

# Methods for <sub>sub-</sub>micron beam size measurements in circular accelerators

Enrico Bravin  
CERN

ALERT 2014, May 5-6, IFIC, Valencia, Spain

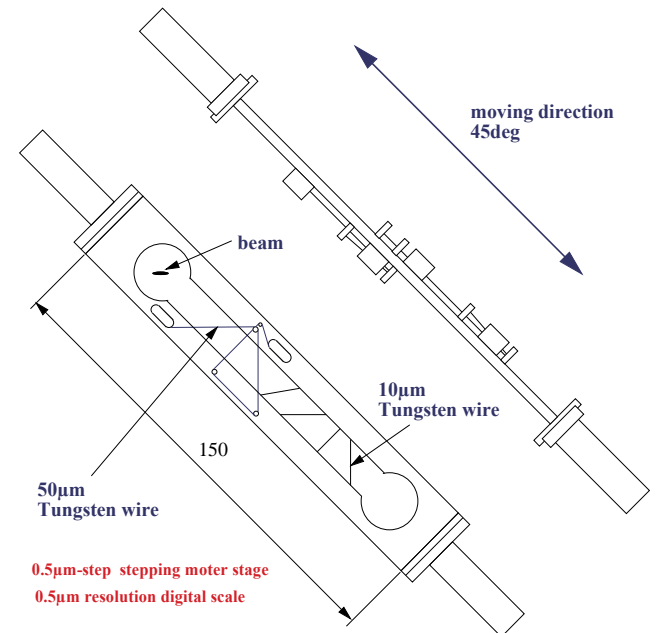
# Introduction

- Interceptive methods
  - Wire scanner
  - Screen imaging (OTR, YAG etc.)
  - Screen interferometry
- Non intercepting
  - Synchrotron radiation imaging
  - Synchrotron radiation interferometry
  - Diffraction radiation
  - Laser wire scanner

# Wire scanner

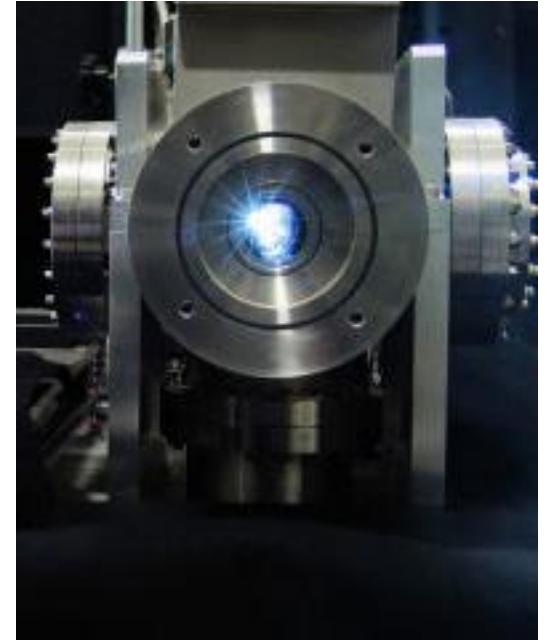
- Used as reference in many particle accelerators
- Few microns resolution achieved (SLC, ATF) on LINAC or transfer line [1]
- Difficult to use in rings due to wire damage

Ex.: for a 4  $\mu\text{m}$  carbon wire moving at 1 m/s in a ring with rev. time of 1  $\mu\text{s}$  and beam of  $\sigma_{x,y}$  of 10  $\mu\text{m}$  the limit is around  $10^9$  particles [2]



# Synchrotron radiation

- Widely used for online monitoring of beam parameters in electron/positron rings
- Radiation generated in all bending magnets
- Need only an extraction viewport and an adequate optical system to obtain the image of the beam
- In most rings however the emitted radiation is diffraction limited

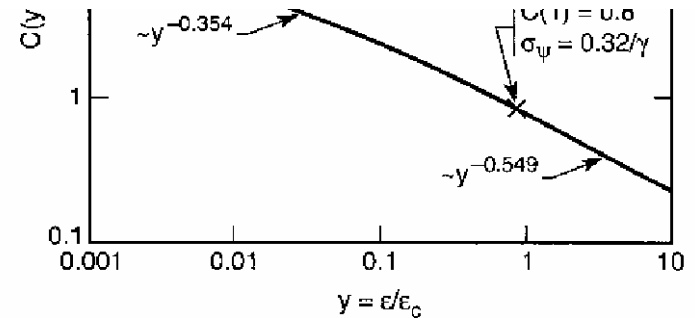
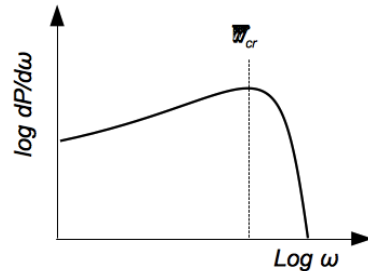
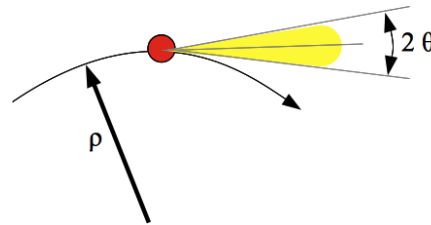


