

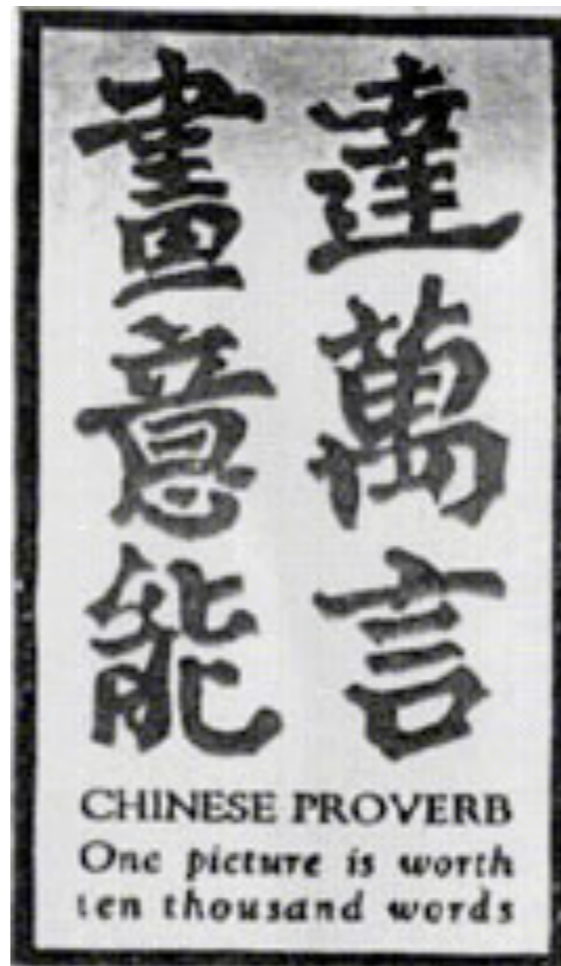
# A Visual Analytics approach for process analysis

# Why visualization?



# Why Visualization?

“A picture is worth a thousand words”



Fred R. Barnard

*Printers' Ink.* December  
8, 1921

# Why Visualization?

"Un bon croquis vaut mieux qu'un long discours"

Napoleon Bonaparte

"A picture shows me at a glance  
what it takes dozens of pages of a book to expound."

Russian writer Ivan Turgenev  
(in *Fathers and Sons* in 1862)

# Why Visualization?

I *see* it...

It is very *clear*

*Show* me why...

She *unveiled*  
the mystery

This *sheds* some *light*  
to the problem

This author is a  
*visionary*

Their explanation  
was rather *obscure*

He always says the truth:  
he is very *transparent* kid

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## IN-SIGHT

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# Why Visualization?

**40+ %** of the brain  
dedicated to **visual tasks**

How many “sevens” do you find?

1093840192384901834093281481083459830985560984095809456894  
0680946804986049860458094802943209385029348509898690285096  
7890956890456809348560394563956034560584560935050358609358  
6904690586034870909289091001012948019238401983401923109234  
0480923489043859023850923896508309683098670395860394586039  
4860934869034586093860938093468093458038034680934568039458  
6034560386034563945839586358568039539568309458038505609568  
0349568345809358045860958603758609458603583405684305680349  
5680395680395840958034860394680938609348609685309456039465  
0439580349758603496093458620943580281039803481894104391092

Please, count...

# Why Visualization?

How many “sevens” do you find?

1093840192384901834093281481083459830985560984095809456894  
0680946804986049860458094802943209385029348509898690285096  
**7**890956890456809348560394563956034560584560935050358609358  
69046905860348**7**0909289091001012948019238401983401923109234  
04809234890438590238509238965083096830986**7**0395860394586039  
4860934869034586093860938093468093458038034680934568039458  
6034560386034563945839586358568039539568309458038505609568  
0349568345809358045860958603**7**58609458603583405684305680349  
5680395680395840958034860394680938609348609685309456039465  
0439580349**7**58603496093458620943580281039803481894104391092

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**7**890956890456809348560394563956034560584560935050358609358  
69046905860348**7**0909289091001012948019238401983401923109234  
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4860934869034586093860938093468093458038034680934568039458  
6034560386034563945839586358568039539568309458038505609568  
0349568345809358045860958603**7**58609458603583405684305680349  
5680395680395840958034860394680938609348609685309456039465  
0439580349**7**58603496093458620943580281039803481894104391092

Visualization provides “*context*”

location, cadence, patterns, proportion, ...

subtle forms of knowledge are combined

connected knowledge = more knowledge !!



# Why Visualization?

are these data random?

what are the most repeated “xy” patterns?

1093840192384901834093281481083459830985560984095809456894  
0680946804986049860458094802943209385029348509898690285096  
7890956890456809348560394563956034560584560935050358609358  
6904690586034870909289091001012948019238401983401923109234  
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5680395680395840958034860394680938609348609685309456039465  
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# Why Visualization?

most repeated “xy” patterns?

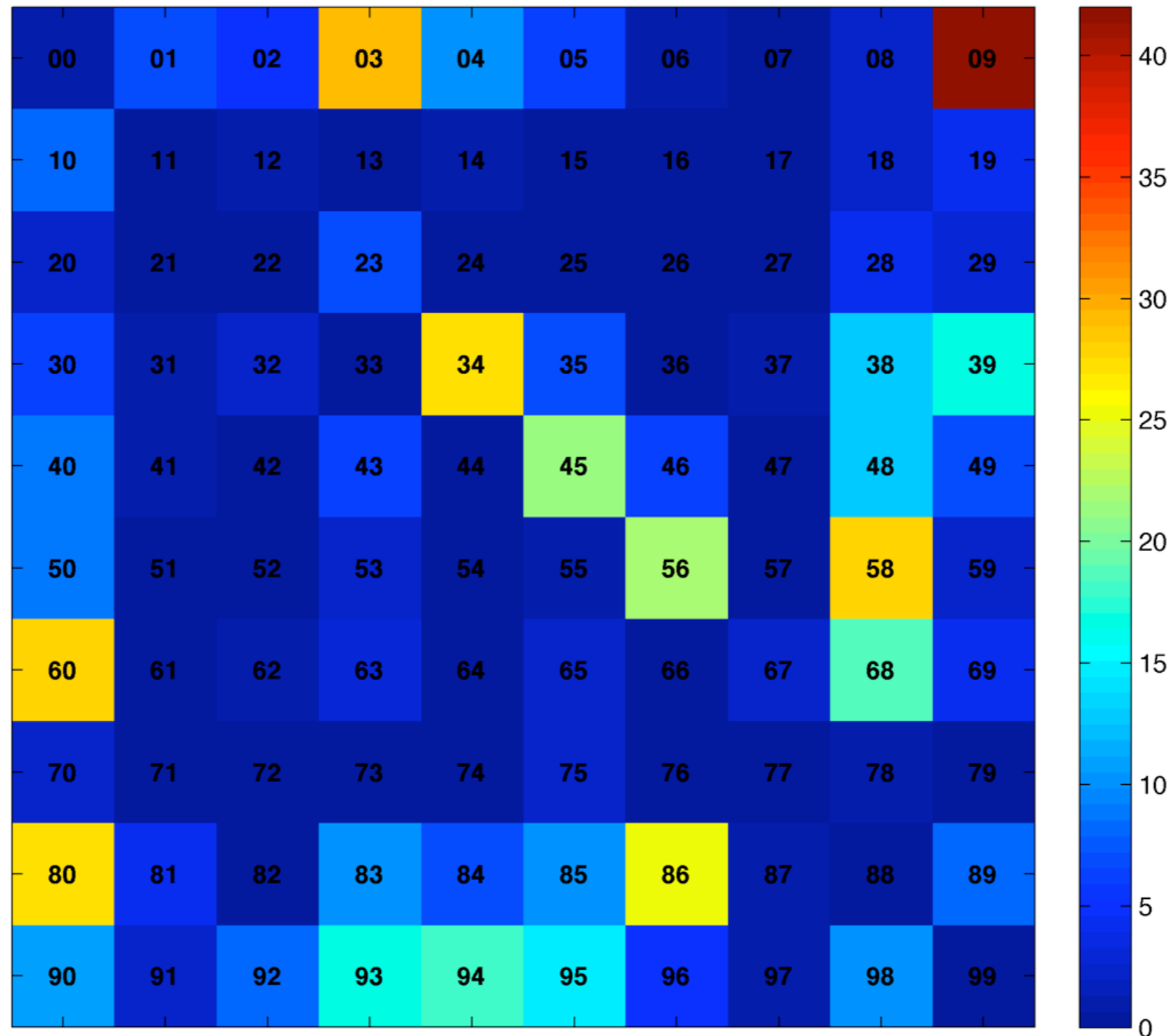
1**09**3840192384901834**09**328148108345983**09**8556**09**84**09**58**09**456894  
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789**09**568904568**09**34856039456395603456058456**09**350503586**09**358  
690469058603487**0909**289**09**10010129480192384019834019231**09**234  
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03495683458**09**35804586**09**586037586**09**458603583405684305680349  
568039568039584**09**5803486039468**09**386**09**3486**09**6853**09**456039465  
0439580349758603496**09**345862**09**43580281039803481894104391**09**2

# Why Visualization?

## second most repeated “xy” patterns

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0680946804986049860458094802943209385029348509898690285096  
789095689045680934856**03**94563956**03**456058456093505**03**58609358  
6904690586**03**4870909289091001012948019238401983401923109234  
048092348904385902385092389650830968309867**03**9586**03**94586**03**9  
4860934869**03**4586093860938093468093458**03**8**03**4680934568**03**9458  
6**03**456**03**86**03**4563945839586358568**03**9539568309458**03**8505609568  
**03**495683458093580458609586**03**7586094586**03**58340568430568**03**49  
568**03**9568**03**95840958**03**486**03**94680938609348609685309456**03**9465  
043958**03**497586**03**496093458620943580281**03**98**03**481894104391092

visual histogram of “xy” patterns?



# Statistics sometimes mislead

## Ancombe's quartet

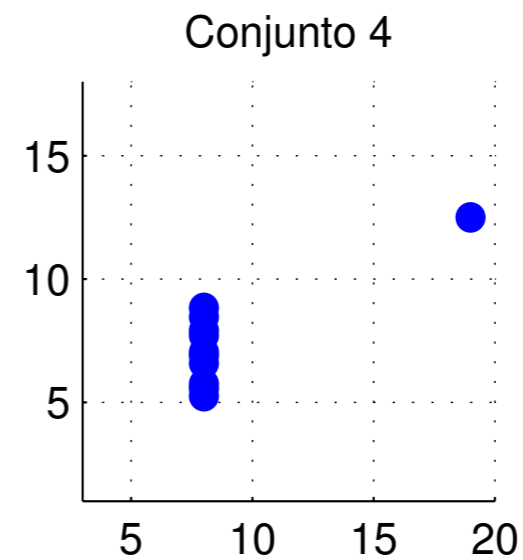
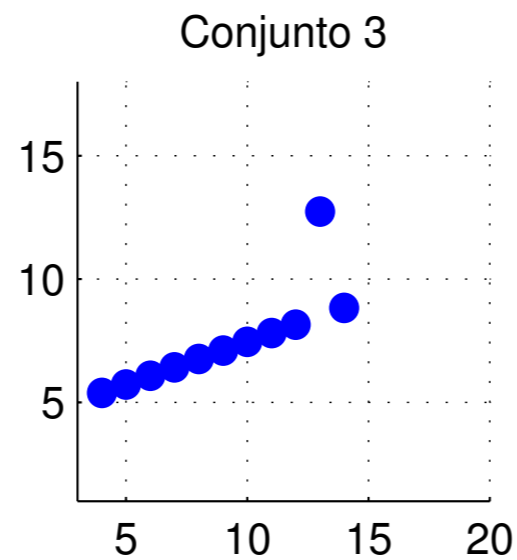
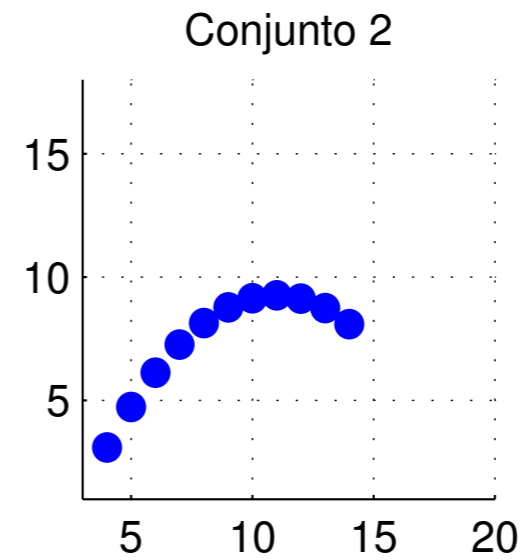
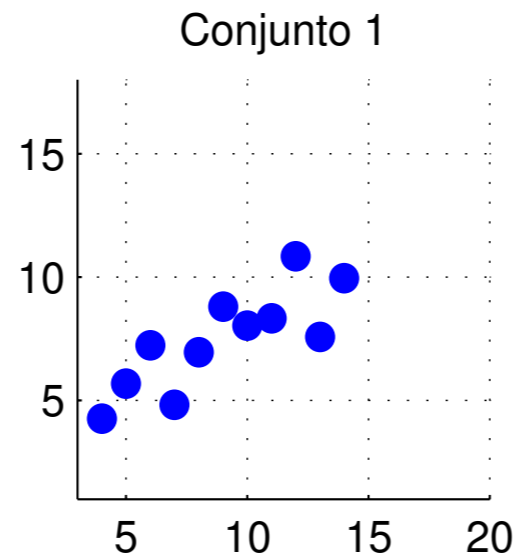
```
clear;
close all;

% Datos del cuarteto Ancombe (http://en.wikipedia.org/wiki/Ancombe's\_quartet)
p = [10.0 8.04 10.0 9.14 10.0 7.46 8.0 6.58
     8.0 6.95 8.0 8.14 8.0 6.77 8.0 5.76
     13.0 7.58 13.0 8.74 13.0 12.74 8.0 7.71
     9.0 8.81 9.0 8.77 9.0 7.11 8.0 8.84
     11.0 8.33 11.0 9.26 11.0 7.81 8.0 8.47
     14.0 9.96 14.0 8.10 14.0 8.84 8.0 7.04
     6.0 7.24 6.0 6.13 6.0 6.08 8.0 5.25
     4.0 4.26 4.0 3.10 4.0 5.39 19.0 12.50
     12.0 10.84 12.0 9.13 12.0 8.15 8.0 5.56
     7.0 4.82 7.0 7.26 7.0 6.42 8.0 7.91
     5.0 5.68 5.0 4.74 5.0 5.73 8.0 6.89];

% Separamos los cuatro conjuntos
x{1} = p(:,1:2);
x{2} = p(:,3:4);
x{3} = p(:,5:6);
x{4} = p(:,7:8);

figure(1);
clf;

for k = 1:4,
    subplot(2,2,k);
    scatter(x{k}(:,1),x{k}(:,2),50,'filled');
    axis equal;
    axis([3 20 1 18]);
    grid on;
    C{k} = cov(x{k}),
    M{k} = mean(x{k}),
    R{k} = corrcoef(x{k}),
    title(sprintf('Conjunto %d',k));
end
```



¡The 4 sets have the same statistic descriptors!

### Covariance Matrices

```
>> for k = 1:4, C{k}, end;
ans =
    11.0000    5.5010
    5.5010    4.1273

ans =
    11.0000    5.5000
    5.5000    4.1276

ans =
    11.0000    5.4970
    5.4970    4.1226

ans =
    11.0000    5.4990
    5.4990    4.1232
```

### Mean vectors

```
>> for k = 1:4, M{k}, end;
ans =
    9.0000    7.5009

ans =
    9.0000    7.5009

ans =
    9.0000    7.5000

ans =
    9.0000    7.5009
```

## Industrial systems also pose a big data problem

- Huge amounts of data
  - Many sensors
  - Ubiquitous information
  - Heterogeneous information
- Complex systems
  - Dynamic behavior
  - Connected, interacting, coupled...
  - Many variables, multiway problems
  - Human factors
  - Interaction with other factories

## Problem:

Get insight  
from an ocean of data

Detect structure in data  
and model it

### References:

*Big data: The next frontier for innovation, competition, and productivity.*

[http://www.mckinsey.com/insights/business\\_technology/big\\_data\\_the\\_next\\_frontier\\_for\\_innovation](http://www.mckinsey.com/insights/business_technology/big_data_the_next_frontier_for_innovation).



## VISUAL EXPLORATION *of* LARGE DATA SETS

Computer systems today store vast amounts of data. Researchers, including those working on the “How Much Information?” project at the University of California, Berkeley, recently estimated, about 1 exabyte (1 million terabytes) of data is generated annually worldwide, including 99.997% available only in digital form. This worldwide data deluge means that in the next three years, more data will be generated than during all previous human history.

Data is often recorded, captured, and stored automatically via sensors and monitoring systems. Many of the simple transactions now part of our everyday lives, such as paying for food and clothes by credit card or using the telephone, are typically recorded for future reference by computers. Many parameters of each transaction are routinely captured, resulting in highly dimensional data. The data is collected because companies, including those engaged in some kind of e-commerce, view it as a source of potentially valuable information that, as a strategic asset, could provide a competitive advantage. But actually finding this valuable information is difficult. Today’s data management systems make it possible to view only small portions of it. If the data is presented in text form, the amount that can be displayed amounts to only about 100 data items—a drop in the ocean when dealing with data sets containing millions of data items. Lacking the ability to adequately explore the large amounts being collected, and despite its potential usefulness, the data

*In the rising tide of business transaction data, these tools help distinguish which are strategic assets and which are not worth collecting in the first place.*

*Daniel A. Keim*

becomes useless and the databases data dumps. Visual data exploration, which aims to provide insight by visualizing the data, and information visualization techniques (such as distorted overview displays and dense pixel displays) can help solve this problem.

Effective data mining depends on having a human in the data exploration process while combining this person’s flexibility, creativity, and general knowledge with the enormous storage capacity and computational power of today’s computers. Visual data exploration seeks to integrate humans in the data exploration process, applying their perceptual abilities to the large data sets now available. The basic idea is to present the data in some visual form, allowing data analysts to gain insight into it and draw conclusions, as well as interact with it. The visual representation of the data reduces the cognitive work needed to perform certain tasks.

Visual data mining techniques have proved their value in exploratory data analysis; they also have great

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**COMMUNICATIONS OF THE ACM** August 2001/Vol. 44, No. 8



# A few Big Data numbers

(according to Mc Kinsey Global Institute report)

**600 \$** cost of a hard disk having space to store  
all the music composed ever

**40%** projected growth in global data  
generated per year

**5%** estimated growth of  
IT spending

[http://www.mckinsey.com/insights/business\\_technology/big\\_data\\_the\\_next\\_frontier\\_for\\_innovation](http://www.mckinsey.com/insights/business_technology/big_data_the_next_frontier_for_innovation)

J. Manyika, M. Chui, B. Brown, J. Bughin, R. Dobbs, C. Roxburgh, and A. H. Byers. Big data: The next frontier for innovation, competition, and productivity. Technical report, McKinsey Global Institute, May 2011.

# A few Big Data numbers

(according to Mc Kinsey Global Institute report)

**60%** potential increase of benefits in retailers' operating margins possible with big data

**300 G\$** potential annual value to USA health care (more than double the total annual health care spending in Spain)

**250 G€** estimated value of big data from EU public administration (more than the greek GDP)

**190k** estimation of highly qualified data analysis experts needed in USA  
+  
**1.5M** estimation of data-savvy managers needed in USA to fully harness big data.

# Visual Analytics

## Data

## Information

## Knowledge

### Process

#### Data acquisition

Advanced sensors  
 Artificial vision  
 Exploitation data  
 Web data (XML, CSV, GeoJSON, etc.)

#### Feature extraction

Frequency analysis (FFT, etc)  
 System Identification  
 Statistical descriptors  
 Geometrical descriptors

#### Intelligent Data Analysis (IDA)

Modeling  
 Prediction  
 Clustering and classification  
 Dimensionality reduction  
 Change/Novelty detection

#### Visualization

Data visualization  
 Interaction mechanisms  
 Interface design  
 Visualization of IDA algorithms

## VISUAL ANALYTICS

Data

Information

Knowledge

**Process**

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**Intelligent Data Analysis (IDA)**

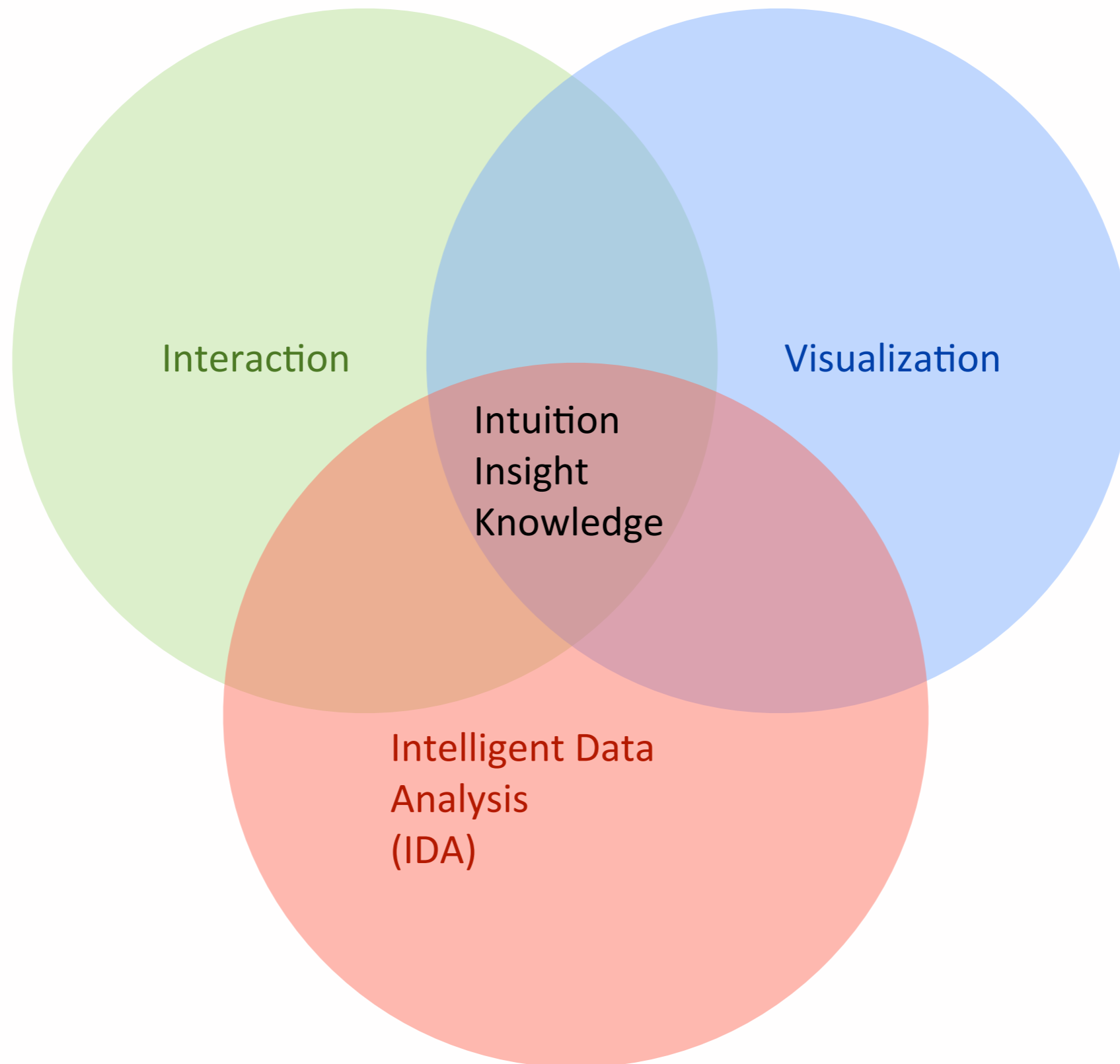
Modeling  
 Prediction  
 Clustering and classification  
 Dimensionality reduction  
 Change/Novelty detection

**Visualization**

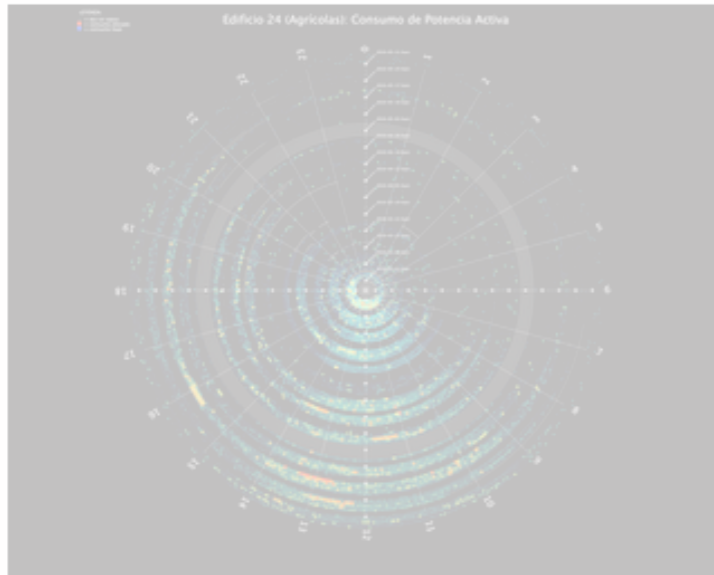
Data visualization  
 Interaction mechanisms  
 Interface design  
 Visualization of IDA algorithms

