

Crab cavity development for CLIC

Contributors

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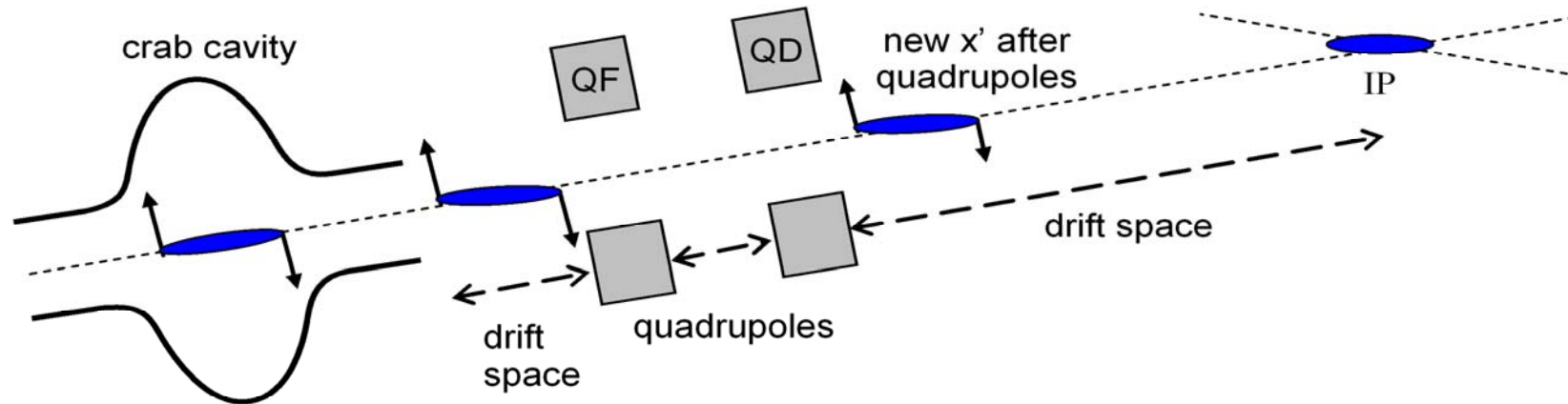
Other Collaborators

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Manchester University	Roger Jones
SLAC	Sami Tantawi





Crab Cavity Function



The crab cavity is a deflection cavity operated with a 90° phase shift.

A particle at the centre of the bunch gets no transverse momentum kick and hence no deflection at the IP.

A particle at the front gets a transverse momentum that is equal and opposite to a particle at the back.

The quadrupoles change the rate of rotation of the bunch.





Crab Cavity Issues

- Wakefields - cause kicks and emittance growth
- Poor Phase Stability - gives large horizontal kicks

Key Required Outcomes

1. Damp, measure and confirm the predicted wakes.
2. Establish feasible/achievable level of phase control performance. (Requirement is beyond state of the art)





Cavity Requirement

- If every sixth bucket filled frequency > 2.0 GHz
- Transverse & longitudinal space not a problem
- Short bunch structure suggests copper structure

Planned Approach

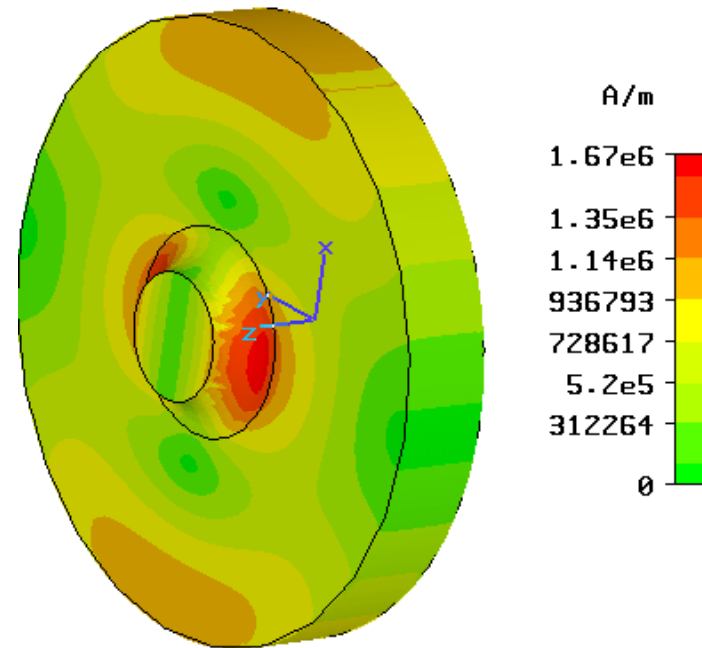
- Design 12 GHz damped detuned TW dipole cavity
- Compute wakefields
- If necessary scale to lower frequency for smaller kicks





Other Issues for a Copper Structure

- RF Source Power requirements
- Pulsed heating on the iris
- Gradient (limited by breakdown?)





Transverse Kick for 3 TeV CM

To minimise required cavity kick R12 needs to be large hence put the cavity close to IP (25 metres suggested)

For 20 mrad crossing and using as 12 GHz structure

$$V_{\max} = \frac{\theta_r E_o c}{R_{12} \omega} = \frac{10^{-2} \times 1.5 \times 10^{12} \times 3 \times 10^8}{25 \times 2\pi \times 12 \times 10^9} = 2.4 \text{ MV}$$

At 20 MV/m transverse gradient this is only 12 cm which is 10-15 cells depending on the cavity design.

This is about 3 MW RF for a SW design probably more for TW.

As vertical kicks caused by unwanted modes in the cavity are dangerous one would like R34 to be small.



Phase synchronisation requirement for no more than 2% luminosity loss

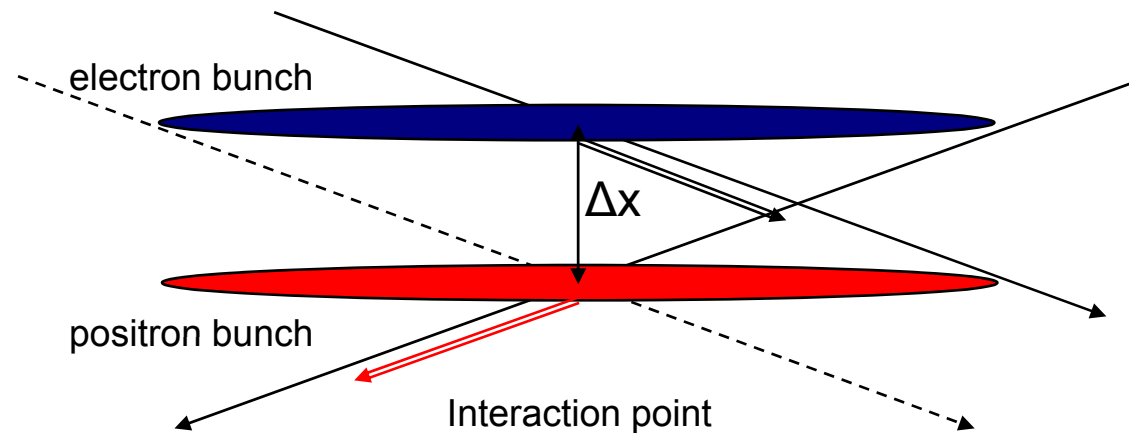
Crabbed crossing angle with phase jitter

Luminosity reduction factor S is given as

$$S = \exp\left(-\frac{\Delta x^2}{4\sigma_x^2}\right)$$

and

$$\Delta x = \frac{c \theta_r \sin(\Delta\phi)}{\omega}$$



	Phase error (degrees)	
Crossing angle	12 GHz	30 GHz
20 mrad	0.02	0.06



Initial assessment

- Without making the wakefield calculation, the crab cavity dimensions can't be finalised
- However, bigger irises can be preferred for possible wakefield suppression.
- For efficient heat transfer, the iris should be of sufficient thickness but not too much to lower the cavity Q .
- Standing wave cavities have much higher shunt impedance and lower surface fields for dipole modes. But if we use the pi mode we have low cavity coupling (nearby modes an issue).
- Travelling wave cavities have a large separation of nearby modes, but will require more power and have higher fields.