# Synchrotron radiation imaging

$$P = \frac{1}{4\pi\epsilon_0} \frac{2}{3} \frac{ce^2\gamma^4}{\rho^2}$$

$$\omega_{cr} = \frac{3}{2} \frac{c\gamma^3}{\rho}$$

$$\sigma_\theta = \frac{2}{\gamma\sqrt{2\pi}} C(y)$$



2-3. The function  $C(y)$ . The limiting slopes, for  $E/E_c \ll 1$  and  $E/E_c \gg 1$ , are indicated.

where  $\sigma_\psi$  is given by

$$\sigma_\psi = \frac{2}{\gamma\sqrt{2\pi}} C(y) = 0.408 \frac{C(y)[\text{mrad}]}{E[\text{GeV}]} \quad (7)$$

X-Ray data booklet

## Diffraction limit

$$\sigma_{diff} \simeq 1.22 \frac{\lambda}{8\sigma_\theta}$$

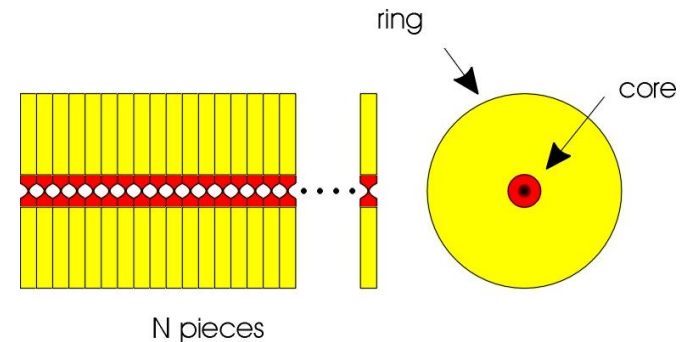
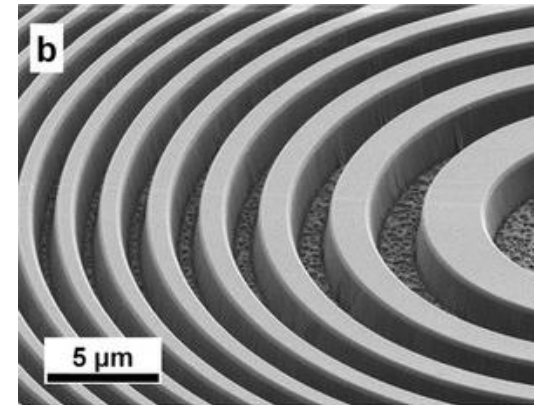
For  $E = 2 \text{ GeV}$  ( $\gamma \sim 4000$ )  $\lambda = 400 \text{ nm}$  and  $\rho = 10 \text{ m}$   
 $E_{cr} = 1.7 \text{ keV}$   
 resolution is around  $25 \text{ } \mu\text{m}$  ( $240 \text{ } \mu\text{m}$  using  $1/\gamma$ )

# X-rays imaging

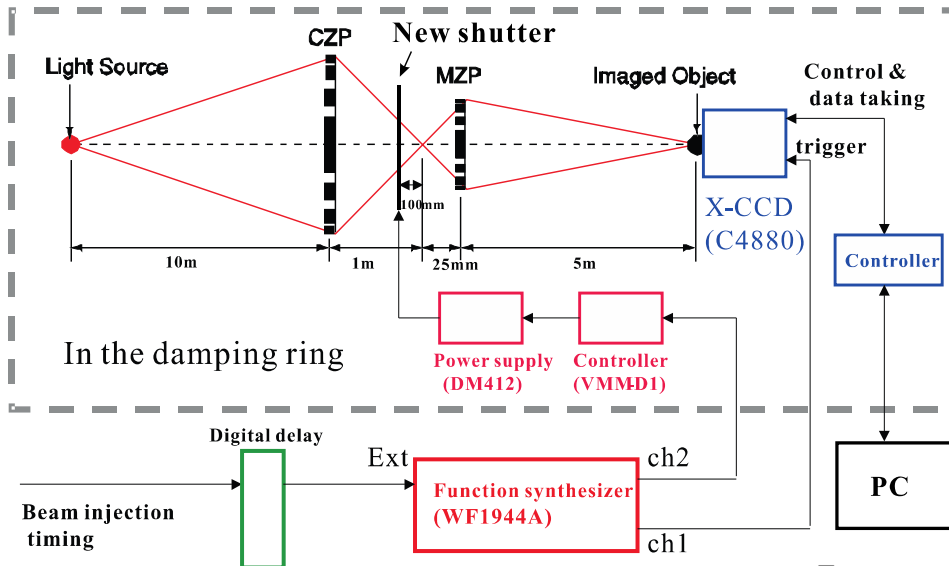
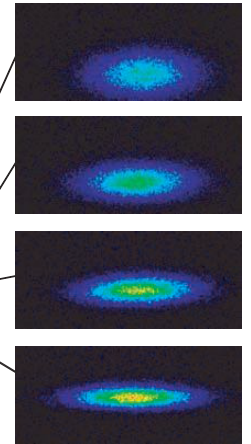
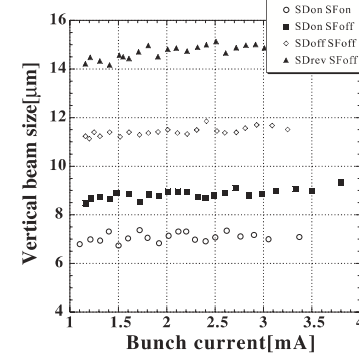
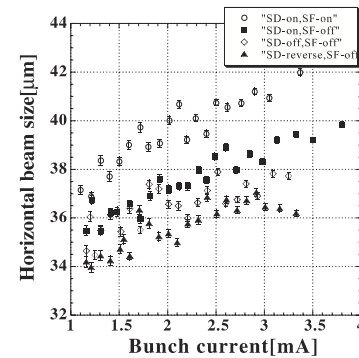
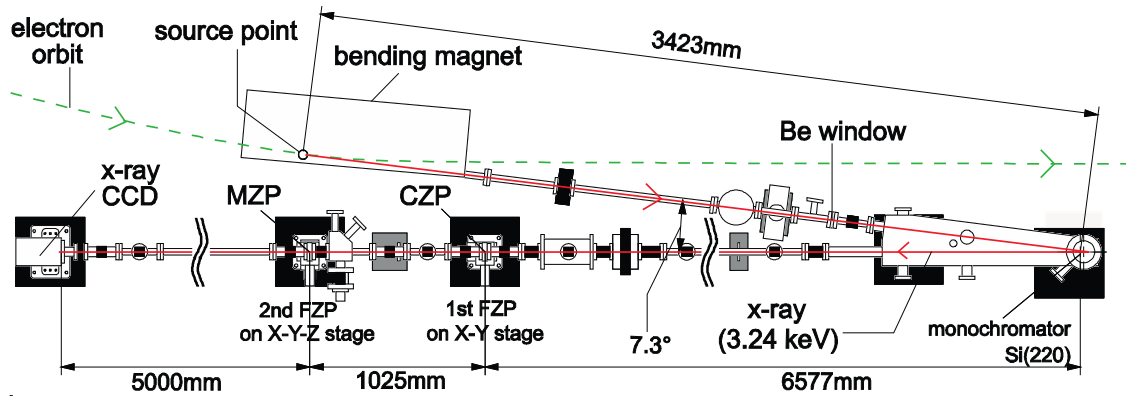
- Reducing the wavelength we can improve the diffraction limit

