

# The CLIC Decelerator

Beam Dynamics Requirement for RF and Instrumentation

CLIC Workshop 2008

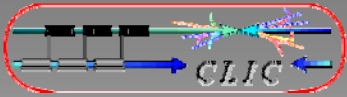
*Erik Adli, CERN/University of Oslo, October 15<sup>th</sup> 2008*

*Lots of input by D. Schulte + the rest of the CLIC team is gratefully acknowledged*

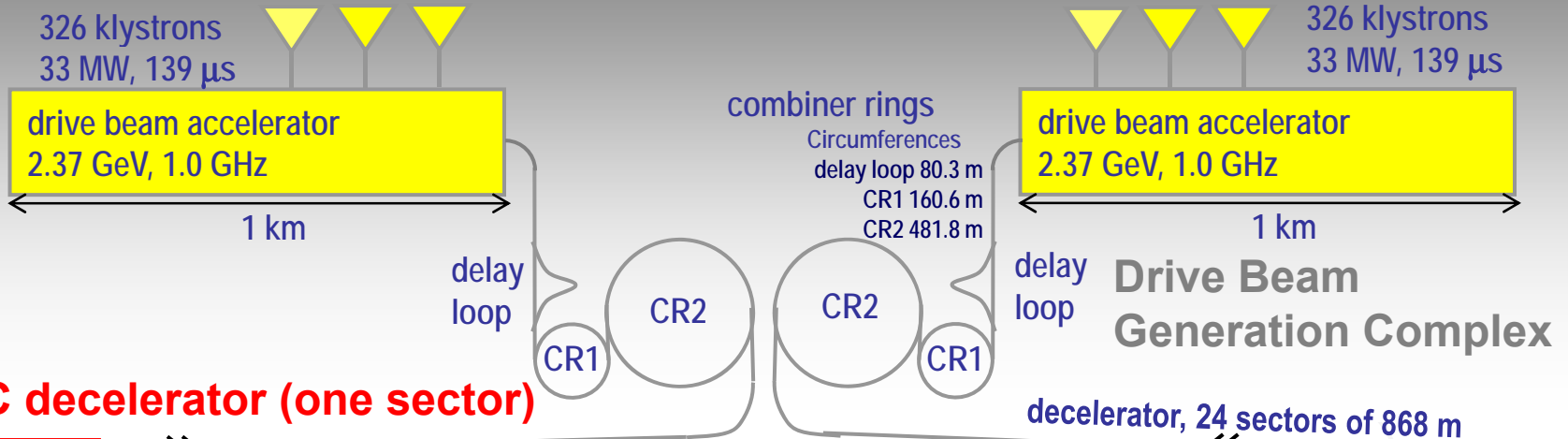


# Outline

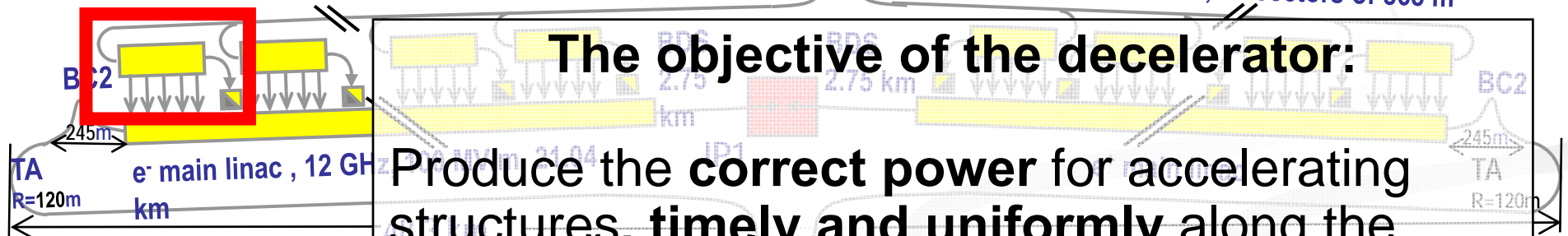
- **Introduction to the Decelerator**
- **Longitudinal dynamics**
- **Transverse dynamics**
- **Alignment and tolerances**
- **Instrumentation needs: outlooks**



# The CLIC decelerator



**CLIC decelerator (one sector)**



**The objective of the decelerator:**

Produce the **correct power** for accelerating structures, **timely and uniformly** along the decelerator, while achieving a **high energy extraction efficiency**

**Uniform power production** implies that the beam must be transported to the end **with very small losses**

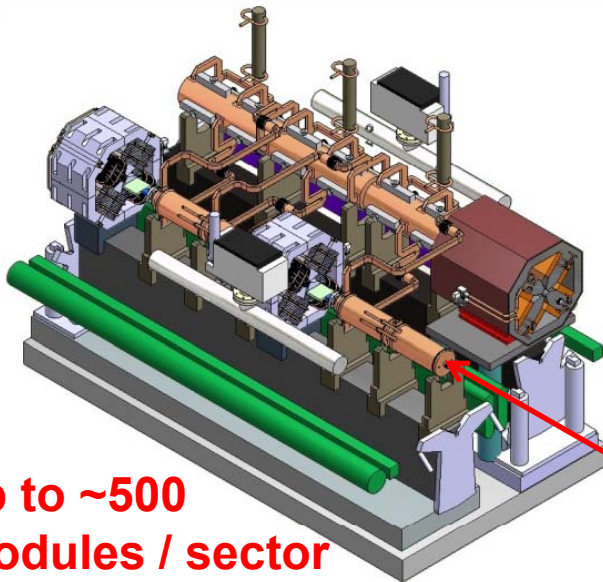
CLIC overall  
3 TeV

Main & Drive Beam generation complexes not to scale



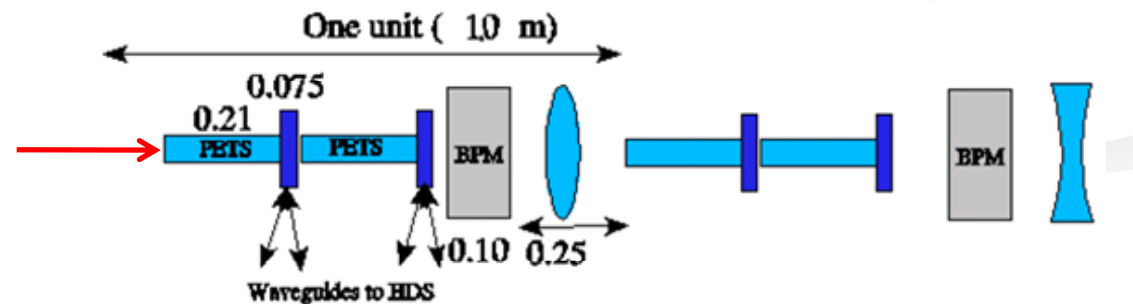
# Lattice

- 24 decelerator sectors per main linac :
  - Each sector receives one drive beam pulse of 240 ns, per main beam pulse
  - Up to  $S=90\%$  of the initial particle energy is extracted within each pulse leading to an energy extraction efficiency of about 84%
  - Varying sector length, because we require equal extraction efficiency per sector, while main linac module configuration changes



up to ~500  
modules / sector

100 A, 2.4 GeV



- **Baseline for decelerator studies:** we study the longest sector (1050 meter) with a PETS slot fill-factor of 71% ("worst case, for beam dynamics")
- Tight **FODO focusing** (large energy acceptance, low beta)
- Lowest energy particles ideally see constant FODO phase-advance  $\mu \approx 90^\circ$ , higher energy particles see phase-advance varying from  $\mu \approx 90^\circ$  to  $\mu \approx 10^\circ$



# Longitudinal dynamics

*Energy extraction and power  
production*

# PETS



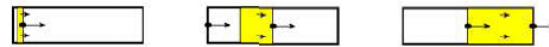
( 1 m PETS for TBTS )

## PETS 12 GHz fundamental mode:

$f=12.0$  GHz,  $R'/Q=2295$  Linac-Ohm/m,  $\beta=0.453$ ,  
 $Q\sim 7000$ ,  $L_{PETS} = 21.3$  cm

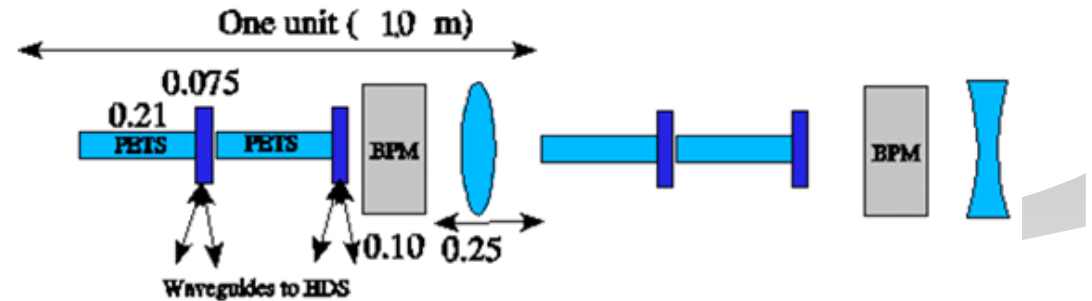
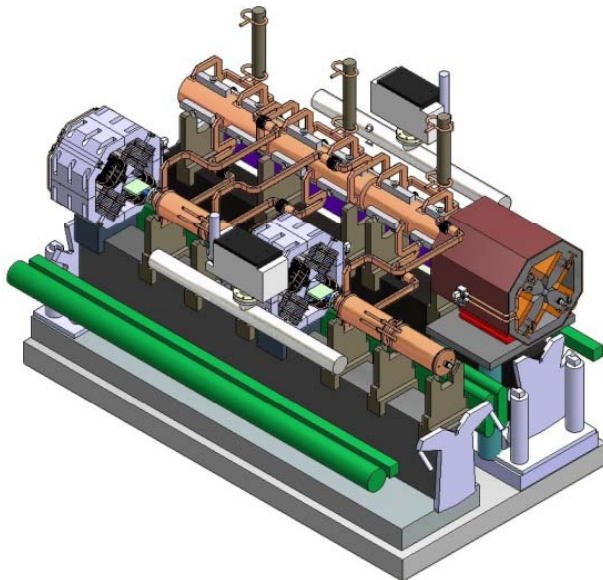
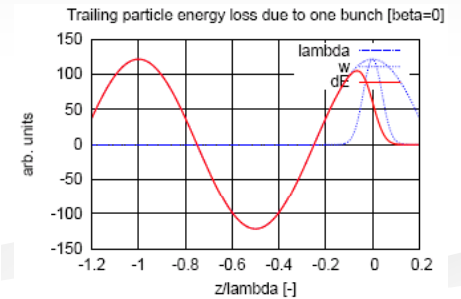
Input to PLACET from PETS design (I. Syratchev): delta wake for fundamental mode for structure with high group velocity.

$$w_L(z) = \omega_L \frac{R'}{Q} \frac{1}{1 - \beta_L} \cos(\omega_L \frac{z}{c}) (L - z \frac{\beta_L}{1 - \beta_L})$$