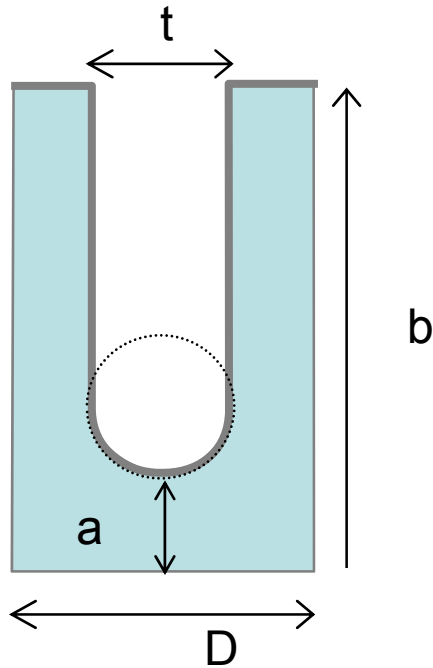
Short study of infinitely periodic coupled dipole cavities

- Electromagnetic simulation tool is CST Microwave studio
- The structure used is a single cell cavity with periodic boundary condition enforced at either ends
- Structures are taken to be copper
- Figures of merit such as the quality factor, R/Q , peak fields and group velocity/ cavity coupling are simulated and compared for various cavity dimensions giving the first dipole frequency at 12 GHz and for various phase advance/cell ($2\pi/3$, $5\pi/6$ and π radians)





The cavity cell structure



- D** Cell length
- t** Iris thickness
- t/2** Iris curvature
- b** Equator radius
- a** Iris radius

Phase advance per cell, ϕ radians	Length of the cell, D mm (11.994 GHz)
$2\pi/3$ (TW)	8.332
$5\pi/6$ (TW)	10.415
π (SW)	12.498

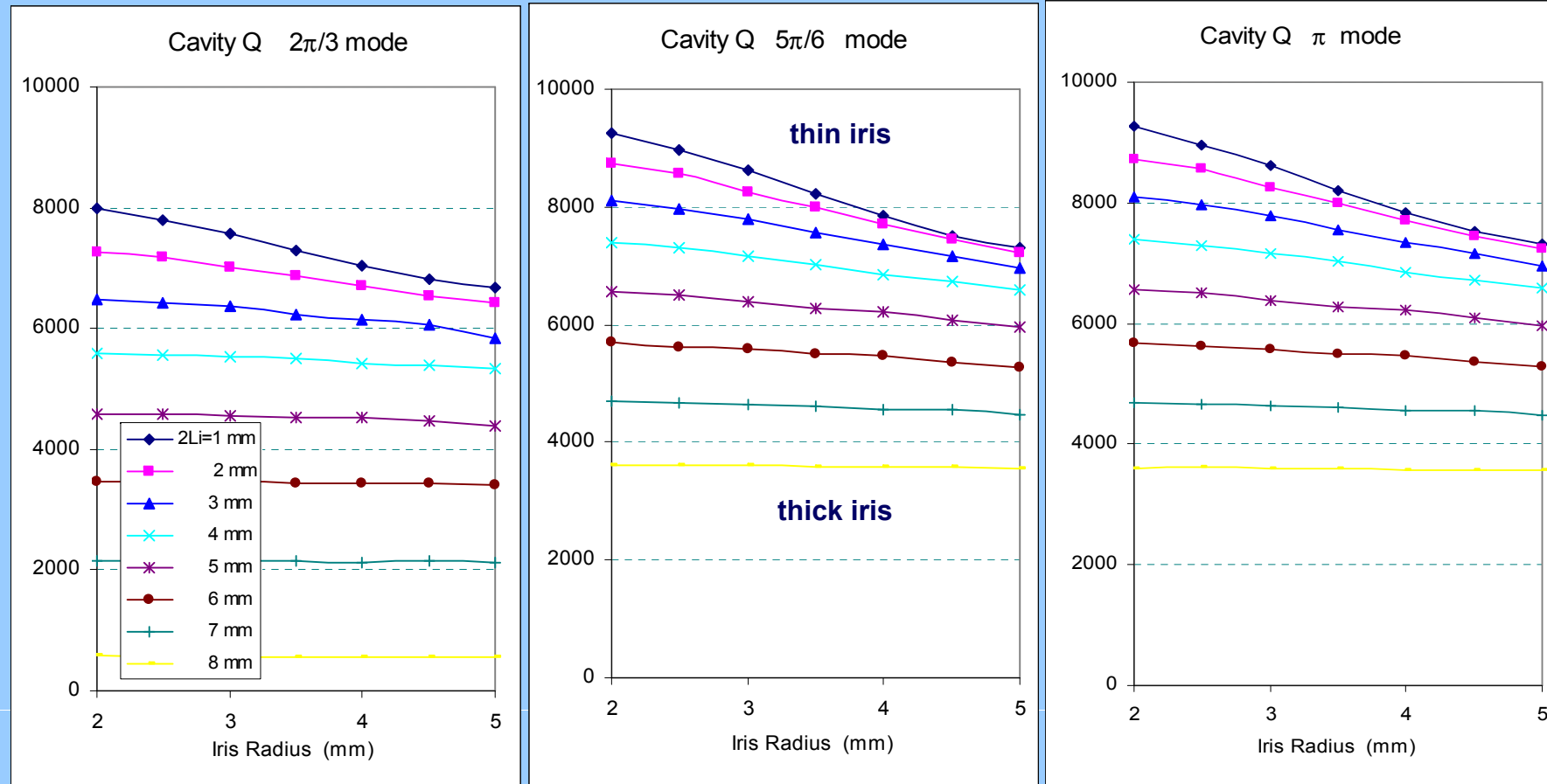
Periodic boundary conditions

Four independent cell parameters –
but one fixed by frequency and one fixed by phase advance
hence investigative plots only vary iris thickness and iris radius