For  $E= 2\text{GeV}$  ( $\gamma= 4000$ )  $\rho= 10\text{ m}$   
and  $\lambda= 0.4\text{ nm}$  (3 keV) the diffraction limit is around  $0.5\ \mu\text{m}$

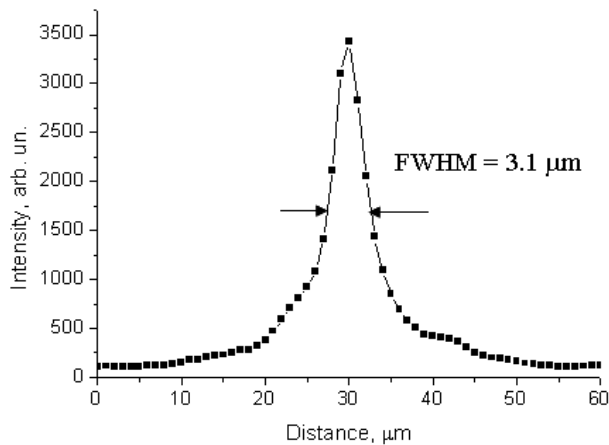
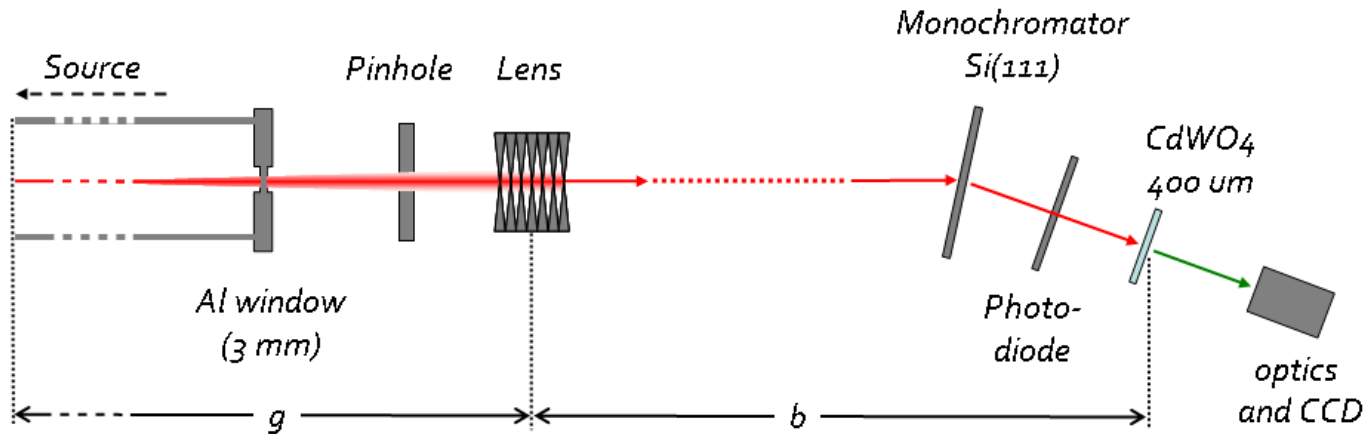
- Still need an optical system for X-rays with very good optical properties
- Fresnel plates
- Compound refractive lenses
- Pin-hole