# Visual Analytics approach

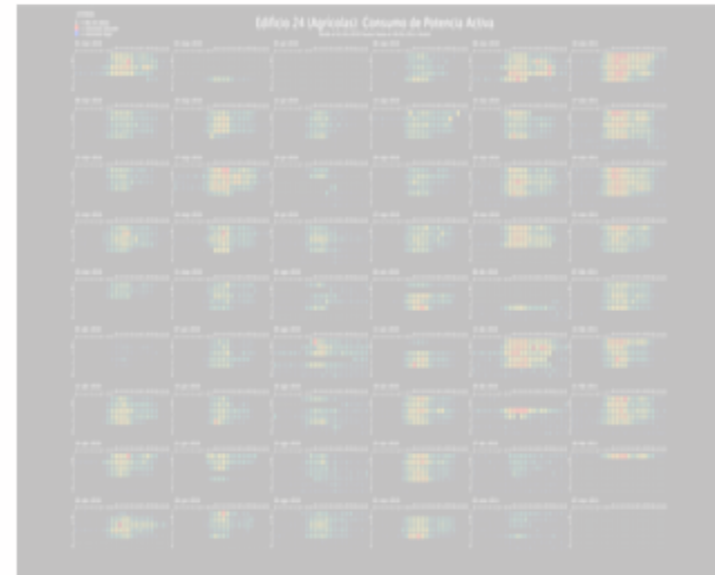
## Human Learning + Machine Learning Synergy



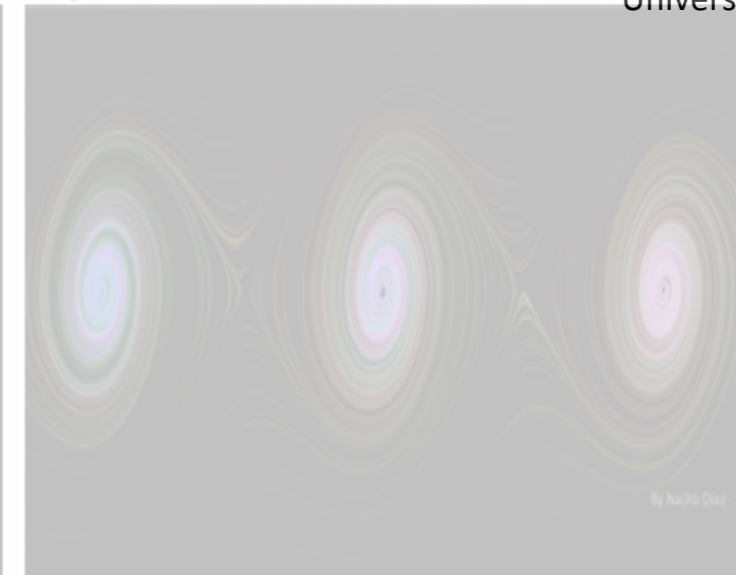
Visualización radial



Visualización calendario

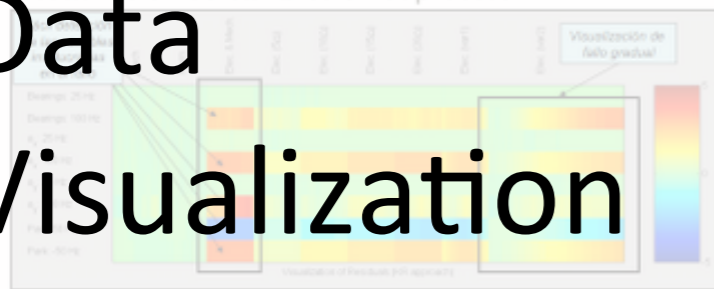


Trayectoria de estados de un sistema dinámico

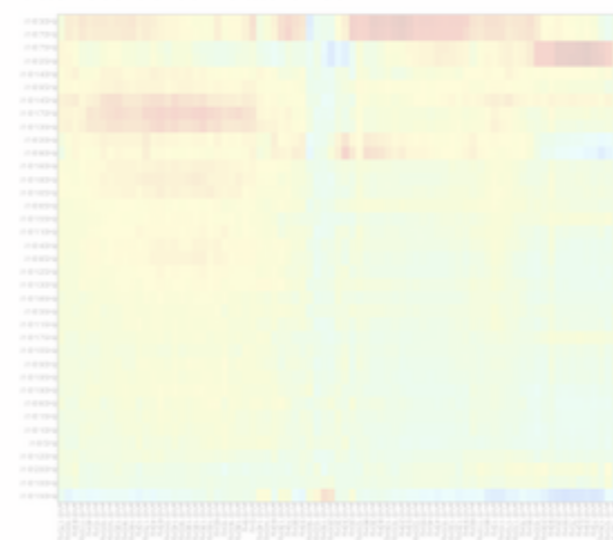


## Data Visualization

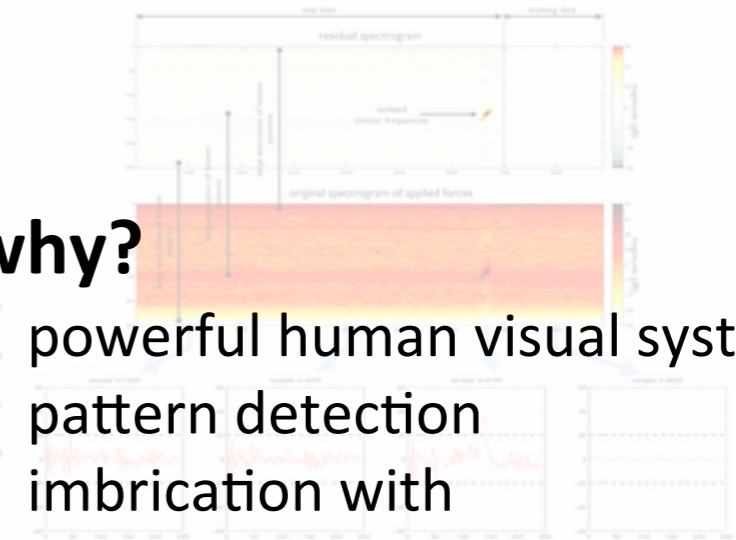
Visualización de cambios en el proceso



Matrices de correlaciones



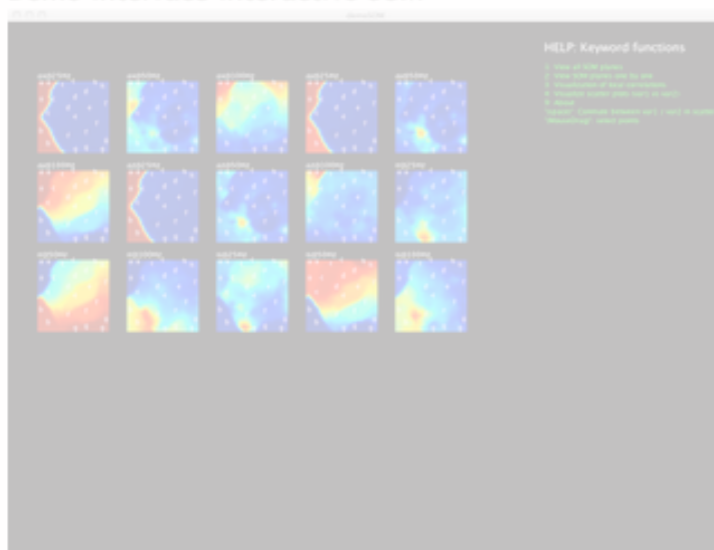
Visualización de cambios en la dinámica



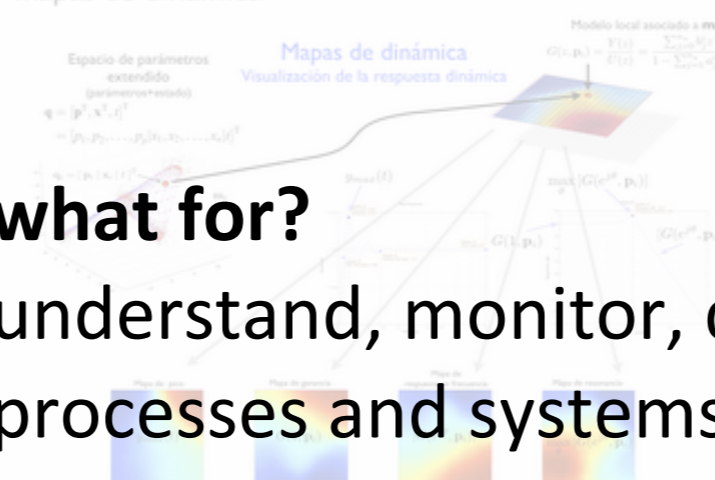
**why?**

- powerful human visual system,
- pattern detection
- imbrication with the cognition process

Demo interface interactivo SOM

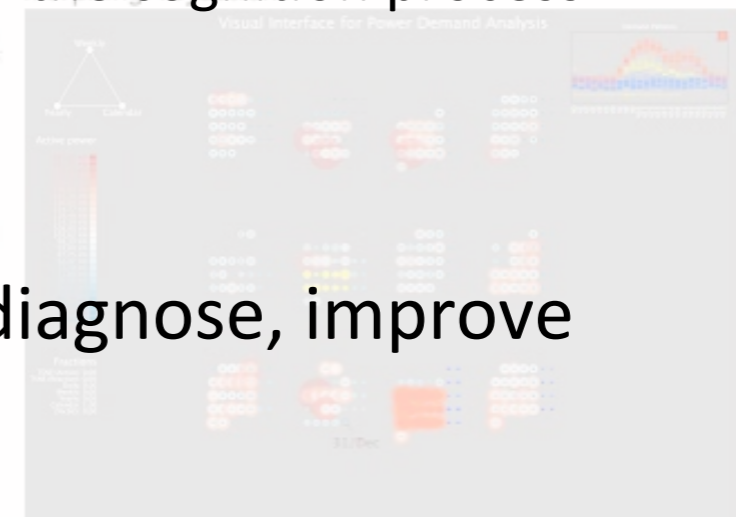


Mapas de dinámica



**what for?**

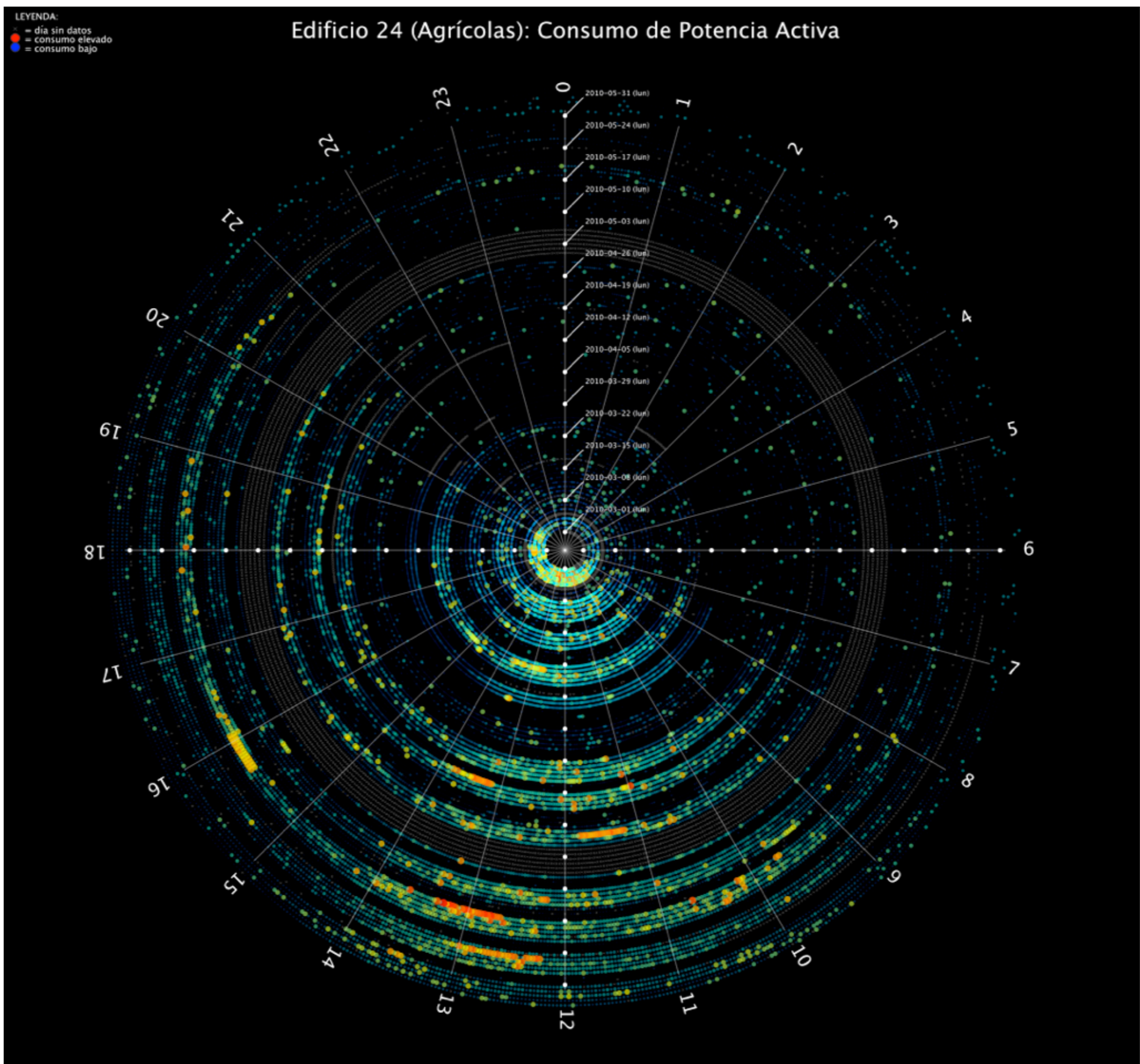
understand, monitor, diagnose, improve processes and systems





# Data visualization

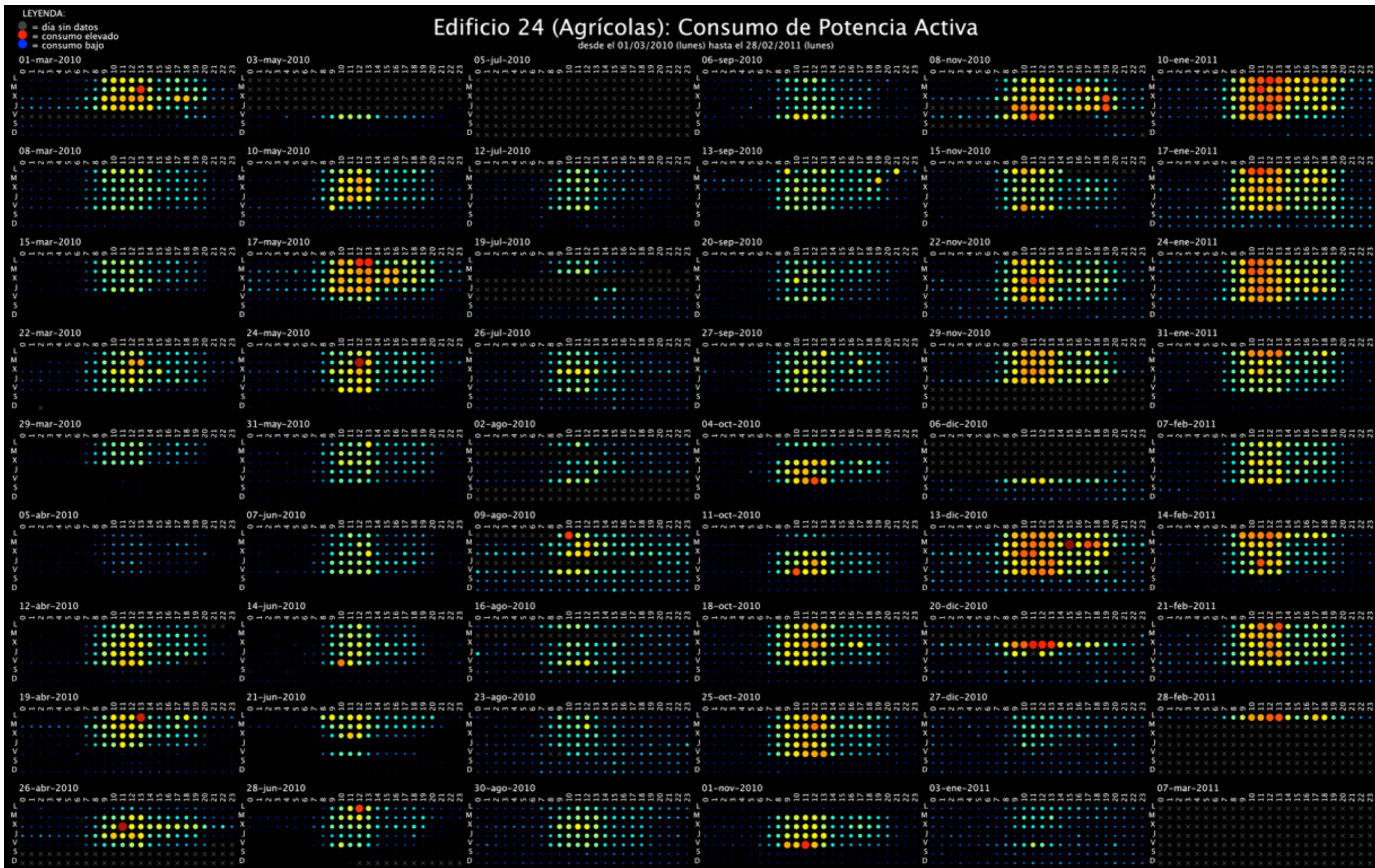
## power demand data visualization (radial)





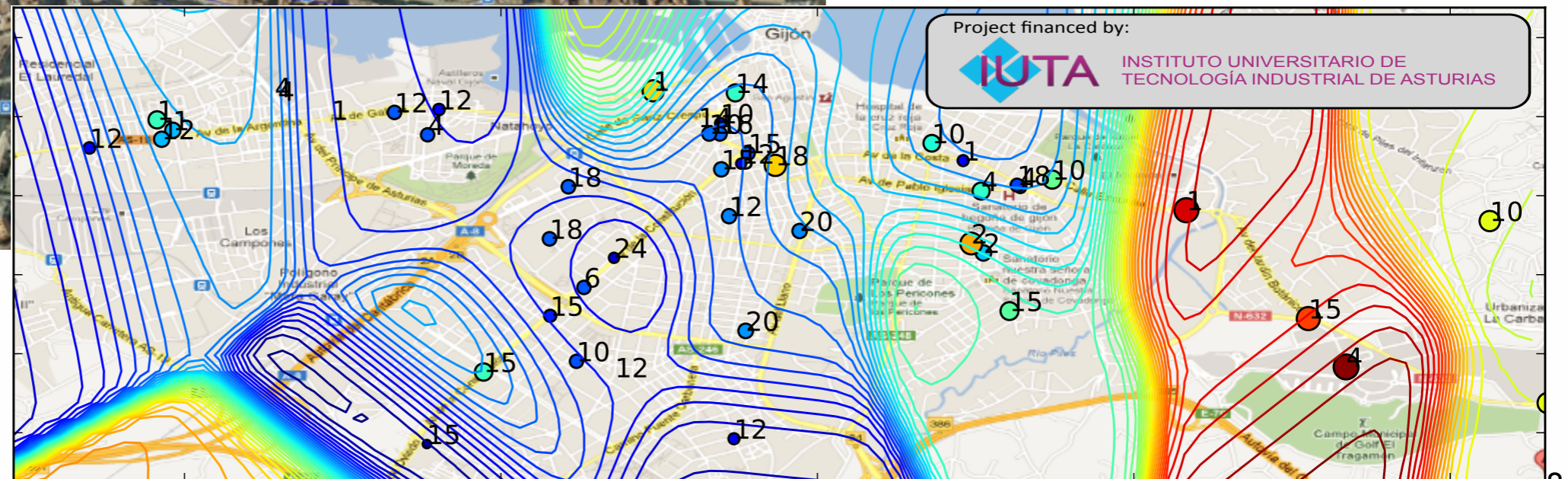
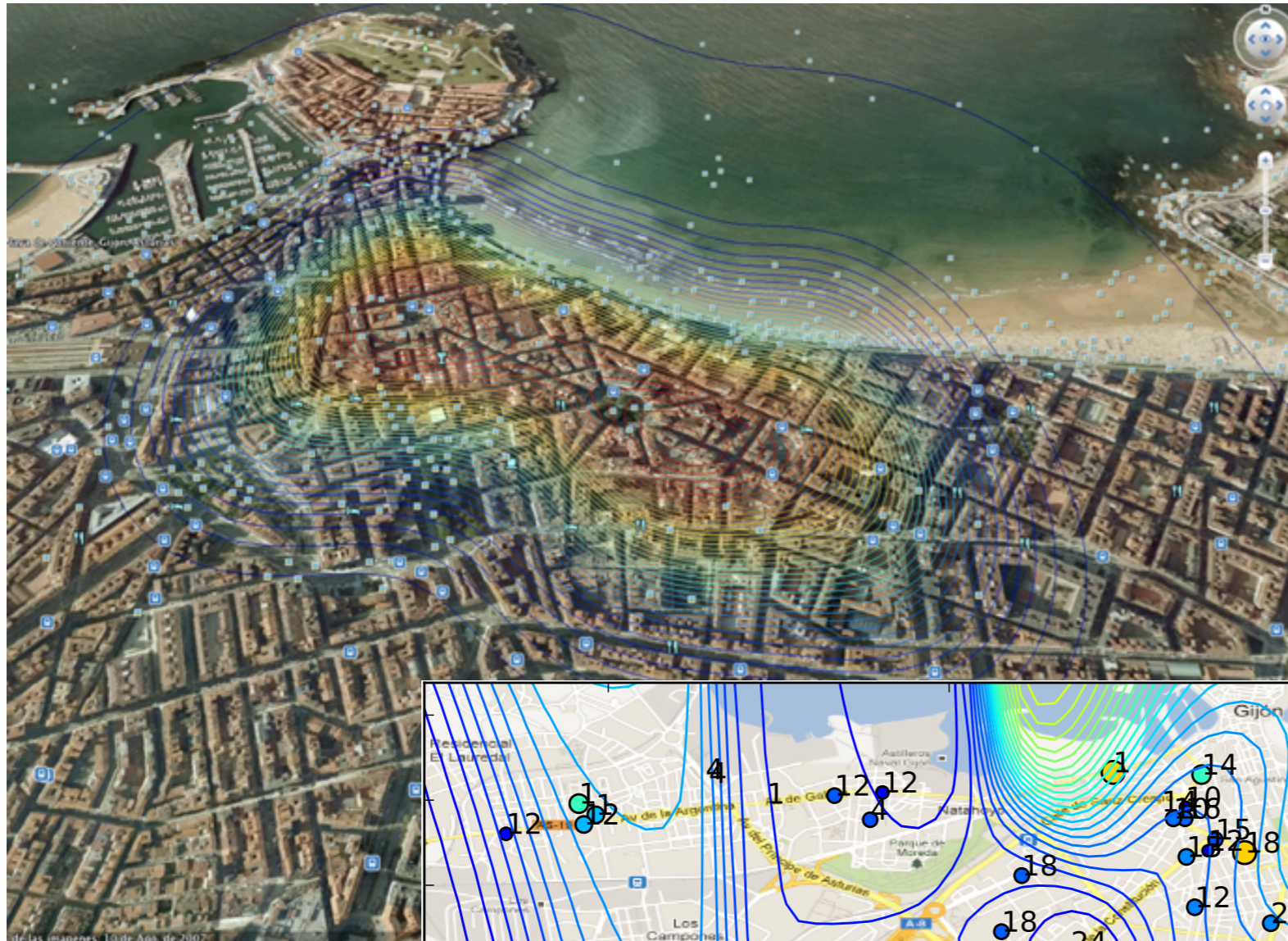
# Data visualization

## power demand data visualization (small-multiples)

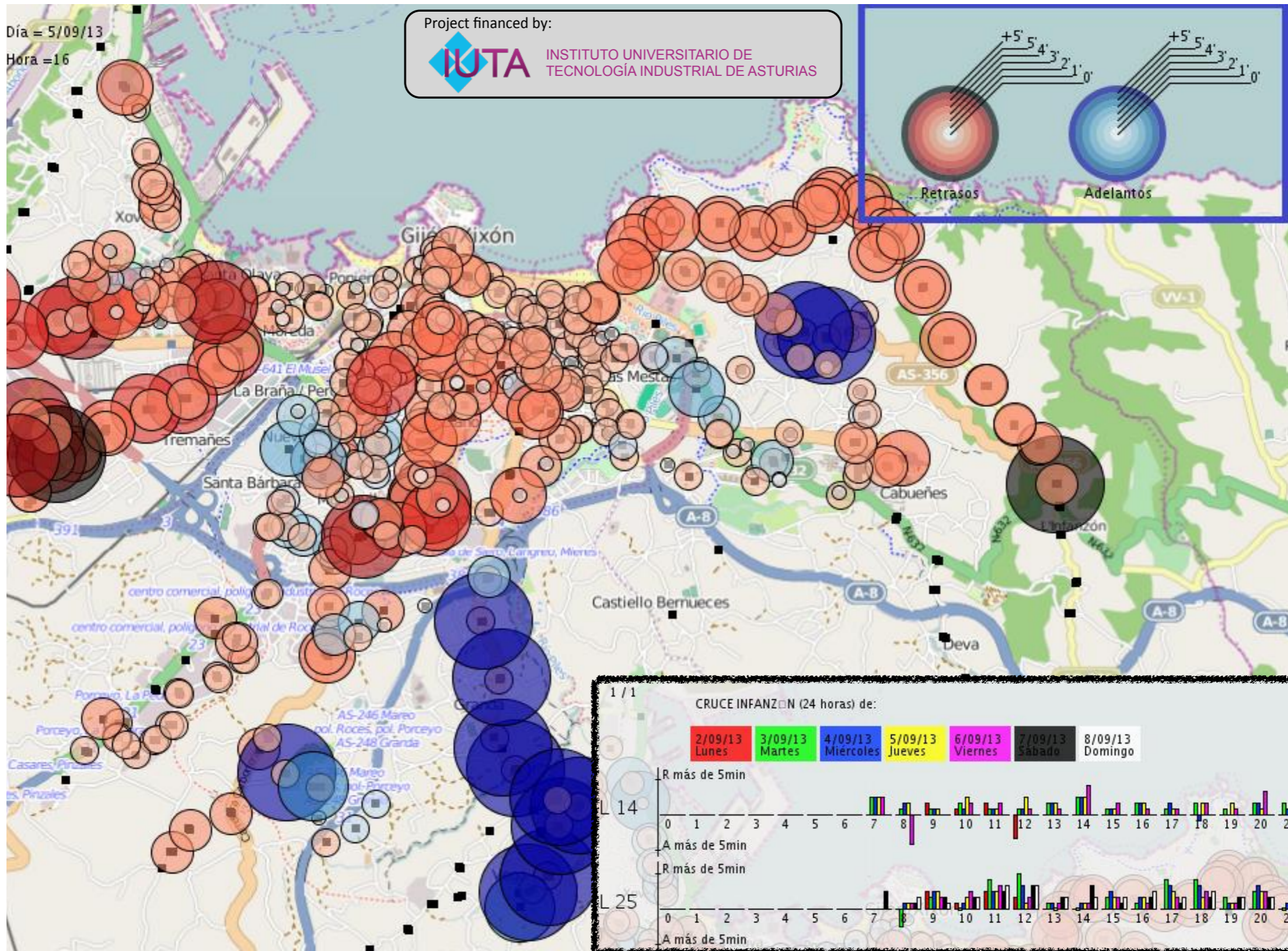




### “Hot spot” visualization from geotagged data









## Manifold learning methods appeared in Science, dec. 2000

- [1] S. T. Roweis and L. K. Saul. Nonlinear dimensionality reduction by locally linear embedding. *Science*, 290:2323–2326, Dec., 22 2000.
- [2] J. B. Tenenbaum, V. de Silva, and J. C. Langford. A global geometric framework for nonlinear dimensionality reduction. *Science*, 290:2319–2323, Dec, 22 2000.

