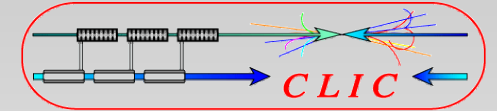


# From natural mutation to DC breakdown

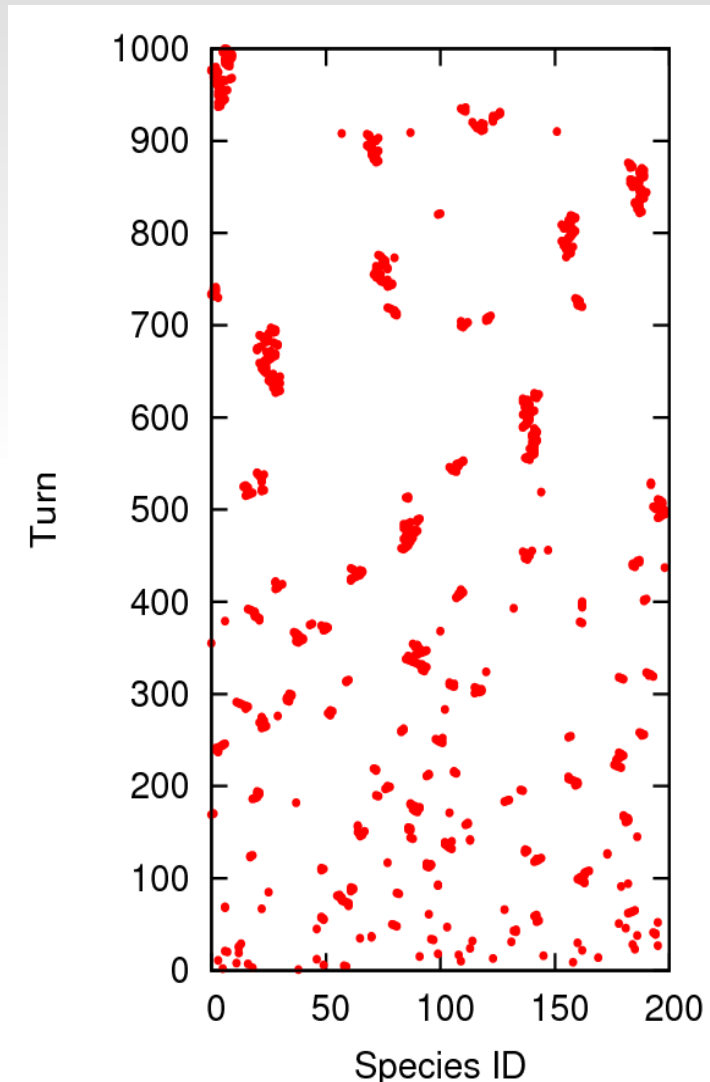
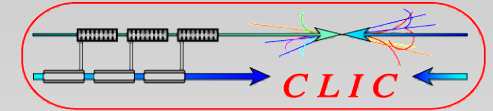
Yngve Inntjore Levinsen

# Motivation



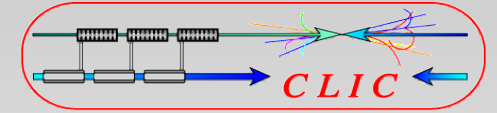
- Understand statistics in DC Spark
- Develop a better understanding of breakdowns (long term, compared to most models which concentrates on one breakdown)
- Test hypotheses of how breakdowns modifies the surface over time

# Background

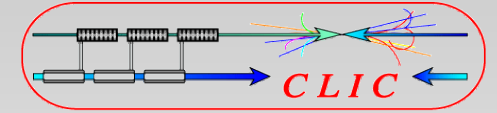


- Bak and Sneppen (1993): "Mutation avalanches" can occur from **undirected** random behaviour
- Each species have a random number, a weakness parameter
- Weakest species mutate, along with its closest neighbours
- Mutation is simply selecting a new random number (**no preferences**)
- After a few turns, local bunches are observed
- No assumptions about what the parameter is, other than it is a "weakness parameter"

# The link



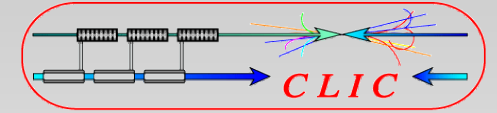
- Breakdowns are (assumed by some) triggered by a weakness parameter ( $\beta$ , but could be more complex)
- Breakdowns often occur in bunches
- ”Turn based”
- Neighbourhood of a breakdown origin is also affected



