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Design and Performance of the LHC beam-based Feedback Control Systems



- There and back again -

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27 km Circumference – 1232 LHC dipole magnet

- B field 8.3 T (11.8 kA) @ 1.9 K (super-fluid Helium)
- two-in-one magnet design:
 two beam tubes with an opening of 56 mm (210 mm separation)

Operating challenges:

• Very low quench levels (~ mJ/cm³) in an environment that stores $MJ \rightarrow GJ$

Control of particle beam stability and losses is paramount!



Traditional requirements on beam stability...

... to keep the beam in the pipe!

- LHC's increased stored intensity and energy much tighter requirements on beam stability:
 - 1. Capability to control particle losses
 - Machine protection (MP) & Collimation
 - Quench prevention
 - 2. Commissioning and operational efficiency



Beam 3 σ envel.

- FBs became a requirement for safe and reliable nominal LHC operation 1.8 mm @ 7 TeV
 - implications on controller reliability, availability and system integration



Combined failure¹: Local orbit bump and collimation efficiency (/kicker failure) → bumps may potentially compromise collimation function





LHC Feedback Operation – Example

Orbit feedback used routinely and mandatory for nominal beam



Most perturbations due to Orbit-FB reference changes around experiments



2009 LHC Commissioning

... somewhat a surprise: 3rd ramp without Tune-Feedback





- Feed-Forward: (FF)
 - Steer parameter using precise process model and disturbance prediction
- Feedback: (FB)
 - Steering using rough process model and measurement of parameter
 - Two types: within-cycle (repetition $\Delta t << 10$ hours) or cycle-to-cycle ($\Delta t > 10$ hours)





Orbit-Feedback as Prototype for all LHC Beam-Based Feedback Systems

- Orbit-Feedback is one of the largest and most complex LHC feedback:
 - 1088 BPMs \rightarrow 2176+ readings @ 25 Hz from 68 front-end computers
 - 530 correction dipole magnets/plane, distributed over ~50 front-end computers
 - Total >3500 devices involved
- Specific requirements fairly distributed opted for central global feedback system
- One central controller (OFC + hot spare):
 - higher numerical load
 - higher network load ($\leftrightarrow \sim 120$ front-ends)
 - dependence of machine operation on single device
 - easier synchronisation between front-ends and FBs
 - flexible correction scheme changes and gain-scheduling
 - most efficient to handle cross-talk and (de-)coupling between FBs





- Feedback Controller (OFC) performing actual feedback controller logic
 - Simple streaming task (10% of total load)
 - Beam data quality checks and real-time filtering (80% of total load)
 - Server running Real-Time Linux OS with periodic constant load
 - multi-core, highly redundant MTBF > 22 yrs (spec, 120 yrs meas.)
 - Technical Network as robust communication backbone
- Service Unit: Interface to high-level software control and interlock systems
 - Proxies user requests, handles asynchronous non-RT tasks





- Divide and Conquer' feedback controller design approach:
 - 1 Compute steady-state corrector settings $\vec{\delta}_{ss} = (\delta_{1,...,\delta_{n}})$ based on measured parameter shift $\Delta x = (x_{1,...,x_{n}})$ that will move the beam to its reference position for t $\rightarrow \infty$.
 - 2 Compute a $\vec{\delta}(t)$ that will enhance the transition $\vec{\delta}(t=0) \rightarrow \vec{\delta}_{ss}$
 - 3 Feed-forward: anticipate and add deflections $\vec{\delta}_{ff}$ to compensate changes domain of well known and properly described sources



feedback-path = measured beam parameter

(N.B. here G(s) contains the process and monitor response function)

space

domain

time



2014-06-02

Linear algebra theorem*:



 though decomposition is numerically more complex final correction is a simple vector-matrix multiplication:

$$\vec{\delta}_{ss} = \tilde{R}^{-1} \cdot \Delta \vec{x} \quad with \quad \tilde{R}^{-1} = \underline{V} \cdot \underline{\lambda}^{-1} \cdot \underline{U}^T \quad \Leftrightarrow \quad \vec{\delta}_{ss} = \sum_{i=0}^n \frac{a_i}{\lambda_i} \vec{v}_i \quad with \quad a_i = \vec{u}_i^T \Delta \vec{x}$$