### Nonlinear Dimensionality Reduction by Locally Linear Embedding

Sam T. Roweis<sup>1</sup> and Lawrence K. Saul<sup>2</sup>

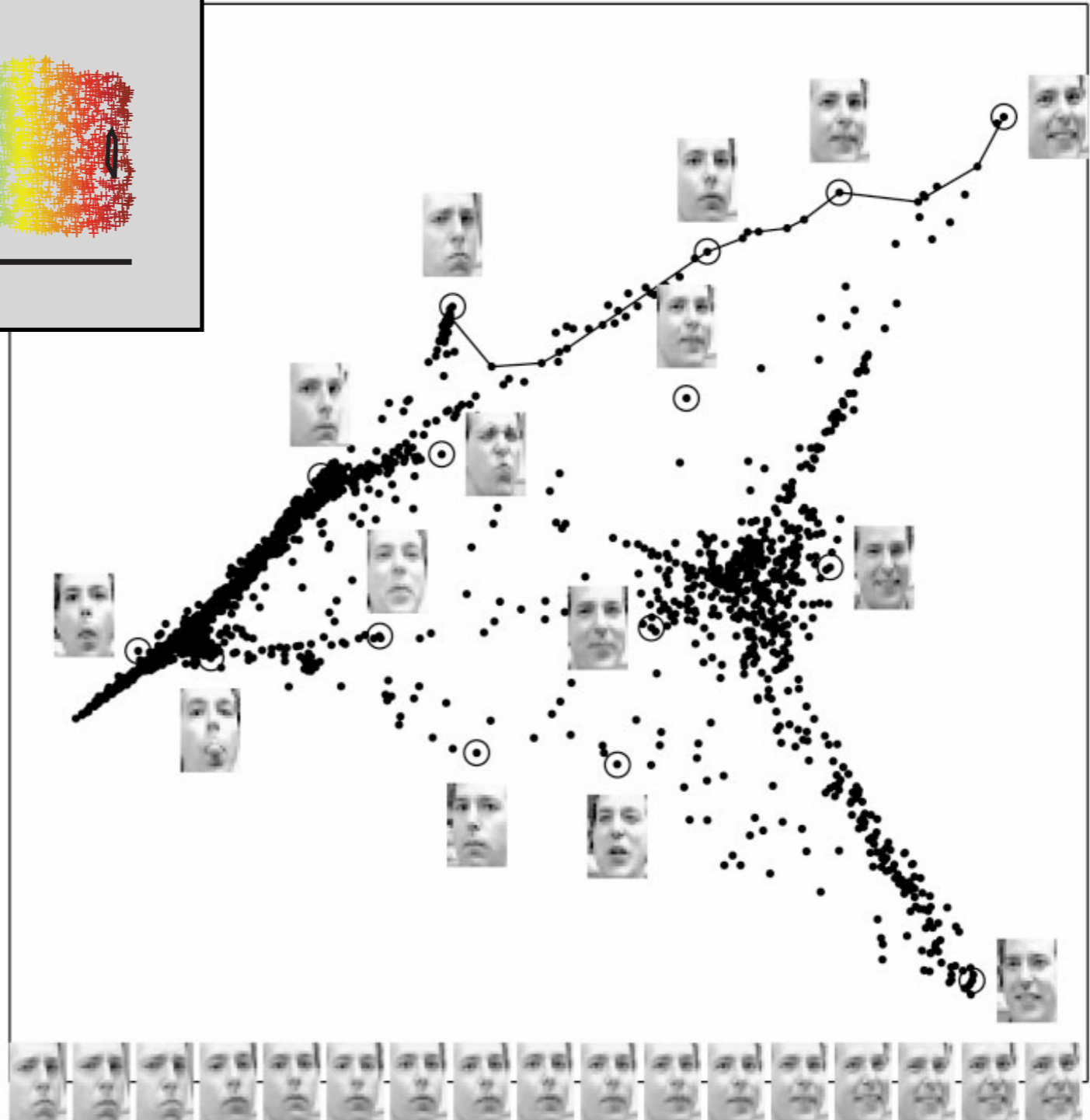
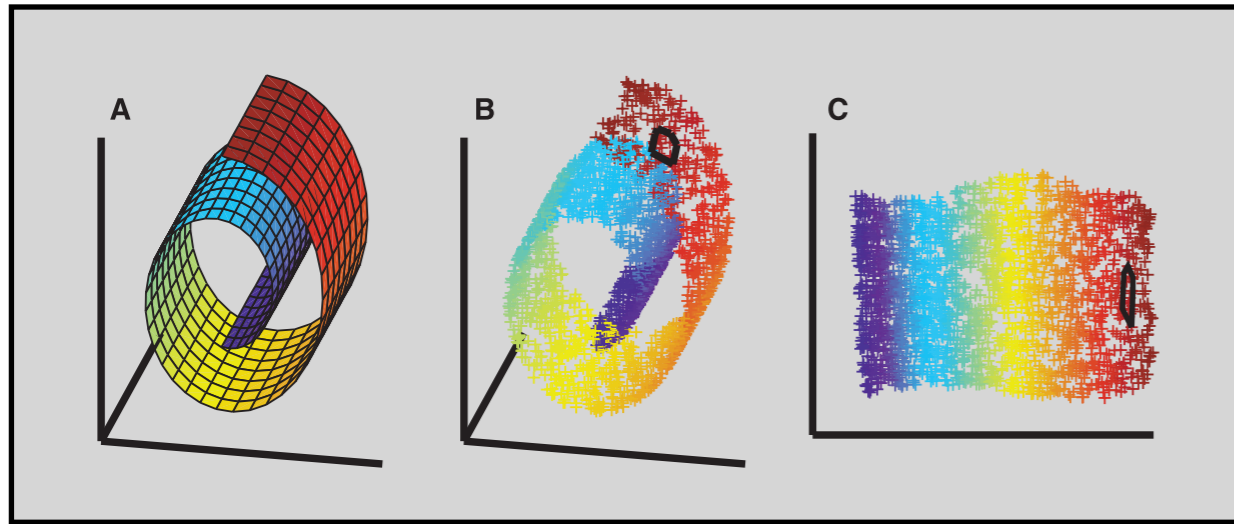
Many areas of science depend on exploratory data analysis and visualization. The need to analyze large amounts of multivariate data raises the fundamental problem of dimensionality reduction: how to discover compact representations of high-dimensional data. Here, we introduce locally linear embedding (LLE), an unsupervised learning algorithm that computes low-dimensional, neighborhood-preserving embeddings of high-dimensional inputs. Unlike clustering methods for local dimensionality reduction, LLE maps its inputs into a single global coordinate system of lower dimensionality, and its optimizations do not involve local minima. By exploiting the local symmetries of linear reconstructions, LLE is able to learn the global structure of nonlinear manifolds, such as those generated by images of faces or documents of text.

### A Global Geometric Framework for Nonlinear Dimensionality Reduction

Joshua B. Tenenbaum,<sup>1\*</sup> Vin de Silva,<sup>2</sup> John C. Langford<sup>3</sup>

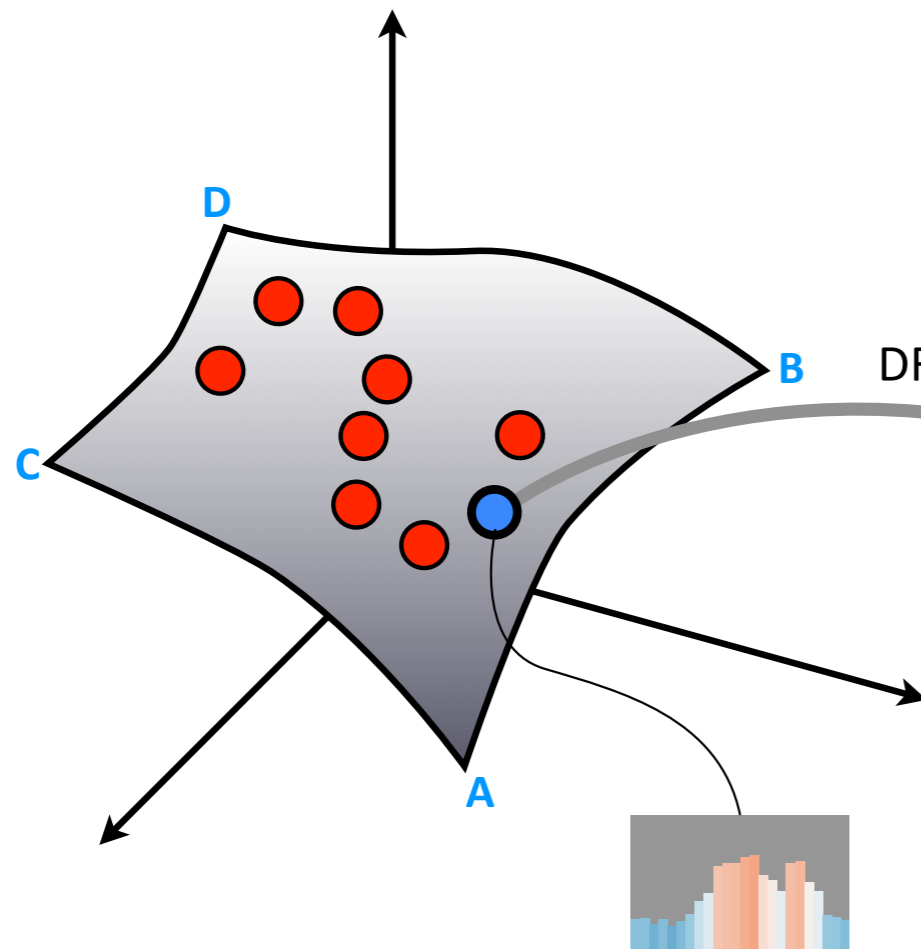
Scientists working with large volumes of high-dimensional data, such as global climate patterns, stellar spectra, or human gene distributions, regularly confront the problem of dimensionality reduction: finding meaningful low-dimensional structures hidden in their high-dimensional observations. The human brain confronts the same problem in everyday perception, extracting from its high-dimensional sensory inputs—30,000 auditory nerve fibers or  $10^6$  optic nerve fibers—a manageably small number of perceptually relevant features. Here we describe an approach to solving dimensionality reduction problems that uses easily measured local metric information to learn the underlying global geometry of a data set. Unlike classical techniques such as principal component analysis (PCA) and multidimensional scaling (MDS), our approach is capable of discovering the nonlinear degrees of freedom that underlie complex natural observations, such as human handwriting or images of a face under different viewing conditions. In contrast to previous algorithms for nonlinear dimensionality reduction, ours efficiently computes a globally optimal solution, and, for an important class of data manifolds, is guaranteed to converge asymptotically to the true structure.

# Dimensionality Reduction

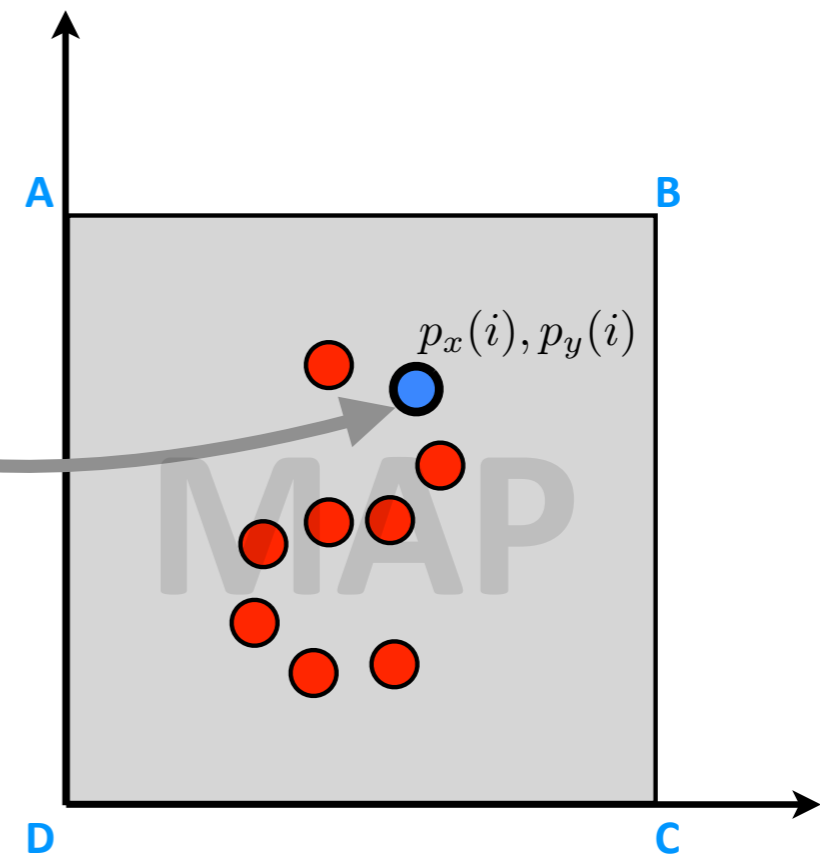


Source:  
(Roweis et al., 2000)

high dimensional space of  
 Feature vectors



2D space  
 for visualization

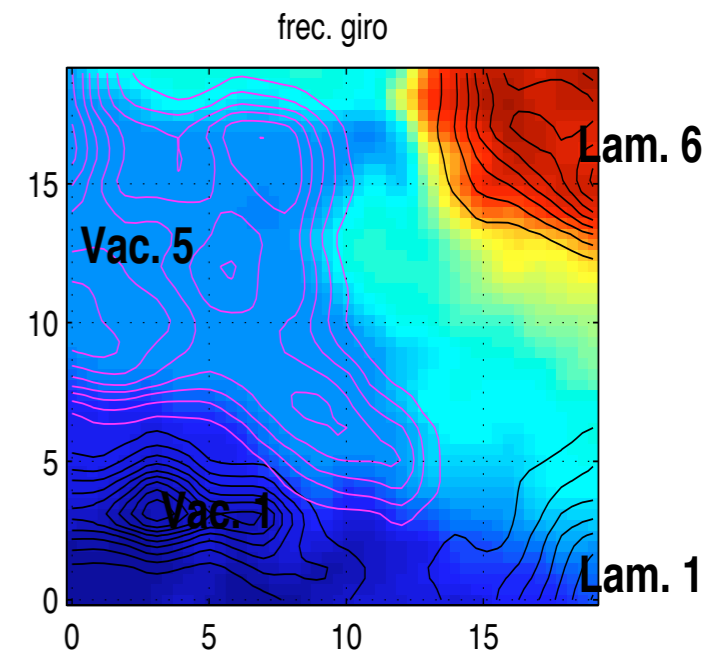
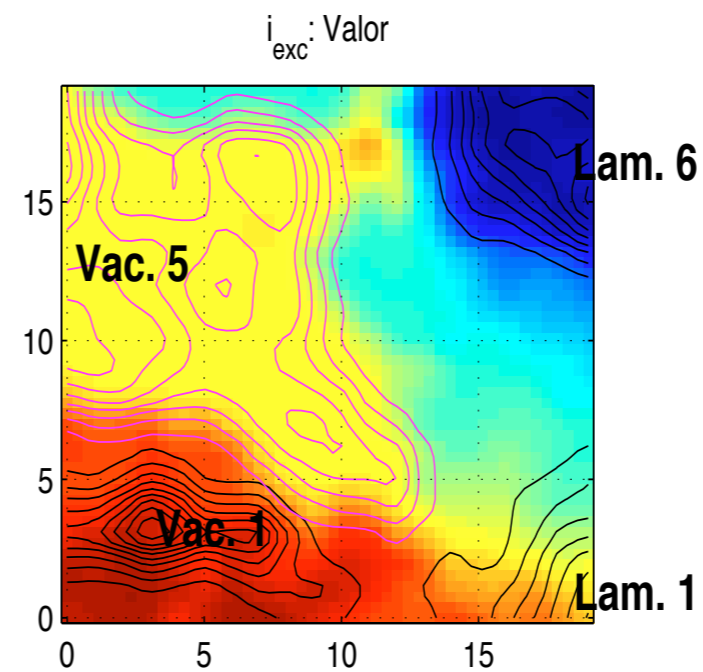
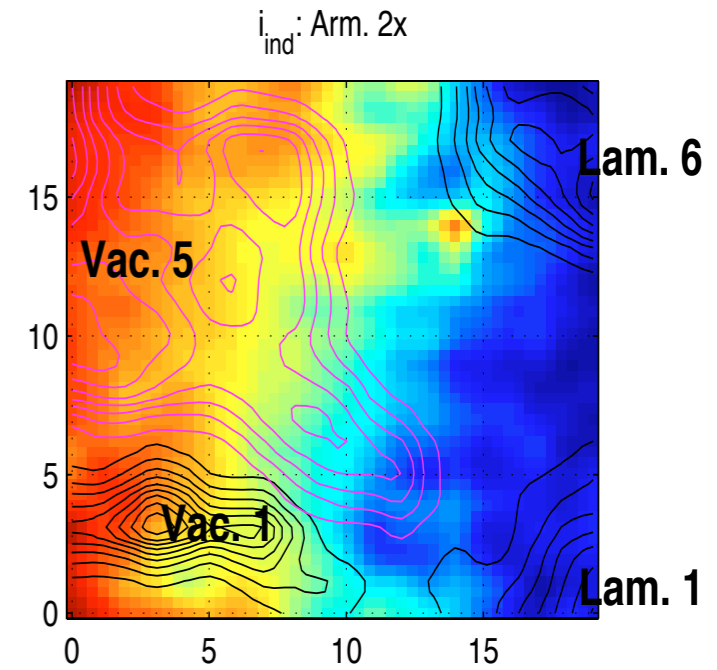
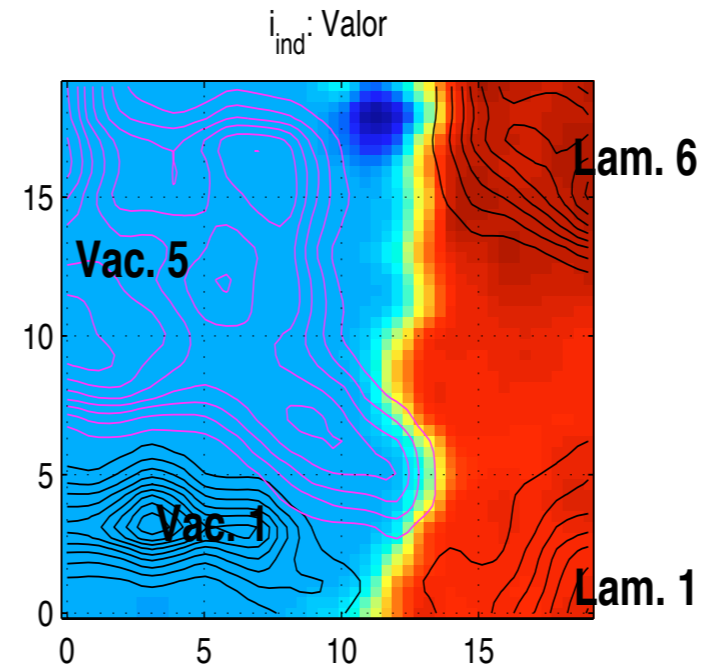
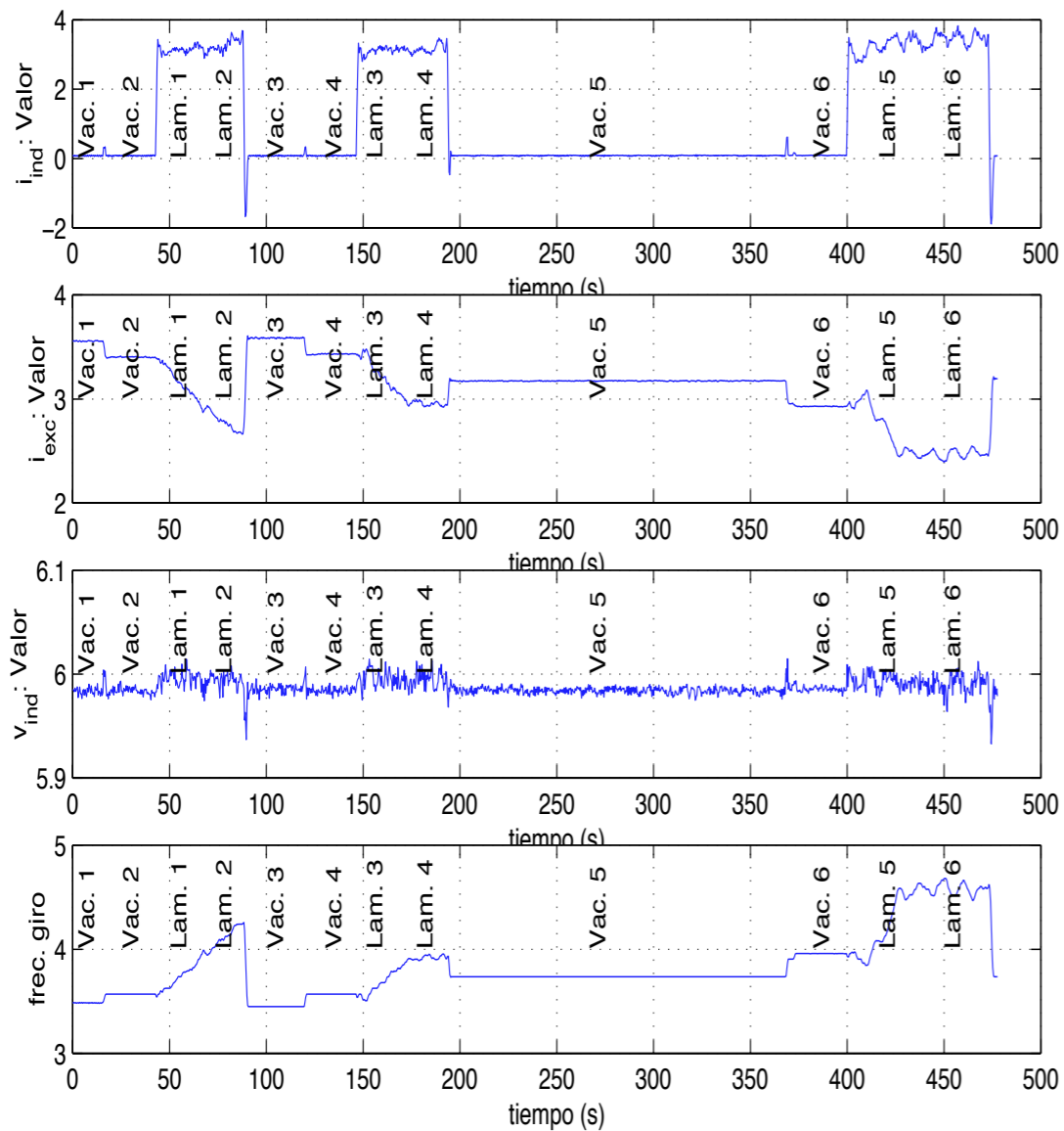


Feature vectors can be:  
 raw process variables  
 harmonics,  
 statistical or geometrical descriptors  
 model parameters,  
 etc.