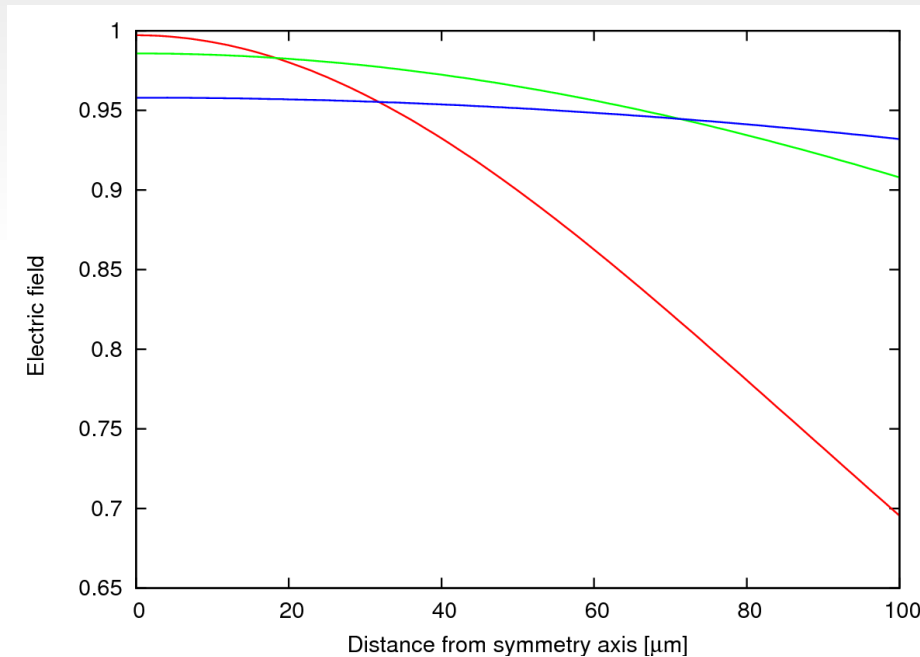
# The basic model

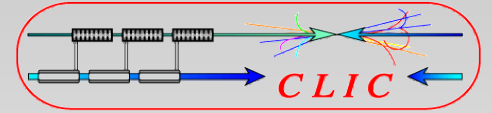
- Cathode surface have n number of weak points (protrusions)
- Positions are initially chosen randomly, but kept fixed for simplicity
- Each weak point have a weakness parameter ( $\beta$ )
- Actual DC tip-plane field distribution is used, with typical gap distances (usually 20  $\mu\text{m}$  unless otherwise specified)

# The basic model



- Actual cathode field distribution used
- Graph shows electric field distribution on cathode normalized in units of parallel plate field ( $V/d$ )
- 20  $\mu\text{m}$  (red), 50  $\mu\text{m}$  (green), 100  $\mu\text{m}$  (blue) gap distances

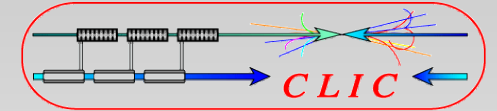




# The basic model

- If a limit  $\beta E$  is reached, a breakdown occurs
- If no breakdown occurs, field emission is assumed capable of slight modification of the protrusion sites
- After a breakdown, a new weakness parameter is chosen for the location, according to a given distribution (i.e. no history of breakdown energy)
- Neighbouring locations redistributed in same way

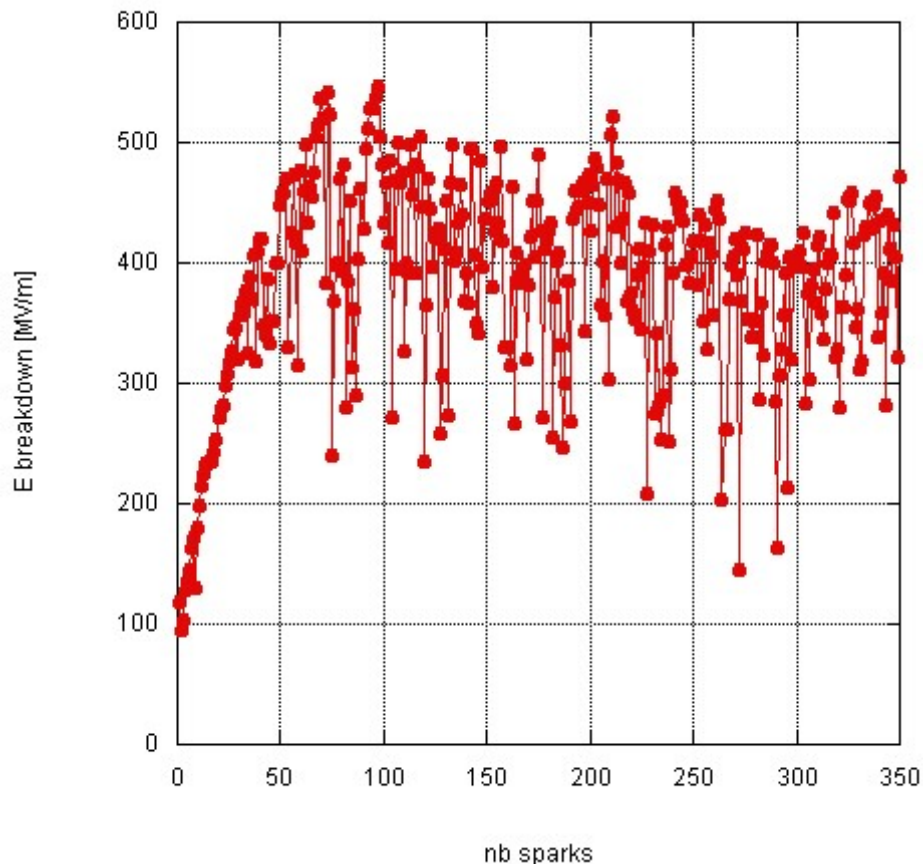
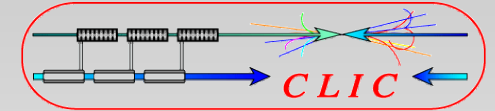
# DC breakdown