# SR imaging using FZP at ATF [3]



# SR imaging at ESRF [4]



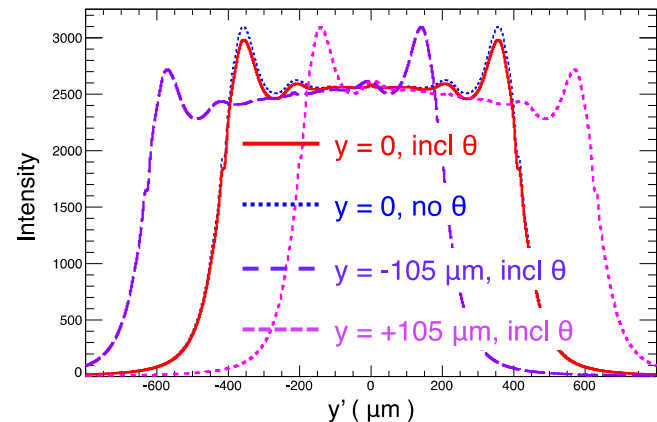
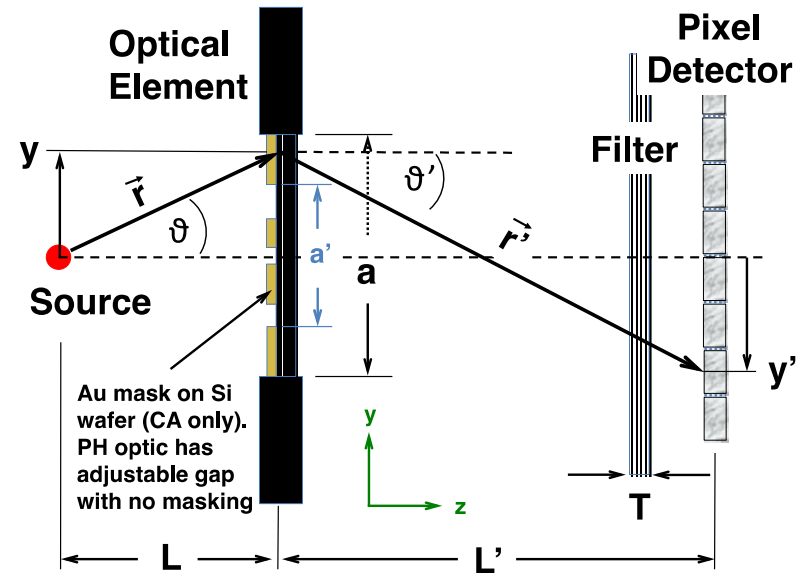
Vertical beam profile obtained with 12.5 keV photons and 5 Al lenses of 49 $\mu\text{m}$  curvature radius

29 lenses are used at 45.6 keV for a focal length of 3.3 m



# SR imaging at CeSR-TA [5]

- Pin-hole camera
  - Single slit 50-1000  $\mu\text{m}$
  - Coded aperture
- 1 keV to 10 keV photons
- Measured beam of 12  $\mu\text{m}$  with 0.5  $\mu\text{m}$  error
- Complex deconvolution of PRF
- Can do single turn single bunch acquisitions
- array of 32 InGaAs photodiodes with 50  $\mu\text{m}$  pitch

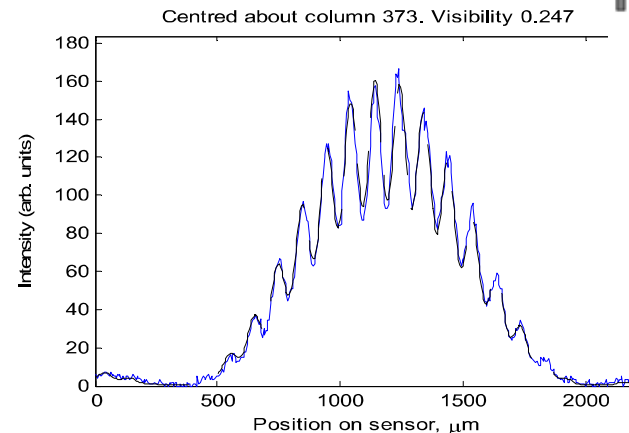
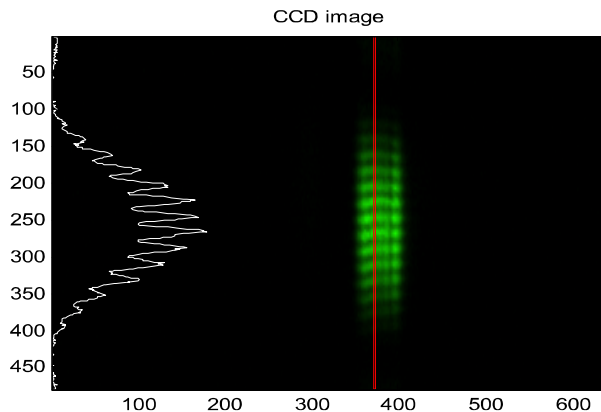
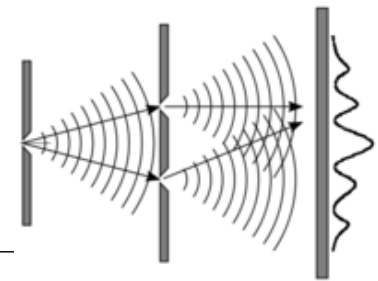