The visualization space:  
 shows a “map” of the process  
 nearby points => similar feature vectors  
 Regions in the VS represent regions in FS

# Dimensionality Reduction

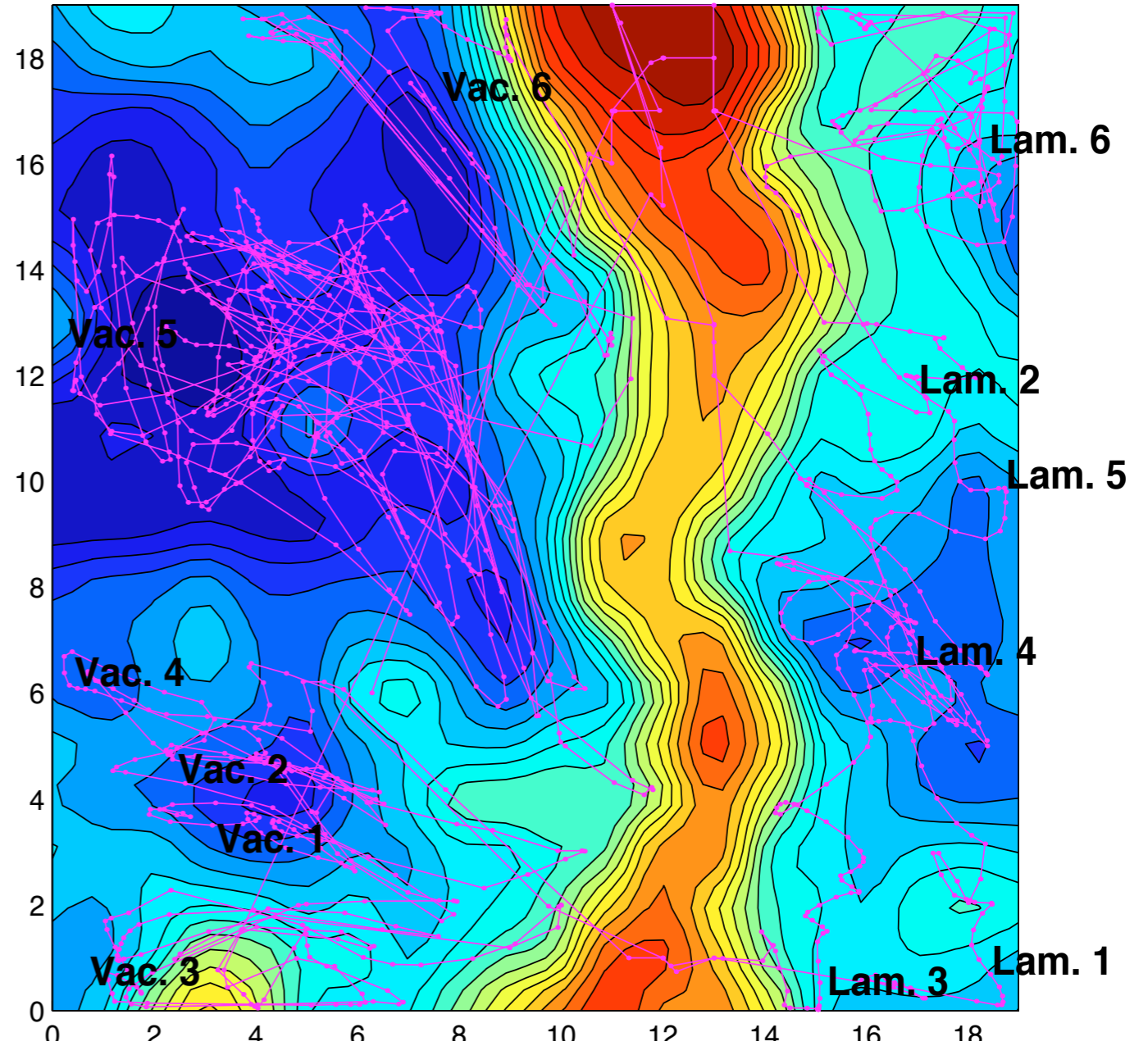
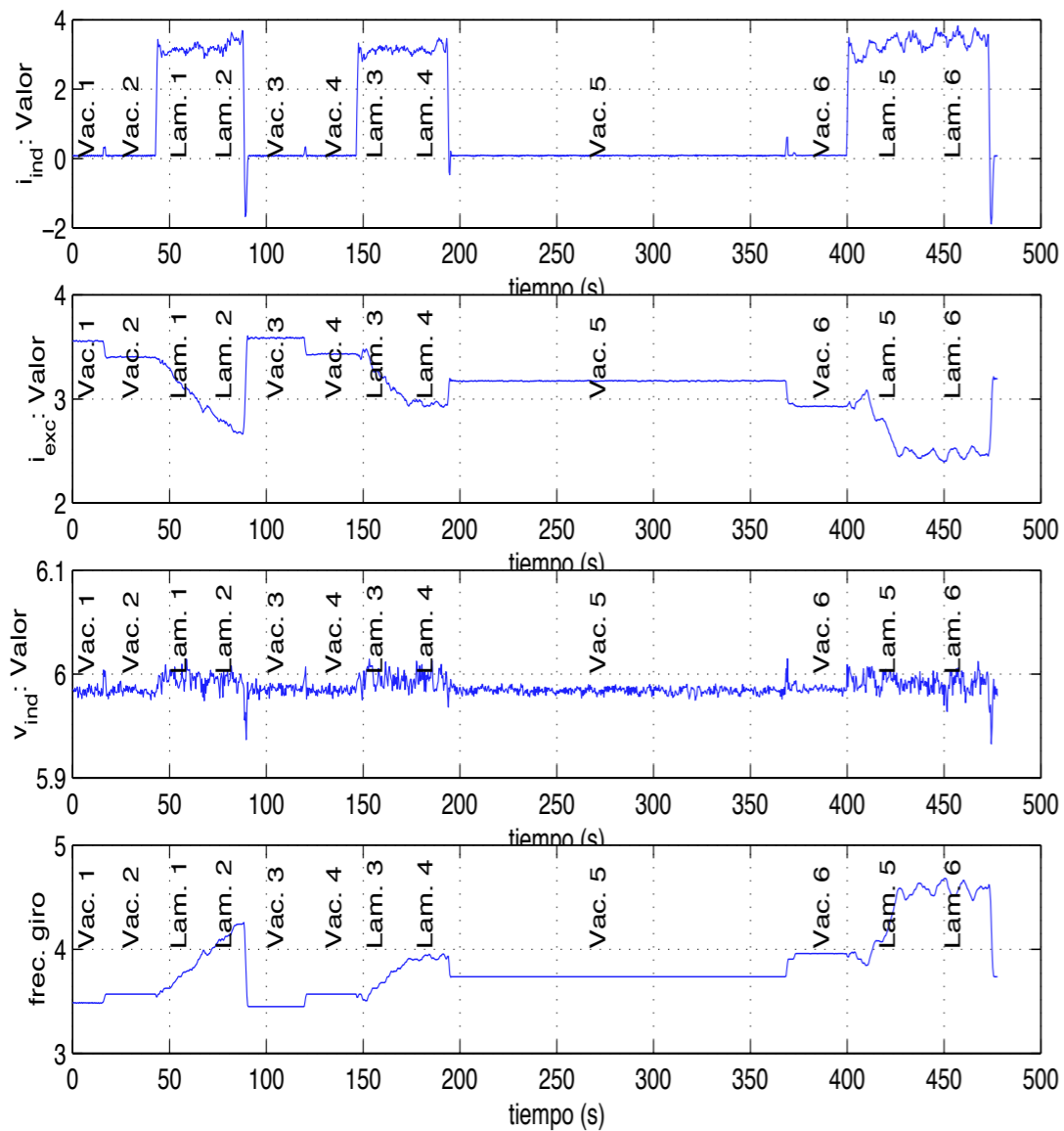
## Process data analysis





# Dimensionality Reduction

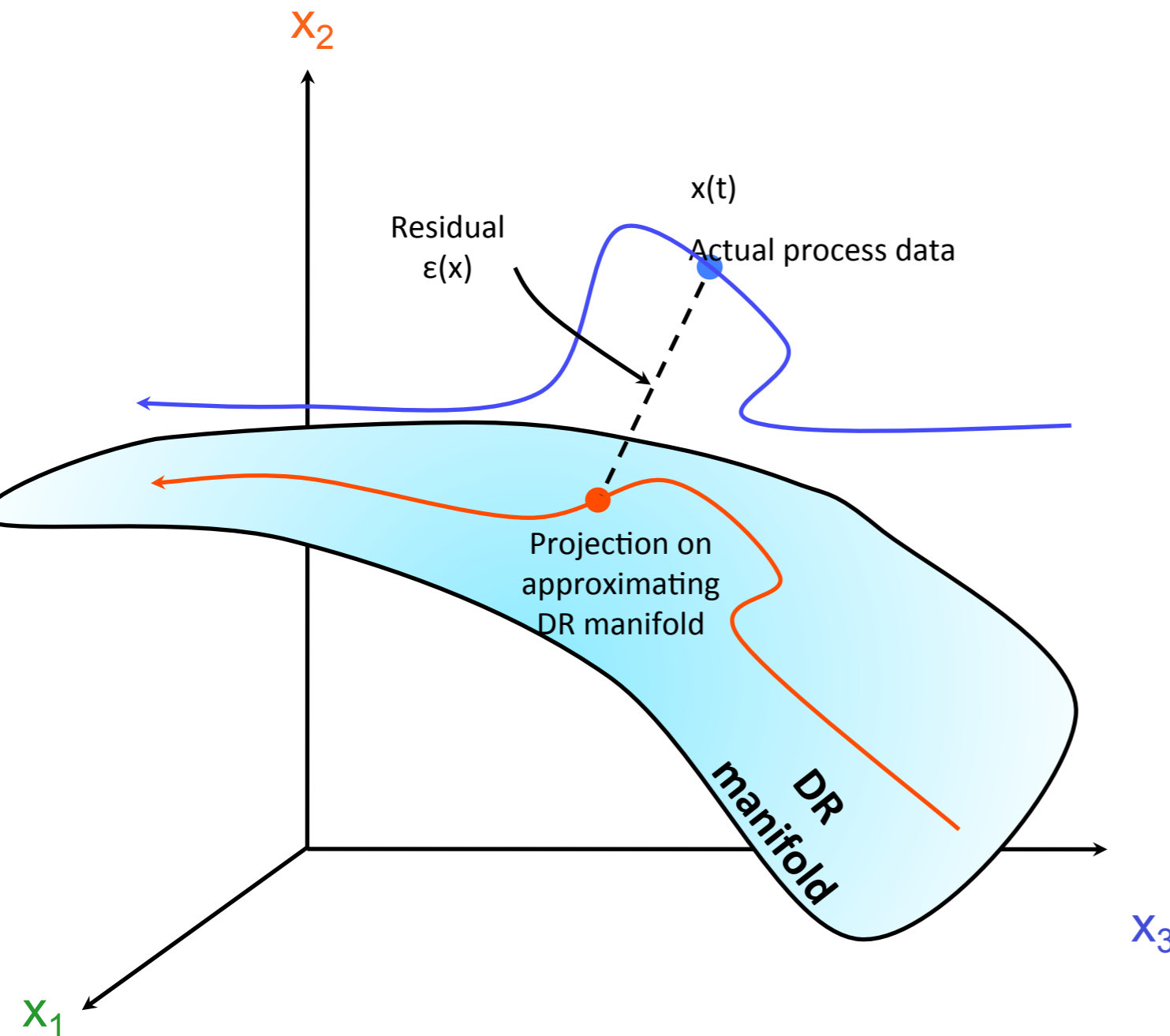
## condition monitoring



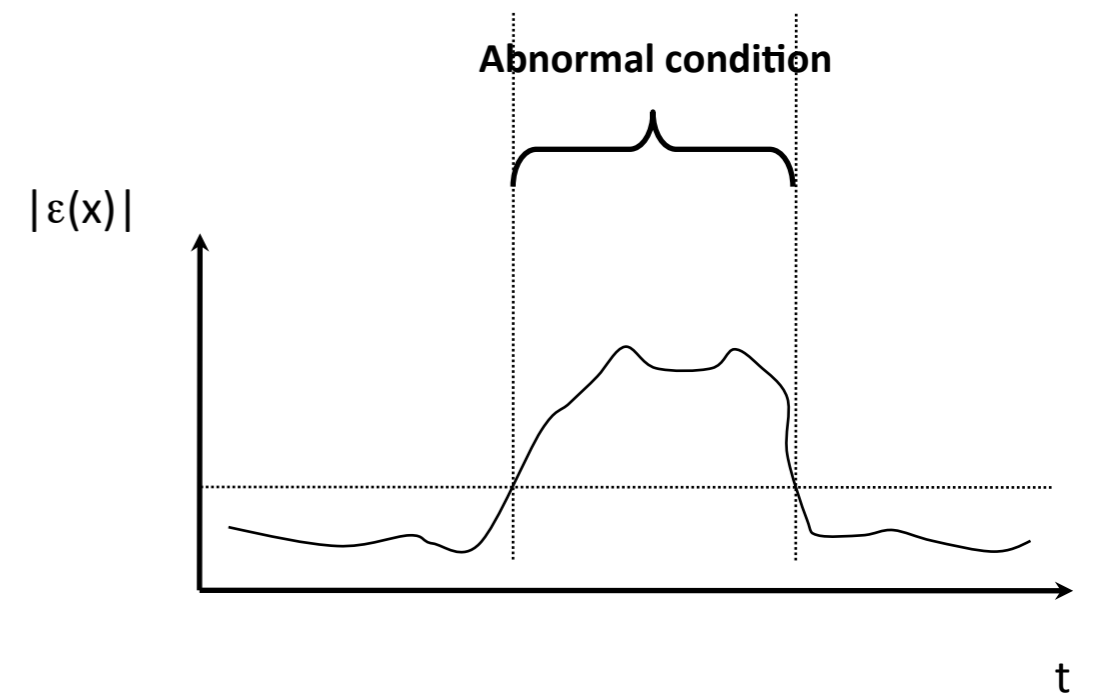


### Process data space

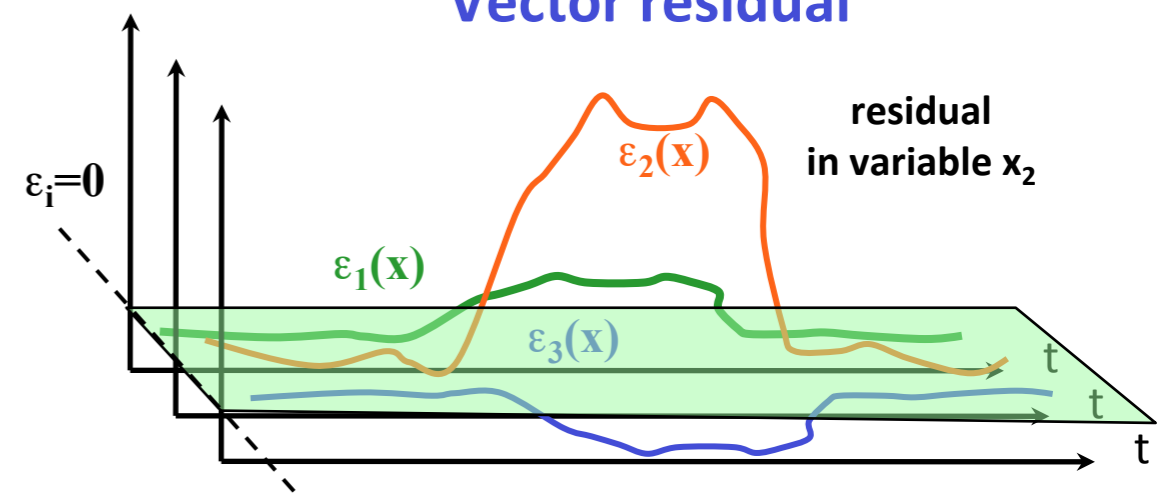
( $x_1, x_2, \dots$  are process variables or features)



### Global residual

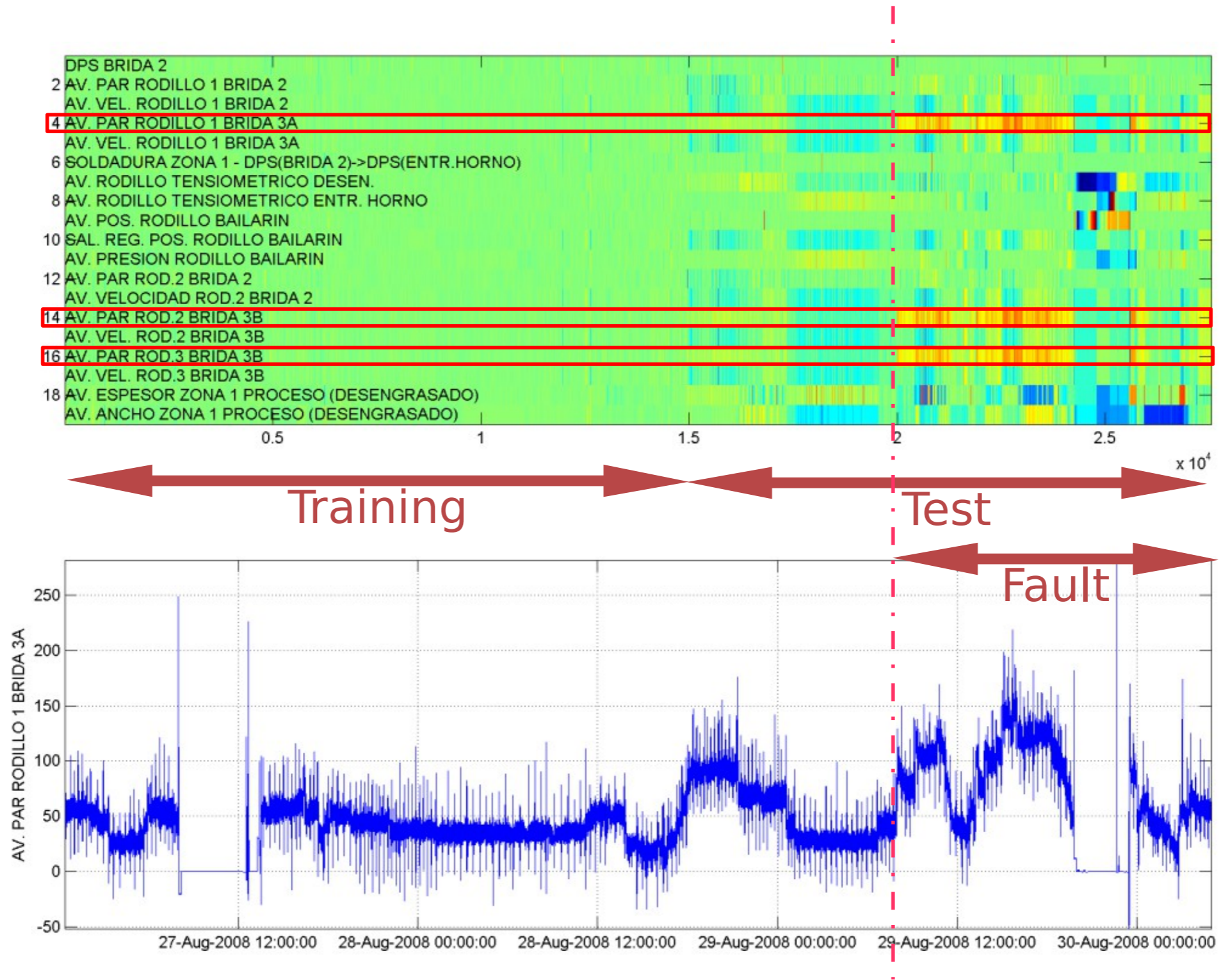


### Vector residual



# Dimensionality Reduction

## Novelty detection based on residuals

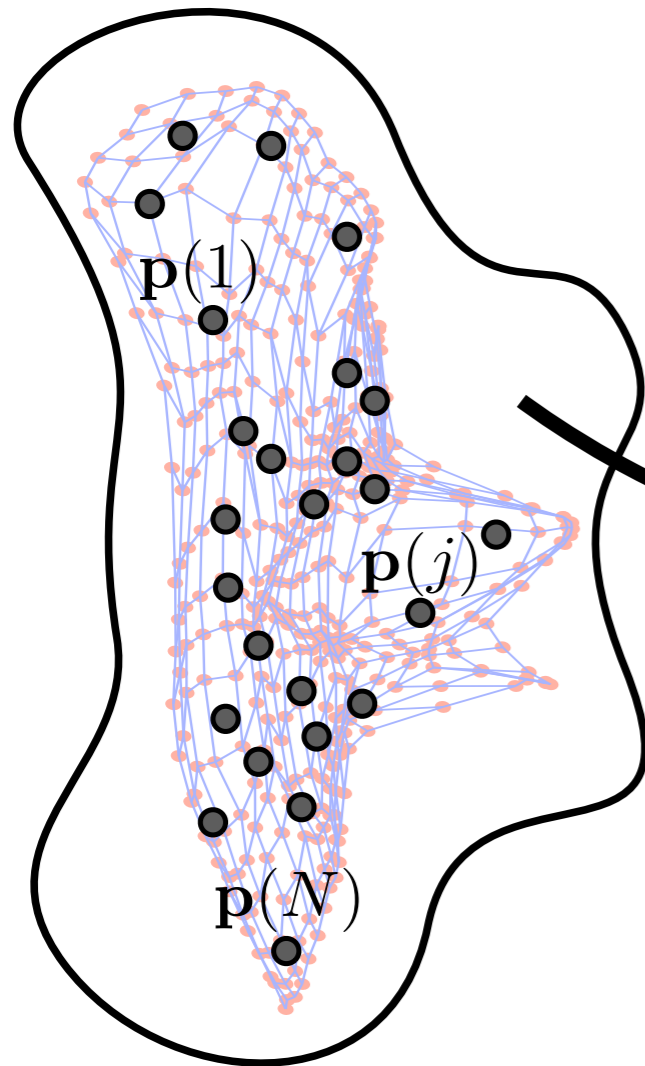


# Dimensionality Reduction

## Visualizing process dynamics through maps

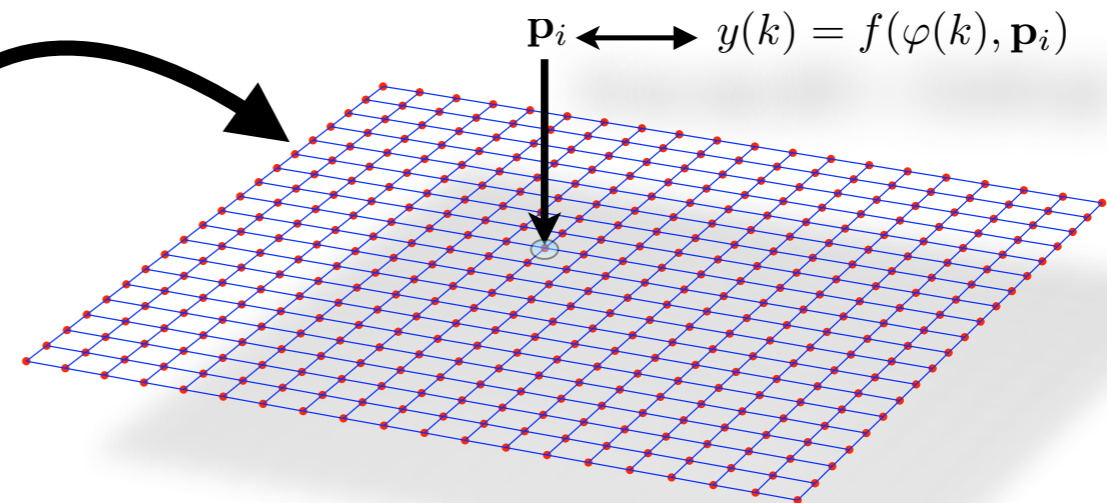
### Basic idea...

input space  
 (parameter set  $P$ )



visualization space

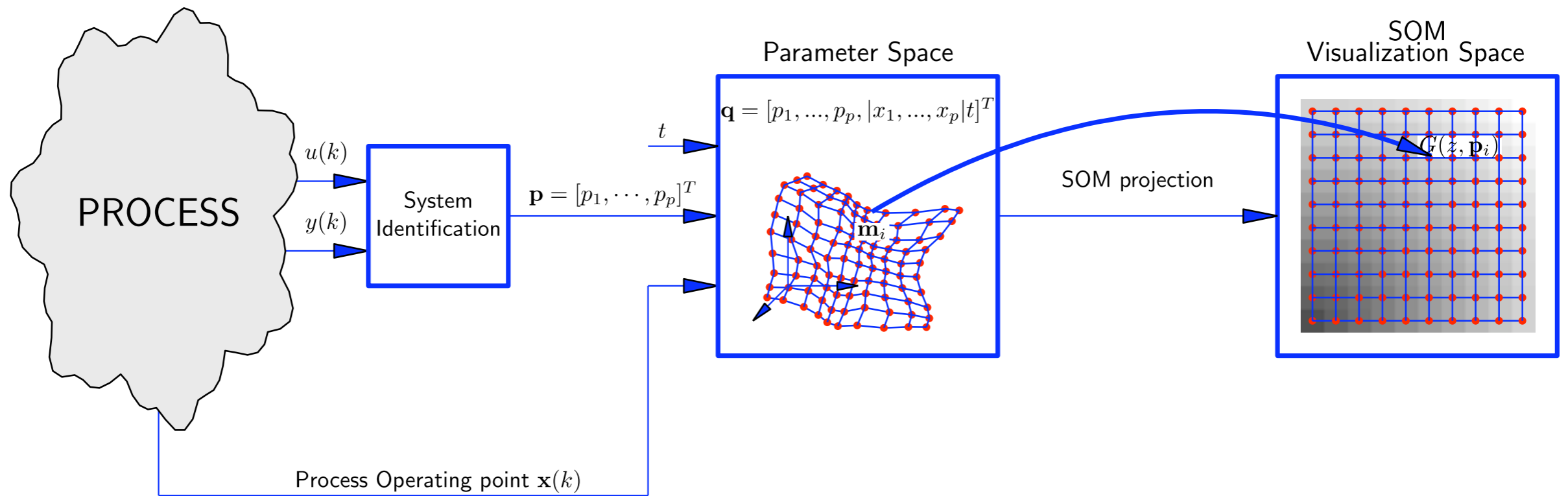
The SOM stores a dynamic model  
 (e.g. transfer function) on each node.  
 This is a **map** of the process dynamics.



