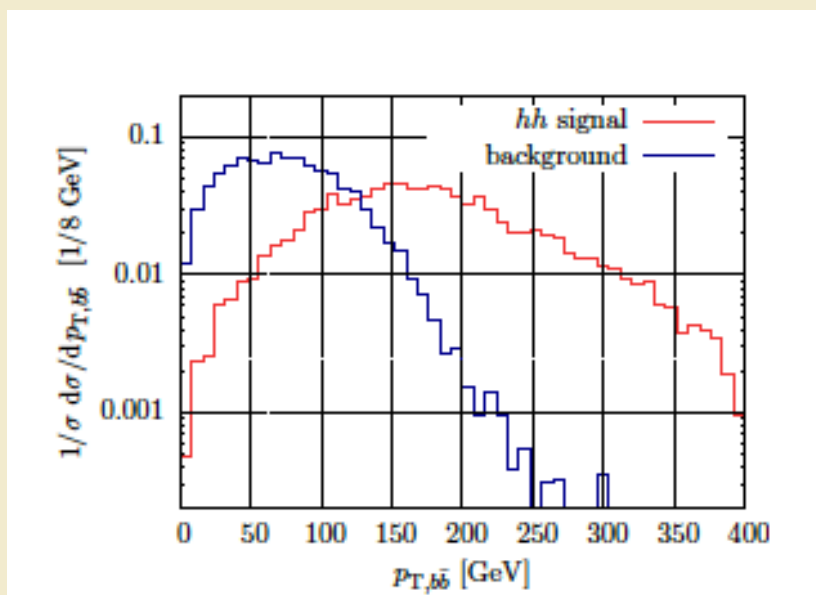
- Statistical accuracy on λ_3 : 50% (8%) at 14 (100) TeV with 3000 fb^{-1}

14 TeV: $HH \rightarrow b\bar{b}W^+W^-$

- Small signal: $W \rightarrow l\nu$, $W \rightarrow \text{Jets}$
 - No cuts: $\sigma \sim 30$ fb
 - 1 isolated lepton: $\rightarrow 4$ fb
 - MET+Jet cuts: $\rightarrow .9$ fb
 - Hadronic W reconstruction: $\rightarrow .3$ fb
 - Kinematic Higgs reconstruction: $\rightarrow .017$ fb
- Huge background from $bbWW$: $S/\sqrt{B} \sim .001$
 -  This channel not seriously considered

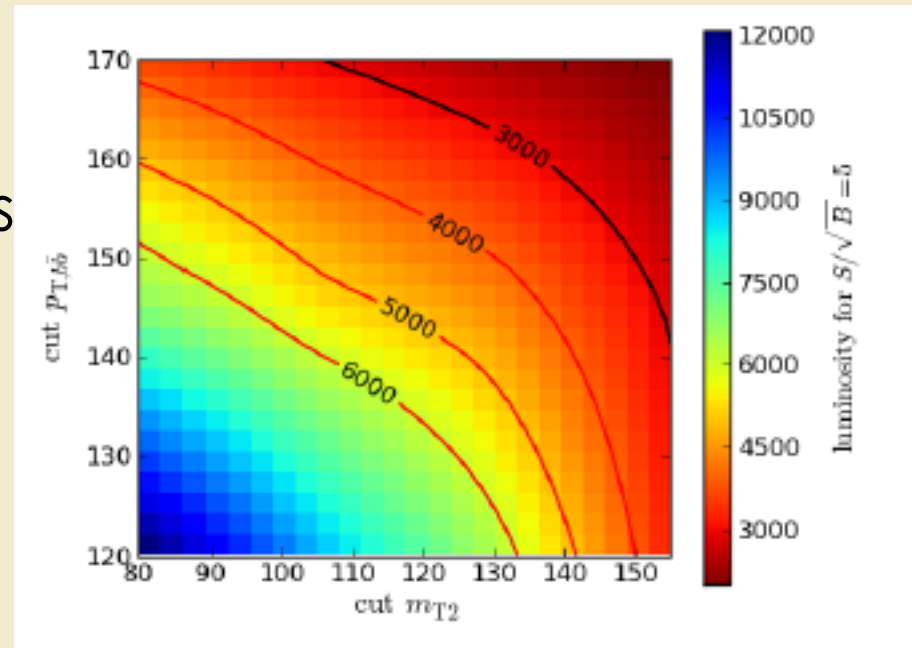
14 TeV: HH \rightarrow bb $\tau\tau$

- Signal: $hh \rightarrow b\bar{b}\tau^+\tau^- + X$
- Largest background: $t\bar{t} \rightarrow (bW^+)(\bar{b}W^-) + X$
 $\rightarrow (b\tau^+\nu)(\bar{b}\tau^-\bar{\nu}) + X$