- numerical robust, minimises parameter deviations Δx and circuit strengths δ
- Easy removal of singularities, (nearly) singular eigen-solutions have $\lambda_i \sim 0$
- to remove those solution: if $\lambda_i \approx 0 \rightarrow '1/\lambda_i := 0'$
- discarded eigenvalues corresponds to solution pattern unaffected by the FB

*G. Golub and C. Reinsch, "Handbook for automatic computation II, Linear Algebra", Springer, NY, 1971



Space Domain: LHC BPM eigenvector #50 λ_{50} = 6.69•10²





Space Domain: LHC BPM eigenvector #100 λ_{100} = 3.38•10²





Space Domain: LHC BPM eigenvector #291 λ_{291} = 2.13•10²





Space Domain: LHC BPM eigenvector #449 λ_{449} = 8.17•10¹





Space Domain: LHC BPM eigenvector #521 λ_{521} = 1.18•10°





- Initially: Truncated-SVD (set λ_i⁻¹:= 0, for i>N)
 - not without issues: removed λ_i allowed local bumps creeping in (e.g. collimation)
- Regularised-SVD (Tikhonov/opt. Wiener filter with $\lambda_i^{-1} := \lambda_i / (\lambda_i^2 + \mu), \mu > 0$)
 - more robust w.r.t. optics errors and mitigation of BPM noise/errors





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 $\vec{\delta}(t=0) \rightarrow \vec{\delta}_{ss}$



feedback-path = measured beam parameter

(N.B. here G(s) contains the process and monitor response function)

space

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domain



- Optimal control¹ for the 'small-signal response' yields classic PI-controller
 - − Single free parameter $\alpha > T... \infty$
 - facilitates trade-off between speed and robustness
 - adaptive gain-scheduling based on operational scenario



¹D. C. Youla et al., *"Modern Wiener-Hopf Design of Optimal Controllers"*, IEEE Trans. on Automatic Control,1976, vol. 21-1,pp. 3-13 & 319-338



Two non-linear effects that need to be addressed by the controller:

- Delays: computation, data transmission, dead-time, etc.
- Rate-Limiter: limited slew rate of corrector circuits (due to voltage limitations)
 - e.g. LHC: $\pm 60A$ converter: $\Delta I/\Delta t|_{max} < 0.5$ A/s





- Rate-limiter in a nut-shell:
 - additional time-delay $\Delta \tau$ that depends on the signal amplitude
 - secondary: introduces harmonic distortions





- Closed-loop bandwidth and phase margin depend on the excitation amplitude:
 - + non-linear phase once rate-limiter is in action...





Functional Description of the LHC Feedback Controller PID Controller & Delays + Rate-Limiter

- In essence, the functional OFC description
 - $G(s) = \underbrace{e}_{\tau s+1} G_{NL}(s)$
 - T: the power converter time constant and
 - → Smith-Predictor and Anti-Windup paths:





$$T(s) = F_Q(s) \cdot e^{-\lambda s} G_{NL}(s)$$





Motivation for Delay and Rate-Limiter Compensation Example: LHC orbit (Q,Q',C⁻, ...) feedback control





To avoid inherent Cross-Talk between FBs... ... Cascading between individual Feedbacks

- Main strategy: derive measurement from FB control variable
 - Q'-tracker using 'Q_{raw} = Q_{meas} Q_{trim}'
 - Sub. Δp/p-mod. from Radial-Loop & Orbit-FB reference







Common Feedback/Feed-forward Control Layout Control implementation split into two sub-systems:

- LHC feedback systems most visible faces are:
 - Feedback Controller (OFC): actual feedback controller logic
 - Service Unit (OFSU): Interface to control system/the world
- However 3500+ devices (~130 FE) and many technical services
 - Overall strength depends on the reliability of the weakest link







Control Paradigms III/III Digital Control System & 'Real-Time'

- LHC feedbacks are 'firm real-time systems'
 - some (limited) margin on occasional missing data
 - additional latencies are critical for loop stability

 $\Delta \varphi = 2 \pi f_{bw} \cdot \Delta t_{delay}$

• "How much phase stability is required (i.e. @1 Hz)?"



dead-line

latency

total system failure (dump)

utility



Two main strategies:

- actual delay measurement and dynamic compensation in SP-branch:
 - only feasible for small systems
- Jitter compensation using a periodic external signal:
 - CERN wide synchronisation of events on sub ms scale
 - The total jitter, the sum of all worst case delays, must stay within "budget".
 - feedback loop frequency of 50 Hz feasible for LHC, if required...