# Dimensionality Reduction

## Visualizing process dynamics through maps

... a bit more detailed approach





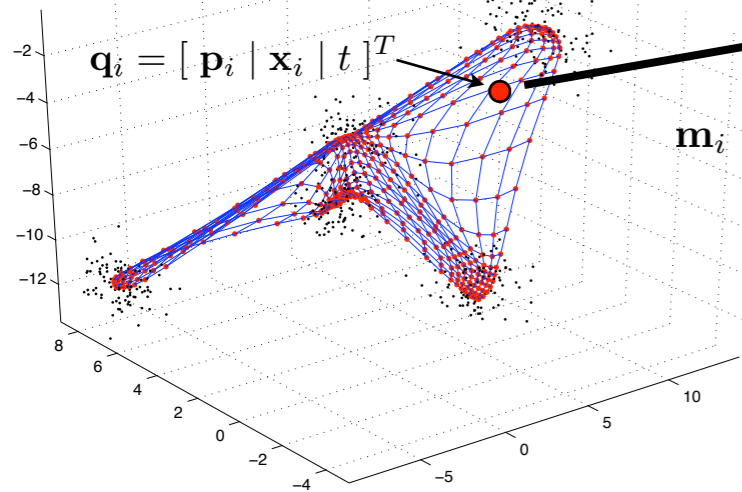
# Dimensionality Reduction

## Visualizing process dynamics through maps

Extended parameter space  
 (parámetros+state)

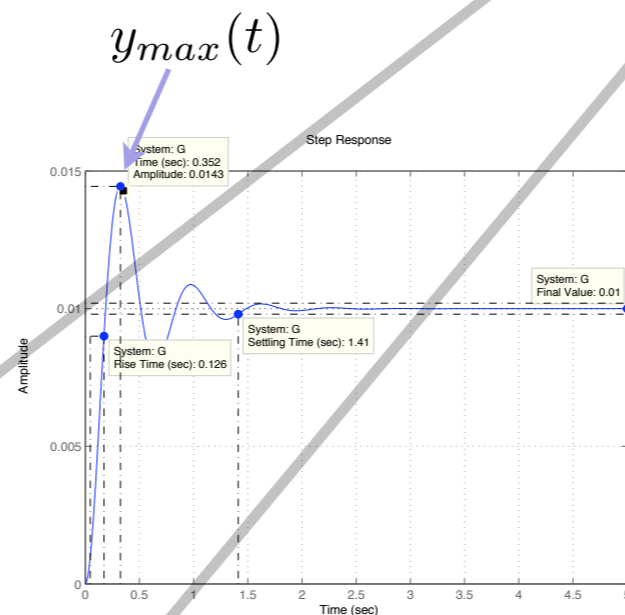
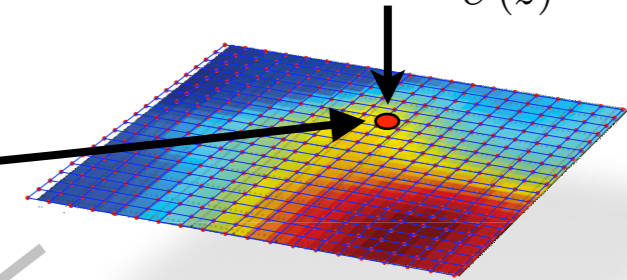
$$\mathbf{q} = [\mathbf{p}^T, \mathbf{x}^T, t]^T$$

$$= [p_1, p_2, \dots, p_p | x_1, x_2, \dots, x_n | t]^T$$

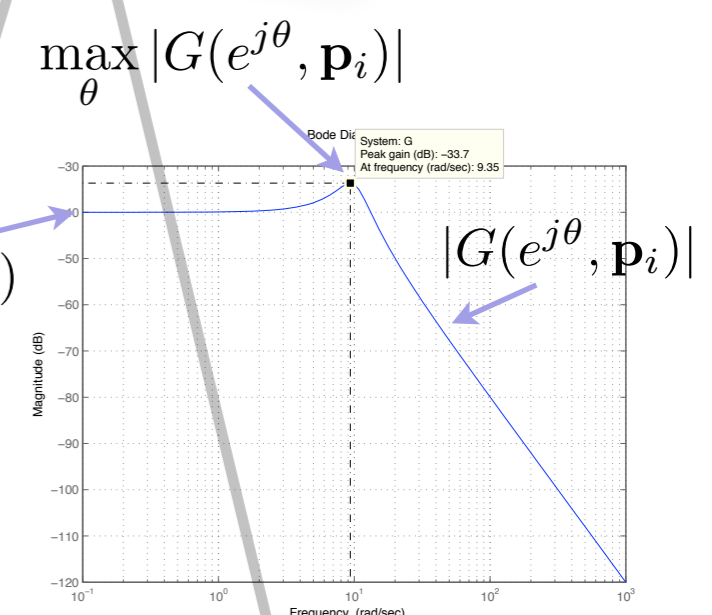


Local model bound to  $\mathbf{m}_i$

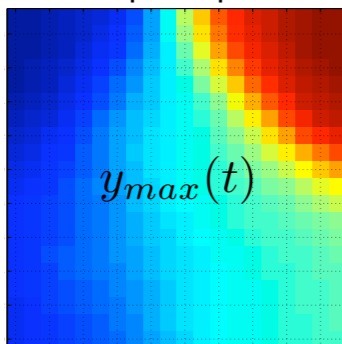
$$G(z, \mathbf{p}_i) = \frac{Y(z)}{U(z)} = \frac{\sum_{j=0}^{n_u} b_j^i z^{-j}}{1 - \sum_{j=1}^{n_y} a_j^i z^{-j}}$$



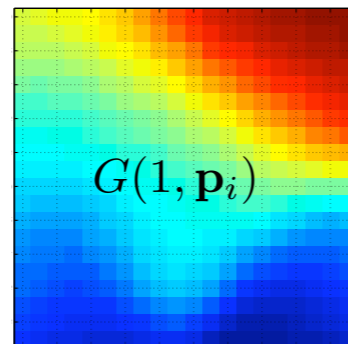
$G(1, \mathbf{p}_i)$



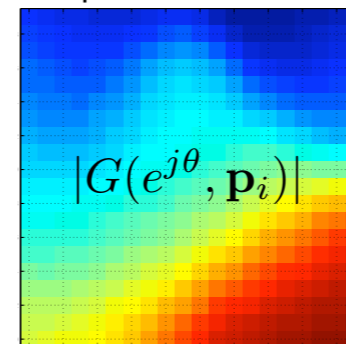
Mapa de pico



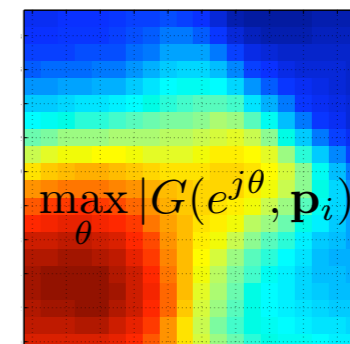
Mapa de ganancia



Mapa de respuesta en frecuencia

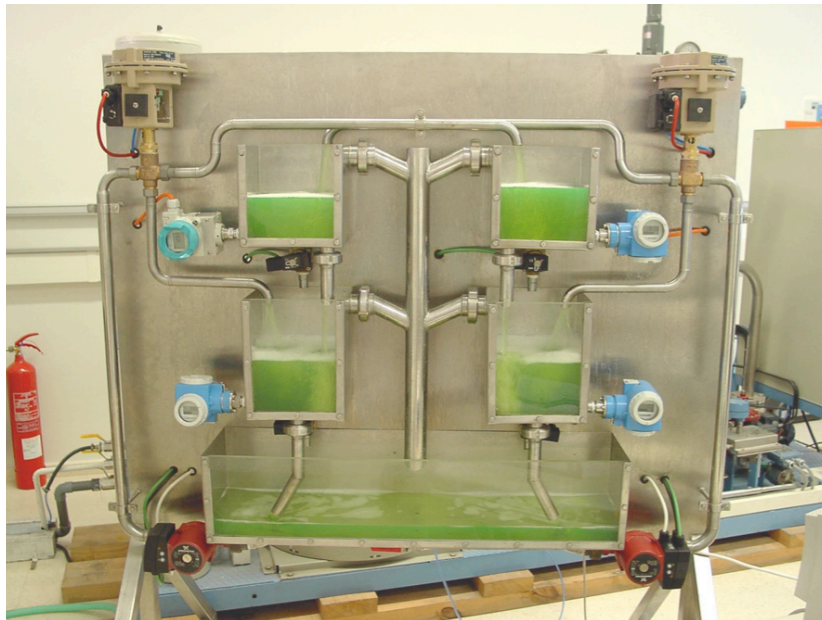


Mapa de resonancia



# Dimensionality Reduction

## Example: visualizing local dynamics



**Dynamic model**

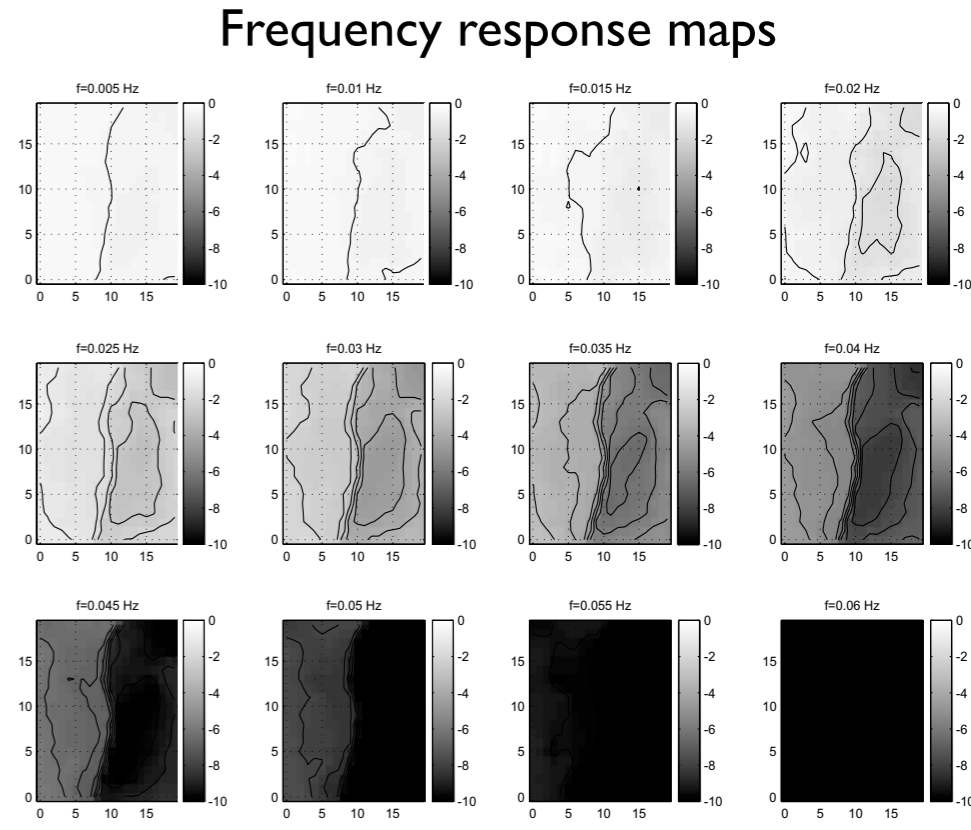
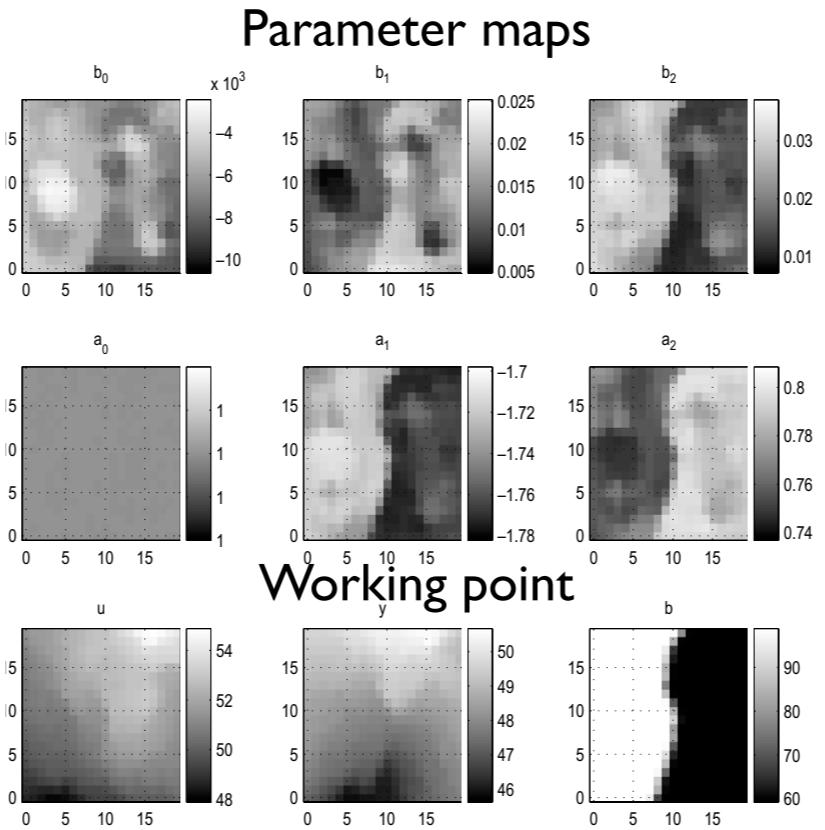
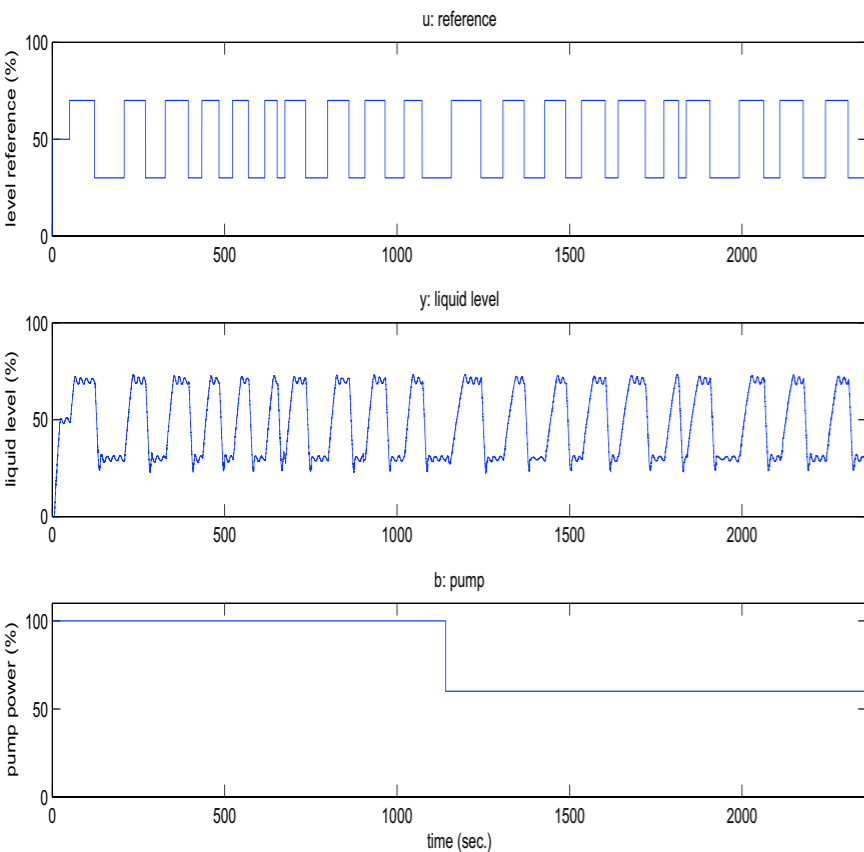
$$y(k) = a_1y(k-1) + a_2y(k-2) + b_0u(k) + b_1u(k-1) + b_2u(k-2)$$

$$G(z, \mathbf{p}_i) = \frac{b_0^i + b_1^i z^{-1} + b_2^i z^{-2}}{1 + a_1^i z^{-1} + a_2^i z^{-2}}$$

**State (working point)**

$$\mathbf{x} = [u, y, b]^T$$

$$\mathbf{q} = [a_1, a_2, b_0, b_1, b_2, |u, y, b]$$

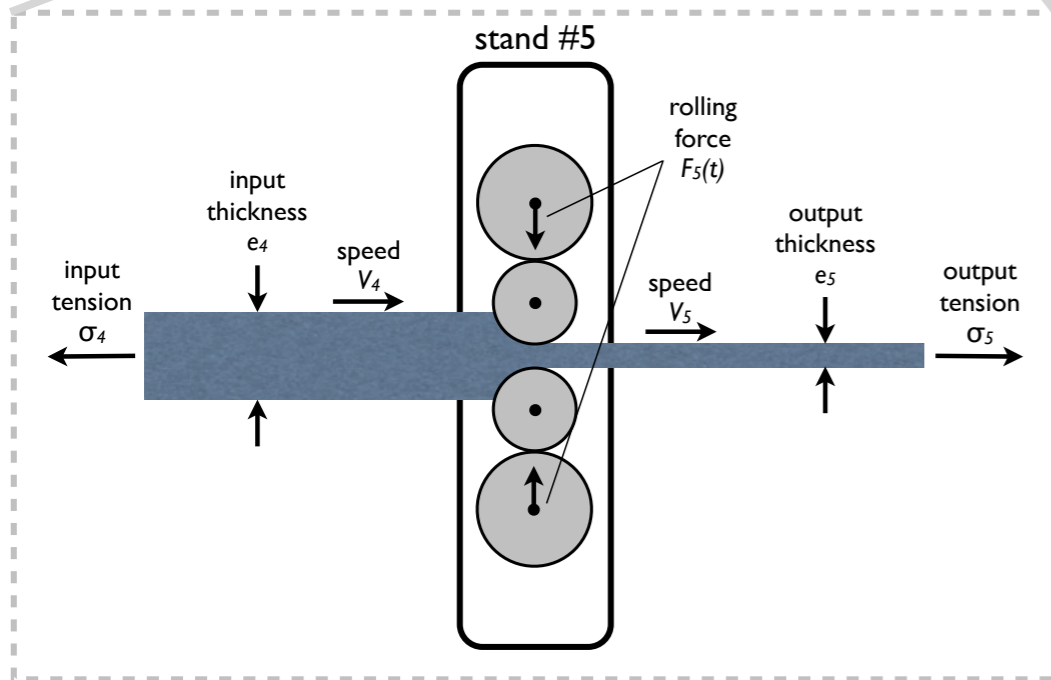
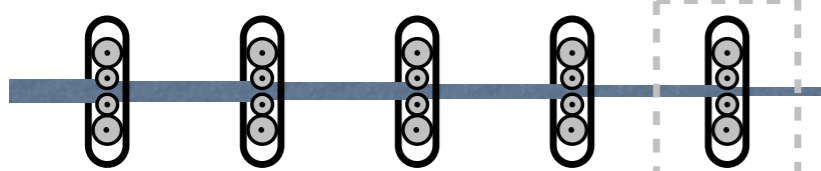




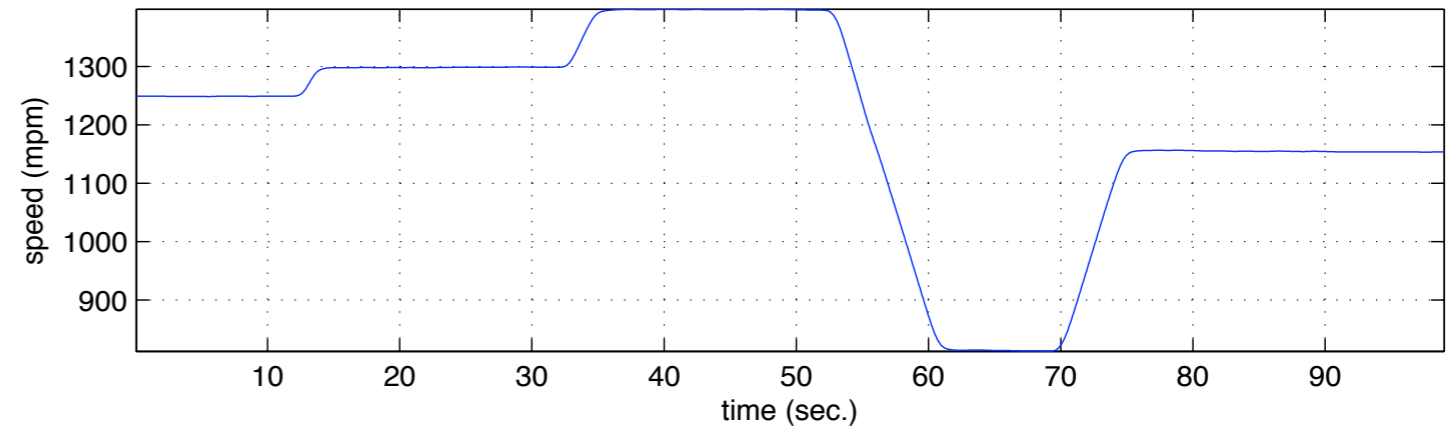
# Dimensionality Reduction

## Building maps of vibrational states (chatter)

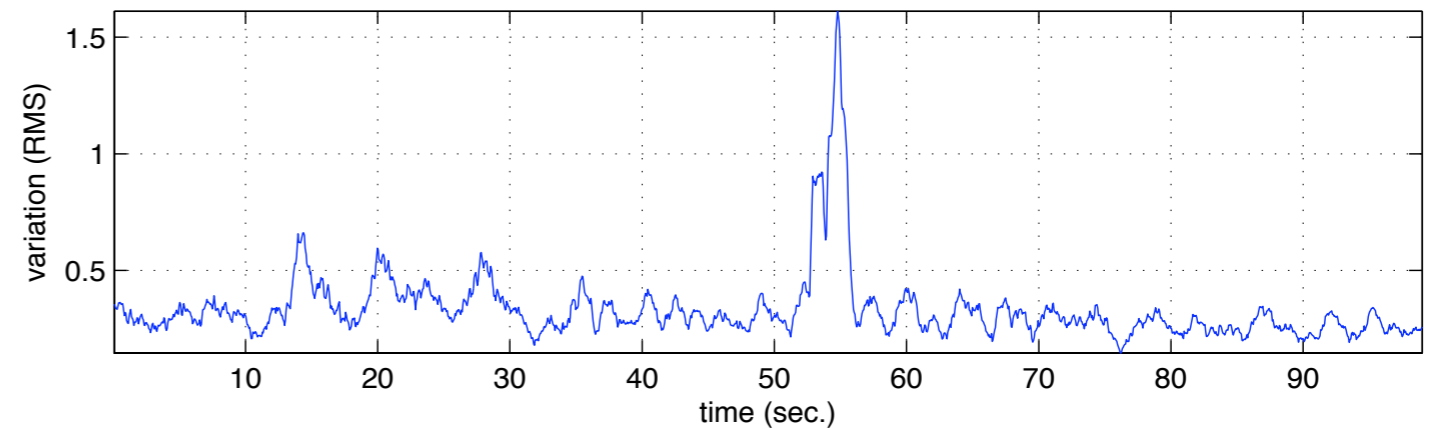
5-stand cold rolling mill



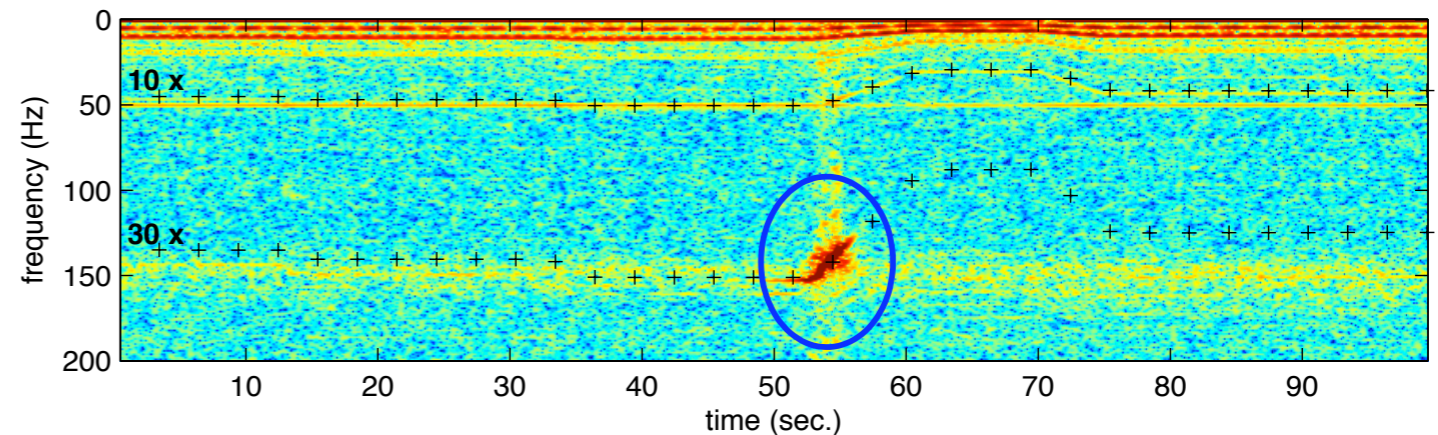
Coil speed at stand 5 ( $v_5$ )