- Initial conditioning is understood by an initial rougher surface (higher  $\beta$  values)
- Initial  $\beta$  values taken from Gaussian distribution with mean 40, standard deviation of 10
- After breakdown,  $\beta$  values are taken from Gaussian distribution with mean 30, standard deviation of 2
- Field emission  $\Rightarrow$  Markov chain (Gaussian distribution with mean equal to previous value, standard deviation small and **proportional to local field**)



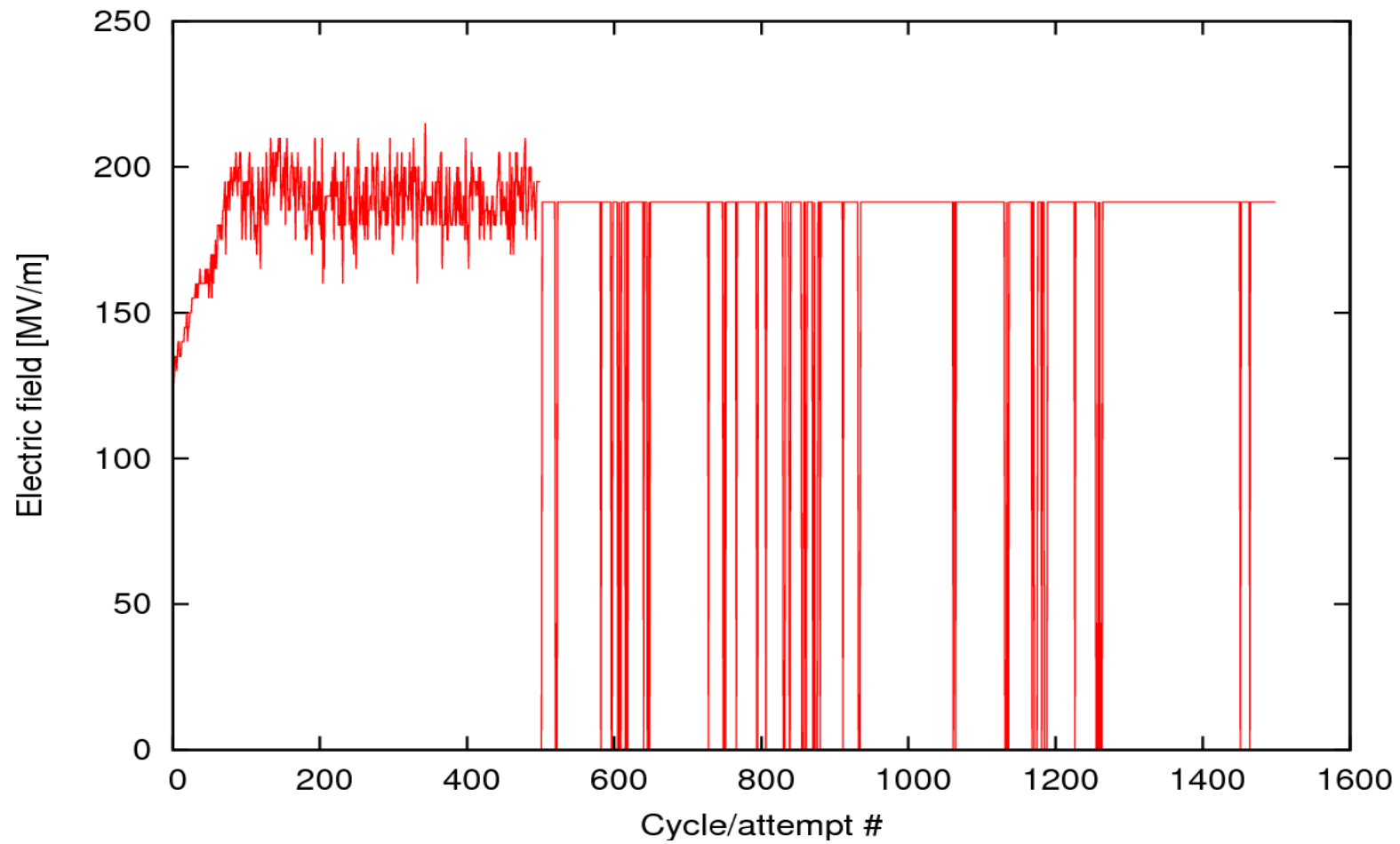
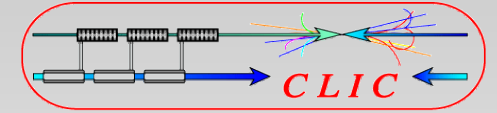
# DC breakdown