# SR interferometry

- Alternative to imaging
- Interference fringes produced by SR passing through two slits (Young's interferometer)
- Visibility of fringes depends on source (beam) size

$$I(y, D) = (I_1 + I_2) \cdot \left\{ \text{sinc} \left( \frac{\pi \cdot a \cdot y \cdot \chi(D)}{\lambda \cdot f} \right) \right\} \cdot \left\{ 1 + \gamma \cdot \cos \left( k \cdot D \cdot \left( \frac{y}{f} + \psi \right) \right) \right\}$$

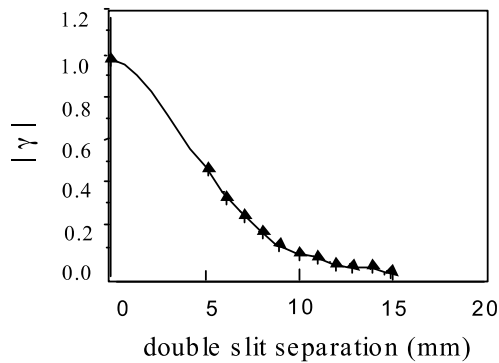
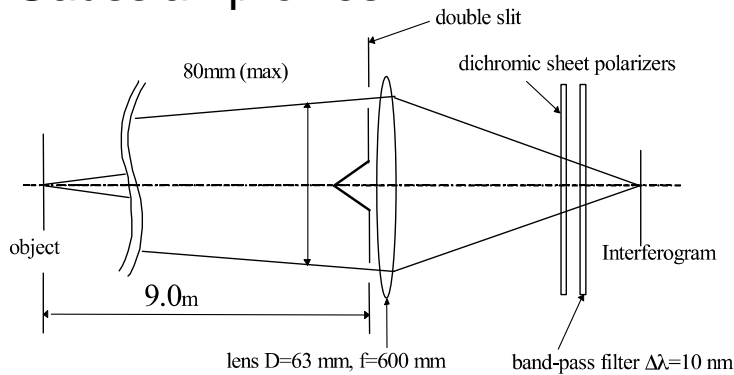
$$\gamma = \left( \frac{2\sqrt{I_1 \cdot I_2}}{I_1 + I_2} \right) \left( \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} \right), \quad \psi = \tan^{-1} \frac{S(D)}{C(D)}$$



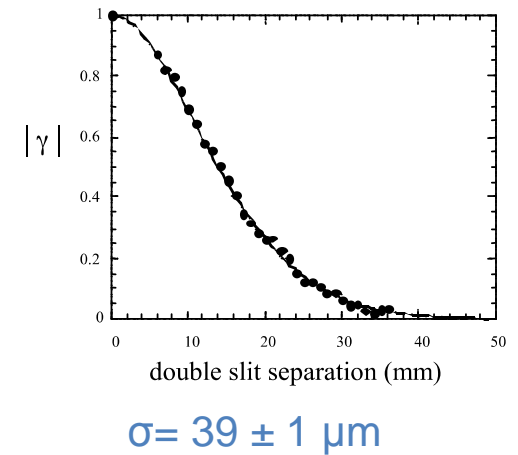
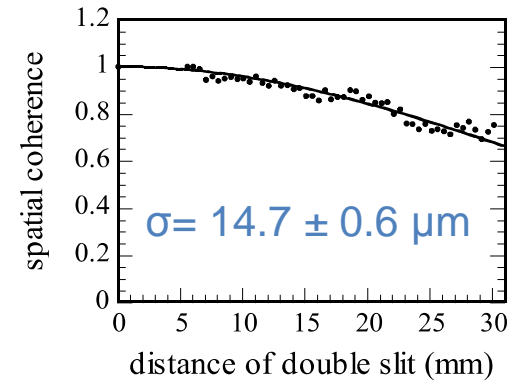
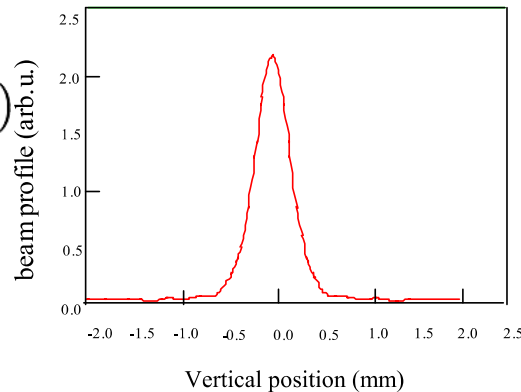
Young's Two-slit Experiment

# SR interferometer at KEK [6]

Developed by Toshi Mitsuhashi at the KEK Photon Factory. Works at 500 nm  
 Very small beams can be measured assuming Gaussian profiles