Q vs iris radius and thickness

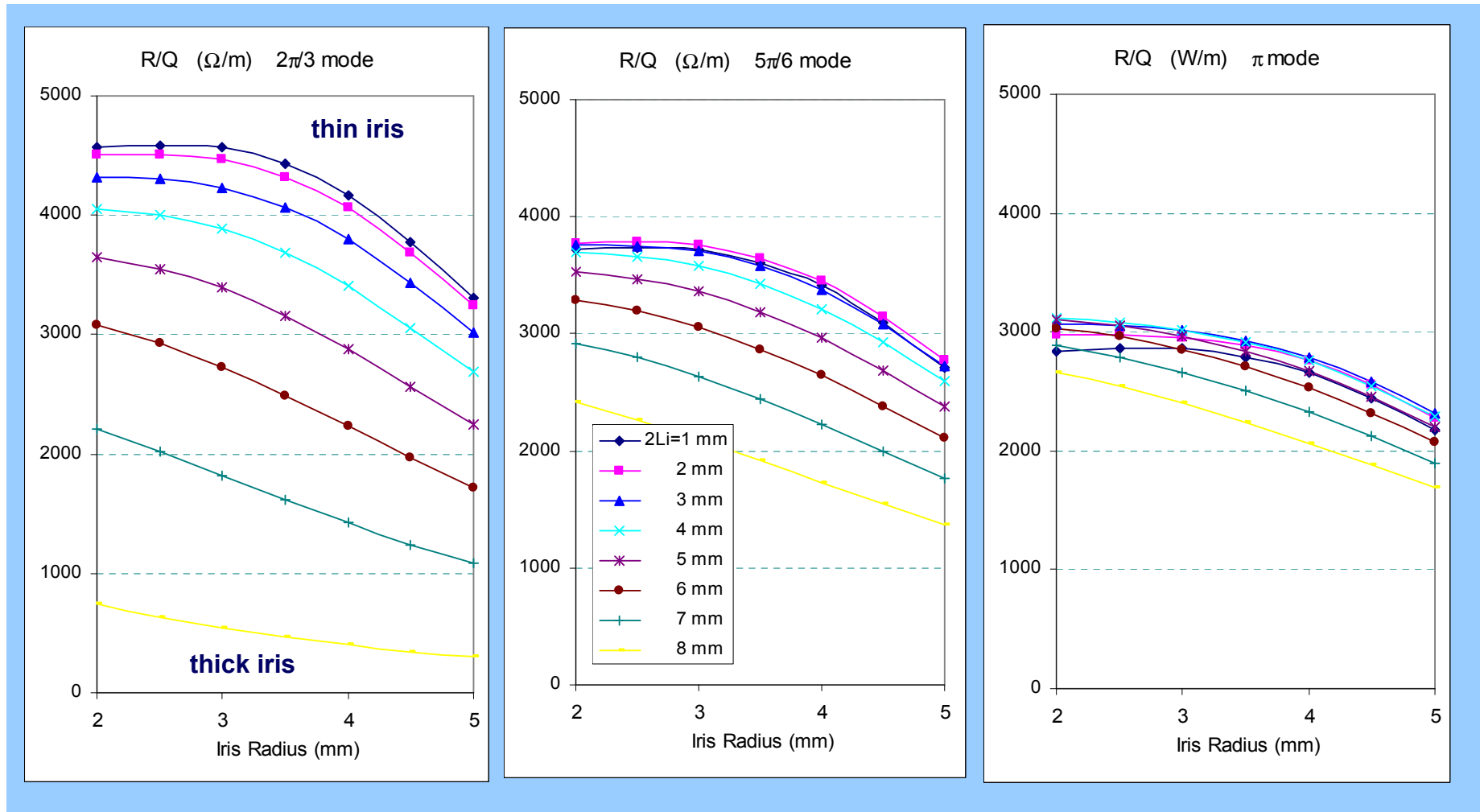


Lines labelled in key correspond to differing iris thicknesses, 2 - 3 mm is preferred
x-axis gives iris radius, 4 mm or above is preferred





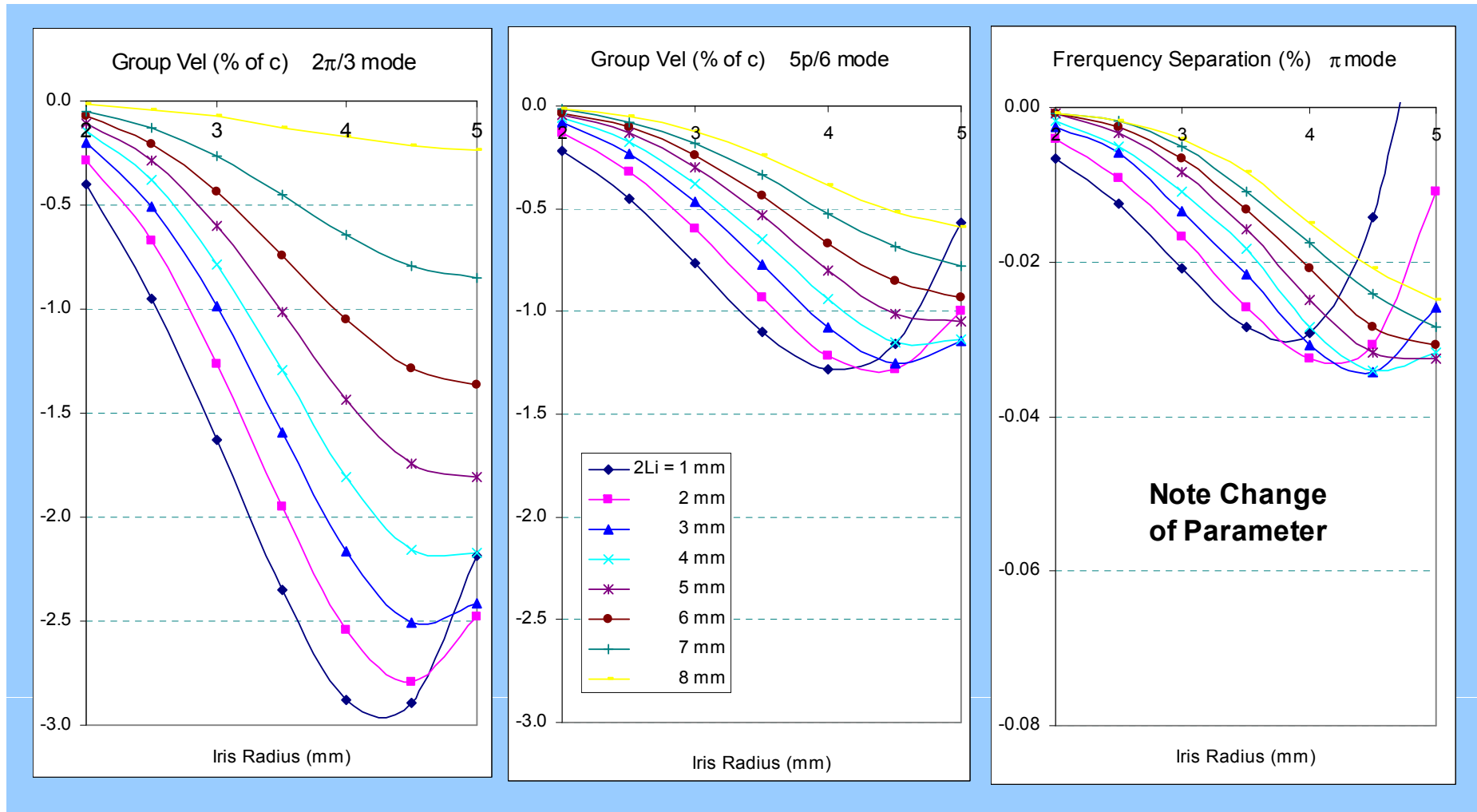
R/Q vs iris radius and thickness



Lines labelled in key correspond to differing iris thicknesses, 2 - 3 mm is preferred
x-axis gives iris radius, 4 mm or above is preferred