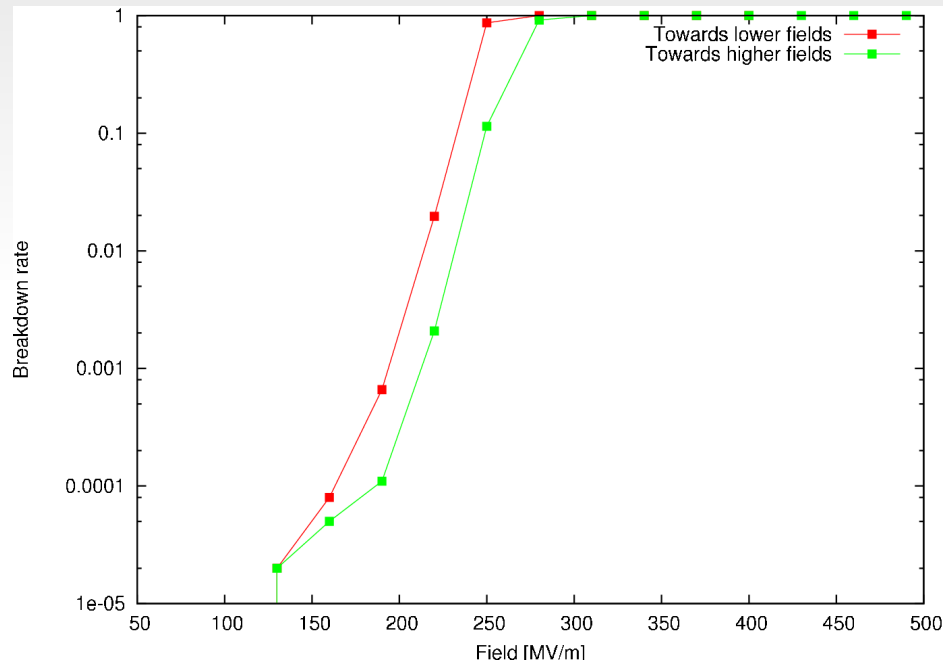
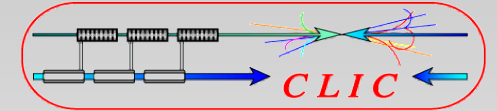
Courtesy A. Descoeudres

- Rapid conditioning, followed by fluctuation around a mean breakdown field, denoted saturated breakdown field
- Some materials show conditioning (e.g. Mo), some do not (e.g. Cu)
- Breakdown rate at saturated breakdown field found to be a few percent