Energy loss: resonantly built up multi bunch wake + noticeable single bunch wake

$$\Delta E(z) = \Delta E_{sb}(z) + \Delta E_{mb}(z)$$





# The effect of deceleration

Baseline parameters [2008]:

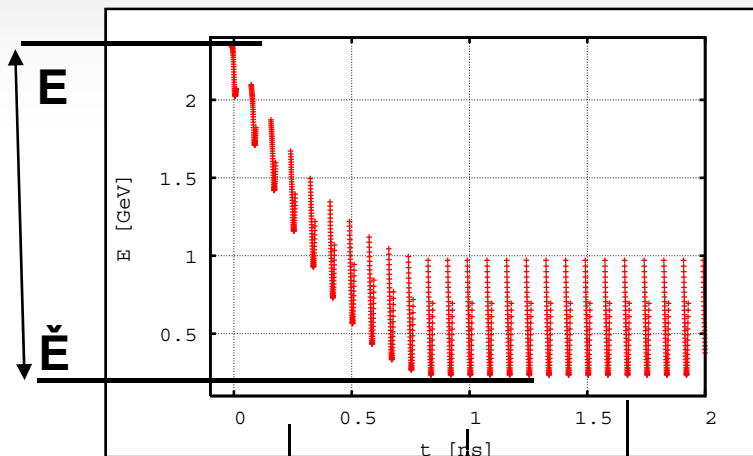
$E_0 = 2.4 \text{ GeV}$ ,  $I = 101 \text{ A}$ ,  $t \approx 240 \text{ ns}$  (2900 bunches)  
 Gaussian bunch,  $\sigma_z = 1 \text{ mm}$ ,  
 $\epsilon_{Nx,y} \approx 150 \mu\text{m} \rightarrow \sigma_{x,y} \approx 0.3 \text{ mm}$  at  $\beta_{\text{max}} = 3.4 \text{ m}$

Resulting energy profile (short transient + long steady-state)

$t_{\text{pulse}} = 240 \text{ ns}$

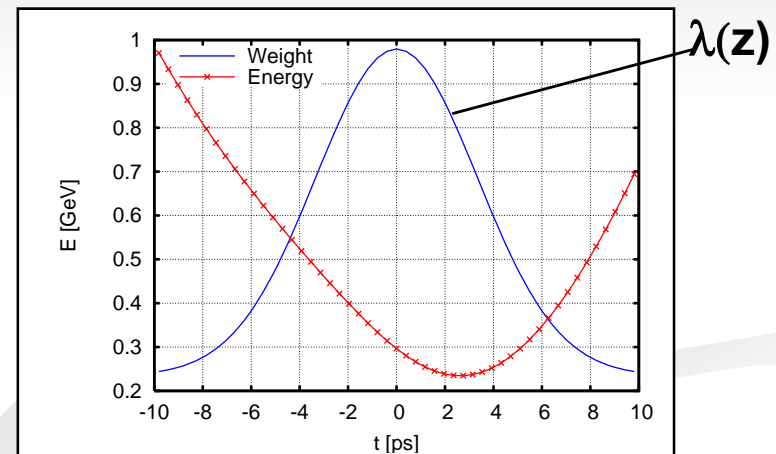
$S = (E - \check{E}) / E = 90\%$

$\check{E} = E(1-S)$   
 $= E - N_{\text{PETS}} \Delta \hat{E} = 240 \text{ MeV}$



$t_b = 83 \text{ ps}$

$t_{\text{fill}} = (L_{\text{PETS}}/v_g)(1-\beta_g) = 1 \text{ ns}$



$\sigma_z = 1 \text{ mm}$

$t_z = 3 \text{ ps}$

Power extracted from beam (ss) :

$$P \approx (1/4) I^2 L_{\text{pets}}^2 FF^2 (R'/Q) \omega_b / v_g = 136 \text{ MW}$$

Power extraction efficiency (ss) :

$$\eta = E_{\text{in}}/E_{\text{ext}} = S FF \eta_{\text{dist}} = 84\%$$

Transport of the decelerator beam: compromise high S (better efficiency, larger envelope) and high E (poorer efficiency, smaller envelope). In this study S=90% used



# Transverse dynamics

*Sources and mitigation of beam  
envelope growth*





# Metrics and criteria

- Because of the minimum-loss requirement we use as **metric the 3-sigma envelope** for the worst particle, defined as :

$$r \equiv \max \sqrt{(|x_i| + 3\sigma_{x,i})^2 + (|y_i| + 3\sigma_{y,i})^2}$$

*Given for maximum of simulated machines (usually 100)*

- **Simulation criterion** for minimum-loss transport:

$$r < \frac{1}{2}a_0 = 5.75 \text{ mm}$$

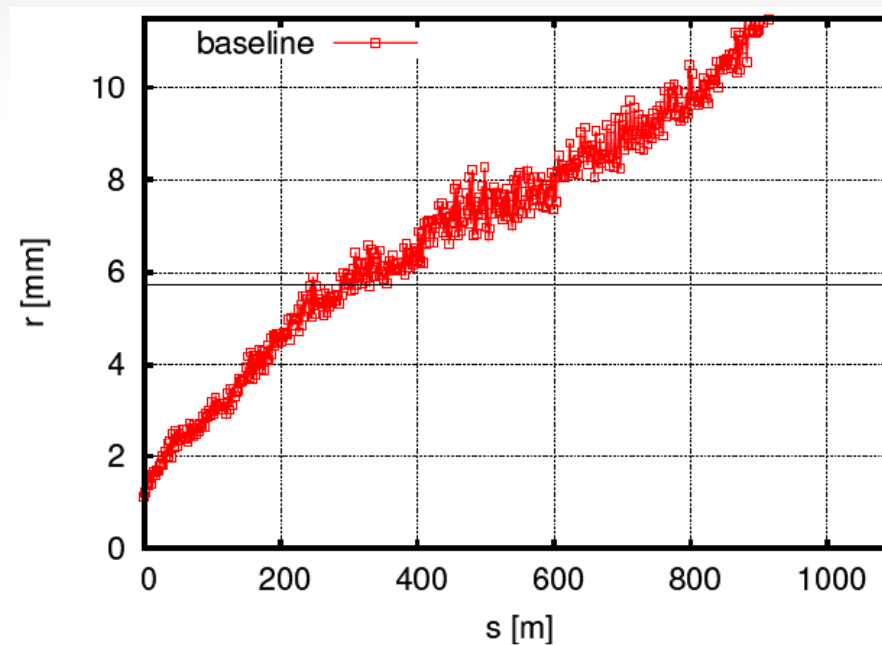
- Factor  $\frac{1}{2}$  : margin for unmodelled effects (particularly higher-order wake fields!)
- We require  $p_{\text{cllc}} > 99\%$ . 50 accelerator sectors  $\Rightarrow p_{\text{sector}} > 99.98\%$  of simulated machines should satisfy this criterion (!)

*Ideally we want the decelerator to be as robust as a (good) klystron – "push the button, and it should deliver the power!" – thus we approach the study with "worst-case" scenarios*

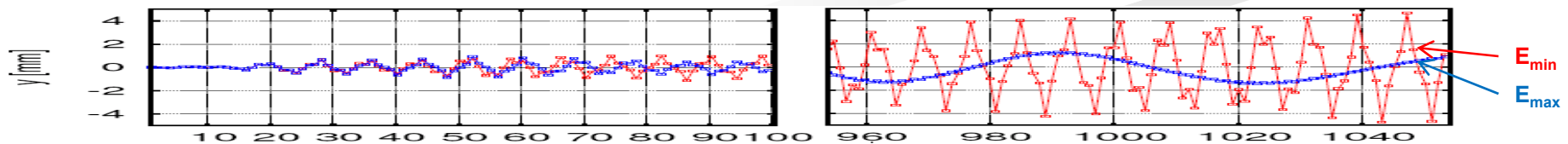


# Results: baseline

- Beam envelope,  $r$ , along the decelerator sector lattice for baseline parameters, incl. component misalignment as expected after static alignment (baseline:  $\sigma_{\text{quad}}=20 \mu\text{m}$ )



- Driver of envelope: mix of higher and lower energy particles

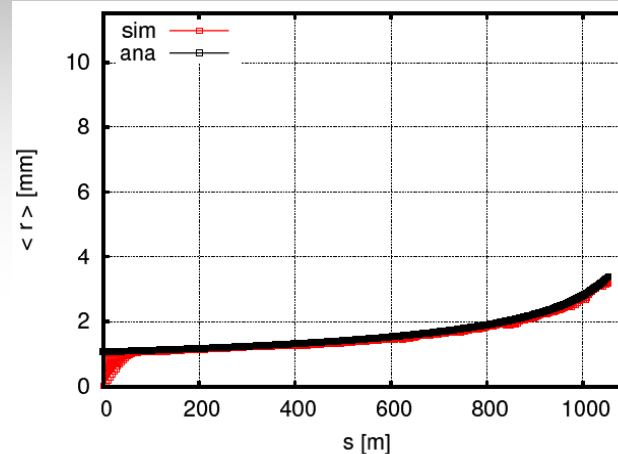




# Minimum final envelope

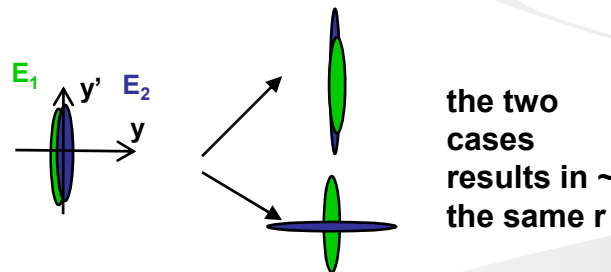
Adiabatic undamping in a **perfect machine** :  $\propto \sqrt{\gamma_i/\gamma_i}$

*3-sigma particle in a perfect beam, perfect machine*



$r_{\min} = 3.3 \text{ mm}$   
(factor  $\sim 3$  increase)

- Relative phase-space orientation of transverse distribution:
  - irrelevant for  $r$
  - emittance growth not necessarily good indication of envelope growth