Group vel. vs iris radius and thickness

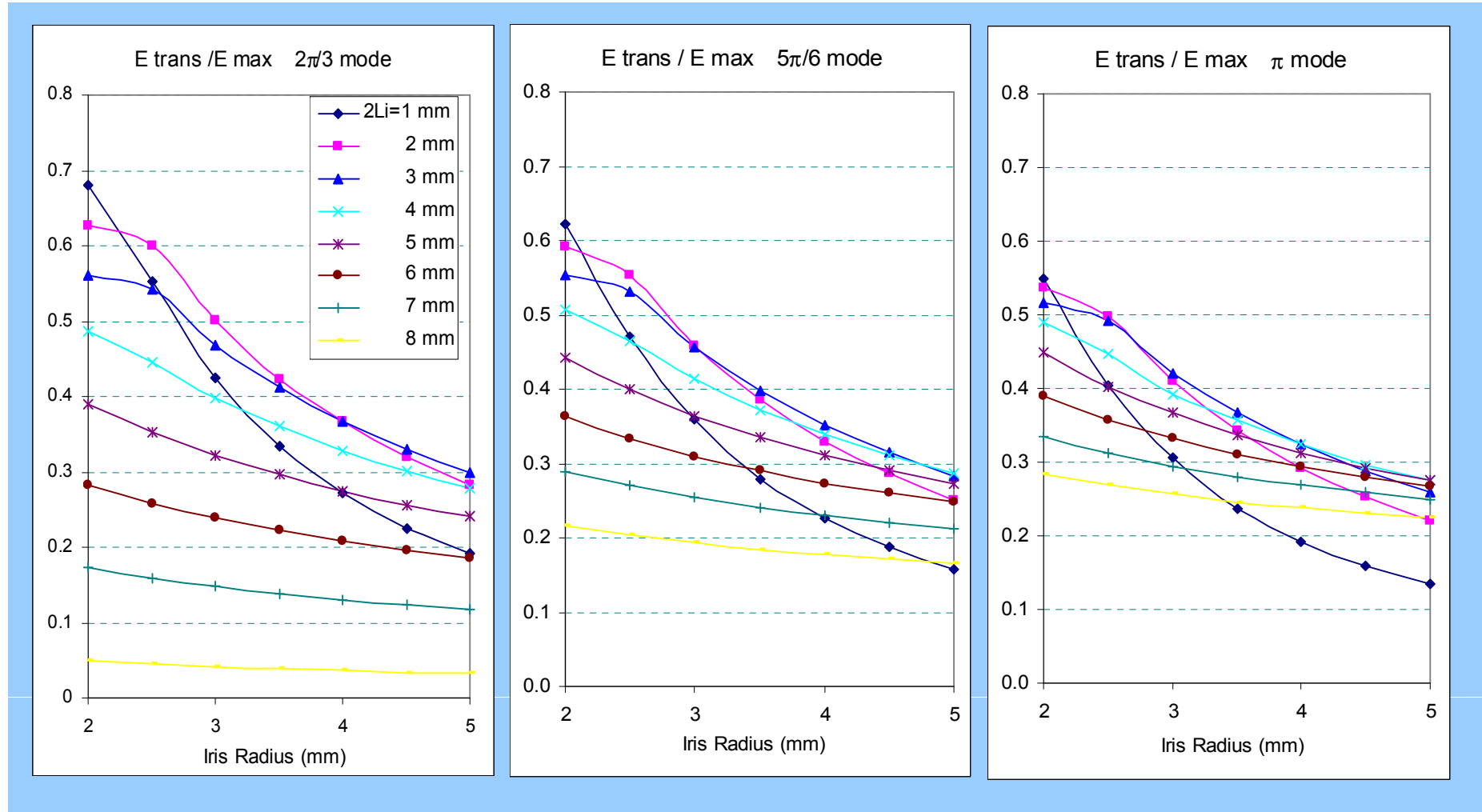


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x-axis gives iris radius, 4 mm or above is preferred





E_{trans}/E_{max} vs iris radius and thickness



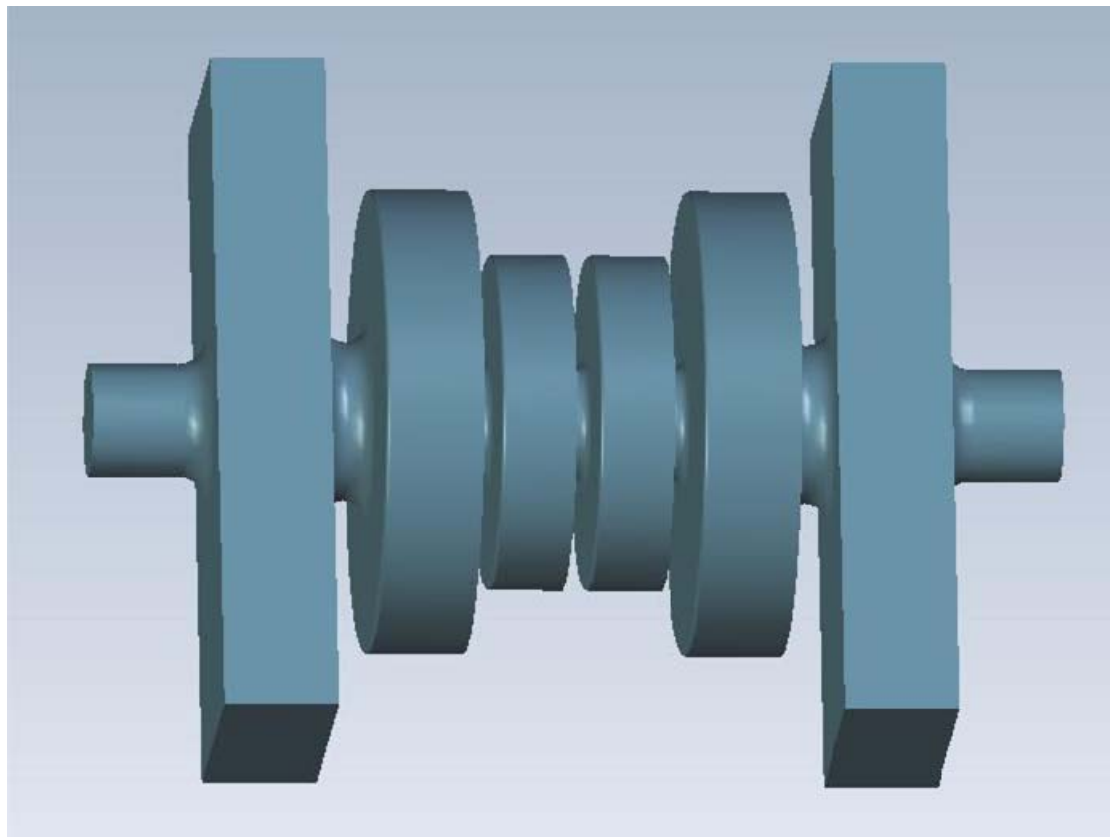
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Design for SLAC Gradient Tests

Rectangular waveguide matched to TE₁₁₁ like mode in first cells which match to TM₁₁₀ like mode in centre cells (only two shown but plan to use three)



frequency	11.424 GHz
phase adv. per cell	120°
mid cell mode	~ TM ₁₁₀
mid cell lengths	8.747 mm
iris mid cell radius	4.00 mm
iris thickness	2.390 mm
mid cell dia.	28.986 mm
end cell mode	~ TE ₁₁₁
end cell dia.	41.180 mm

Picture shows internal volume from MWS simulation

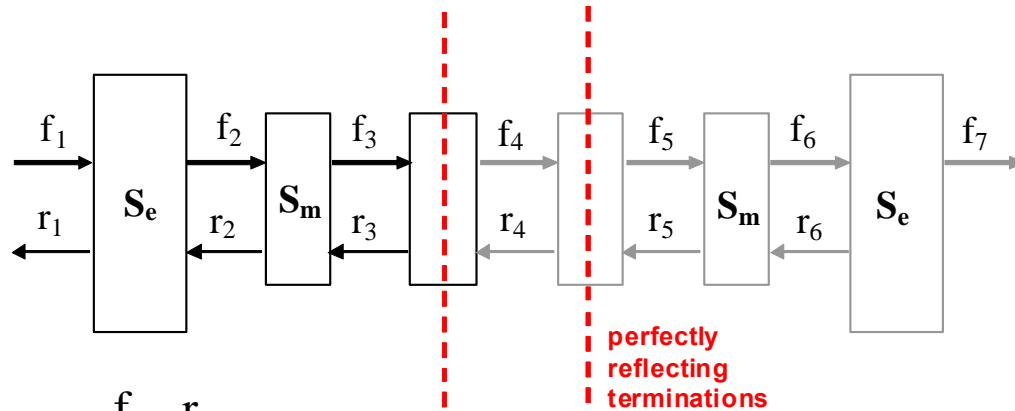




Matching Technique



Use procedure of Alesini D., Gallo A., Spataro B., Marinelli A. & Palumbo L. (Frascati)
Nuclear Instruments and methods in physics research A 580 (2007) 1176-1183



For a matched lossless structure admitting just a forward wave with fixed phase advance ϕ per cell we must have

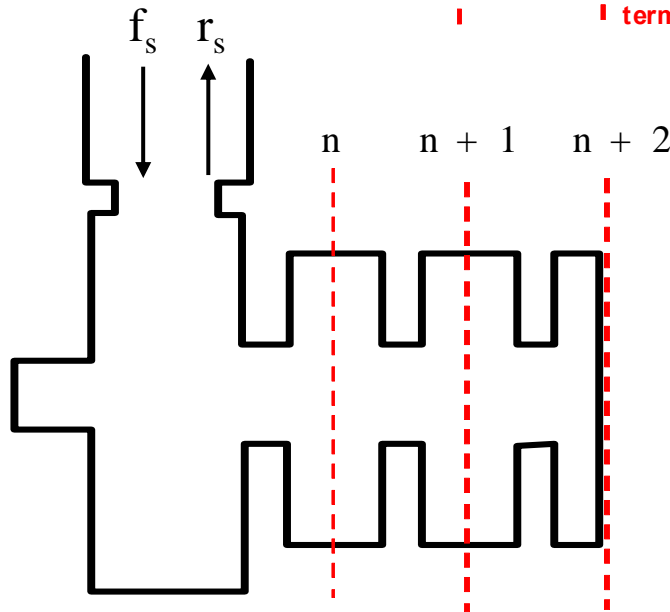
$$r_1 = r_2 = r_3 = r_4 = r_5 = r_6 = 0$$

implies

$$S_e(1,1) = S_e(2,2) = S_m(1,1) = S_m(2,2) = 0$$

$$\frac{r_1}{f_1} = \Gamma_c \quad \frac{r_s}{f_s} = \Gamma_s \quad \phi = \text{phase advance per cell}$$

if
$$\frac{\Gamma_s(n+1)}{\Gamma_s(n)} = \frac{\Gamma_s(n+2)}{\Gamma_s(n+1)} = e^{-j2\phi} \quad \text{then } S_e(1,1) = 0$$



Simulate real lossless structure with cut planes

Hence plot ratio of reflection coefs for structures shorted at n and $n+1$ as function of two matching cell parameters and interpolate to find parameters giving correct phase advance with no attenuation.





