

Electroweak boson production in double parton scattering

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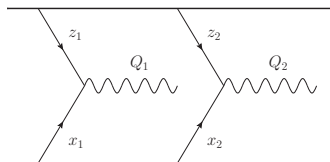
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- ▶ We study W^+W^- and Z^0Z^0 electroweak boson production in double parton scattering (DPS) .
- ▶ We use the QCD evolution equations for double parton distribution functions (DPDFs) in our studies.
- ▶ In particular, we are interested in the impact of splitting terms in the evolution equations on the DPS cross sections.

- ▶ Double parton scattering and DPDF
- ▶ QCD evolution equations for DPDF and their solution
- ▶ Relative transverse momentum dependence of DPDF
- ▶ Electroweak boson production in DPS
- ▶ The role of the single splitting contribution
- ▶ Summary

Double parton scattering



- ▶ DPS cross section in collinear approximation

$$\sigma_{AB} = \frac{N}{2} \sum_{f_1 f_2 f'_1 f'_2} \int dx_1 dx_2 dz_1 dz_2 \frac{d^2 \mathbf{q}}{(2\pi)^2} D_{f_1 f_2}(x_1, x_2, Q_1, Q_2, \mathbf{q})$$
$$\times \hat{\sigma}_{f_1 f'_1}^A(Q_1) \hat{\sigma}_{f_2 f'_2}^B(Q_2) D_{f'_1 f'_2}(z_1, z_2, Q_1, Q_2, -\mathbf{q})$$

- ▶ Double parton distribution functions (DPDF) in a hadron

$$D_{f_1 f_2}(x_1, x_2, Q_1, Q_2, \mathbf{q}), \quad 0 < x_1 + x_2 \leq 1$$

- ▶ \mathbf{q} is a relative transverse momentum of two partons.

QCD evolution equations

- ▶ For equal hard scales and zero relative transverse momentum

$$D_{f_1 f_2}(x_1, x_2, t) \equiv D_{f_1 f_2}(x_1, x_2, Q, Q, \mathbf{q} = 0)$$

- ▶ Evolution equations in LLA

$$\begin{aligned} \partial_t D_{f_1 f_2}(x_1, x_2, t) &= \sum_{f'} \int_{x_1}^{1-x_2} \frac{du}{u} P_{f_1 f'}\left(\frac{x_1}{u}\right) D_{f' f_2}(u, x_2, t) \\ &+ \sum_{f'} \int_{x_2}^{1-x_1} \frac{du}{u} P_{f_2 f'}\left(\frac{x_2}{u}\right) D_{f_1 f'}(x_1, u, t) \\ &+ \frac{1}{x_1 + x_2} \sum_{f'} P_{f' \rightarrow f_1 f_2}\left(\frac{x_1}{x_1 + x_2}\right) D_{f'}(x_1 + x_2, t) \end{aligned}$$

+ DGLAP evolution equations for single PDFs $D_f(x, t)$.

- ▶ Evolution parameter

$$t \equiv t(Q) = \int_{Q_0^2}^{Q^2} \frac{\alpha_s(\mu^2)}{2\pi} \frac{d\mu^2}{\mu^2}$$

Evolution equations for Mellin moments

- ▶ For Mellin moments (in flavour matrix notation)

$$\tilde{D}(n_1, n_2, t) = \int_0^1 dx_1 \int_0^1 dx_2 x_1^{n_1} x_2^{n_2} \Theta(1 - x_1 - x_2) D(x_1, x_2, t)$$
$$\tilde{D}(n, t) = \int_0^1 dx x^n D(x, t)$$

and matrices of anomalous dimensions

$$\gamma_n = \int_0^1 dx x^n P(x), \quad \tilde{\gamma}_{n_1 n_2} = \int_0^1 dx x^{n_1} (1-x)^{n_2} P(x)$$

- ▶ Non-homogeneous first order linear differential equations

$$\partial_t \tilde{D}(n_1, n_2, t) = \underbrace{\gamma_{n_1} \tilde{D}(n_1, n_2, t) + \tilde{D}(n_1, n_2, t) \gamma_{n_2}^T}_{\text{homogeneous}} + \underbrace{\tilde{\gamma}_{n_1 n_2} \tilde{D}(n_1 + n_2, t)}_{\text{non-hom.}}$$