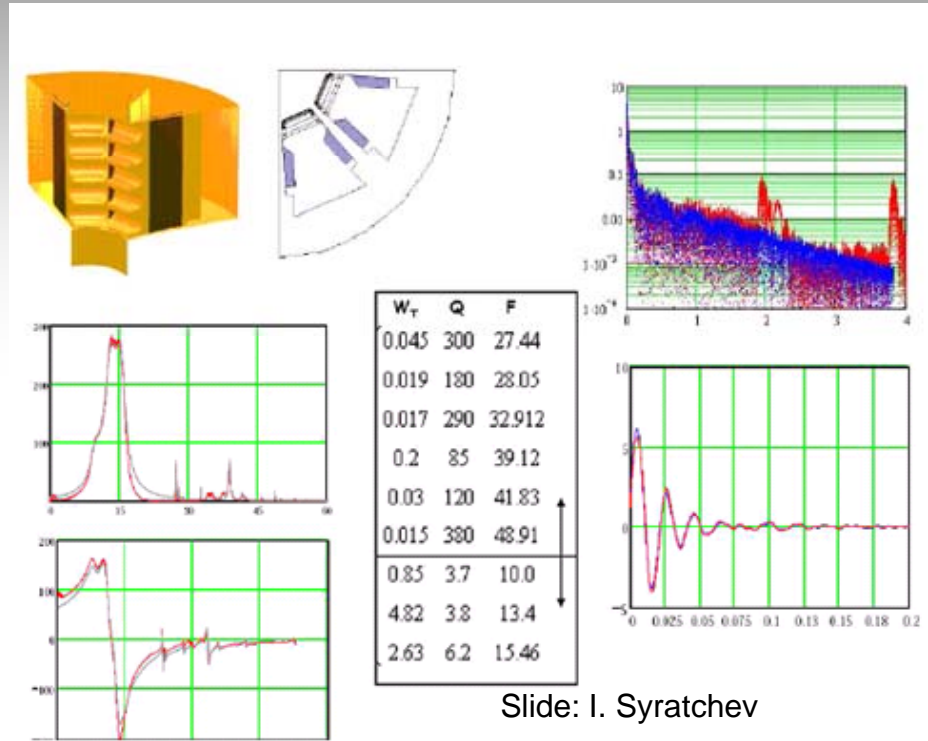


- To study the various contributions to the envelope growth it is often useful to work with a "pencil beam" of **slice centroids** only, and we denote the *centroid envelope* as  $r_c$



# Transverse wakes: dipole modes

- PETS transverse impedance is simulated and a set of discrete dipole modes are extracted to represent the impedance (I. Syratchev)
- Each mode implemented in PLACET ( $f_T$ ,  $w_T$ ,  $Q_T$ ,  $\beta_T$ ) and included in the PETS element (D. Schulte)



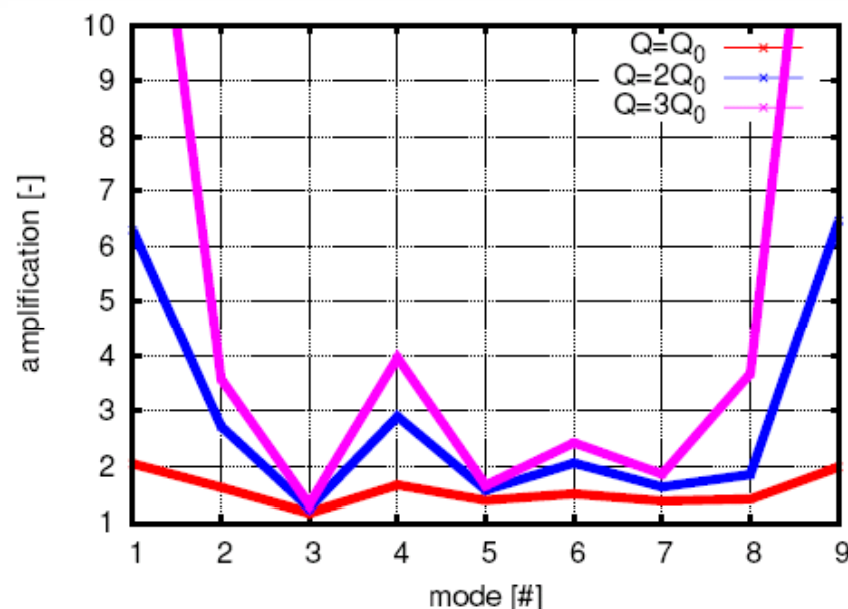
$$W_{T_i}(z) = w_{T_i} \sin\left(\omega \frac{z}{c}\right) \left(L - z_{ij} \frac{\beta_T}{1 - \beta_T}\right) e^{-z\omega/2cQ(1-\beta_T)} [V/Cm]$$

$$\Delta y'_w = \sum_{modes} \frac{\Delta p_{y,w}}{m_w c} = \sum_{modes} y_s \frac{q_s q_w}{E_w} W_{\delta T}(z) [rad]$$

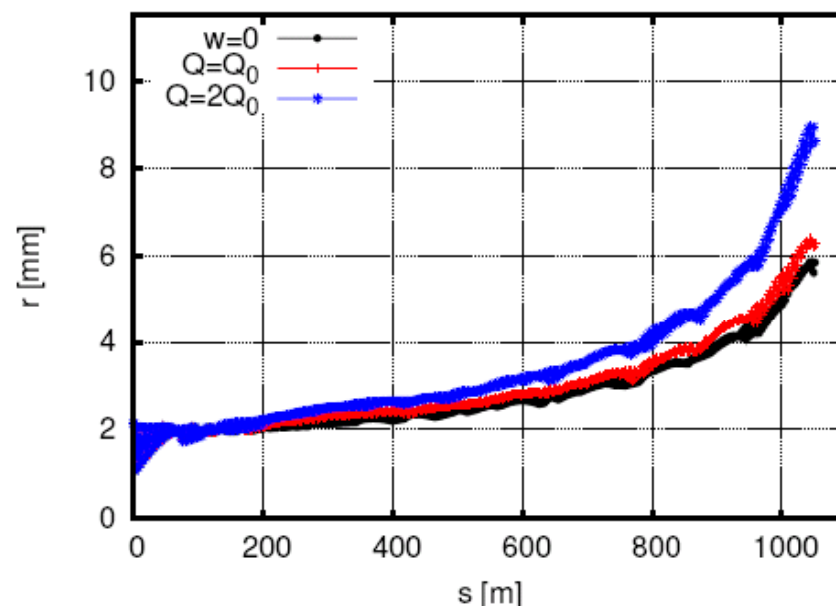


# Input to PETS design

- During the 12 GHz PETS design, beam dynamics simulations were done in an iterative process with the PETS design to ensure small amplification due to transverse wakes. **Summary:**



***Amplification of centroid motion,  $r_c$ , for each dipole mode (beam jittered at mode frequency)***

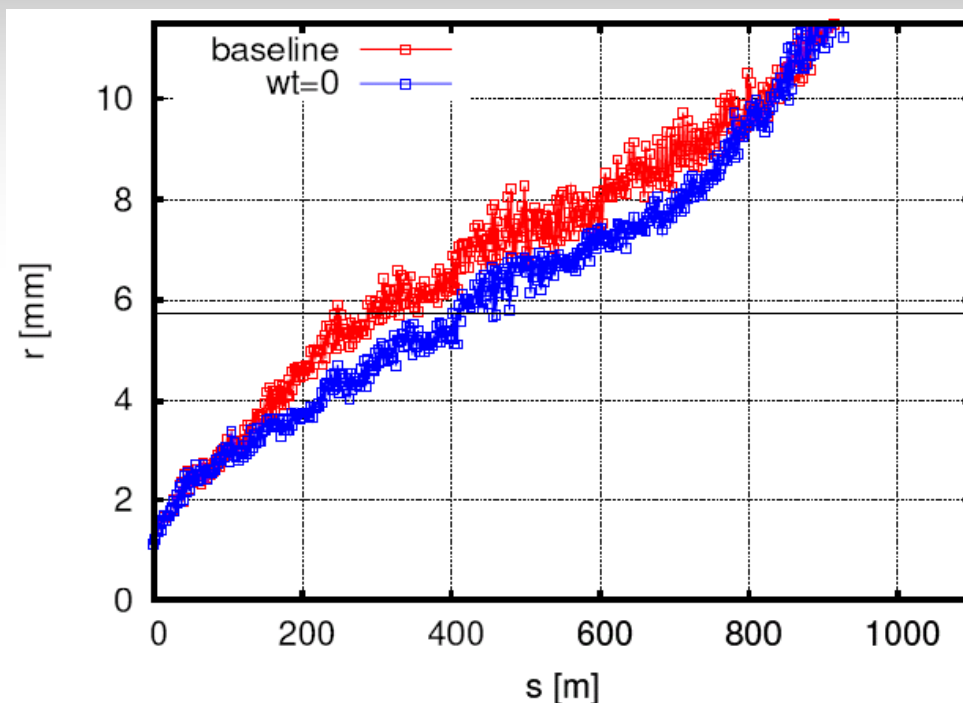


***Amplification of total beam envelope,  $r$ , jitter on all mode frequencies ( $1\sigma$  jitter in total)***



# Results: baseline

- Baseline + case w/o transverse wakes



*"Guide" to graphs: red will usually mean baseline parameters*

- Effect PETS transverse wakes mitigated efficiently for nominal PETS parameters. Envelope is now mainly driven by quadrupole kicks. However,  $Q=2Q_0$  leads to unacceptable wake amplification.
- However, quadrupole kicks alone + undamping already leads to unacceptable beam envelope

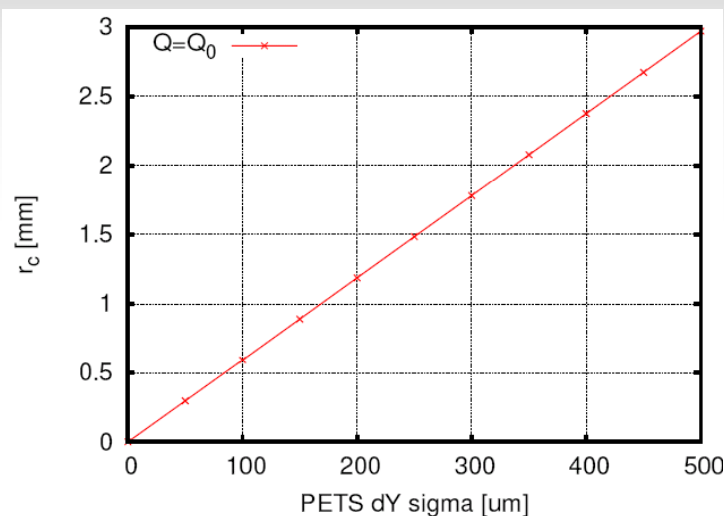


# Alignment



# Alignment tolerance requirement

We require that no single misalignment should drive our centroid (pencil beam) envelope more than 1 mm,  $r_c < 1$  mm (here max. out of 10000 mach):



Tolerance	Value	Comment
PETS offset	100 $\mu\text{m}$	$r_c < 1$ mm fulfilled
PETS angles	$\sim 1$ mrad	$r_c < 1$ mm fulfilled
Quad angles	$\sim 1$ mrad	$r_c < 1$ mm fulfilled
Quad offset	20 $\mu\text{m}$	As small as possible, within reasonable limits. 20 $\mu\text{m}$ is within spec. of alignment system ( $r_c < 1$ mm $\Rightarrow$ quad offset of 1 $\mu\text{m}$ )
BPM accuracy (incl. static misalignment and elec. error)	?	
BPM precision (diff. measurement)	?	