Floquet Theorem

- Used Floquet theorem to fine tune the structure.

Christopher Nantista, Sami Tantawi, and Valery Dolgashev, Low-field accelerator structure couplers and design techniques, Phys. Rev. ST Accel. Beams 7, 072001 (2004)

$$\Delta(z) = \frac{E(z + P) - E(z - P)}{E(z)}$$

$$\Sigma(z) = \frac{E(z + P) + E(z - P)}{E(z)}$$

$$R = \frac{2 \sin \psi - i \Delta(z)}{2 \sin \psi + i \Delta(z)}$$

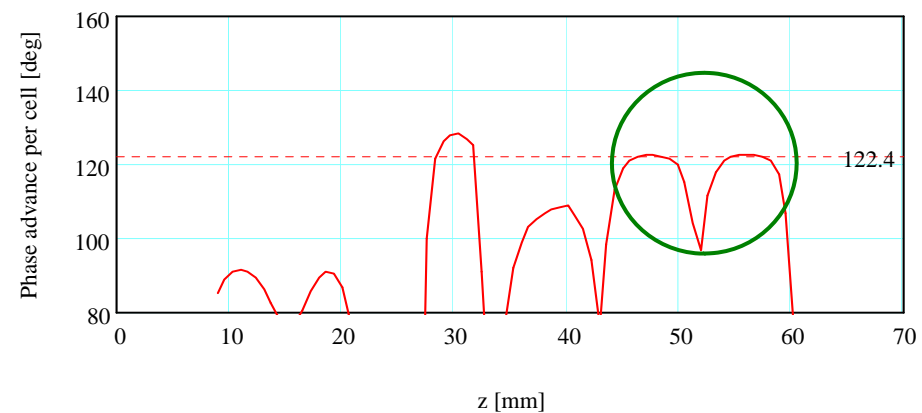
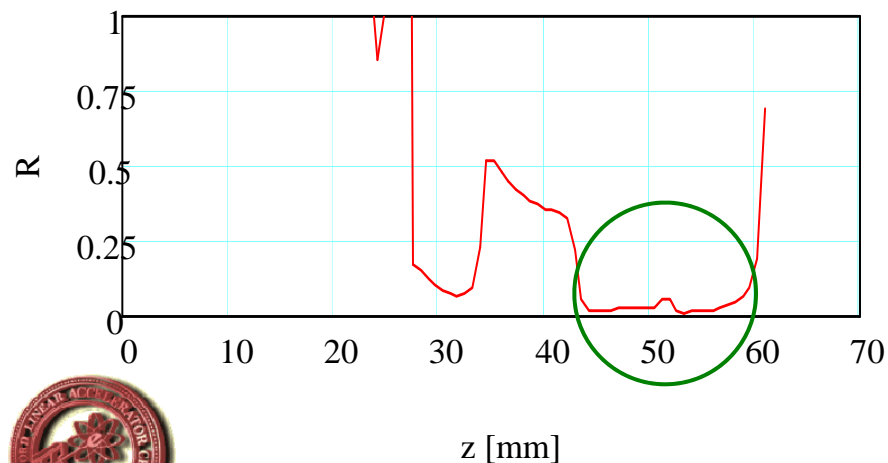
E = field

P = cell length

R = reflection coefficient

ψ = required phase advance

$$\psi = \cos^{-1} \frac{\Sigma(z)}{2}$$

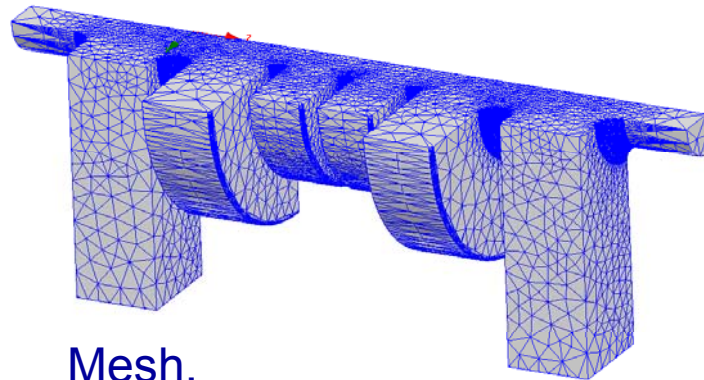




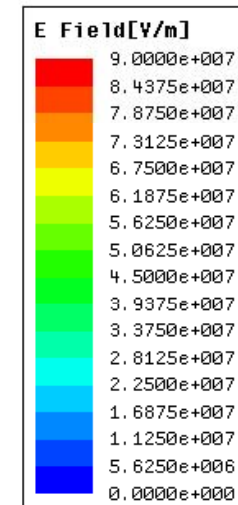
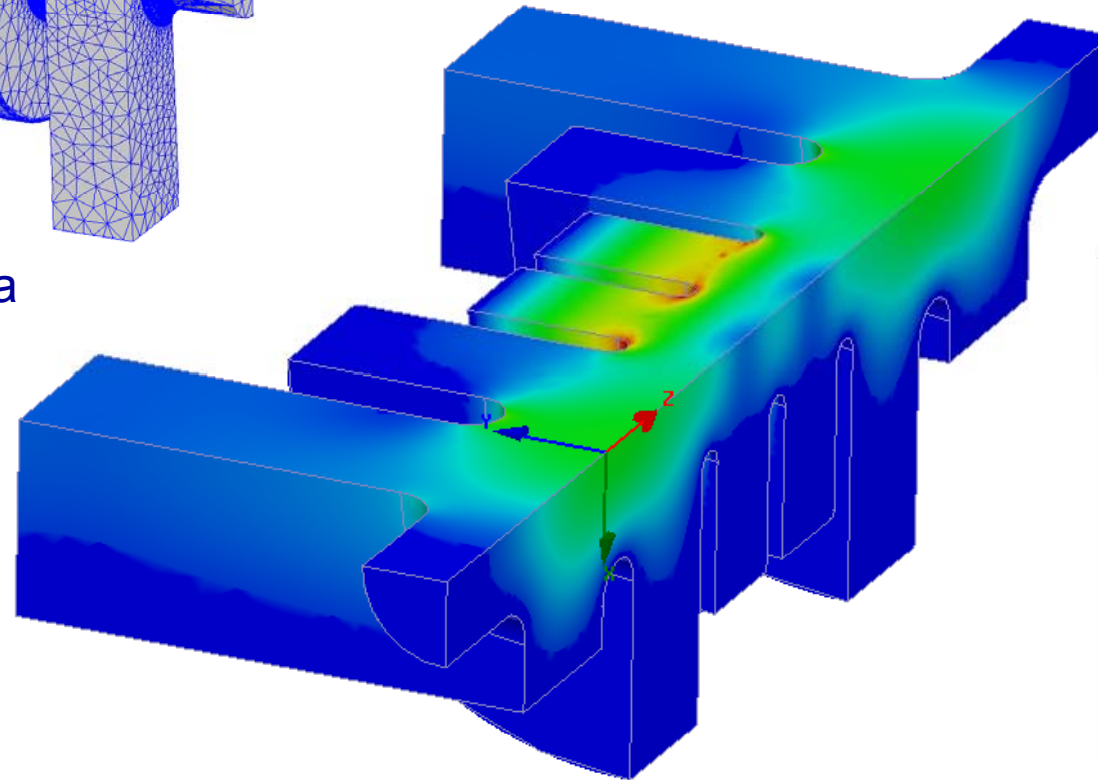
HFSS simulation – Electric Field