14 TeV: $HH \rightarrow bb\tau\tau$

- Luminosity for 5σ measurement of λ_3 with p_{Tbb} and m_{T2} cuts



Comparisons

	HL-LHC	HE-LHC	VLHC
\sqrt{s} (TeV)	14	33	100
$\int \mathcal{L} dt$ (fb ⁻¹)	3000	3000	3000
$\sigma \cdot \text{BR}(pp \rightarrow HH \rightarrow bb\gamma\gamma)$ (fb)	0.089	0.545	3.73
S/\sqrt{B}	2.3	6.2	15.0
λ (stat)	50%	20%	8%

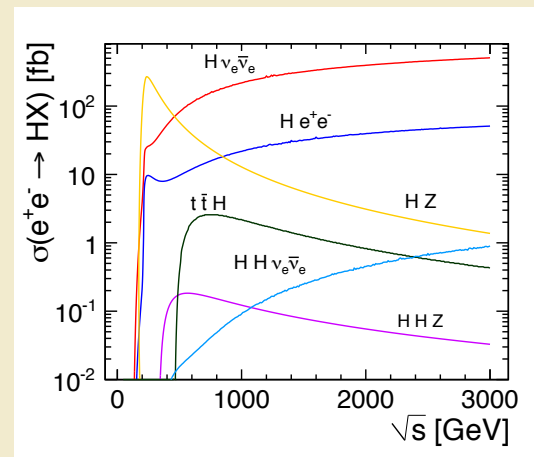
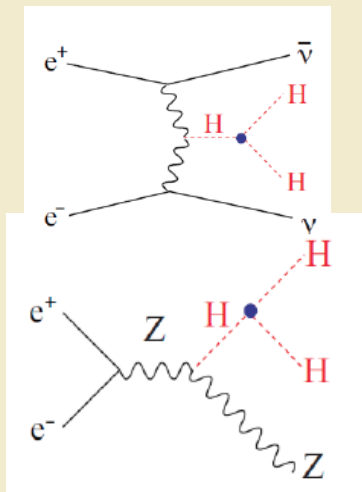
	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC1400	CLIC3000
\sqrt{s} (GeV)	500	500	500/1000	500/1000	1400	3000
$\int \mathcal{L} dt$ (fb ⁻¹)	500	1600 [‡]	500+1000	1600+2500 [‡]	1500	+2000
$P(e^-, e^+)$	(-0.8, 0.3)	(-0.8, 0.3)	(-0.8, 0.3/0.2)	(-0.8, 0.3/0.2)	(0, 0)/(-0.8, 0)	(0, 0)/(-0.8, 0)
$\sigma(ZHH)$	42.7%		42.7%	23.7%	-	-
$\sigma(\nu\bar{\nu}HH)$	-	-	26.3%	16.7%		
λ	83%	46%	21%	13%	28/21%	16/10%

- 5 σ deviation requires 4% measurement
- Exclusion of 20% deviation at 95% CL requires 10% measurement

Conclusions

- Measuring HH production required to understand Higgs potential
- Hard to make HH rate much different from SM rate because of constraints from single Higgs production and electroweak measurements
- Small rates....serious study of experimental possibilities just beginning

e^+e^- machines have low rates for HH



	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC1400	CLIC3000
\sqrt{s} (GeV)	500	500	500/1000	500/1000	1400	3000
$\int \mathcal{L} dt$ (fb $^{-1}$)	500	1600 ‡	500+1000	1600+2500 ‡	1500	+2000
$P(e^-, e^+)$	(-0.8, 0.3)	(-0.8, 0.3)	(-0.8, 0.3/0.2)	(-0.8, 0.3/0.2)	(0, 0)/(-0.8, 0)	(0, 0)/(-0.8, 0)
$\sigma(ZHH)$	42.7%		42.7%	23.7%	-	-
$\sigma(\nu\bar{\nu}HH)$	-	-	26.3%	16.7%		
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