Thickness variation ( $\delta_5$ )



Spectrogram of rolling forces ( $F_5$ )



# Dimensionality Reduction

## Building maps of vibrational states (chatter)

### Dynamic models (AR)

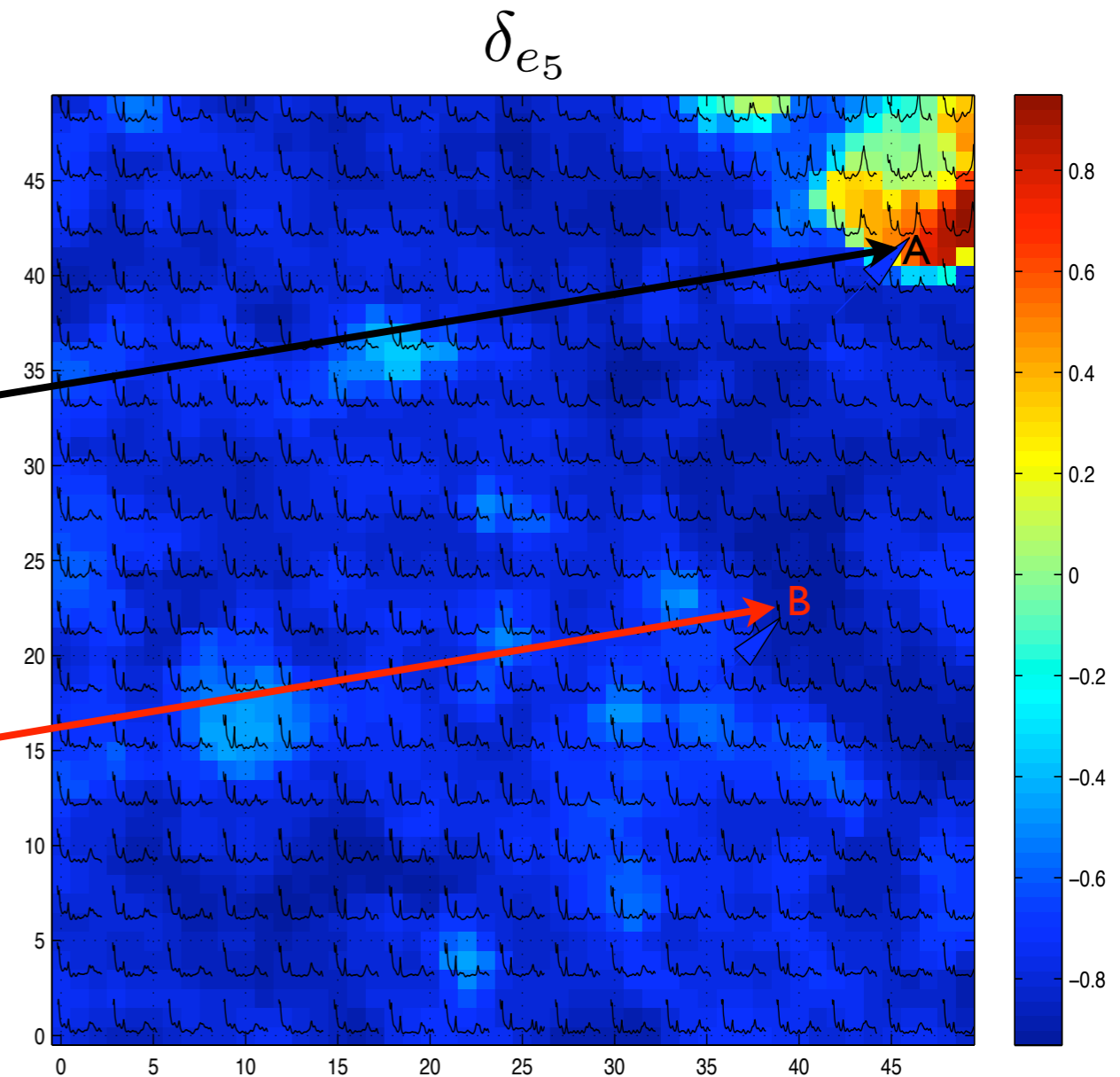
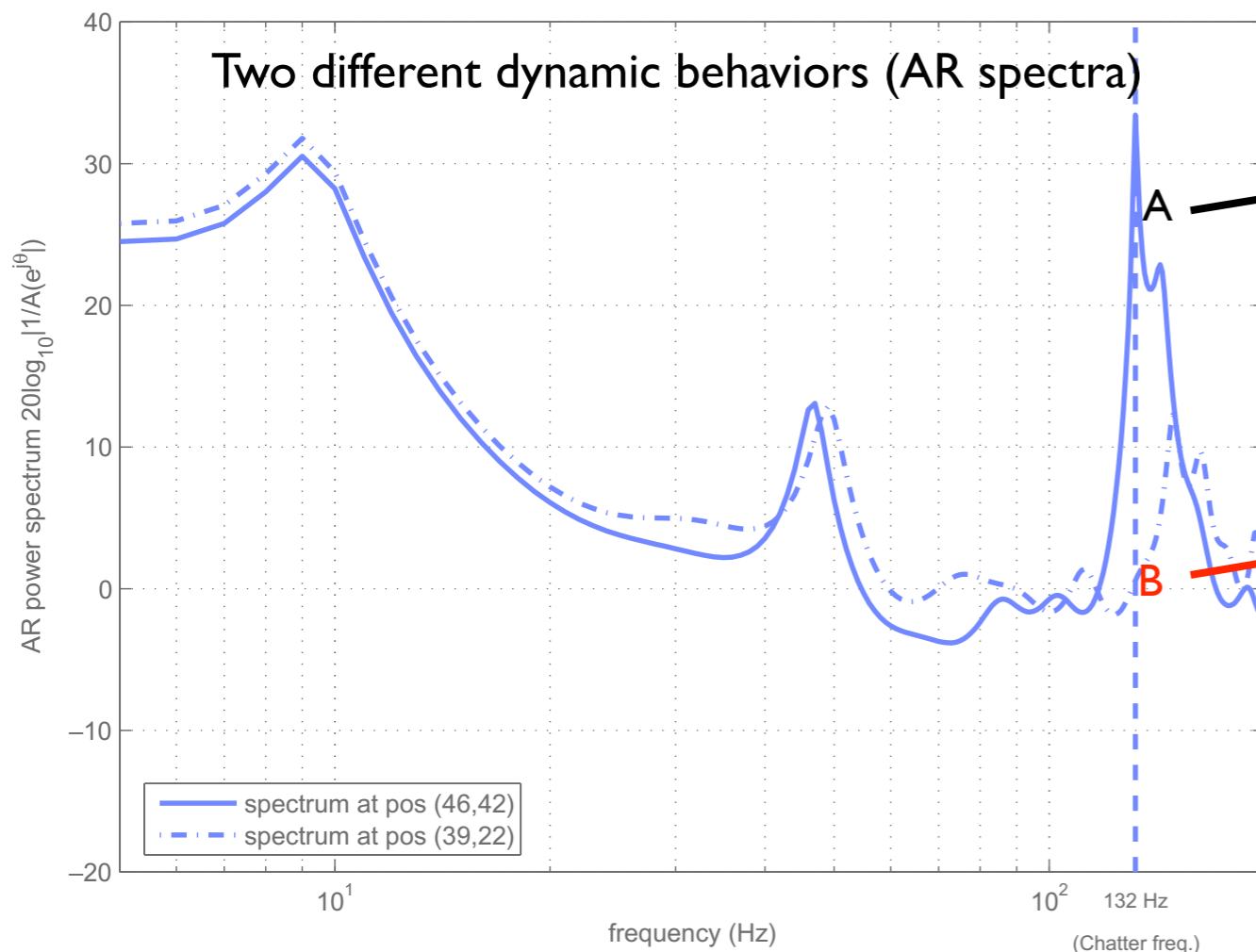
$$F_5(k) = a_1 F_5(k-1) + \dots + a_{29} F_5(k-29) + \epsilon$$

$$\mathbf{p} = [a_1, a_2, \dots, a_{29}]^T$$

### Working point

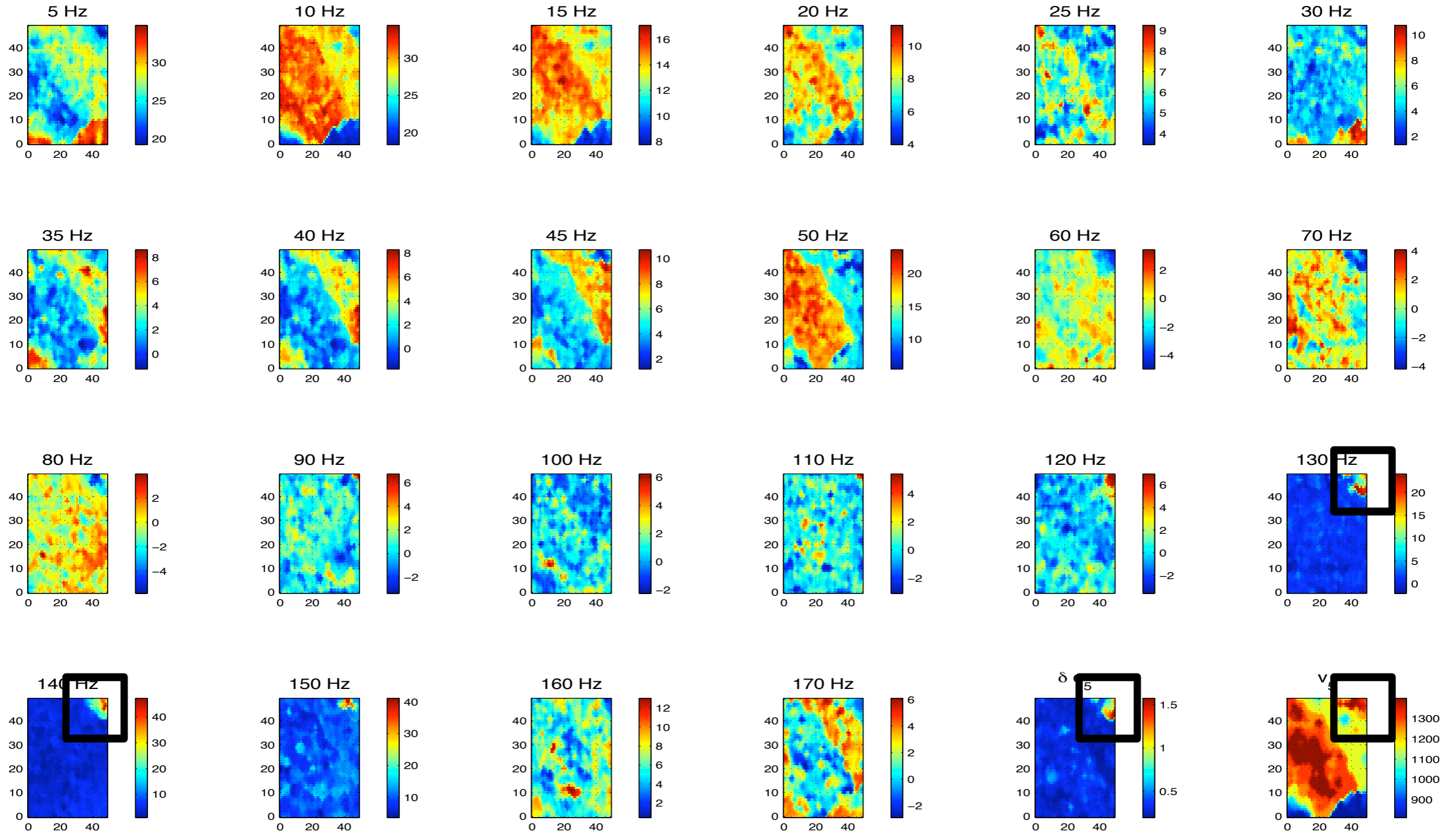
$$\mathbf{x}_i = [\delta e_5, v_5]^T$$

$$\mathbf{q} = [a_1, a_2, \dots, a_{29}, |\delta e_5, v_5|^T$$



# Dimensionality Reduction

## Building maps of vibrational states (chatter)



# Dimensionality Reduction

## vibration analysis in rotating machines

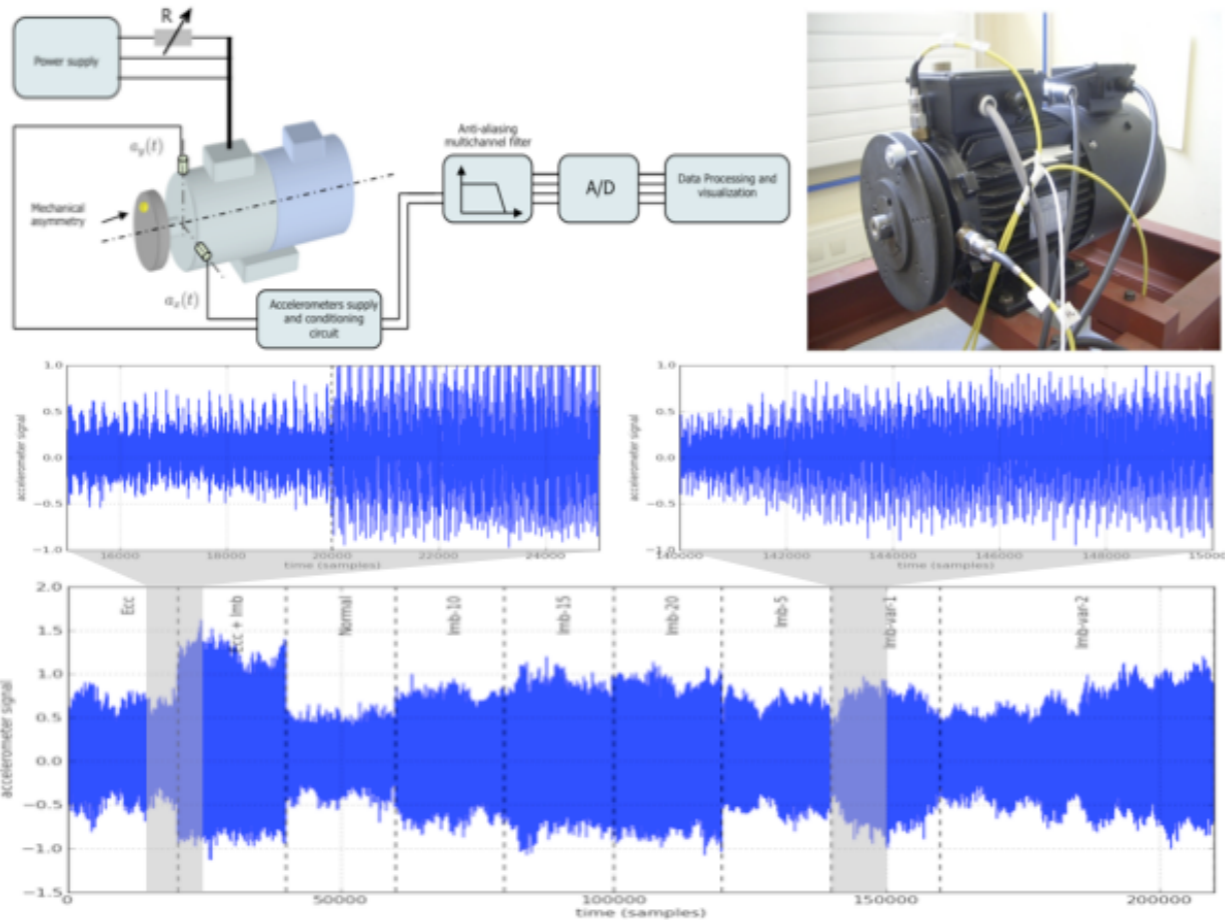
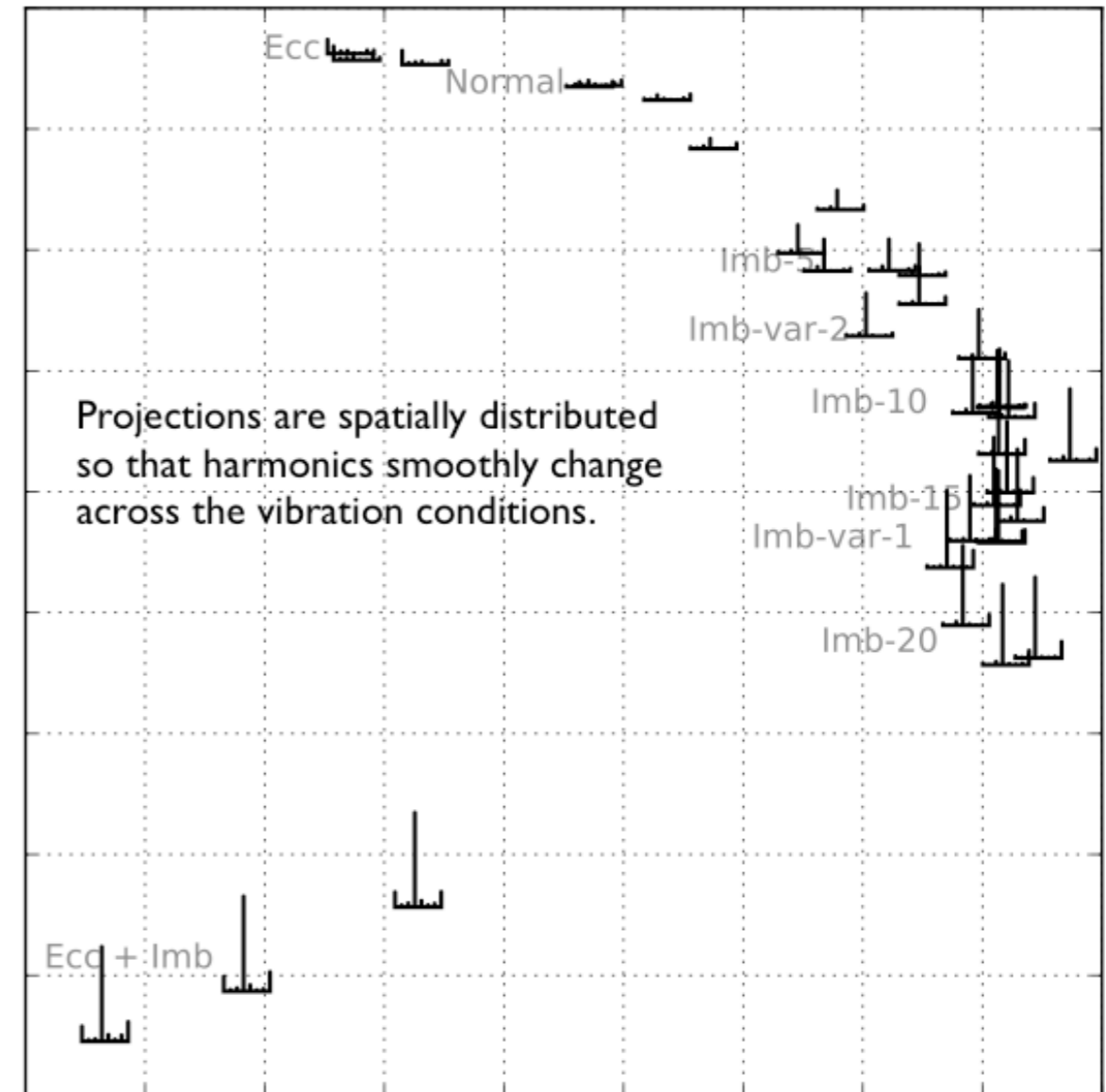


Table 1. Description of the 9 experiments.

Experiment No.	Label	Description
#1	'Ecc'	Mechanical eccentricity
#2	'Ecc+Imb'	Mechanical eccentricity + Electrical imbalance
#3	'Normal'	No eccentricity, no electrical imbalance.
#4	'Imb-10'	Electrical imbalance (fixed load, 10 $\Omega$ )
#5	'Imb-15'	Electrical imbalance (fixed load, 15 $\Omega$ )
#6	'Imb-20'	Electrical imbalance (fixed load, 20 $\Omega$ )
#7	'Imb-5'	Electrical imbalance (fixed load, 5 $\Omega$ )
#8	'Imb-var-1'	Electrical imbalance (variable load, low $\rightarrow$ high $\rightarrow$ low)
#9	'Imb-var-2'	Electrical imbalance (variable load, low $\rightarrow$ high)

## map of vibrational states

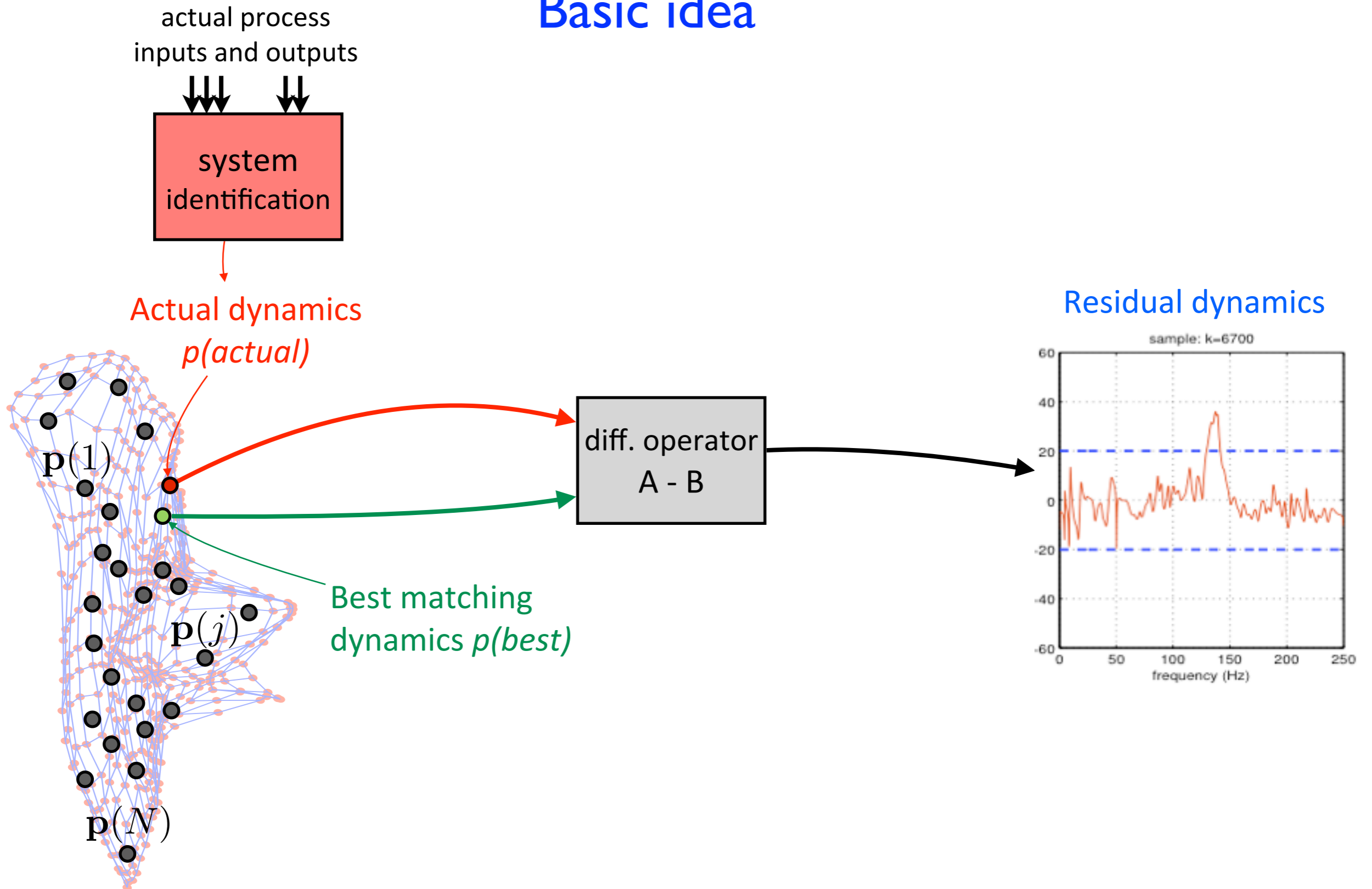




# Dimensionality Reduction

## Novelty detection in dynamic behavior

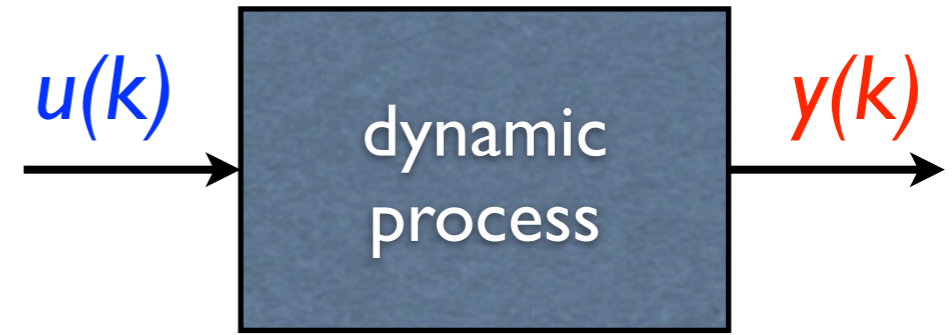
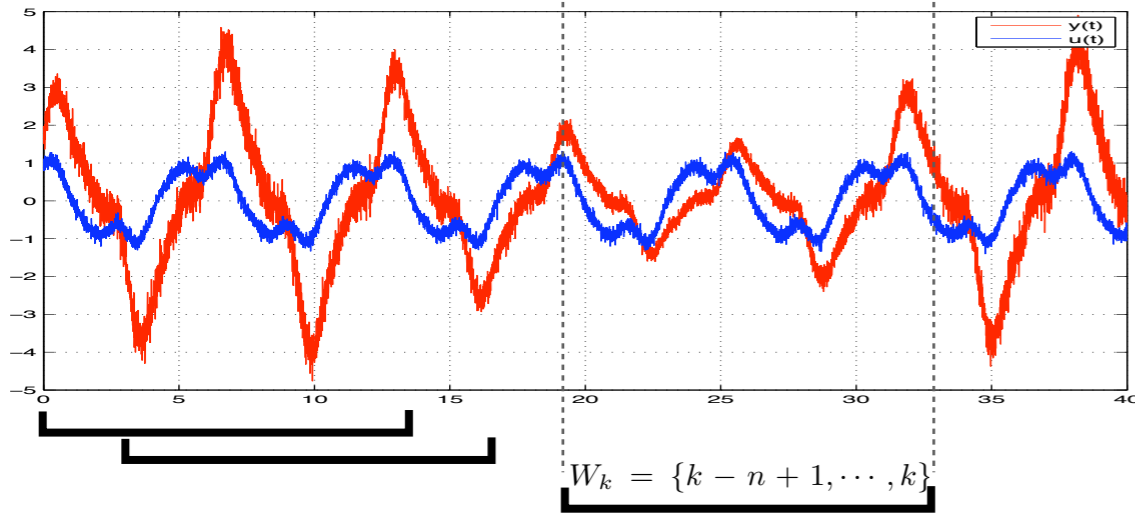
### Basic idea