Seems feasible for all misalignment types, except quad offset

$\Rightarrow$  **Beam-Based Alignment of quads necessary**



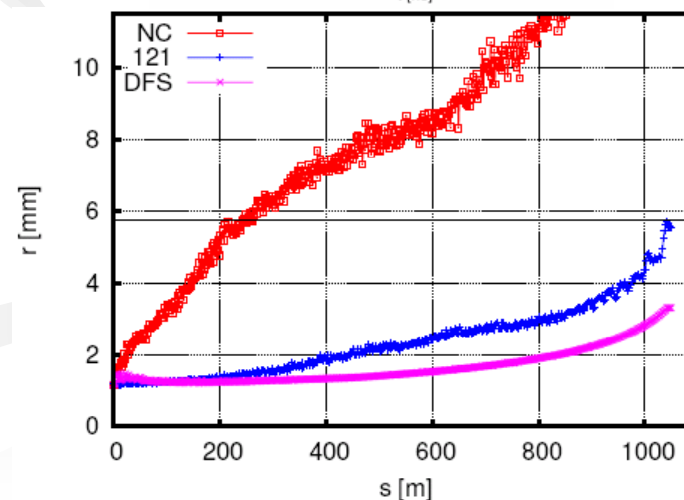
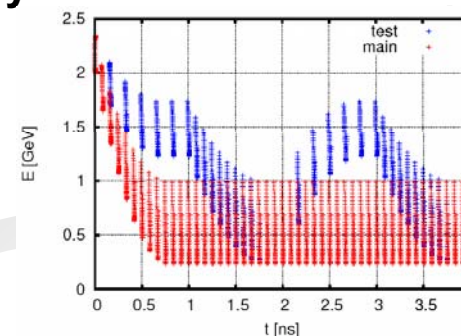


# Need for Beam-Based Alignment

- Beam envelope several factors far too large for an uncorrected machine
- 1-to-1 steering steers the beam centroid into BPM centres. However, the remaining quad kicks are enough to build up significantly *dispersive trajectories* so that the *envelope* is still large after 1-to-1 with BPM accuracy of 20  $\mu\text{m}$  (misalign. + el. error)
- Thus of interest to **minimize dispersive trajectories**: e.g. Dispersive Free Steering: using empty bunches by delayed switching we can in principle perform **Dispersive-Free Steering within one pulse, without changing any machine or beam parameters**, except the SHB switching.

Tolerance	Value	Comment
PETS offset	100 $\mu\text{m}$	$r_c < 1 \text{ mm}$ fulfilled
PETS angles	$\sim 1 \text{ mrad}$	$r_c < 1 \text{ mm}$ fulfilled
Quad angles	$\sim 1 \text{ mrad}$	$r_c < 1 \text{ mm}$ fulfilled
Quad offset	20 $\mu\text{m}$	Must be as small as possible. 20 $\mu\text{m}$ is within spec. of alignment system ( $r_c < 1 \text{ mm} \Rightarrow$ quad offset of 1 $\mu\text{m}$ )
BPM accuracy	20 $\mu\text{m}$	Must be as small as possible.
BPM precision	$\sim 2 \mu\text{m}$	Suppresses significant tails in distribution of envelopes

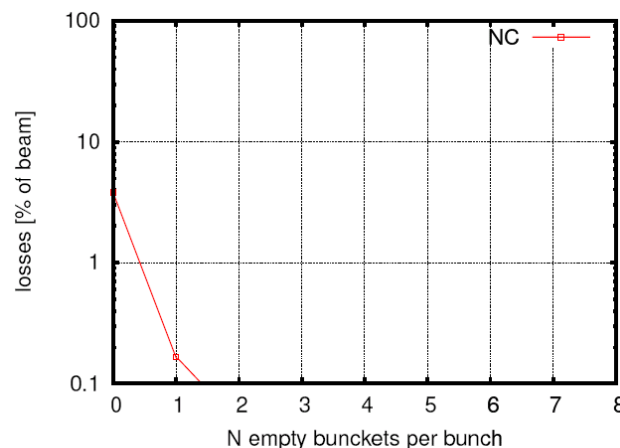
For more on  
**BBA: see talk  
 E. Adli  
 "Alignment  
 studies:  
 Decelerator and  
 CTF3"**  
 Room: 60-6-002:  
 16-Oct, 14:20 )





# BBA and tune-up aspects

- Significant losses (several %) is expected if the nominal beam is transported in a machine before beam-based alignment is applied
  - Losses also means difficulties for response-based steering machines like DFS (sensitivity to current jitter, BPM might become less predictable with losses)
- The BBA should be initialized with a low current beam (**short pulse as well as empty buckets**) – the resulting higher energy and smaller avg. current leads to much smaller envelope and losses
  - Implies that BPMs must be sensitive down to a fraction of nominal current



- The average current will gradually be increased (less empty buckets). For each increase in current a BBA procedure, first 1-to-1 then DFS will be applied to the initial beam. When nominal avg. current is reached one can increase pulse length towards the nominal



# Instrumentation

*Work in progress*

## Main tasks of Drive Beam instrumentation:

- “Do we transport the beam well?”
  - If not: “why not? What and where is the problem?”
- “Do we produce the correct power (amplitude and phase)?”
- Ensure performance of beam-based alignment
- Commissioning: special needs

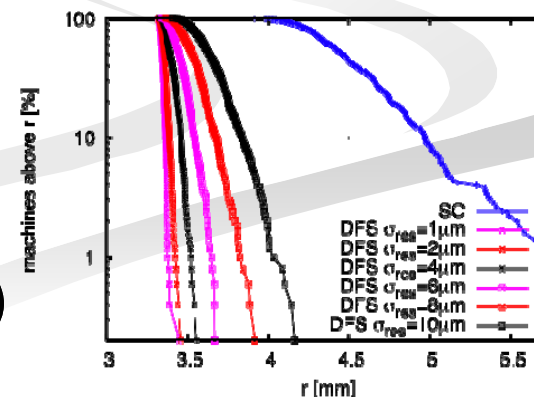


# Along lattice: BPMs

The need for beam-based alignment implies:

- One BPM per quadrupole (baseline)
- Total number of BPMs:  $\sim 24 * 2 * 900 = \sim 40000$
- Production beam: 100 A (50 A for BBA/DFS)
  - **BPM accuracy:**  $\sim 20 \mu\text{m}$  (incl. static misalignment)
  - **BPM diff. meas:**  $2 \mu\text{m}$  ( $\leftrightarrow$  precision of  $\sim 1 \mu\text{m}$  ?)
- Commission beam:  $\sim 100/N$  A, ( $N \sim 10$ )
  - BPM (abs. pos.) accuracy:  $\sim 20 \mu\text{m}$
  - BPM diff. meas : up to  $10 \mu\text{m}$  probably ok (with gradually better resolution up to  $2 \mu\text{m}$  for 100 A)
- Expected centroid displacement:
  - $< 3 \text{ mm}$  (uncorrected machine)
- Expected rms size
  - $< 4 \text{ mm}$  (uncorrected machine)
- Available length for BPMs:  $\approx 9 \text{ cm}$
- **Time resolution:**  $\sim 20 \text{ ns}$  (fraction of  $t_p$ )
- Machine protection: yes (TBC)

(exact values will need further study)





# At sector start : I and FF

- Power production depends mainly on PETS parameters, bunch frequency + **current** and **Form Factor** :

$$P \approx (1/4) I^2 L_{\text{pets}}^2 F(\sigma)^2 (R'/Q) \omega_b / v_g$$

- We suggest to be able to estimate power production from drive beam entering the decelerator to within ~0.1%
- *Precision* measurement of these parameters at the start of the lattice:
  - **Current measurement, precision: <= 0.1%**
  - Form factor, precision: <= 0.1 %
  - $F(\sigma) \propto \exp(-(1/2)\sigma^2/\lambda^2) \rightarrow$  **bunch-length meas. precision: ~1%**  
(**one-shot** measurement is probably ok)
- In addition: **continuous current monitoring** along lattice, but with **relaxed precision (~1%)** - ideally: BPMs used as current monitors?



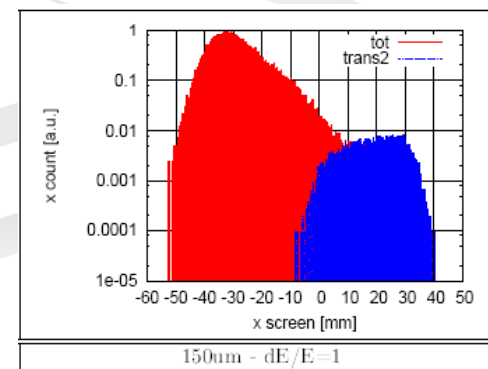
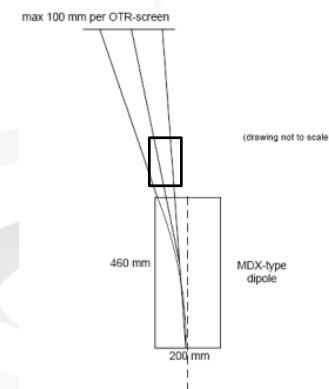
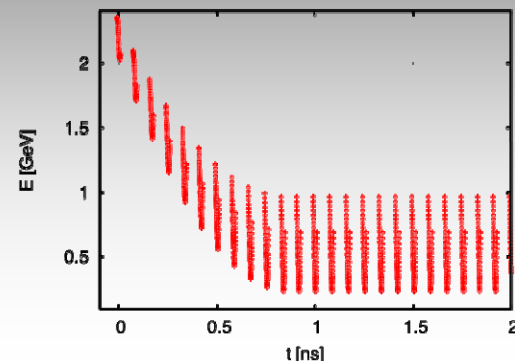
# Along lattice: loss monitors

- Important for tune up, failure monitoring and localization of fault
- High sensitivity (could risk small but steady losses along the lattice). Suggested sensitivity: ~1% of one bunch: 80 pC on one detector (depending on interval)
- Spatial intervals of detectors: TBD, but order of some 10's of meter is suggested
- Challenge: separate drive beam losses and main beam losses (main difference: E)



# Sector dump: energy measurement

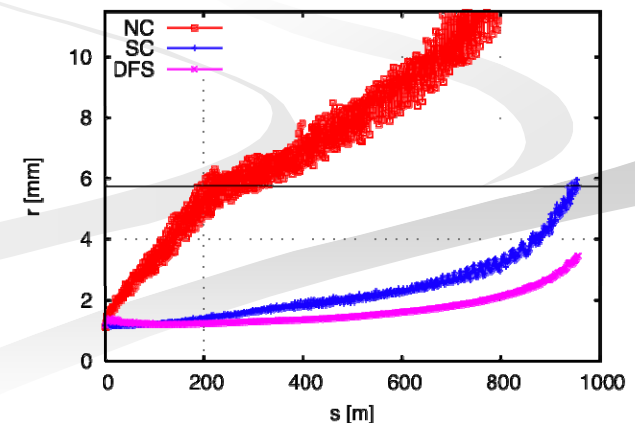
- Spectrometer dump
  - Measure energy extracted from beam
- Desirable: one **fast BPM** (12 GHz) to verify time-resolved centroid energy of each bunch
  - ~ 10um seems sufficient, depending on geometry
- Desirable: **segmented dump**, total beam energy measurement (cross-check with power production)
  - ~ 100 um screen resolution
  - ~ 3 OM dynamic range
  - ~ 20 ns time resolution (segmented dump)