11.424 GHz deflection mode,
20 MW transmitted power

Maximum
surface electric field
~90 MV/m



Mesh,
338,882 tetrahedra



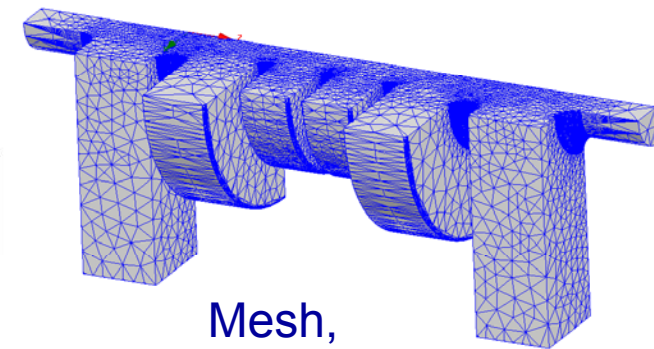
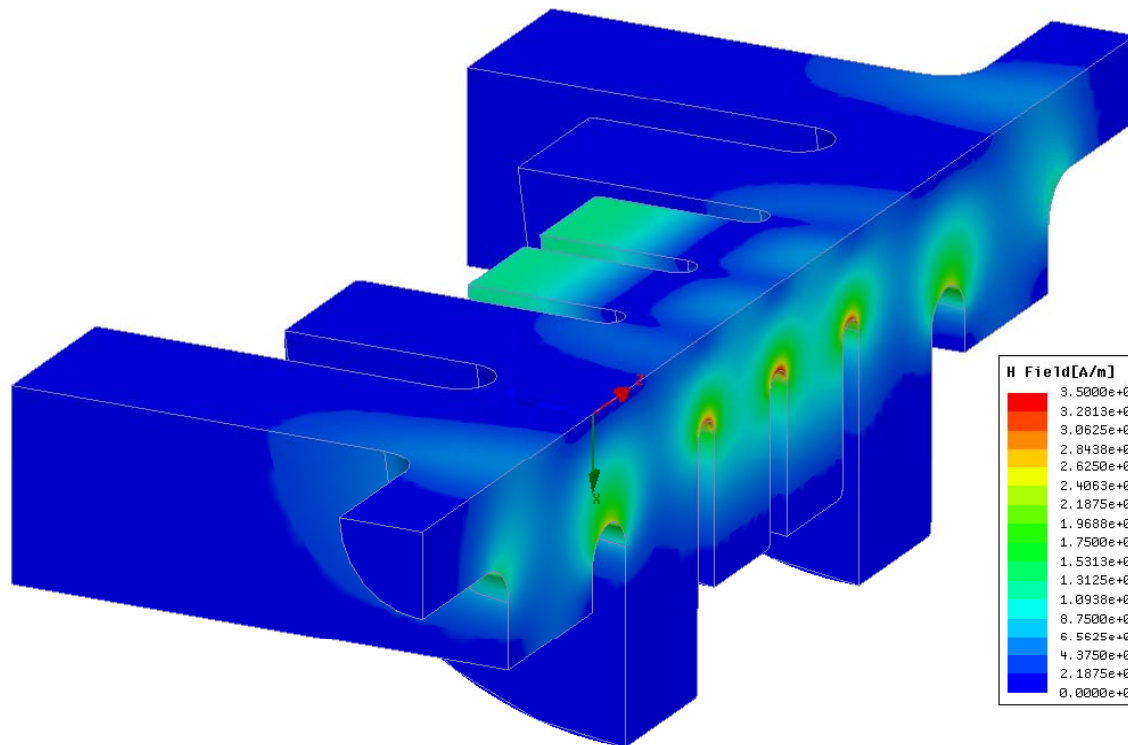