# DC breakdown

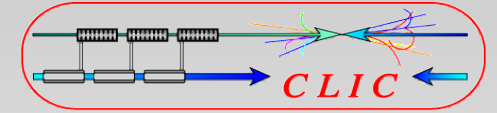


# DC breakdown



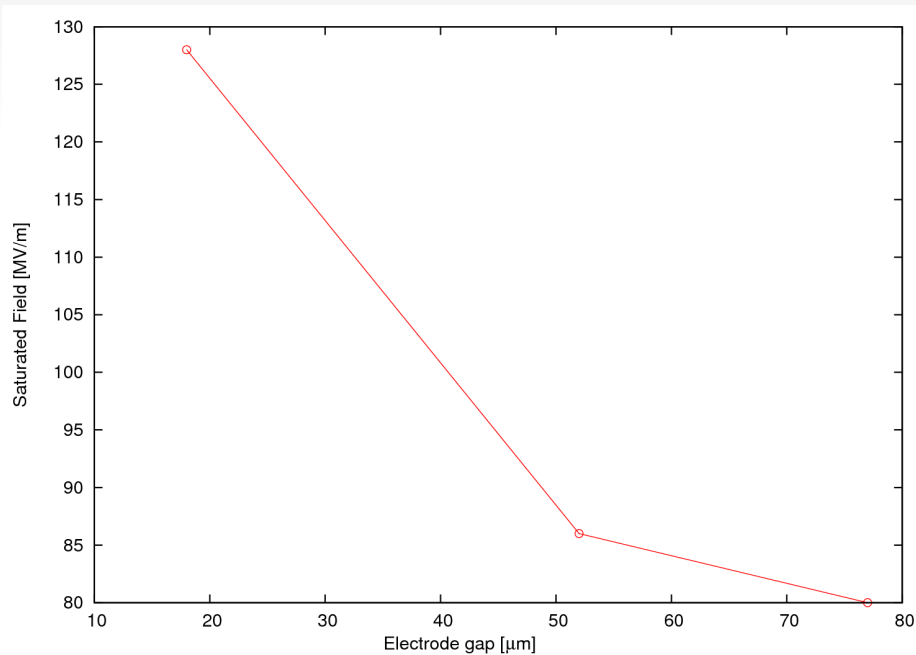
- 100k attempts at each field value
- First decreasing field until 0 breakdown rate, then increasing again
- Similar "directional dependence" found in experiments