# Along lattice: transverse profile monitors

- At selected positions along the lattice
  - ~10 per decelerator would give good picture of envelope growth
  - Important for tune up and failure monitoring
  - 1 sigma transverse size:
    - uncorrected machine : 0.3 mm at start up to 3 mm at end
    - Corrected machine: 0.3 mm at start up to 1 mm at end
  - Range: desired to observe 3 sigma size
  - Precision: 50 um adequate

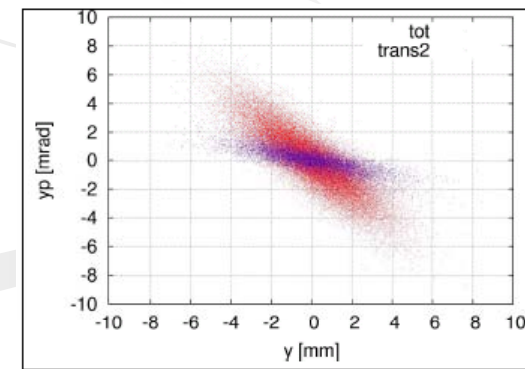
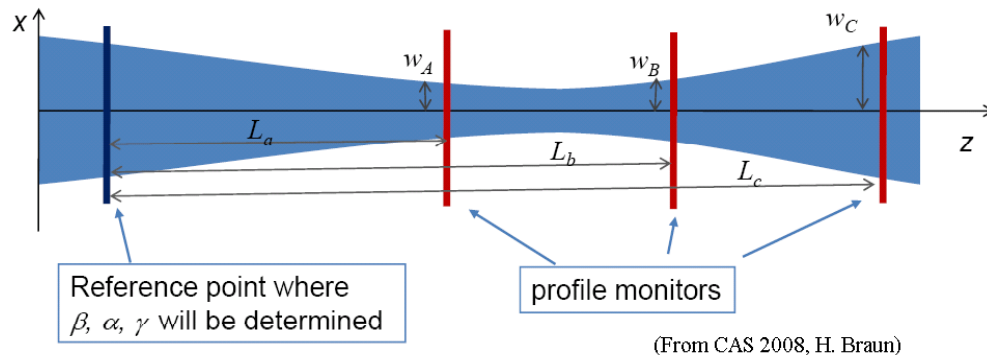






# Dump: transverse phase-space

- Transverse phase-space
  - Useful for tune-up
  - Useful for verification of beam dynamics
  - Set of profile monitors better than quad-scan, due to energy spread :
  - See the transverse screens slide (need to have at least 3 profiles towards the end of the decelerator)



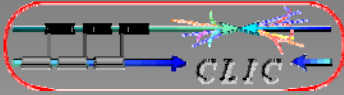


# Conclusion: decelerator

- Simulations gives **reasonable confidence for minimum-loss transport of the decelerator beam**
- **Beam-Based Alignment is needed**, and **Dispersion-Free Steering** seems to be an excellent alternative
- Dispersion-Free Steering comes almost "**for free**" with the use of delayed switching
- **Tune-up procedures** must be applied
- Simulations need to be benchmarked and technology needs to be proven: **TBTS and TBL**

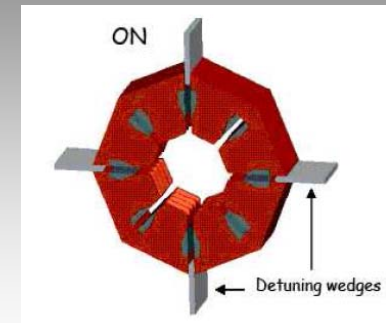


**Extra (more)**

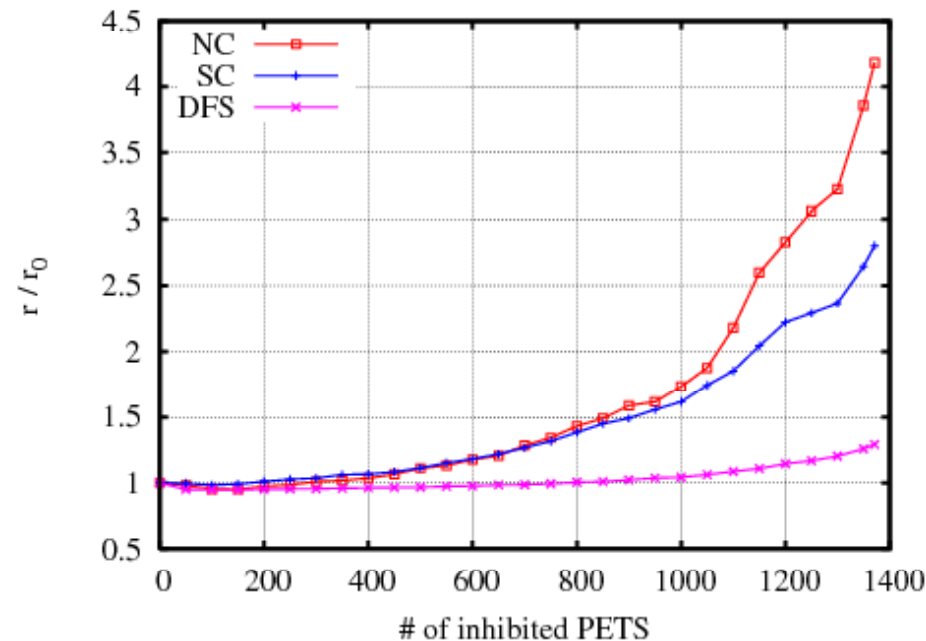


# PETS: effect of inhibition

- "Petsonov": on/off mechanism
  - Simulated as  $R/Q=0$ ,  $Q_T=2Q_{T0}$  (worst-case)
- Effect of inhibition on the beam dynamics:
  - the lack of deceleration leads to higher minimum beam energy and thus less adiabatic undamping and less energy spread
  - dipole wake kicks increase; for a steered trajectory the change of kicks will in addition spoil the steering
  - the coherence of the beam energy will increase, and thus also the coherent build up of transverse wakes



*A number of random PETS inhibited (averaged over 100 seeds)*



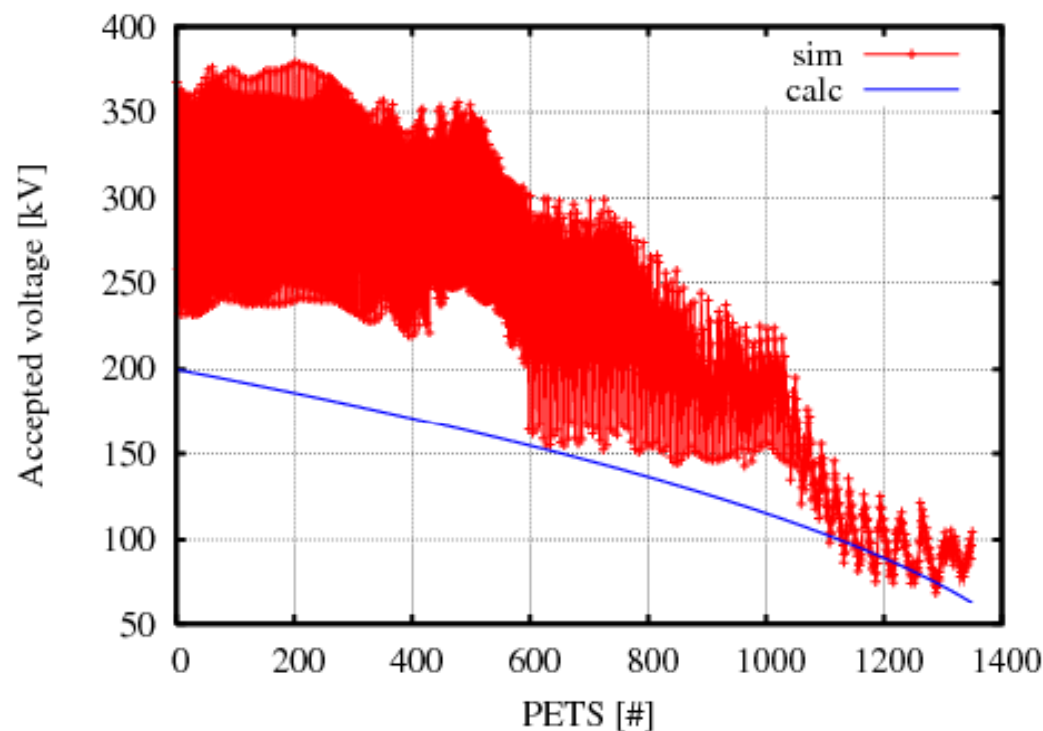
*Negligible effect on beam envelope for up to 1/3 of all PETS inhibited, and even more for a DFS steered machine*



## PETS: estimation of accepted break down voltage

- Maximum accepted transverse voltage accepted if we require  $r_c < 1$  mm due to this kick

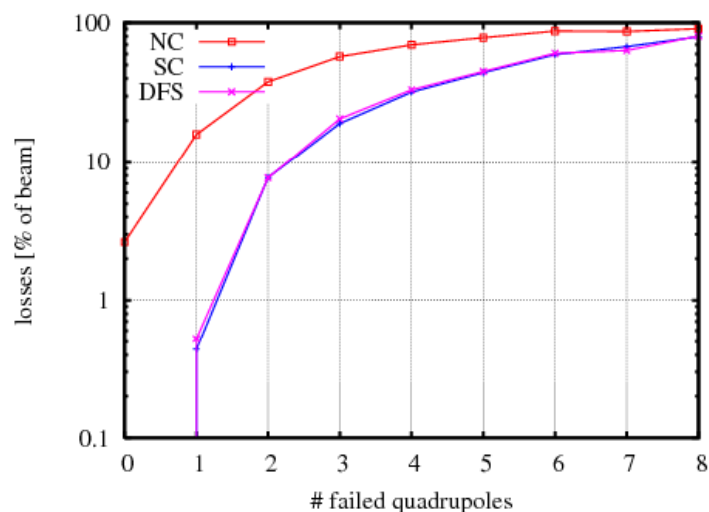
$$U = \Delta y' \times E = \frac{r}{A\hat{\beta}} / \sqrt{\frac{E_i}{E_f}} \times E_i = \frac{r}{A\hat{\beta}} \sqrt{E_i E_f}$$