HFSS Simulation Magnetic Field

11.424 GHz deflection mode,
20 MW transmitted power

Maximum surface
magnetic field ~ 350 kA/m

Pulse heating 24 deg. C
for 200 ns pulse

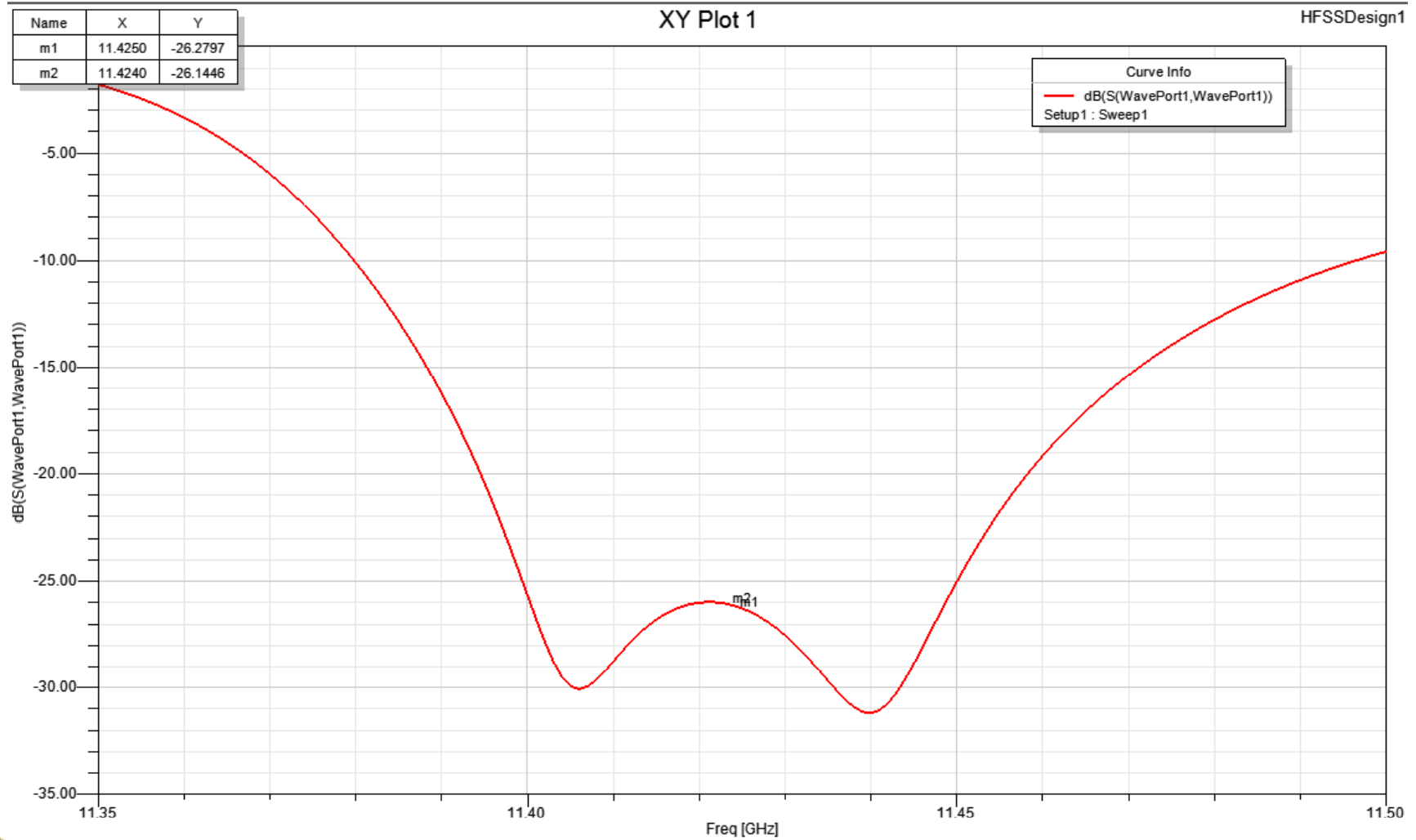


Mesh,
338,882
tetrahedra



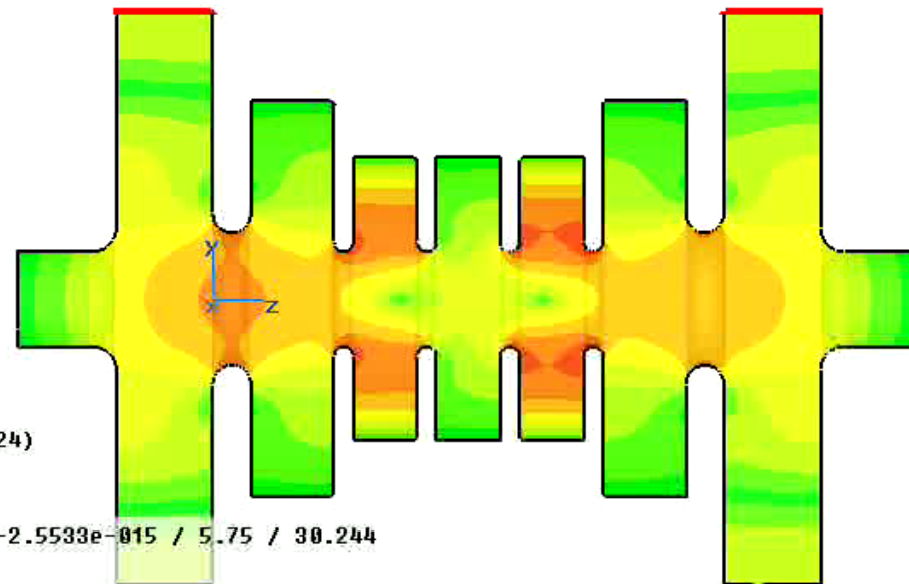


Coupler Matching HFSS prediction

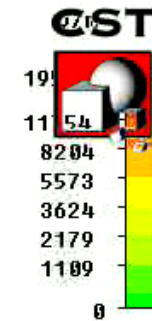




Travelling wave simulation

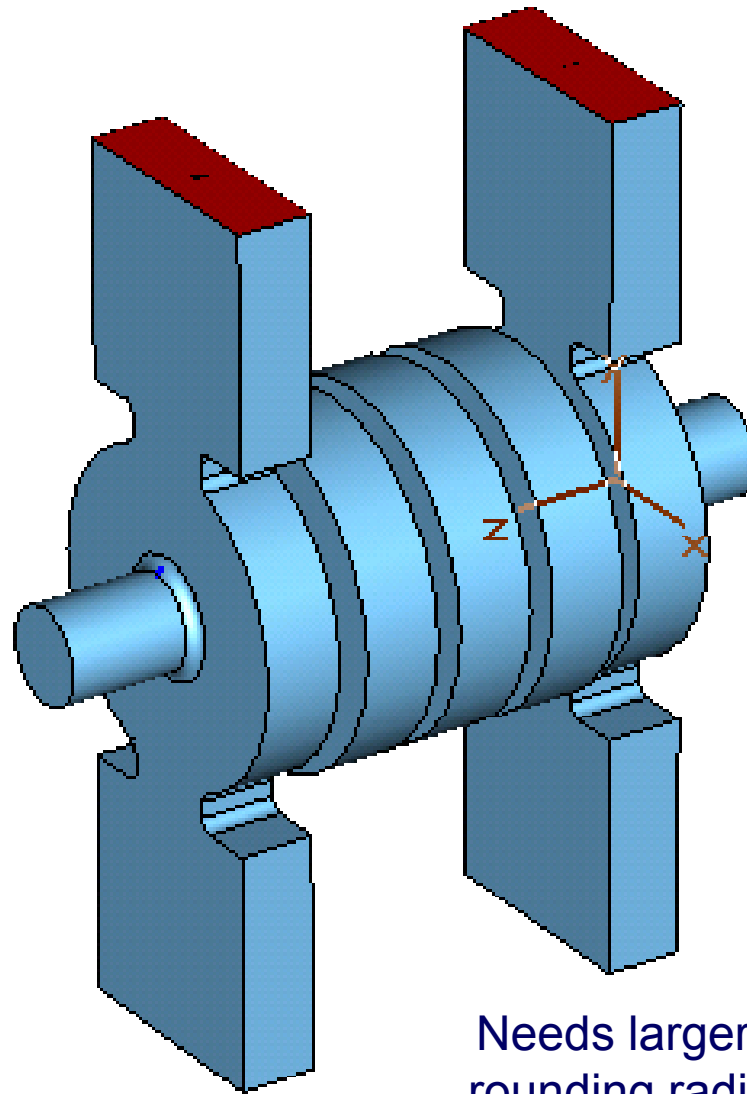


Type	E-Field (peak)
Monitor	e-field (f=11.424)
Component	Abs
Plane at x	0
Maximum-2d	22981.9 V/m at -2.5533e-015 / 5.75 / 30.244
Frequency	11.424
Phase	0 degrees





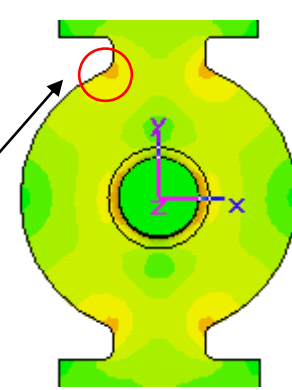
Coupler Design for CTF3 tests



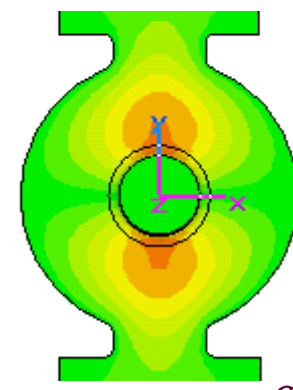
frequency	11.994 GHz
phase adv. per cell	120°
cell length	8.337 mm
Iris radius	4 mm
Iris thickness	2 mm
mid cell radius	14.457 mm
end cell radius	13.673 mm
coupling slot width	9.087mm
coupling slot thickness	2.275 mm