- TechNet round-trip tests: difference between standard and RT-Linux Kernel
 - Important: measure probability & upper-bound (worst-case) latency





Snapshot of the day with removed mains harmonics





Measurement drifts ~100 um/h w/o significant temperature changes
 Orbit-FB may convert these measurement errors into real orbit shift



now mitigated by temperature controlled racks



LHC Feedback Operation

Trims became de-facto standard to assess the FB and machine performance





LHC Feedback ... one of the more visible systems in the CCC – Importance of Controls Integration and SW Usability





Earth Tides dominating Orbit Stability during Physics:

• Known effect from LEP \rightarrow changes the machine circumference/energy







Summary

- Generally, feedback performed their designed job.
- Pushing LHC machine parameter envelope also implied increased performance constraints on Feedback operation (notably orbit stability during squeeze)
 will improve FB sub-systems to keep up with LHC progress post-LS1
- Main paradigms:
 - Split 'space/time' domain design to leverage different user background experiences
 - Nested-loop design to minimise inter-loop cross-talk
 - Central simple input-processing-output feedback controller
 - Managed by service unit (OFSU, settings management, data proxy)
 - LHC Technical-Network as communication backbone
 - 'Firm real-time' constraints using Real-Time capable Linux



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From Decay/Snap-back expected dynamic perturbations

| | Orbit | Tune | Chroma. | Energy | Coupling |
|---------------------------|--------|---------|---------|----------|----------|
| | [0] | | [units] | [Δρ/ρ] | [0_] |
| Exp. Perturbations ('06): | ~ 0.5 | 0.014 | ~ 70 | ± 1.5e-4 | ~0.01 |
| Nom. Requirements: | ± 0.15 | ±0.001 | 2 ± 1 | ± 1e-4 | « 0.01 |
| Achieved Stability ('13): | ~ 0.1 | ~ 0.001 | ± 2 (7) | ~1e-5 | < 0.003 |

- Initial assumptions and plans (2006-2009):
 - Chromaticity considered as most critical parameter
 - FB Priority list: Chromaticity \rightarrow Coupling/Tune \rightarrow Orbit \rightarrow Energy
- What turned out to be needed operationally
 - 2009 \rightarrow 2011: <u>Tune</u> \rightarrow Orbit & Energy/Radial-Loop \rightarrow Q'(t) $\rightarrow ... \rightarrow C^{-}$
 - impressive Q'(t), C⁻ and beta-beat stability/reproducibility
 - In 2012: Orbit & Tune (snap-back, instabilities)
 - Higher energy & smaller- $\beta^* \rightarrow$ much tighter collimator settings \rightarrow convert smallest orbit deviations into losses/dumps



- Separates specific accelerator physics from specific control theory
 - can test the two domains independently
 - ample expertise/resources in one but not the other domain
 - \rightarrow KISS principle: keep it simple and safe
 - Multiple-Input-Multiple-Output (MIMO) in space-domain
 - Can modify correction algorithm without having to worry about whether overall loop remains stable
 - Maintains physical meaning of the individual control variables
 - Basically relying on inversion of response matrices \rightarrow SVD
 - Quasi-Single-Input-Single Output (SISO) in time-domain
 - Similar control problem/laws as e.g. for power converters
 - Time-domain controller identical for orbit, energy, Q/Q' vs. integrated/more complex 'Kalman' or 'Youla-Kucera-Klein'-based method



Time-Domain: Optimal Controller Design Youla's affine parameterisation II/II

Using Youla's method: "design closed loop in a open loop style":

Youla showed¹ that all stable closed loop controllers D(s) can be written as:

$$D(s) = \frac{Q(s)}{1 - Q(s)G(s)} \tag{1}$$

Example: first order system

$$G(s) = \frac{\kappa_0}{\tau s + 1} \quad \text{with } \tau \text{ being the circuit time constant}$$
(2)
sing for example the following ansatz:

Us

$$Q(s) = F_Q(s)G^i(s) = \frac{1}{\alpha s+1} \cdot \frac{\tau s+1}{K_0}$$
(3)
Response/optimality can be directly deduced by construction of F₀(s)