# Dimensionality Reduction

## Novelty detection in dynamic behavior

Example: input (blue) and output (red) from a process



Get data from  $k_{th}$  window

$$\{y(k), \varphi(k)\}_{k \in W_k}$$

minimize:

$$J = \sum_{k \in I_j} \|y(k) - f(\varphi(k), \mathbf{p}(k))\|^2$$

SOM bmu

$$c(k) = \arg \min_i \{\|\mathbf{p}(k) - \mathbf{m}_i\|\}$$

$$\mathbf{m}_{c(k)} \longleftarrow \mathbf{p}(k)$$

$$G(e^{j\theta}, \mathbf{m}_{c(k)})$$

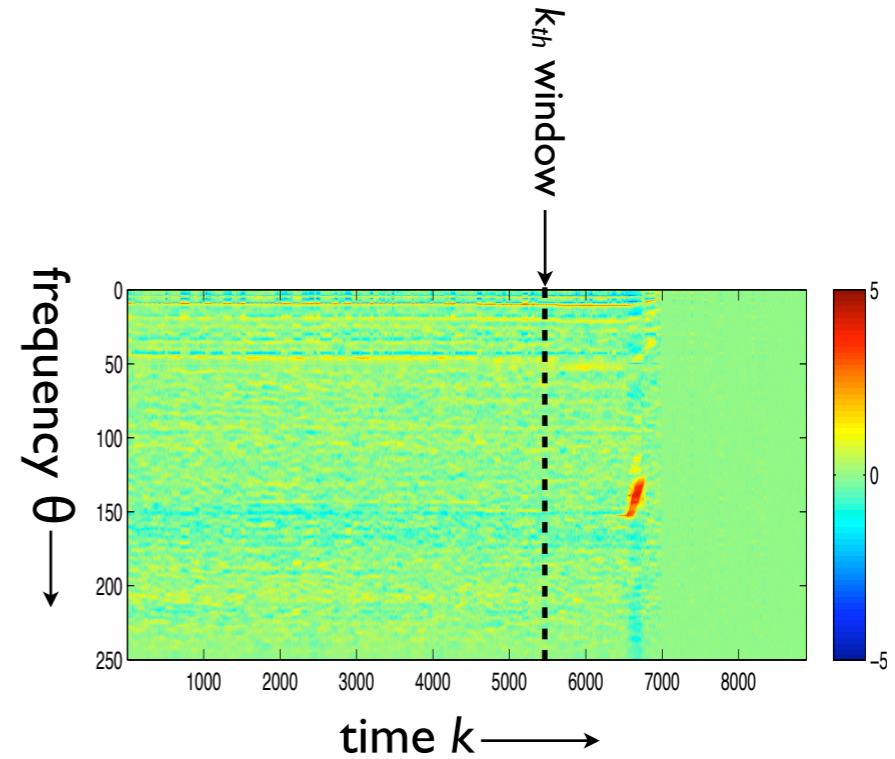
(closest model)

$$G(e^{j\theta}, \mathbf{p}(k))$$

(actual model)

Compare models  
(actual vs closest)

$$\mathbf{R}(e^{j\theta}, k) = \frac{G(e^{j\theta}, \mathbf{p}(k))}{G(e^{j\theta}, \mathbf{m}_{c(k)})}$$

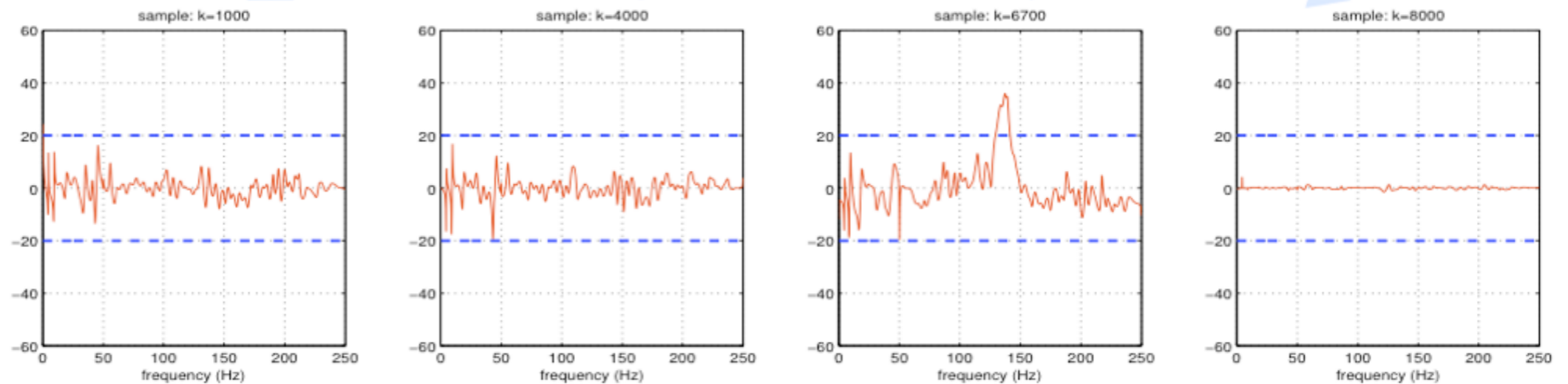
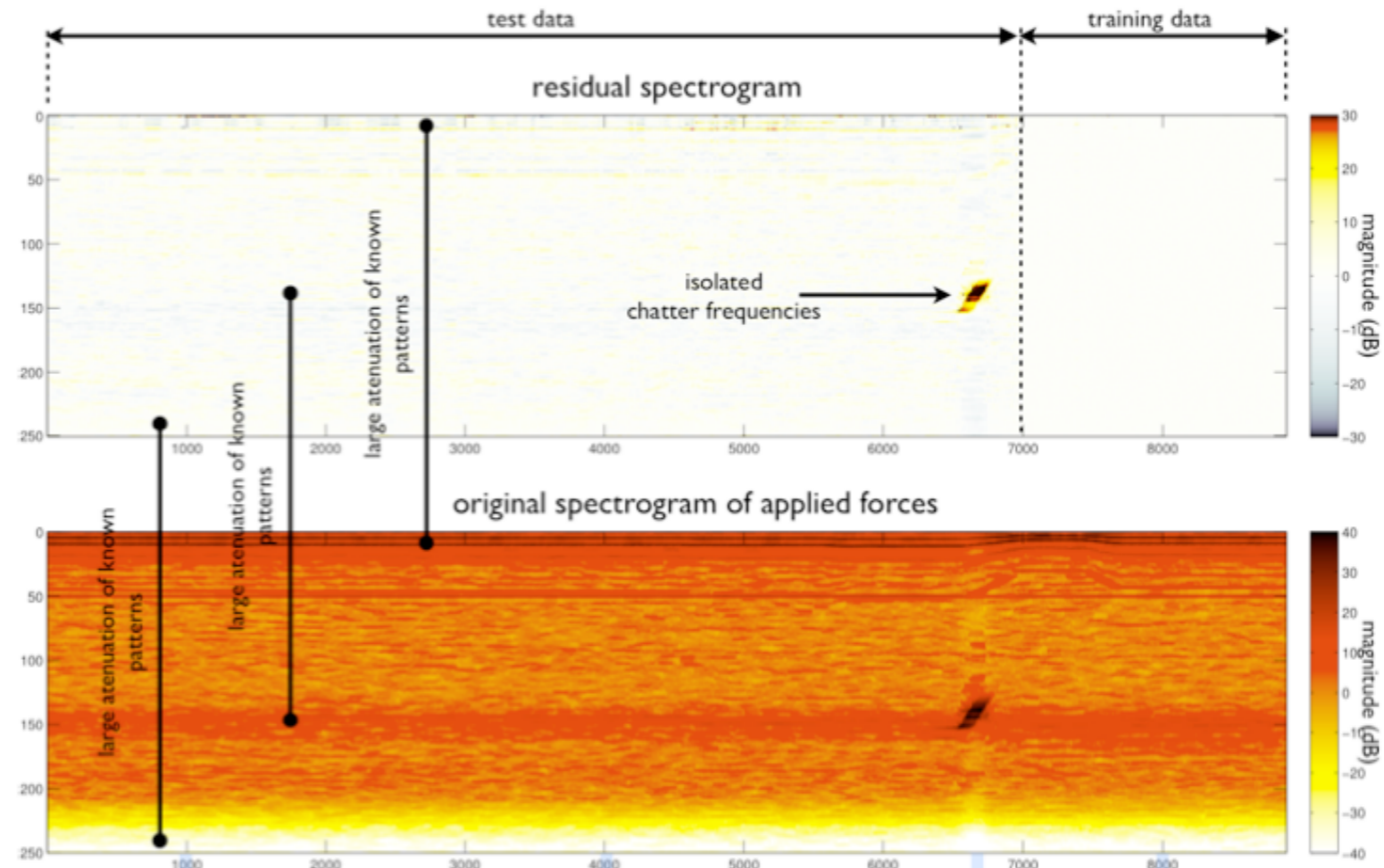
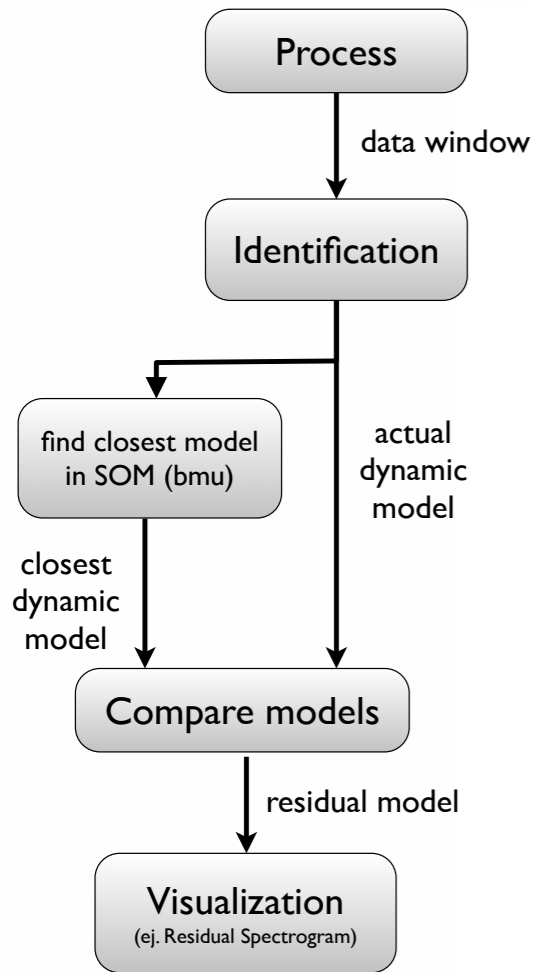


visualize



# Dimensionality Reduction

## Example: Isolation of harmful dynamics

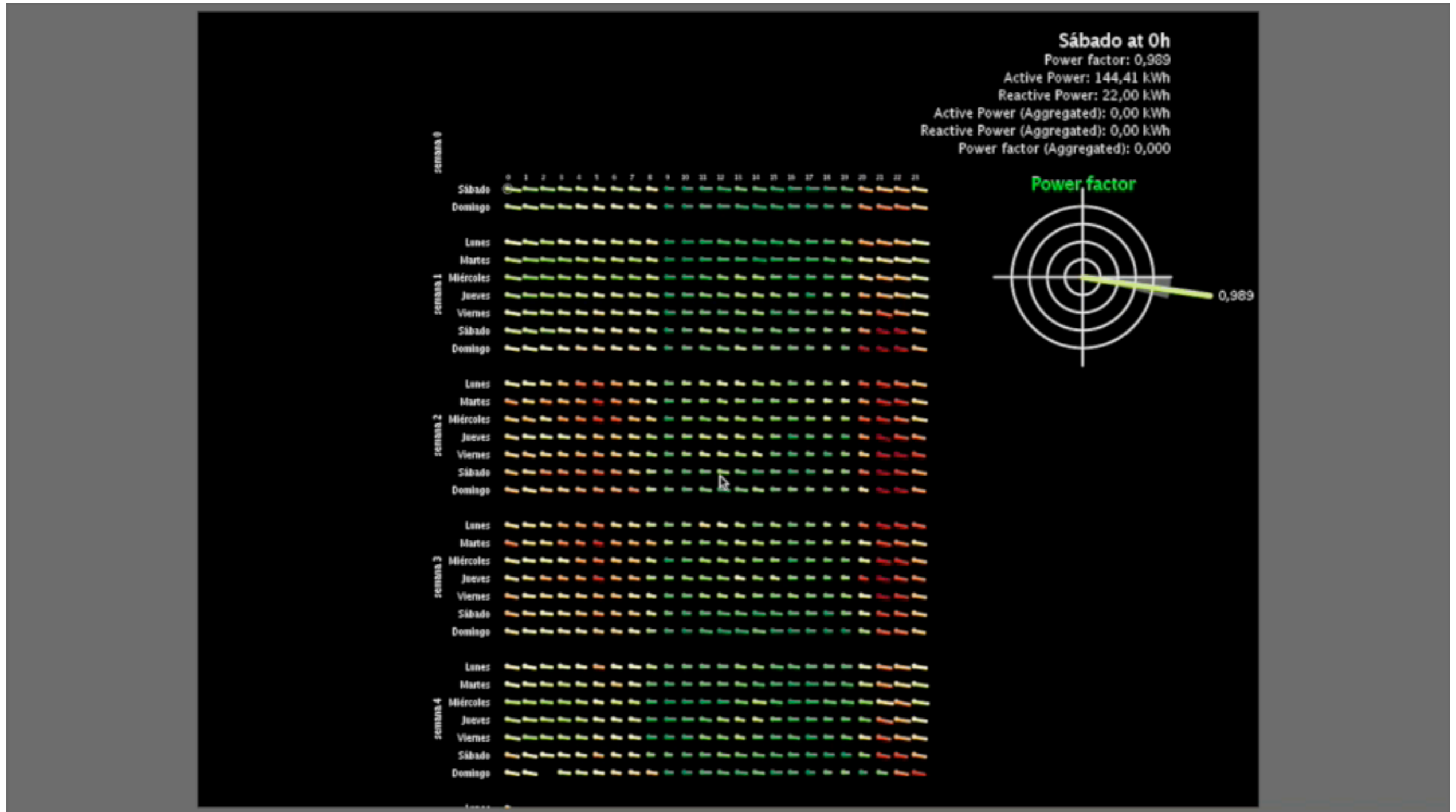


# Interaction

a new dimension for data understanding

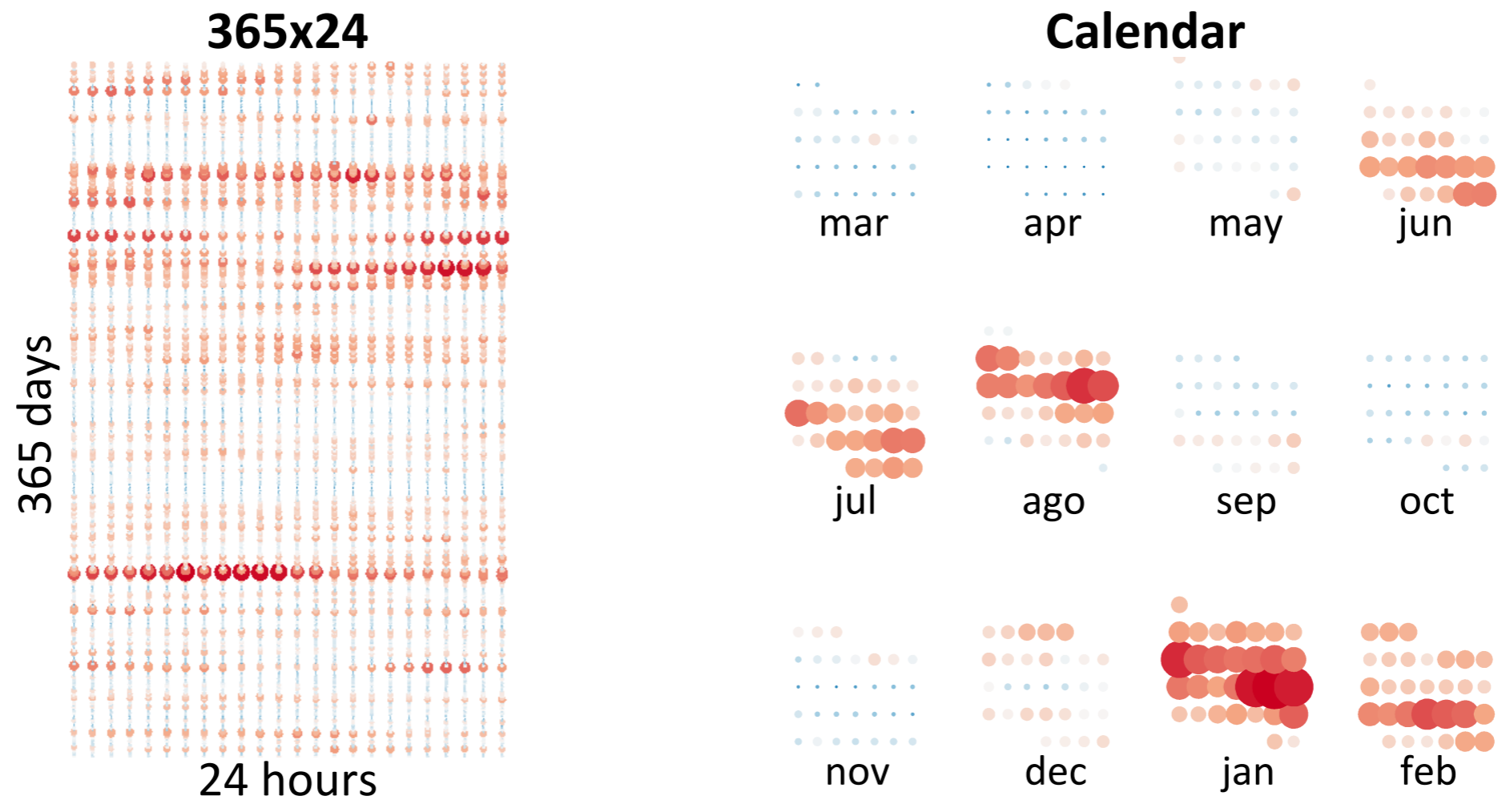
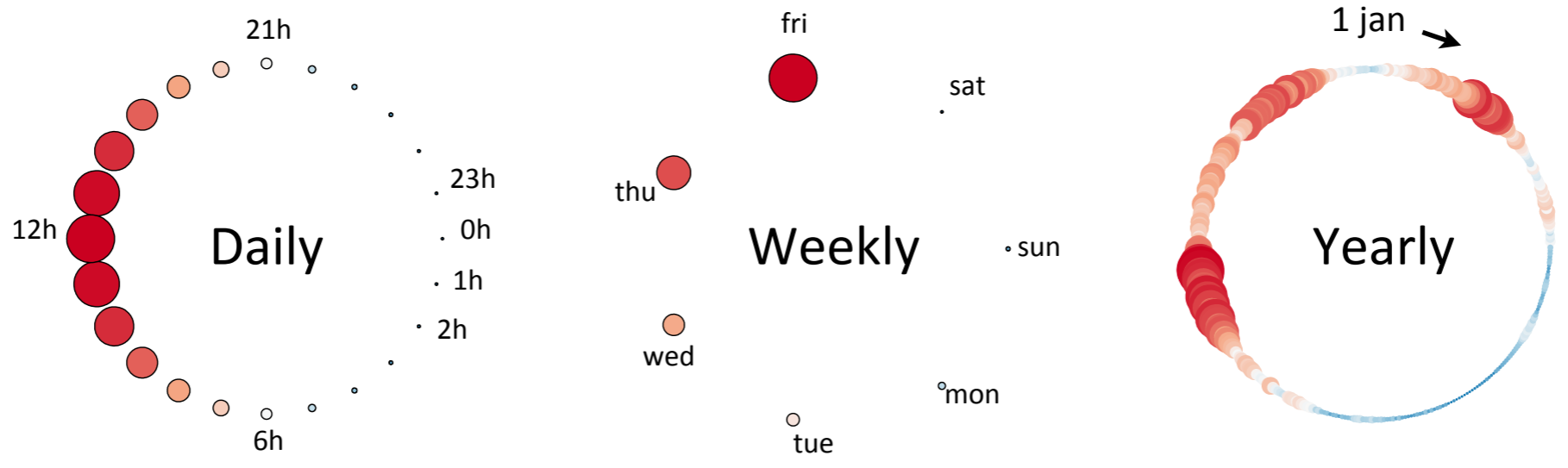
# Basic interaction

zoom, pan, hover...