Needs larger rounding radii

H end cell

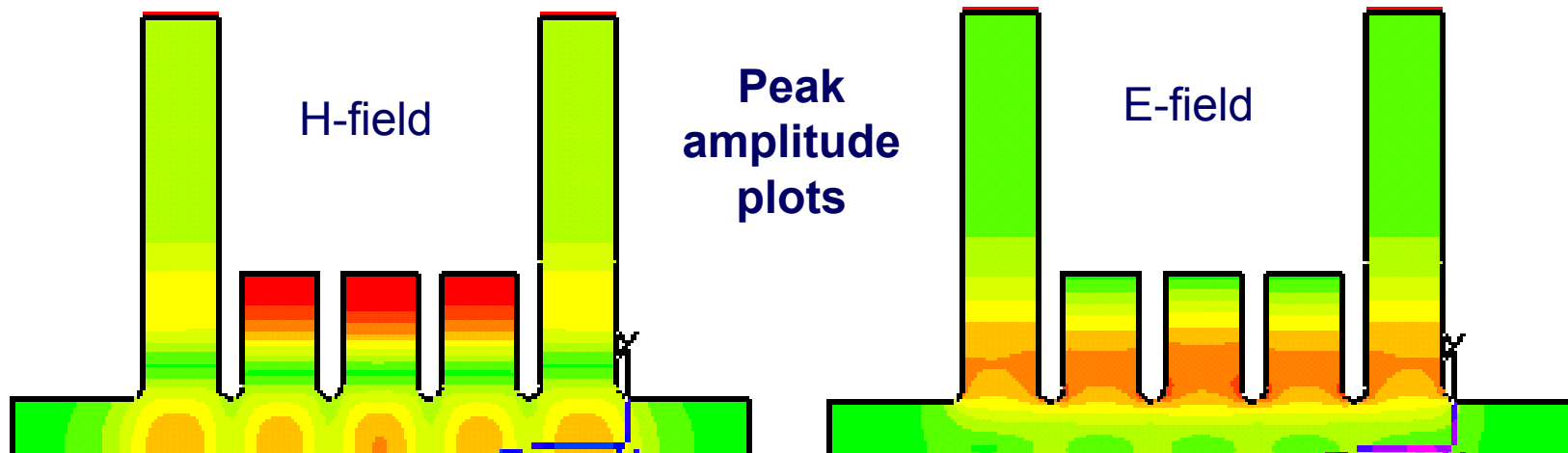
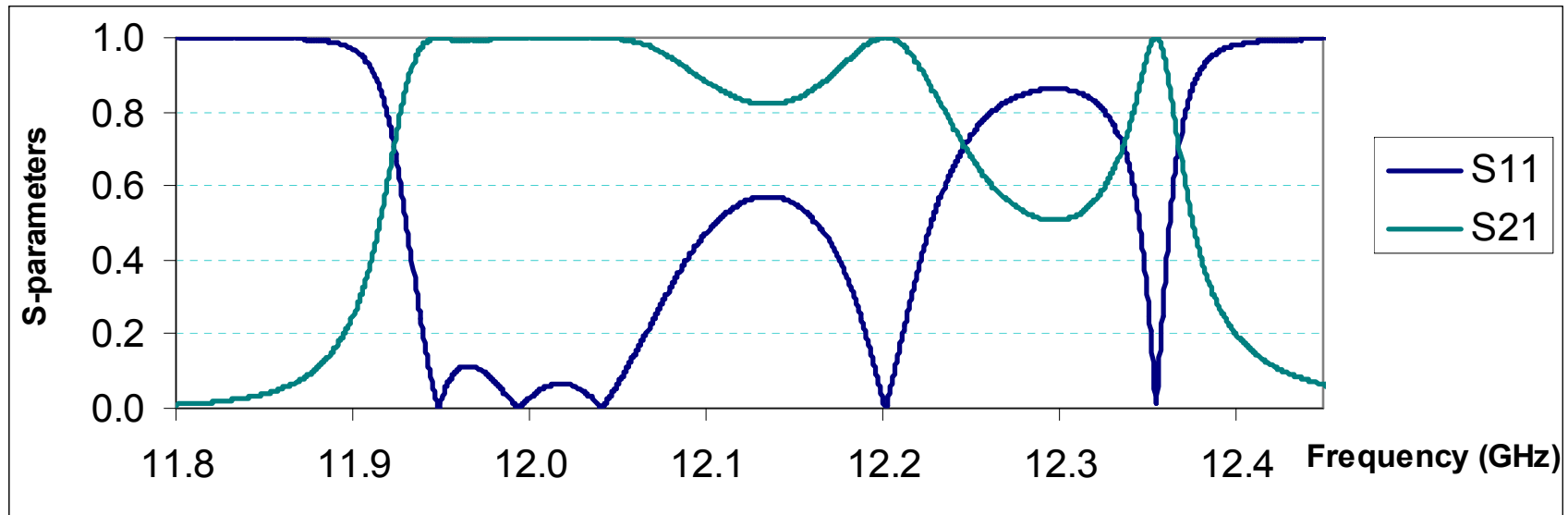


E end cell





S parameters & E field uniformity for a matched TW



Only 5 cells are used in the simulations but final design will have more cells.





Beam-loading Issues

- Beam-loading is typically large and depends on bunch offset
- Beam-loading might at worst vary randomly

Estimating voltage induced in crab cavity from one offset bunch

$r_b \sim 0.5$ mm (hopefully not this bad)

$R/Q = 4000$

$\phi = 0$

$q = 0.6$ nC

$\omega = 2\pi \times 12$ GHz

$$\delta V_i = \frac{1}{2} \frac{r_b \omega}{c} \omega \left(\frac{R_d}{Q} \right) q \cos \phi$$

$\delta V = 95$ V

$V = 2.4$ MV / cells ~ 160 kV

hence 32 offset bunches could shift amplitude by 2%





Phase Control Issues

- Microphonics are insignificant for thick copper structures.
- Structure length is proportional to phase error hence need good temperature stability and central mounting.
- How much might beam-loading perturb phase in CLIC crab cavity?
(Expected to be small?)
- Can travelling wave phase be determined accurately from the input phase or do unwanted modes, temperature and beam-loading give large uncertainties?
(If yes then only worry about source)
- If unwanted modes, temperature stability and beam-loading not a problem the phase stability is determined by Klystron or PET structure hence must drive cavities on opposing beams with same device.

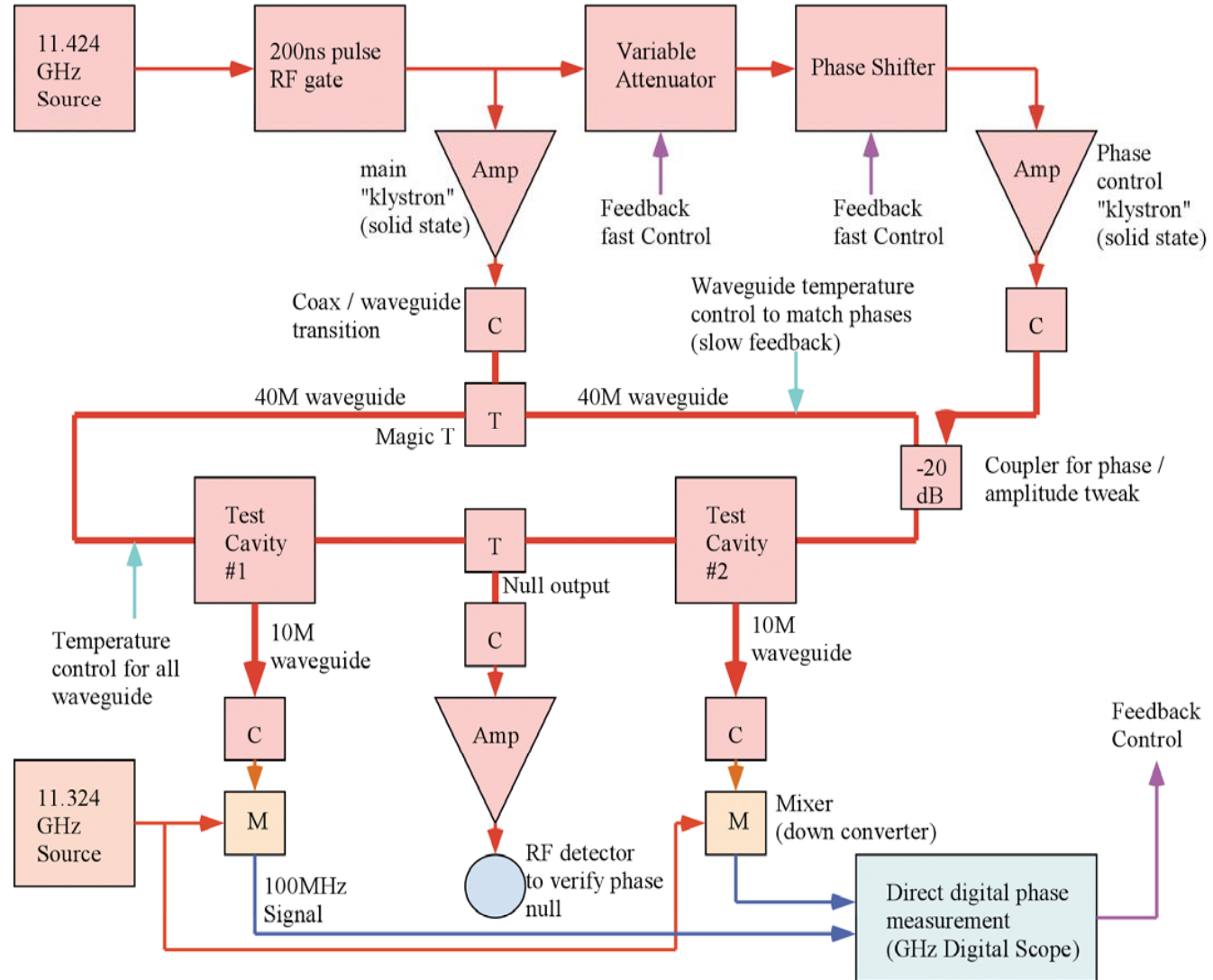




NLC phase synchronisation proposal



Crab Cavity Phase Stabilization Test System



courtesy of J. Frisch



Next Steps

- investigate maximum gradient vs. pulse length for X-band dipole structure at SLAC
- investigate pulse heating
- develop damped detuned structures.
- cooling requirements and mechanical design.
- determine likely phase and amplitude control performance for operation from a Klystron and from the PET structures.
- design beam test experiments.