 $G^{i}(s)$, pseudo-inverse of the nominal plant G(s)

 $\rightarrow T_0(s) = \frac{1}{\alpha s + 1}$

(1)+(2)+(3) yields the following PI controller:

$$D(s) = K_P + K_i \frac{1}{s}$$
 with $K_p = K_0 \frac{\tau}{\alpha} \wedge K_i = K_0 \frac{1}{\alpha}$

¹D. C. Youla et al., "Modern Wiener-Hopf Design of Optimal Controllers", IEEE Trans. on Automatic Control, 1976, vol. 21-1, pp. 3-13 & 319-338



- Tune-FB driving and accelerating early commissioning in 2009-2011
 - Tunes kept stable to better than 10^{-3} for most part of the ramp and squeeze





Feed-Forward Back-Bone – Field-Description for LHC (FiDeL) Example: b₃ – Compensation – Static Part





Control Paradigms II/III

• Machine imperfections cause steady-state offset ε_{ss} and scale error ε_{scale} :

$$\Delta x(s) = R_i(s) \cdot \delta_i \rightarrow \Delta x(s) = R_i(s) \cdot (\epsilon_{ss} + (1 + \epsilon_{scale}) \cdot \delta_i)$$



 Uncertainties and scale error of beam response function affects convergence speed (= feedback bandwidth) rather than achievable stability



- Feed-forward of Q'(t)-Feedback signal for next fill turned out to be sufficient!
 - enforced by strict pre-cycling following physics, access or circuits 'off '...





- Closed-loop bandwidth and phase margin depend on excitation amplitude:
 - + non-linear phase once rate-limiter kicks in...





Orbit Stability during β*-Squeeze

Losses and orbit movement at H-TCP.C6R7.B2 well correlated



- Maximum drift rates of 40 um/s \rightarrow (close to) limit of Orbit-FB at 4 TeV
 - Underpinned by FB instability observation for 5x bandwidth increase
- At this speed, OFC needs to operate with correct optics



Bandwidth modifier w.r.t. eigenvalue index (<1 more stable, >1 diminishes stability margin)





Quirky side effect:

Machine circumference changes are propagated via Q' also to the tune



- Probably the slowest high-precision Q' measurement in the World
 - Short-Term Tune-Stability of ~10⁻⁶!
- However, stability during nominal physics operation is typically driven by impedance and beam-beam related effects.



Typical Q/Q'(t) Control Room View 2010 Statistics: Out of 191 Ramps...



- ... 155 ramps with > 99% transmission, 178 ramps with > 97% transmission
- ... only 12 ramps lost with beam (6 with Tune-FB during initial 3.5 TeV comm.)
- ... "if without FBs": 83 crossings of 3^{rd} , 4^{th} or C⁻ resonance, 157 exceeded $|\Delta Q|$ >0.01
- Impressive performance for the first year of operation and low-ish intensities:

FB Beam Control@LHC, Ralph.Steinhagen@CERN.ch, Advanced Control Engineering, 2014-06-02



Control Paradigms III/III Digital Control System & 'Real-Time'

- ... "A system is said to be real-time if the total correctness of an operation depends not only upon its logical correctness, but also upon the time in which it is performed. [..] are classified by the consequence of missing a deadline:
 - Hard Missing a deadline is a total system failure.
 - Firm Infrequent deadline misses are tolerable, but may degrade the system's quality of service. The usefulness of a result is zero after its deadline.
 - Soft The usefulness of a result degrades after its deadline, thereby degrading the system's quality of service."





- 1. "There is no science in real-time-system design"
- 2. "Advances in supercomputer hardware will take care of RT requirements."
- 3. "[..] is equivalent to fast computing."
- 4. "[..] research is performance engineering."
- 5. "[..] systems function in a static environment."
- 6. "[..] is assembly coding, priority IRQ programming, and device driver writing."
- 7. "[..] all been solved in other areas of computer science or operations research."
- 8. "It is not meaningful to talk about guaranteeing RT performance, because we cannot guarantee that the hardware will not fail and the software is bug free or that the actual operating conditions will not violate the specific design limits."
- Obviously, the above is wrong but seems to be sometimes forgotten when discussing the specific technical implications.