# DC breakdown

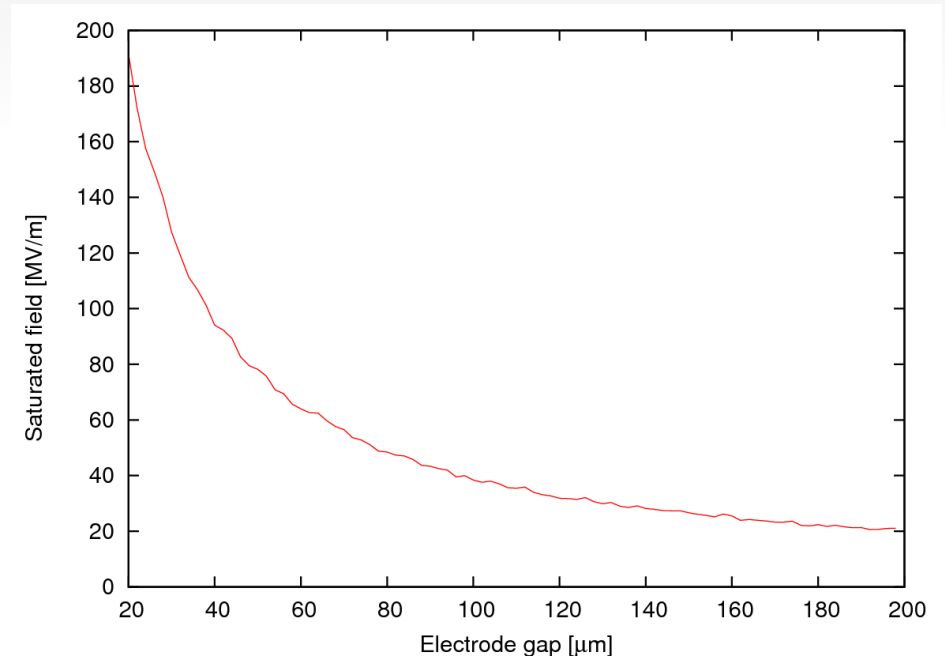


Electrode gap distance dependence for saturated breakdown field

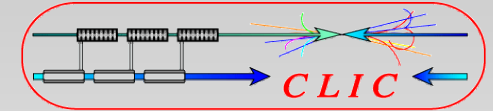
Experiment



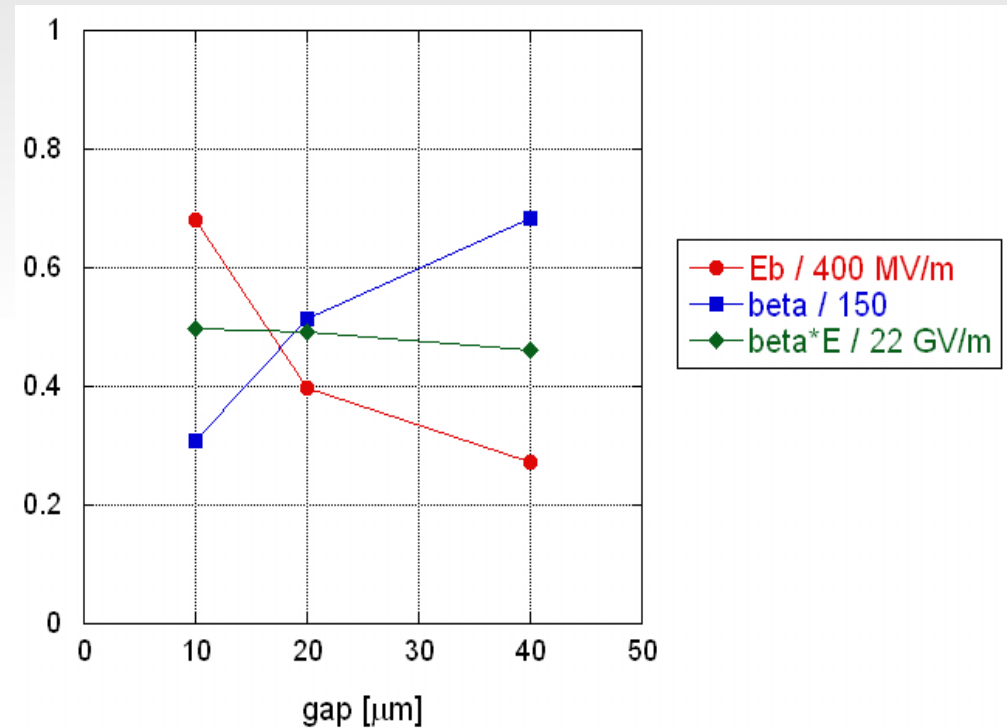
Model



# DC breakdown

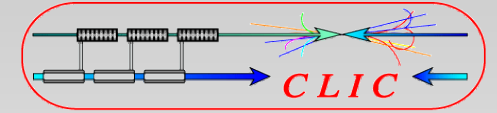


- Gap distance dependence on molybdenum electrodes (A. Descoeudres)
- Local breakdown field is independent on gap distance, macroscopic breakdown field is not!
- But macroscopic breakdown field is what we are actually interested in...