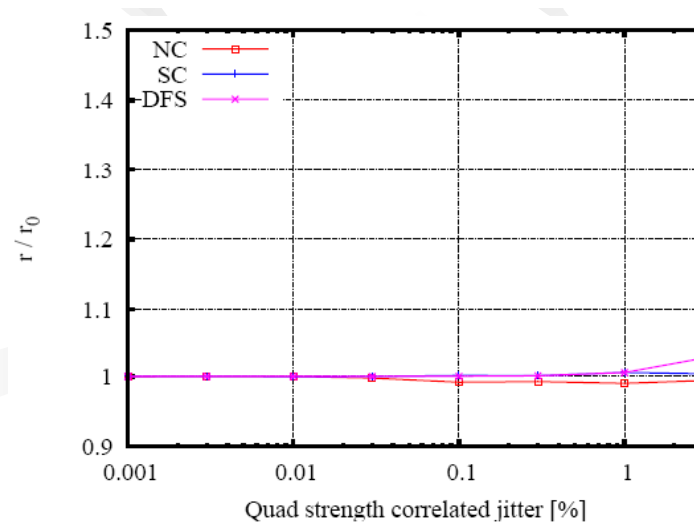
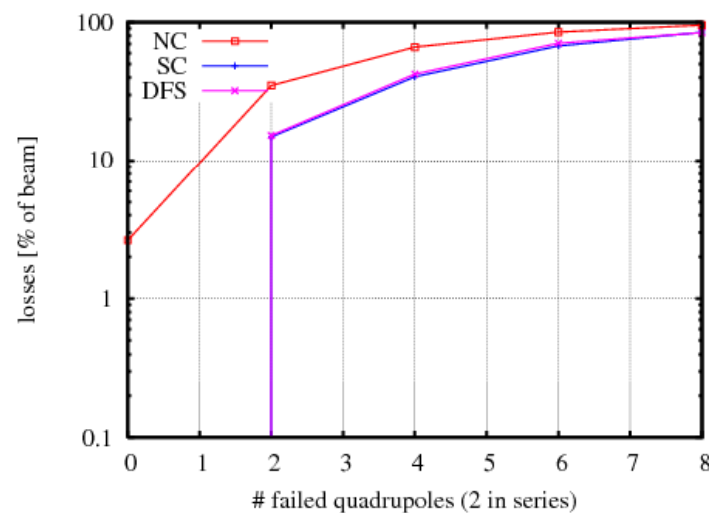
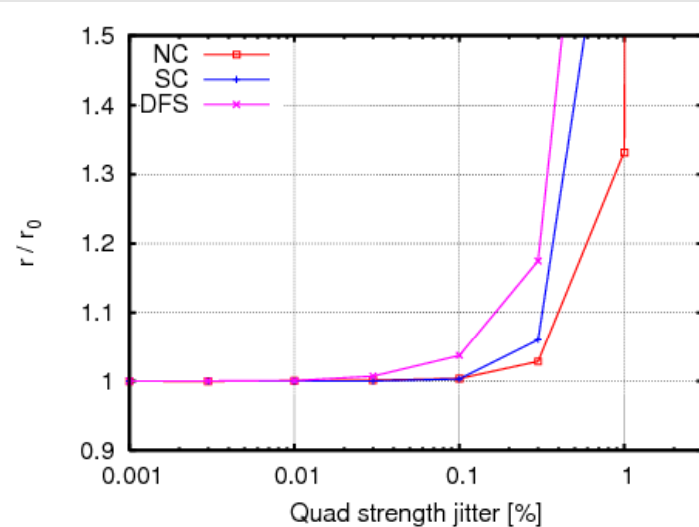


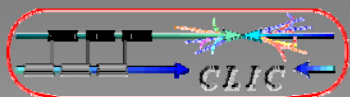
# Quadrupole jitter and failure

**Losses as function of random quad failure**



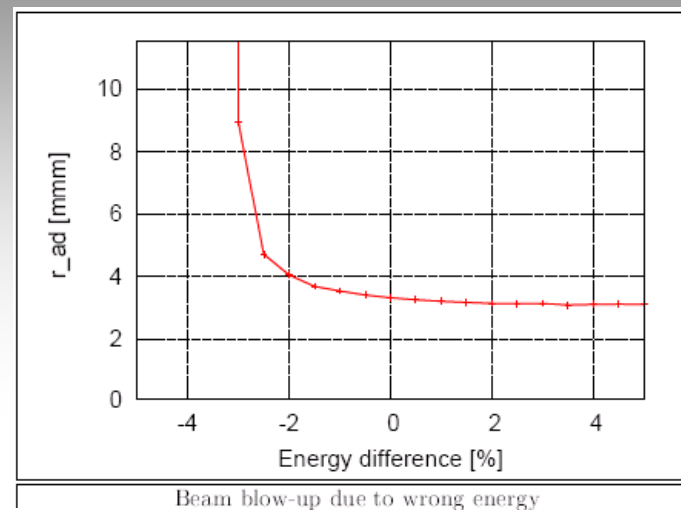
**Envelope increase as function of quad jitter**



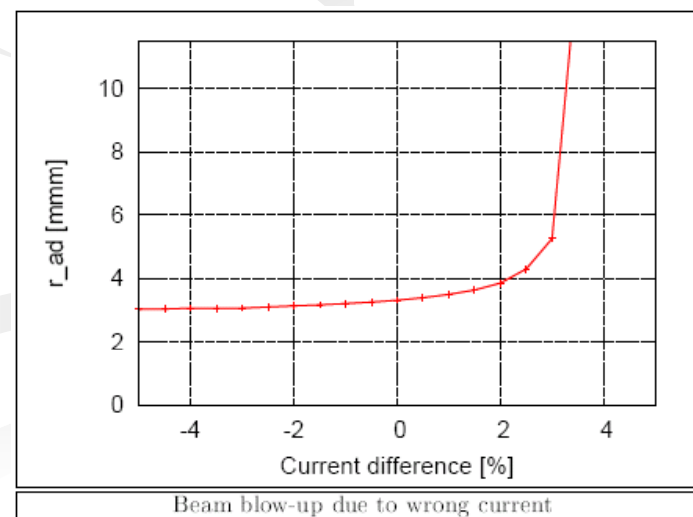


# Lattice focusing

**For a given optics 3% change, or more, in initial current or energy will induce losses**



$$E_{unstable}/E_0 < (1 - S) \left( \frac{\sin(\mu/2)}{\sin(180^\circ/2)} \right) + S \approx 0.97$$

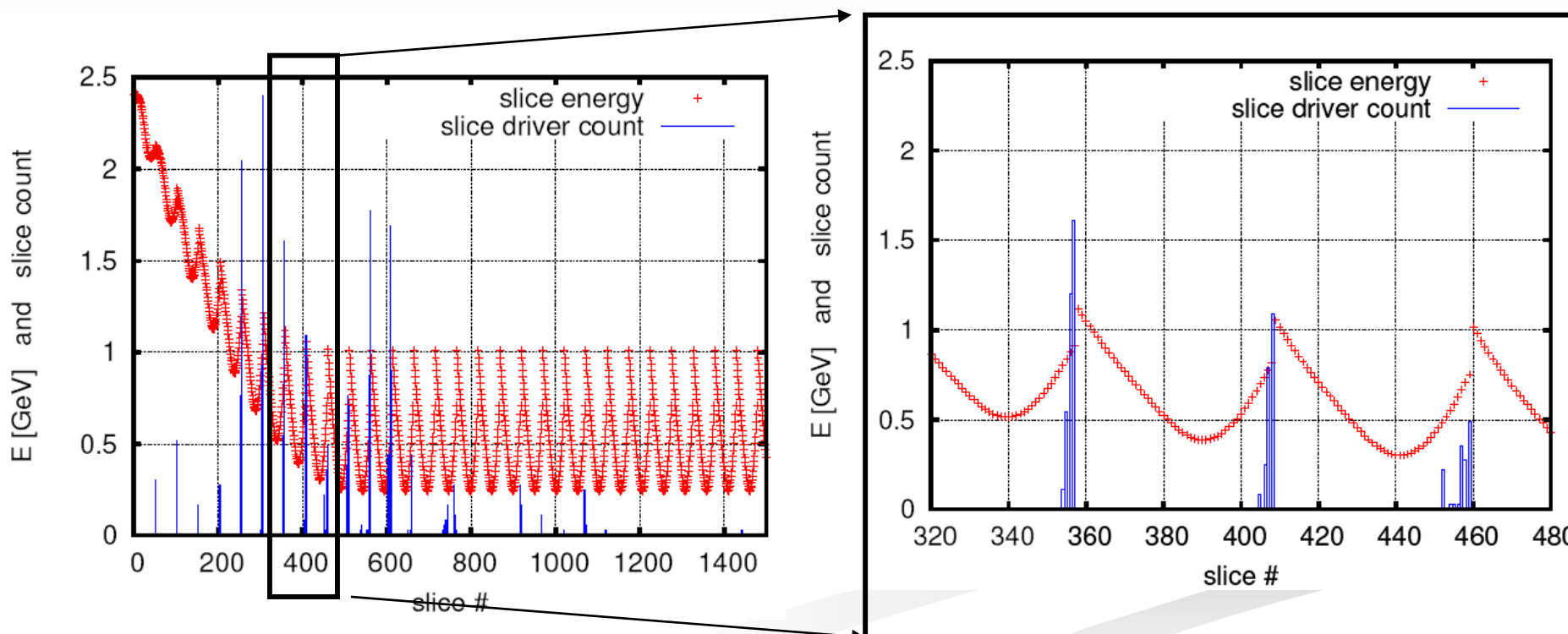


$$I_{unstable}/I_0 > \frac{1}{S} - \left( \frac{1}{S} - 1 \right) \frac{\sin(\phi_0/2)}{\sin(180^\circ/2)} \approx 1.03$$



# Origin of wake amplification

- Further investigation shows the amplification of the envelope typically [depending on scenario] is driven by particles towards the end of the bunch  
→ single bunch dipole wake significant



**Corollary: since single bunch wake is sine-like, shorter bunch-length might reduce PETS wake amplification**



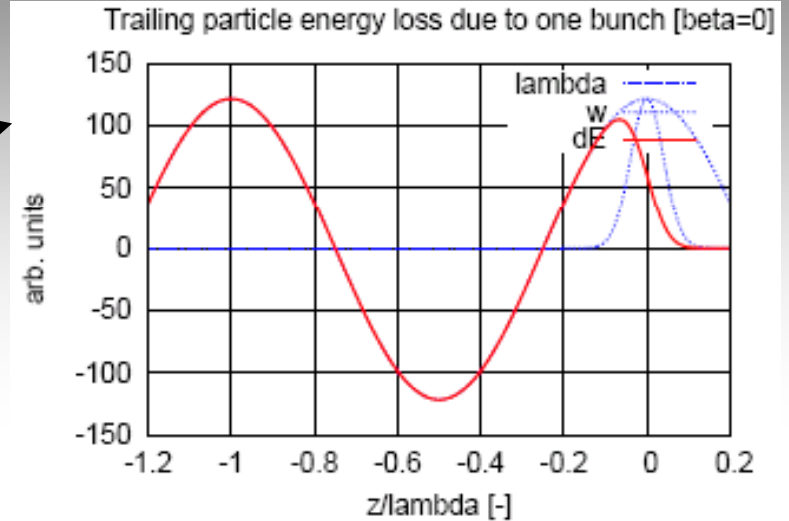


# PETS energy extraction

Single particle energy loss:

$$\Delta E(z) = N e^2 \int_z^\infty dz' \lambda(z') w_L(z' - z)$$

example for  
Gaussian  
bunch



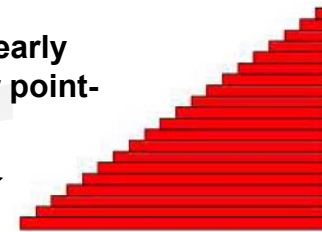
PETS longitudinal d-wake, including group velocity:

$$w_L(z) = \omega_L \frac{R'}{Q} \frac{1}{1 - \beta_L} \cos(\omega_L \frac{z}{c}) (L - z \frac{\beta_L}{1 - \beta_L})$$