Solution to evolution equations

- ▶ Solution = General solution to homogenous equation
+ Particular solution to non-homogeneous equation.

$$\begin{aligned}\tilde{D}(n_1, n_2, t) &= e^{\gamma_{n_1} t} \tilde{D}_0(n_1, n_2) e^{\gamma_{n_2}^T t} \\ &+ \int_0^t dt' e^{\gamma_{n_1}(t-t')} \tilde{\gamma}_{n_1 n_2} \tilde{D}(n_1 + n_2, t') e^{\gamma_{n_2}^T (t-t')}\end{aligned}\quad (1)$$

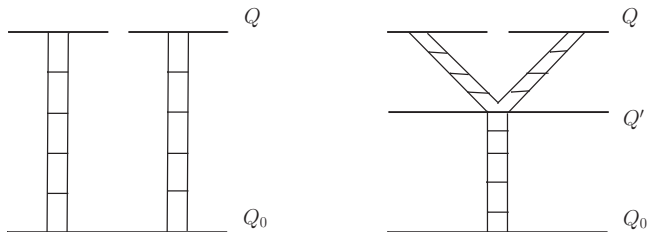
+ solution for single PDF

$$\tilde{D}(n, t) = e^{\gamma(n) t} \tilde{D}_0(n)$$

- ▶ Need to impose initial conditions $\tilde{D}_0(n_1, n_2)$ and $\tilde{D}_0(n)$ at $t = 0$.
(Gaunt, Stirling 2009)

Graphical illustration

- ▶ Solution (1) is the sum of two terms

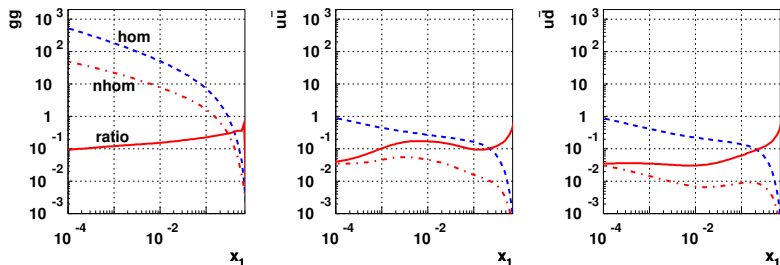


$$D(x_1, x_2, Q) = D^{(hom)}(x_1, x_2, Q) + D^{(nhom)}(x_1, x_2, Q)$$

- ▶ Two partons from a hadron + two partons from **splitting** of a point like parton.

Numerical solution

Plots of $x_1 x_2 D_{f_1 f_2}(x_1, x_2, Q)$ for fixed $x_2 = 10^{-2}$ and $Q^2 = 10^3 \text{ GeV}^2$



For $x_1, x_2 < 10^{-1}$, the splitting part of the solution is significantly smaller

$$\frac{D^{(nhom)}}{D^{(hom)}} \sim 10^{-1}$$

Relative transverse momentum dependence

- ▶ Homogeneous solution with the factorized \mathbf{q} -dependence:

$$\tilde{D}^{(1)}(n_1, n_2, t, \mathbf{q}) = \tilde{D}^{(hom)}(n_1, n_2, t) F_{2g}^2(\mathbf{q})$$

with two-gluon nucleon form factor (Blok, Dokshitzer, Frankfurt, Strikman 2009)

$$F_{2g}(\mathbf{q}) = \frac{1}{(1 + \mathbf{q}^2/m_g^2)^2}$$

where m_g - effective gluon mass. **Strong suppression** for $\mathbf{q}^2 \gg m_g^2$.

- ▶ Splitting part of the solution with modified lower integration limit

$$\tilde{D}^{(2)}(n_1, n_2, t, \mathbf{q}) = \int_{t(\mathbf{q})}^t dt' e^{\gamma_{n_1}(t-t')} \tilde{\gamma}_{n_1 n_2} \tilde{D}(n_1 + n_2, t') e^{\gamma_{n_2}^T(t-t')}$$

- ▶ **No form factor suppression** due to splitting from a point-like parton.