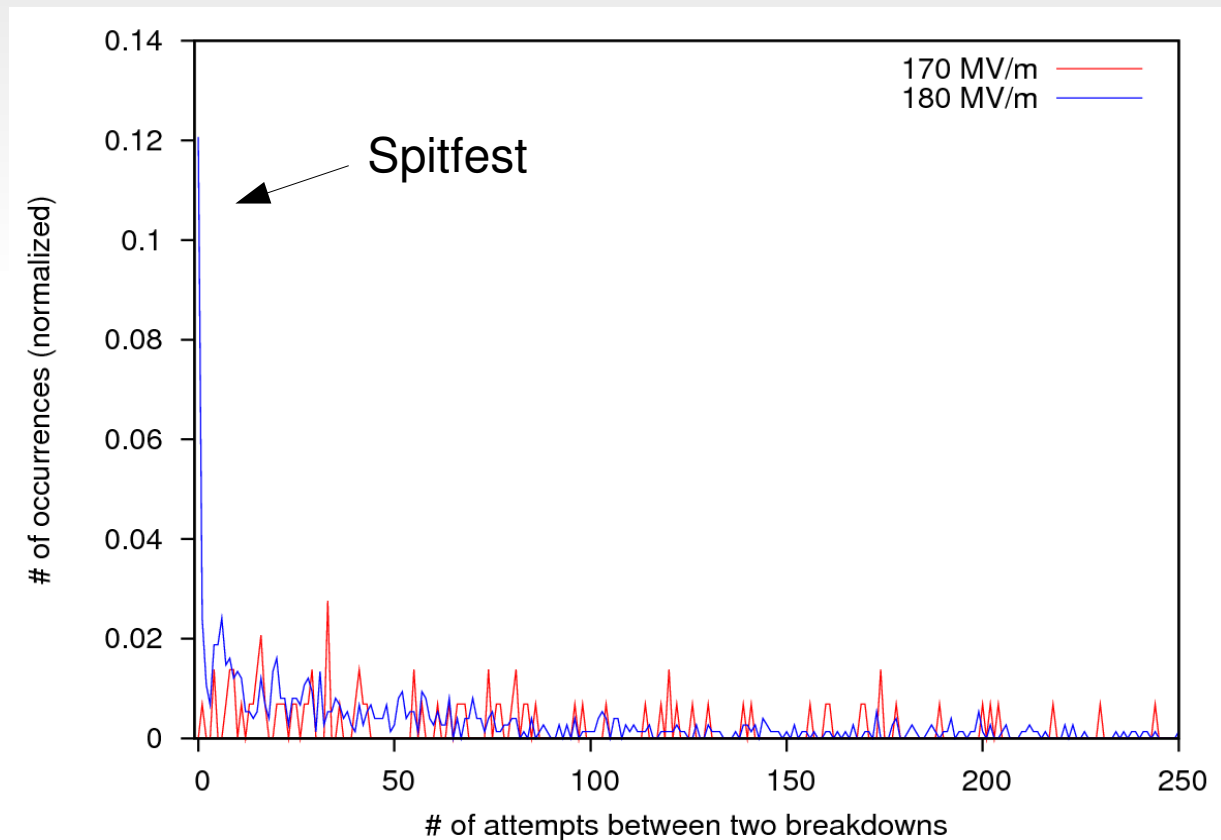


Courtesy A. Descoeudres

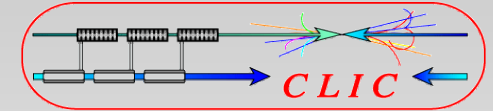
# Spitfest



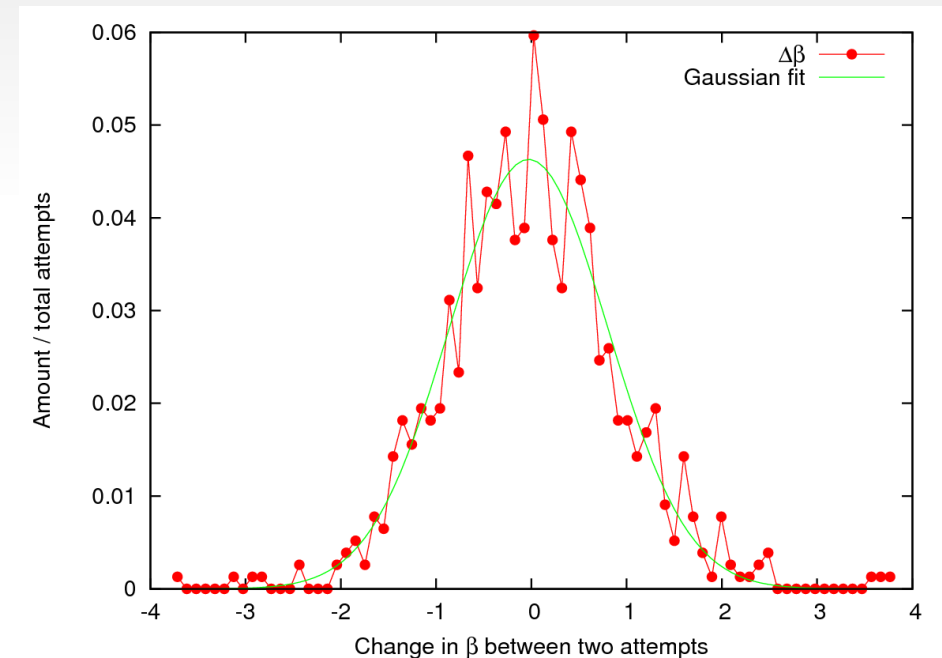
- Spitfest / bunching of breakdowns
- Only visible for higher breakdown rates
- A rather abrupt transition in the simulation