Energy loss from leading bunches + single bunch component:

$$\Delta E(z) = \Delta E_{sb}(z) + \Delta E_{mb}(z)$$

field builds up linearly  
(and stepwise, for point-  
like bunches)



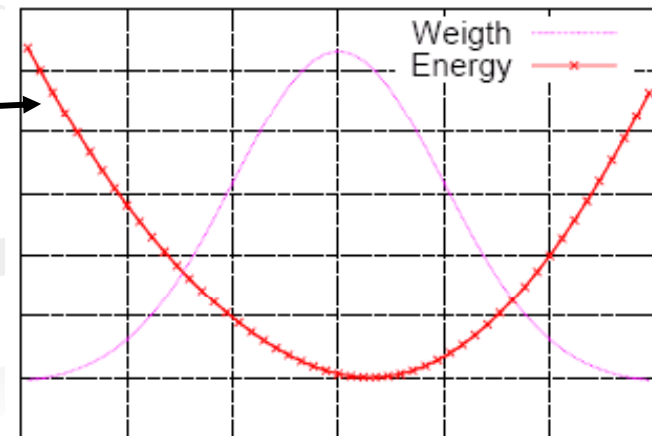
**Approx:** sb component equal to mb, and linear field increase:

$$\Delta E(z) \approx \frac{n_{sb}}{2} L_{PETS} A N e^2 F(\lambda) \cos kz$$

Integrating  $\Delta E$  over bunch gives second  
form factor, and times  $f_b$  gives extr. power:

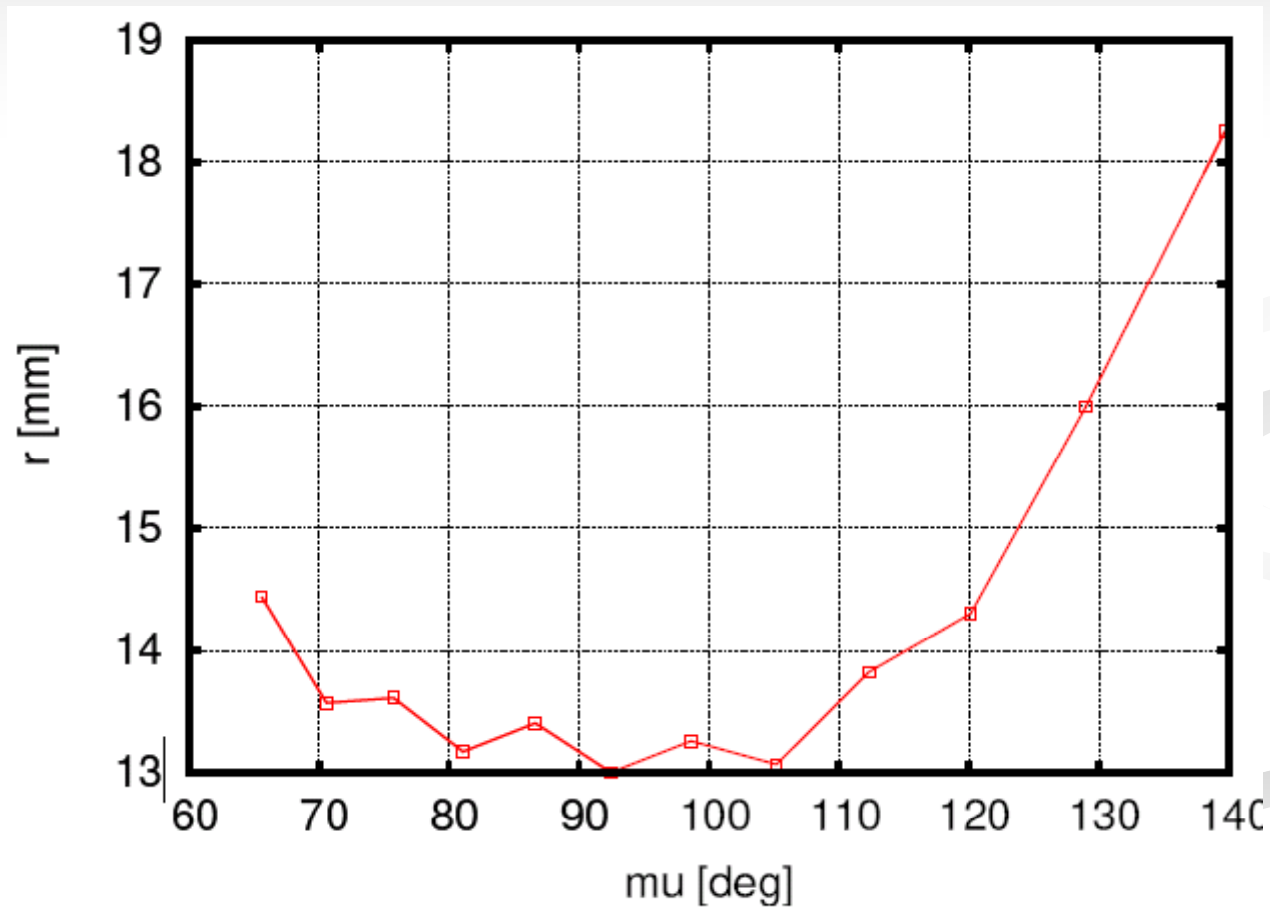
$$P \approx \frac{1}{2} I^2 L_{PETS}^2 F^2(\lambda) \frac{R'}{Q} \omega_L \frac{1}{\beta_L c} \quad (\text{x } 1/2 \text{ for linac-Ohms})$$

if mb assumption is good,  
wake function is recognized  
for particle energy loss of z





# Dependence on FODO phase-advance





# Simulation overview

***The following effects are included in the simulation studies :***

- PETS transverse effects (baseline)
  - Transverse wakes (long and short range)
  - RF-kicks
  - Adiabatic undamping
- Lattice component misalignment (baseline)
  - PETS misalignment (offset, angle)
  - Quadrupole misalignment (offset, angle)
  - BPM misalignment (offset, angle), BPM finite precision
- Beam perturbations (studied separately)
  - Beam offset
  - Beam jitter

***Not included in the simulations for the work presented here :***

- Higher-order wakes
  - Effect should be limited within  $r < \frac{1}{2}a_0$  (but probably worth looking further into)
- Resistive-wall wake
  - Estimates following the strategy in [B. Jeanneret et al.] show that the effect is small
- Energy spread: Spread is small comparable to PETS induced spread, but to fulfill  $S=90\%$   $E_0$  should be increased by  $\sim E_0(1+3\sigma_E)$  which is “assumed” here
- Longitudinal effects and phase jitter
  - Some result established in earlier work [D. Schulte]
  - On-going work
- Background and halo simulations
  - On-going work by I. Ahmed

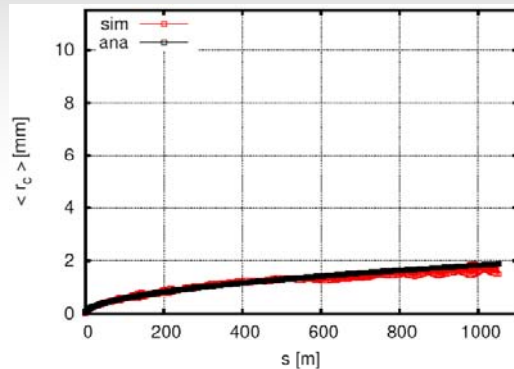


# Effect of quadrupole kicks

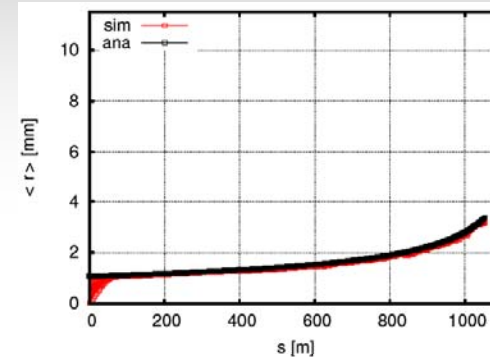
- Random kicks from offset quads increase the centroid envelope as  $\sqrt{N_{\text{quad}}}$
- For a FODO lattice without PETS the contribution would have been  $r_c \approx 2$  mm for quad offsets of  $20 \mu\text{m}$

**quad kicks alone (lowest E drives r)**

$$\frac{\sigma_{\text{quad}}}{\cos(\mu_{\text{cell}}/2)} 2\sqrt{2N_{\text{cell}}}$$



" × "

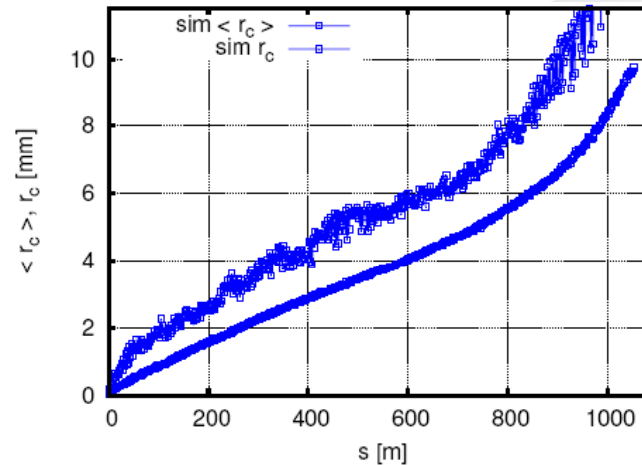


**adiabatic undamping (lowest E drives r)**

$$\approx 3\sqrt{2L_{\text{cell}}\epsilon_N/\gamma f}$$

- However, the combined effect of quadrupole kicks and the adiabatic undamping leads to a quickly increasing beam envelope:

=



**quad kicks + adiabatic undamping**

*Thus: quadrupole kicks + ad. undamping alone drives the beam envelope above our limit (perhaps a bit surprisingly)*



# Decelerator: conclusions

- Simulations gives **reasonable confidence for minimum-loss transport of the decelerator beam**
- **Beam-Based Alignment is needed**, and **Dispersion-Free Steering** seems to be an excellent alternative
- Dispersion-Free Steering comes almost "**for free**" with the use of delayed switching
- **Tune-up procedures** must be applied
- Simulations need to be benchmarked and technology needs to be proven: **TBTS and TBL**