Relative transverse momentum dependence

- ▶ The general form of the DPDFs in the x-space

$$D(x_1, x_2, Q, \mathbf{q}) = \underbrace{D^{(1)}(x_1, x_2, Q, \mathbf{q})}_{\text{strongly suppressed}} + \underbrace{D^{(2)}(x_1, x_2, Q, \mathbf{q})}_{\text{not suppressed}}$$

- ▶ DPS cross section can be written as the sum (Ryskin, Snigirev 2011)

$$\sigma_{AB} = \sigma_{AB}^{(11)} + \sigma_{AB}^{(12+21)} + \sigma_{AB}^{(22)}$$

where

$$\begin{aligned} \sigma_{AB}^{(ij)} &= \frac{N}{2} \sum_{f_i, f'_i} \int dx_1 dx_2 dz_1 dz_2 \frac{d^2 \mathbf{q}}{(2\pi)^2} D_{f_1 f_2}^{(i)}(x_1, x_2, Q, \mathbf{q}) \\ &\times \hat{\sigma}_{f_1 f'_1}^A(Q) \hat{\sigma}_{f'_2 f_2}^B(Q) D_{f'_1 f'_2}^{(j)}(z_1, z_2, Q, -\mathbf{q}) \end{aligned}$$

- ▶ We do not consider $\sigma_{AB}^{(22)}$ (two splitting contribution) - Jo Gaunt talk.

Electroweak boson production in DPS

- ▶ **Pocket formula** for DPS cross section for W^+W^- production

$$\frac{d^2\sigma_{W^+W^-}}{dy_1 dy_2} = \frac{1}{\sigma_{\text{eff}}} \frac{d\sigma_{W^+}}{dy_1} \frac{d\sigma_{W^-}}{dy_2}$$

with $\sigma_{\text{eff}} \approx 15$ mb and single scattering cross sections

$$\frac{d\sigma_{W^\pm}}{dy_{1,2}} = \frac{2\pi G_F}{3\sqrt{2}} \frac{M_W^2}{s} \sum_{qq'} |V_{qq'}|^2 \{q(x_{1,2}) \bar{q}'(z_{1,2}) + \bar{q}(x_{1,2}) q'(z_{1,2})\}$$

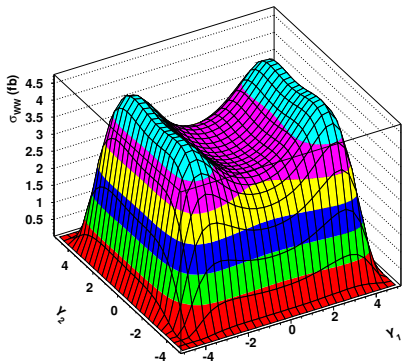
and parton momentum fractions

$$x_{1,2} = \frac{Q}{\sqrt{s}} e^{y_{1,2}}, \quad z_{1,2} = \frac{Q}{\sqrt{s}} e^{-y_{1,2}}$$

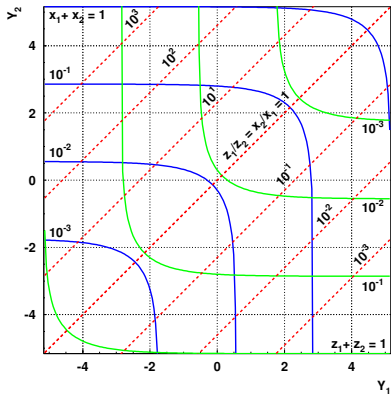
- ▶ PDFs are taken at the hard scale $Q = M_W$ and $\sqrt{s} = 14 \text{ TeV}^2$

Pocket formula results

W^+W^- cross section



W^+W^- rapidity plane



- ▶ Standard contribution

$$\frac{d\sigma^{(11)}}{dy_1 dy_2} = \frac{m_g^2}{28\pi} \sigma_{hard}^2 D^{(1)} \times D^{(1)}$$