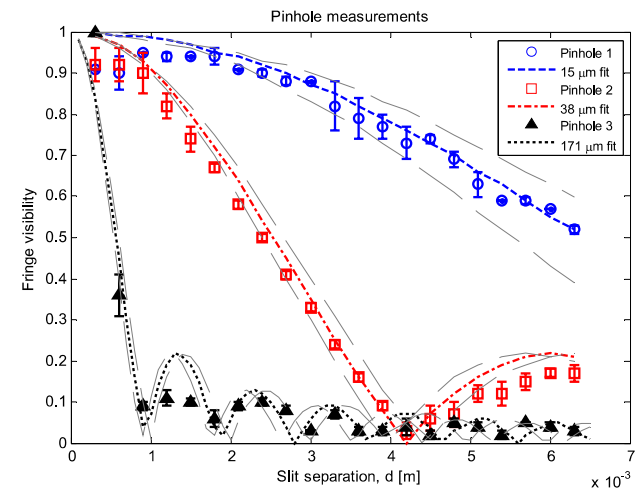
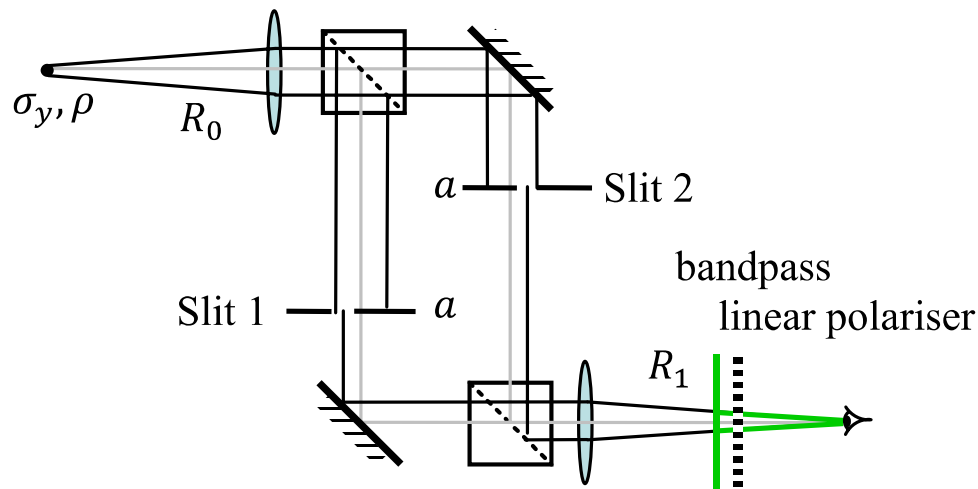


$\mathcal{F}(D)$



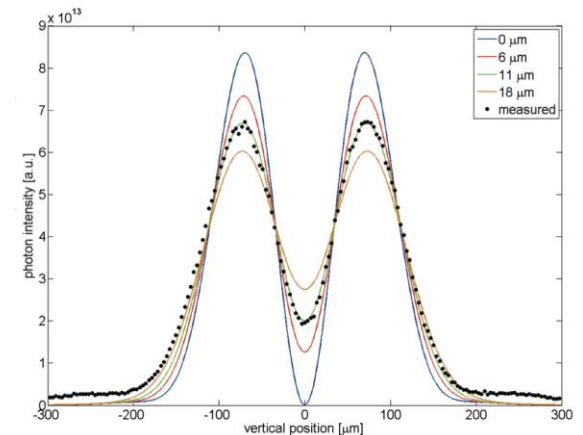
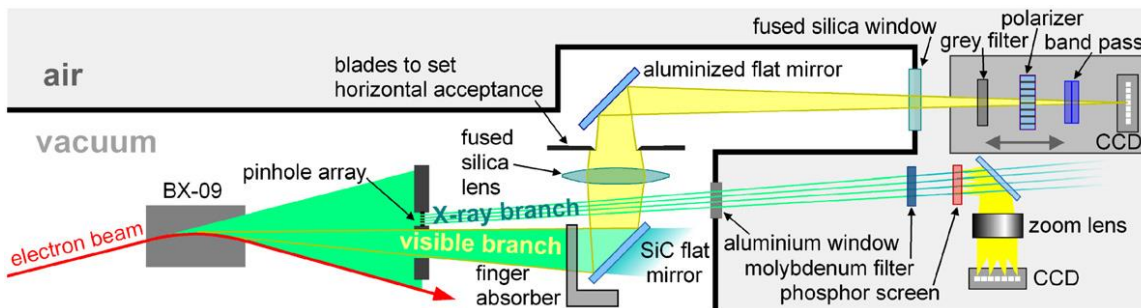
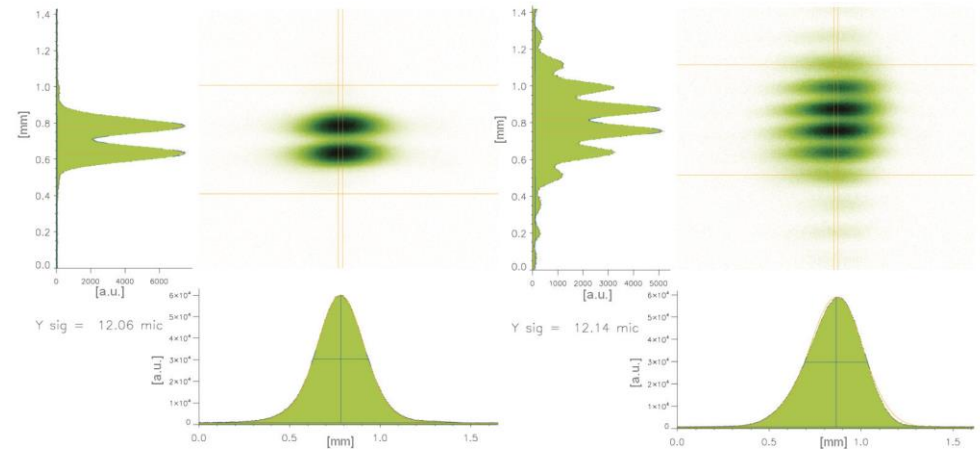
# Another slit solution [7]