Tolerance	Value	Comment
PETS offset	100 $\mu\text{m}$	$r_c < 1 \text{ mm}$ fulfilled
PETS angles	$\sim 1 \text{ mrad}$	$r_c < 1 \text{ mm}$ fulfilled
Quad angles	$\sim 1 \text{ mrad}$	$r_c < 1 \text{ mm}$ fulfilled
Quad offset	20 $\mu\text{m}$	Must be as small as possible to be able to transport alignment beam
BPM accuracy (incl. static misalignment and elec. error)	20 $\mu\text{m}$	Must be as small as possible to be able to do initial correction
BPM precision (diff. measurement)	$\sim 2 \mu\text{m}$	Allows efficient suppression envelope growth due to dispersive trajectories

**Static tolerances**

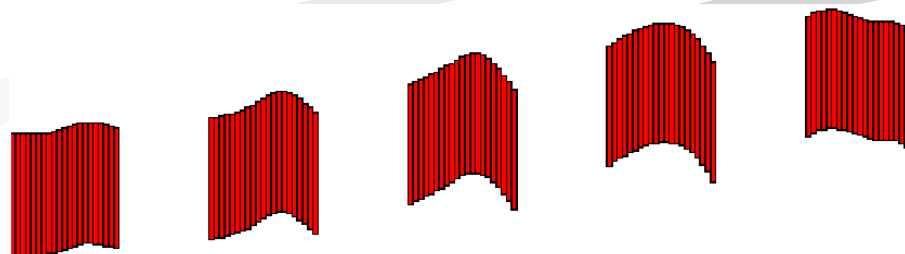
Tolerance	Value	Comment
Quadrupole position jitter	1 $\mu\text{m}$	$r/r_0 < 5 \%$
Quadrupole field ripple	$1 \cdot 10^{-3}$	$r/r_0 < 5 \%$
Current jitter	$< 1\%$	Stability req. only – RF power constraints might be tighter.
Beta mismatch, $d\beta/\beta$	10 %	$r/r_0 < 5 \%$

**Dynamic tolerances**



# Baseline parameters for this study

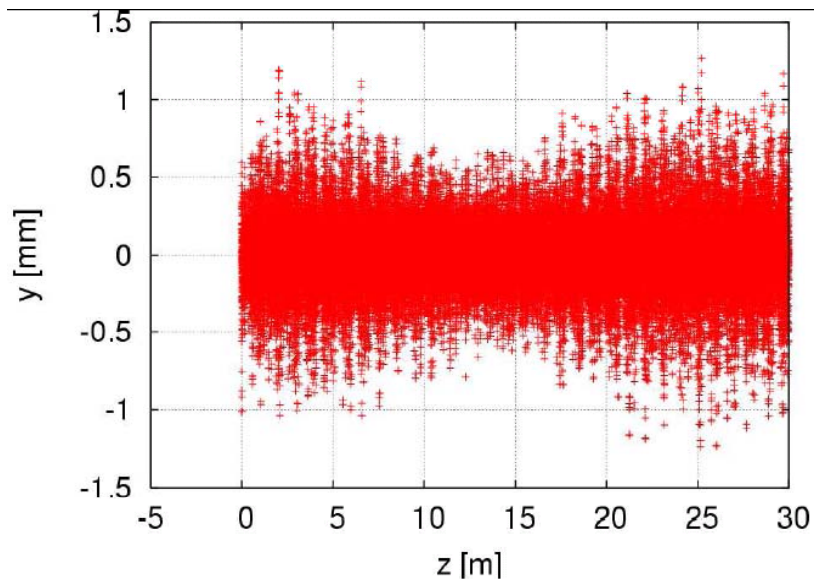
- **Baseline parameters [CLIC parameters 2008]**
  - **$E_0 = 2.4 \text{ GeV}$** 
    - $\sigma_E=0$  in most simulations (see later slide for more on  $\sigma_E$ )
  - **$I = 101 \text{ A}$**
  - $f_b = 12 \text{ GHz}$  (bunch spacing  $d = 25 \text{ mm}$ )
  - $t \approx 240 \text{ ns}$  (2900 bunches)
  - Gaussian bunch,  $\sigma_z = 1 \text{ mm}$
  - $\varepsilon_{Nx,y} \approx 150 \mu\text{m} \rightarrow \sigma_{x,y} \approx \mathbf{0.3 \text{ mm}}$  at  $\beta_{\text{max}} = 3.4 \text{ m}$
  - **Half-aperture:  $a_0=11.5 \text{ mm}$**  (driven by PETS)
- **Simulation tool: PLACET (D. Schulte)**
  - Sliced beam model:
    - bunch divided into slices with individual  $(z, E)$
    - each slice: transverse distribution
    - BPM, Quad and PETS elements



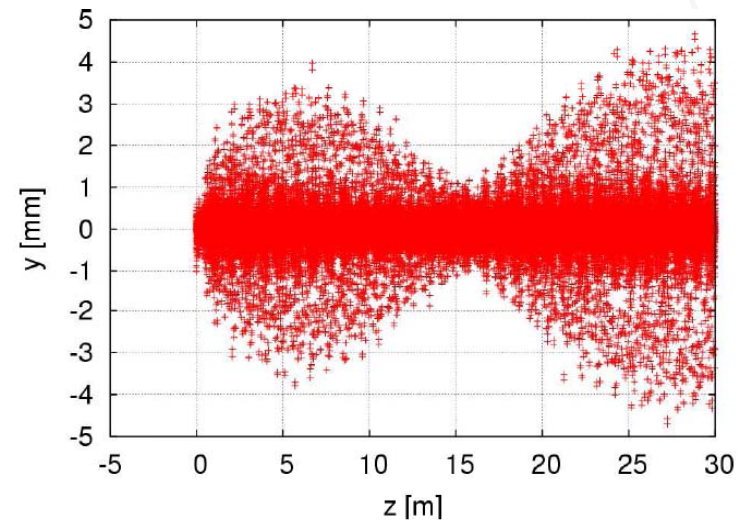


# Instabilities along the beam

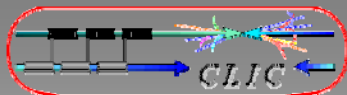
- NB: Q-factor larger than the nominal increase multi-bunch wake and might lead to instability growing along the beam
- Here illustrated for  $Q=Q_0$  and  $Q=2Q_0$
- Deemed unacceptable (even if centroid  $r_c$  envelope is constrained)



$Q=Q_0$



$Q=2Q_0$



# Dispersion-free steering

- 1-to-1 correction does not give an adequate steering due to the large variation of dispersive trajectories, we therefore seek to minimize the dispersive trajectories by applying Dispersion-Free Steering (DFS), [Raubenheimer and Ruth, 1991]

- Our implementation uses response matrices to minimize:

$$\chi^2 = w_0 \Sigma y_{0,i}^2 + w_1 \Sigma (y_{1,i} - y_{0,i})^2$$

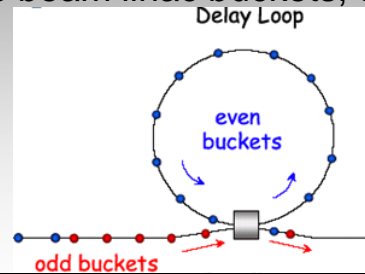
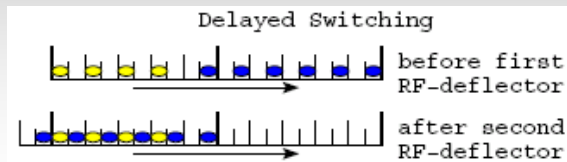
- We need a test-beam that generates a difference trajectory with large energy leverage
  - however: higher energy beam not available and lower energy beam will not be stable (with the same focusing)
- Instead we take advantage of the PETS → reduced current, in form of empty buckets, can be used to generate generate a test beams with different energy





# DFS: test-beam generation

- By adjusting the switching of the drive beam linac buckets, one can generate the test-beam in the same pulse as the nominal beam

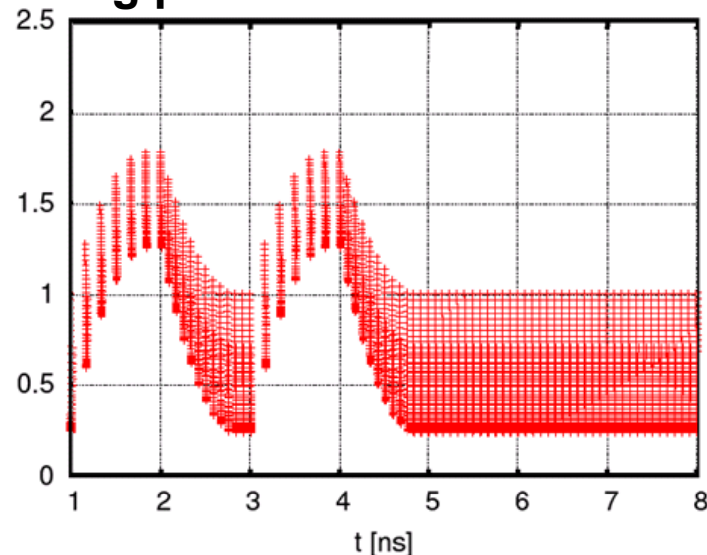


**Example of DFS beam generation scheme:**

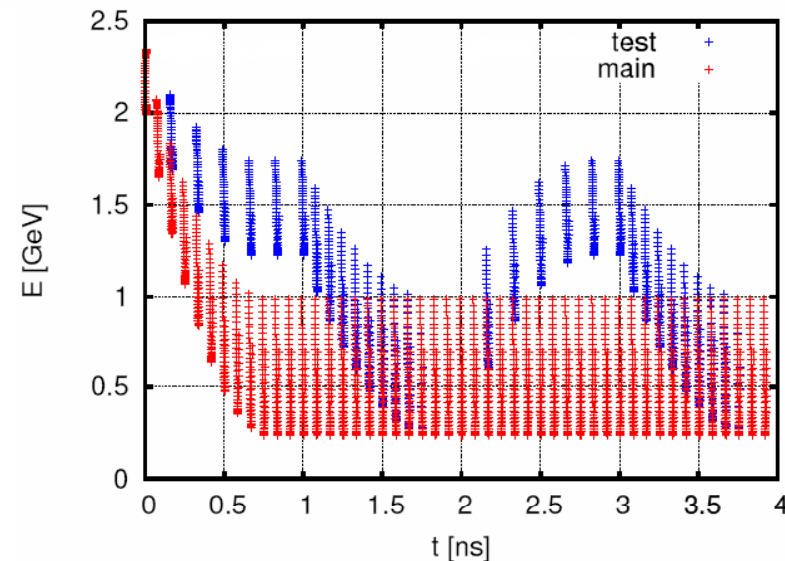
Of the 12 initial E+O pulses:

- First 3: nominal E+O recombination
- Next 3: Delay switching to ~half of O buckets
- Next 3: nominal
- Last 3: Delay switching

## Resulting pattern:



Test-beam and nominal beam in the same pulse



Test-beam energy compared to nominal beam

## Advantages with this method :

- quadrupole strengths are kept constant – **machine unchanged**
- main-beam and test-beam can be combined **in one pulse**
- Large energy-leverage

( The example scheme above might not be optimal wrt. BPM readings → to be investigated further )