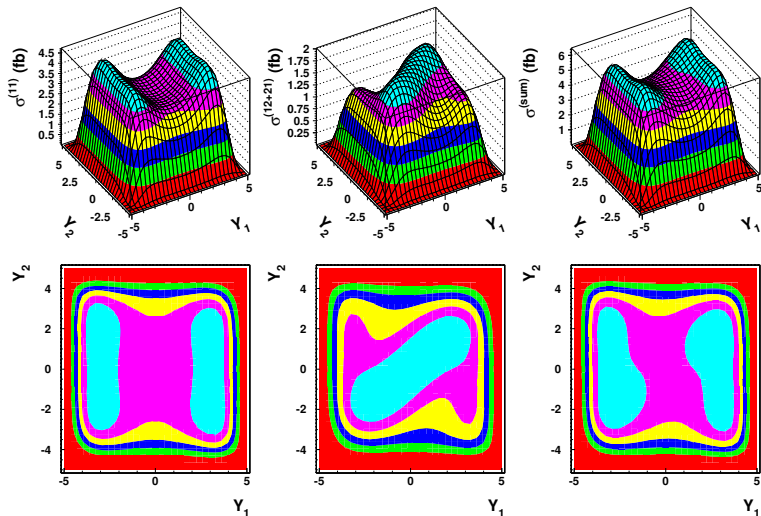
- ▶ Single splitting contribution

$$\frac{d\sigma^{(12+21)}}{dy_1 dy_2} = \frac{m_g^2}{12\pi} \sigma_{hard}^2 \left\{ D^{(1)} \times D^{(2)} + D^{(2)} \times D^{(1)} \right\}$$

- ▶ Prefactors from integration of F_{2g}^4 and F_{2g}^2 , respectively, over \mathbf{q} .
- ▶ We use $m_g = 1.5$ GeV to get $\sigma_{\text{eff}} \approx 15$ mb.
- ▶ DPDFs from numerical solutions to the evolution equations.

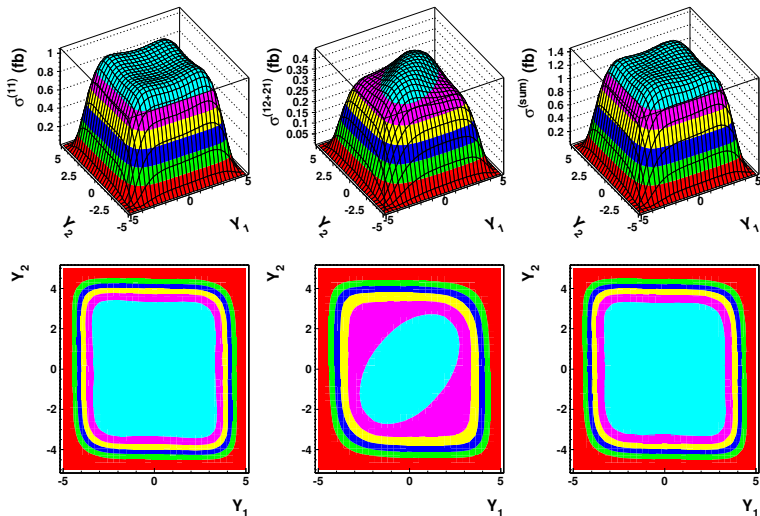
Analysis with evolution equations

W^+W^- production from DPS



Analysis with evolution equations

$Z^0 Z^0$ production from DPS



Single splitting contribution

- ▶ The single splitting contribution is important.
- ▶ Contribution to the total DPS cross sections is sizable.

in [fb]	$\sigma_{tot}^{(11)}$	$\sigma_{tot}^{(12+21)}$	$\sigma_{tot}^{(12+21)} / \sigma_{tot}^{(11)}$
W^+W^-	256	97	0.38
Z^0Z^0	61	22	0.36

- ▶ It changes the correlation pattern in rapidity for W^+W^- production in DPS.

Single splitting contribution

- ▶ Its significance can also be illustrated in terms of the effective cross section

$$\sigma_{\text{eff}} = \frac{N}{2} \frac{(d\sigma_A/dy_1)(d\sigma_B/dy_2)}{d\sigma_{AB}/dy_1 dy_2}$$