- Solution implemented at the Australian synchrotron
- No mechanical limit on the distance between slits
- Designed for 532 nm
- Demonstrated pin-hole measurement  $15 \pm 2 \mu\text{m}$



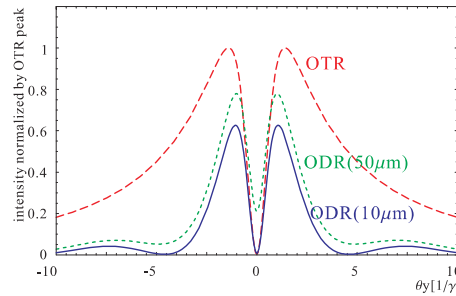
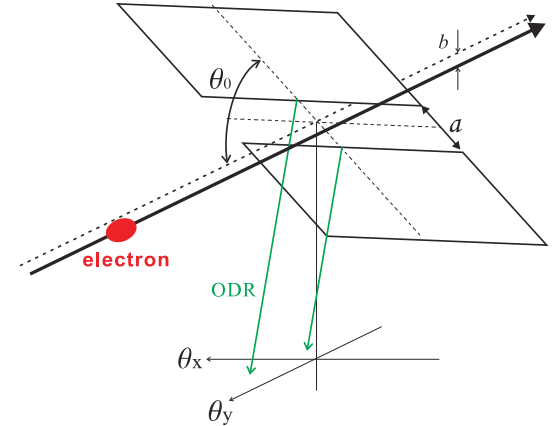
# Alternative interferometry at SLS [8]

- Uses the two lobes of the  $\pi$  polarization to create a “natural” interferometer
- Possible to insert a mask between the lobes to increase the visibility
- Measured  $3.6 \pm 0.6 \mu\text{m}$

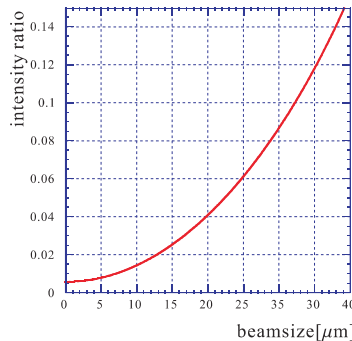
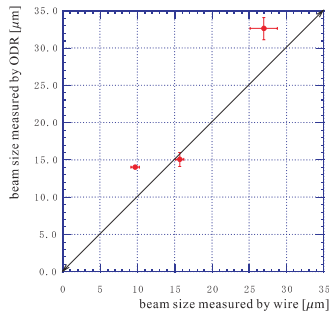
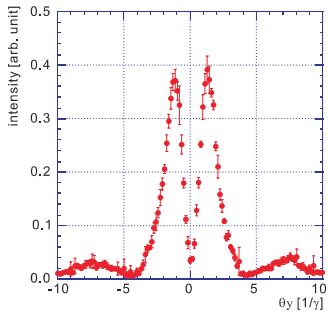


# Diffraction radiation [9]

- Based on the analysis the angular distribution of the “vertical” polarization of the optical diffraction radiation



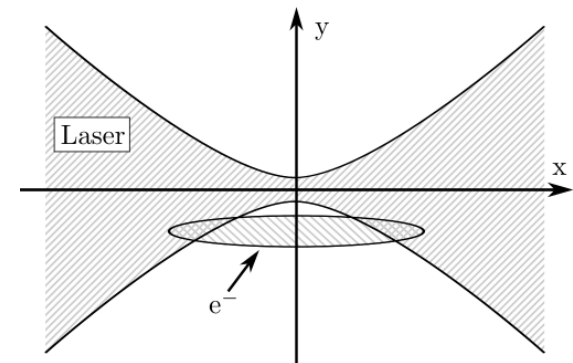
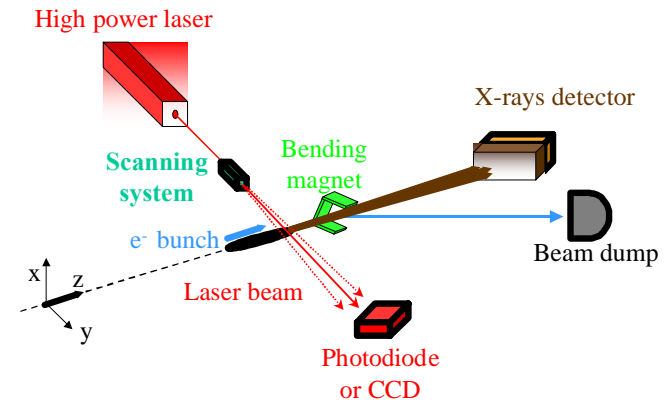
$$\frac{dW_y}{d\omega d\Omega} = \frac{\alpha\gamma^2}{2\pi^2} \frac{\exp\left(-\frac{2\pi a \sin \theta_0}{\gamma\lambda} \sqrt{1+t_x^2}\right)}{1+t_x^2+t_y^2} \times \left\{ \exp\left(\frac{8\pi^2}{\gamma^2\lambda^2} \sigma_y^2 (1+t_x^2)\right) \cosh\left(\frac{4\pi b}{\gamma\lambda} \sqrt{1+t_x^2}\right) - \cos\left(\frac{2\pi a \sin \theta_0}{\gamma\lambda} \theta_y + \psi\right) \right\} \quad (1)$$