# Animated Transitions

example: electric power demand analysis



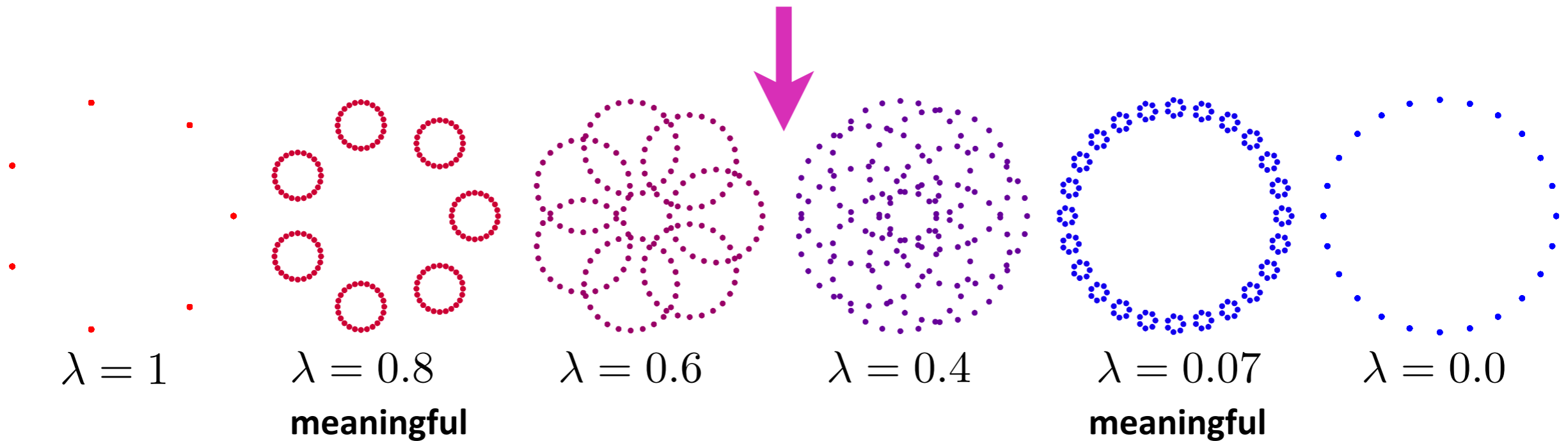


# Animated Transitions

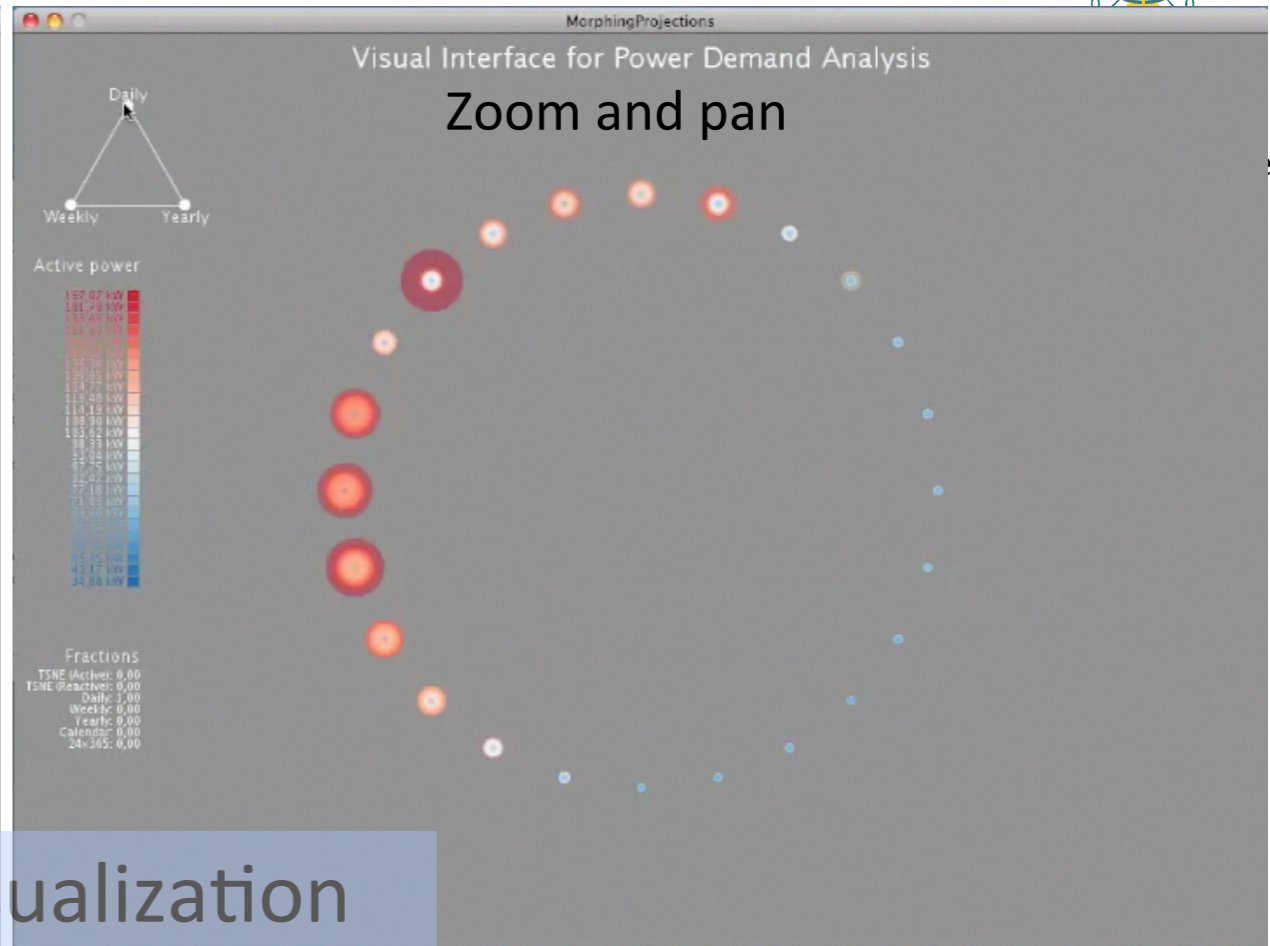
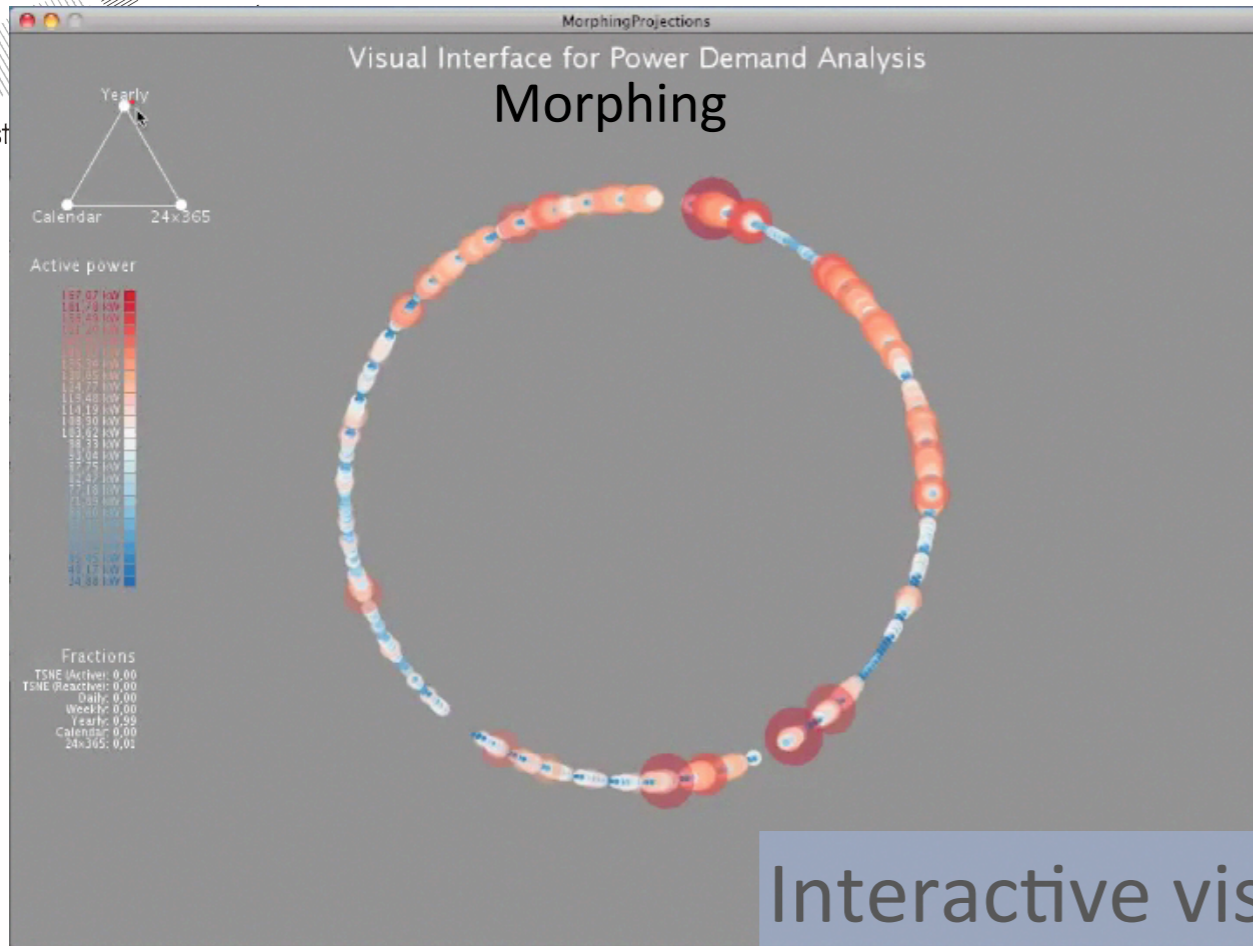
## morphing operation



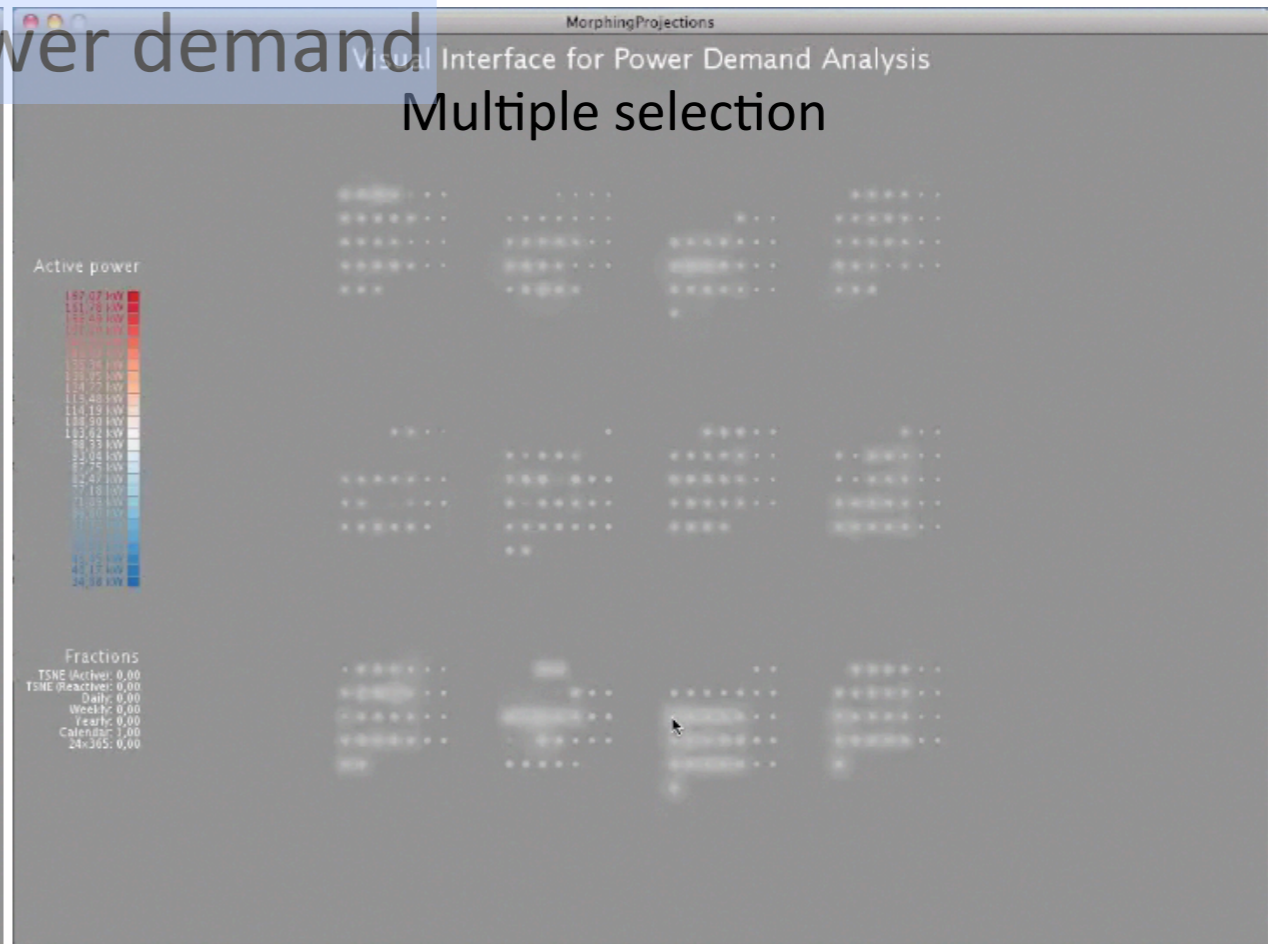
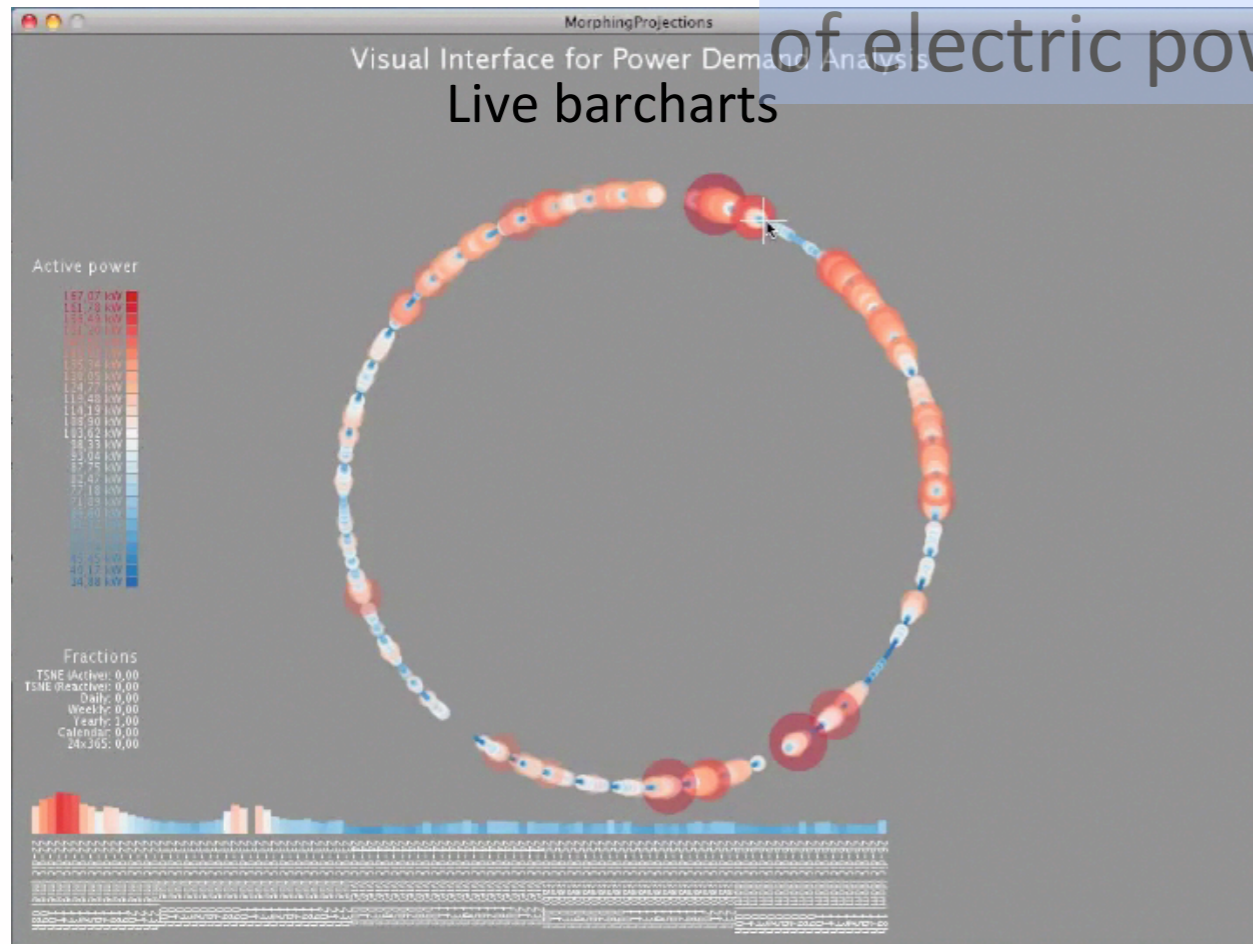
$$\mathbf{z}(i) = \lambda \mathbf{p}(i) + (1 - \lambda) \mathbf{q}(i)$$







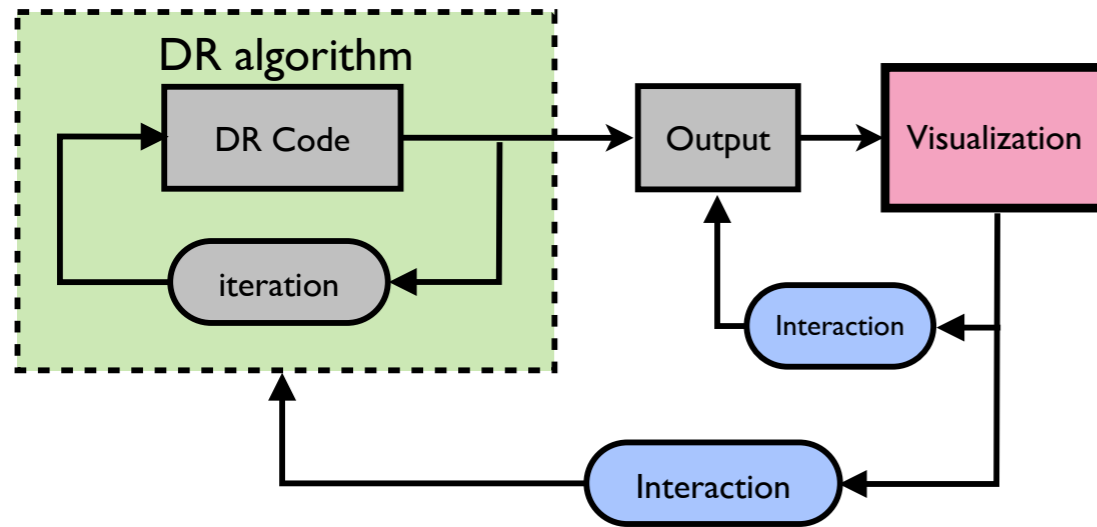
Interactive visualization of electric power demand



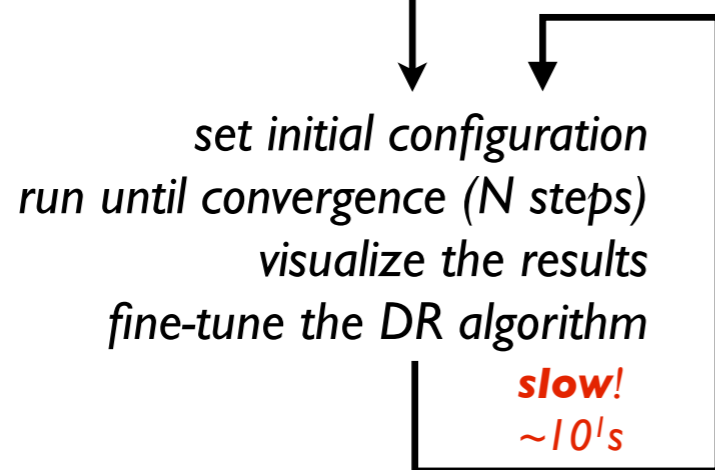


# Interactive Dimensionality Reduction (iDR)

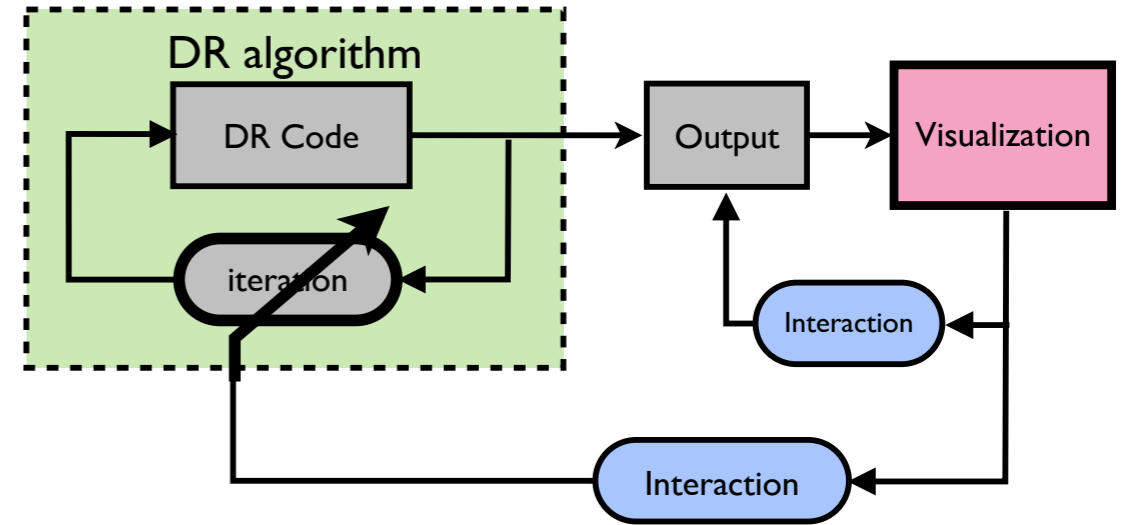
## plain DR



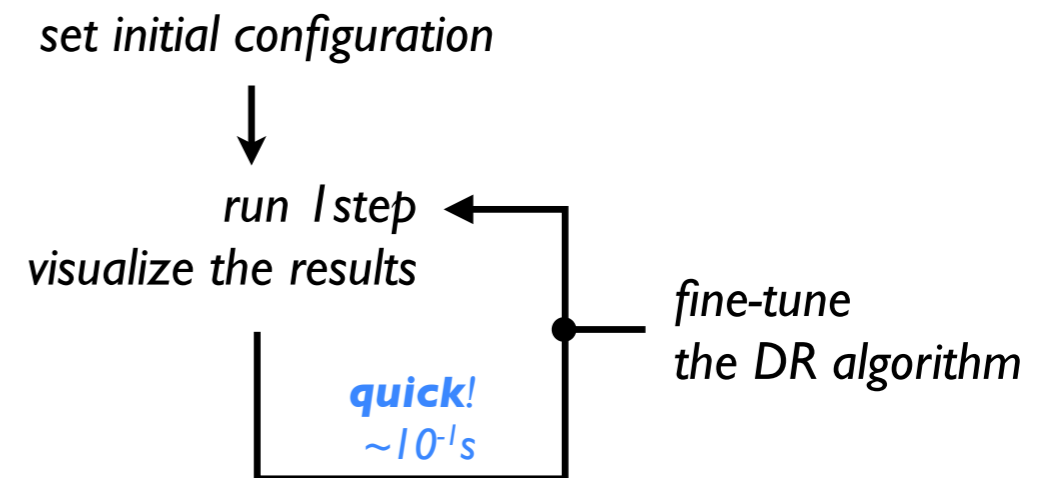
batch mode interaction scheme



## interactive DR



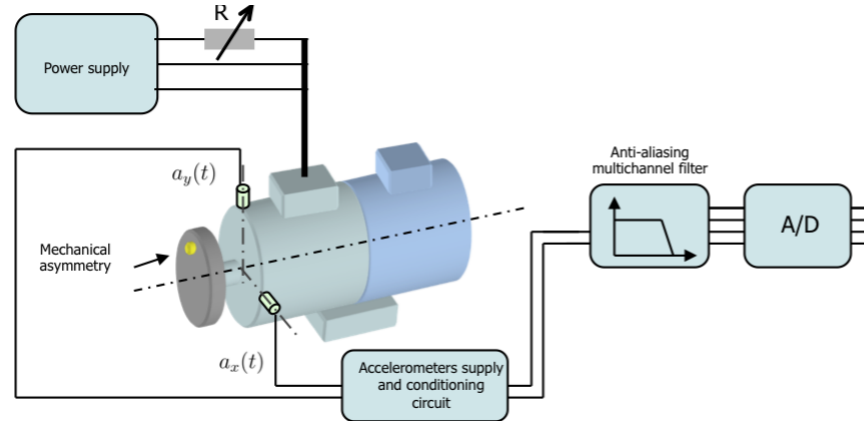
iDR interaction scheme



enables a quick feedback to the user  
 and hence a much better user integration  
 in the exploration process

# Interactive Dimensionality Reduction

## fault analysis of AC motor



### Application interface with iDR user-driven modification of the input metric space

Javascript application using processingjs (<http://processingjs.org>)

Analysis of three vibration signals  $a_x(t)$   $a_y(t)$   $a_z(t)$  and two phase currents  $i_R(t)$ ,  $i_S(t)$

of a 4kW 2 pole-pair asynchronous motor <http://isa.uniovi.es/~idiaz/demos/iDR-vibracionesMotor/>

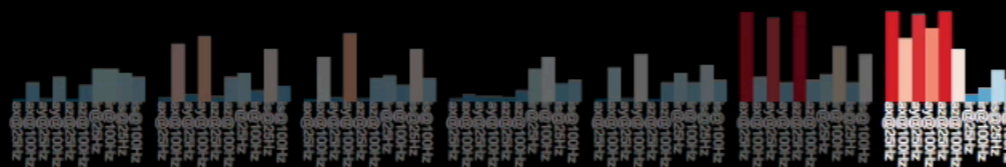
### Analítica Visual iDR

Análisis de vibraciones de un motor de inducción

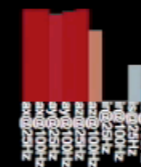
ax@25Hz  
 ax@100Hz  
 ay@25Hz  
 ay@100Hz  
 az@25Hz  
 az@100Hz  
 ir@25Hz  
 ir@100Hz  
 is@25Hz  
 is@100Hz



Patrones detectados



Patrón actual:  
 aMec + aElec



Pesos (arrastrar ratón)





Thank you for your attention!