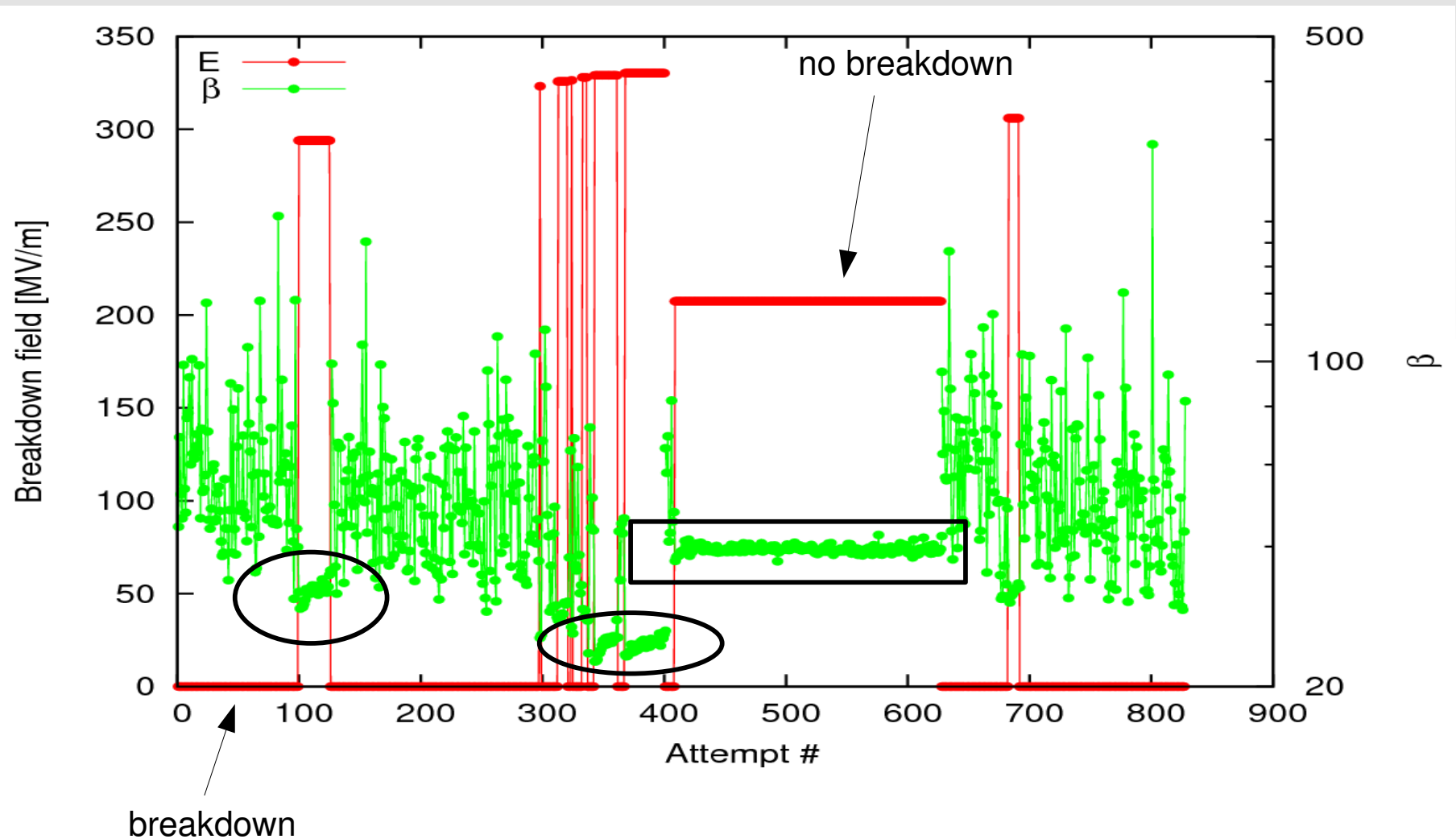
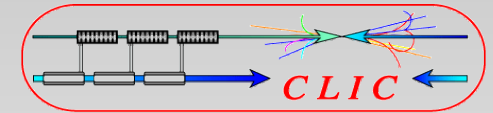
# Field emission modification



- 1500 attempts without breakdown
- $E = 225 \text{ MV/m}$
- Measured  $\beta$  between each attempt
- Assuming  $\sigma_{total} = \sqrt{\sum \sigma^2}$
- Found that  $\beta$  change according to Gaussian distribution with mean  $\sim 0$ , st.dev.  $\sim 0.8$
- Found in simulation that st.dev.  $\sim 0.3$  **looked** reasonable for this field value

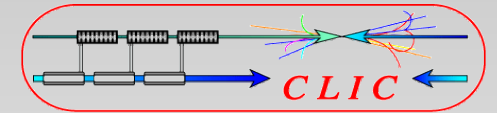


# Field emission modification

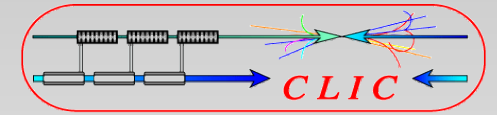




# Some observations

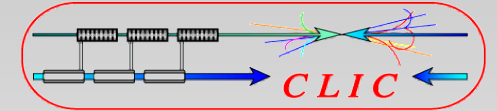


- The randomness we observe in experiments does not exclude a fixed limit for breakdown initiation
- The bunchedness (spitfest) in breakdown rate experiments can be understood from simple statistics
- It is not necessarily straight forward to compare results from DC Spark to RF results
- Saturated breakdown field is dependent on geometry / "probed area"



# Backup slides

# Field emission



- Without any surface modification, this model can also easily calculate field emission if the weakness parameter is assumed to be  $\beta$  (correct tip-plane cathode field distribution is used)
- Gives a gap distance dependence on the measured  $\beta$
- Plot of  $\ln\left(\frac{I}{E^2}\right)$  vs.  $\frac{1}{E}$  gives  $\beta$  from the slope of the curve (straight line for Fowler–Nordheim field emission)

# Field emission