ATF: E=1.28 GeV,  $\lambda= 550$  nm

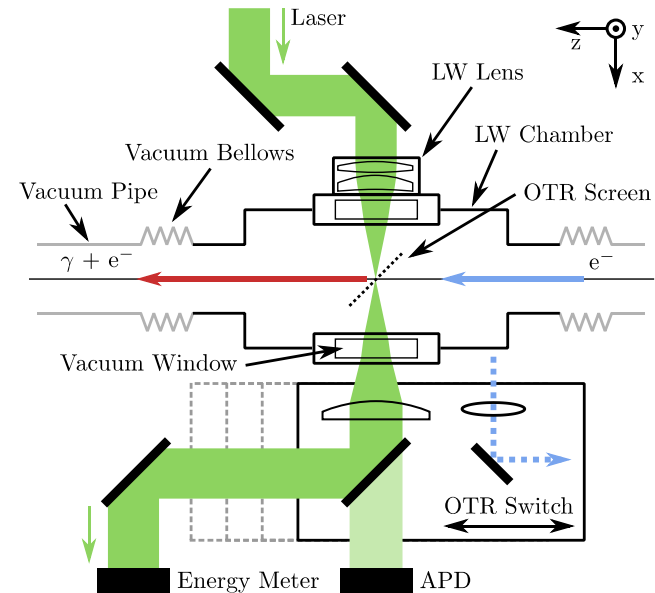
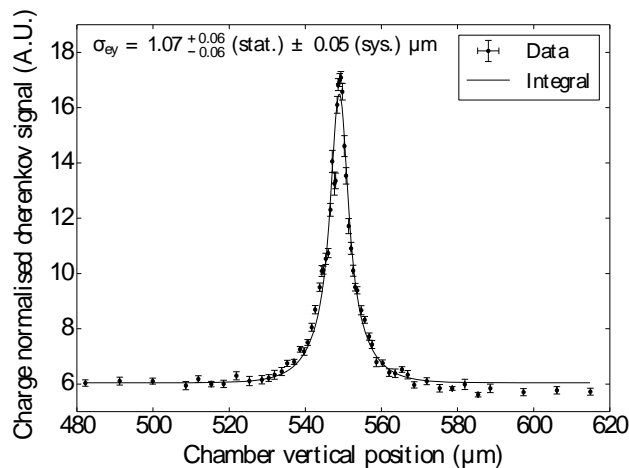
# Laser wire scanner

- Scan a collimated laser beam across the electron beam and observe the X-Rays/ $\gamma$ -Rays produced in the inverse Compton scattering process
- Difficult to measure small beams with high aspect ratio (Rayleigh range)



# LWS at ATF [10]

- 1.28 GeV beam on extraction line of ATF
- Vertical beam size around  $1\mu\text{m}$
- Horizontal size  $100\mu\text{m}$
- Laser 532 nm focused to  $1\mu\text{m}$
- Fit data with complex model





# Conclusions

- A selection of methods presented with relative examples
- Measuring small (microns) beams is possible
- Measuring small (microns) beams is difficult
- For circular machines methods based on synchrotron radiation are the most indicated

But ... if you really need to measure sub-micron beams

T. Shintake et al.,

“EXPERIMENTS OF NANOMETER SPOT SIZE MONITOR AT FFTB USING  
LASER INTERFEROMETRY”

# References

- 1 M. Sapinski et al., “Carbon Fiber Damage in Accelerator Beam”, CERN-BE-2009-028 BI
- 2 H. Hayano, “WIRE SCANNERS FOR SMALL EMITTANCE BEAM MEASUREMENT IN ATF”, 20th International Linear Accelerator Conference, Monterey, CA, USA, 21 - 25 Aug 2000, pp.e-proc. MOC01
- 3 H. Sakai et al., “MEASUREMENT OF THE BEAM PROFILES WITH THE IMPROVED FRESNEL ZONE PLATE MONITOR”, EPAC 2006, Edimburgh, Scotland, THOBF102
- 4 F. Ewald et al., “CHARACTERISATION OF AI-COMPOUND REFRACTIVE LENSES FOR X-RAYS”, IBIC 2013, Oxford, UK, WEPF12
- 5 J. P. Alexander et al., “Vertical beam size measurement in the CESR-TA  $e^+e^-$  storage ring using x-rays from synchrotron radiation”, <http://arxiv.org/abs/1311.6769>
- 6 T. Mitsuhashi, “MEASUREMENT OF SMALL TRANSVERSE BEAM SIZE USING INTERFEROMETRY”, DIPAC 2001, Grenoble, France, IT06
- 7 K.P. Wootton et al., “A NOVEL SYNCHROTRON RADIATION INTERFEROMETER FOR THE AUSTRALIAN SYNCHROTRON”, IPAC’10, Kyoto, Japan, MOPD079
- 8 A. Saa Hernandez et al., “THE NEW SLS BEAM SIZE MONITOR, FIRST RESULTS”, IPAC2013, Shanghai, China, MOPWA041
- 9 T. Muto et al., “DEVELOPMENT OF THE NON-INVASIVE BEAM SIZE MONITOR USING ODR”, EPAC 2004, Lucerne, Switzerland, THOALH02
- 10 L. J. Nevay et al., “Laserwire at the Accelerator Test Facility 2 with Sub-Micrometre Resolution”, <http://arxiv.org/abs/1404.0294>