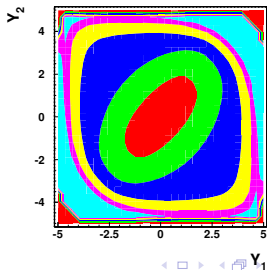
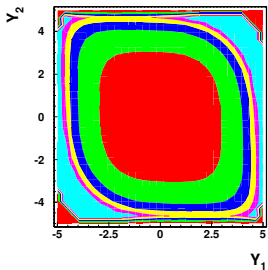
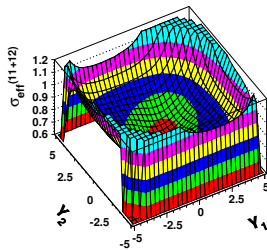
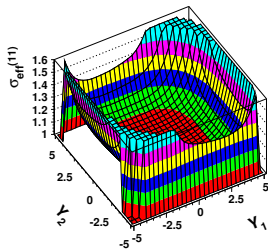
for two cases:

$$\sigma_{AB} = \sigma_{AB}^{(11)} \qquad \sigma_{AB} = \sigma_{AB}^{(11)} + \sigma_{AB}^{(12+21)}$$

- ▶ σ_{eff} is a function of boson rapidities: $\sigma_{\text{eff}}(y_1, y_2)$.

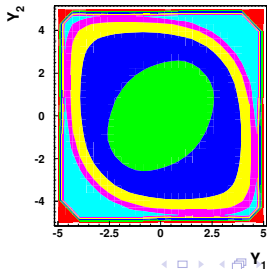
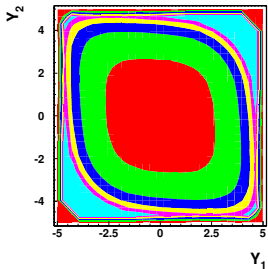
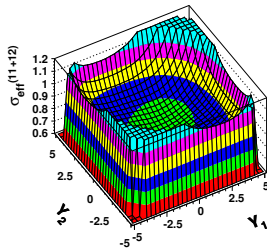
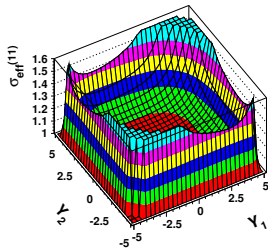
σ_{eff} for W^+W^- production

σ_{eff} in units of 15 mb for W^+W^-



σ_{eff} for $Z^0 Z^0$ production

σ_{eff} in units of 15 mb for $Z^0 Z^0$



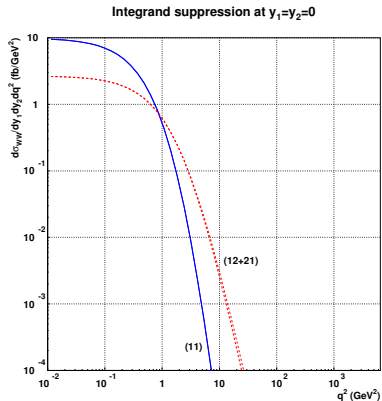
Summary

- ▶ The W^+W^- and Z^0Z^0 electroweak boson production in DPS has been studied in detail with the evolution equations for DPDFs.
- ▶ The significance of the single splitting contribution to DPS cross sections has been quantified.
- ▶ The single splitting contribution contributes up to 40 % to standard analyses.
- ▶ The single splitting contribution changes the standard correlation in rapidity of the produced W^+W^- bosons in DPS.

Backup slides

Single splitting contribution

$$\frac{d\sigma_{W^+W^-}^{(ij)}}{dy_1 dy_2 dq^2} \text{ as a function of } \mathbf{q}^2 \text{ for } y_1 = y_2 = 0$$



Modification of the lower integration limit in $D^{(nhom)}$ unimportant.

Single splitting contribution

The single splitting contribution is less suppressed with rising \mathbf{q}^2 due to single form factor F_{2g}^2 in comparison to the double form factor F_{2g}^4 in the no splitting contribution. Thus from \mathbf{q} -dependence

$$\sigma^{(12+21)} : \sigma^{(11)} = 2.33 : 1$$

But

$$\frac{d\sigma_{W^+W^-}^{(11)}}{dy_1 dy_2} = \frac{m_g^2}{28\pi} DPDF^{(1)} \cdot DPDF^{(1)}$$

$$\frac{d\sigma_{W^+W^-}^{(12+21)}}{dy_1 dy_2} = \frac{m_g^2}{12\pi} \left\{ DPDF^{(1)} \cdot DPDF^{(2)} + DPDF^{(2)} \cdot DPDF^{(1)} \right\}$$

and the splitting part $DPDF^{(2)}$ is much smaller ($\sim 10^{-1}$) than the homogeneous part $DPDF^{(1)}$. Thus $\sigma^{(11)}$ wins.